

# Multiple parton scattering effects in proton-proton collisions at the LHC

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Antoni Szczurek 60th Birthday

7th September 2017, Polish Academy of Arts and Sciences, Kraków, Poland



# Multi-particle final states at the LHC

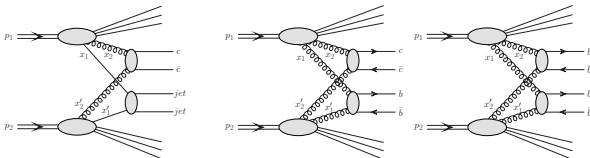
The high luminosity already achieved at the LHC potentially allows to study more complicated final states and opens new possibilities in testing dynamics of pQCD processes

**Our interest:** phenomena of Multiple-Parton Interactions (MPI)

**During last years:** Double-Parton Scattering (DPS) effects in  $pp$ -collisions

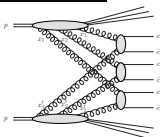
- $pp \rightarrow c\bar{c}c\bar{c} X$  (supported by the LHCb double charm data)
- $pp \rightarrow 4\text{jets} X$  (needs dedicated experimental analyses)

**Very recently:**  $pp \rightarrow c\bar{c} + 2\text{jets} X$ ,  $pp \rightarrow c\bar{c}b\bar{b} X$ ,  $pp \rightarrow b\bar{b}b\bar{b} X$

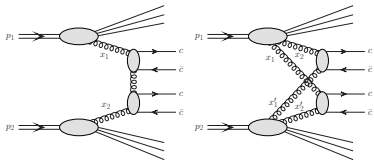


Can we observe some evidence of DPS effects in these cases?

**A step beyond the DPS:** Triple-parton scattering (TPS) in  $pp \rightarrow c\bar{c}c\bar{c}c\bar{c} X$



Can we observe some evidence of TPS effects at the LHC in the case of triple charm production?

SPS vs. DPS: Inclusive  $c\bar{c}c\bar{c}$ LHCb at  $\sqrt{s} = 7$  TeV

## CHARM MESON-MESON pair production:

DD pairs – both mesons containing c-quarks

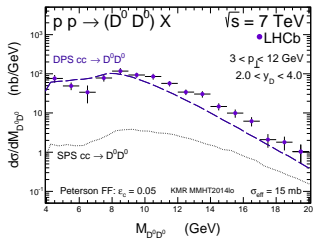
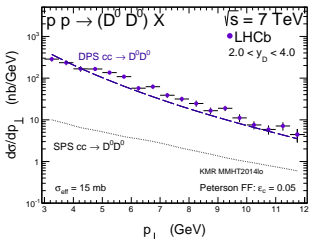
- impossible to be produced within standard SPS single  $c\bar{c}$  mechanism
- SPS double charm very small

First measurement by LHCb: J. High Energy Phys. 06, 141 (2012)

Cross section much larger than the SPS predictions

⇒ clear evidence for DPS?

Mode	$\sigma$ [nb]
$D^0D^0$	$690 \pm 40 \pm 70$
$D^0\bar{D}^0$	$6230 \pm 120 \pm 630$



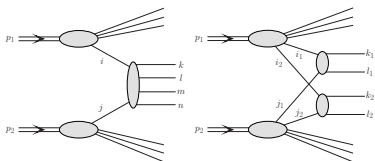
Łuszczak, Maciuta, Szczurek, Phys.Rev. D85 (2012) 094034

Maciuta, Szczurek, Phys.Rev. D87 (2013) no.7, 074039

Hameren, Maciuta, Szczurek, Phys.Rev. D89 (2014) no.9, 094019



## SPS vs. DPS: Inclusive 4jets

 $\sqrt{s} = 13 \text{ TeV}$ Optimal conditions for exploring DPS effects:

- keep jet- $p_T$ 's as low as possible:

symmetric: all 4 jets with  $p_T > 20 \text{ GeV}$

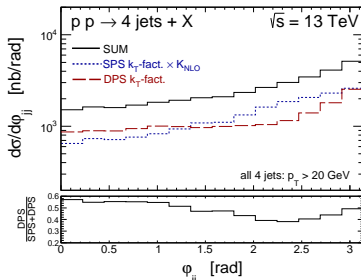
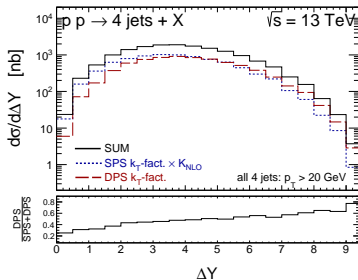
asymmetric: 1<sup>st</sup> jet:  $p_T > 35 \text{ GeV}$

2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup> jet:  $p_T > 20 \text{ GeV}$

- concentrate on jets most remote in rapidity

Maciula, Szczurek, Phys.Lett. B749 (2015) 57-62

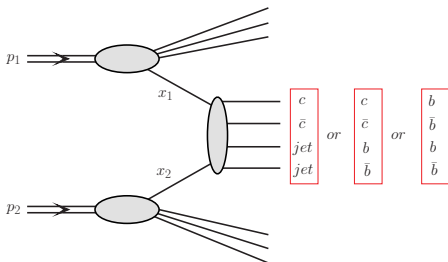
Kutak, Maciula, Serino, Szczurek, Hameren, Phys.Rev. D94 (2016) no.1, 014019



- large rapidity distances between the most remote jets
- small azimuthal angles between the two jets most remote in rapidity



# Single-Parton Scattering (SPS) mechanism



Calculations are done in two different ways:

- LO collinear parton-model approach
- **NEW:**  $k_T$ -factorization approach with fully gauge-invariant tree-level  $2 \rightarrow 4$  off-shell matrix elements
  - **first time:** off-shell initial state partons
  - exact kinematics from the very beginning and additional hard dynamics coming from transverse momenta of incident partons
  - part of higher-order (real) corrections included (depending on the model of unintegrated, transverse momentum dependent PDFs)

## $2 \rightarrow 4$ pQCD subprocesses:

9 channels for  $c\bar{c} + 2jets$

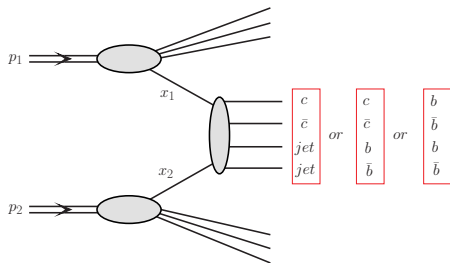
$$\begin{array}{ll}
 gg \rightarrow gg c \bar{c} & q \bar{q} \rightarrow q' \bar{q}' c \bar{c} \\
 gg \rightarrow q \bar{q} c \bar{c} & q \bar{q} \rightarrow g g c \bar{c} \\
 gq \rightarrow g q c \bar{c} & qq \rightarrow qq c \bar{c} \\
 qg \rightarrow q g c \bar{c} & q q' \rightarrow q q' c \bar{c} \\
 q \bar{q} \rightarrow q \bar{q} c \bar{c} &
 \end{array}$$

2 channels for  $c\bar{c}b\bar{b}$  and  $b\bar{b}b\bar{b}$

$$\begin{array}{ll}
 gg \rightarrow c \bar{c} b \bar{b} & q \bar{q} \rightarrow c \bar{c} b \bar{b} \\
 gg \rightarrow b \bar{b} b \bar{b} & q \bar{q} \rightarrow b \bar{b} b \bar{b}
 \end{array}$$



# Single-Parton Scattering (SPS) mechanism



## $2 \rightarrow 4$ pQCD subprocesses:

9 channels for  $c\bar{c} + 2\text{jets}$

$$\begin{array}{ll}
 gg \rightarrow gg c \bar{c} & q \bar{q} \rightarrow q' \bar{q}' c \bar{c} \\
 gg \rightarrow q \bar{q} c \bar{c} & q \bar{q} \rightarrow g g c \bar{c} \\
 gq \rightarrow g q c \bar{c} & qq \rightarrow qq c \bar{c} \\
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 \end{array}$$

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 gg \rightarrow c \bar{c} b \bar{b} & q \bar{q} \rightarrow c \bar{c} b \bar{b} \\
 gg \rightarrow b \bar{b} b \bar{b} & q \bar{q} \rightarrow b \bar{b} b \bar{b}
 \end{array}$$

**KaTie** (A. van Hameren): <https://bitbucket.org/hameren/KaTie> arXiv:1611.00680

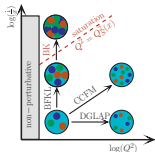
basics of the theory behind: Kutak, Kotko, Hameren, J. High Energy Phys. 01 (2013) 078;

Kutak, Salwa, Hameren, Phys.Lett. B727 (2013) 226-233

- complete Monte Carlo program for tree-level calculations of any process within the Standard Model
- any initial-state partons on-shell or off-shell
- scattering amplitudes are calculated numerically via Dyson-Schwinger recursion generalized also to tree-level off-shell amplitudes
- double-parton scattering available too!



# Unintegrated parton distribution functions (uPDFs)

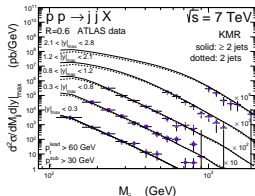
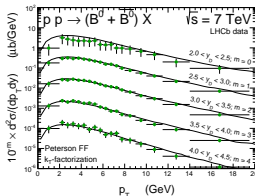
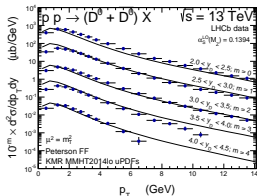


Most popular models:

- Kwieciński, Jung (CCFM, wide range of  $x$ )
- Kimber-Martin-Ryskin (DGLAP-BFKL, wide range of  $x$ )
- Kwieciński-Martin-Staśto (BFKL-DGLAP, small  $x$ -values)
- Kutak-Staśto (BK, saturation, only small  $x$ -values)

We use: **Kimber-Martin-Ryskin (KMR) approach:**

- calculated from collinear PDFs (most up-to-date PDF sets can be used)
- unintegrated quarks available (important for reliable predictions for jets)
- unique feature: possible additional hard emission from the uPDF (part of higher order corrections)

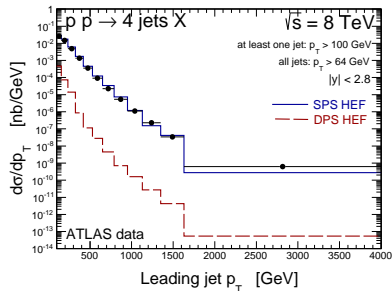
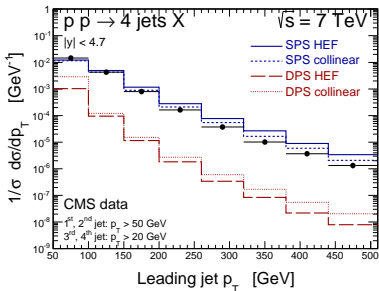


- works well for inclusive charm, bottom and inclusive dijet at the LHC

- **good starting point for DPS predictions for  $c\bar{c} + 2\text{jets}$ ,  $c\bar{c}b\bar{b}$  and  $b\bar{b}b\bar{b}$**



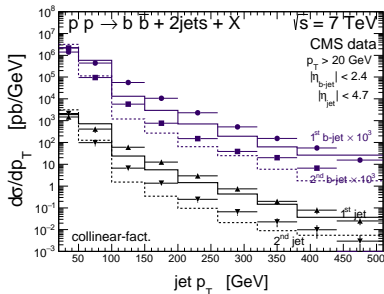
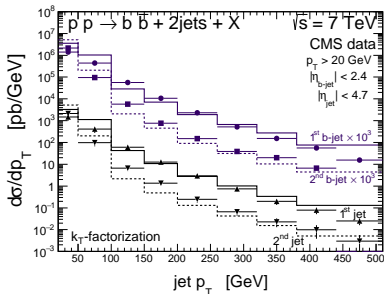
## Inclusive 4jets

CMS, ATLAS at  $\sqrt{s} = 7, 8 \text{ TeV}$ Testing SPS 2  $\rightarrow$  4 calculations: KaTie + KMR uPDFs in multi-jet production

- CMS and ATLAS data described by the SPS mechanism
- DPS mechanism strongly suppressed by too hard jet- $p_T$  cuts
- KaTie + KMR uPDFs gives reasonable description of the data sets



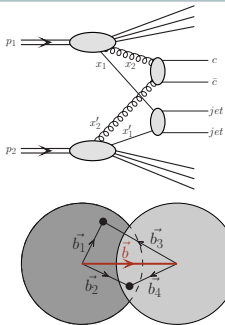


Inclusive  $2b + 2j$ CMS at  $\sqrt{s} = 7$  TeVTesting SPS 2  $\rightarrow$  4 calculations: KaTie + KMR uPDFs in multi-jet production

- CMS data described with the SPS mechanism
- DPS effects in hard- $p_T$   $b$ -flavour production are expected to be negligible
- KaTie + KMR uPDFs gives reasonable description of the data sets ( $p_T$ -slope better described than in the collinear case)



# Double-parton scattering (DPS) mechanism



**DPS in general form** for  $pp \rightarrow c \bar{c} k l X$ :

$$d\sigma^{DPS} = \frac{1}{2} \cdot \sum_{i,j,k,l} \Gamma_{i\bar{j}}(b, x_1, x_2; \mu_1^2, \mu_2^2) \Gamma_{j\bar{k}}(b, x'_1, x'_2; \mu_1^2, \mu_2^2) \\ \times d\sigma_{ij \rightarrow kl}(x'_1, x_1, \mu_1^2) \cdot d\sigma_{g\bar{g} \rightarrow c\bar{c}}(x_2, x'_2, \mu_2^2) dx_1 dx_2 dx'_1 dx'_2 d^2b$$

**DPDF** - emission of one parton with assumption that second parton is also emitted

$$\Gamma_{i,j}(b, x_1, x_2; \mu_1^2, \mu_2^2) = F_i(x_1, \mu_1^2) F_j(x_2, \mu_2^2) F(b; x_1, x_2, \mu_1^2, \mu_2^2)$$

- longitudinal and transverse correlations between two partons
- spin, flavor and color correlations
- well established theory: e.g. Diehl, Ostermeier, Schafer, JHEP 03, 089 (2012)  
but not yet available for phenomenological studies

## Factorized ansatz (pocket-formula)

In a simple probabilistic picture process initiated by:

two simultaneous hard parton-parton scatterings in one proton-proton interaction

$$\sigma^{DPS} = \frac{1}{\sigma_{eff}} \cdot \sum_{i,j,k,l} \sigma^{SPS}(ij \rightarrow kl) \cdot \sigma^{SPS}(gg \rightarrow c\bar{c})$$

two subprocesses are not correlated and do not interfere

- $\sigma_{eff} \Rightarrow$  model parameter  $\Rightarrow$  normalization of  $\sigma^{DPS}$



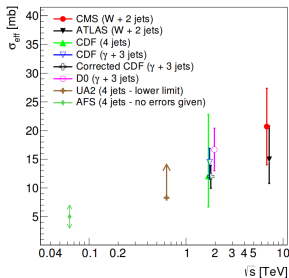
# Double-parton scattering (DPS) mechanism

## Factorized ansatz (pocket-formula)

- a good approximation for **small-x partons**
- **color/flavor correlations suppressed** in evolution (Kasemets et al., Phys. Rev. D91, 014015 (2015))
- **spin (polarization) correlations very small** (Echevarria et al. JHEP 04, 034 (2015))

## Separation of longitudinal and transverse degrees of freedom

- **DPDFs in multiplicative form:**  $\Gamma_{ij}(b; x_1, x_2, \mu_1^2, \mu_2^2) = F_i(x_1, \mu_1^2)F_j(x_2, \mu_2^2)F(b)$
- only transverse correlations taken into account
- $\sigma_{eff} = \left[ \int d^2b (F(b))^2 \right]^{-1}$ ,  $F(b)$  - overlap of the matter distribution in transverse plane where  $b$  is a distance between both partons
- nonperturbative quantity with dimension of cross section, connected to transverse size of proton



- extracted from several experimental analyses
- in principle may not be universal
- detailed studies: Seymour, Siódmok, JHEP 10, 113 (2013)
- LHCb double charm data:  $\sigma_{eff} = 21_{-6}^{+7}$  mb
- ATLAS 4jets data:  $\sigma_{eff} = 14.9$  mb
- **world average:**  $\sigma_{eff} \approx 15$  mb (large uncertainties)



Inclusive  $D^0 + 2\text{jets}$ 

$$\sqrt{s} = 13 \text{ TeV}$$

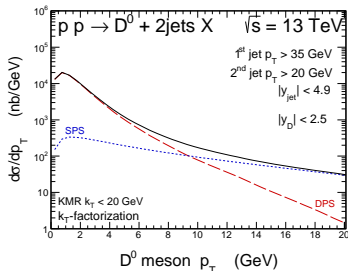
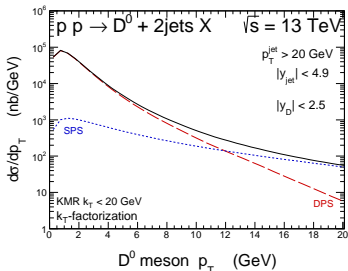
The calculated "visible" cross sections in microbarns for the ATLAS detector acceptance:

$D^0$  meson (or  $\bar{D}^0$  antimeson):  $|y| < 2.5$ ,  $p_T > 3.5 \text{ GeV}$

both jets:  $|y| < 4.9$ ,  $R_{\text{cone}} = 0.5$

experimental jet- $p_T$ mode	SPS	DPS	$\frac{DPS}{SPS+DPS}$
both jets $p_T > 20 \text{ GeV}$	3.74	18.49	83 %
$p_T^{\text{lead}} > 35 \text{ GeV}$ , $p_T^{\text{sub}} > 20 \text{ GeV}$	1.76	4.52	72 %
$p_T^{\text{lead}} > 50 \text{ GeV}$ , $p_T^{\text{sub}} > 35 \text{ GeV}$	0.43	1.25	74 %

- large cross sections ( $\mu\text{b}$ )
- DPS dominated samples



Evident enhancement in the region of  $p_T \lesssim 10 \text{ GeV}$   
 because of the presence of the DPS mechanism



Inclusive  $D^0 + 2\text{jets}$ 

$$\sqrt{s} = 13 \text{ TeV}$$

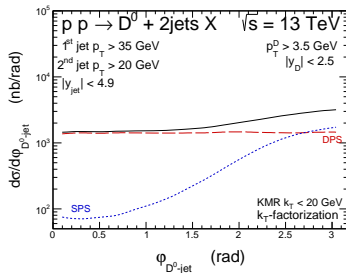
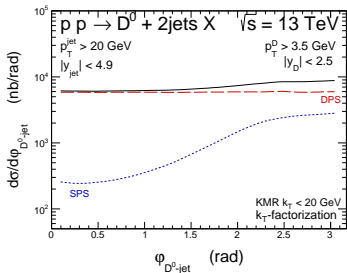
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Almost decorrelated distribution in  $\varphi_{D^0\text{-jet}}$  azimuthal angle  
 because of the presence of the DPS mechanism



# Inclusive $D^0\bar{D}^0 + 2\text{jets}$

 $\sqrt{s} = 13 \text{ TeV}$ 

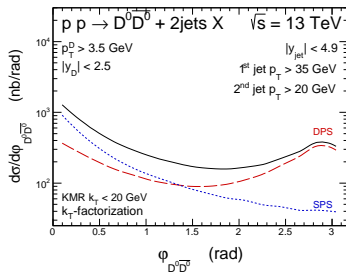
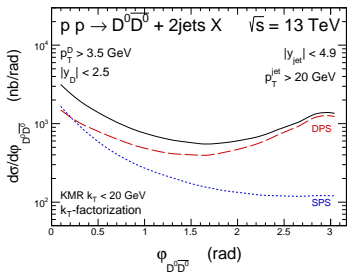
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both,  $D^0$  meson and  $\bar{D}^0$  antimeson:  $|y| < 2.5$ ,  $p_T > 3.5 \text{ GeV}$

both jets:  $|y| < 4.9$ ,  $R_{\text{cone}} = 0.5$

experimental jet- $p_T$ mode	SPS	DPS	$\frac{DPS}{SPS+DPS}$
both jets $p_T > 20 \text{ GeV}$	1.10	2.35	68 %
$p_T^{\text{lead}} > 35 \text{ GeV}$ , $p_T^{\text{sub}} > 20 \text{ GeV}$	0.55	0.58	51 %
$p_T^{\text{lead}} > 50 \text{ GeV}$ , $p_T^{\text{sub}} > 35 \text{ GeV}$	0.15	0.14	52 %

- smaller than in the single- $D$  case but still large
- the relative DPS contribution slightly reduced



Evident enhancement in the region of  $\varphi_{D^0\bar{D}^0} \gtrsim \frac{\pi}{2}$   
because of the presence of the DPS mechanism



Inclusive  $D^0 B^+$ 

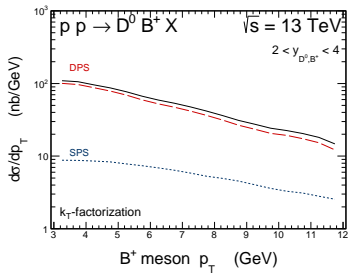
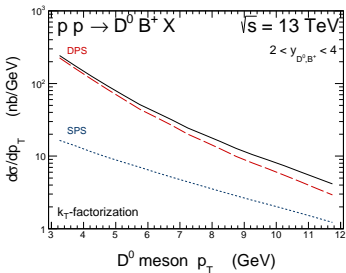
$$\sqrt{s} = 7, 13 \text{ TeV}$$

The calculated "visible" cross sections in nanobarns for the LHCb detector acceptance:

$D^0$  and  $B^+$  meson (or  $\bar{D}^0$  and  $B^-$  antimeson):  $2 < y < 4$ ,  $3 < p_T < 12 \text{ GeV}$

Final state	Mechanism	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 13 \text{ TeV}$
$D^0 B^+ + \bar{D}^0 B^-$	DPS	115.50	418.79
	SPS	21.13	51.46

- large cross sections (nb)
- DPS dominated samples



Evident enhancement in the whole region of considered  $p_T$ 's  
because of the presence of the DPS mechanism



Inclusive  $D^0 B^+$  $\sqrt{s} = 7, 13 \text{ TeV}$ 

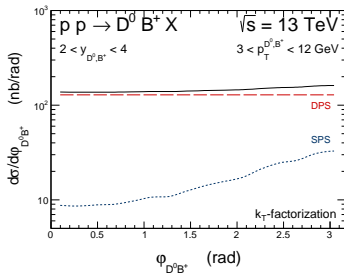
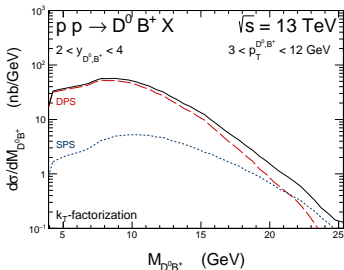
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	SPS	21.13	51.46

- large cross sections (nb)

- DPS dominated samples



- Evident enhancement in the region of  $M_{D^0 B^+} < 15 \text{ GeV}$
- Almost decorrelated distribution in  $\varphi_{D^0 B^+}$  azimuthal angle





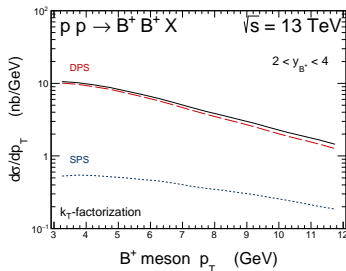
Inclusive  $B^+ B^+$  $\sqrt{s} = 7, 13 \text{ TeV}$ 

The calculated "visible" cross sections in nanobarns for the LHCb detector acceptance:

both  $B^+$  mesons (or both  $B^-$  antimesons):  $2 < y < 4, \quad 3 < p_T < 12 \text{ GeV}$

Final state	Mechanism	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 13 \text{ TeV}$
$B^+ B^+ + B^- B^-$	DPS	11.04	43.40
	SPS	1.31	3.39

- large cross sections (nb)
- DPS dominated samples



Evident enhancement in the whole region of considered  $p_T$ 's because of the presence of the DPS mechanism



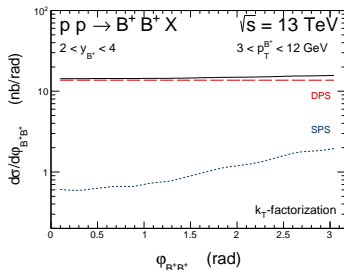
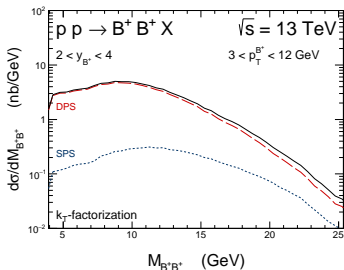
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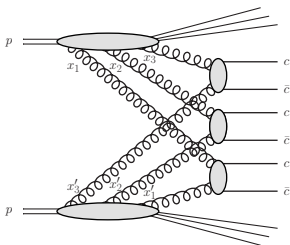
- large cross sections (nb)
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- Evident enhancement in the region of  $M_{B^+ B^+} < 20 \text{ GeV}$
- Almost decorrelated distribution in  $\varphi_{B^+ B^+}$  azimuthal angle



# Triple charm in triple-parton scattering (TPS)



## First theoretical analysis for charm quarks:

d'Enterria, Snigirev, *Phys.Rev.Lett.* 118, no. 12, 122001 (2017)

- a generic expressions to compute TPS cross sections
- total charm quark cross sections in NNLO collinear approach

## Our calculations:

Maciuta, Szczurek, *Phys.Lett.* B772 (2017) 849-853

- analysis for triple  $D$  meson production
- $k_T$ -factorization approach
- differential distributions

## Factorized ansatz for TPS (pocket-formula)

In a simple probabilistic picture process initiated by:

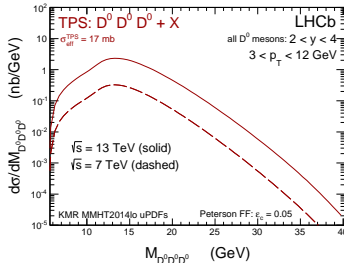
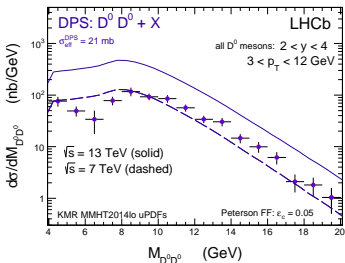
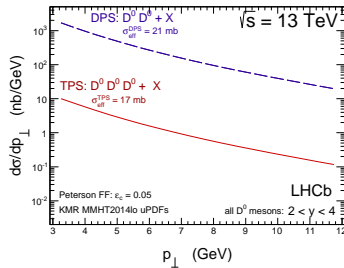
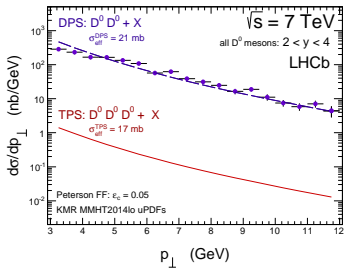
three simultaneous hard parton-parton scatterings in one proton-proton interaction

$$\sigma_{pp \rightarrow c\bar{c}c\bar{c}c\bar{c}}^{\text{TPS}} = \left( \frac{1}{3!} \right) \frac{\sigma_{pp \rightarrow c\bar{c}}^{\text{SPS}} \cdot \sigma_{pp \rightarrow c\bar{c}}^{\text{SPS}} \cdot \sigma_{pp \rightarrow c\bar{c}}^{\text{SPS}}}{\sigma_{\text{eff,TPS}}^2}$$

three subprocesses are not correlated and do not interfere

- $\sigma_{\text{eff,TPS}} = k \times \sigma_{\text{eff,DPS}}$ , with  $k = 0.82 \pm 0.11$
- $\sigma_{\text{eff,DPS}} = 21 \text{ mb}$  (extracted from LHCb data)  $\Rightarrow \sigma_{\text{eff,TPS}} = 17 \text{ mb}$



Inclusive  $D^0 D^0 D^0$  $\sqrt{s} = 7, 13 \text{ TeV}$ 

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$$\sqrt{s} = 7, 13 \text{ TeV}$$

**The integrated cross sections** for double and triple  $D^0$  meson production (in nb) within the LHCb acceptance:  $2 < y_{D^0} < 4$  and  $3 < p_T^{D^0} < 12 \text{ GeV}$  calculated in the  $k_T$ -factorization approach.

Final state	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 13 \text{ TeV}$
DPS: $\sigma(D^0 D^0 + X)$	784.74	2992.91
TPS: $\sigma(D^0 D^0 D^0 + X)$	2.38	17.71

**Number of events** for different values of the feasible integrated luminosity in the LHCb experiment for the calculated cross sections

$\sqrt{s}$	Integrated Luminosity	DPS ( $D^0 D^0$ )	TPS ( $D^0 D^0 D^0$ )
7 TeV	355 $\text{pb}^{-1}$	$0.43 \times 10^6$	51
	1106 $\text{pb}^{-1}$	$1.34 \times 10^6$	159
13 TeV	1665 $\text{pb}^{-1}$	$7.70 \times 10^6$	1789
	5000 $\text{pb}^{-1}$	$23.11 \times 10^6$	5374

- a few thousands of events of triple  $D^0$  production at  $\sqrt{s} = 13 \text{ TeV}$



# Conclusions

We have studied if and how the DPS effects can be observed at the LHC for different reactions in the sector of open heavy mesons:

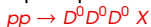


- cross sections of the order of microbarns at  $\sqrt{s} = 13$  TeV within the ATLAS detector acceptance
- regions of phase space where the DPS component clearly dominates over SPS one are identified



- cross sections of the order of hundreds ( $D^0 B^+$ ) and tens ( $B^+ B^+$ ) nanobarns at  $\sqrt{s} = 13$  TeV within the LHCb detector acceptance
- DPS components dominate in the LHCb fiducial volume of the phase space.

We have presented first estimation of the triple-parton scattering production of triple open charm meson:



- a few thousands of events of triple  $D^0$  production can be observed at  $\sqrt{s} = 13$  TeV within the LHCb detector acceptance

Thank You for attention!

