

# Precise determinations of the strong coupling in lepton collisions



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based on

arXiv:1603.08927, 1606.03453, 1708.04093, 1804.09146, 1807.11472,  
1902.08158

and unpublished results of ongoing work

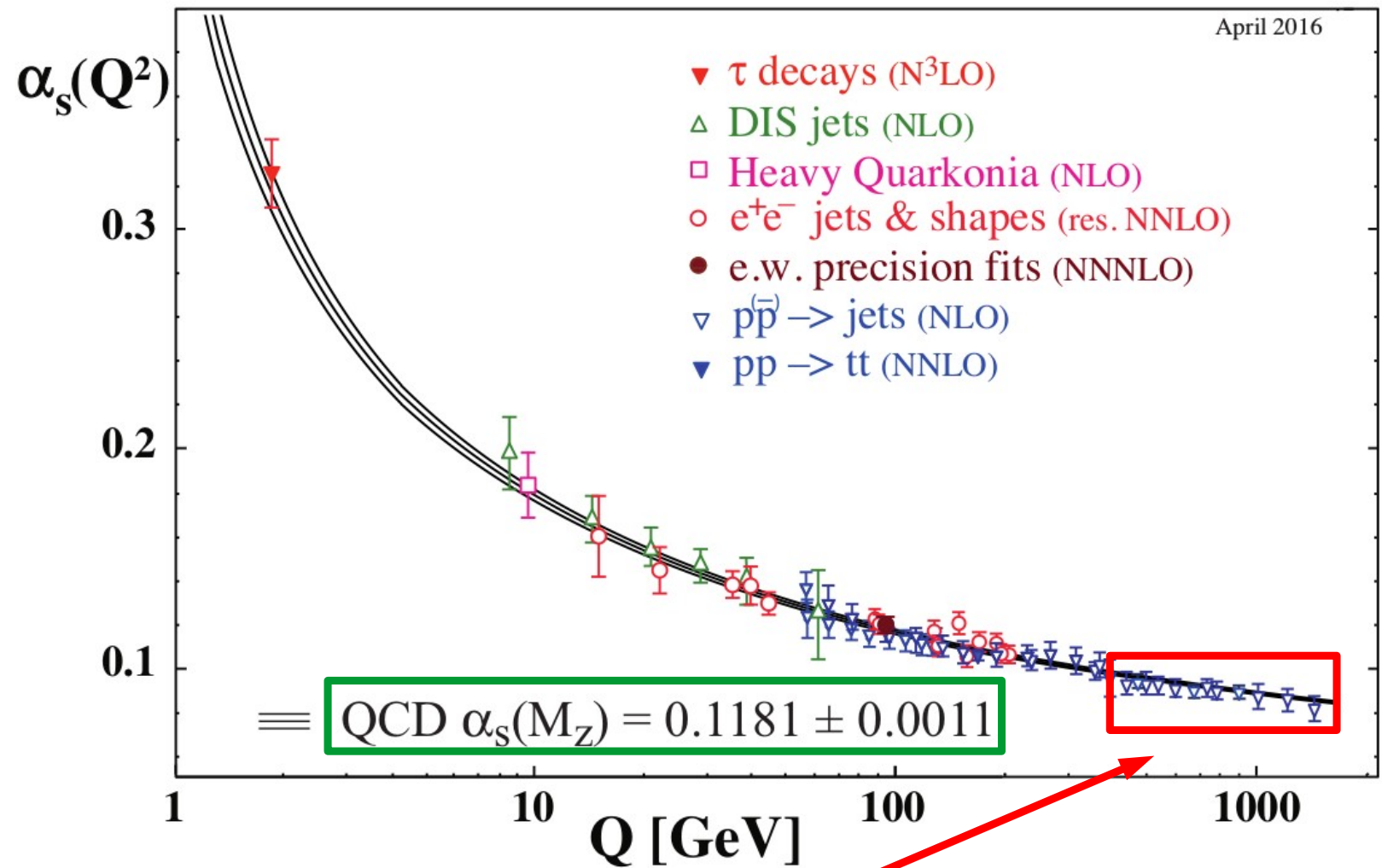
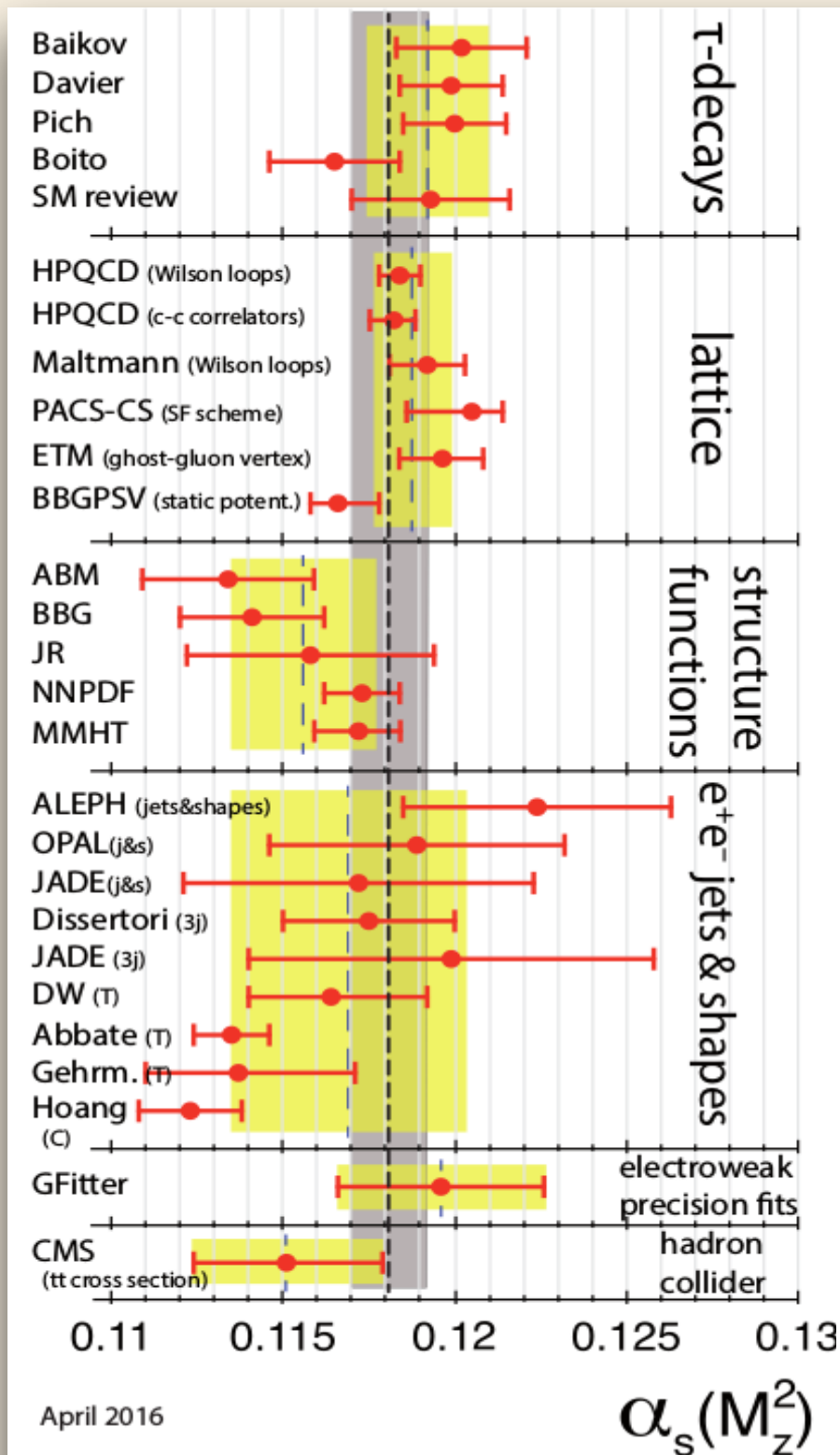
FFK-2019, Tihany  
12 June 2019

# Outline

- Status of the strong coupling
- New measurements of  $\alpha_s$
- Conclusions and Outlook

Status of the strong coupling

# PDG 2016 on $\alpha_s$



not included in average:  
 LHC data, but only NLO theory

dominated by lattice

$$\frac{\Delta\alpha_s(M_Z)}{\alpha_s(M_Z)} = 0.9\%$$

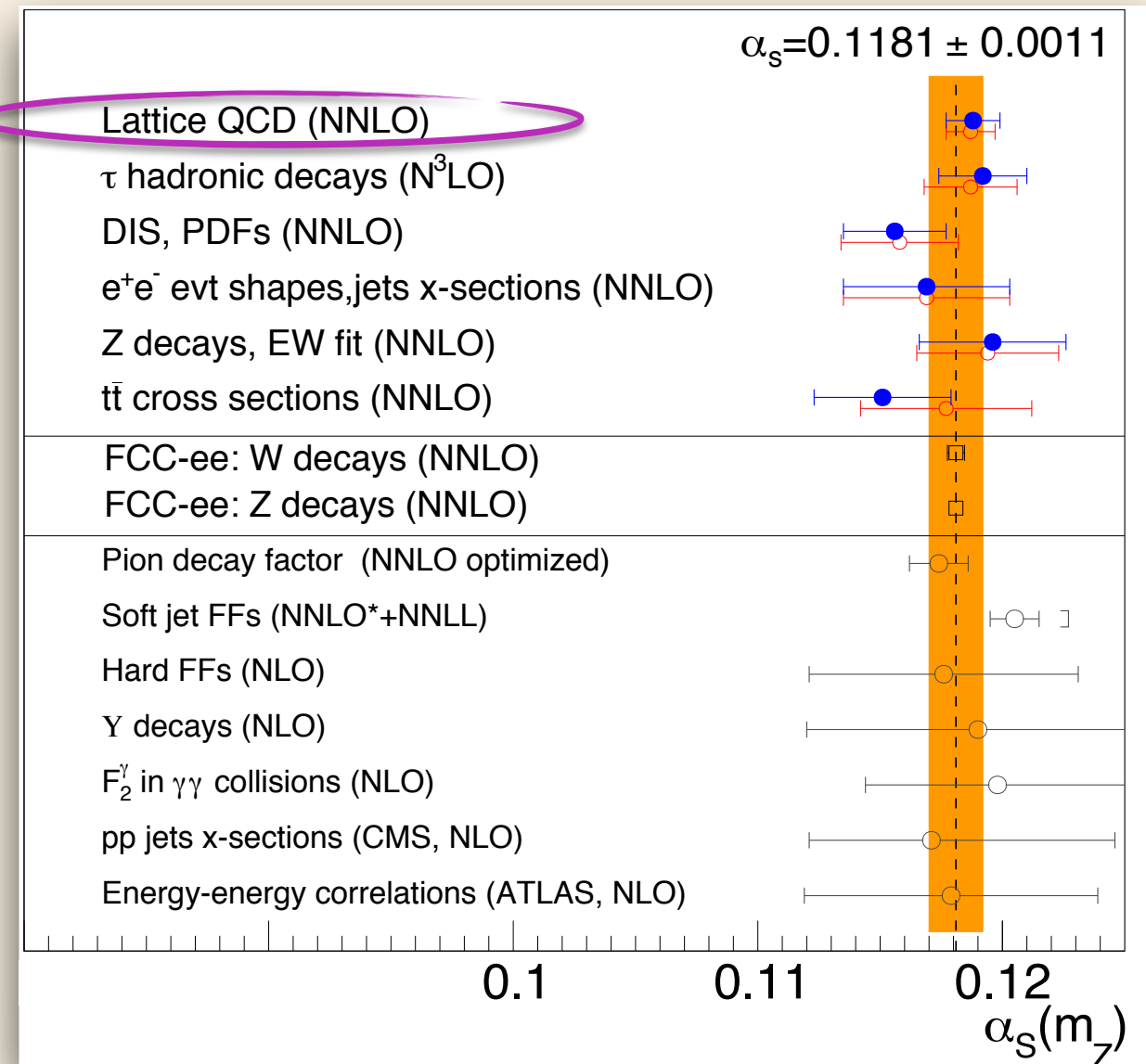
PDG 1992: 2.4%

PDG, Chin. Phys. C40 (2016) 100001



# Lattice unbeatable?

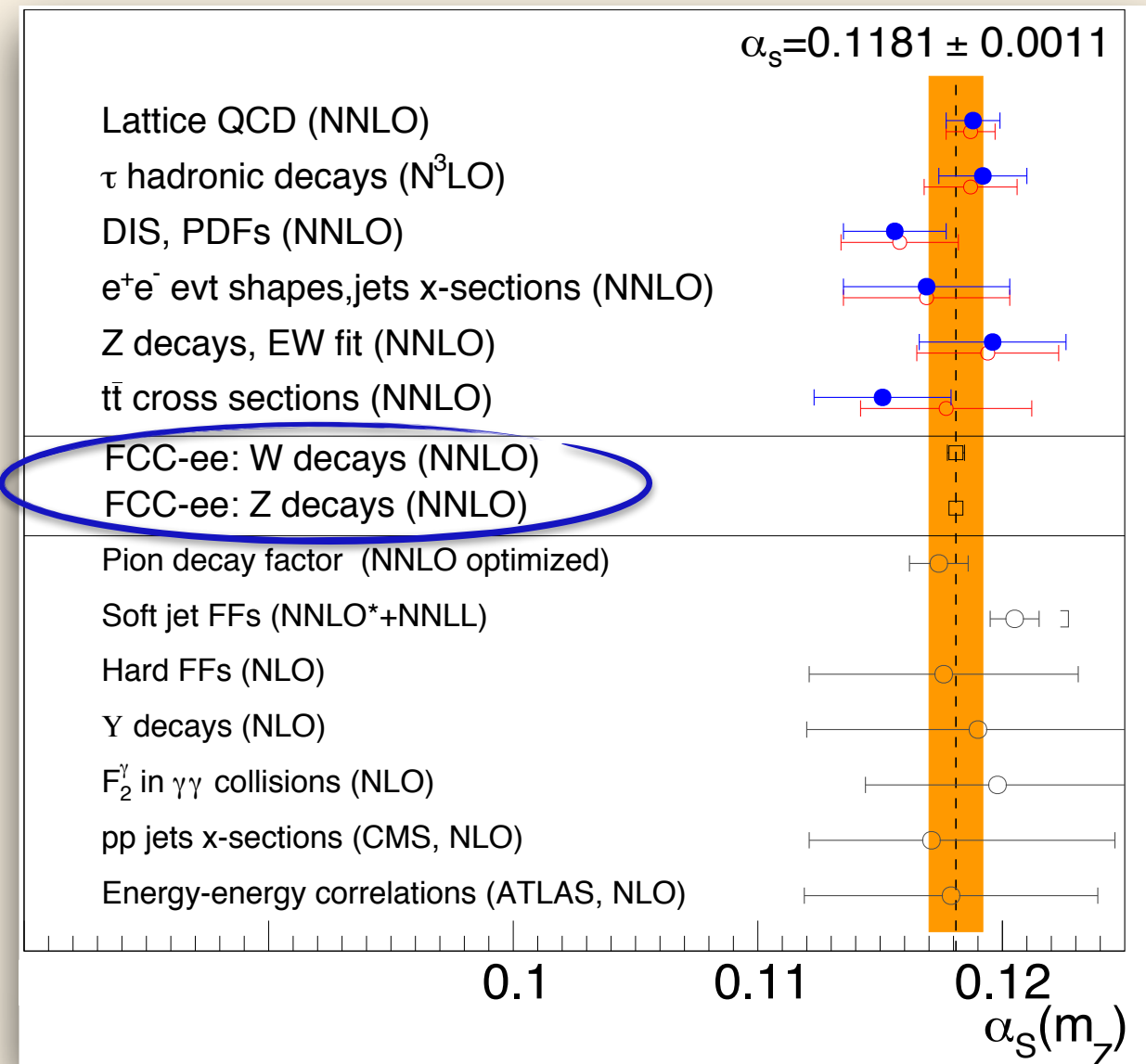
recent prevailing view:  
lattice is unbeatable



D. d'Enterria, arXiv: 1806.06156

# Lattice unbeatable?

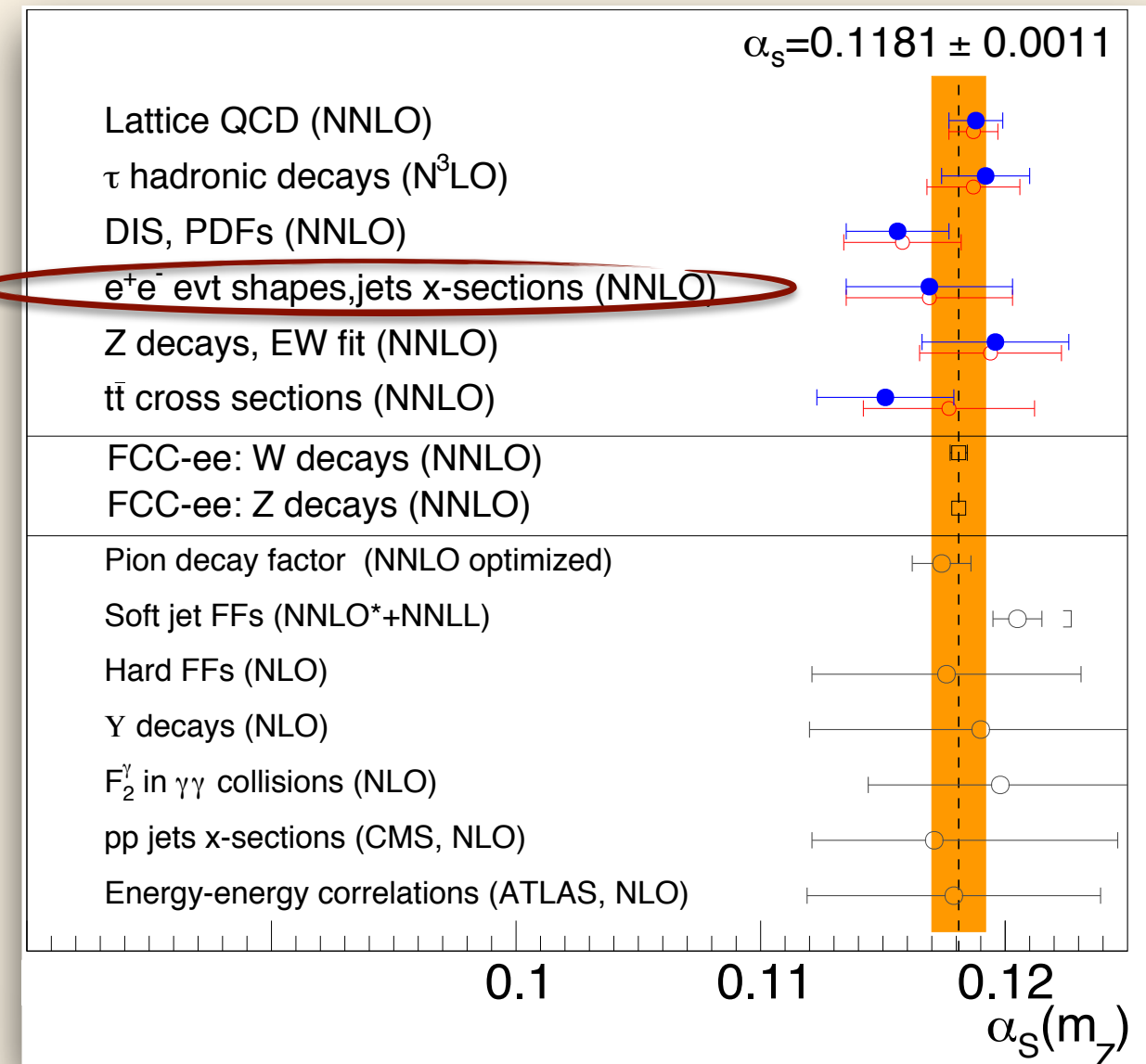
- recent prevailing view:  
lattice is unbeatable
- yet determination of  $\alpha_s$  from experiments remains desirable  
(or at least a fancy)



D. d'Enterria, arXiv: 1806.06156

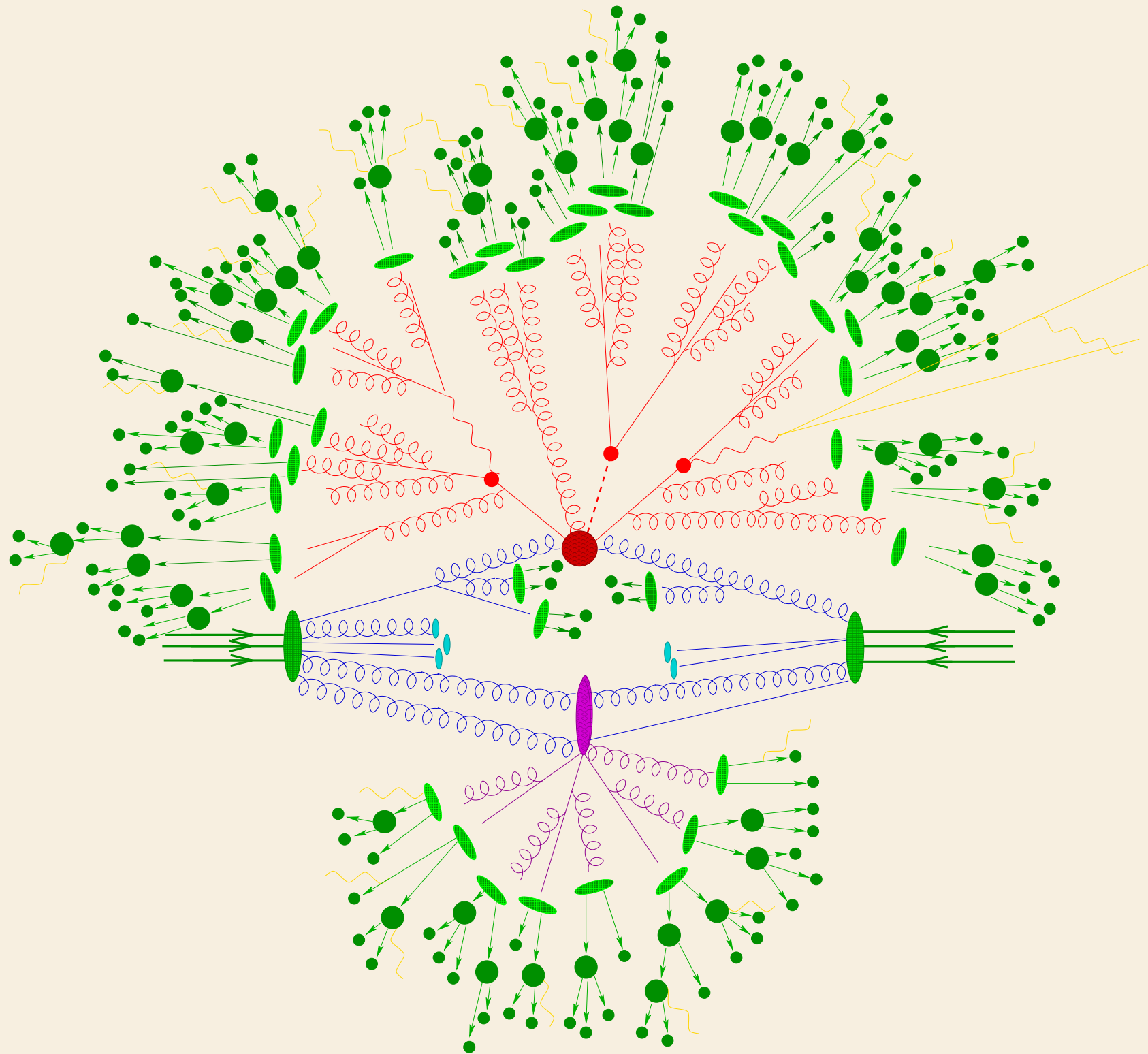
# Lattice unbeatable?

- recent prevailing view:  
lattice is unbeatable
- yet determination of  $\alpha_s$  from experiments remains desirable  
(or at least a fancy)
- $e^+e^-$  event shapes, jets
  - ✓ are sensitive to  $\alpha_s$
  - ✓ are measured extensively
  - ✓ can almost be computed from first principles  
(assuming local parton-hadron duality)

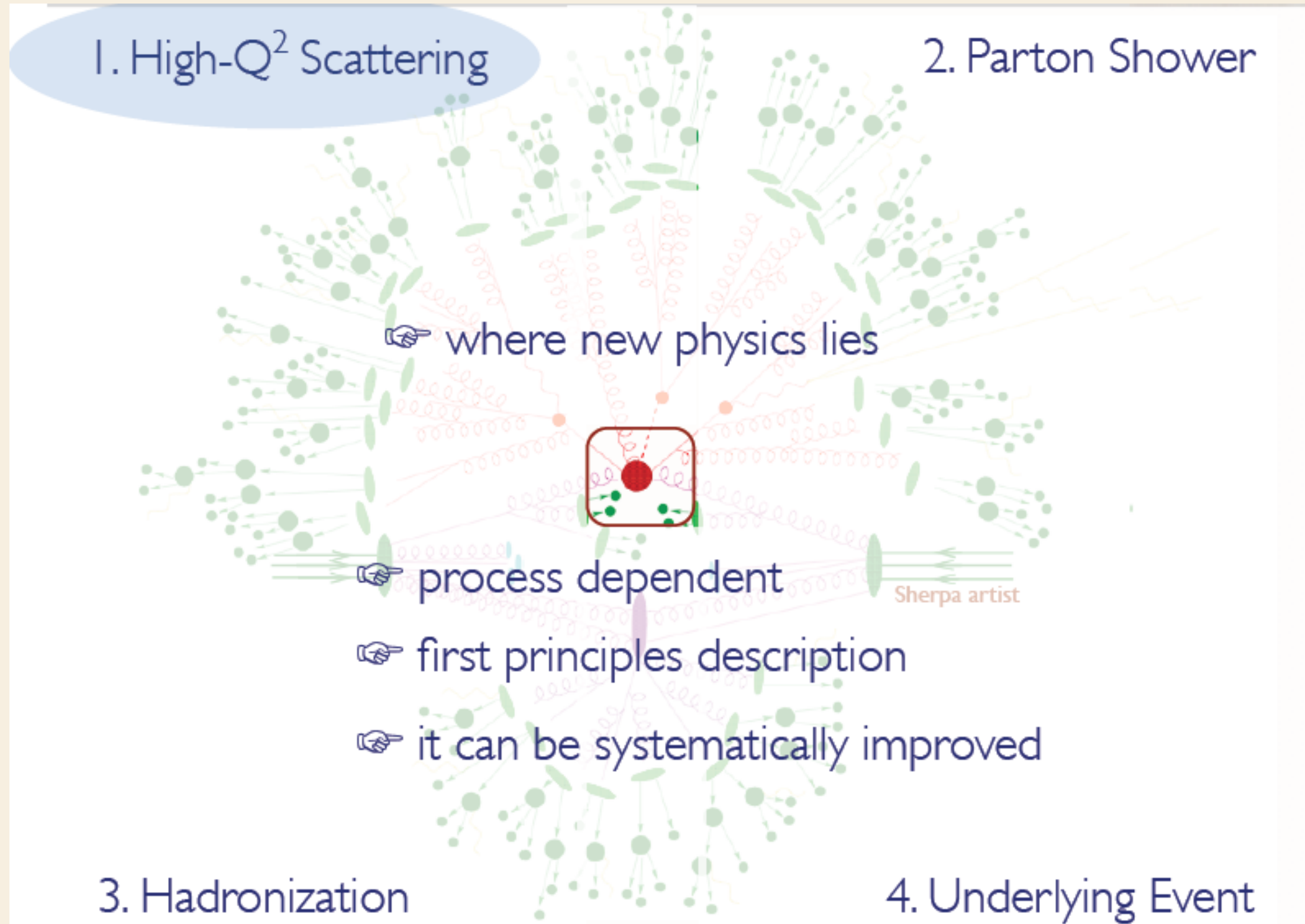


D. d'Enterria, arXiv: 1806.06156

# Our picture of a high-energy particle collision



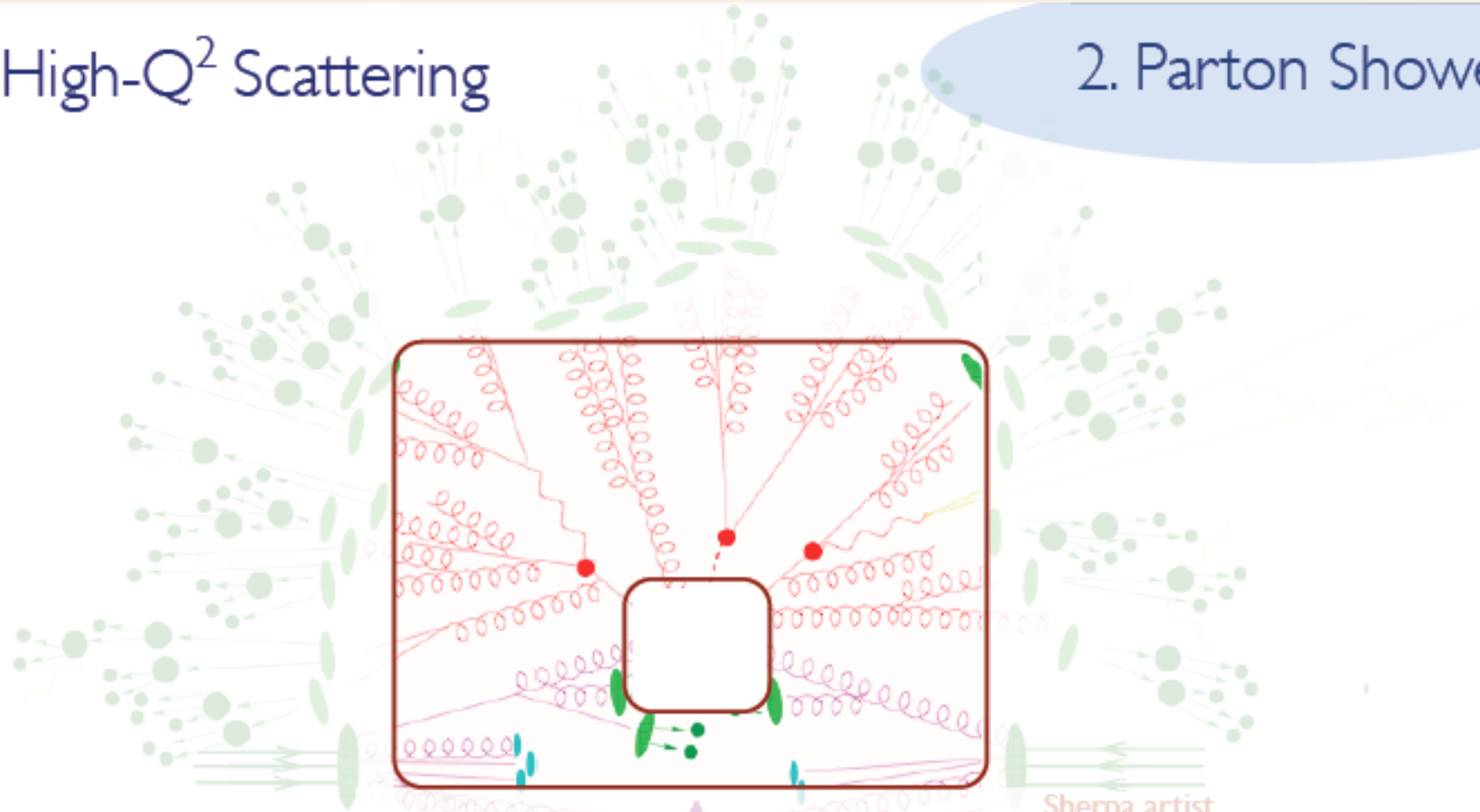
# Our picture of a high-energy particle collision



# Our picture of a high-energy particle collision

1. High- $Q^2$  Scattering

2. Parton Shower



Sherpa artist

- ☞ QCD - "known physics"
- ☞ universal/ process independent
- ☞ first principles description

3. Hadronization

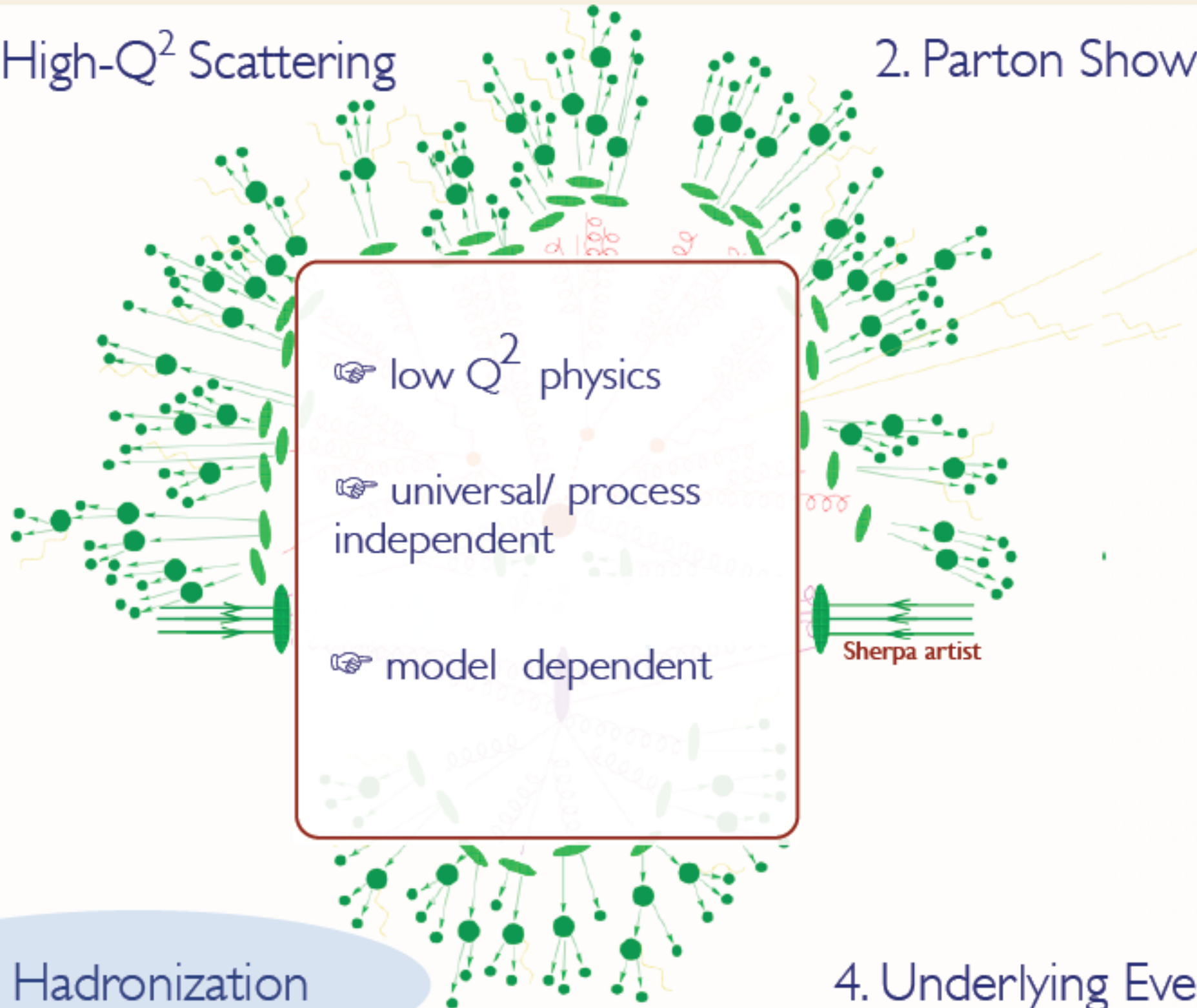
4. Underlying Event



# Our picture of a high-energy particle collision

1. High- $Q^2$  Scattering

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3. Hadronization

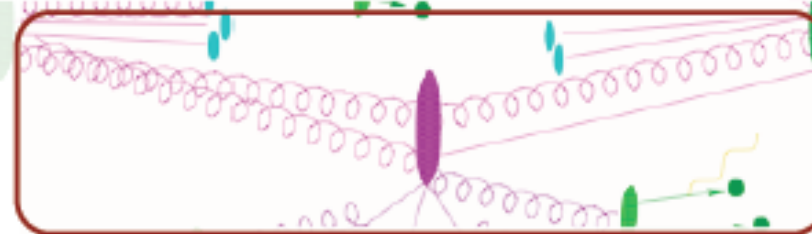
4. Underlying Event

# Our picture of a high-energy particle collision

1. High- $Q^2$  Scattering

2. Parton Shower

- low  $Q^2$  physics
- energy and process dependent
- model dependent



Sherpa artist

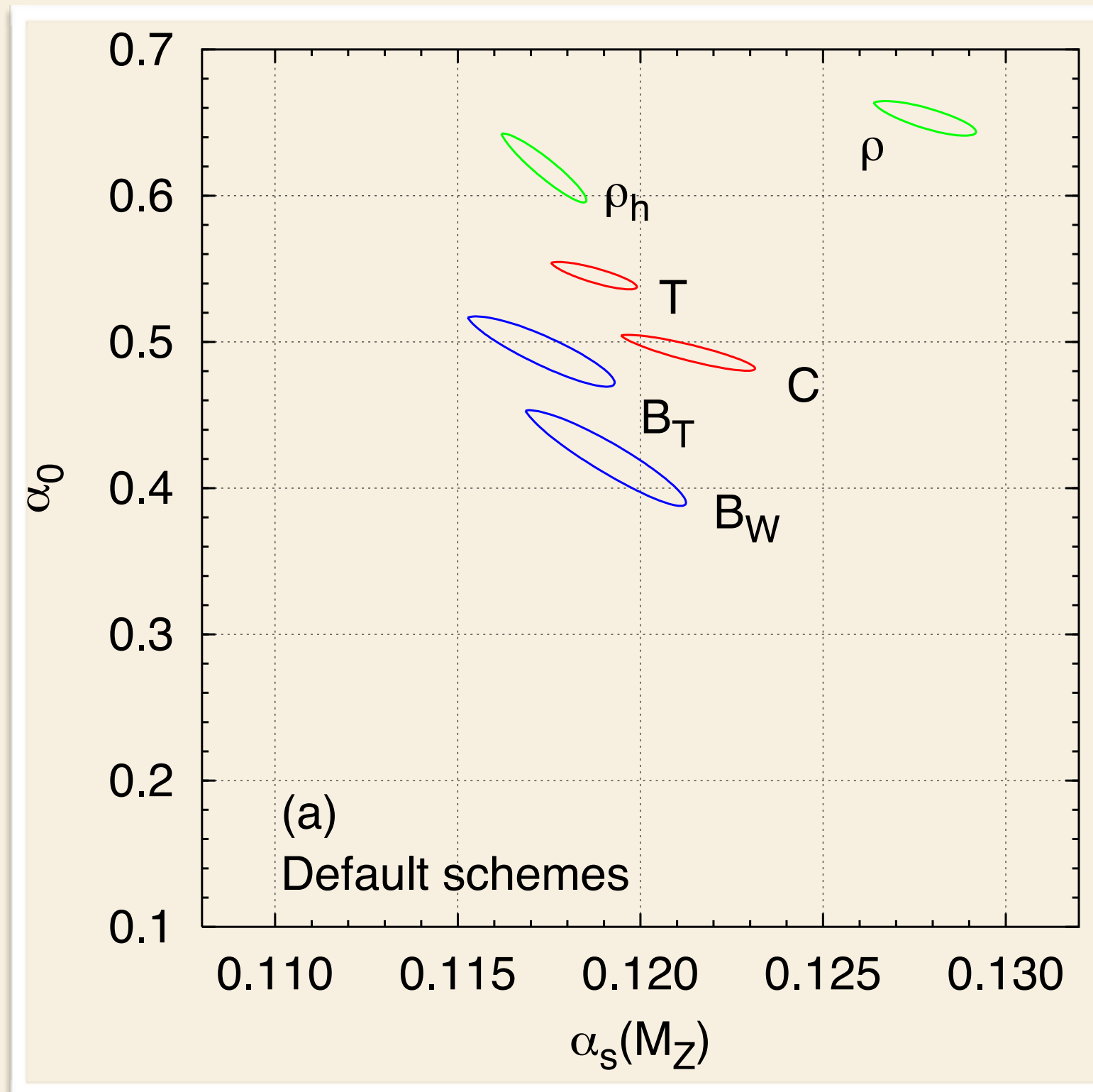
**absent in lepton collisions**

3. Hadronization

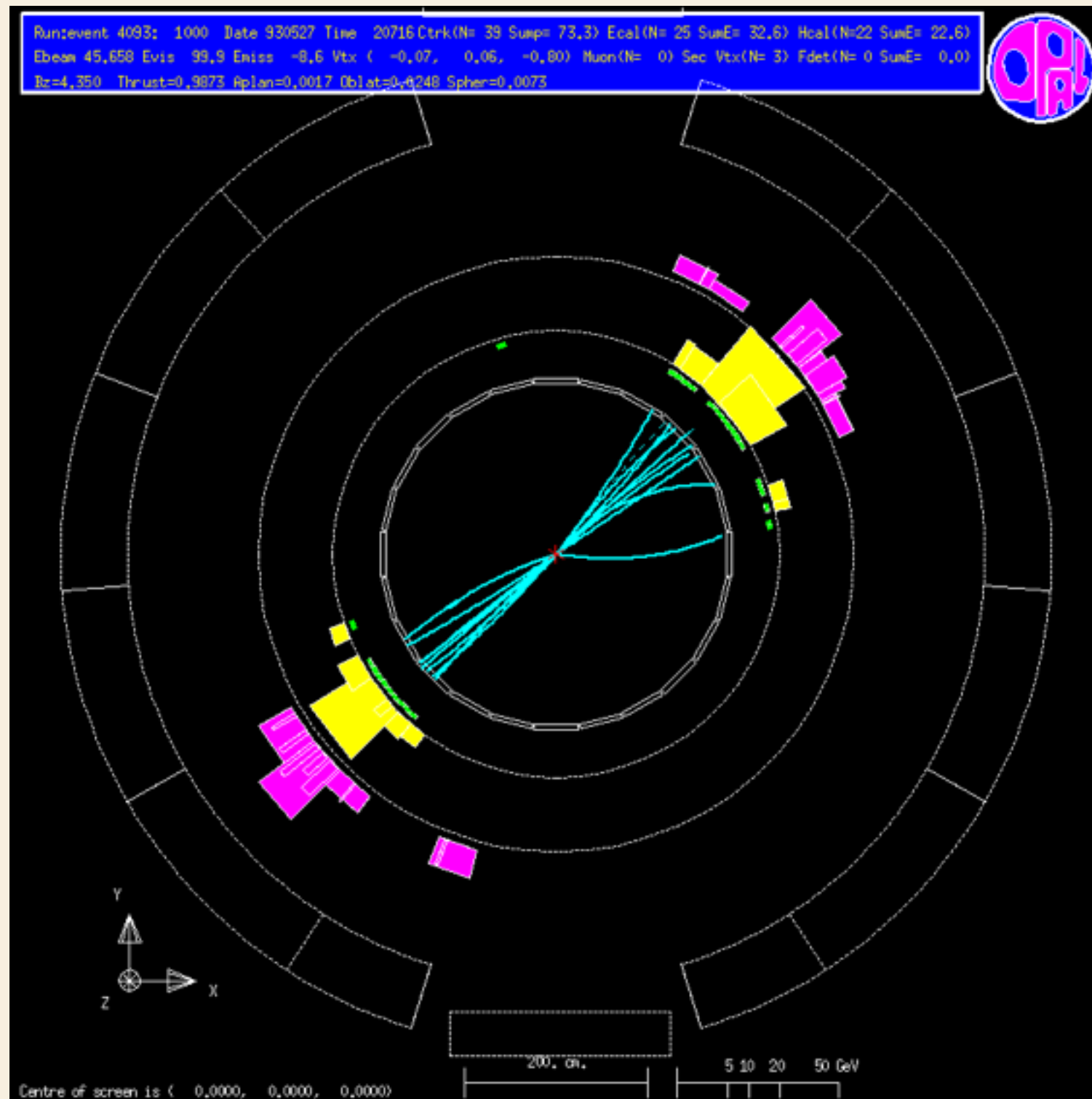
4. Underlying Event



# Shapes at NLO+NLL+power corr.+had. mass at LEP



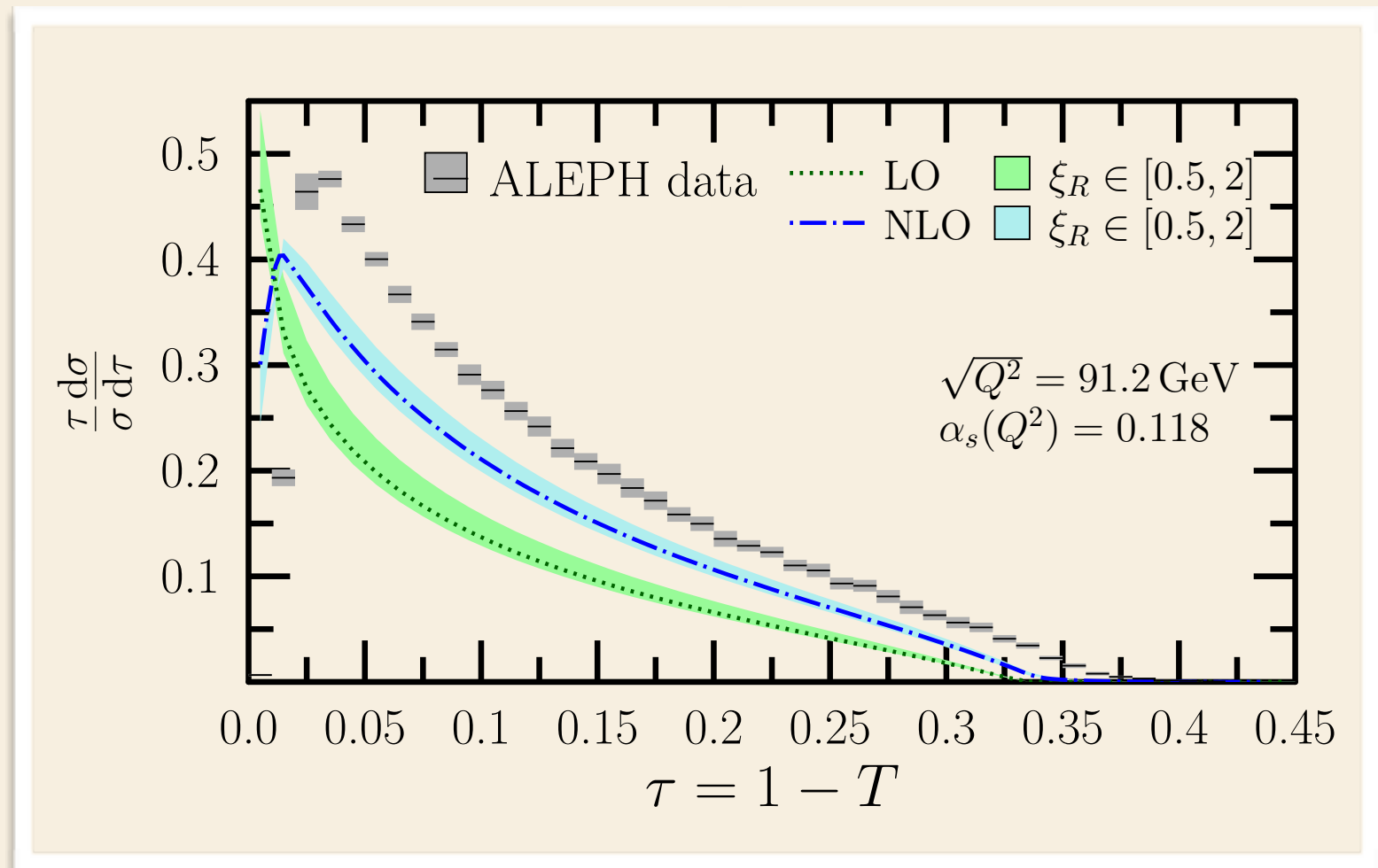
T = thrust: how pencil-like is the event



# Three-jet event shapes at LEP

- ▶ LO vs. NLO vs. data:

suffer large  
perturbative &  
hadronization  
corrections



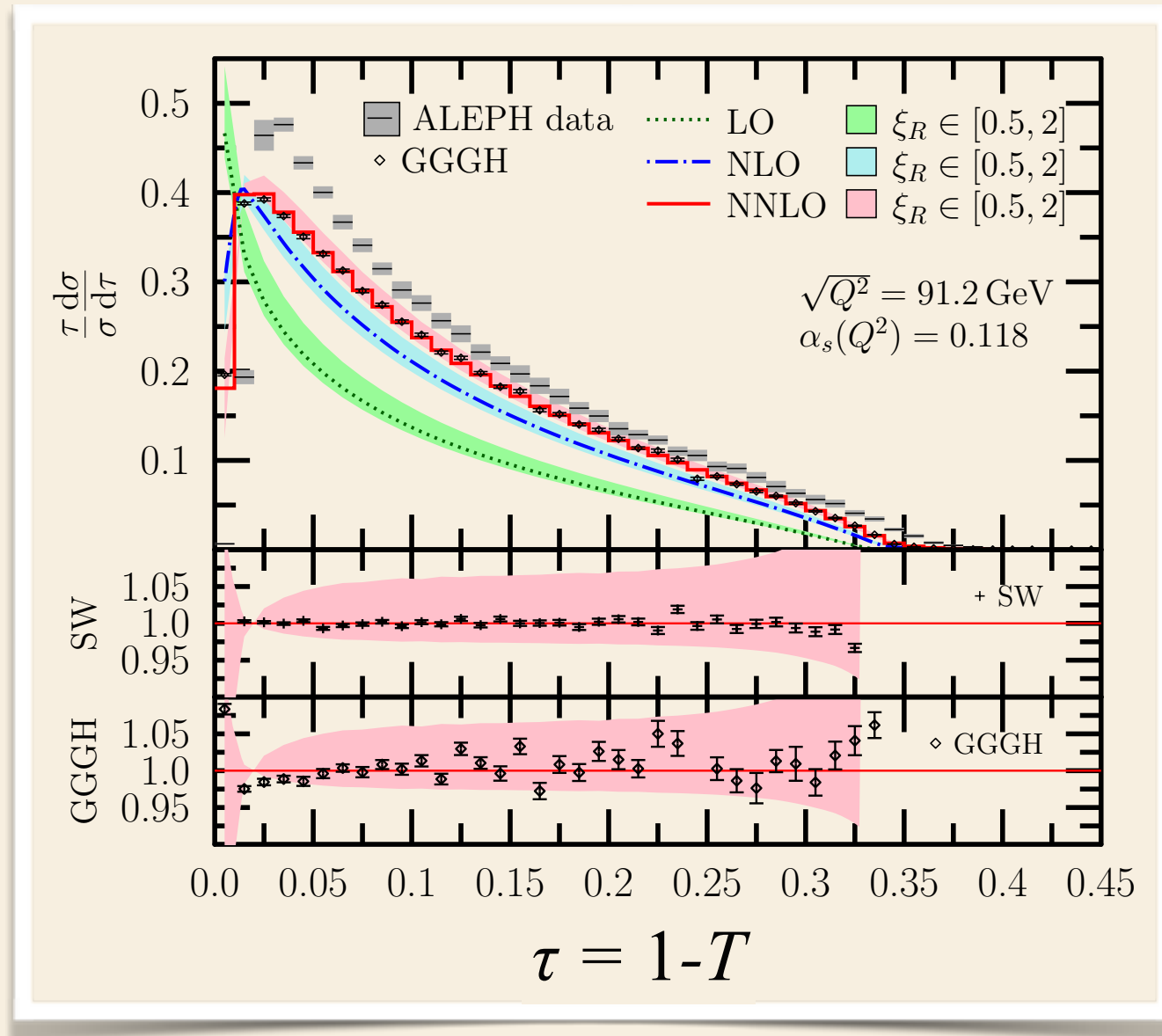
- ▶ new since LEP:

- ✓ NNLO corrections

- ✓ N<sup>2</sup>LL or N<sup>3</sup>LL resummation

New measurements of  $a_s$

# NNLO is not enough



$$T = \max_{\vec{n}} \left( \frac{\sum_i |\vec{n} \cdot \vec{p}_i|}{\sum_i |\vec{p}_i|} \right)$$

$$\frac{\tau d\sigma}{\sigma d\tau} = \left( \frac{\alpha_s}{2\pi} \right) A(\tau) + \left( \frac{\alpha_s}{2\pi} \right)^2 B(\tau) + \left( \frac{\alpha_s}{2\pi} \right)^3 C(\tau)$$

A, B and C computed with **MCCSM** (=Monte Carlo for CoLoRFulNNLO Subtraction Method)

# Analytic structure of perturbative expansion

$$\frac{\tau}{\sigma} \frac{d\sigma}{d\tau} = \left(\frac{\alpha_s}{2\pi}\right) A(\tau) + \left(\frac{\alpha_s}{2\pi}\right)^2 B(\tau) + \left(\frac{\alpha_s}{2\pi}\right)^3 C(\tau)$$

$$\begin{aligned} A(\tau) &= A_1 L + A_0, & L &= -\ln \tau \\ B(\tau) &= B_3 L^3 + B_2 L^2 + B_1 L + B_0, \\ C(\tau) &= C_5 L^5 + C_4 L^4 + C_3 L^3 + C_2 L^2 + C_1 L + C_0 \\ &\vdots & \vdots & \vdots & \vdots \end{aligned}$$

LL NLL N<sup>2</sup>LL N<sup>3</sup>LL ...

needs resummation of all orders

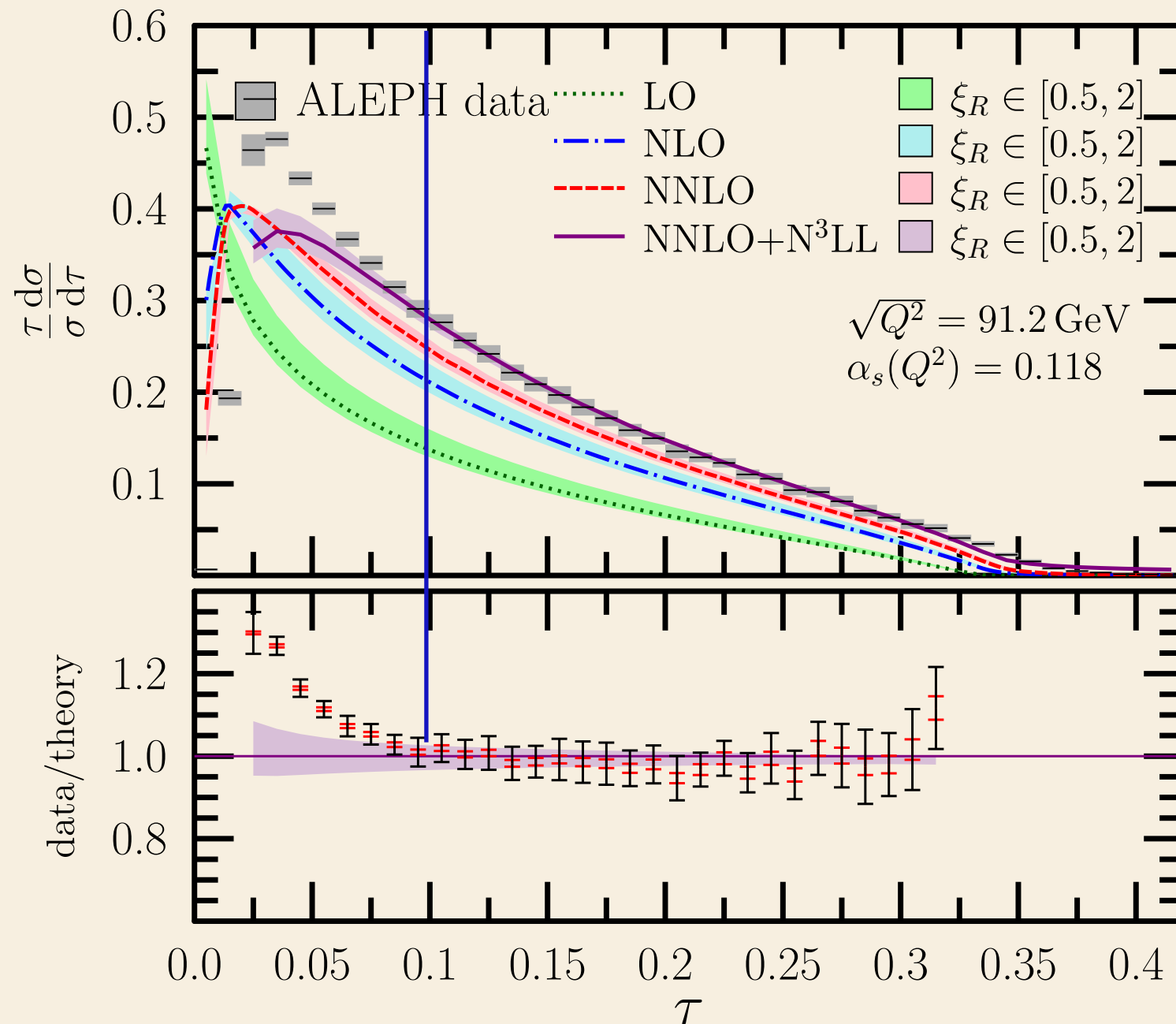
# How to improve?

✓ Match to approximate predictions that resum large logarithms of the event shapes

precise predictions are available, e.g.:

- $N^3LL$  for thrust ( $\tau$ ),  $C$ -parameter and heavy jet mass ( $\rho$ )
- $N^2LL$  for broadenings and EEC

# Matching NNLO with N<sup>3</sup>LL



Works for  $\tau > 0.1$ , fails in peak regions



# How to improve?

✓ Match to approximate predictions that resum large logarithms of the event shapes

precise predictions are available, e.g.:

– N<sup>3</sup>LL for thrust ( $\tau$ ),  $C$ -parameter and heavy jet mass ( $\rho$ )

– N<sup>2</sup>LL for broadenings and EEC

✓ Correct for hadronisation

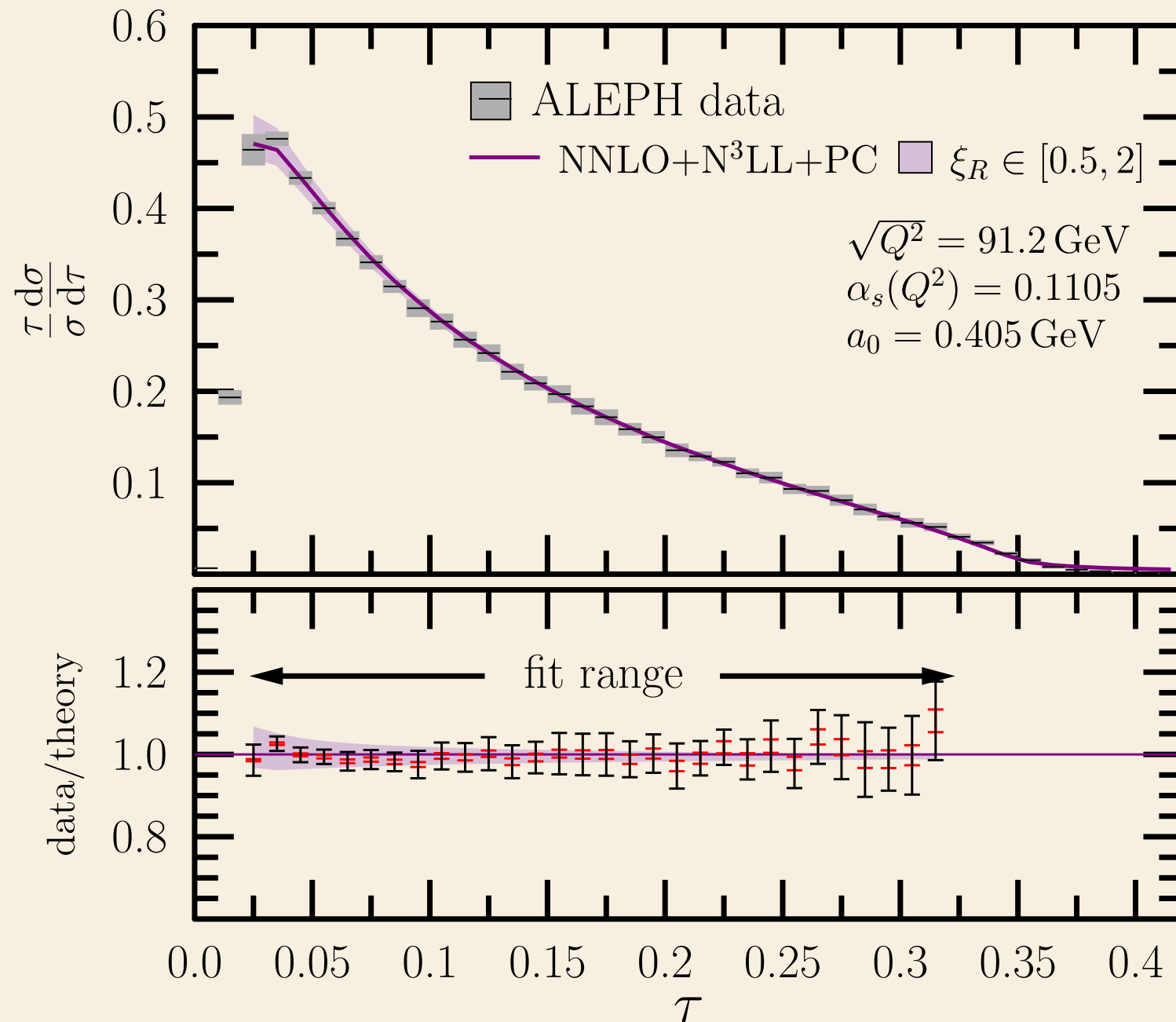
two options:

– estimate of hadronisation using modern MC tools

– use analytic model for power corrections, e.g.:

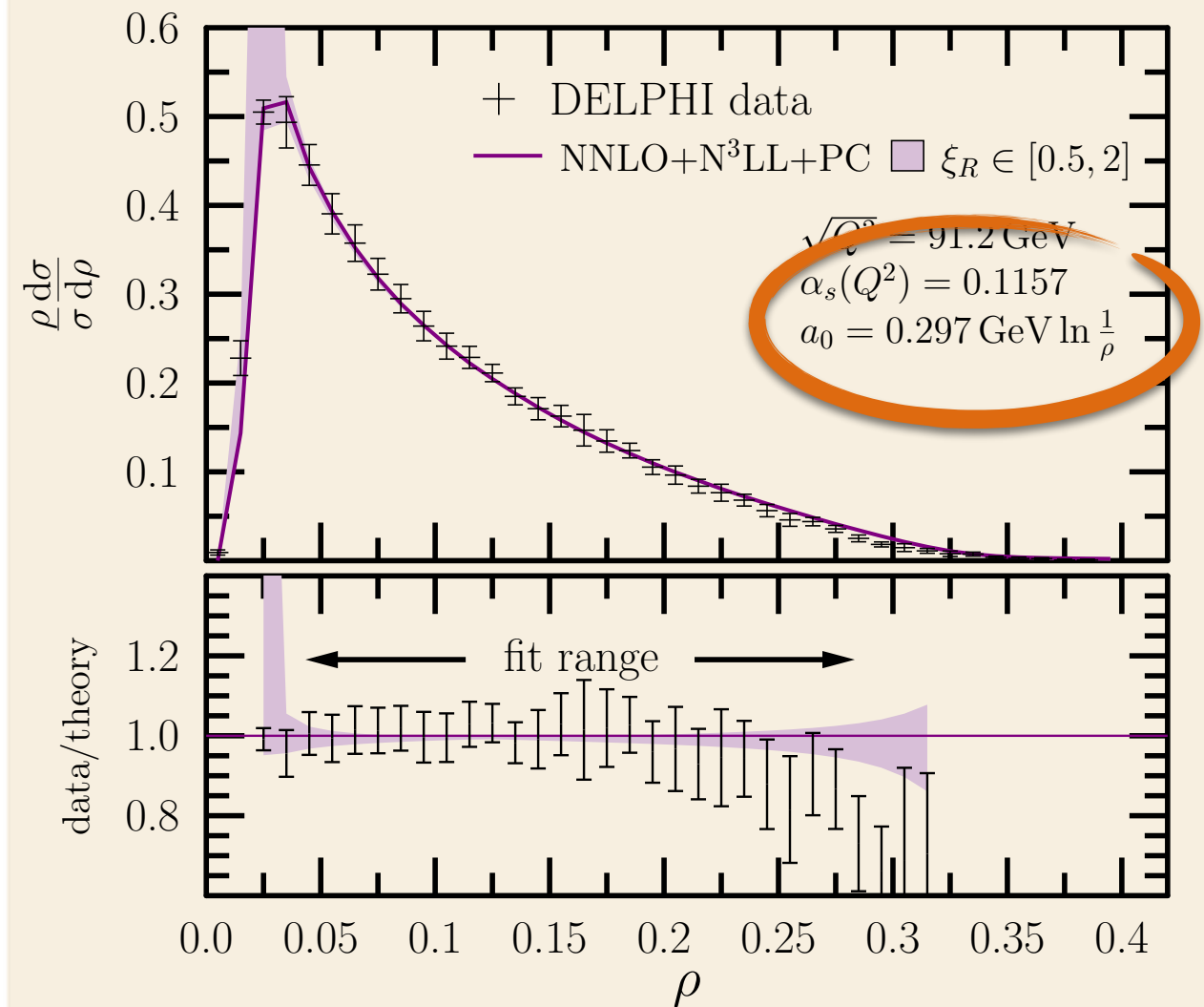
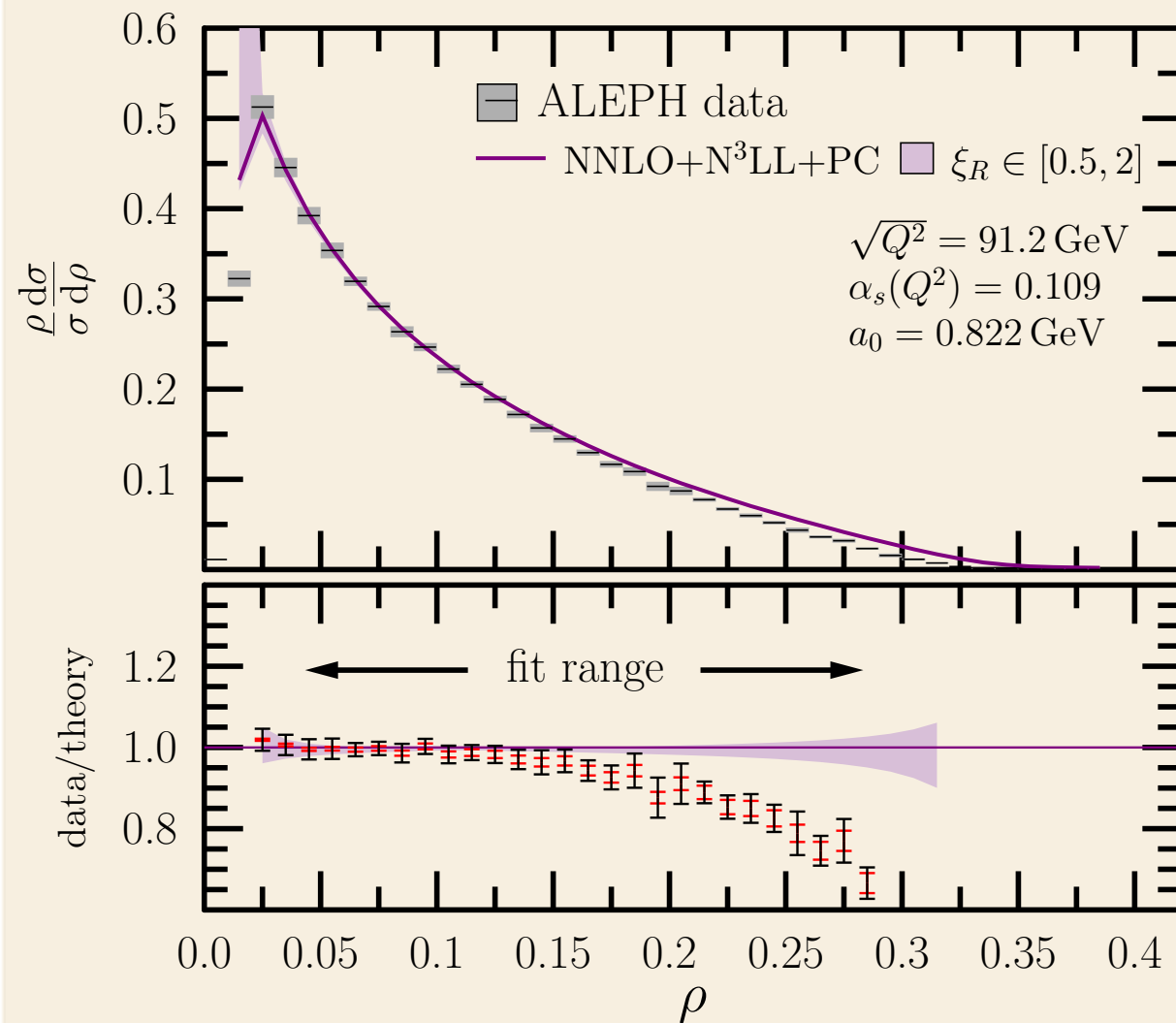
$$\frac{\tau}{\sigma} \frac{d\sigma}{d\tau}(\tau) \rightarrow \frac{\tau}{\sigma} \frac{d\sigma}{d\tau}(\tau - 2a_0)$$

# Fit to data with NNLO+N<sup>3</sup>LL+PC



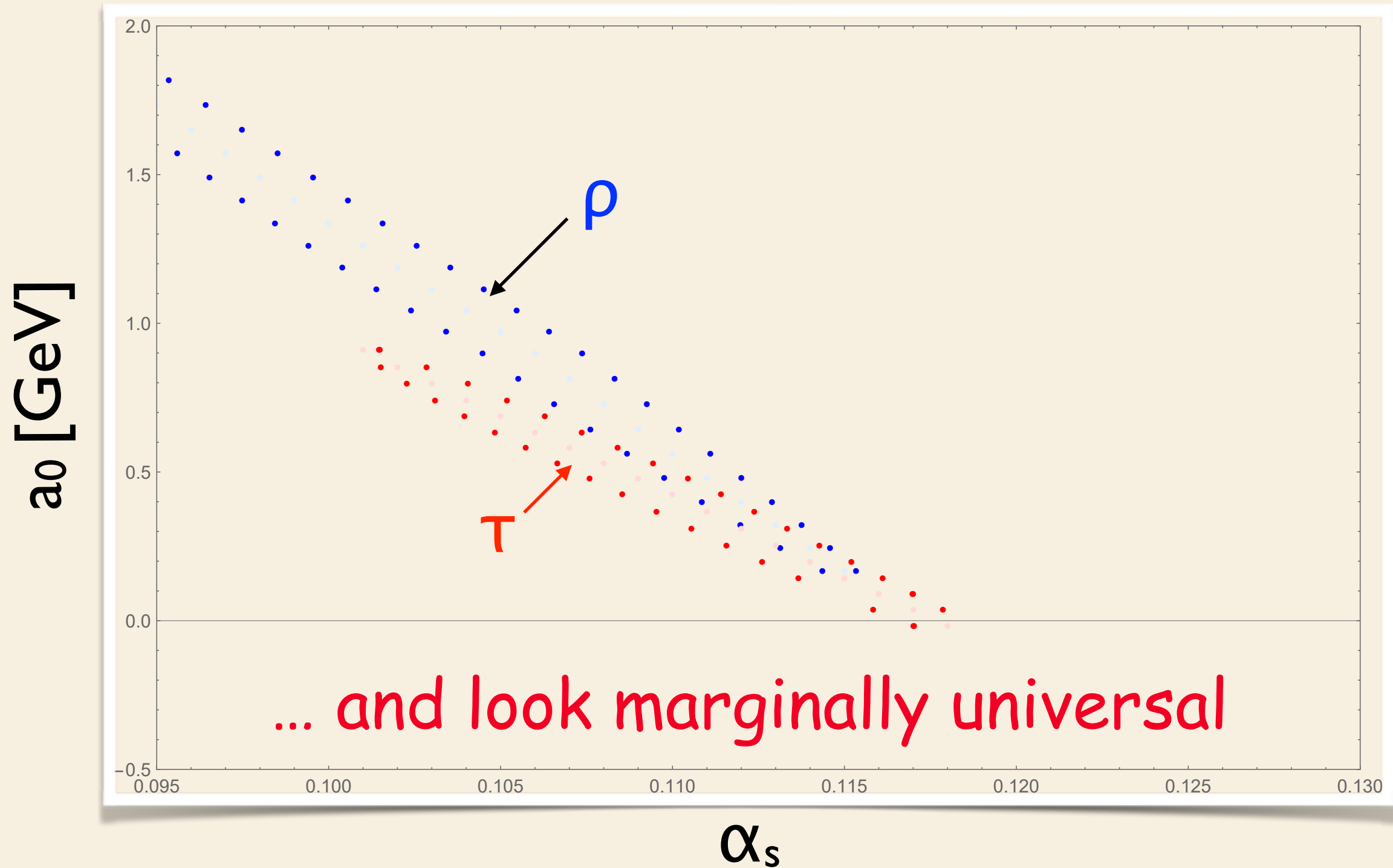
Works down to the peak, but

# Fit data on heavy jet mass with NNLO+N<sup>3</sup>LL+PC

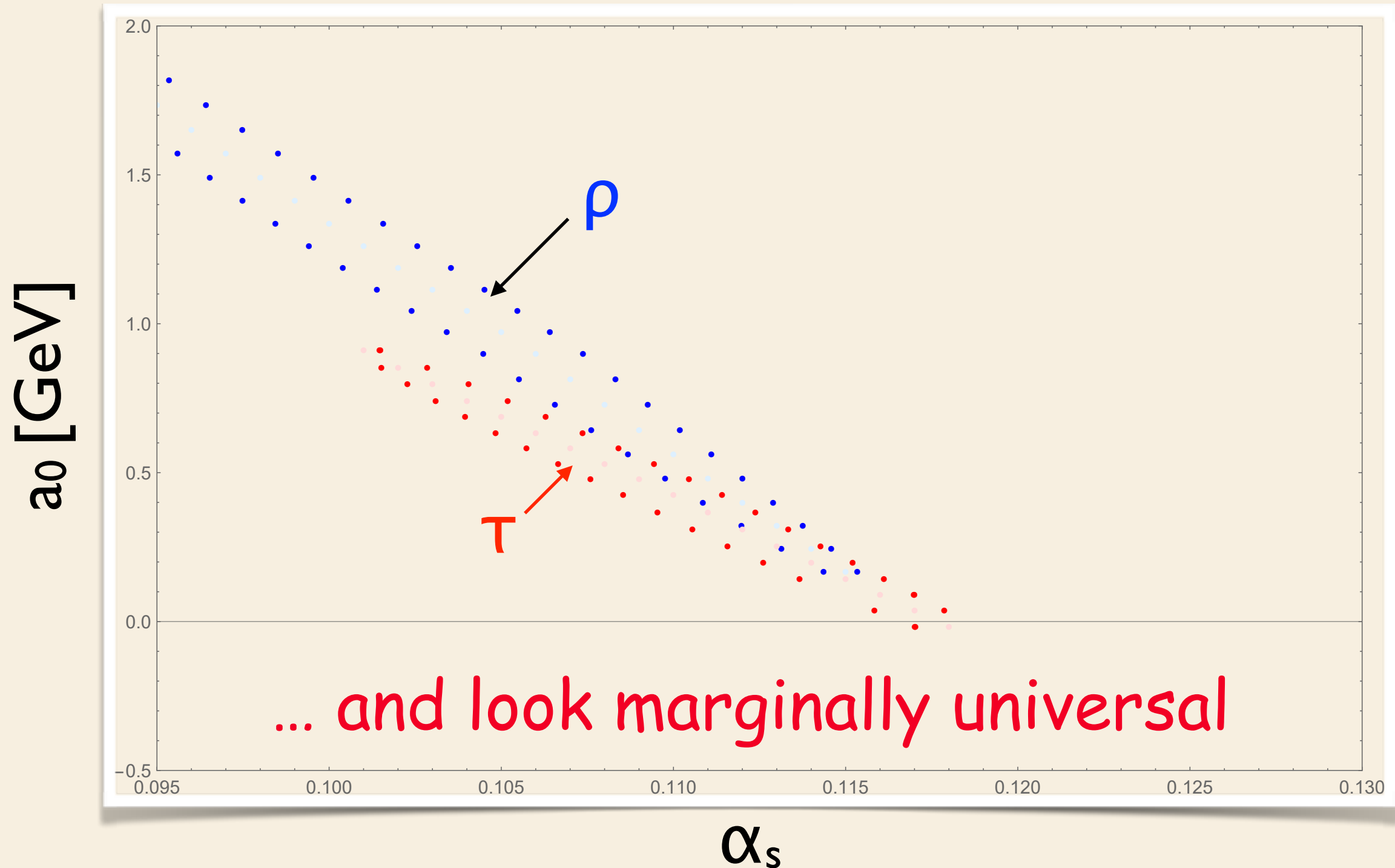


... not as expected

# Fit to data with PC



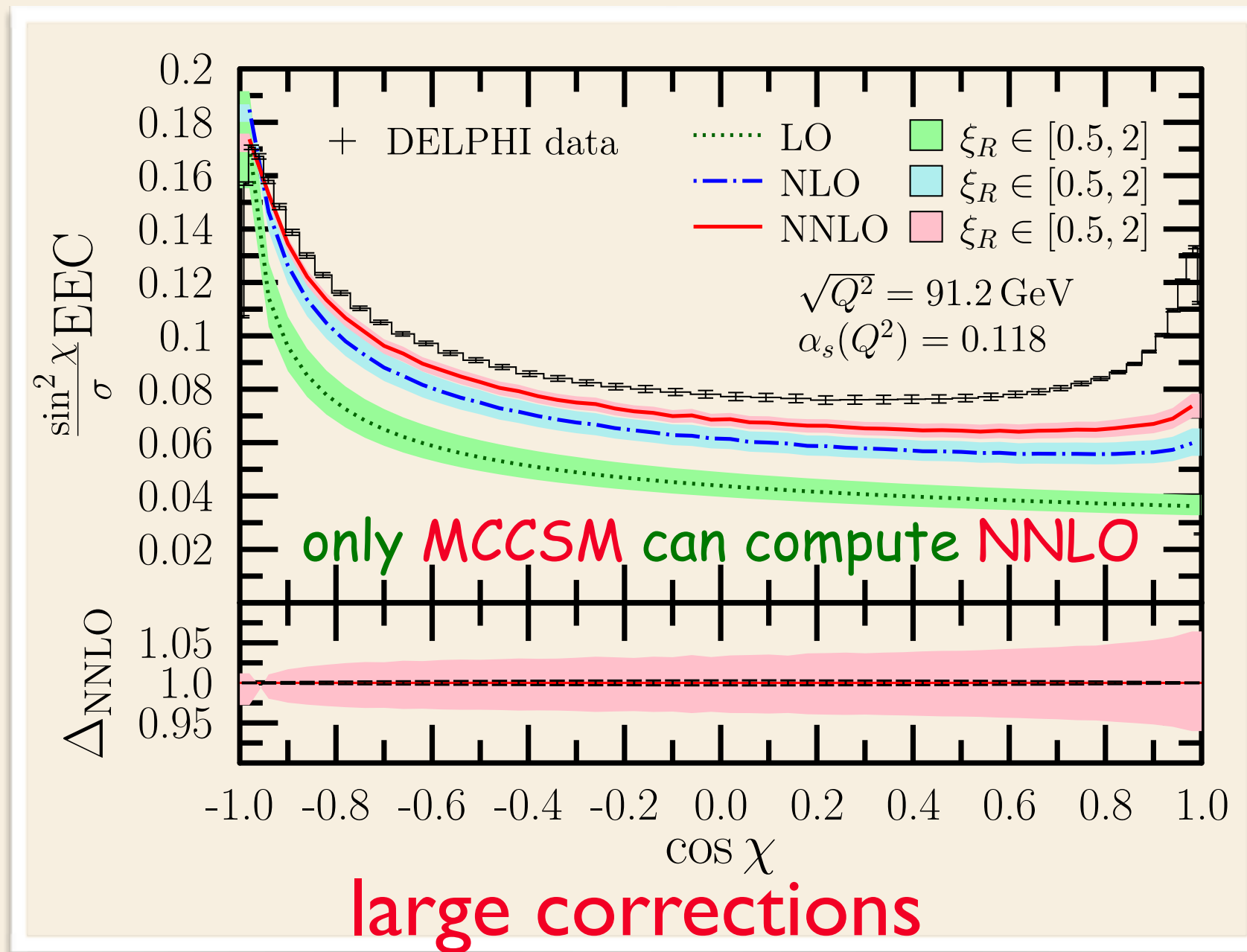
# Fit to data with PC



... and look marginally universal

but  $a_0$  and  $\alpha_s$  are strongly anticorrelated

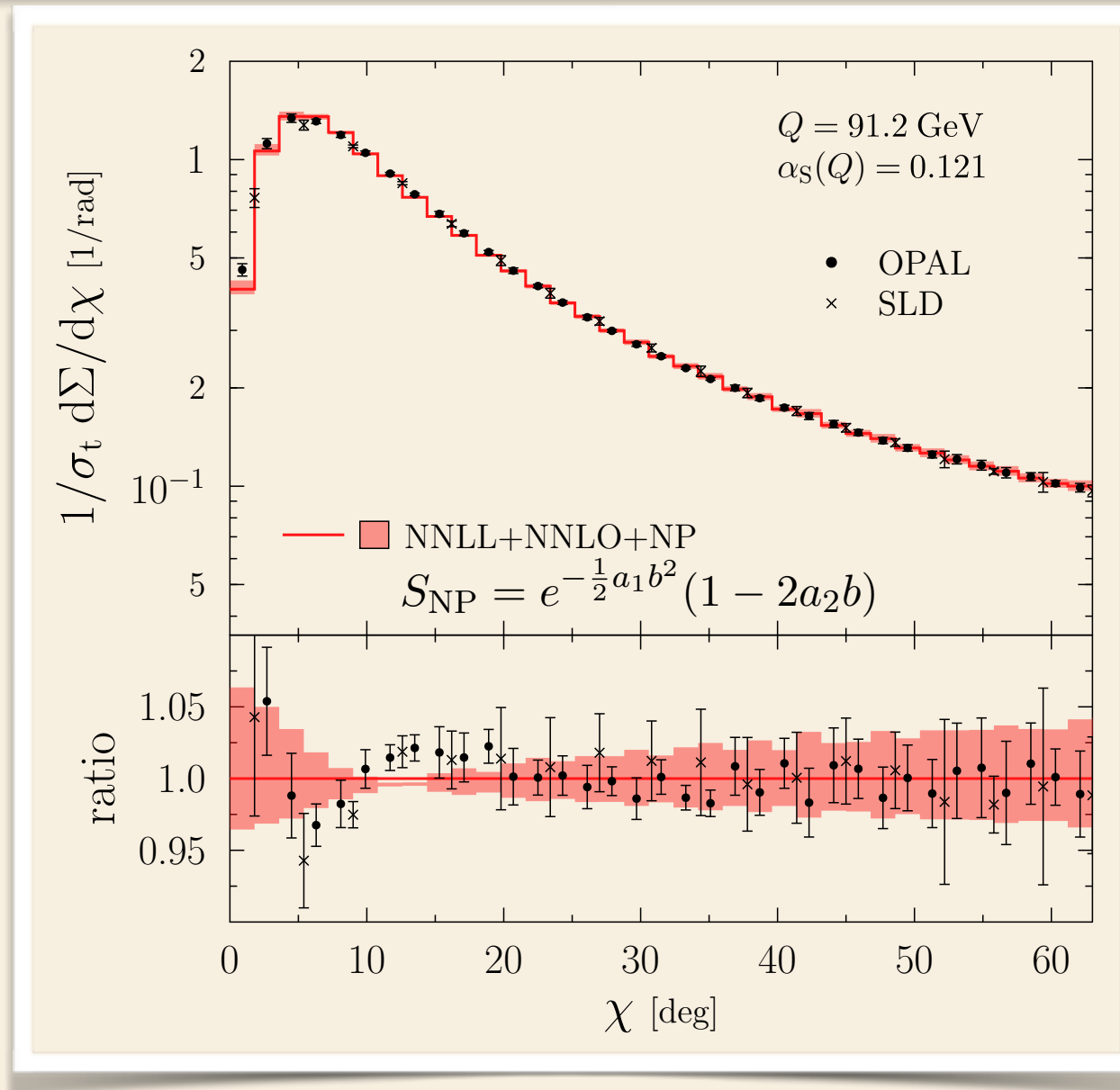
# EEC @ fixed orders



$$\text{EEC}(\chi) = \frac{1}{\sigma_{\text{had}}} \sum_{i,j} \int \frac{E_i E_j}{Q^2}$$

$$\times d\sigma_{e^+e^- \rightarrow ij+X} \delta(\cos \chi + \cos \theta_{ij})$$

# EEC @ NNLO+NNLL+NP



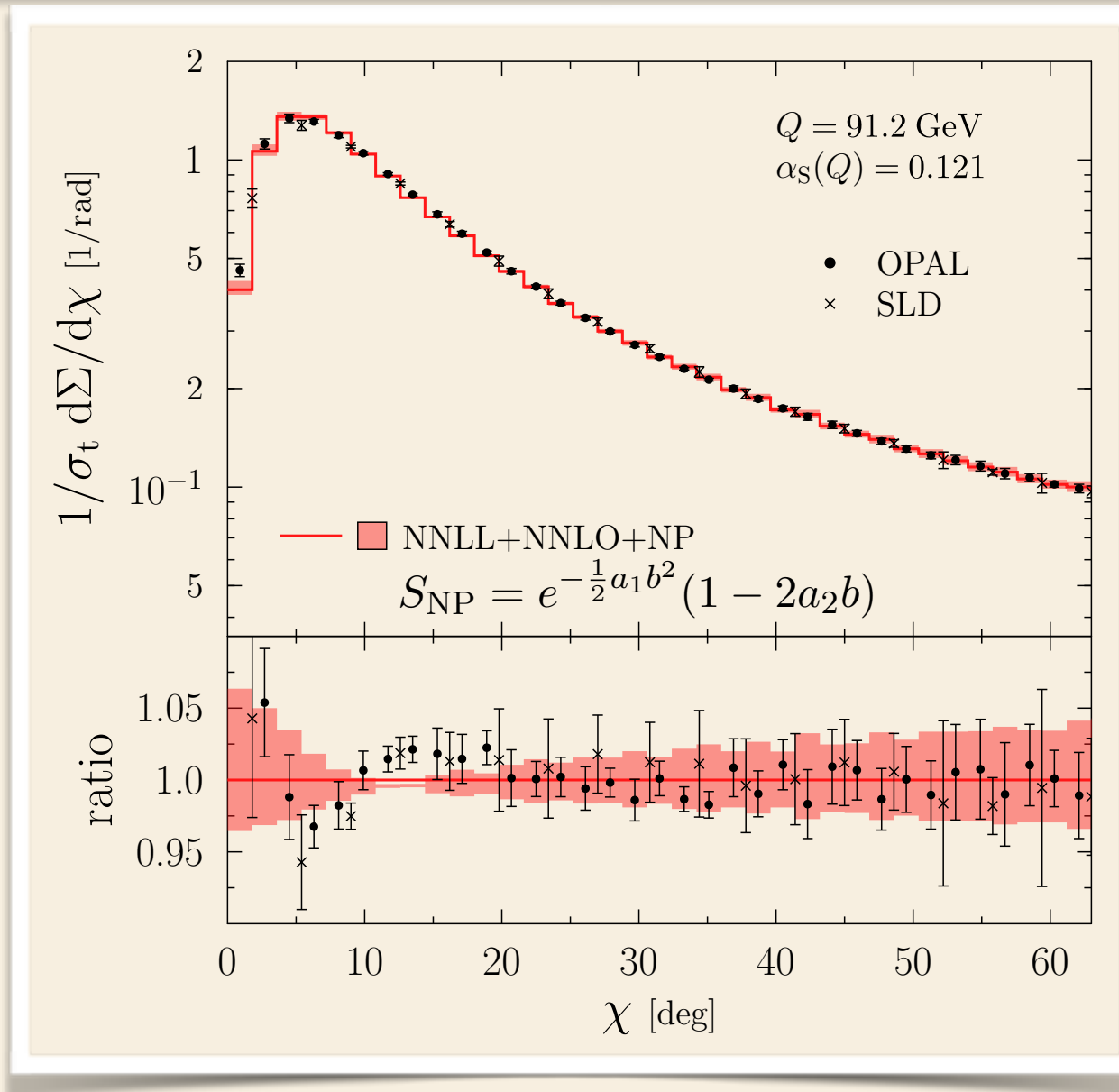
$$\alpha_S(M_Z) = 0.121^{+0.001}_{-0.003}$$

$$a_1 = 2.47^{+0.48}_{-2.38} \text{ GeV}^2$$

$$a_2 = 0.31^{+0.27}_{-0.05} \text{ GeV}$$

$$\text{corr}(\alpha_S, a_1, a_2) = \begin{pmatrix} 1 & 0.05 & -0.97 \\ 0.05 & 1 & -0.07 \\ -0.97 & -0.07 & 1 \end{pmatrix}$$

# EEC @ NNLO+NNLL+NP



$$\alpha_S(M_Z) = 0.121^{+0.001}_{-0.003}$$

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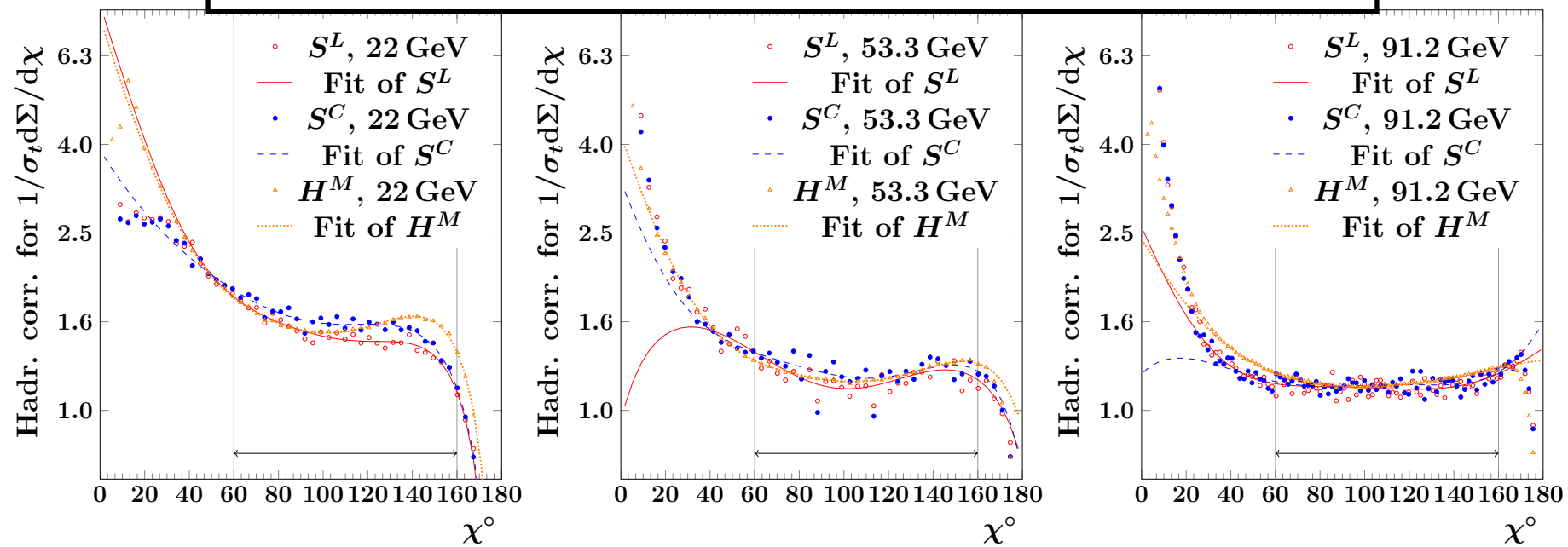
👉 parameters are strongly anticorrelated



# How to improve?

- ✓ Correct for hadronisation, 2nd option:
  - estimate of hadronisation using modern MC tools

$$\frac{1}{\sigma_t} \frac{d\Sigma}{d \cos \chi} = \frac{1}{\sigma_t} \int \sum_{i,j} \frac{E_i E_j}{Q^2} d\sigma_{e^+e^- \rightarrow ij+\chi} \delta(\cos \chi + \cos \theta_{ij})$$



Hadronization corrections are parametrized using smooth functions to tame statistical fluctuations

Parametrization is valid only in the fit range

# Fit results

Global fit at NNLL+NLO:

$$\alpha_S(M_Z) = 0.12200 \pm 0.00023(\text{exp.}) \pm 0.00113(\text{hadr.}) \pm 0.00433(\text{ren.}) \pm 0.00293(\text{res.})$$

with combined uncertainty:  $\alpha_S(M_Z) = 0.12200 \pm 0.00535$

Global fit at NNLL+NNLO:

$$\alpha_S(M_Z) = 0.11750 \pm 0.00018(\text{exp.}) \pm 0.00102(\text{hadr.}) \pm 0.00257(\text{ren.}) \pm 0.00078(\text{res.})$$

with combined uncertainty:  $\alpha_S(M_Z) = 0.11750 \pm 0.00287$

The effect of NNLO on central value is moderate but not negligible, *ren.* uncertainty down by a factor of 2, *res.* uncertainty down by a factor of 3

The overall uncertainty is dominated by theoretical uncertainty (*ren.* and *res.*)

# Works better for jet rates

Global fit at NNLL+NNLO:

$$\alpha_s(M_Z) = 0.11881 \pm 0.00063(\text{exp.}) \pm 0.00101(\text{hadr.}) \pm 0.00045(\text{ren.}) \pm 0.00034(\text{res.})$$

with combined uncertainty:  $\alpha_s(M_Z) = 0.11881 \pm 0.00131(\text{comb.})$

compared to result using energy-energy correlation:

Global fit at NNLL+NNLO:

$$\alpha_s(M_Z) = 0.11750 \pm 0.00018(\text{exp.}) \pm 0.00102(\text{hadr.}) \pm 0.00257(\text{ren.}) \pm 0.00078(\text{res.})$$

with combined uncertainty:  $\alpha_s(M_Z) = 0.11750 \pm 0.00287$

Conclusions

# Conclusions

Precise determination of the strong coupling using hadronic final states in electron-positron annihilation requires

- careful selection of observables (and data – not discussed here)
- methods to reduce hadronisation corrections
- estimation of the hadronisation corrections with modern MCs

New determination based on NNLO+NNLL+non-perturbative corrections from MC simulation gives

$$\alpha_s(M_Z) = 0.11881 \pm 0.00131(\text{comb.})$$

with uncertainty competitive with other determinations

Outlook

# Outlook: prospects for $a_s$

Method	Current relative precision	Future relative precision
$e^+e^-$ evt shapes	expt $\sim 1\%$ (LEP) thry $\sim 1-3\%$ (NNLO+up to N <sup>3</sup> LL, n.p. signif.) [27]	$< 1\%$ possible (ILC/TLEP) $\sim 1\%$ (control n.p. via $Q^2$ -dep.)
$e^+e^-$ jet rates	expt $\sim 2\%$ (LEP) thry $\sim 1\%$ (NNLO, n.p. moderate) [28]	$< 1\%$ possible (ILC/TLEP) $\sim 0.5\%$ (NLL missing)
precision EW	expt $\sim 3\%$ ( $R_Z$ , LEP) thry $\sim 0.5\%$ (N <sup>3</sup> LO, n.p. small) [9, 29]	0.1% (TLEP [10]), 0.5% (ILC [11]) $\sim 0.3\%$ (N <sup>4</sup> LO feasible, $\sim 10$ yrs)
$\tau$ decays	expt $\sim 0.5\%$ (LEP, B-factories) thry $\sim 2\%$ (N <sup>3</sup> LO, n.p. small) [8]	$< 0.2\%$ possible (ILC/TLEP) $\sim 1\%$ (N <sup>4</sup> LO feasible, $\sim 10$ yrs)
$ep$ colliders	$\sim 1-2\%$ (pdf fit dependent) [30, 31], (mostly theory, NNLO) [32, 33]	0.1% (LHeC + HERA [23]) $\sim 0.5\%$ (at least N <sup>3</sup> LO required)
hadron colliders	$\sim 4\%$ (Tev. jets), $\sim 3\%$ (LHC $t\bar{t}$ ) (NLO jets, NNLO $t\bar{t}$ , gluon uncert.) [17, 21, 34]	$< 1\%$ challenging (NNLO jets imminent [22])
lattice	$\sim 0.5\%$ (Wilson loops, correlators, ...) (limited by accuracy of pert. th.) [35-37]	$\sim 0.3\%$ ( $\sim 5$ yrs [38])

Determination of strong coupling from  $e^+e^-$  data with decreased theoretical uncertainty might be possible

# How to improve?

- ✓ Correct for hadronisation, 2nd option:
  - estimate of hadronisation using modern MC tools
- ✓ Find observable quantities with small perturbative and hadronisation corrections:

motto: "large uncertainty in small quantity is small uncertainty"



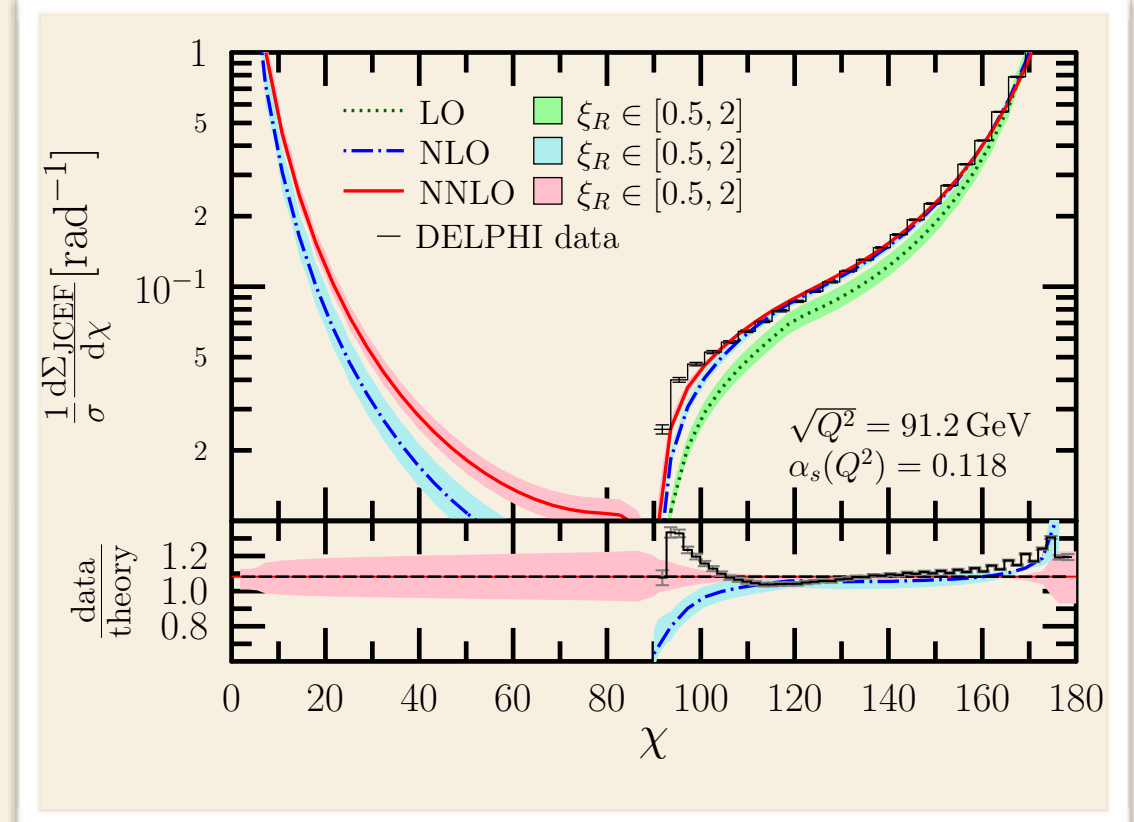
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jet cone energy fraction:

$$\frac{d\Sigma_{\text{JCEF}}}{d \cos \chi} = \sum_i \int \frac{E_i}{Q} d\sigma_{e^+e^- \rightarrow i+X} \delta\left(\cos \chi - \frac{\vec{p}_i \cdot \vec{n}_T}{|\vec{p}_i|}\right)$$



# How to improve?

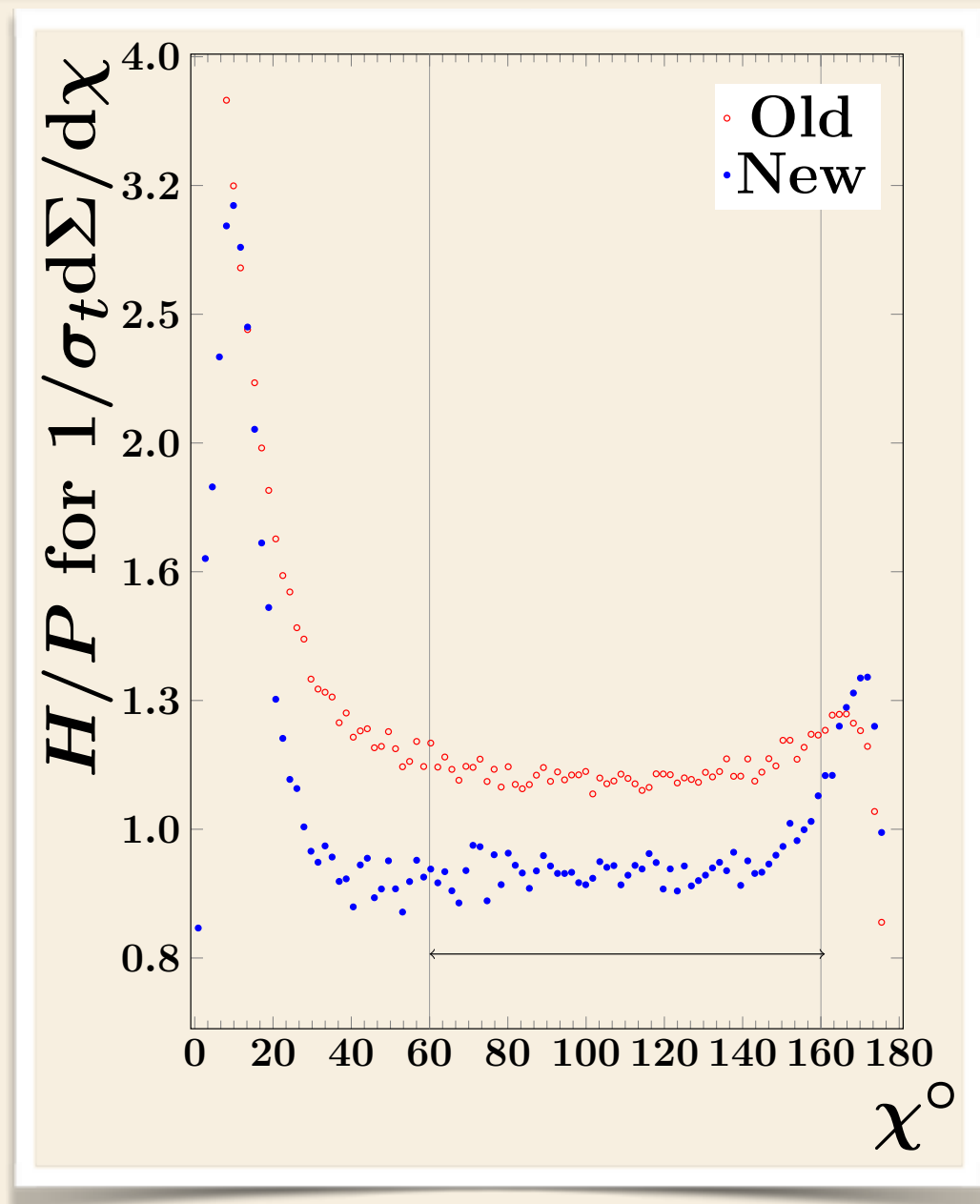
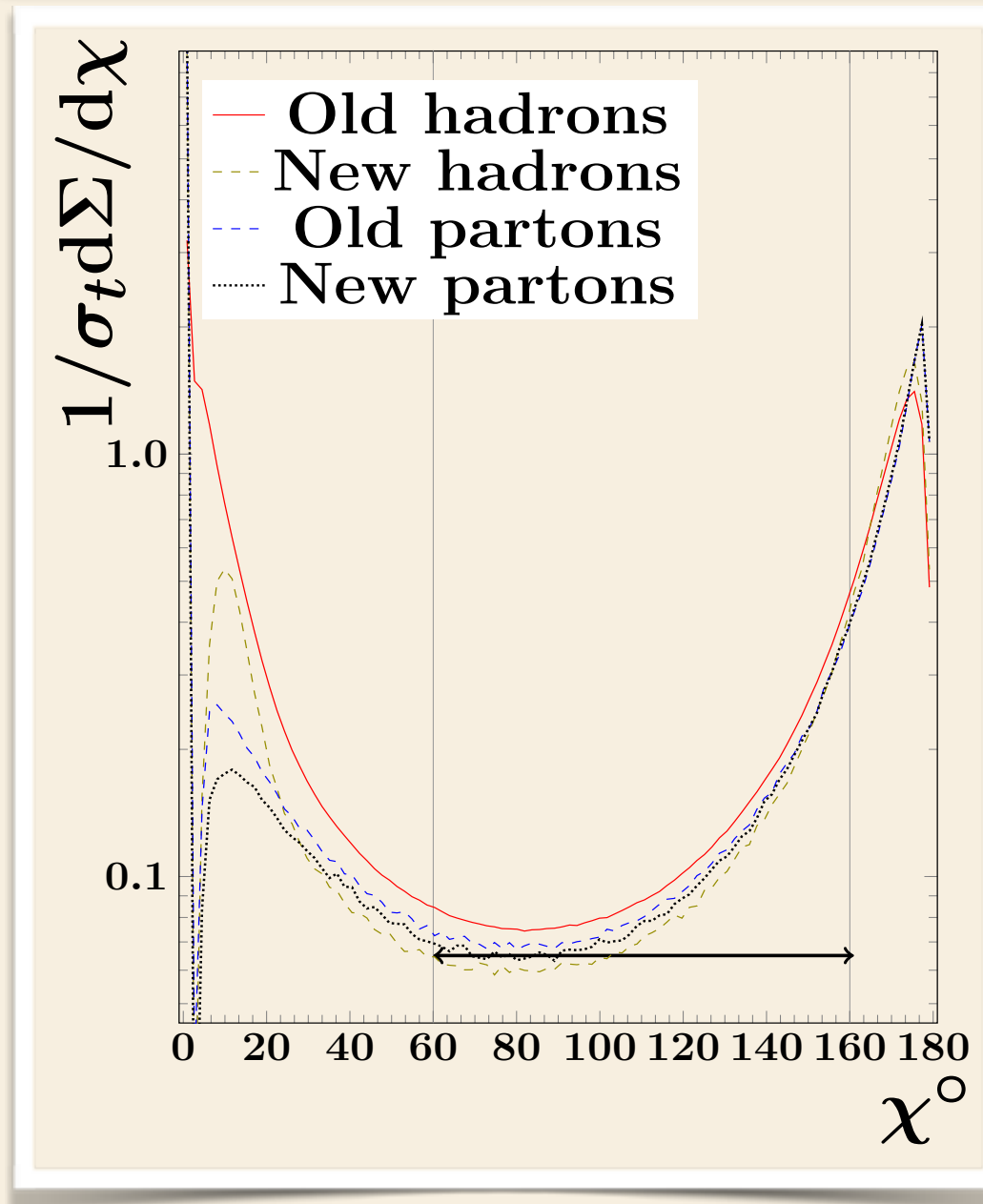
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- precluster hadrons and compute shapes from jets

Decamp et al [ALEPH], Phys.Lett. B257 (1991) 479-491

# Preclustering reduces hadronization corrections



Old: without, New: with preclustering  
(requiring 5 jets)

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motto: "large uncertainty in small quantity is small uncertainty"

- precluster hadrons and compute shapes from jets  
Decamp et al [ALEPH], Phys.Lett. B257 (1991) 479-491
- groomed (soft drop) event shapes, designed to reduce contamination from non-perturbative effects

Work in progress...