

Two-loop QED corrections
to the bound-electron g factor
involving the magnetic loop

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Provides a measure of the Zeeman splitting of energy levels

$$\Delta E = g \frac{\mu_B}{\hbar} \langle \psi | \mathbf{J} \cdot \mathbf{B} | \psi \rangle$$

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Measurement in **Penning trap**

Precision: 10^{-11} for medium-light H-like ions

Soon to come: same precision for medium and heavy H-like ions (e.g. Ca, Xe, Pb)

→ Motivates improvements of theory

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QED calculations

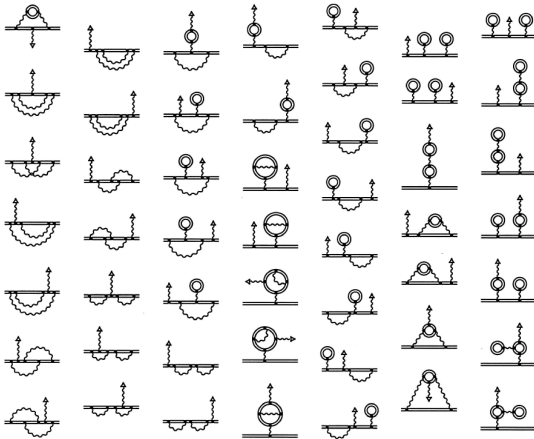
- Perturbative approach: free e^- + perturbative binding to nucleus (series in $(Z\alpha)$)
- Non-perturbative approach: bound state QED

Loops from QED are to be treated perturbatively in all approaches (series in α)

Current knowledge of two-loop corrections:

- Perturbative approach: $(Z\alpha)^4$ [K. Pachucki, A. Czarnecki, U. D. Jentschura, V. A. Yerokhin, Phys. Rev. A **72**, 022108 (2005)]
 $(Z\alpha)^5$ [A. Czarnecki, M. Dowling, J. Piclum, R. Szafron, Phys. Rev. Lett. **120**, 043203 (2018)]
- Non-perturbative approach: partial knowledge

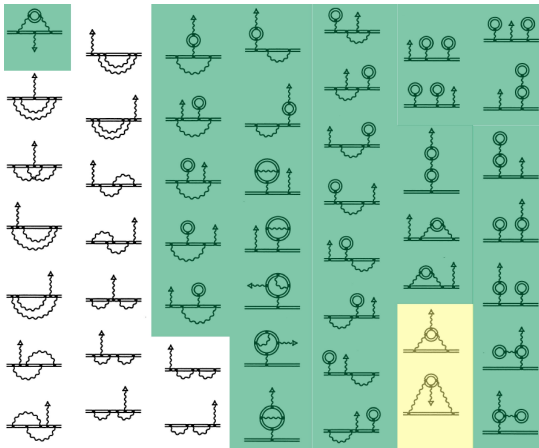
Two-loop QED corrections



50 total diagrams
(29 inequivalent diagrams)

(from T. Beier *et al.*, *Phys. Rev. A* 62,
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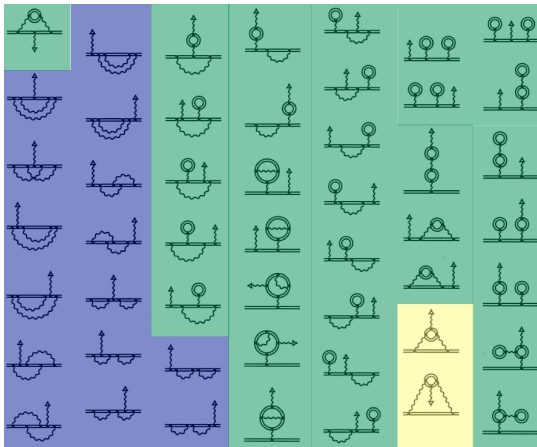
Diagrams with 0&1 self-energy loops
→ Treated in

[V.A. Yerokhin, Z. Harman, Phys. Rev. A
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(with **free VP** (e^-e^+) loops)

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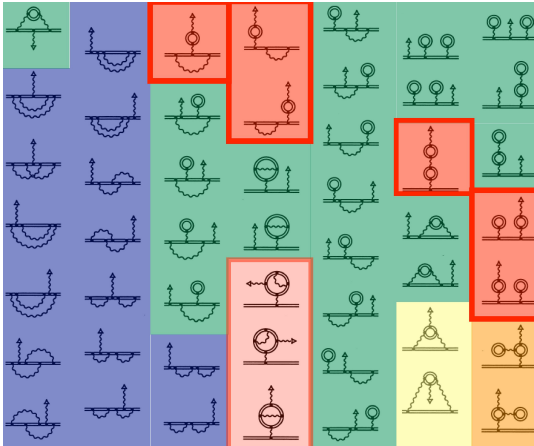
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Diagrams with 2 self-energy loops
→ Calculation in progress

[B. Sikora, Ph.D. thesis,
Ruprecht-Karls-Universität Heidelberg
(2018)]

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This work: revisit **diagrams that vanished in the free VP loop approach** & calculate lowest nonvanishing contribution