

Towards high-precision spectroscopy of sympathetically cooled H₂⁺

Julian Schmidt¹, Thomas Louvradoux¹, Mohammad Haidar¹, Johannes Heinrich¹, Jean-Philippe Karr^{1,2}, Laurent Hilico^{1,2}

¹Laboratoire Kastler Brossel, Sorbonne Université, ENS, CNRS ; 4 place Jussieu, Case 74, 75005 Paris, France

²Département de Physique, Univ EVRY Université Paris Saclay, rue du père André Jarlan 91025 Evry, France

Motivations

- High-resolution spectroscopy of rovibrational transitions in H₂⁺ or HD⁺ allows for precise tests of molecular QED and determination of m_p/m_e at the ~0.01 ppb level and shed light on the proton radius puzzle

$$v = cR_{\infty} \left[E_{nr}(\mu_{pe}) + A_{QED}(\alpha) + A^{fs} \left(\frac{r_p}{a_0} \right)^2 \right] \quad \text{and} \quad E_{nr} \propto 1/\sqrt{\mu_{pe}}$$

Comparison of H₂⁺ and HD⁺

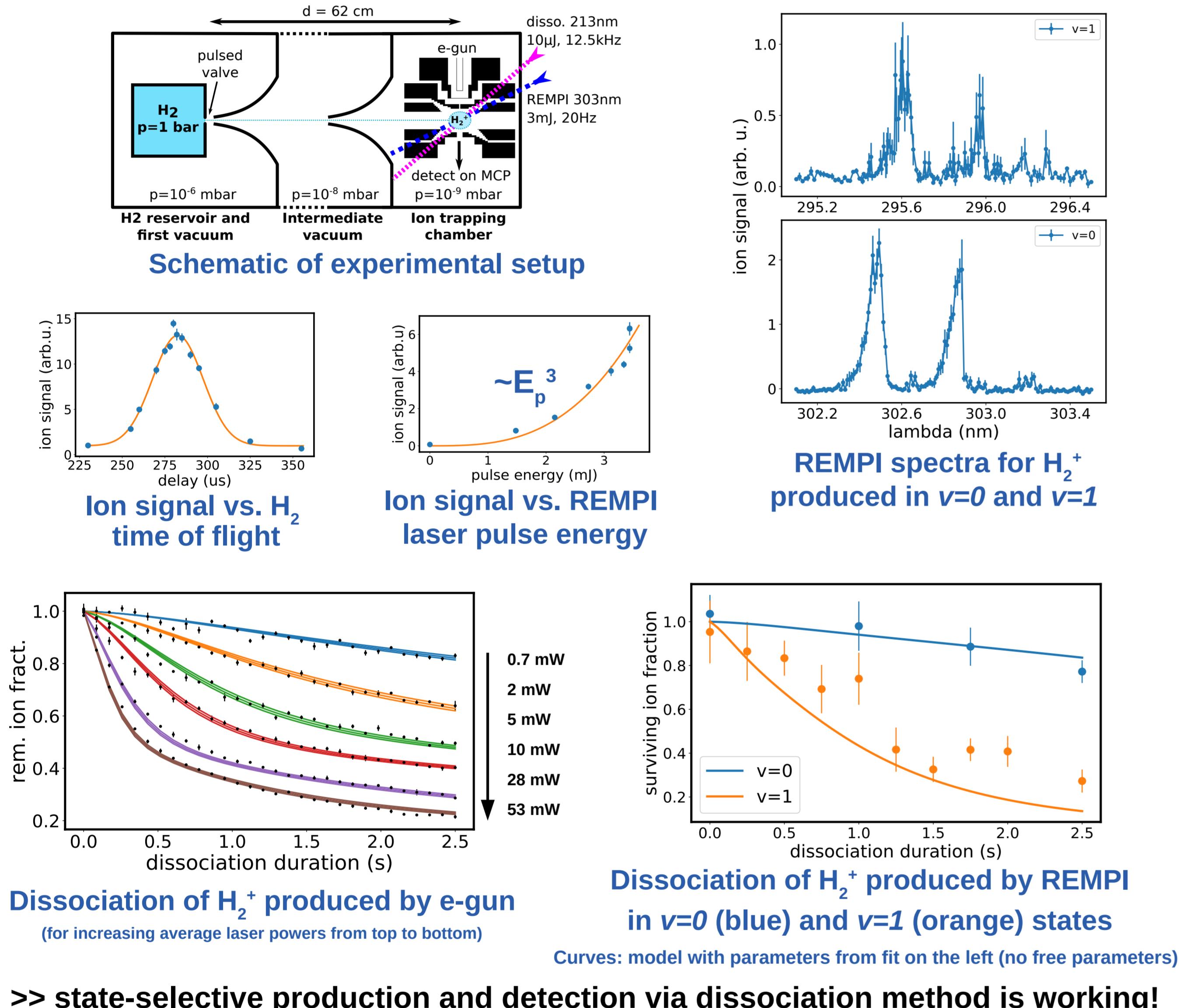
	H ₂ ⁺	HD ⁺
Line width	10 ⁻⁷ Hz	~ 10 Hz
Interesting for	m _p /m _e	μ/m _e ($\mu = m_d m_p / (m_d + m_p)$)
Transition	v=1 v=0 Weak two-photon 2E1 transition	v=9 v=4 Strong two-photon / Rotational one-photon transition
Systematic effects	Light shift 5 × 10 ⁻¹⁶	

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S. Schiller et al., Phys. Rev. Lett. **113**, 023004 (2014)
J.-Ph. Karr et al., Phys. Rev. A **94**, 050501 (2016)
J. Biesheuvel et al., Nat. Comm. **7**, 10385 (2016)
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S. Alighanbari et al., Nat. Phys. **14**, 555 (2018)

HD+ two-photon spectroscopy in the Lamb-Dicke regime
Hydrogen molecular ion clocks
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Hydrogen molecular ions and fundamental constants
HD+ v=0..v=8 transition frequency measurement
H₂⁺ and HD⁺ ionisation energies and trans. frequencies
HD+ rotational spectroscopy in the Lamb-Dicke regime

State-selective production of H₂⁺ molecular ions

Experimental results from hyperbolic trap setup (see "Experimental setups")

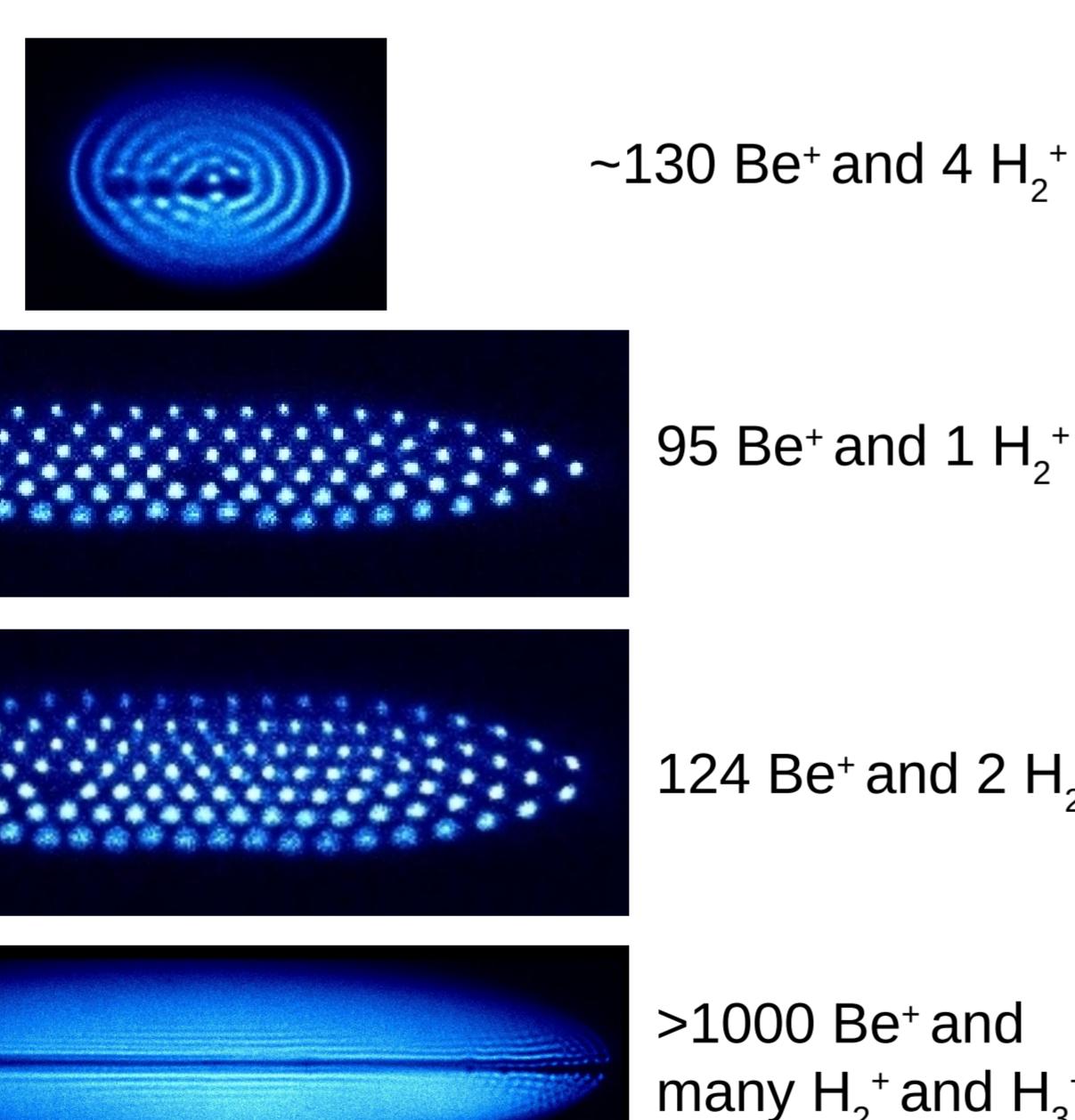
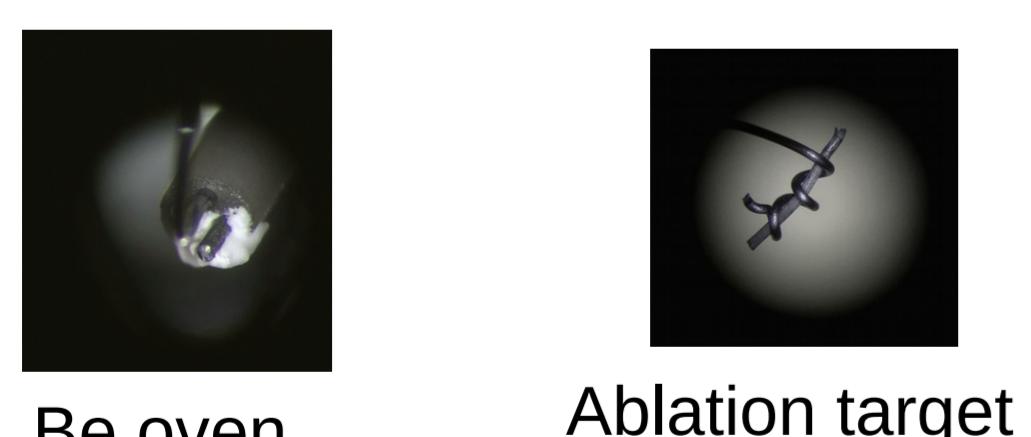


First Be⁺ ion clouds

With H₂⁺ ions from background gas

Beryllium ion loading

- with e-gun or non-resonant photo-ionization with 213 nm laser
- from oven (resistive heating) or ablation (532 nm pulsed laser)



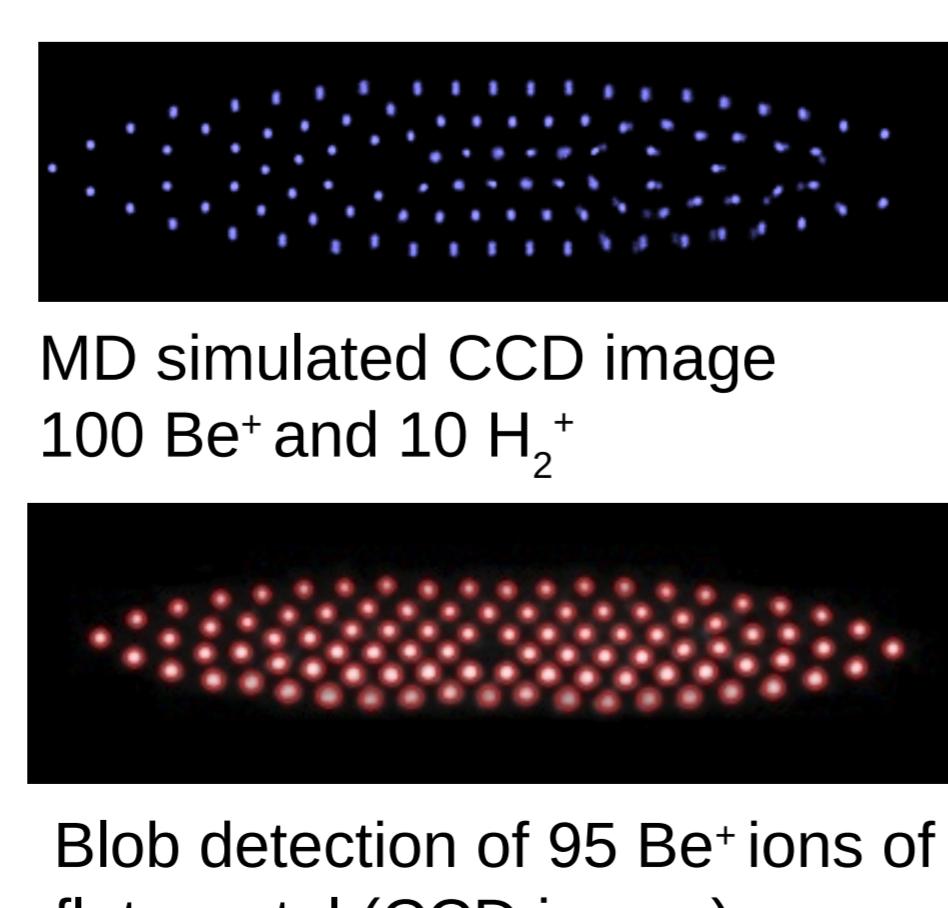
Comparison of ion crystal images with simulations

For given CCD image, what is the number of Be⁺, H₂⁺, H₃⁺ ions?

- Compare with molecular dynamics simulations
- Tickle curve (fluorescence signal depends on H₂⁺ number)

Count Be⁺ ions (blobs) with image analysis, then identify H₂⁺ dark ions ("empty sites") in

- CCD image:
 - by estimating the surface
 - with pattern recognition



Theory: Transition frequencies from (v = 0, L=2) → (v'=1, L'=2) in H₂⁺

ν_{nr}	65 412 414 314.5
ν_{α^2}	1 077 263.8
ν_{α^3}	-274 145.4
ν_{α^4}	-1 935.5(1)
ν_{α^5}	120.8(1)
ν_{α^6}	-2.3(5)
ν_{tot}	65 413 215 616.1(5)

Contributions to uncertainty:

(5) theory m_p/m_e r_p/Ry

CODATA 2018

• Hyperfine and QED corrections

• Combine H, D, H₂⁺, HD⁺ spectroscopy data to determine m_p/m_e, μ/m_e, Ry, r_p, r_d

Experimental method

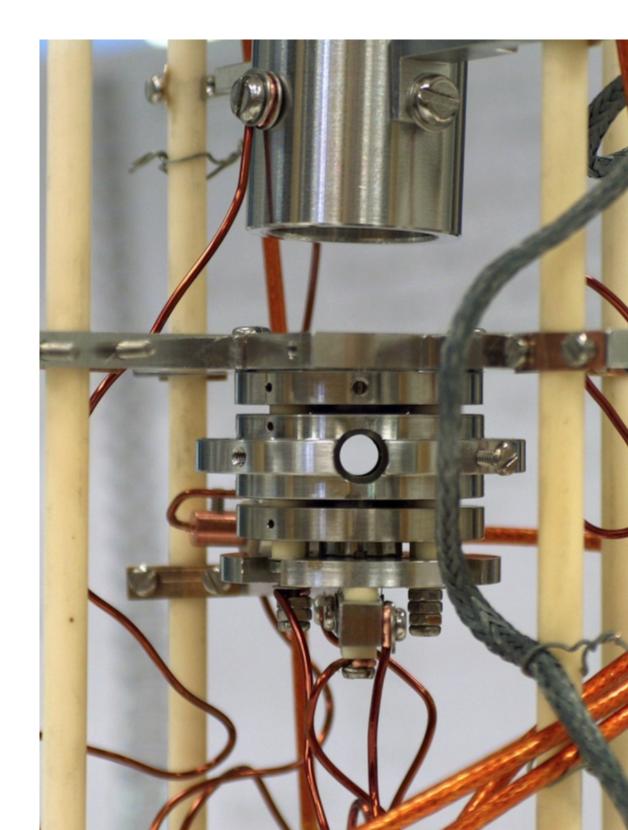
Step 1: State-selective production of cold H₂⁺ molecular ions

- Molecular beam injects H₂ molecules into ion trap
- (3+1) Resonant multiphoton ionization (REMPI) using a pulsed laser at 303 nm at the center of an ion trap
- H₂⁺ is sympathetically cooled by laser cooled Be⁺ ions

Step 2: REMPD spectroscopy

- Drive 2-photon transition from v=0, L=2 → v=1, L=2 with cavity-enhanced mid-IR spectroscopy laser (9.17 μm)
- H₂⁺ ions excited to the v=1 state are dissociated by 213 nm laser and lost from the trap
- Count number of H₂⁺ ions before and after spectroscopy and dissociation

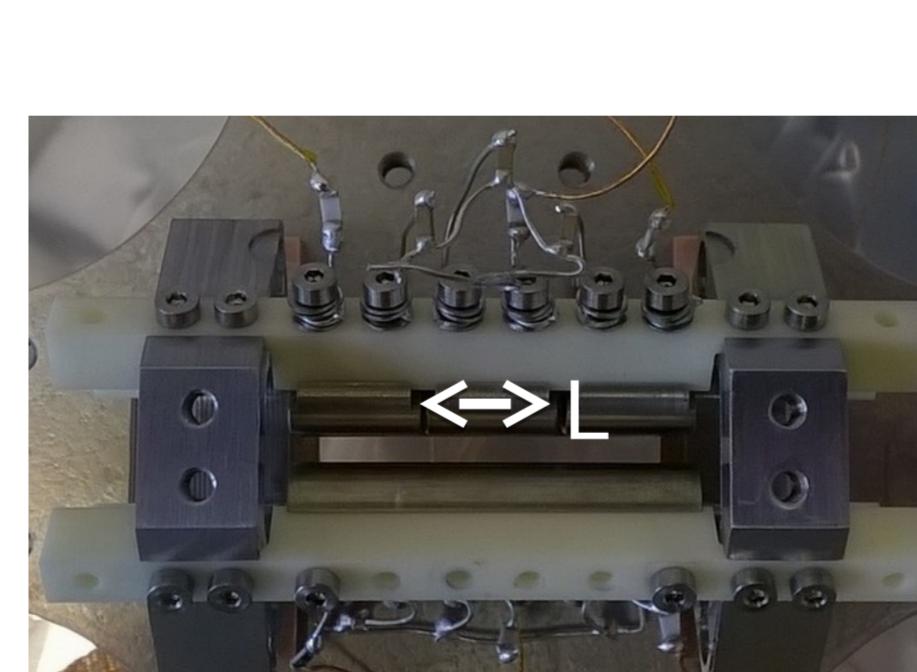
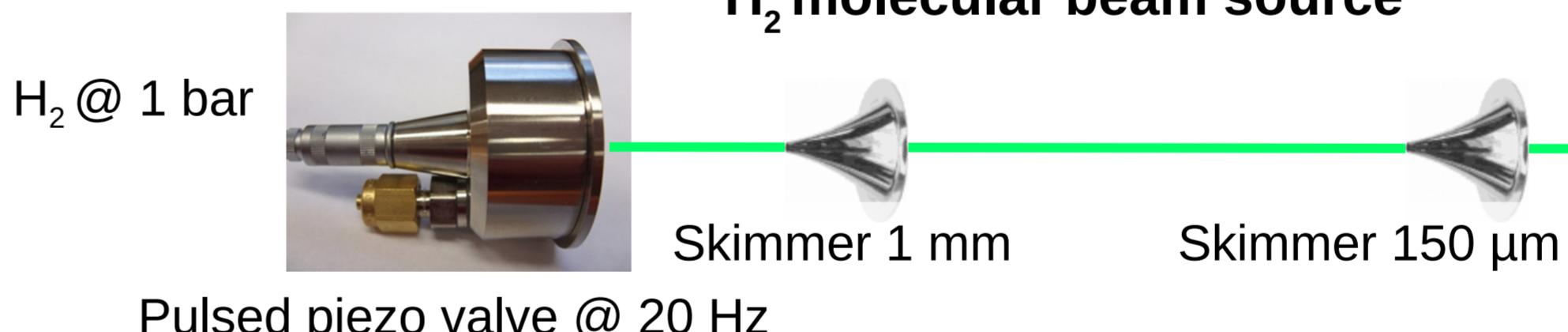
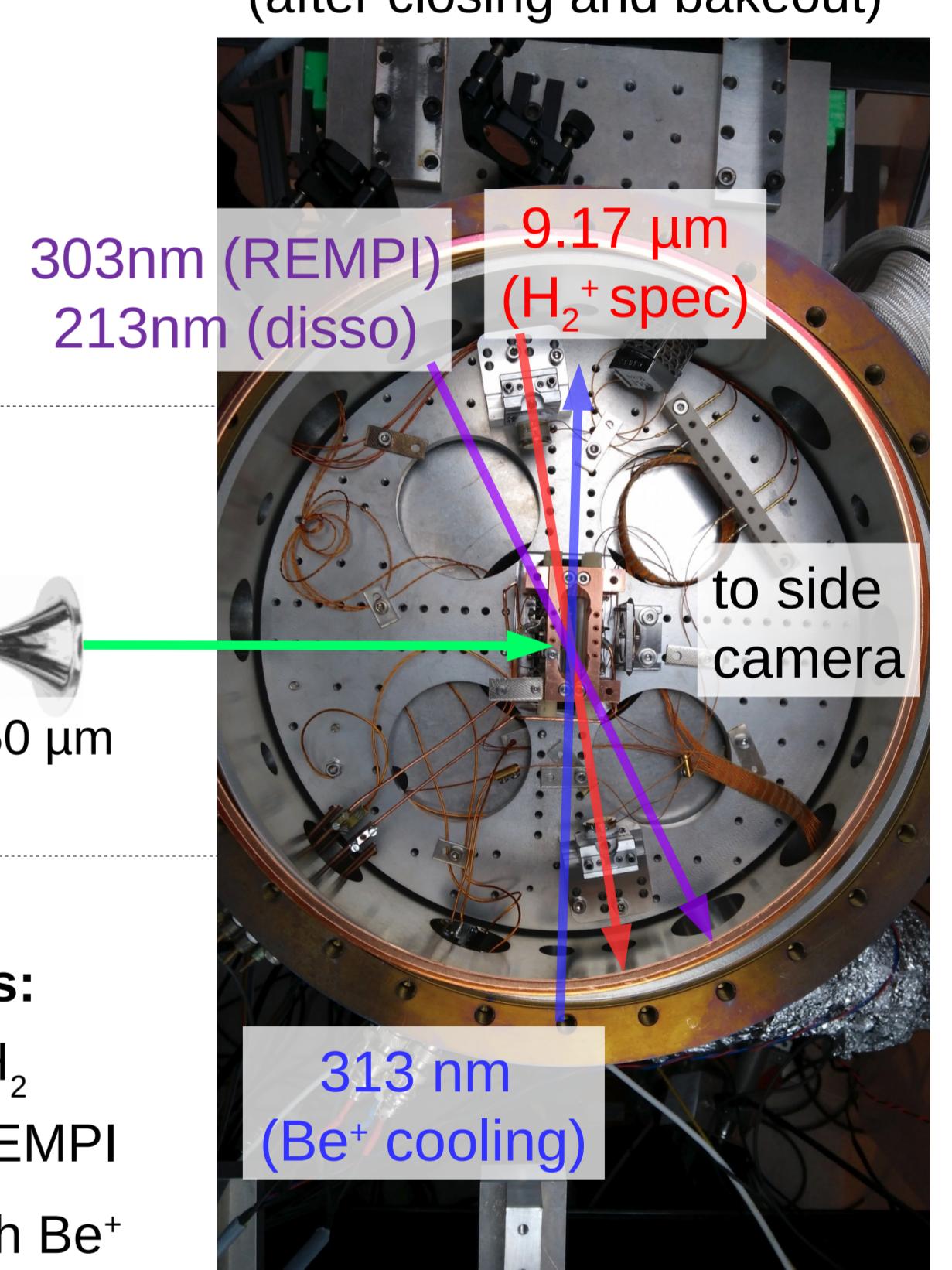
Experimental setups



Hyperbolic trap features:

- In situ ionisation of H₂ by electron impact or REMPI
- Detection: high voltage extraction to MCP
- Trap properties:
 $R_0 = 4.2$ mm, $Z_0 = 3$ mm
 $\Omega = 2\pi \times 14$ MHz, $U_{rf} = 150$ V

UHV chamber with linear trap @ 10⁻¹⁰ mBar (after closing and bakeout)



Linear trap features:

- In situ ionisation of H₂ by electron impact or REMPI
- Sympathetic cooling with Be⁺
- Detection: imaging of mixed Coulomb crystals (Be⁺ + H₂⁺)
- Trap properties:
 $R_0 = 3.5$ mm, $L = 12$ mm,
 $\Omega = 2\pi \times 13$ MHz, $U_{rf} = 500$ V

Conclusions and outlook

- Theory: m_p/m_e can be obtained from hydrogen molecular ion spectroscopy with 15 ppt accuracy

- Ion trap ready

- Micromotion minimisation by fluorescence/RF correlations

- H₂⁺ spectroscopy enhancement cavity implemented

- Addition of the H₂⁺ source to the linear trap setup

- Find best method to measure a fractional loss of H₂⁺

- State selected H₂⁺ ion creation inside the laser cooled Be⁺ ion cloud

- Search for H₂⁺ two-photon signal