

The ALPHATRAP g -factor experiment

α
TRAP

International Conference on Precision
Physics and Fundamental Physical
Constants FFK 2019

11.06.2019

Alexander Egl

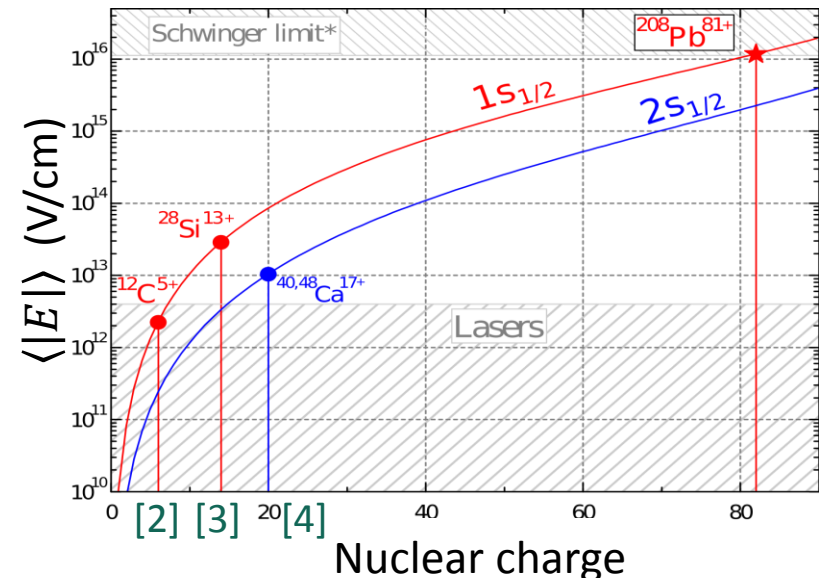
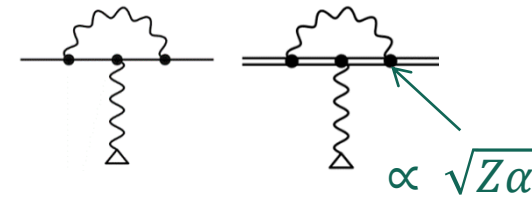


Quantum Electrodynamics (QED) In Strong Fields

- QED describes interaction of light/photons and charged particles
- Impressive theory predictions and most precise experimental results, e.g. electron magnetic moments: $g-2$, g -factor in highly charged ions (HCI) [1]
 - Most stringently tested theory in weak fields

- Validity of QED in strong fields?
 - Test of bound state QED (BS-QED) under extreme conditions in high electric and magnetic fields of heavy HCI
 - g -factor measurements in H or Li-like systems
 - Fine structure and hyperfine structure spectroscopy

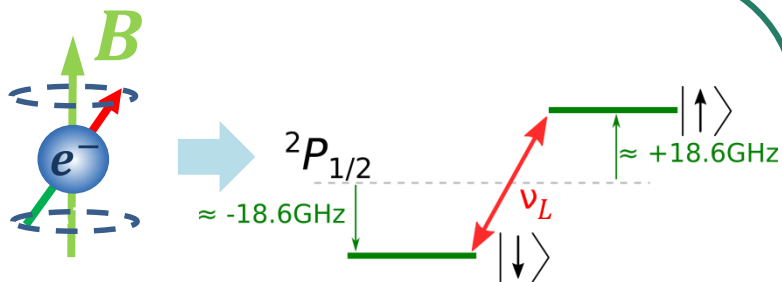
→ Combine strongest field and highest precision



[1] H. Häffner, et al., Phys. Rev. Lett. 85, 5308 (2000)
 J.Verdu, et al., Phys. Rev. Lett. 92, 093002 (2004)
 [2] S. Sturm, et al., Nature 506, 7489 (2014)
 [3] S. Sturm, et al., Phys. Rev. Lett. 107, 023002 (2011)
 [4] F. Köhler, et al. Nat. Comm. 7, 10246 (2016)

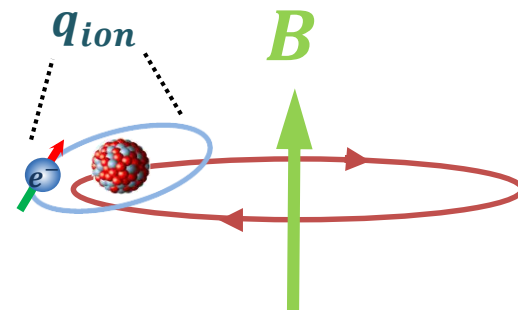


Measurement principle



$$\nu_L = \frac{g}{4\pi} \frac{e}{m_e} B$$

Measure the Larmor frequency
in a well-known magnetic field



$$\nu_c = \frac{1}{2\pi} \frac{q_{ion}}{m_{ion}} B$$

Measure the free cyclotron frequency
to determine magnetic field

$$g = 2 \frac{\nu_L}{\nu_c} \frac{q_{ion}}{m_{ion}} \frac{m_e}{e}$$

to be measured $\Gamma = \nu_L/\nu_c$

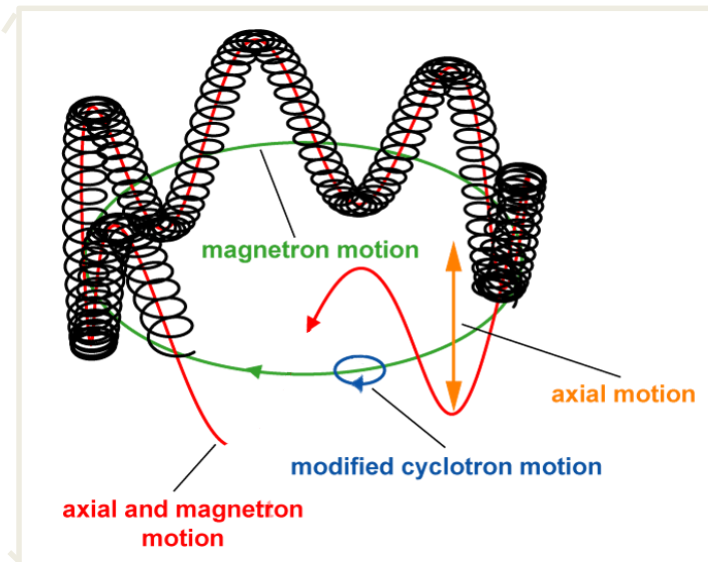
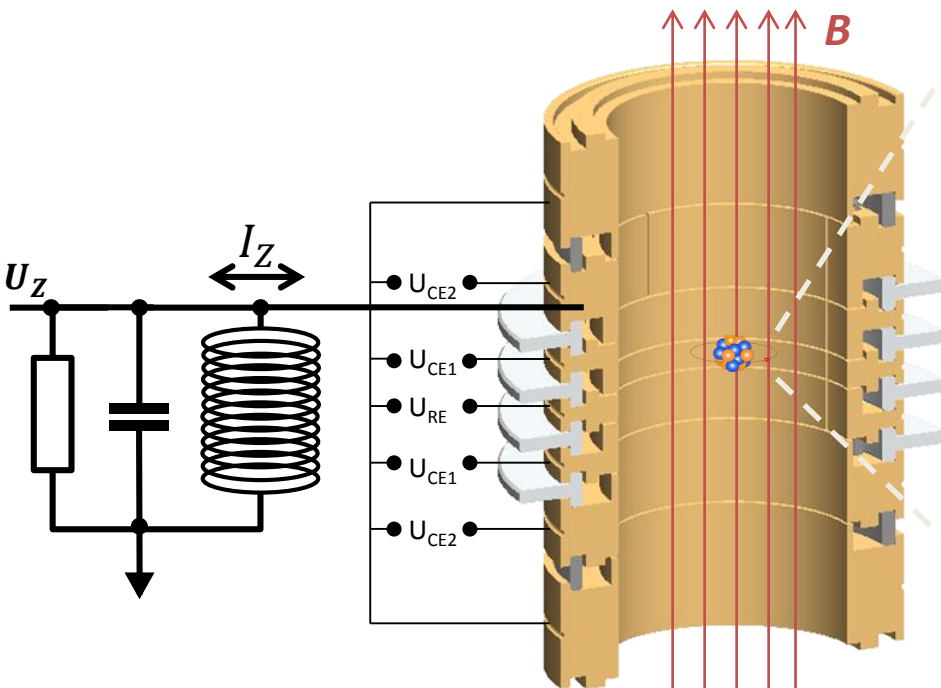
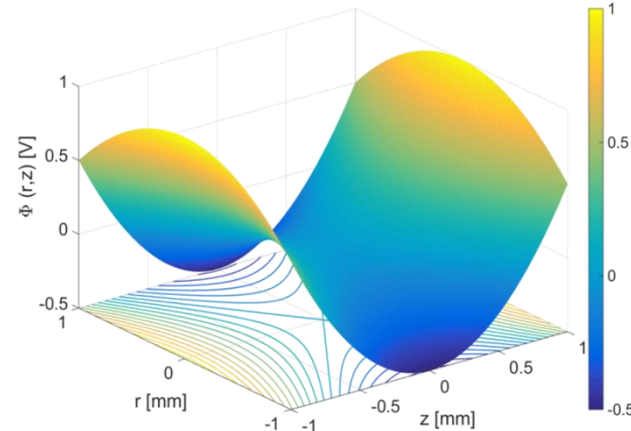
Independent precision experiments

Penning Trap - Principle

Experimental Conditions:

- Single, cold ion
- Homogeneous magnetic field: $\sim 4\text{T}$
- Cryogenic temperature: $\sim 4.2\text{ K}$
- Extremely high vacuum: $\leq 10^{-17}\text{ mbar}$
- Long storage times: \sim months

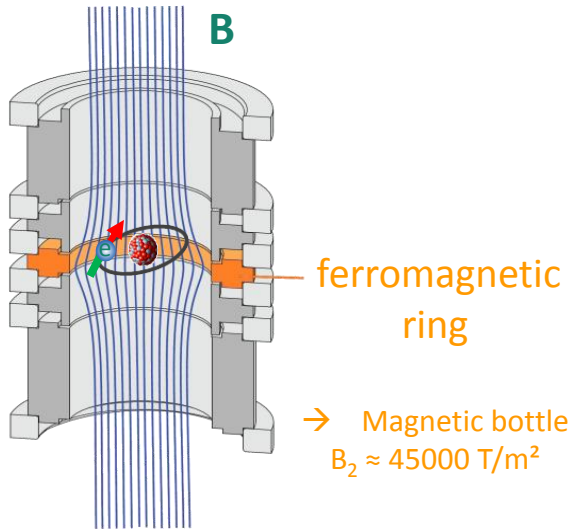
$$\Gamma = \frac{v_L}{v_c}$$



$$v_c = \frac{1}{2\pi} \frac{q_{ion}}{m_{ion}} B = \sqrt{v_z^2 + v_+^2 + v_-^2}$$

Spin state detection- Continuous Stern Gerlach Effect

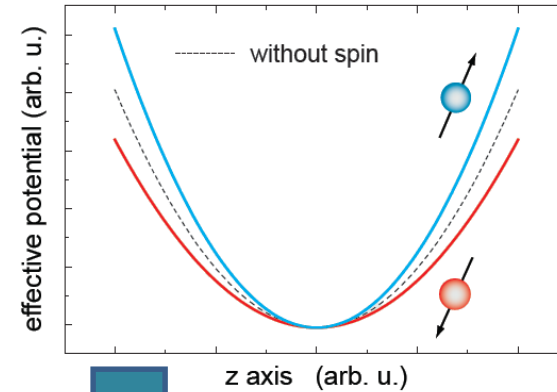
Introducing magnetic bottle inhomogeneity



$$\Gamma = v_L / v_C$$

additional potential:

$$\Phi_z^{\text{mag}} = \pm \mu_z \left[B_0 + B_2 \left(z^2 - \frac{\rho^2}{2} \right) \right]$$

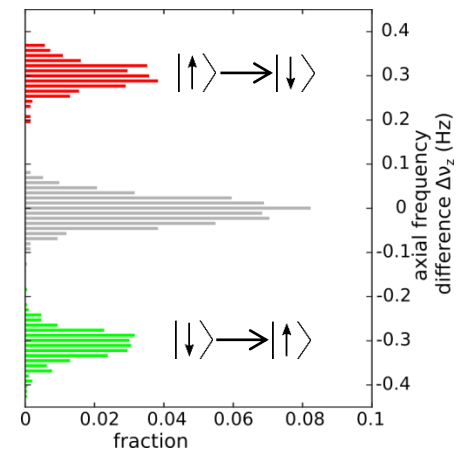
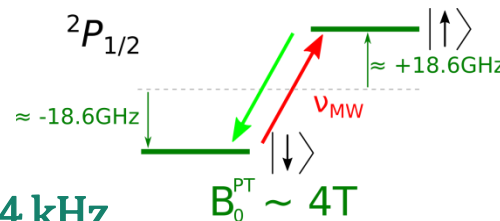


Continuous Stern-Gerlach effect:

axial frequency offset between “up” and “down” spin orientation

$$\Delta \nu_z \approx \frac{B_2 g \mu_B}{4\pi^2 m_{ion} \nu_z}$$

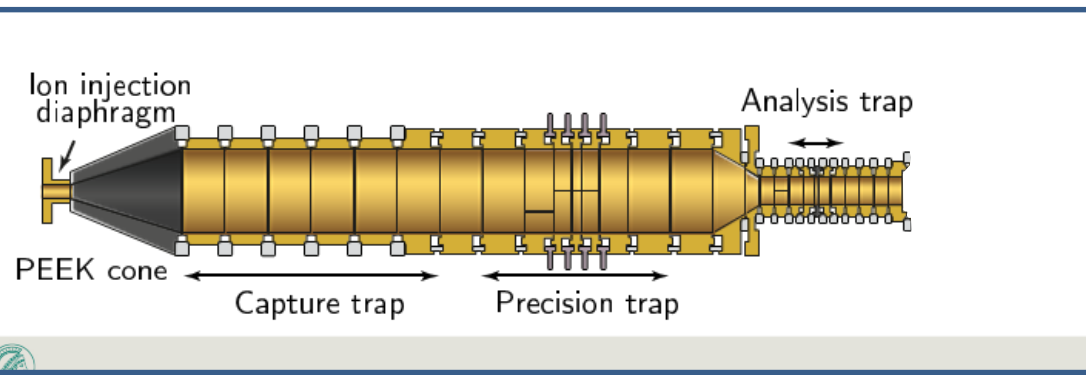
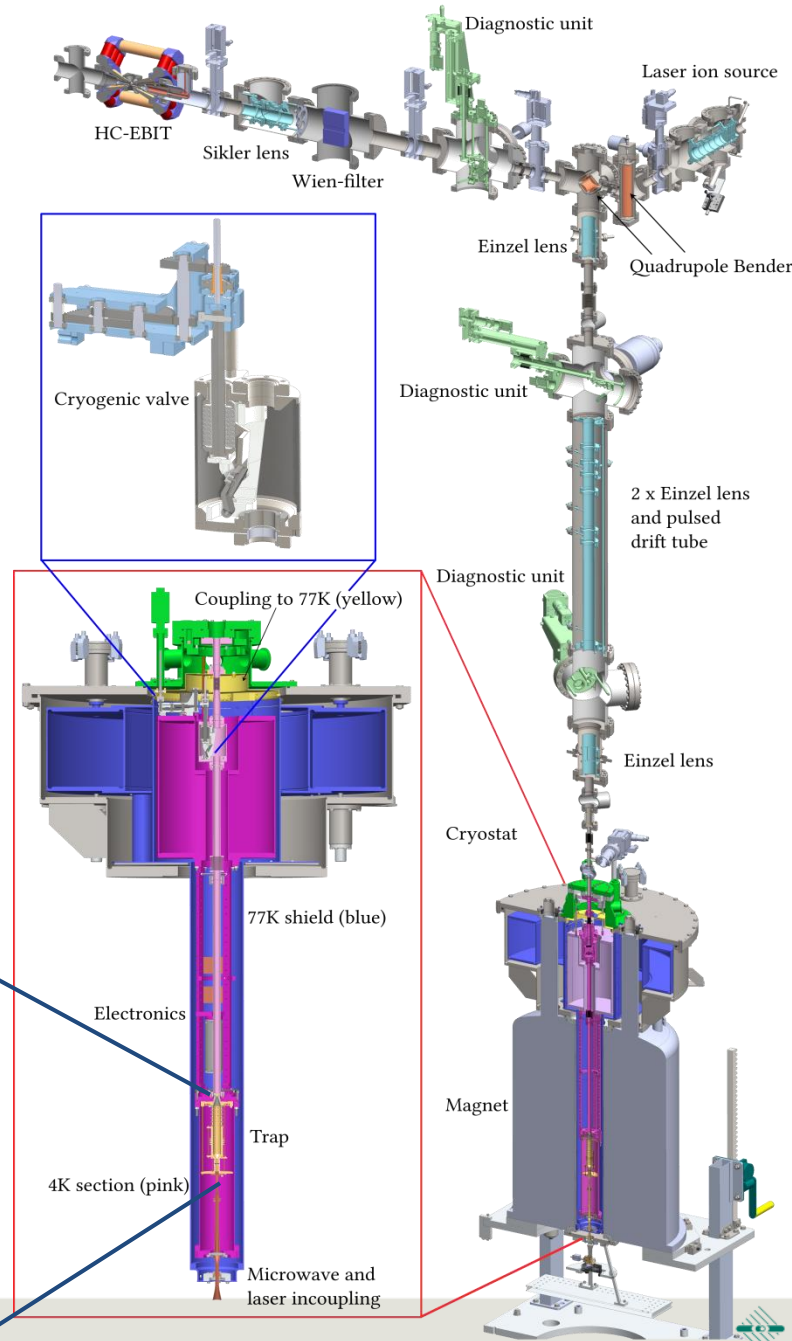
@ $\nu_z \approx 334 \text{ kHz}$



	$^{12}\text{C}^{5+}$	$^{28}\text{Si}^{13+}$	$^{40}\text{Ar}^{13+}$	$^{208}\text{Pb}^{81+}$
$\Delta \nu_z$	3.1 Hz	1.3 Hz	312 mHz	156 mHz

The ALPHATRAP setup

- Access to externally produced ions
 - Laser ion source (Be^+)
 - HC-EBIT
 - HD-EBIT (commissioning phase)
- Transport through room-temperature beamline into 4K section
- Separated by cryogenic valve



Double Trap System

20mm

Capture section

- dynamic ion capturing
- storage of ions (months)

Precision Trap (PT)

- homogeneous B

$$B_1 = 2.638(24) \text{ mT/m}$$

$$B_2 = 0.0643(32) \text{ T/m}^2$$

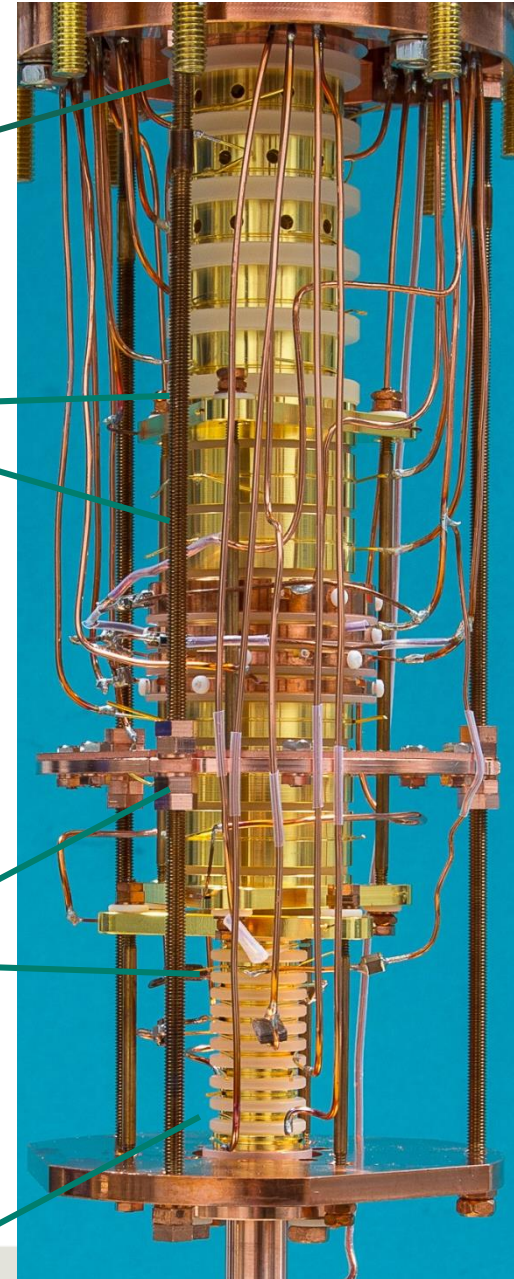
- measurement of ν_c
 - spin flips induction ν_L
- $$\left. \begin{array}{l} \nu_L \\ \nu_c \end{array} \right\} \frac{\nu_L}{\nu_c} = \Gamma$$

- Laser spectroscopy

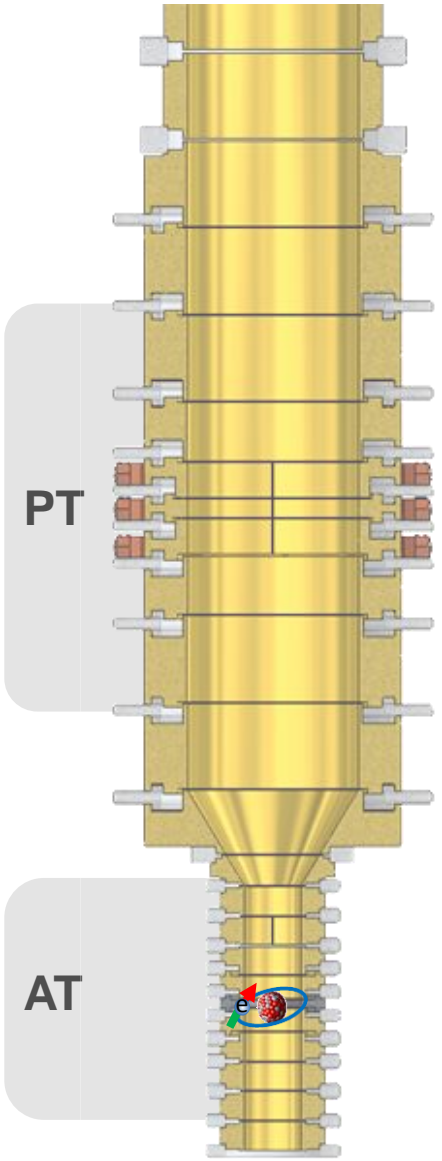
Analysis Trap (AT)

- strong B_2 (44 kT/m^2)

- Spin state **detection** and **preparation**



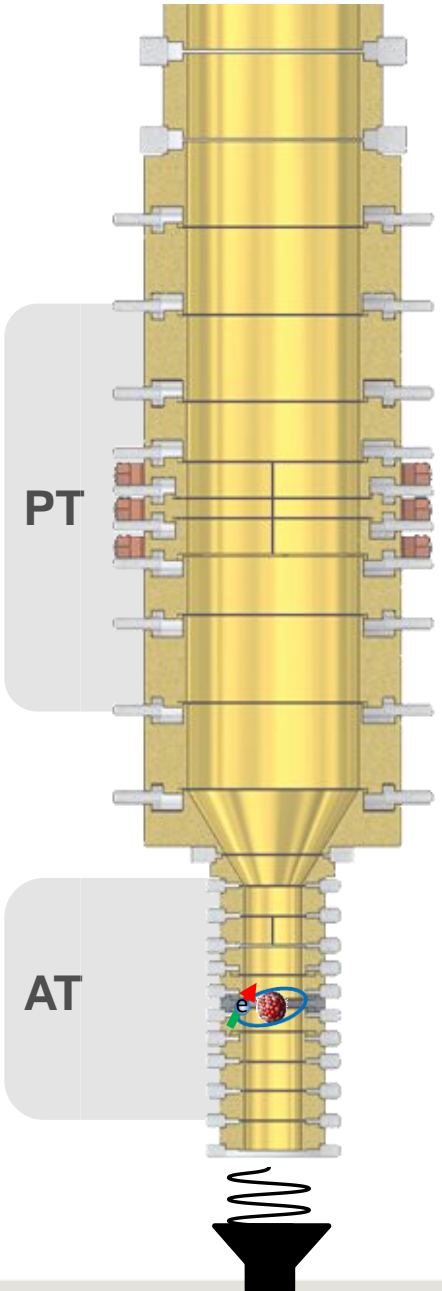
Measurement cycle



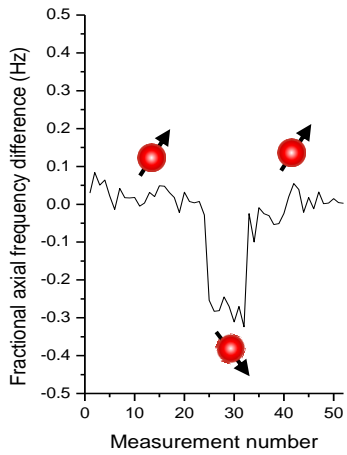
microwave
horn



Measurement cycle

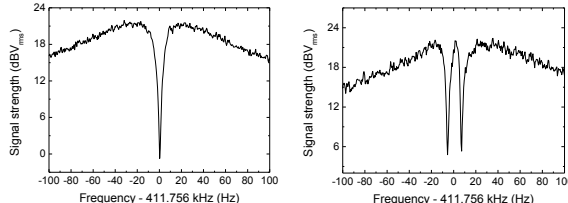


AT: Detection and preparation of spin orientation



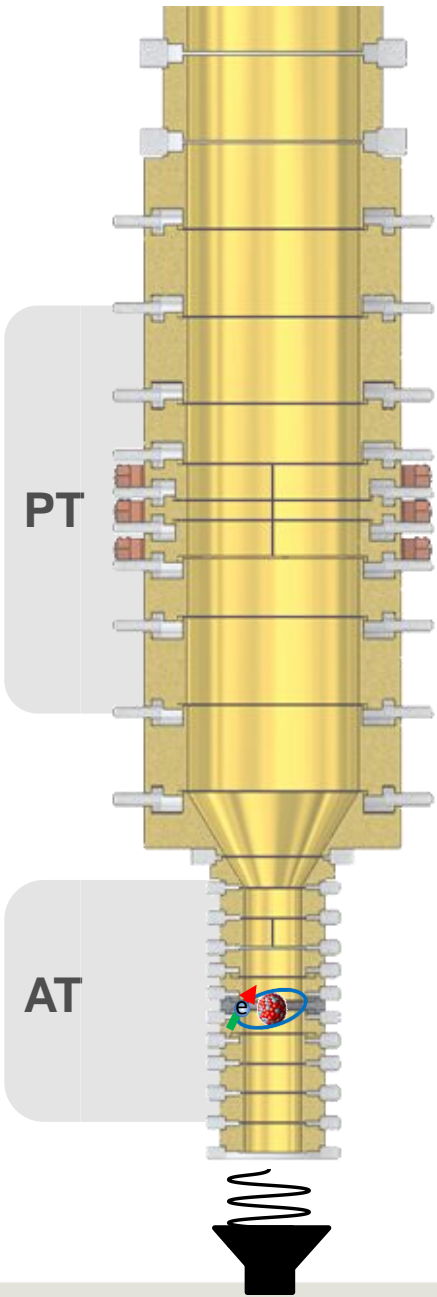
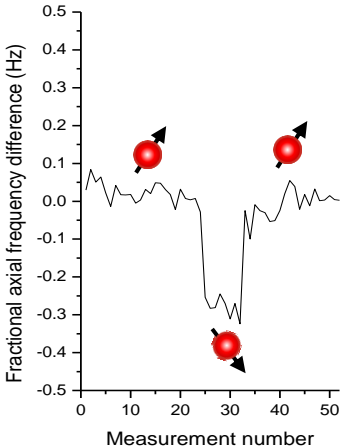
Measurement cycle

PT: Measurement of motional frequencies and probe with spectroscopy frequency



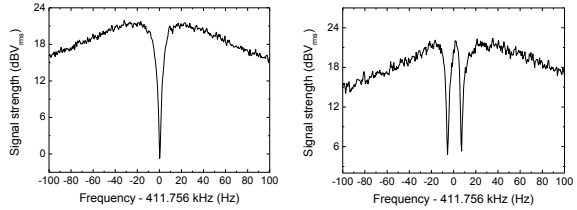
$$v_Z^2 + v_+^2 + v_-^2 = v_C^2$$

AT: Detection and preparation of spin orientation



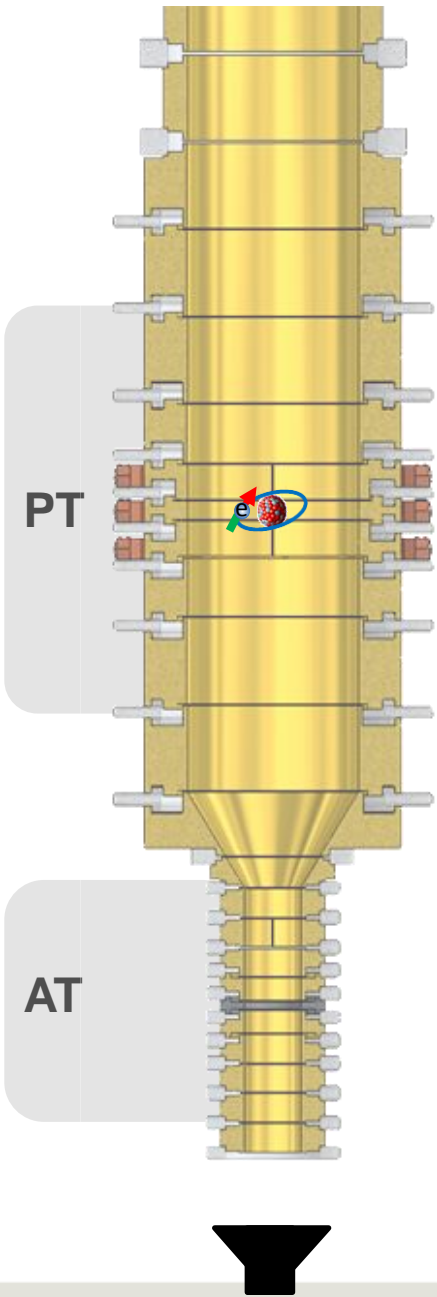
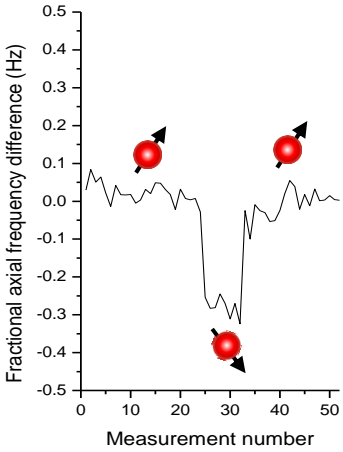
Measurement cycle

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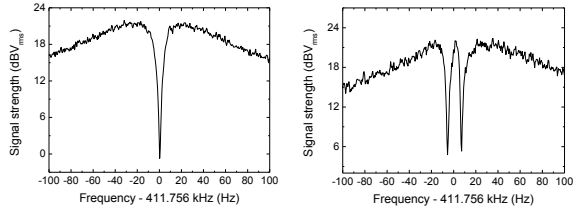
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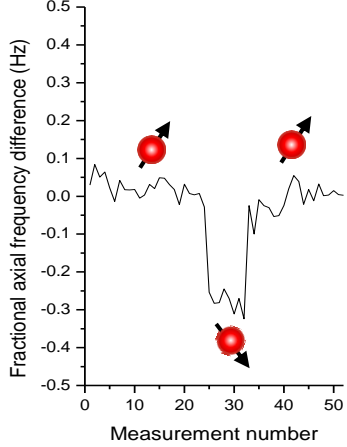
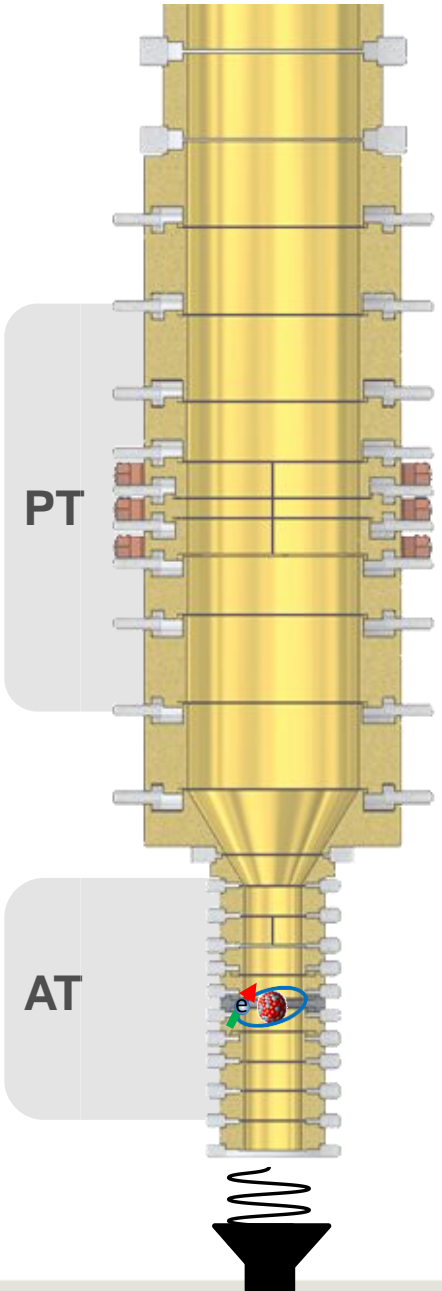
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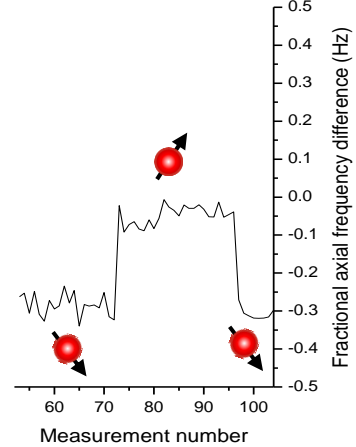


$$v_Z^2 + v_+^2 + v_-^2 = v_C^2$$

AT: Detection and preparation of spin orientation

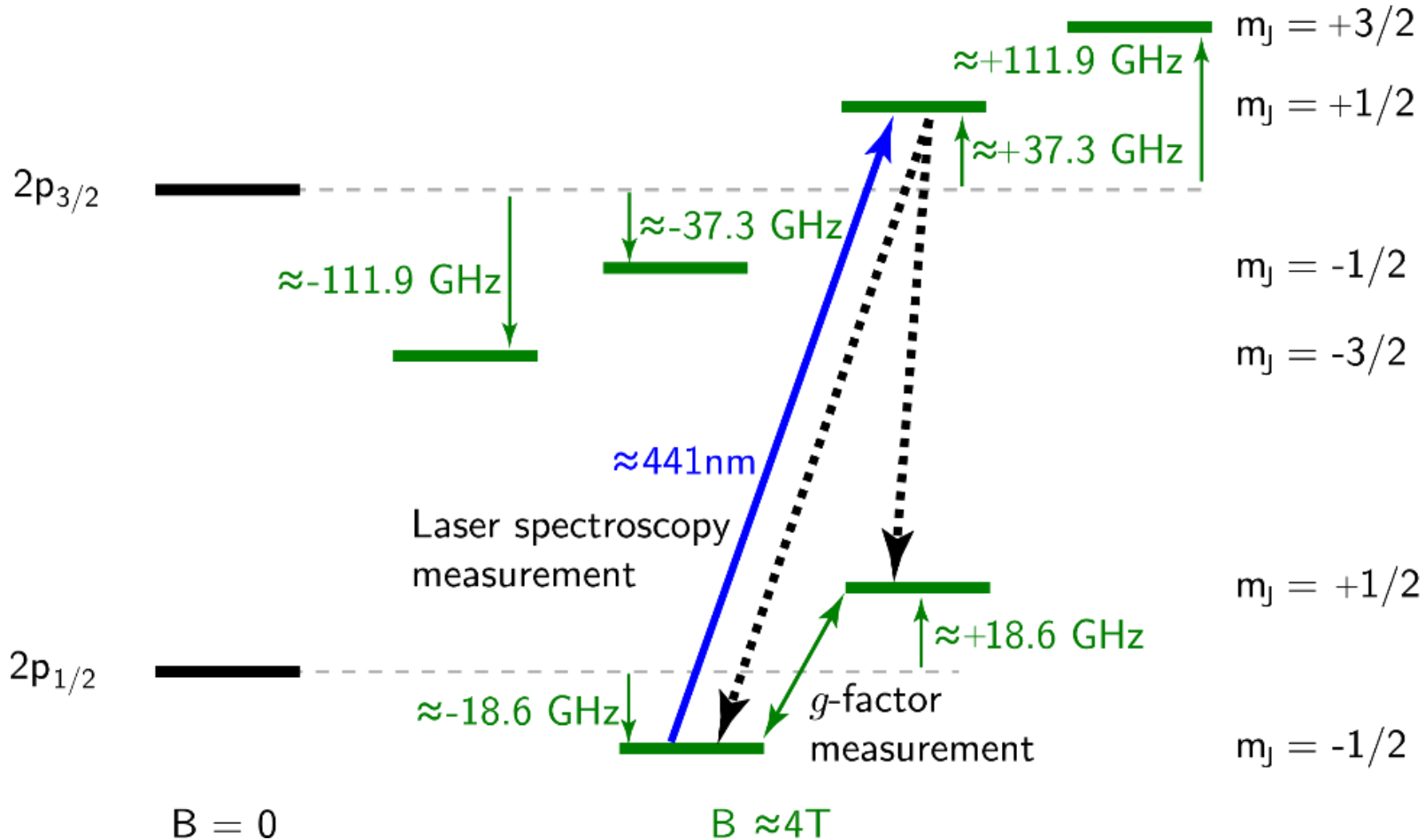


Compare
spin state



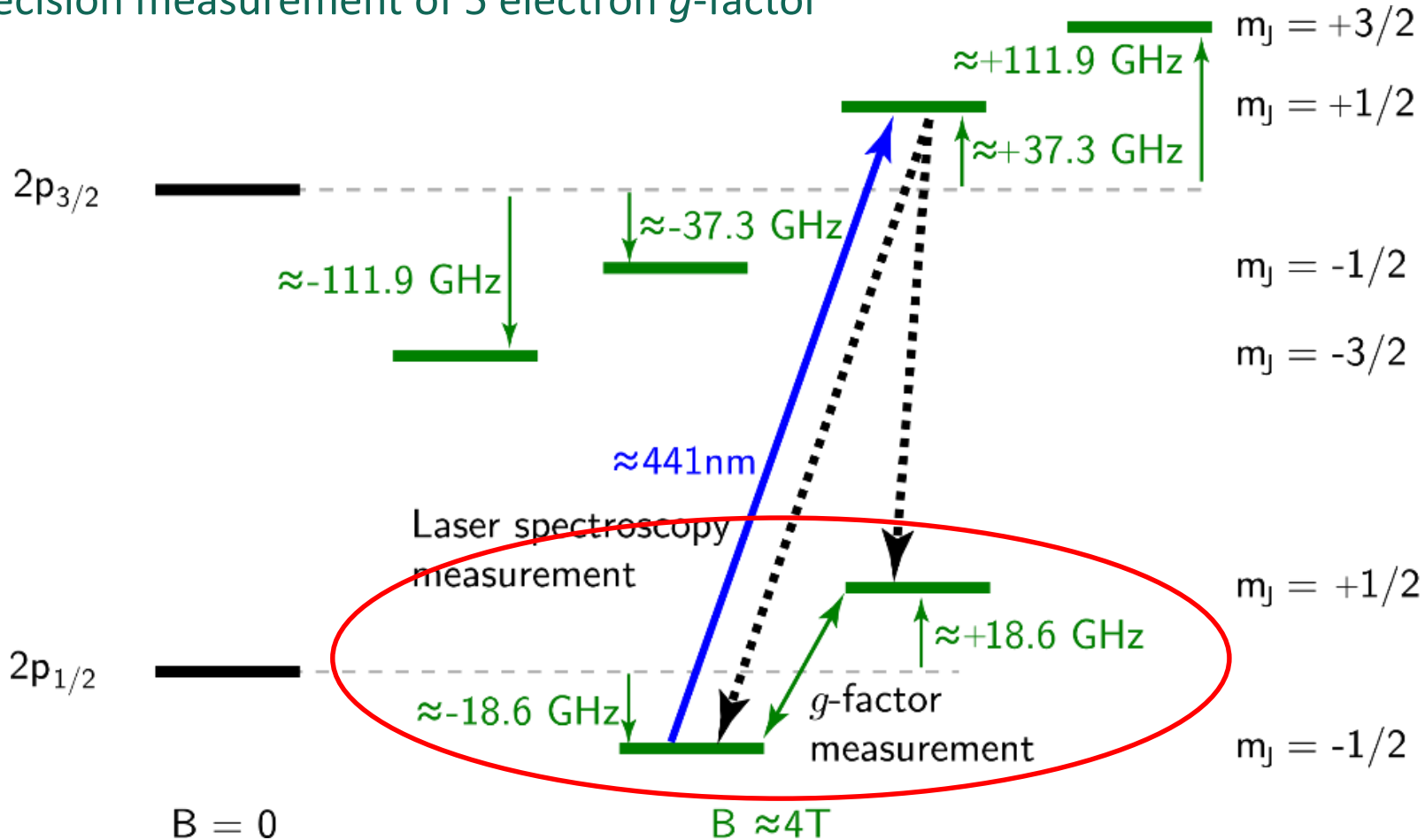
Measurements so far

$^{40}\text{Ar}^{13+}$ measurements

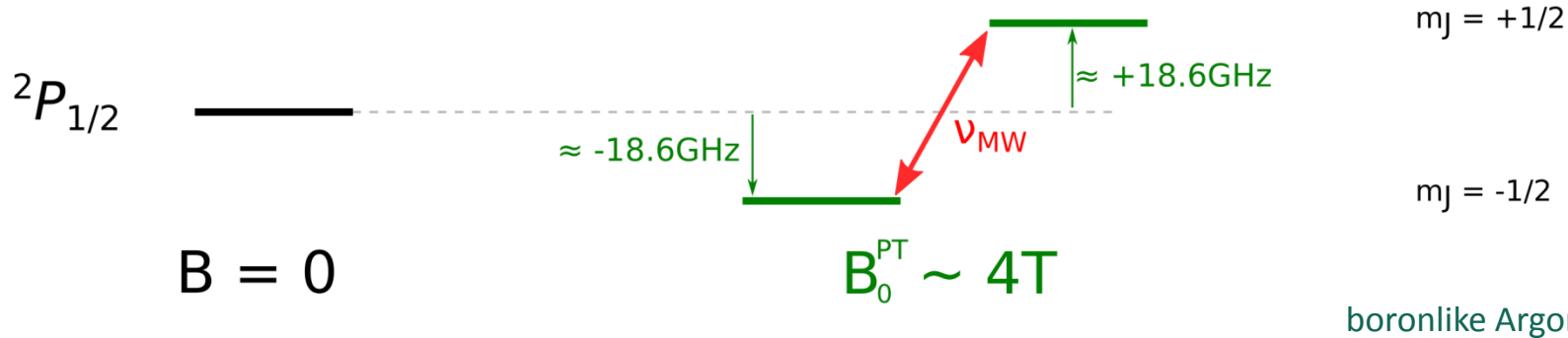


Measurements so far

$^{40}\text{Ar}^{13+}$ measurement of g -factor:
first high precision measurement of 5 electron g -factor



Measurement of the g -factor of $^{40}\text{Ar}^{13+}$ (preliminary results)



boronlike Argon: $g \approx 2/3$

- 3 different theoretical values:
- 120 σ deviation between first 2

J. P. Marques et al. [1]	0.663899(2)
Glazov/Agababaev et al. [2]	0.6636488(12)
Shchepetnov et al. [3]	0.6636477(7)
S. Verdebout et al. [4]	0.663728 (-)

- Measured 2 resonances

[1] Physical Review A 94, 042504 (2016)

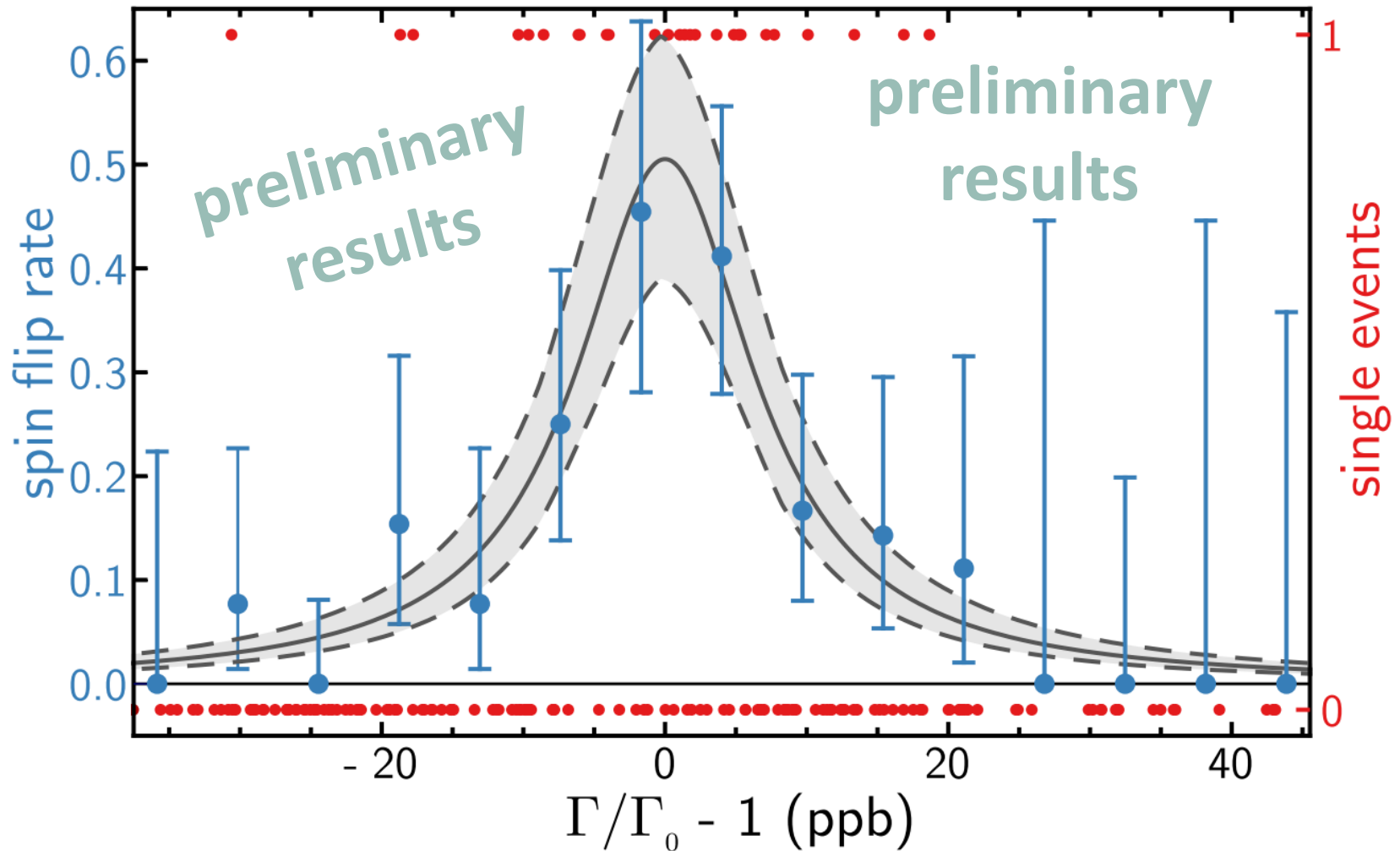
[2] HCI 2018 Conference Talk, Group of Volotka, Shabaev et al.

[3] J. Phys. Conf. Ser. 583 012001

[4] At. Data Nucl. Data Tables 100, 1111 (2014); no error given

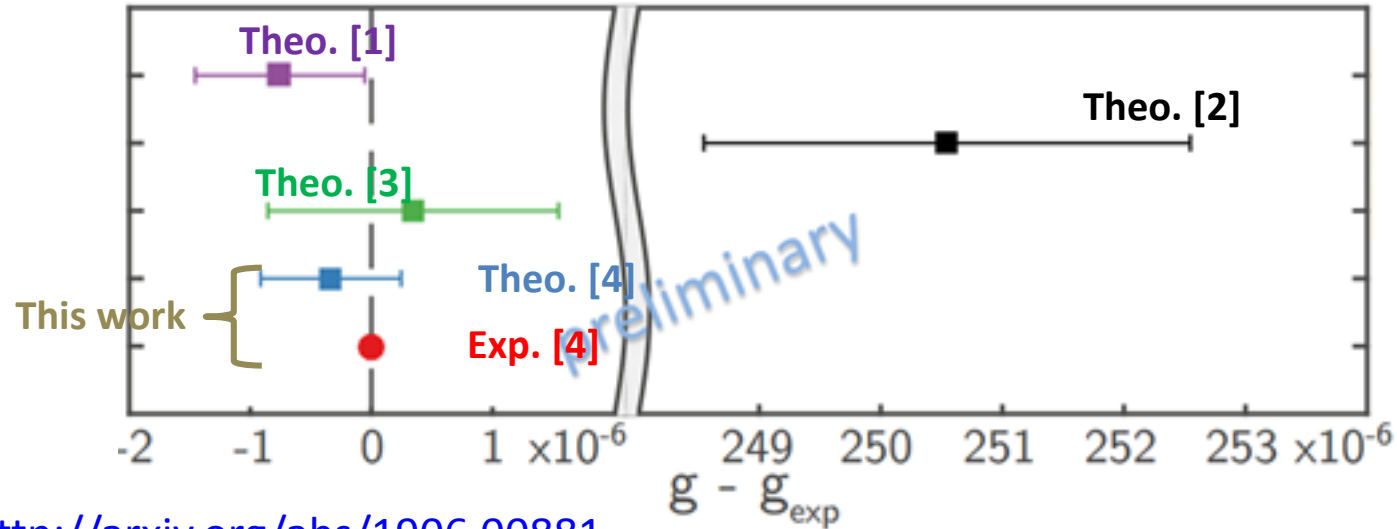
Measurement of the g -factor of $^{40}\text{Ar}^{13+}$

(preliminary results)



Gaussian fitted by maximum likelihood estimation (binned data only for representation)

Comparison with Current Theory



<http://arxiv.org/abs/1906.00881>

Shchepetnov <i>et al.</i> [1]	0.663 647 7(7)
J. P. Marques <i>et al.</i> [2]	0.663 899(2)
Glazov/Agababaev <i>et al.</i> [3]	0.663 648 8(12)

- A maximum of 120σ deviation comparing the existing theoretical predictions
- Our experimental result shows the agreement with the current theory at 10^{-7} level. (**Experiment precision at 10^{-9}**)

[1] A. A. Shchepetno *et al.*, *J. Phys. Conf. Ser.* 583 012001

[2] J. P. Marques *et al.*, *PHYSICAL REVIEW A* 94, 042504 (2016)

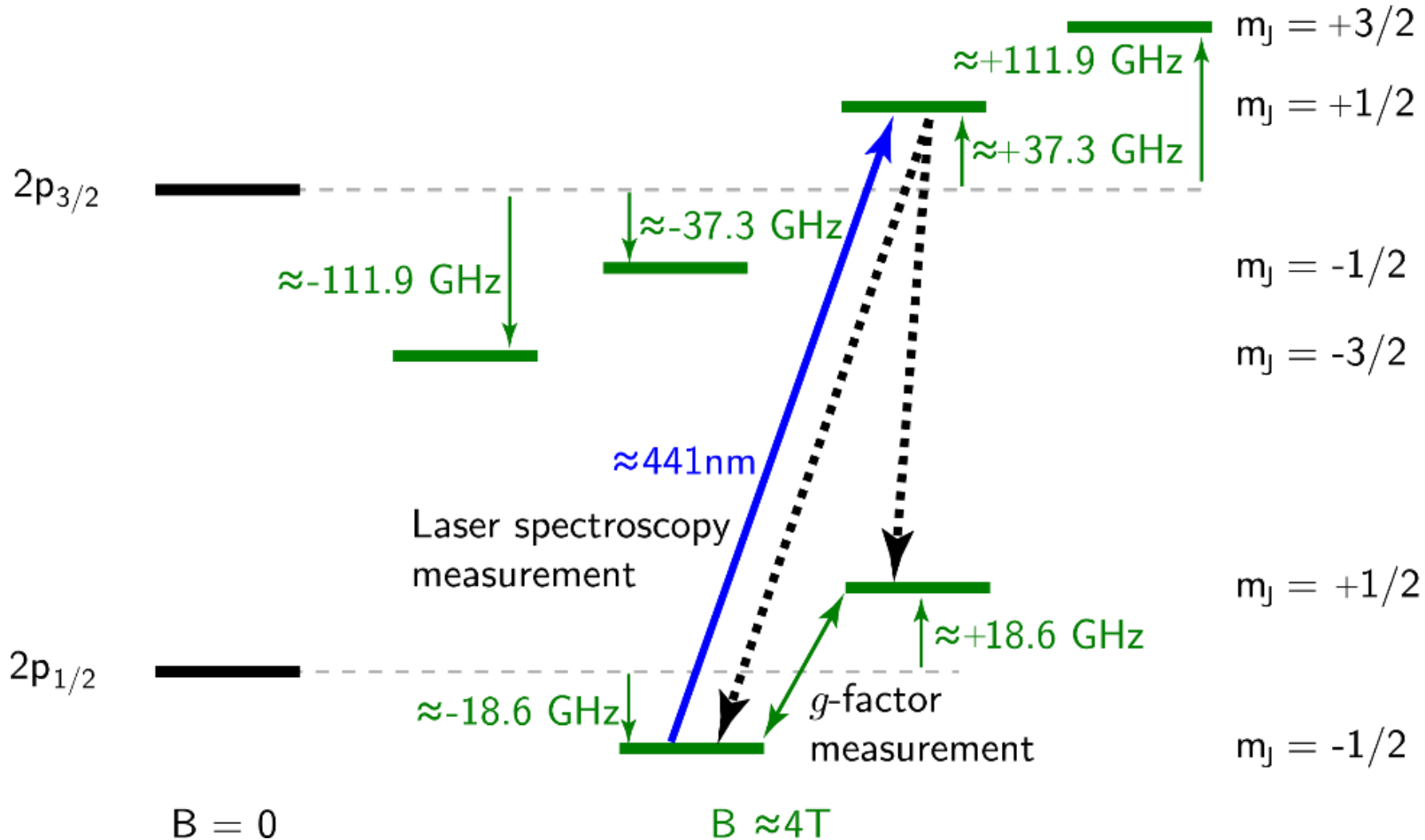
[3] V. A. Agababaev *et al.*, *HCI 2018 Conference Talk*, Group of Volotka, Shabaev *et al.*

[4] I. Arapoglou *et al.*, *Phy. Rev. Lett.* accepted, <http://arxiv.org/abs/1906.00881>



Measurements so far

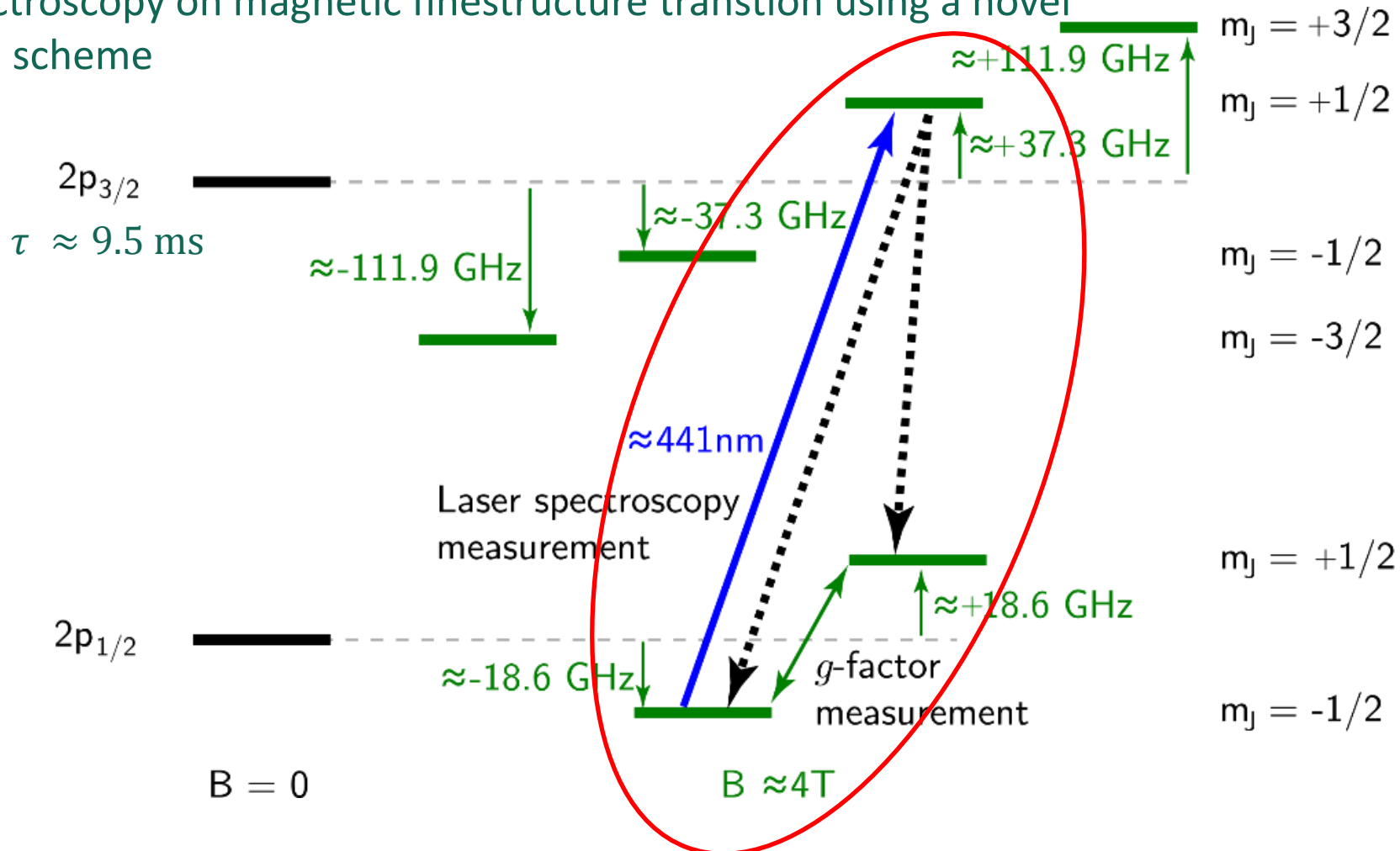
$^{40}\text{Ar}^{13+}$ measurements



Measurements so far

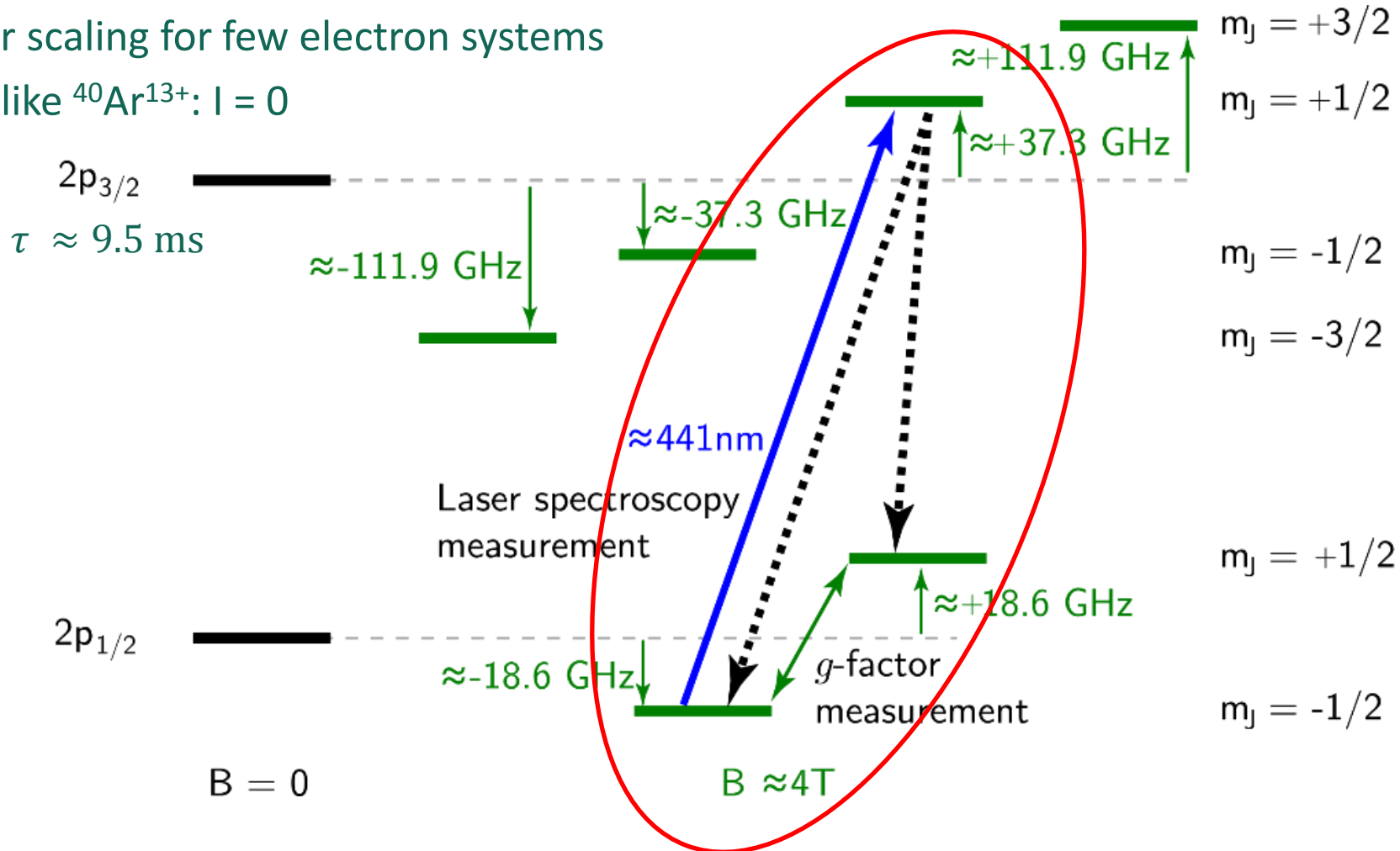
$^{40}\text{Ar}^{13+}$ measurement of finestructure transition:

laser spectroscopy on magnetic finestructure transition using a novel detection scheme



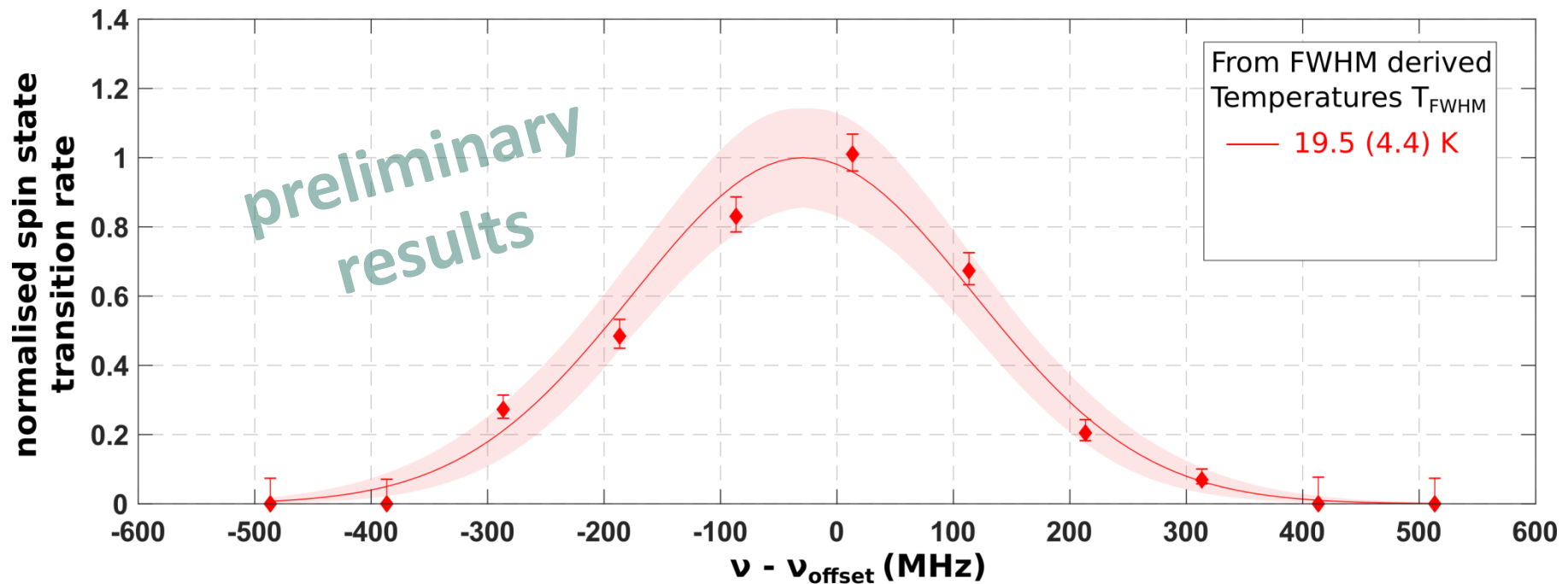
Measurements so far

- For hydrogenlike ions transition energy scaling:
 $\propto Z^2$ for principal, $\propto Z^3$ for HFS, $\propto Z^4$ for FS
- Similar scaling for few electron systems
- boronlike $^{40}\text{Ar}^{13+}$: $l = 0$



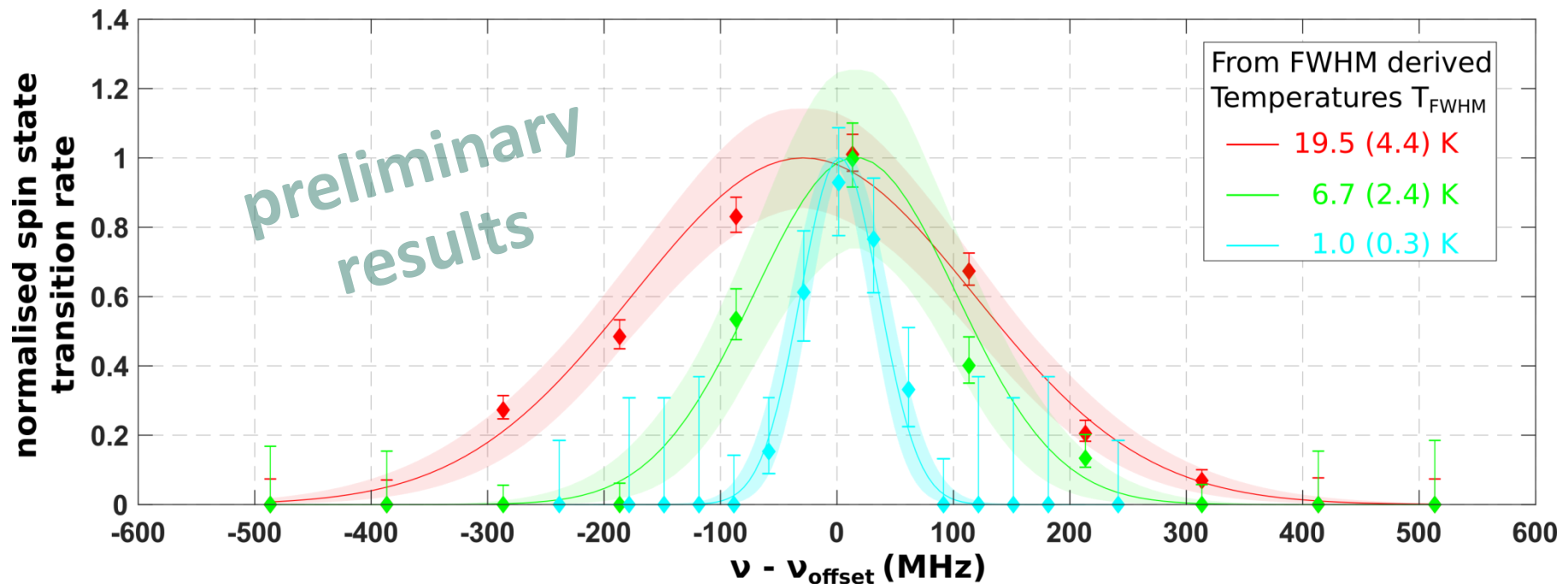
Results – Resonance for $|1/2, -1/2\rangle \leftrightarrow |3/2, +1/2\rangle$ ($= |J, m_j\rangle$)

- Derived temperature from FWHM $\rightarrow 19.5 \pm 4.4$ K



Results – Resonance for $|1/2, -1/2\rangle \leftrightarrow |3/2, +1/2\rangle$ ($= |J, m_j\rangle$)

- Derived temperature from FWHM $\rightarrow 1.0 \pm 0.3$ K
- Negative electronic feedback applied, expected lower temperature of factor ≈ 3
- Adiabatic cooling by lowering of trapping potential depth by factor of 3.8
 \rightarrow lowered temperature by $\approx 3 \times 3.8 = 11.4$



Summary & Perspectives

- First high precision measurement of boronlike g-factor
Sturm, Sven, et al. "The ALPHATRAP experiment." The European Physical Journal Special Topics 227.13 (2019): 1425-1491.
- Fine structure spectroscopy without fluorescence detection
- ALPHATRAP: access to heavy HCl via HD-EBIT:
 - control over single ion states and preparation
 - long storage times
 - low energy
- QED tests of heavy HCl e.g. HFS splitting in hydrogen- and lithiumlike $^{209}\text{Bi}^{82+,80+}$
- Isotope shift measurement for g-factor in HCl → high sensitivity to nuclear effects



Thank you for your attention



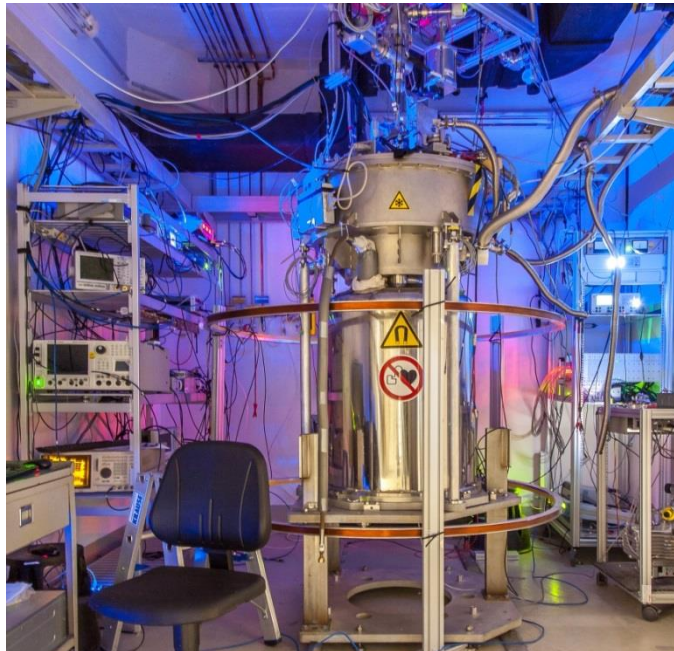
+ for Ar¹³⁺ FS Laser spectroscopy:

W. Nörtershäuser¹, K. König¹,
T. Ratajczyk¹

¹ IKP, TU Darmstadt

The ALPHATRAP Team:

Klaus Blaum
Sven Sturm
Bingsheng Tu
Andreas Weigel
Ioanna Arapoglou
Alexander Egl
Tim Sailer
& ...



+ for Ar¹³⁺ *g*-factor measurement:

H. Cakir¹, V. A. Yerokhin^{1,2}, N. S.
Oreshkina¹, V. A. Agababaev^{3,4}, A.
V. Volotka^{3,5,6}, D. V. Zinenko³, D. A.
Glazov³, Z. Harman¹, C.H. Keitel¹

¹ MPIK

² Peter the Great St. Petersburg University

³ St Petersburg State University

⁴ St Petersburg Electrotechnical University

⁵ Helmholtz-Institut Jena

⁶ GSI Darmstadt



Considerations for line shape

- Ion bound in a harmonic potential
 - Axial motion: $z(t) = z_0 \cos[\omega_z t]$
 - Doppler shift: $\omega_{Lab} = \omega_0 + k_L v_{ion}$



$$- E(t) = E_0 \exp \left[(i \int_0^t \omega_0 t - k_L \omega_z z_0 \sin(\omega_z t') dt') \right]$$

$$- \mathcal{F}\{E(t)\} = E(\omega) = \dots = E_0 \sum_{\alpha=-\infty}^{+\infty} i^\alpha J_\alpha(\eta)$$

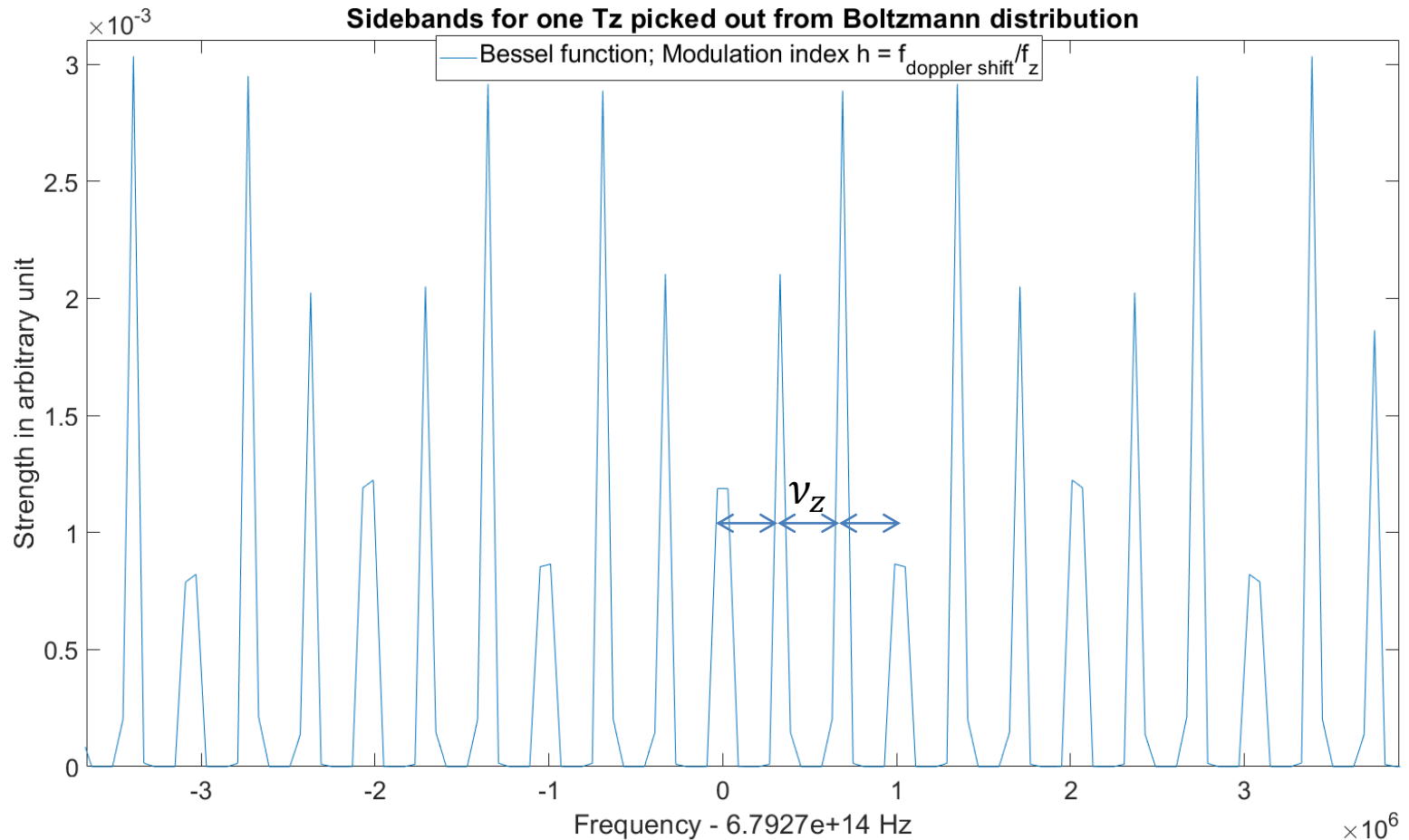
$$- I(\omega) \propto I_0 \sum_{\alpha=-\infty}^{+\infty} |J_\alpha(\eta)|^2$$

- modulation index η indicates by how much the modulated variable varies around its unmodulated level. It relates to variations in the carrier frequency. The Bessel function gives then the strength of the α^{th} sideband

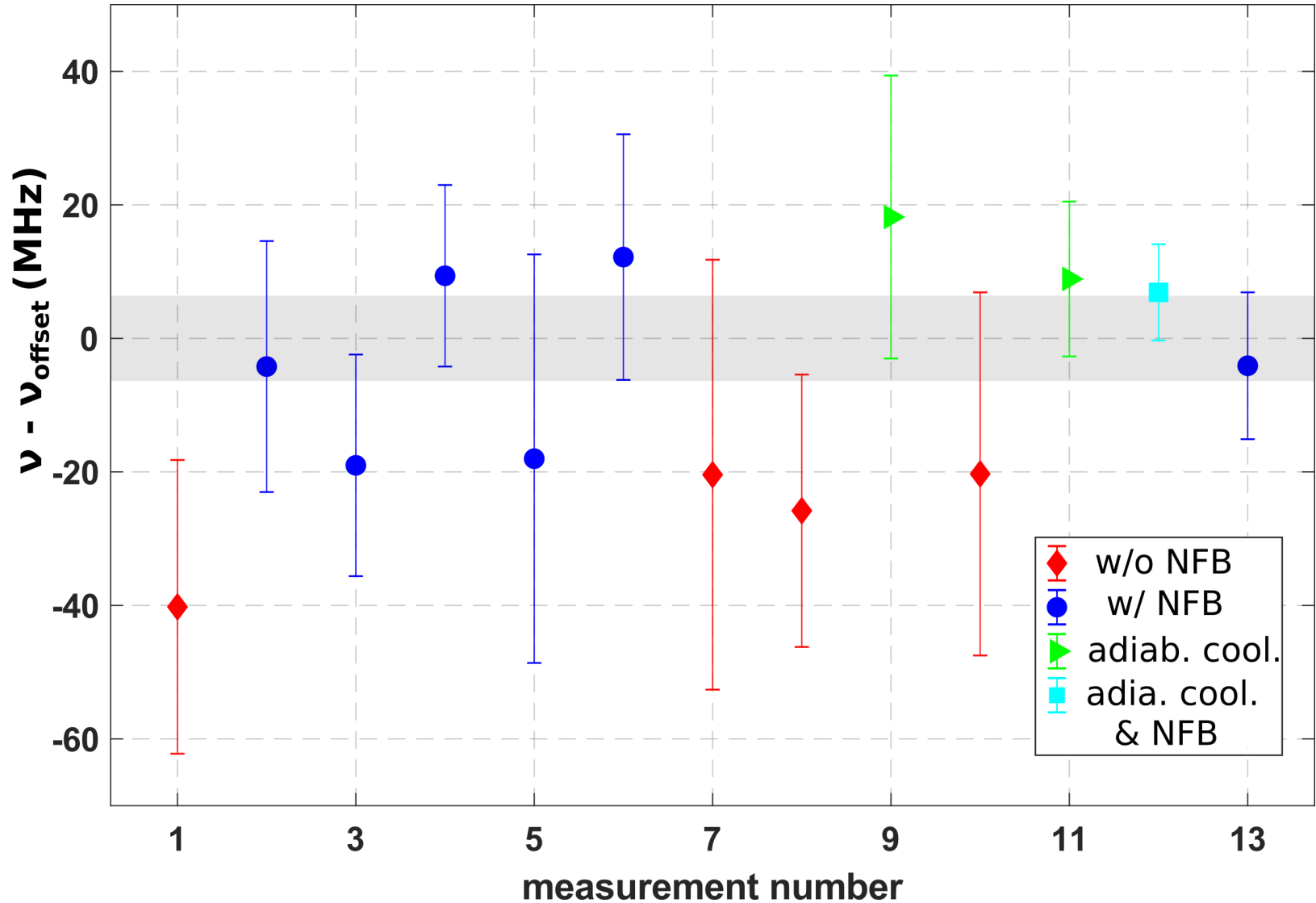


Simulations

- Sideband spectrum for one specific temperature picked out of this distribution



Center of resonances



Outlook

- Isotope shift measurement for g-factor in HCl
- Ground state g-factor of HCl
- Precision increased by sympathetic laser cooling, development of cooling scheme for HCl \leftrightarrow Be⁺ ions
- Improved laser system: line width narrowing e.g. ULE cavities, absolute frequency determination via frequency comb
- Spectroscopy, e.g. of Li-like and H-like Bismuth

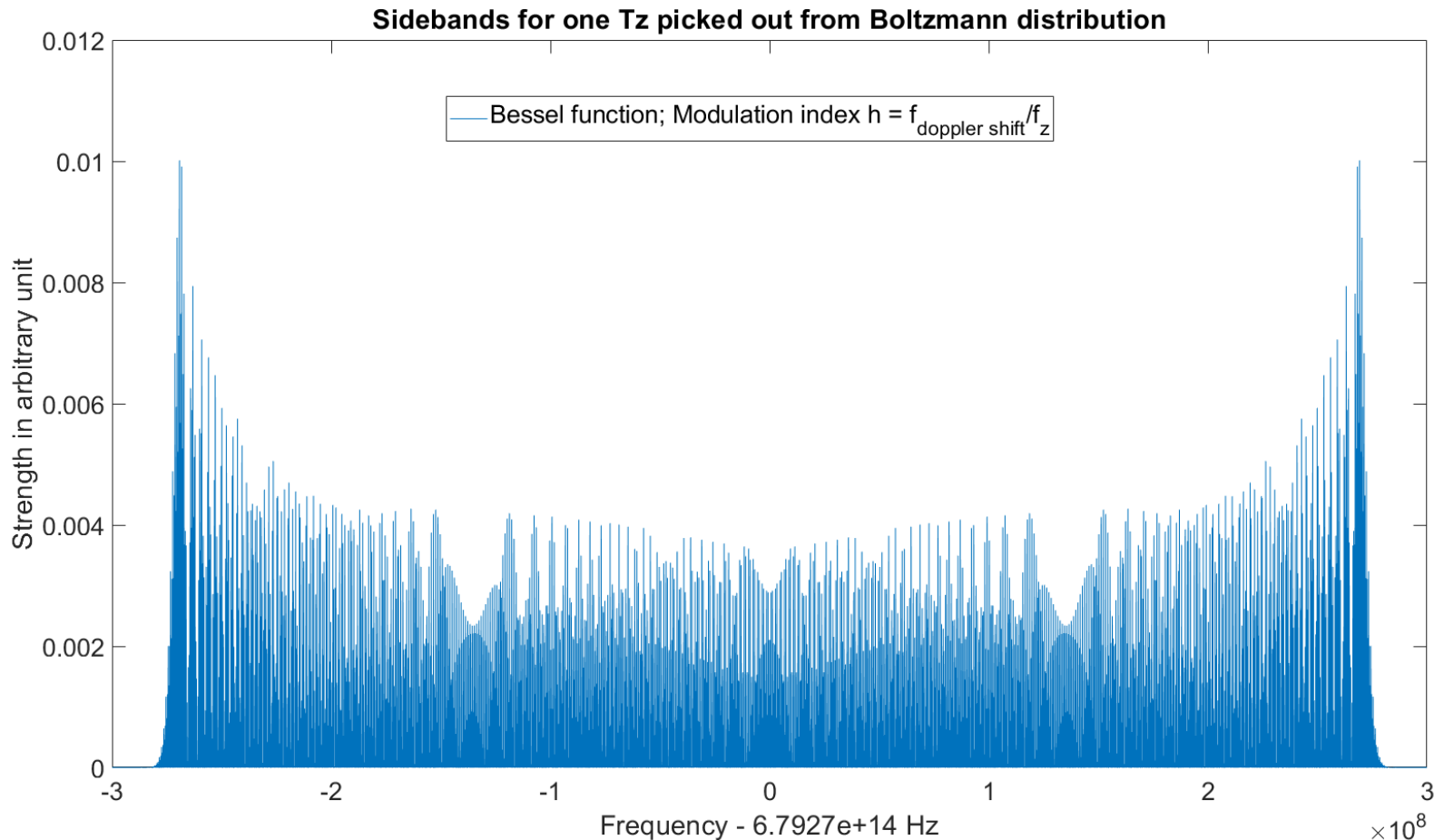


Laser Cooling for ALPHATRAP

- Increase precision by
 - **Sympathetic Cooling** of a highly-charged ion
 - Phase Sensitive Detection Methods benefit from small radial kinetic energies during the phase evolution time → **smaller magnetic and relativistic shifts**
- **Facilitation of the Spin-Flip measurement** in the AT
- Open up new type of measurements: **Coulomb Crystals** in Penning traps (crystal made of a single Be^{1+} ion and a single HCl) → measurements of $\Delta g \rightarrow \alpha$

Considerations for line shape

- Sideband spectrum for one specific energy out of the thermal Boltzmann distribution



Considerations for line shape

$$\Delta f_{FWHM} = f_0 \sqrt{\frac{8k_B T \ln(2)}{m_{ion} c^2}}$$

- Smoothing and comparison of the Gaussian lineshape (Doppler broadening)

