

Constraints on light Z' models with flavor changing couplings

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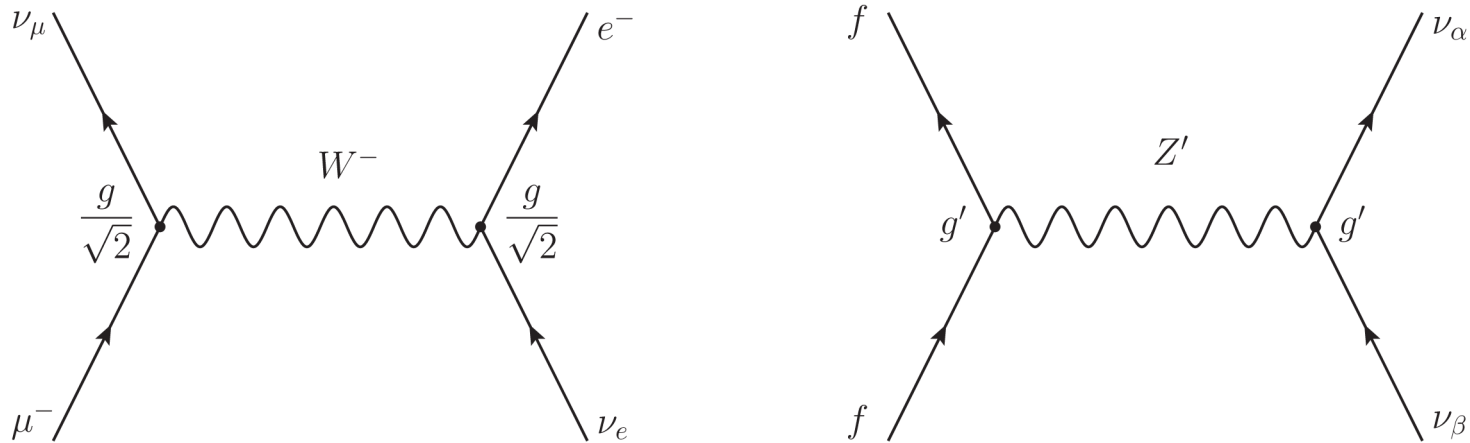
Collaborators

- ❖ Sofiane M. Boucenna (INFN, Italy)
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- ❖ Patrick Huber (Virginia Tech)
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Non-Standard Interactions of the Neutrino

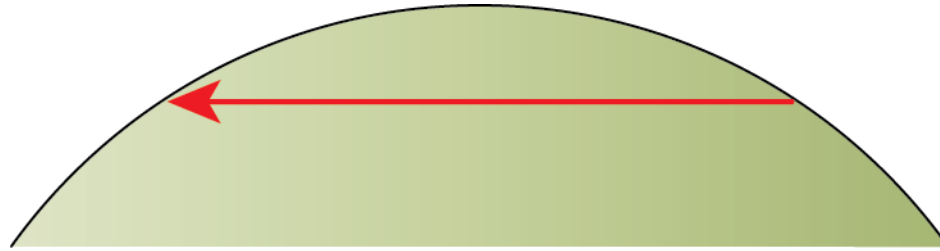
$$\mathcal{L}_{\text{NSI}} = -2\sqrt{2}G_F \sum_{\alpha,\beta,f,C} \varepsilon_{\alpha\beta}^{fC} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P_C f)$$

- ❖ Many models of New Physics Beyond the Standard Model predict neutrino NSI's



$$\varepsilon = 2 \left(\frac{g'}{g} \right)^2 \left(\frac{M_W}{M_{Z'}} \right)^2 = 0.03 g'^2 \left(\frac{1000 \text{ GeV}}{M_{Z'}} \right)^2$$

Non-Standard Interactions of the Neutrino



- ❖ Neutrino Oscillation experiments on the Earth are sensitive to:

$$\begin{aligned}\varepsilon_{\alpha\beta} &= \sum_{f=u,d,e} \left(\varepsilon_{\alpha\beta}^{fL} + \varepsilon_{\alpha\beta}^{fR} \right) \frac{N_f}{N_e} \\ &= 3 \left(\varepsilon_{\alpha\beta}^{uL} + \varepsilon_{\alpha\beta}^{uR} \right) + 3 \left(\varepsilon_{\alpha\beta}^{dL} + \varepsilon_{\alpha\beta}^{dR} \right) + \left(\varepsilon_{\alpha\beta}^{eL} + \varepsilon_{\alpha\beta}^{eR} \right)\end{aligned}$$

- ❖ Expected DUNE sensitivities (from [P. Coloma JHEP03\(2016\)016](#))

$$|\varepsilon_{\alpha\beta}| < 0.1 \sim 0.01$$

- ❖ Do models exist that predict such large NSI's ?

Interactions must be SU(2) x U(1) invariant:

$$\mathcal{L} = -2\sqrt{2}G_F\varepsilon_{\mu\tau}^{eL}(\bar{\nu}_\mu\gamma^\mu P_L\nu_\tau)(\bar{e}\gamma_\mu P_L e)$$

❖ Case 1: $(\bar{L}_\mu\gamma^\mu L_\tau)(\bar{L}_e\gamma_\mu L_e)$

$$= \left[(\bar{\nu}_\mu\gamma^\mu P_L\nu_\tau)(\bar{\nu}_e\gamma_\mu P_L\nu_e) + (\bar{\nu}_\mu\gamma^\mu P_L\nu_\tau)(\bar{e}\gamma_\mu P_L e) \right. \\ \left. + (\bar{\mu}\gamma_\mu P_L\tau)(\bar{\nu}_e\gamma^\mu P_L\nu_e) + (\bar{\mu}\gamma_\mu P_L\tau)(\bar{e}\gamma_\mu P_L e) \right]$$

Constrained by $\tau \rightarrow \mu ee$: $|\varepsilon_{\mu\tau}^{eL}| < 10^{-4}$

❖ Case 2: $(\bar{L}_\mu i\sigma_2 L_e^c)(\bar{L}_\tau^c i\sigma_2 L_e)$

$$= \frac{1}{2}(\bar{\nu}_\mu\gamma^\mu P_L\nu_\tau)(\bar{e}\gamma_\mu P_L e) - \frac{1}{2}(\bar{\nu}_e\gamma^\mu P_L\nu_\tau)(\bar{\mu}\gamma_\mu P_L e) \\ - \frac{1}{2}(\bar{\nu}_\mu\gamma^\mu P_L\nu_e)(\bar{e}\gamma_\mu P_L\tau) + \frac{1}{2}(\bar{\nu}_e\gamma^\mu P_L\nu_e)(\bar{\mu}\gamma_\mu P_L\tau)$$

Constrained by $\mu \rightarrow e\nu_e\nu_\tau, \tau \rightarrow e\nu_e\nu_\mu, \tau \rightarrow \mu\nu_e\nu_e$: $|\varepsilon_{\mu\tau}^{eL}| < 10^{-3}$

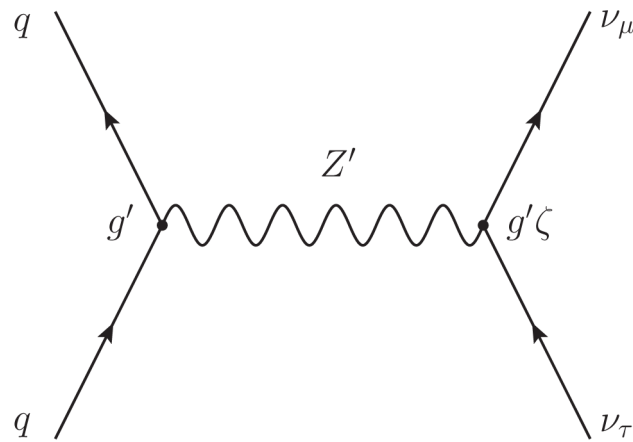
Recent Proposals

- Y. Farzan, “A model for large non-standard interactions of neutrinos leading to the LMA-Dark solution,” [Phys. Lett. B748 \(2015\) 311-315](#), arXiv:1505.06906
- ❖ Y. Farzan and I. M. Shoemaker, “Lepton Flavor Violating Non-Standard Interactions via Light Mediators,” [JHEP07\(2016\)033](#), arXiv:1512.09147
- ❖ Y. Farzan and J. Heeck, “Neutrinophilic Non-Standard Interactions,” [Phys. Rev. D 94, 053010 \(2016\)](#), arXiv:1607.07616
- ❖ D. V. Forero and W.-C. Huang, “Sizable NSI from the $SU(2)_L$ scalar doublet-singlet mixing and the implications in DUNE,” [JHEP03\(2017\)018](#), arXiv:1608.04719
- ❖ K. S. Babu, A. Friedland, P. A. N. Machado, I. Mocioiu, “Flavor Gauge Models Below the Fermi Scale,” [arXiv:1705.01822](#)
- ❖ etc.

Farzan-Shoemaker Model

- ❖ Y. Farzan and I. M. Shoemaker, “Lepton Flavor Violating Non-Standard Interactions via Light Mediators,” **JHEP07(2016)033**, arXiv:1512.09147

$$\varepsilon = 2 \left(\frac{g'}{g} \right)^2 \left(\frac{M_W}{M_{Z'}} \right)^2 = 0.03 g'^2 \left(\frac{1000 \text{ GeV}}{M_{Z'}} \right)^2 = 0.03 \left(\frac{g'}{10^{-4}} \right)^2 \left(\frac{100 \text{ MeV}}{M_{Z'}} \right)^2$$



$$\varepsilon_{\mu\tau}^{qC} \sim 0.005 \quad \rightarrow \quad \varepsilon_{\mu\tau} \sim 0.06$$

- ❖ Is the model truly viable?

Farzan-Shoemaker Model : Fermion Content

❖ $SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)'$ gauge theory

❖ Quarks:

$$Q_i = \begin{bmatrix} u_{Li} \\ d_{Li} \end{bmatrix} \sim \left(3, 2, +\frac{1}{6}, 1 \right), \quad u_{Ri} \sim \left(3, 1, +\frac{2}{3}, 1 \right), \quad d_{Ri} \sim \left(3, 1, -\frac{1}{3}, 1 \right)$$

❖ Leptons:

$$L_0 = \begin{bmatrix} \nu_{L0} \\ \ell_{L0} \end{bmatrix} \sim \left(1, 2, -\frac{1}{2}, 0 \right), \quad \ell_{R0} \sim (1, 1, -1, 0),$$
$$L_+ = \begin{bmatrix} \nu_{L+} \\ \ell_{L+} \end{bmatrix} \sim \left(1, 2, -\frac{1}{2}, +\zeta \right), \quad \ell_{R+} \sim (1, 1, -1, +\zeta),$$
$$L_- = \begin{bmatrix} \nu_{L-} \\ \ell_{L-} \end{bmatrix} \sim \left(1, 2, -\frac{1}{2}, -\zeta \right), \quad \ell_{R-} \sim (1, 1, -1, -\zeta),$$

❖ Extra (heavy) fermions for anomaly cancellation (?)

Farzan-Shoemaker Model : Scalar Content

❖ Higgses:

$$\begin{aligned}
 H &= \begin{bmatrix} H^+ \\ H^0 \end{bmatrix} \sim \left(1, 2, +\frac{1}{2}, 0 \right) , \\
 H_{++} &= \begin{bmatrix} H_{++}^+ \\ H_{++}^0 \end{bmatrix} \sim \left(1, 2, +\frac{1}{2}, +2\zeta \right) , \\
 H_{--} &= \begin{bmatrix} H_{--}^+ \\ H_{--}^0 \end{bmatrix} \sim \left(1, 2, +\frac{1}{2}, -2\zeta \right) .
 \end{aligned}$$

❖ Yukawa couplings:

$$\begin{aligned}
 &\sum_{i=1}^3 \sum_{j=1}^3 \left(\lambda_{ij} \overline{d_{Ri}} H^\dagger Q_j + \tilde{\lambda}_{ij} \overline{u_{Ri}} \tilde{H}^\dagger Q_j \right) + h.c. \\
 &+ \sum_{j=0,+,-} \left(f_j \overline{\ell_{Rj}} H^\dagger L_j \right) + h.c. \\
 &+ \left(c_- \overline{\ell_{R+}} H_{--}^\dagger L_- + c_+ \overline{\ell_{R-}} H_{++}^\dagger L_+ \right) + h.c.
 \end{aligned}$$

Farzan-Shoemaker Model : Symmetry Breaking

❖ Higgs VEV's:

$$\langle H^0 \rangle = \frac{v}{\sqrt{2}}, \quad \langle H_{++}^0 \rangle = \frac{v_+}{\sqrt{2}}, \quad \langle H_{--}^0 \rangle = \frac{v_-}{\sqrt{2}},$$

❖ Assume $v_+ = v_- = \frac{w}{\sqrt{2}}$ (no Z-Z' or γ -Z' mixing at tree-level)

❖ Gauge boson masses:

$$M_W = \frac{g_2}{2} \sqrt{v^2 + w^2}, \quad M_Z = \frac{\sqrt{g_1^2 + g_2^2}}{2} \sqrt{v^2 + w^2}, \quad M_{Z'} = 2\zeta g' w$$

Farzan-Shoemaker Model : Z' Mass & Coupling

- ❖ The mass of the Z' is chosen to be:

$$135 \text{ MeV} < M_{Z'} < 200 \text{ MeV}$$

so that the decays

$$\pi^0 \rightarrow \gamma + Z', \quad Z' \rightarrow \mu^+ + \mu^-$$

cannot occur

- ❖ Range of the Z' -exchange force comparable to that of strong interactions $\rightarrow Z'$ interactions between quarks can be sizable but still be masked by the strong force (?)
- ❖ Z' coupling to the leptons are strongly constrained by:

$$\tau \rightarrow \mu + Z'$$

Farzan-Shoemaker Model : Problems

- ❖ $U(1)$ charges are ill defined in models with multiple $U(1)$'s
→ They necessarily mix under renormalization group running
(See W. A. Loinaz and T. Takeuchi, [Phys.Rev. D60 \(1999\) 115008](#))
- ❖ Constraint on $\zeta g'$ does not allow the generation of Z' mass in the 135~200 MeV range without making the Higgs VEV w too large for the W and Z masses
→ Need to introduce a SM-singlet scalar
- ❖ Full MNS neutrino mixing matrix cannot be generated.
The $U(1)'$ singlet lepton cannot mix with the non-singlet leptons.
→ Need to introduce a more scalars
- ❖ Not clear whether the fermions necessary for anomaly cancelation can be made heavy → Even more scalars?

Constraints on the Z' couplings revisited:

- ❖ Z' -quark coupling
- ❖ Z' -lepton coupling

- ❖ Semi-Empirical Mass Formula of Nuclei:

$$E_B = a_V A - a_S A^{2/3} - a_C \frac{Z^2}{A^{1/3}} - a_A \frac{(A - 2Z)^2}{A} \pm \delta(A, Z)$$

- ❖ Coulomb term:

$$E_C = \frac{3 Q^2}{5 R} = \frac{3 (eZ)^2}{5 (r_0 A^{1/3})} = (0.691 \text{ MeV}) \frac{(1.25 \text{ fm})}{r_0} \frac{Z^2}{A^{1/3}}$$

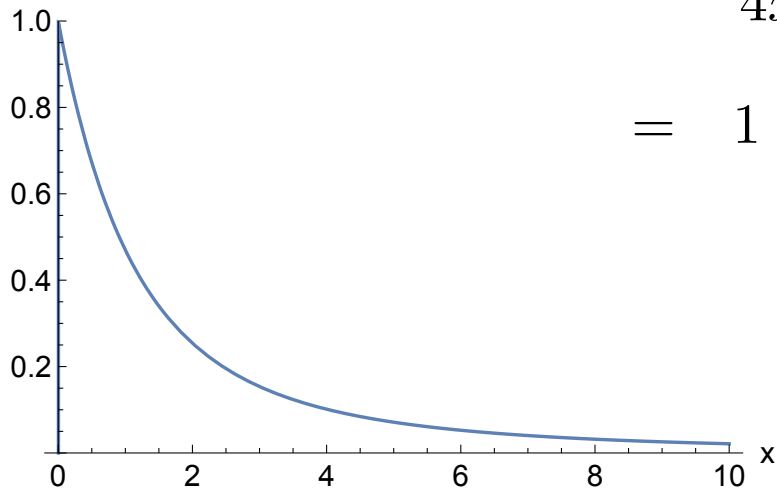
Z' potential energy:

❖ Z' potential energy term:

$$\begin{aligned} E_{Z'} &= \frac{3}{5} \frac{Q'^2}{R} f(mR) = \frac{3}{5} \frac{(3g'A)^2}{(r_0 A^{1/3})} f(mr_0 A^{1/3}) \\ &= (0.691 \text{ MeV}) \frac{(1.25 \text{ fm})}{r_0} \left(\frac{3g'}{e} \right)^2 A^{5/3} f(mr_0 A^{1/3}) \end{aligned}$$

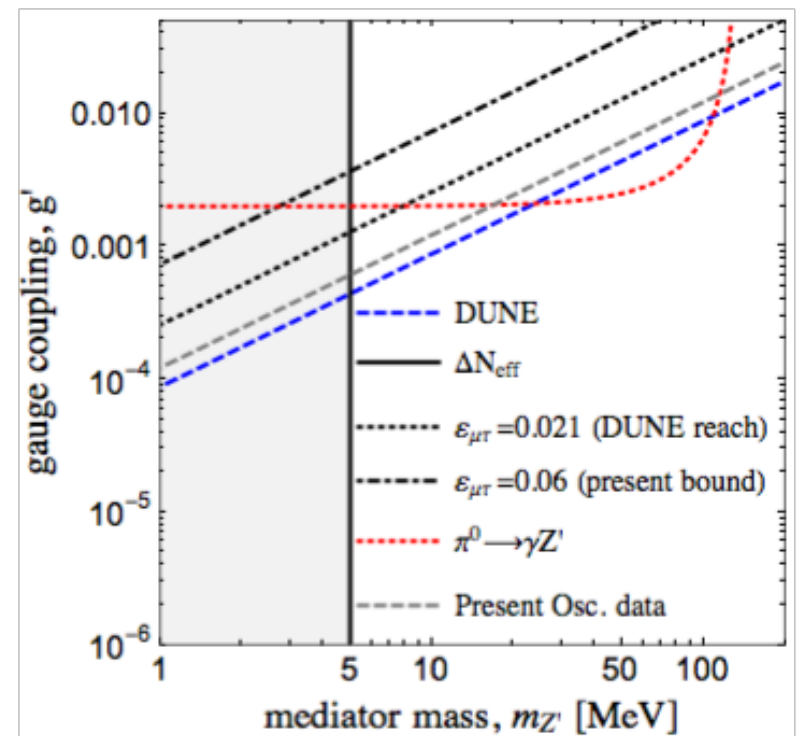
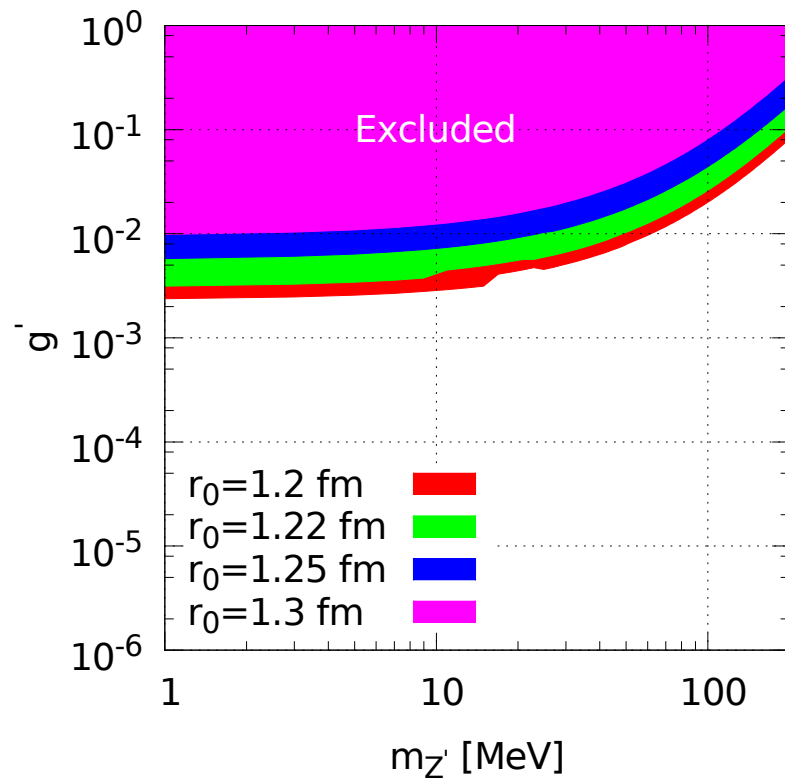
where

$$\begin{aligned} f(x) &\equiv \frac{15}{4x^5} \left[1 - x^2 + \frac{2x^3}{3} - (1+x)^2 e^{-2x} \right] \\ &= 1 - \frac{5x}{6} + \frac{3x^2}{7} - \frac{x^3}{6} + \dots \end{aligned}$$

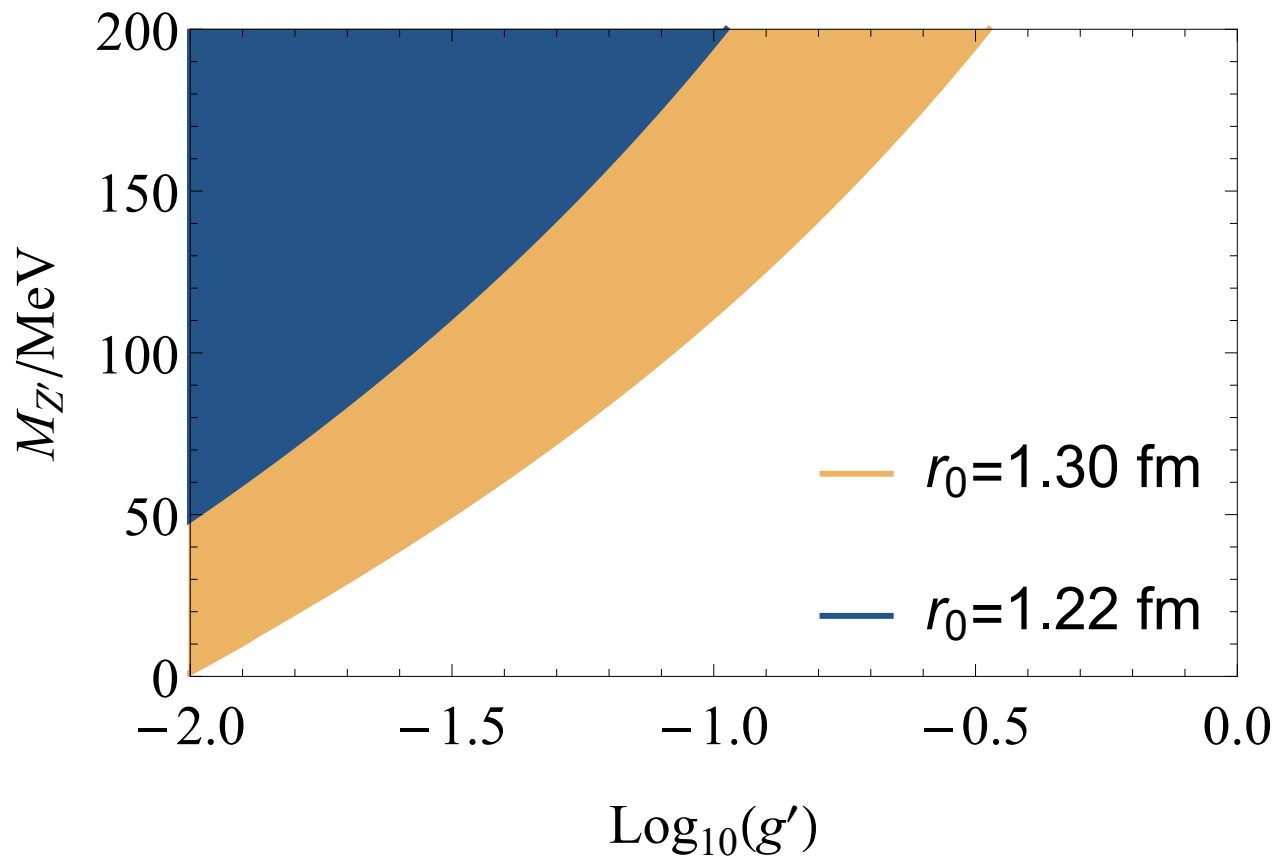


Result of Fit:

- ❖ Our result from fit to stable nuclei (90% C.L. left) compared to Figure from Farzan-Shoemaker paper (JHEP07(2016)033 right)



Result of Fit:

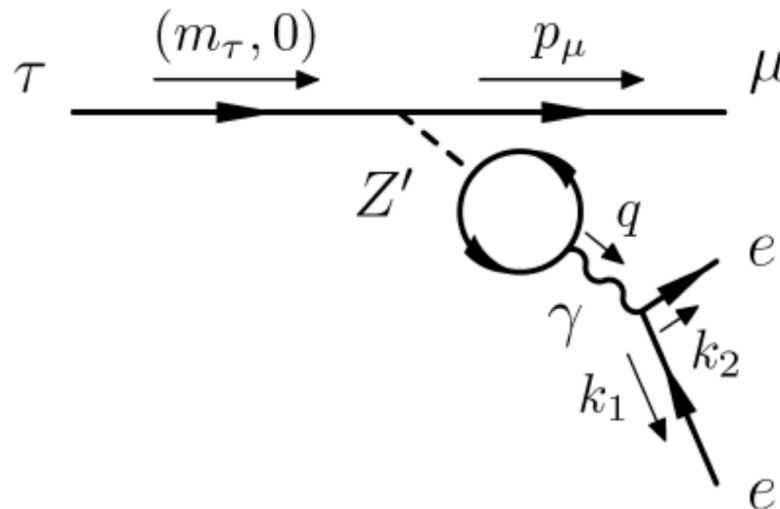


Coupling to the electron from photon-Z' mixing:

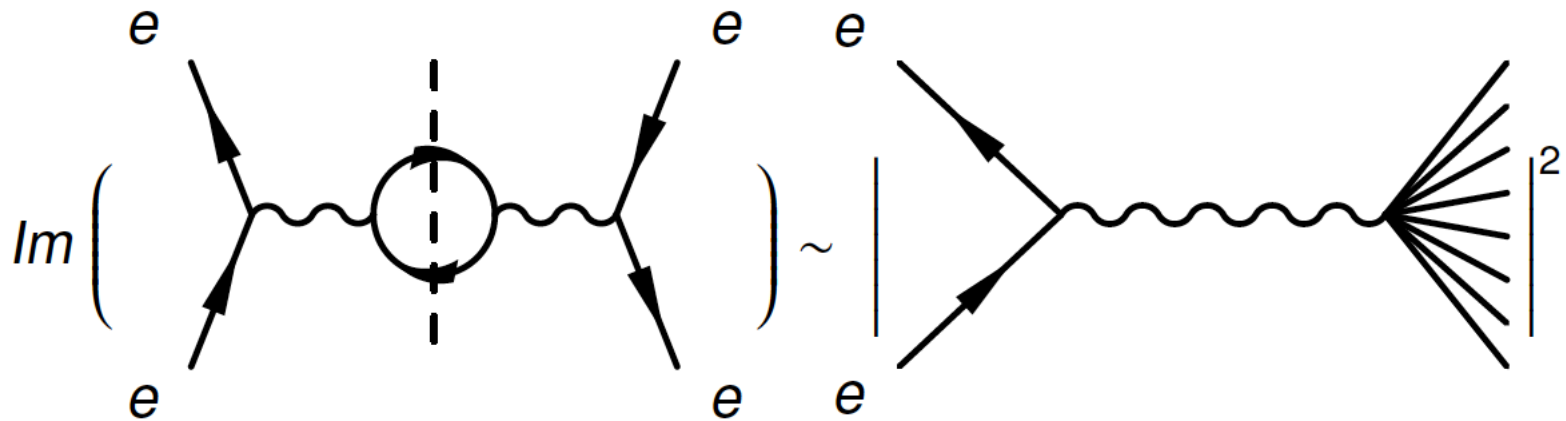
- ❖ Recall that $\tau \rightarrow \mu e e$ is strongly bounded:

$$B(\tau^- \rightarrow \mu^- e^- e^+) < 1.8 \times 10^{-8}$$

- ❖ At tree level the Z' does not couple to electrons
- ❖ But Z' and the photon can mix!



Optical Theorem:



$$\Pi'_{\gamma\gamma}(q^2) - \Pi'_{\gamma\gamma}(0) = -\frac{1}{12\pi^2} \int_{4m_\pi^2}^{\infty} \frac{q^2}{s(s - q^2)} R(s) ds$$

where

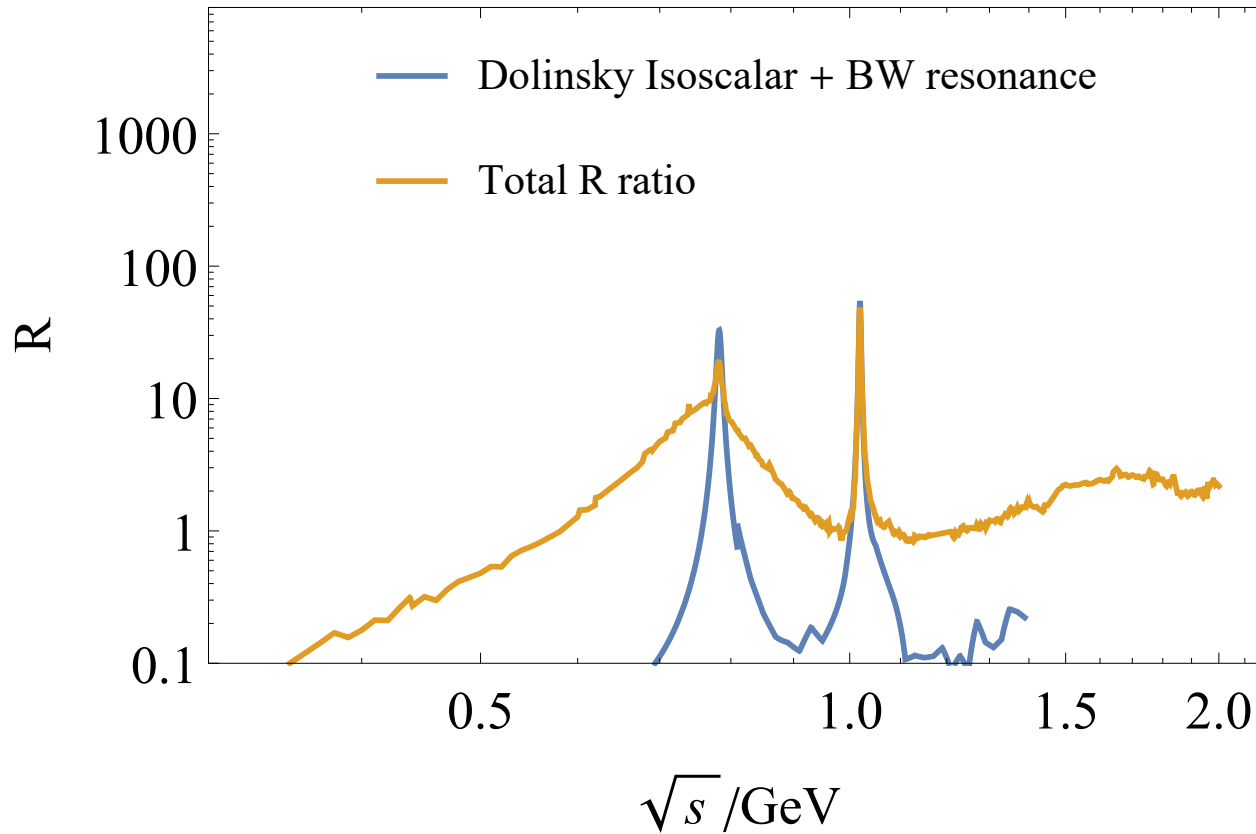
$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

photon-photon and photon-Z' correlations:

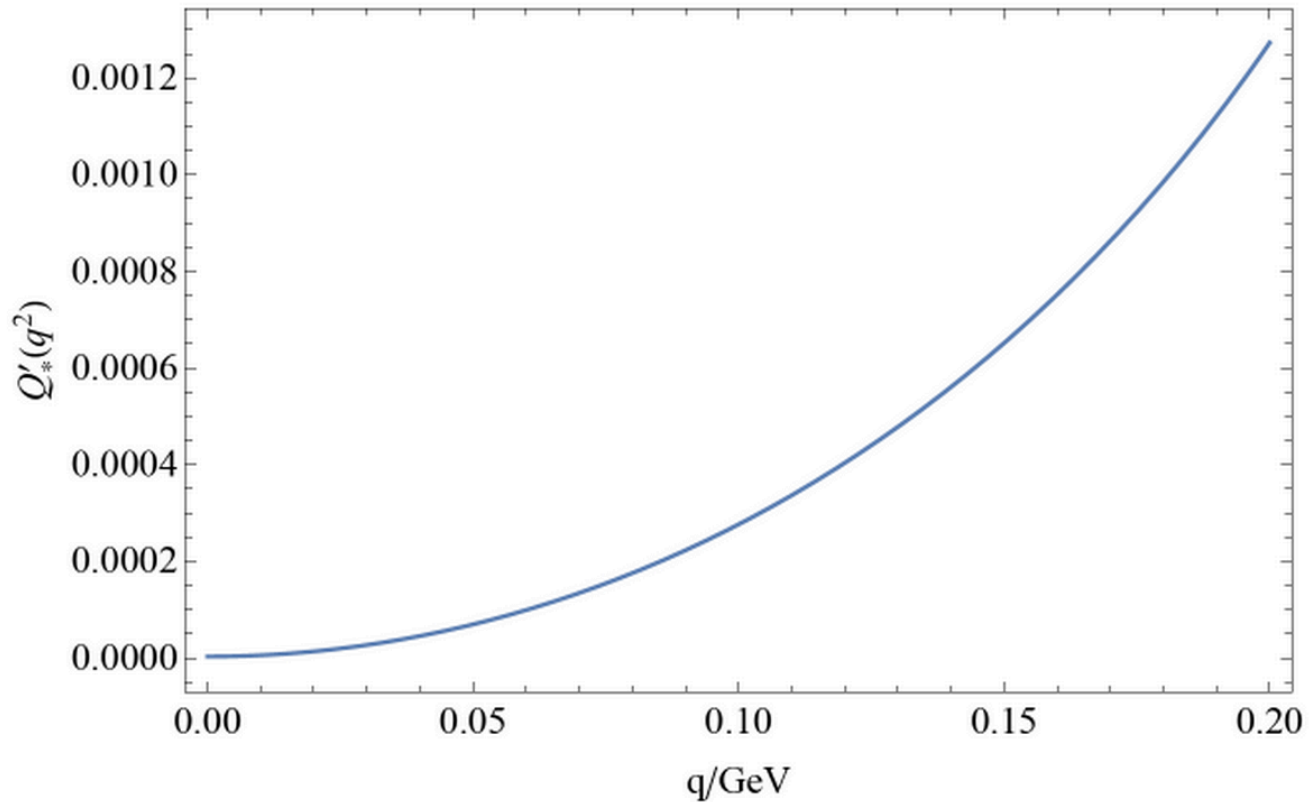
$$\begin{aligned}\Pi'_{\gamma\gamma} &\propto \left\langle \left(\frac{2}{3} \bar{u} \gamma_\mu u - \frac{1}{3} \bar{d} \gamma_\mu d \right) \left(\frac{2}{3} \bar{u} \gamma_\nu u - \frac{1}{3} \bar{d} \gamma_\nu d \right) \right\rangle \\ &\approx \left(\frac{1}{6} \right)^2 \langle (\bar{u} \gamma_\mu u + \bar{d} \gamma_\mu d) (\bar{u} \gamma_\nu u + \bar{d} \gamma_\nu d) \rangle \\ &\quad + \left(\frac{1}{2} \right)^2 \langle (\bar{u} \gamma_\mu u - \bar{d} \gamma_\mu d) (\bar{u} \gamma_\nu u - \bar{d} \gamma_\nu d) \rangle\end{aligned}$$

$$\begin{aligned}\Pi'_{\gamma Z'} &\propto \left\langle \left(\frac{2}{3} \bar{u} \gamma_\mu u - \frac{1}{3} \bar{d} \gamma_\mu d \right) (\bar{u} \gamma_\nu u + \bar{d} \gamma_\nu d) \right\rangle \\ &\approx \frac{1}{6} \langle (\bar{u} \gamma_\mu u + \bar{d} \gamma_\mu d) (\bar{u} \gamma_\nu u + \bar{d} \gamma_\nu d) \rangle\end{aligned}$$

Separation of Isovector and Isoscalar parts:

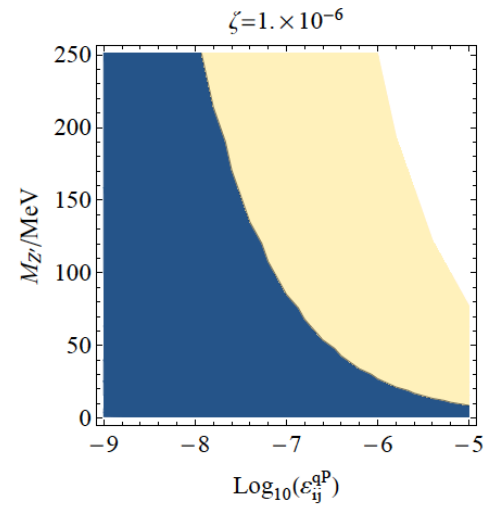
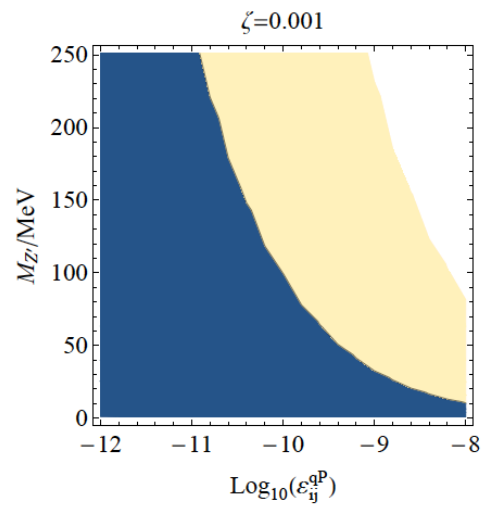
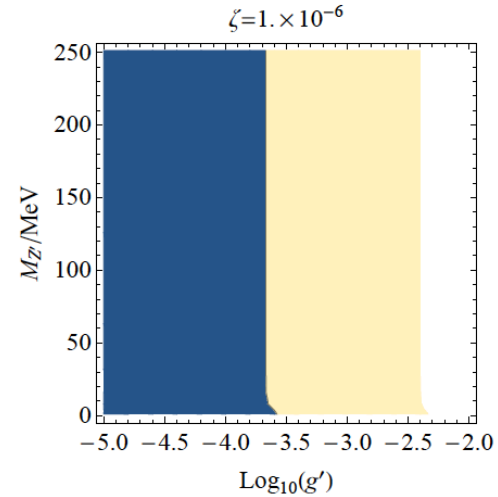
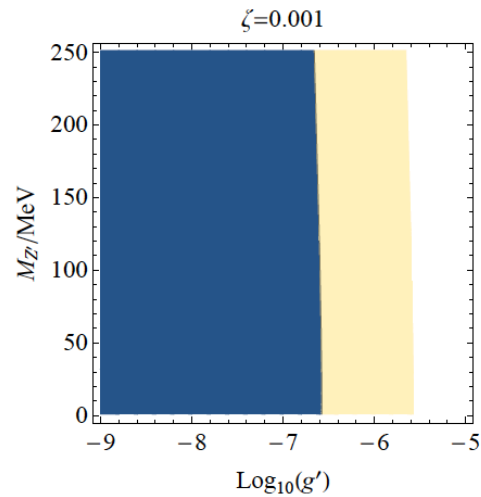


Running of the effective coupling to electrons:



Resulting bounds:

$Br(\tau \rightarrow \mu ee) \leq 1.8 \times 10^{-8}$ (Belle, PDG):



Does this bound apply?

❖ For the Z' decay into an electron-positron decay to be observable, the Z' must decay inside the detector

❖ Belle central drift chamber:
 Z' must decay within 0.88 m to 1.7 m

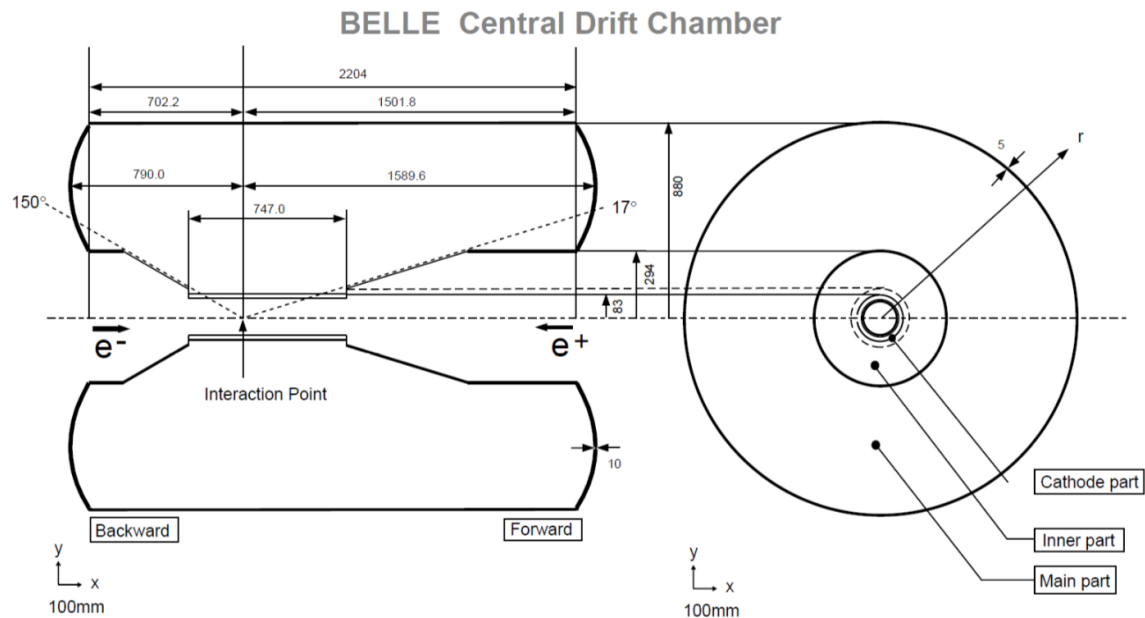


Fig. 22. Overview of the CDC structure. The lengths in the figure are in units of mm.

Two-body decay bound:

❖ Argus (1995)

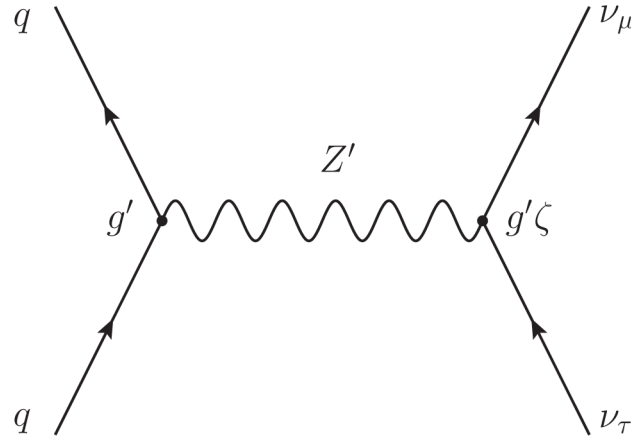
$$\begin{aligned} B(\tau \rightarrow \mu + Z') &< 5 \times 10^{-3} \\ &\downarrow \\ g'\zeta &< 6 \times 10^{-8} \left(\frac{M_{Z'}}{200\text{MeV}} \right) \end{aligned}$$

❖ Belle has 2000 times more statistics and is expected to improve the bound to 1×10^{-4} (Yoshinobu and Hayasaka, 2016)

$$\begin{aligned} B(\tau \rightarrow \mu + Z') &< 1 \times 10^{-4} \\ &\downarrow \\ g'\zeta &< 9 \times 10^{-9} \left(\frac{M_{Z'}}{200\text{MeV}} \right) \end{aligned}$$

Conclusion :

- ❖ Both g' and $g'\zeta$ are more tightly bound than originally assumed



- ❖ Constructing viable models that predict sizable neutrino NSI's is not easy!