

**HF-RFQ  
and  
S-Band BTW**

**Cavities for Medical Applications**

KT Medical Applications Seminar  
07.07.2017

Benjamin Koubek  
BE-RF-LRF

# Overview



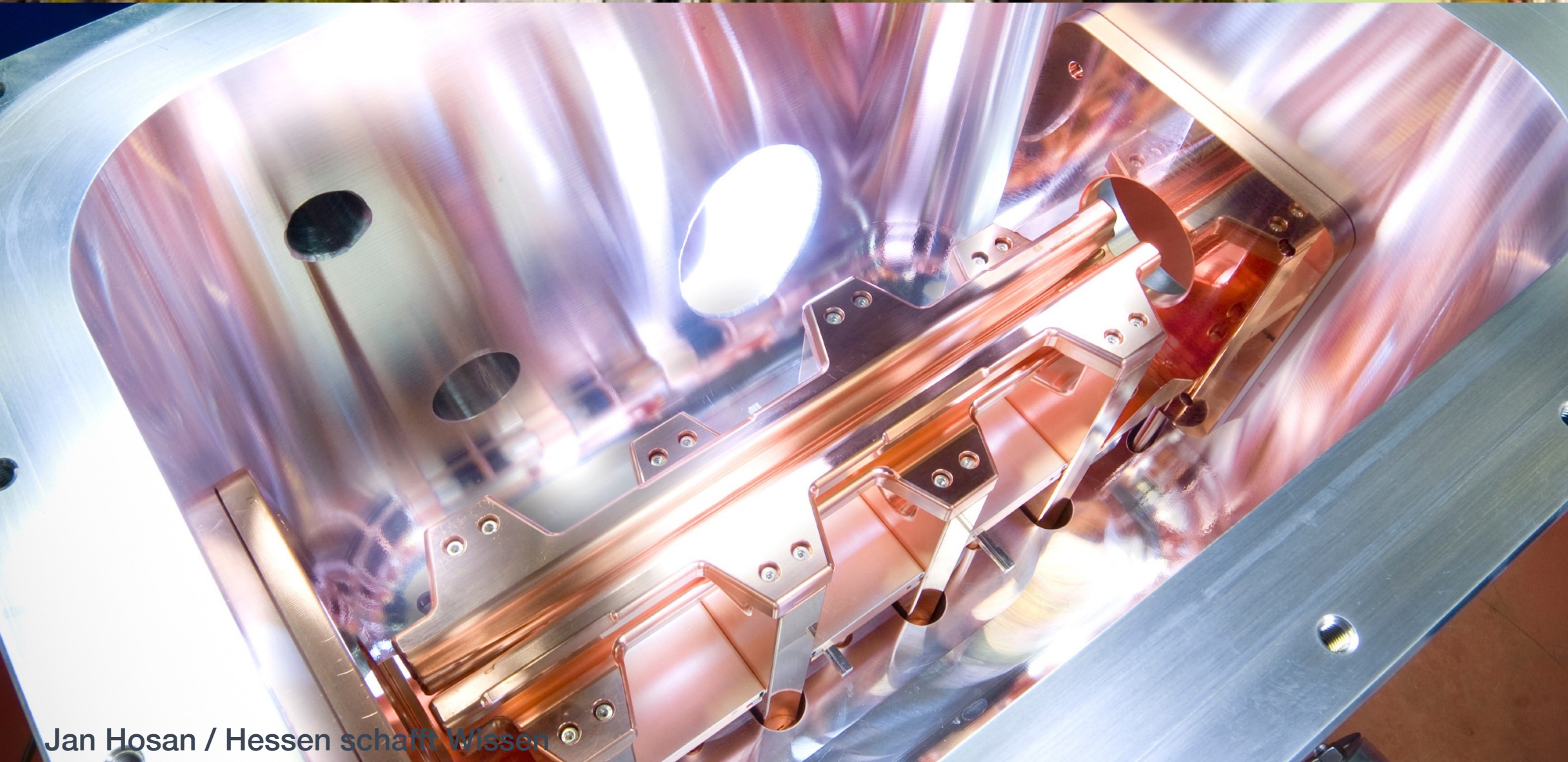
<https://media-cdn.tripadvisor.com/media/photo-s/03/9b/2f/80/frankfurt.jpg>



[www.uni-frankfurt.de](http://www.uni-frankfurt.de)

## Accelerator Physics

- RF simulations
- RF measurements
- Tuning



Jan Hosan / Hessen schafft Wissen

Benjamin Koubek

KT Medical Applications Seminar 2017

# Overview

Why Protons for Cancer Therapy?  
State of the Art Facilities

Projects

750 MHz RFQ for Medical Applications

RF Measurements

Tuning Algorithm Development

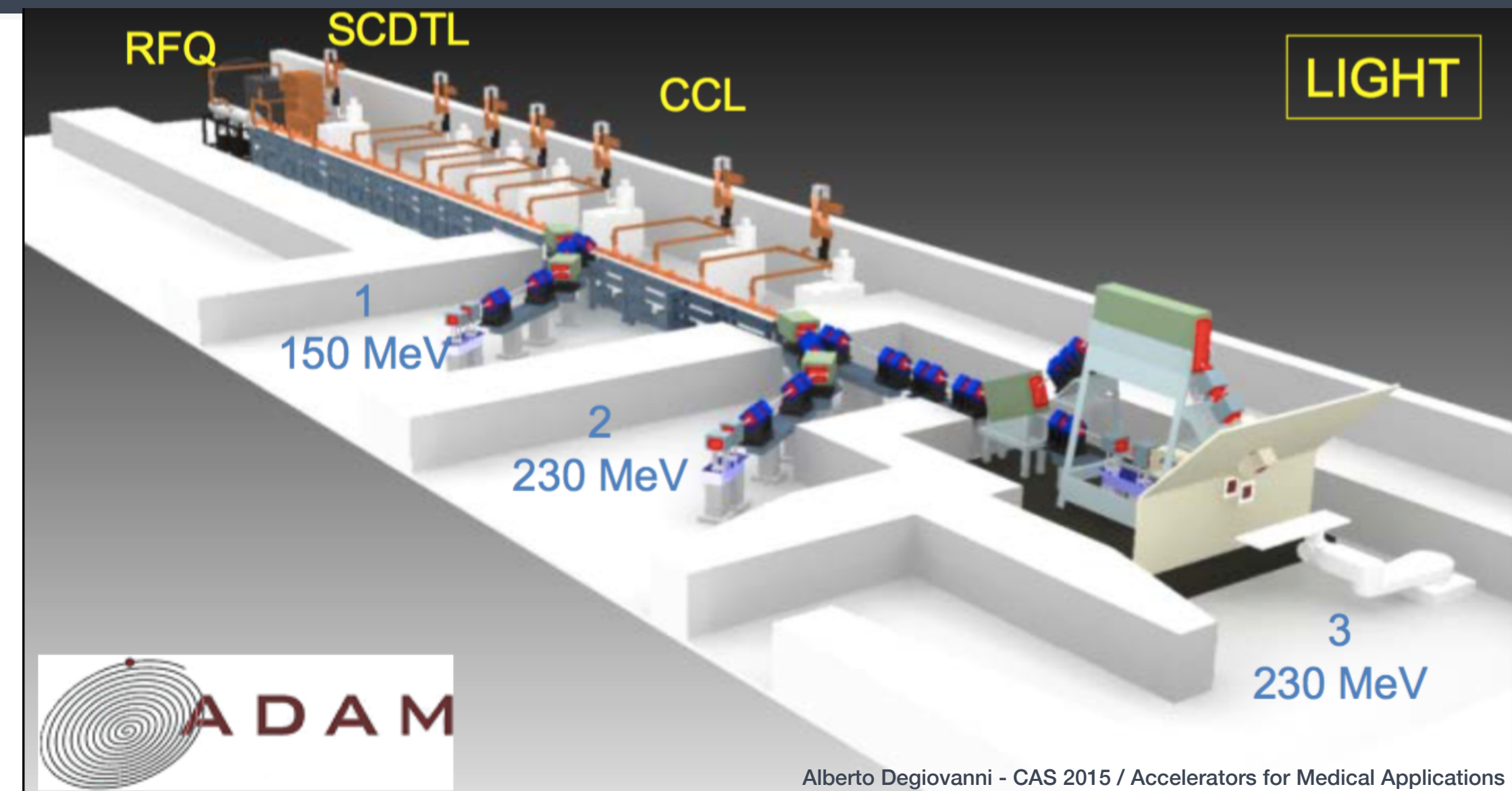
Tuning of the RFQ

3 GHz BTW Structure for TULIP

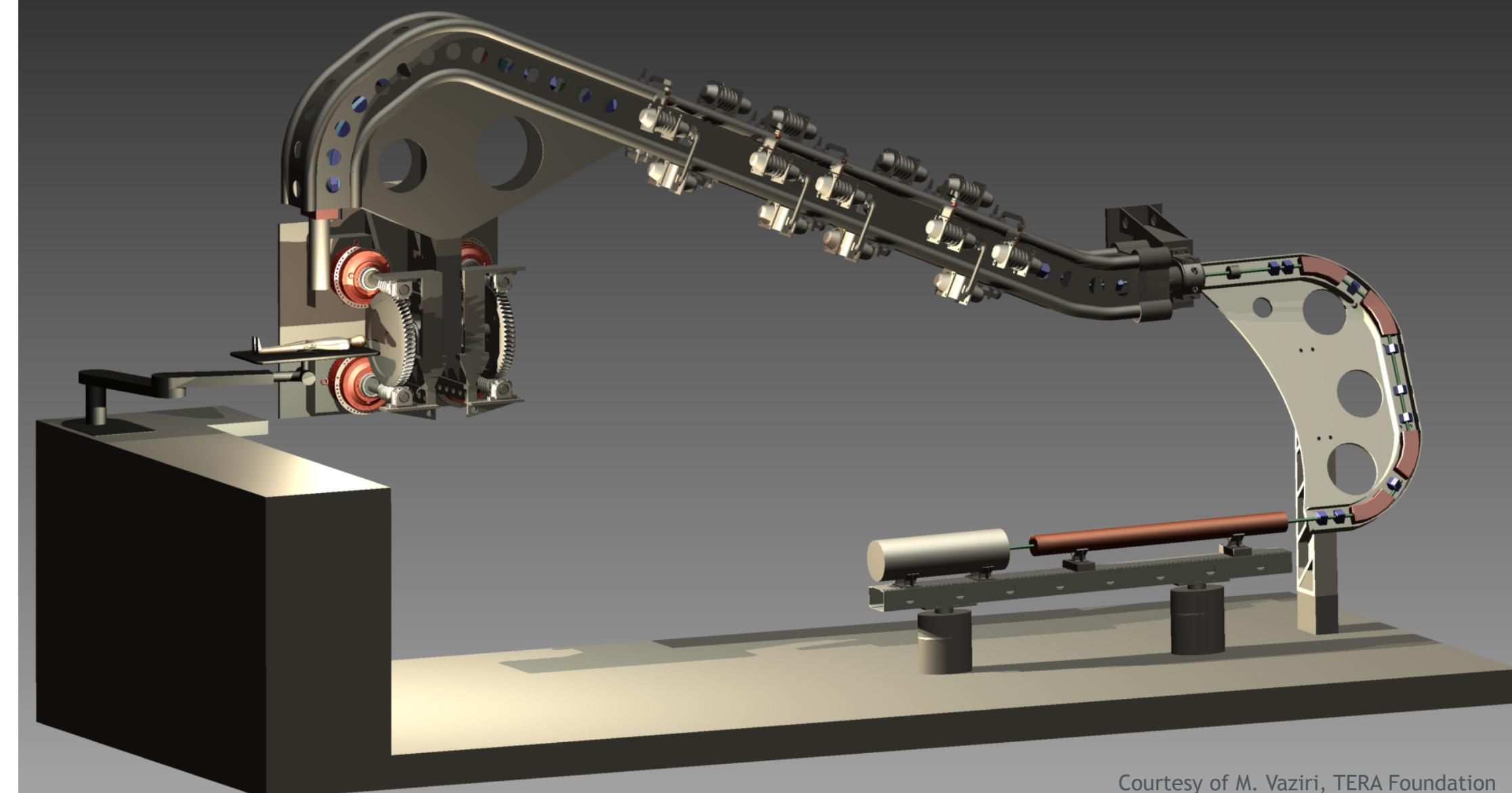
Conditioning of the Structure

Breakdown Studies

Data Analysis

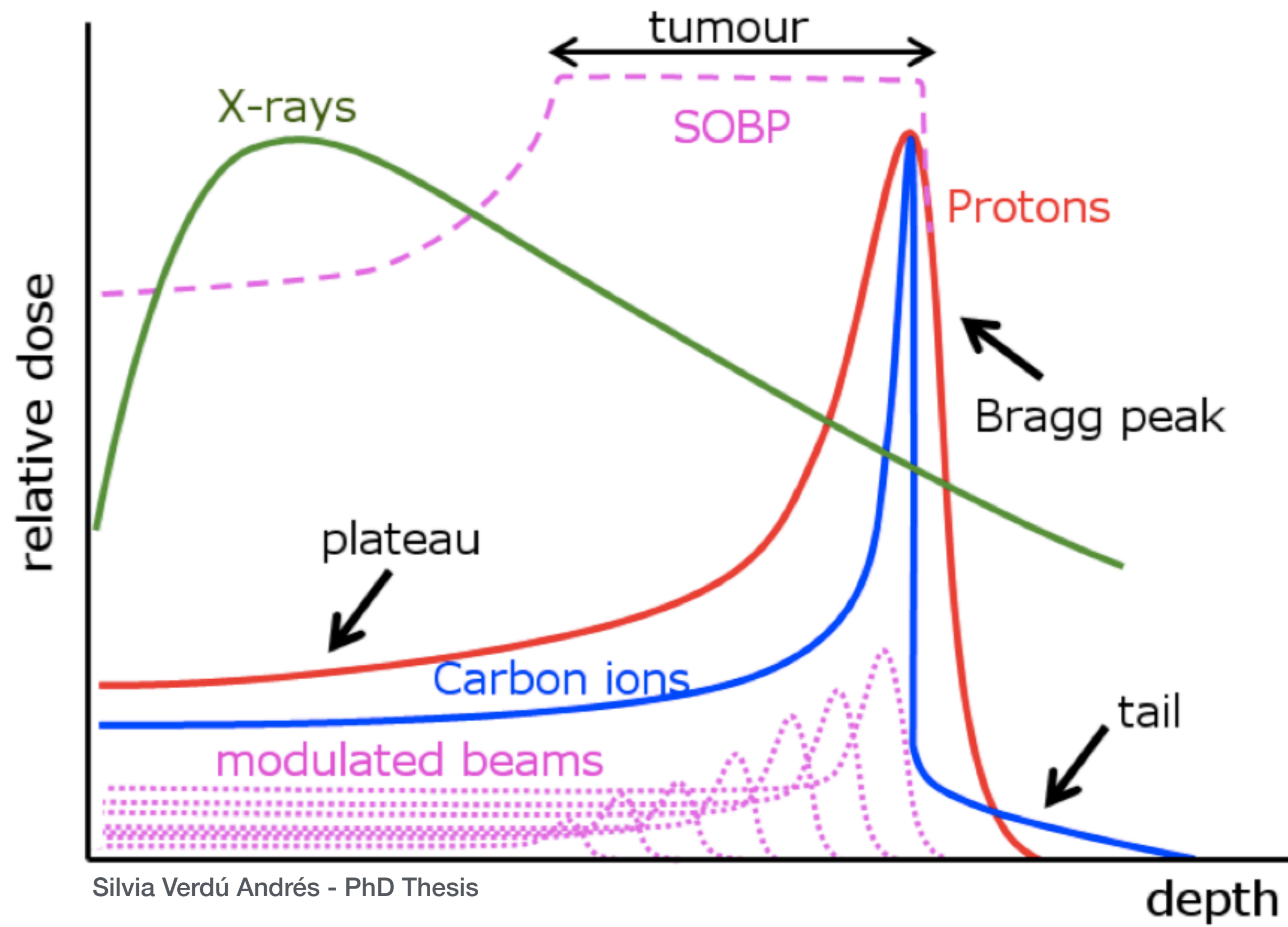


Alberto Degiovanni - CAS 2015 / Accelerators for Medical Applications



Courtesy of M. Vaziri, TERA Foundation

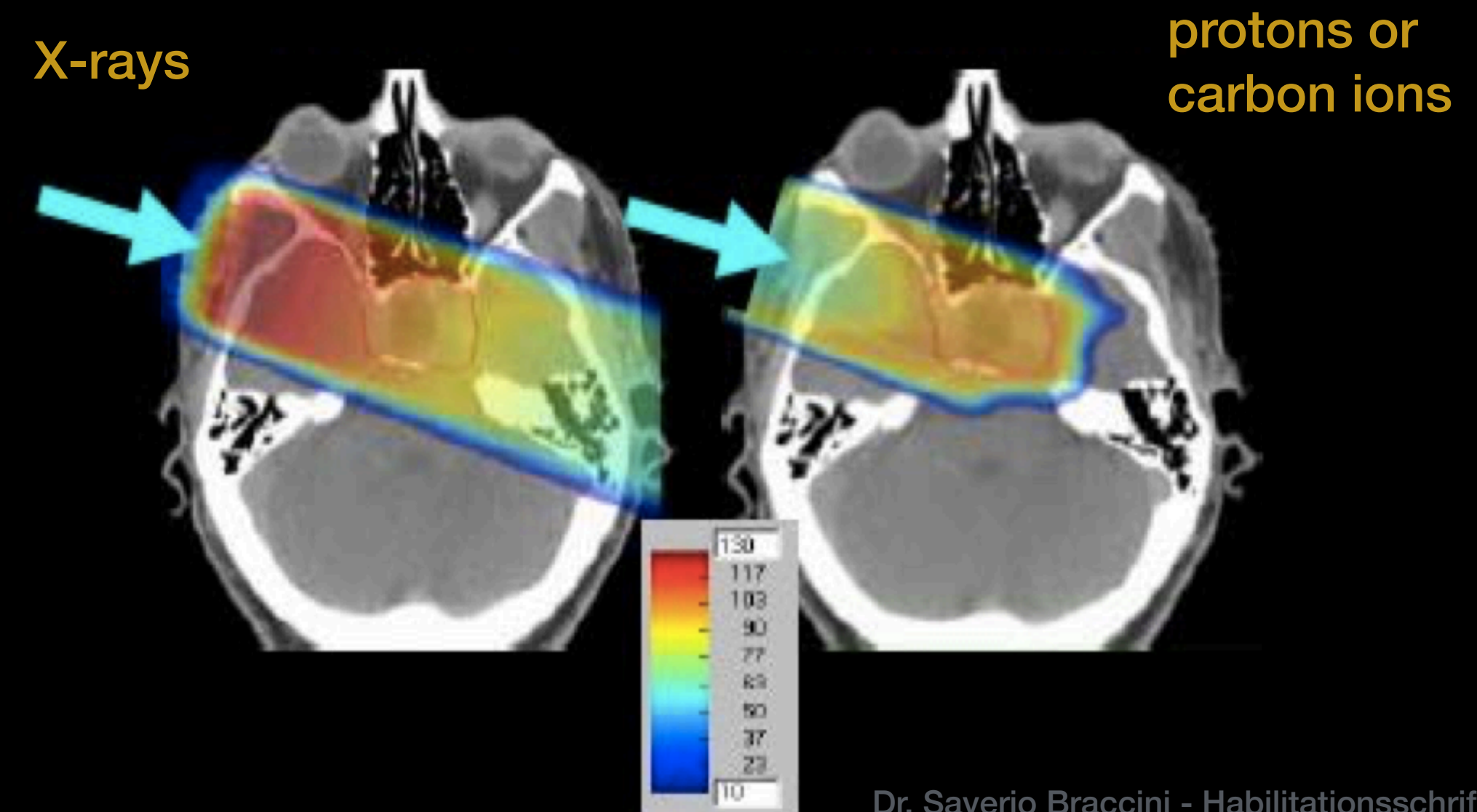
# Hadron Therapy - Basic Concept



Silvia Verdú Andrés - PhD Thesis



<https://www.klinikum.uni-heidelberg.de>

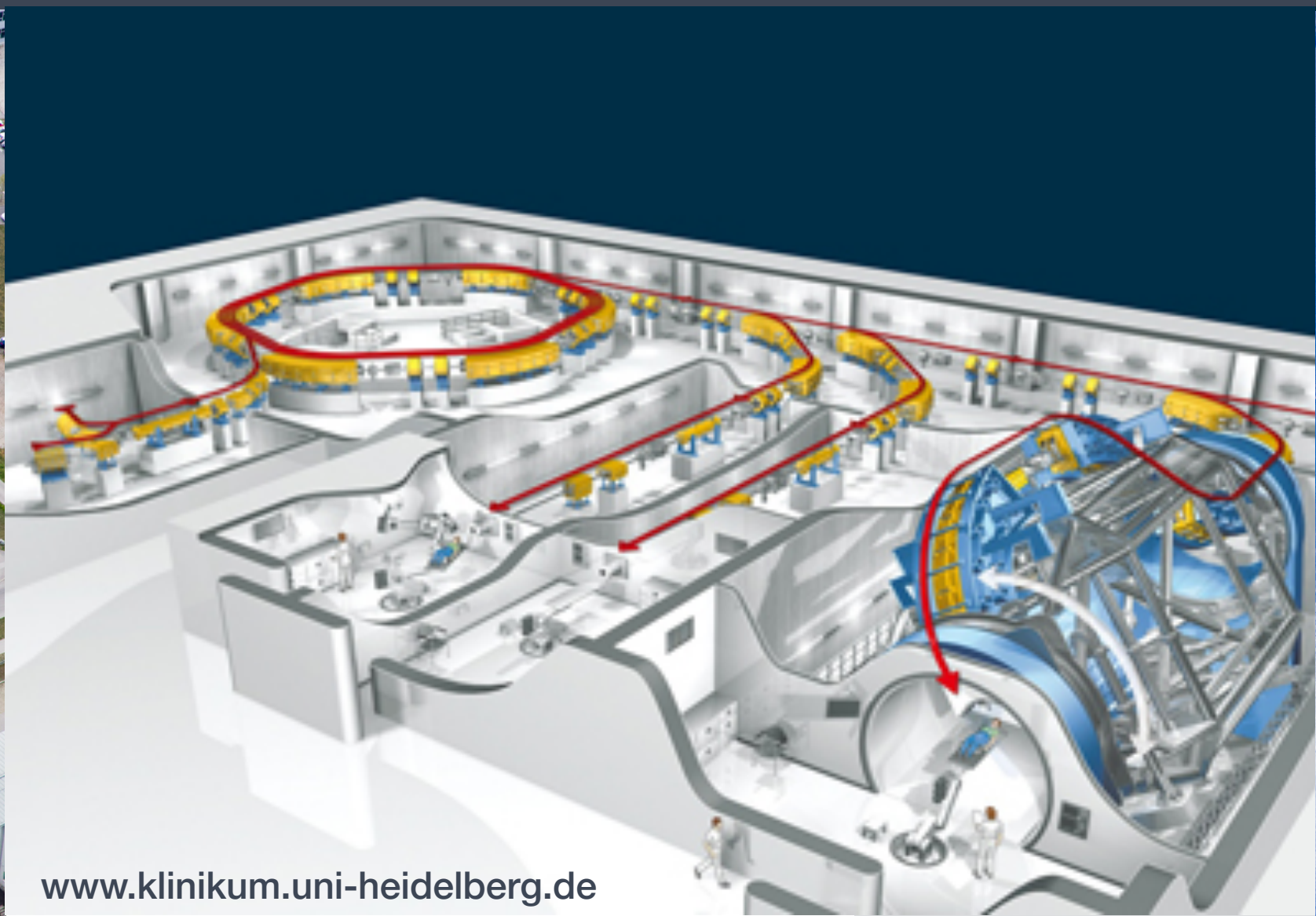


Dr. Saverio Braccini - Habilitationsschrift

# State of the Art Facilities



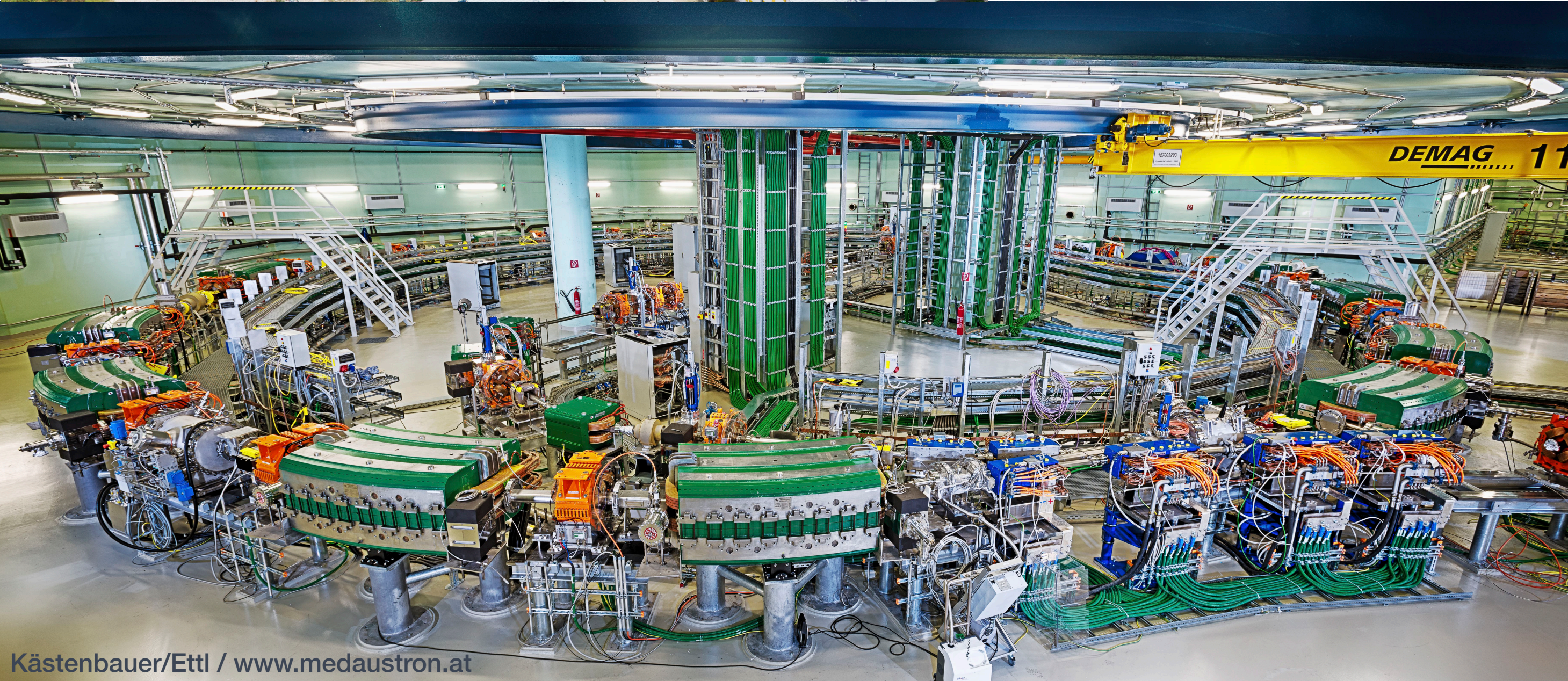
Jug Thule / [www.medaustron.at](http://www.medaustron.at)



[www.klinikum.uni-heidelberg.de](http://www.klinikum.uni-heidelberg.de)

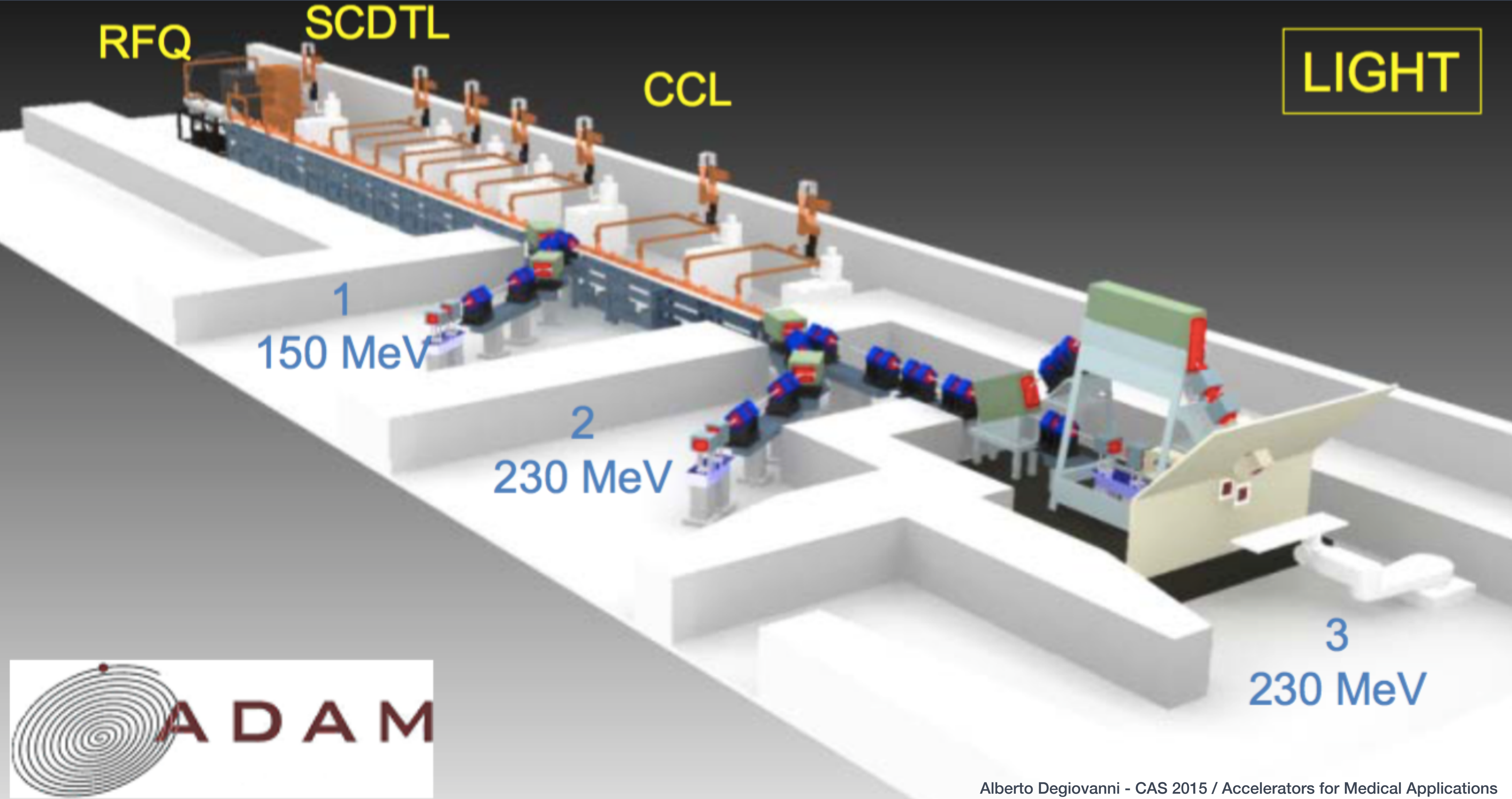


[www.klinikum.uni-heidelberg.de](http://www.klinikum.uni-heidelberg.de)



Kästenbauer/Ettl / [www.medaustron.at](http://www.medaustron.at)

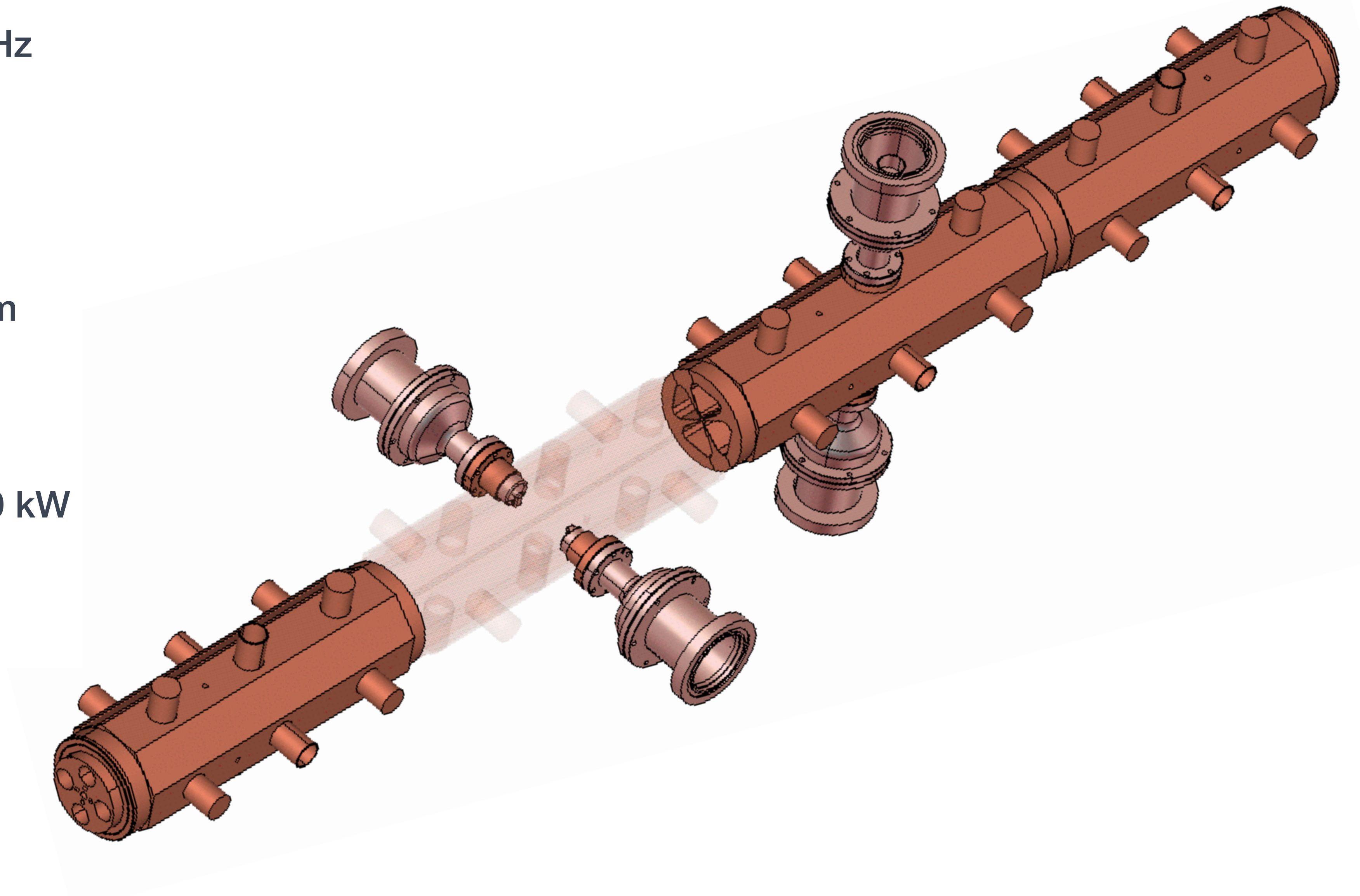
# ADAM - LIGHT



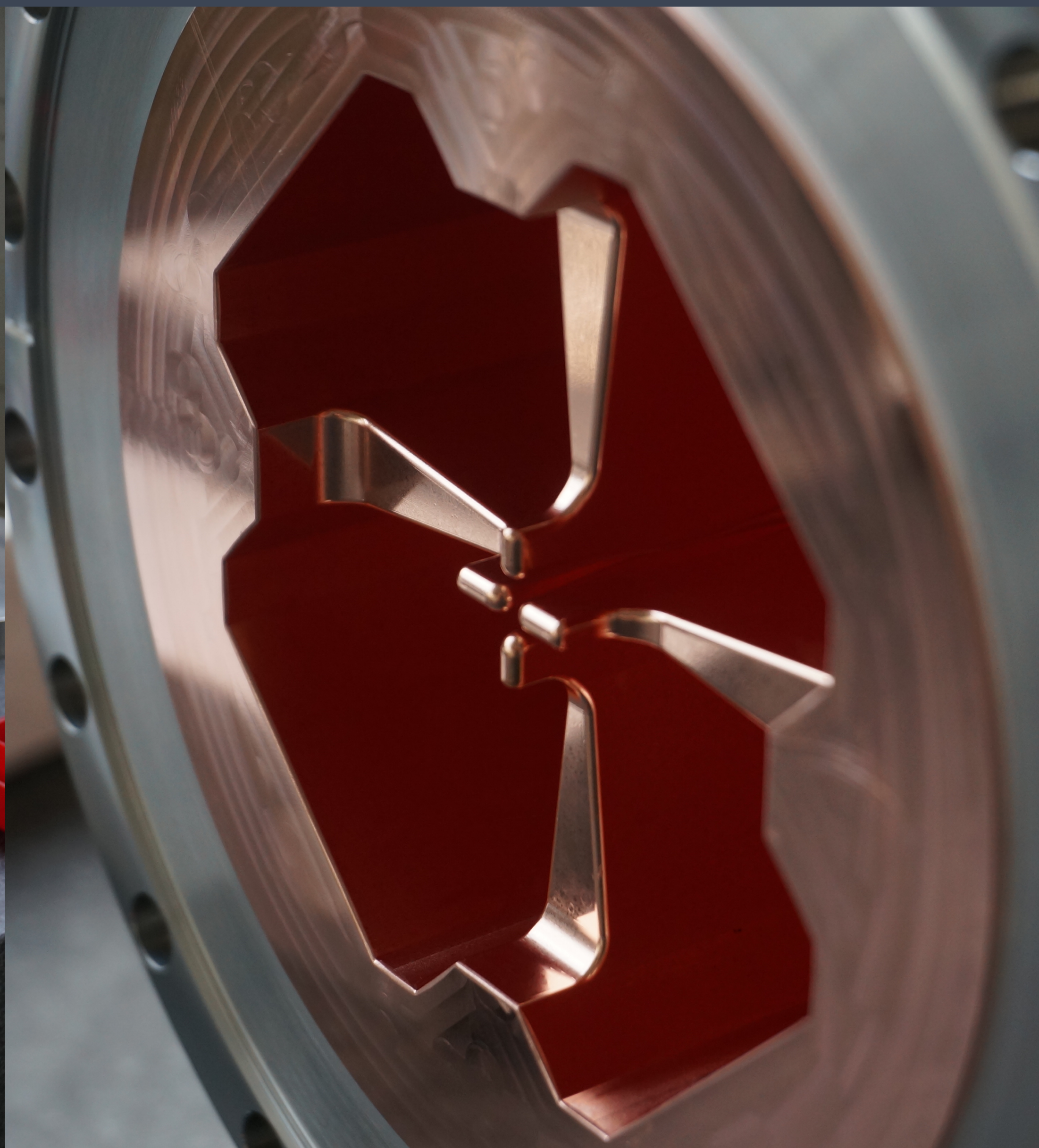
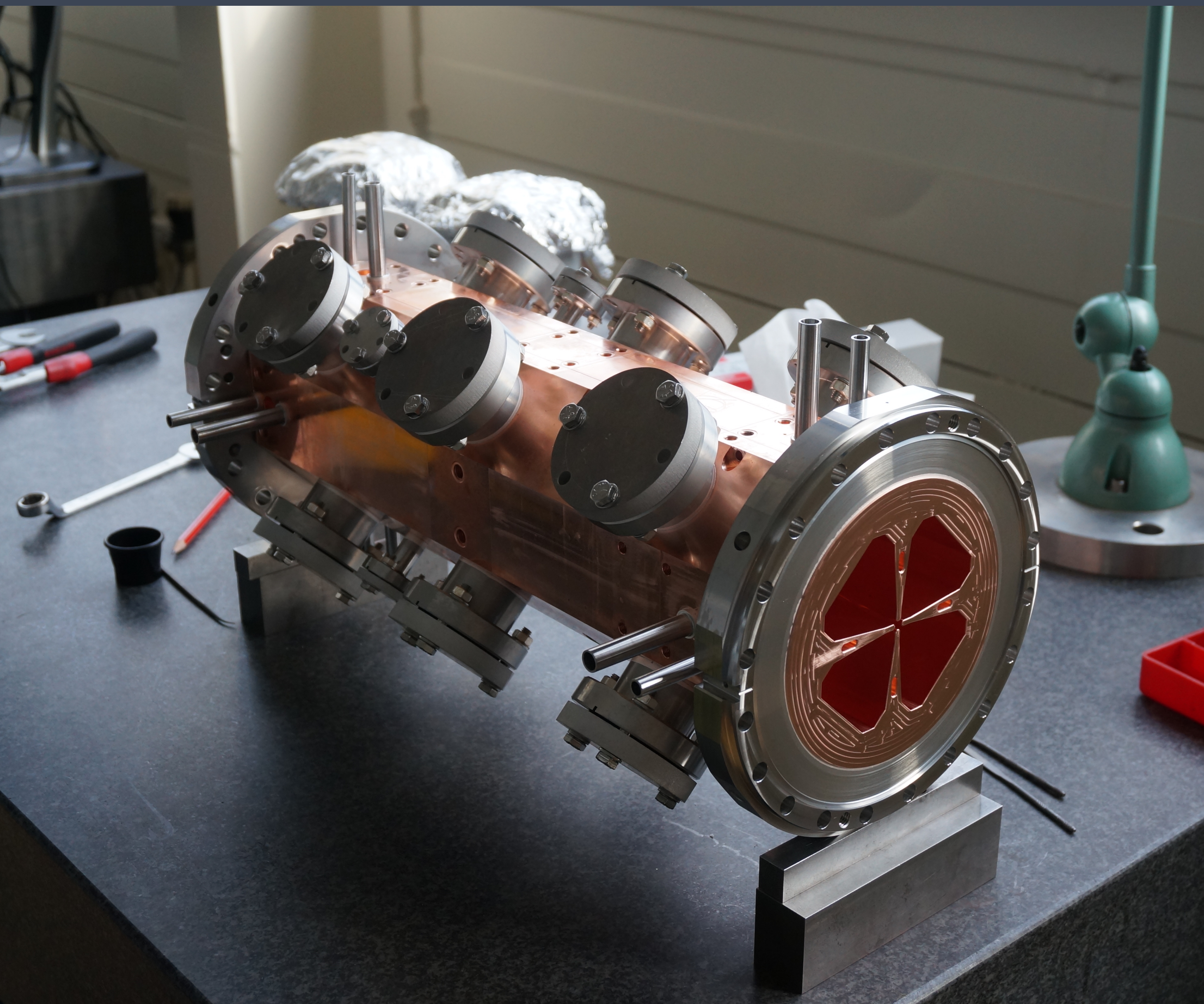
Alberto Degiovanni - CAS 2015 / Accelerators for Medical Applications

# 750 MHz RFQ

Frequency	750 MHz
Input Energy	40 keV
Output Energy	5 MeV
Length	2 m
Diameter	0.134 m
# Modules	4
# Tuners	32
Power Supply IOT	4 x 100 kW
# Power Couplers	4
# Pickup Antennas	16

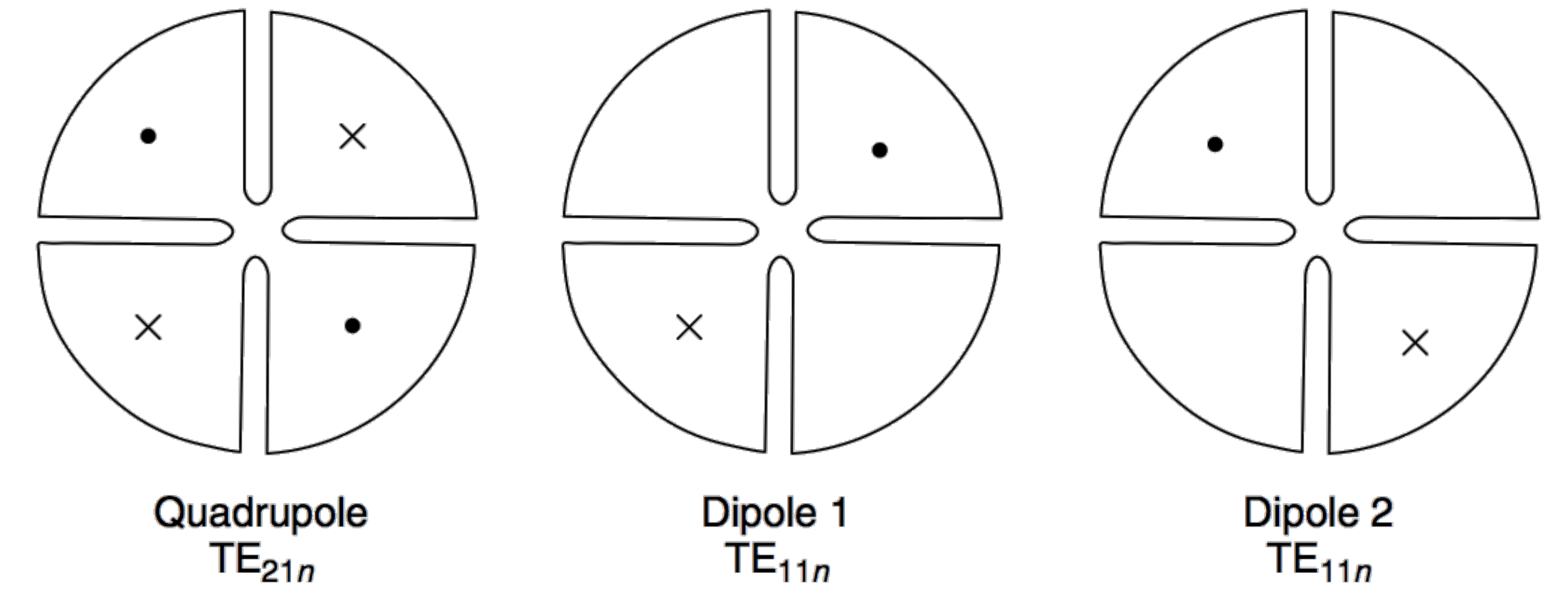
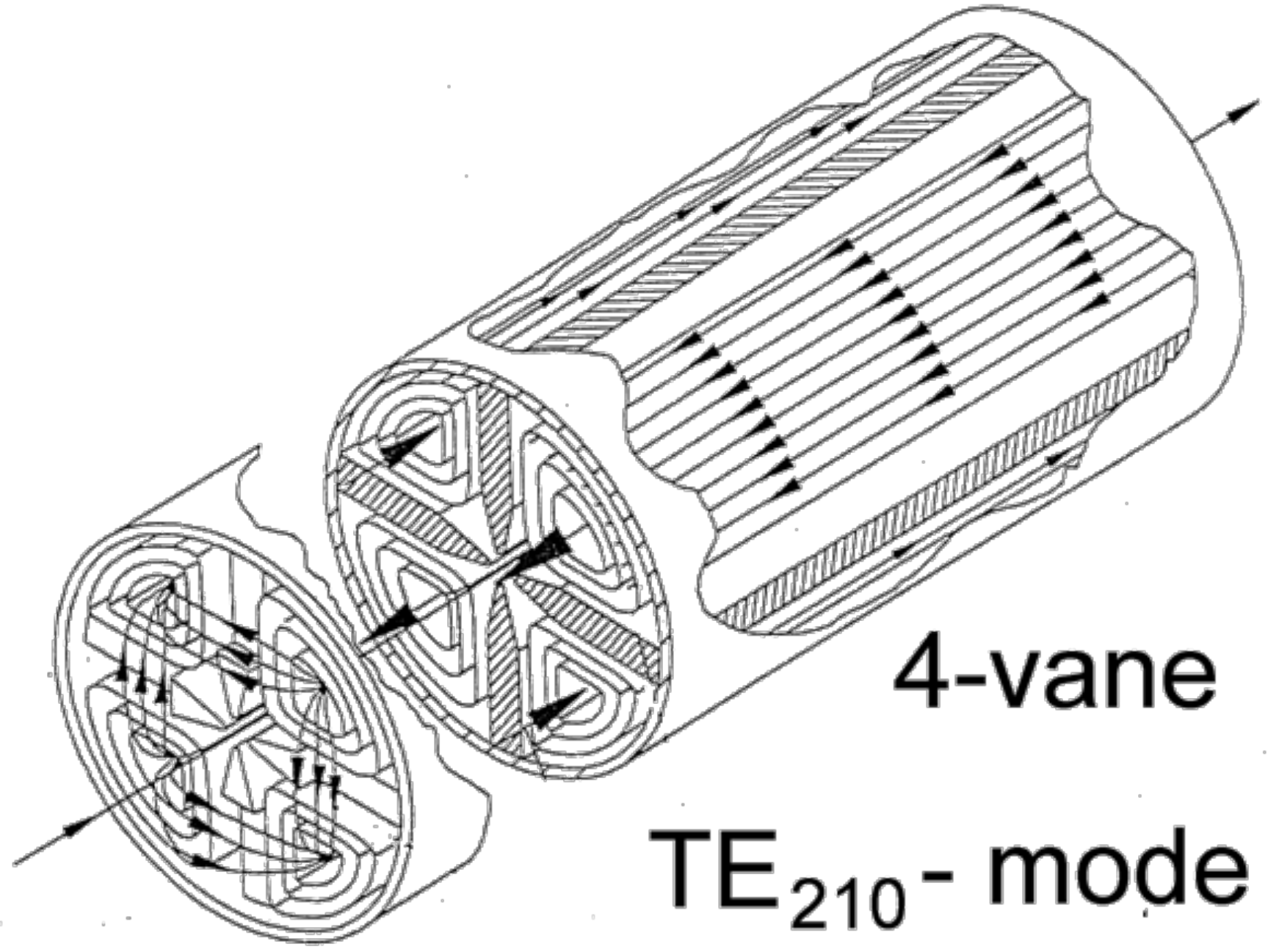


# Module Extremities





# 4-vane RFQ

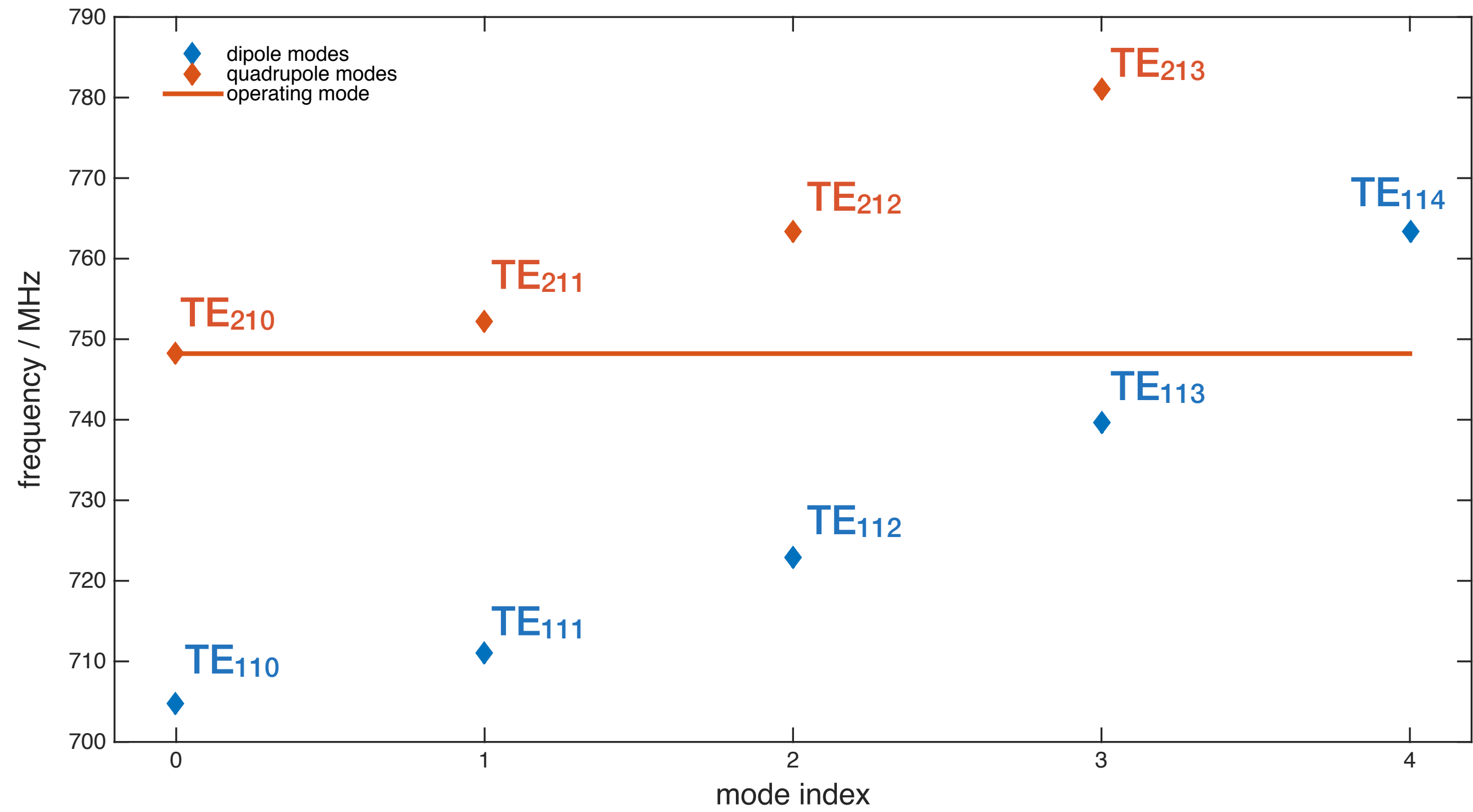


$$Q = (q_1 - q_2 + q_3 - q_4) / 4$$

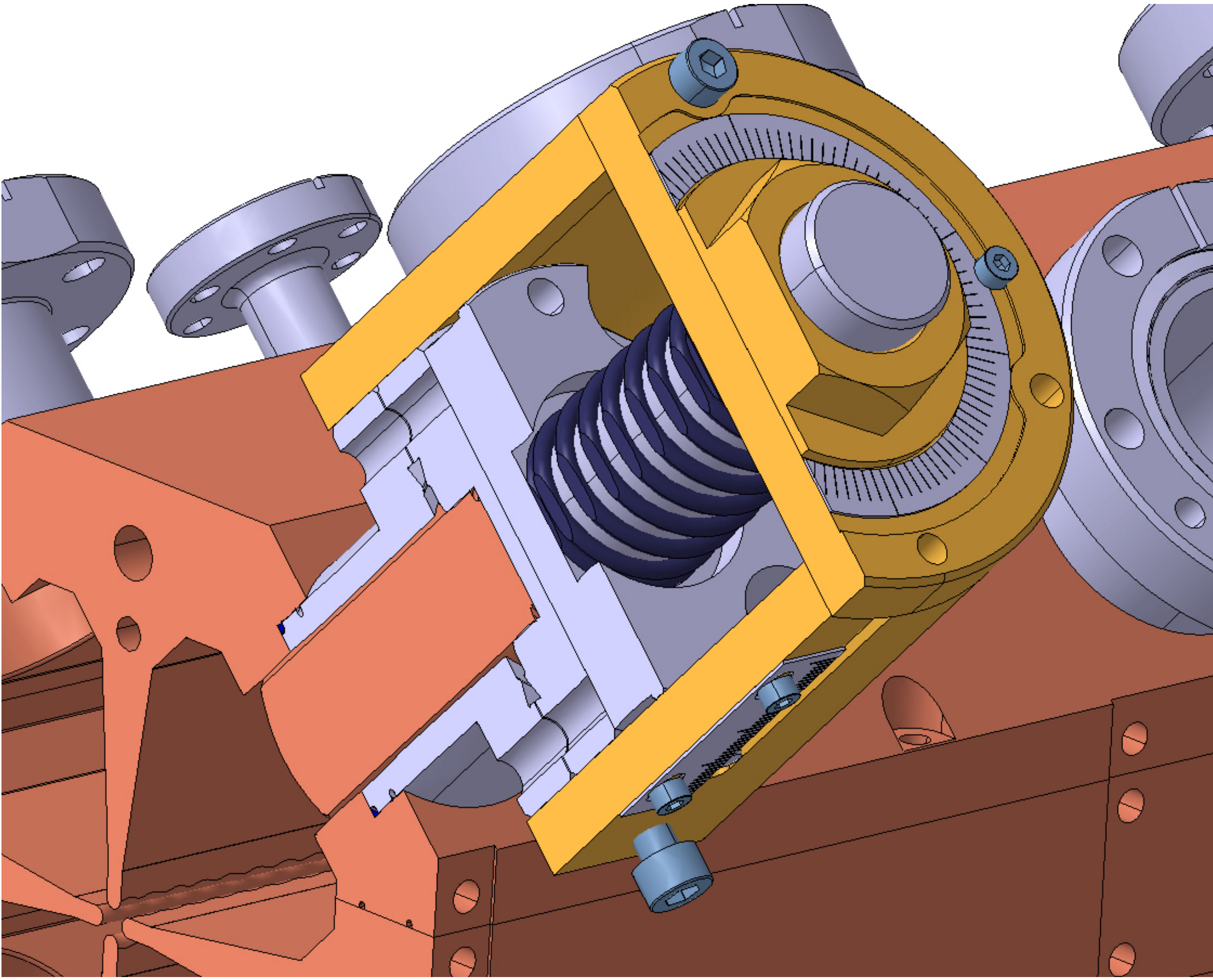
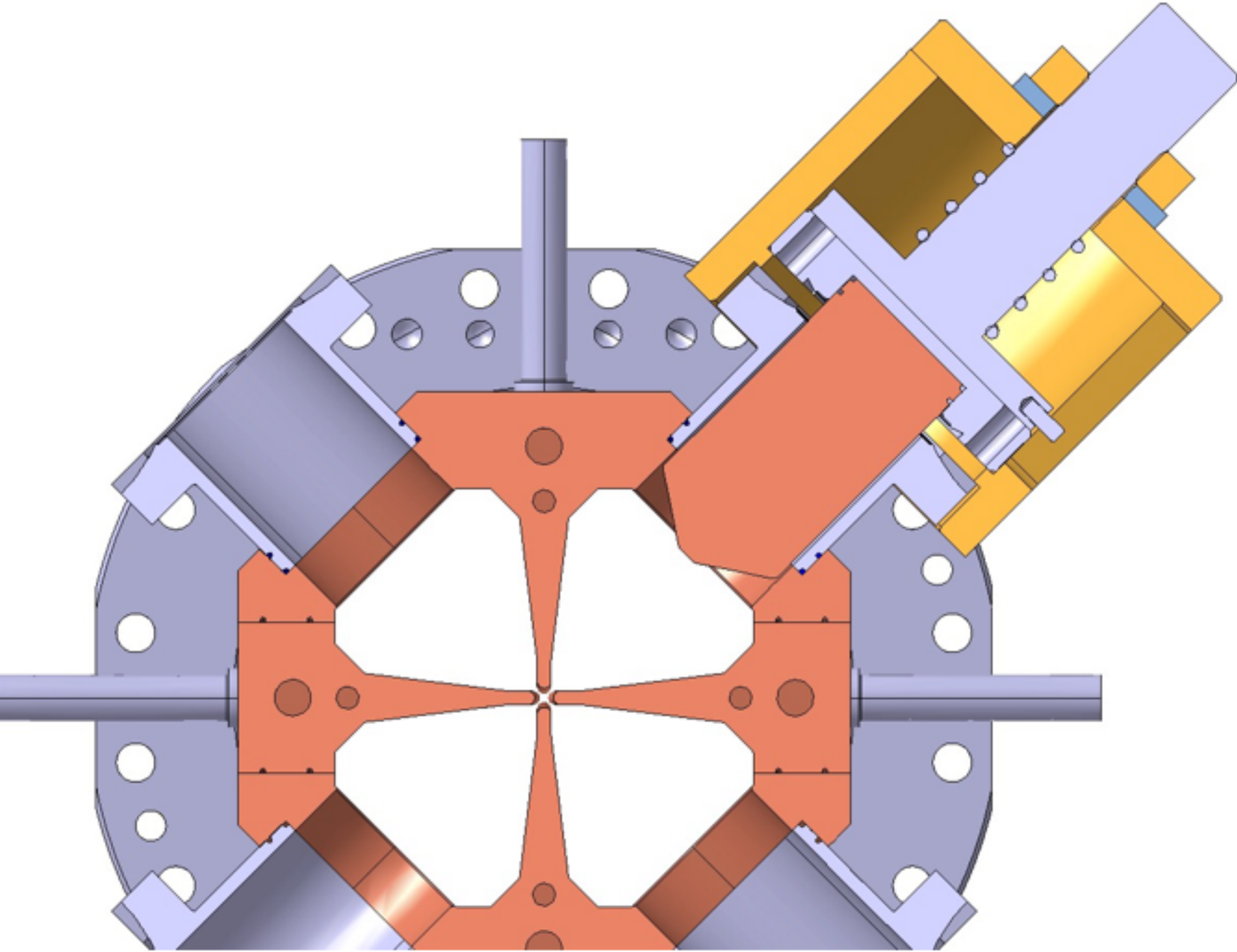
$$Ds = (q_1 + q_3) / 2$$

$$Dt = (q_2 + q_4) / 2$$

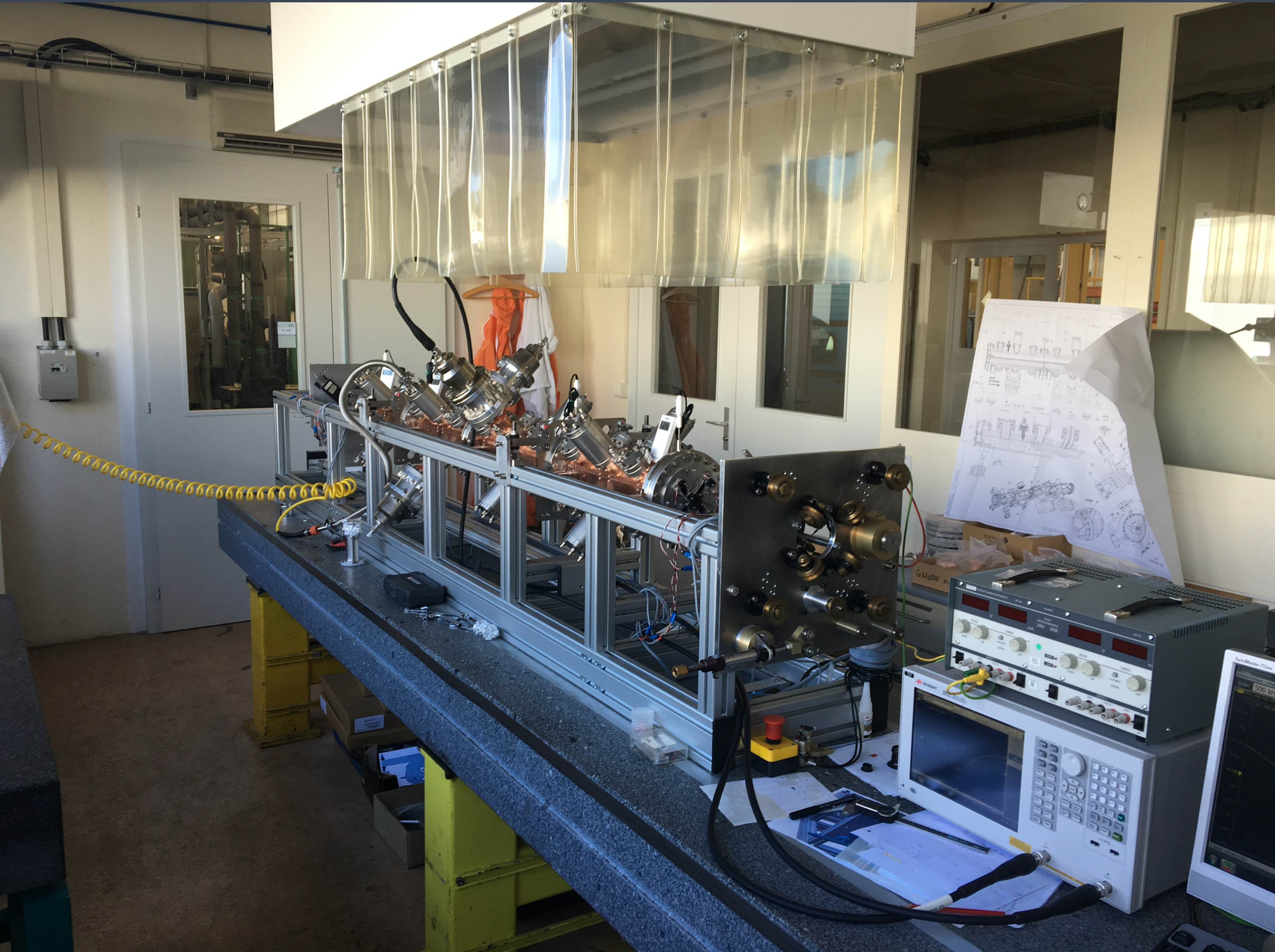
$$Ds = Dt = 0$$



# Tuner Tooling



# Bead Pull System



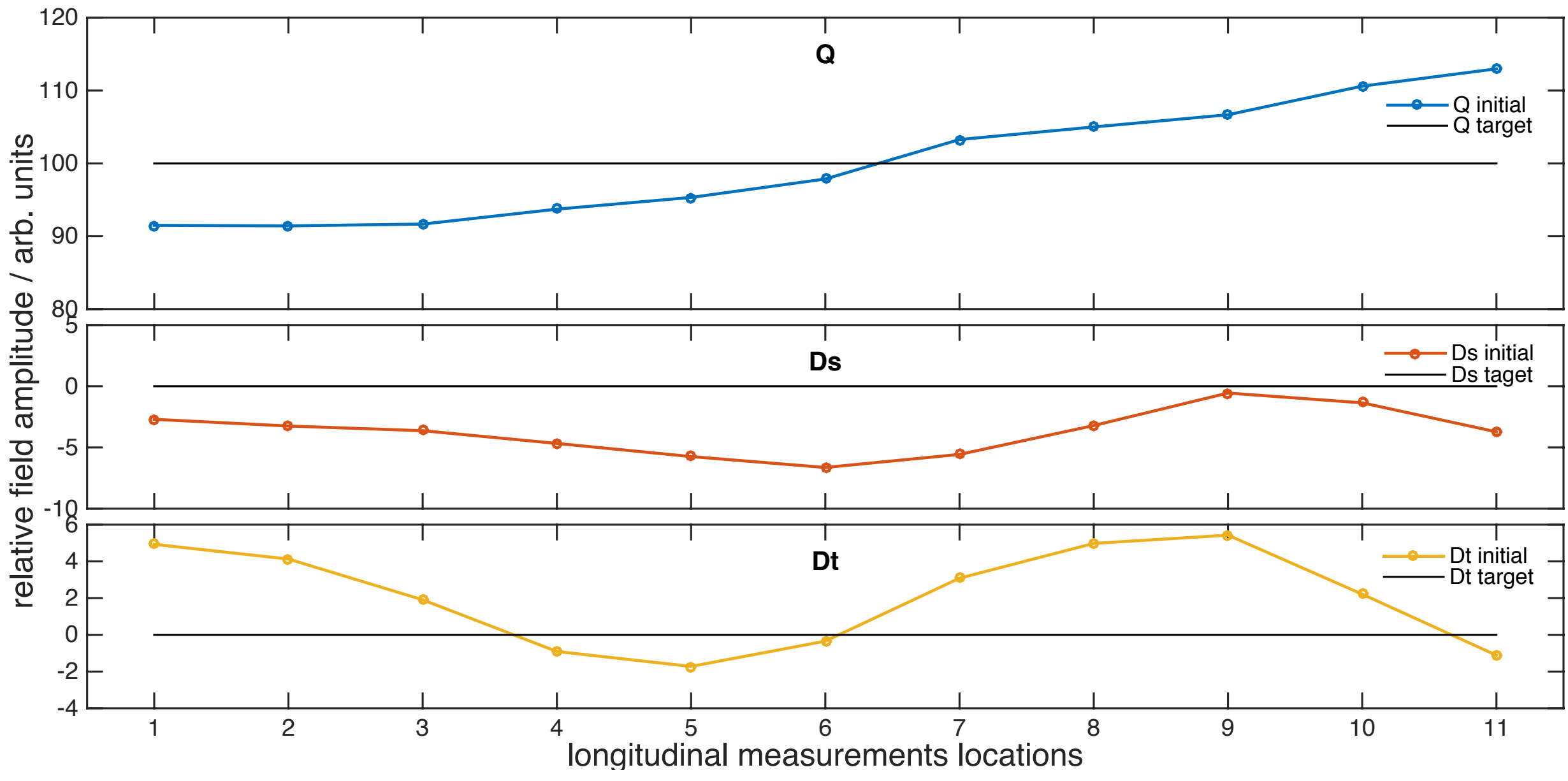
# Tuning Algorithm

$$Q = (q_1 - q_2 + q_3 - q_4)/4 = \text{const.}$$

$$Ds = (q_1 - q_3)/2 = 0$$

$$Dt = (q_2 - q_4)/2 = 0$$

$$\begin{bmatrix} 100 - V_1 \\ \vdots \\ 100 - V_{11} \\ 0 - V_{12} \\ \vdots \\ 0 - V_{22} \\ 0 - V_{23} \\ \vdots \\ 0 - V_{33} \end{bmatrix}$$



# Tuning Algorithm

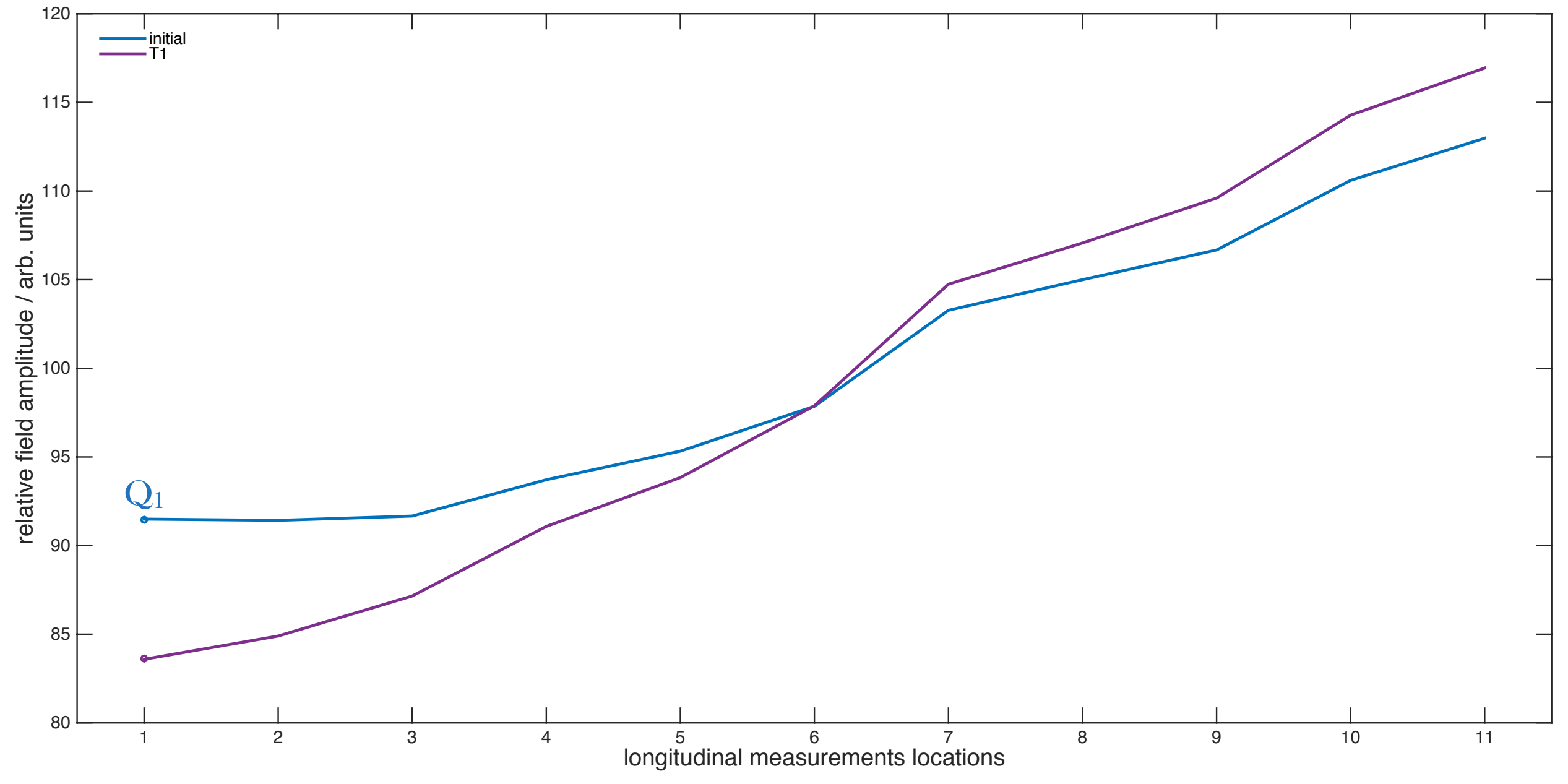
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$$\frac{\partial Q_1}{\partial T_1}$$



# Tuning Algorithm

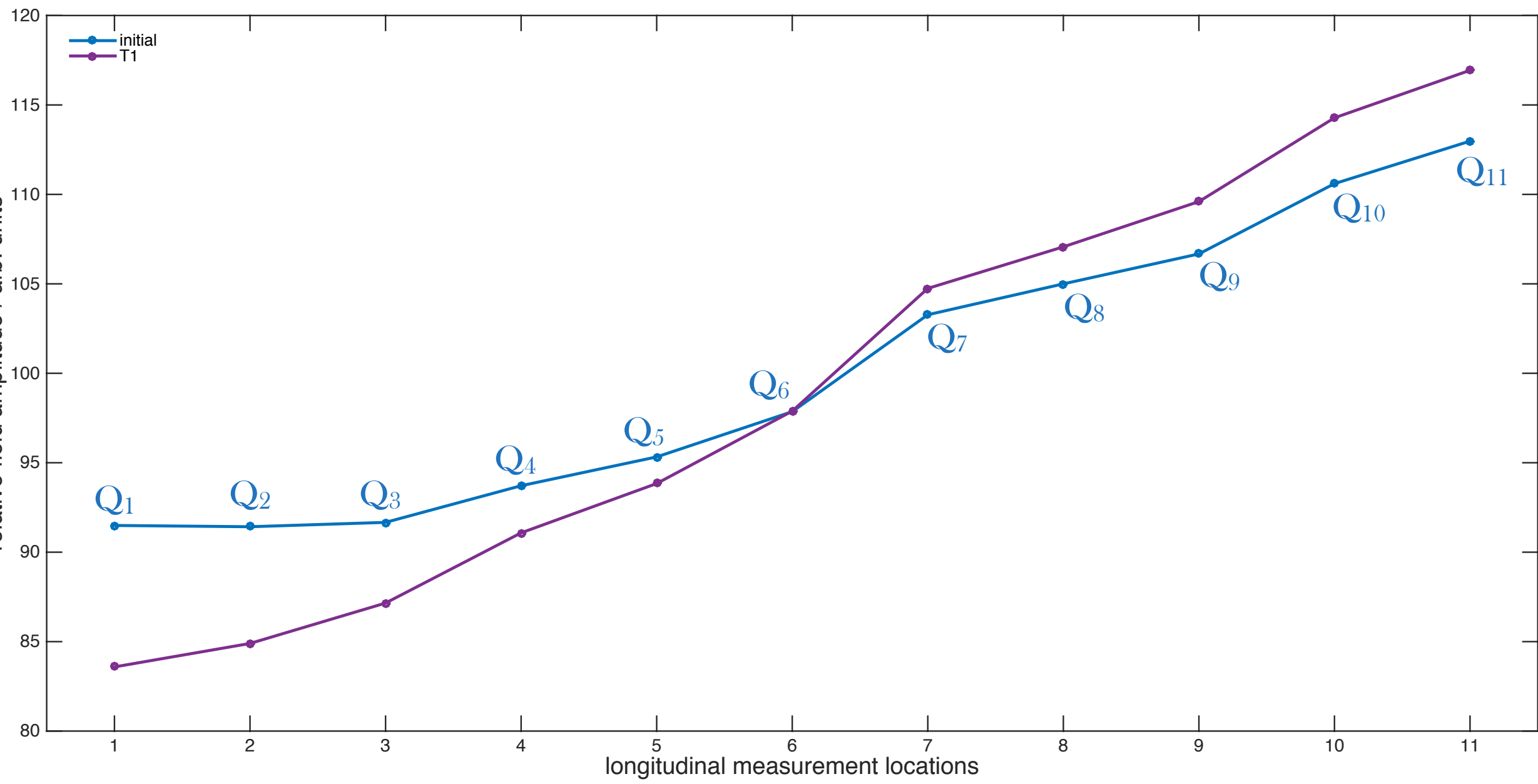
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$$\begin{bmatrix} \frac{\partial Q_1}{\partial T_1} \\ \vdots \\ \frac{\partial Q_{11}}{\partial T_1} \end{bmatrix}$$



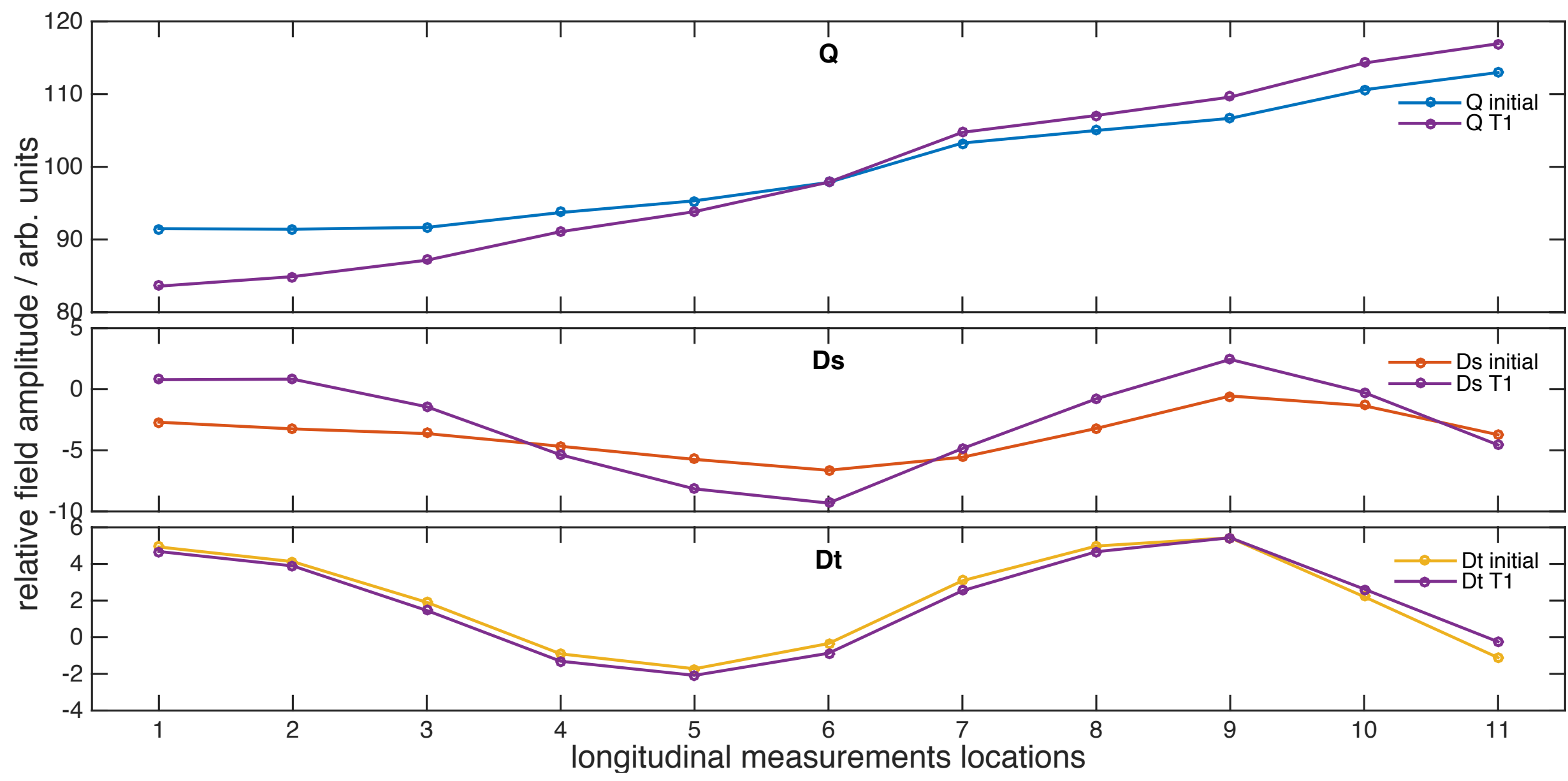
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$$\begin{bmatrix} 100 - V_1 \\ \vdots \\ 100 - V_{11} \\ 0 - V_{12} \\ \vdots \\ 0 - V_{22} \\ 0 - V_{23} \\ \vdots \\ 0 - V_{33} \end{bmatrix} \begin{matrix} \frac{\partial Q_1}{\partial T_1} \\ \vdots \\ \frac{\partial Q_{11}}{\partial T_1} \\ \frac{\partial Ds_1}{\partial T_1} \\ \vdots \\ \frac{\partial Ds_{11}}{\partial T_1} \\ \frac{\partial Dt_1}{\partial T_1} \\ \vdots \\ \frac{\partial Dt_{11}}{\partial T_1} \end{matrix}$$



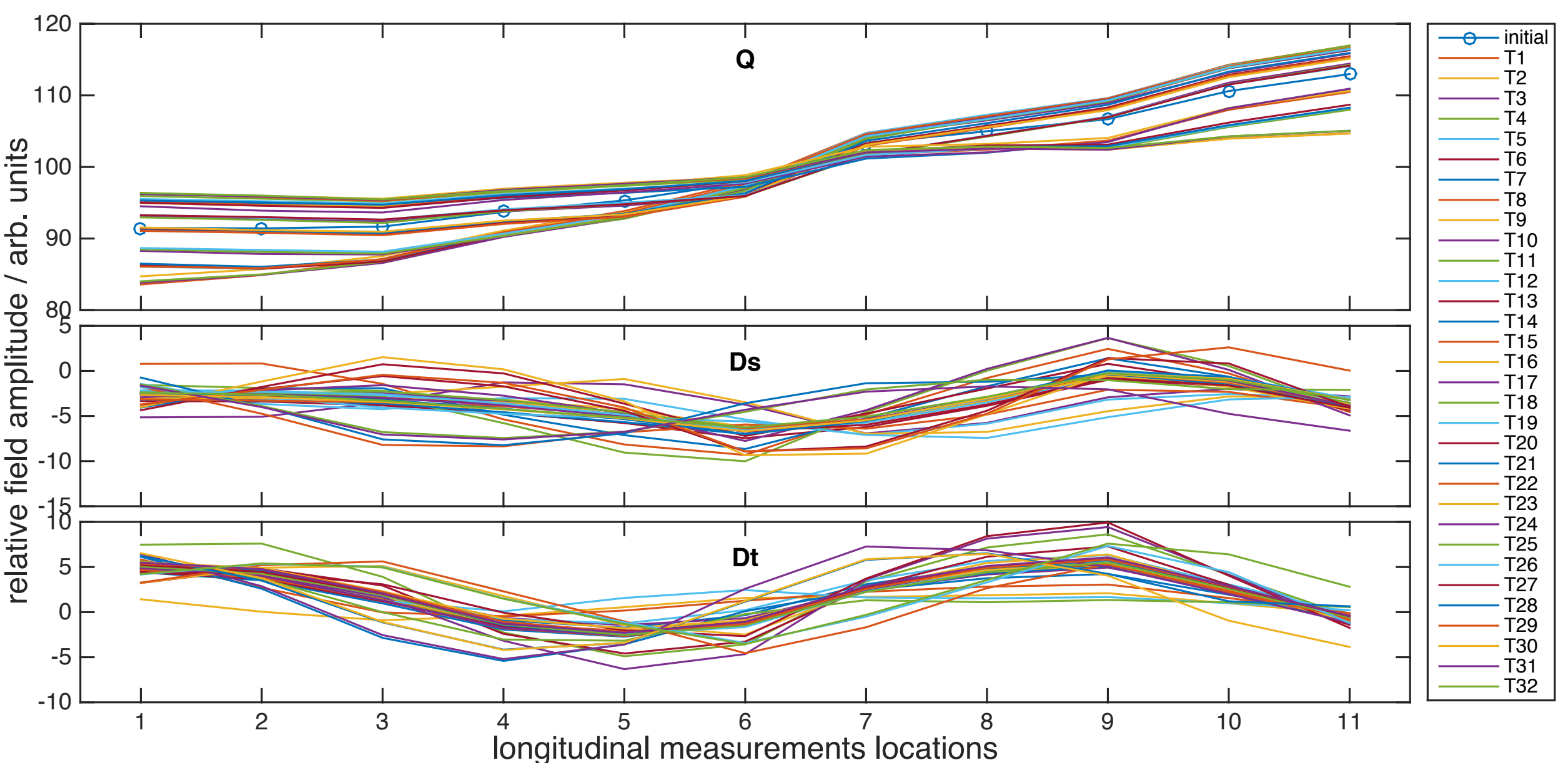
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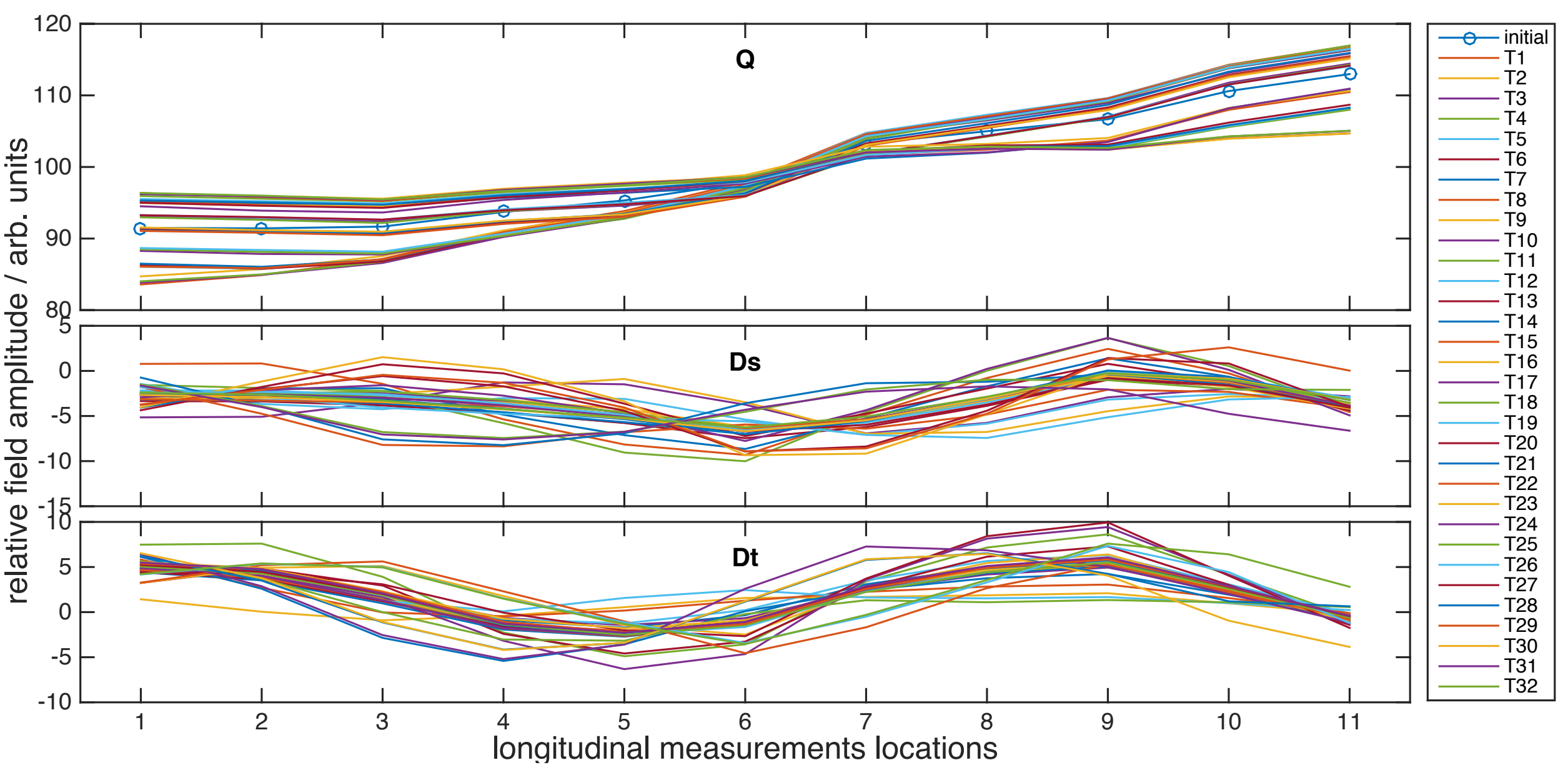
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$$\vec{V} = \mathbf{M} \cdot \vec{T}$$

$$\Downarrow$$

$$\vec{T} = \mathbf{M}^{-1} \cdot \vec{V}$$

# SVD - Singular Value Decomposition

$$\boxed{\vec{V}} = \mathbf{M} \cdot \vec{T}$$

$$\boxed{\vec{T}} = \mathbf{M}^{-1} \cdot \vec{V}$$

$$\mathbf{M}^{-1} = (\mathbf{U} \cdot \mathbf{S} \cdot \mathbf{V}^T)^{-1} \approx \mathbf{V} \cdot \mathbf{S}_0^{-1} \cdot \mathbf{U}^T$$

$$\mathbf{M} = \mathbf{U} \cdot \mathbf{S} \cdot \mathbf{V}^T$$

$$\begin{bmatrix} \cdot & \cdot & \cdot \\ \cdot & M & \cdot \\ \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \end{bmatrix} = \begin{bmatrix} \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & U & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \end{bmatrix} \begin{bmatrix} \sigma_1 \\ \sigma_2 \\ \sigma_3 \end{bmatrix} \begin{bmatrix} \cdot \\ \cdot \\ V^T \\ \cdot \\ \cdot \end{bmatrix}$$

$$\mathbf{S}_0^{-1} = \begin{cases} 1/\sigma_i & \text{if } \sigma_i > t \\ 0 & \text{otherwise} \end{cases}$$

$$\mathbf{S} = \text{diag}(\sigma_1, \sigma_2, \dots, \sigma_n)$$

$$\sigma_1 \geq \sigma_2 \geq \dots \geq \sigma_n$$

$$\boxed{\vec{T}_{svdi}} = \overbrace{(\mathbf{V} \cdot \mathbf{S}_i^{-1} \cdot \mathbf{U}^T)}^{\mathbf{M}_i^{-1}} \cdot \vec{V}$$

$$\boxed{\vec{V}} \approx \vec{V}_{svdi} = \mathbf{M} \cdot \vec{T}_{svdi}$$

$$\mathbf{S}^{-1} = \begin{bmatrix} 1/\sigma_1 & & & & \\ & 1/\sigma_2 & & & \\ & & \ddots & & \\ & & & & 1/\sigma_n \end{bmatrix}$$

$$\mathbf{M}^{-1} = \mathbf{V} \cdot \mathbf{S}^{-1} \cdot \mathbf{U}^T$$

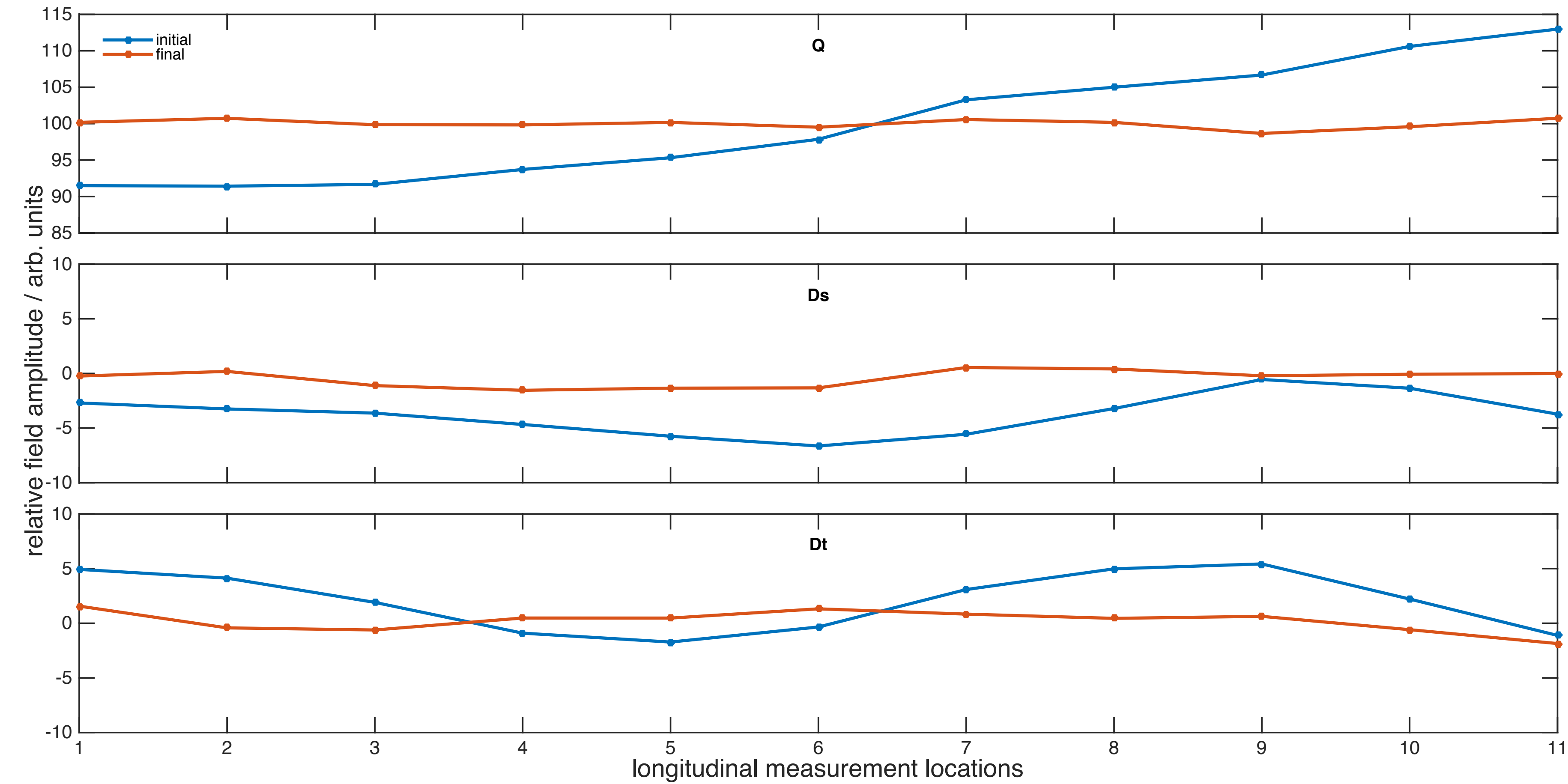
# Results

Component      Q      Ds      Dt

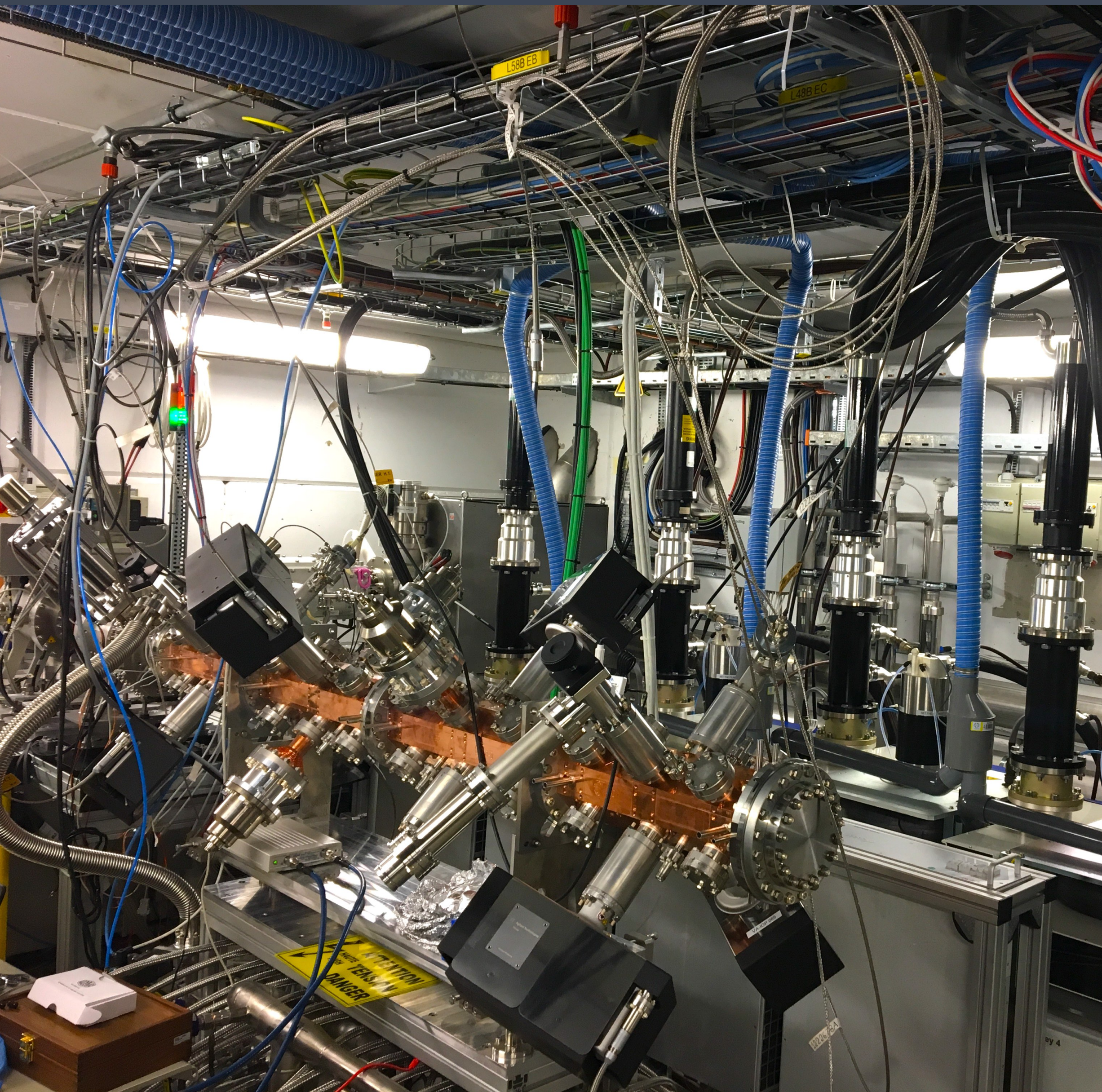
**Initial**     $\pm 10.8\%$      $\pm 3.0\%$      $\pm 3.6\%$

**Target**       $\pm 2\%$        $\pm 2\%$        $\pm 2\%$

**Final**       $\pm 1.0\%$        $\pm 1.0\%$        $\pm 1.7\%$



# Status



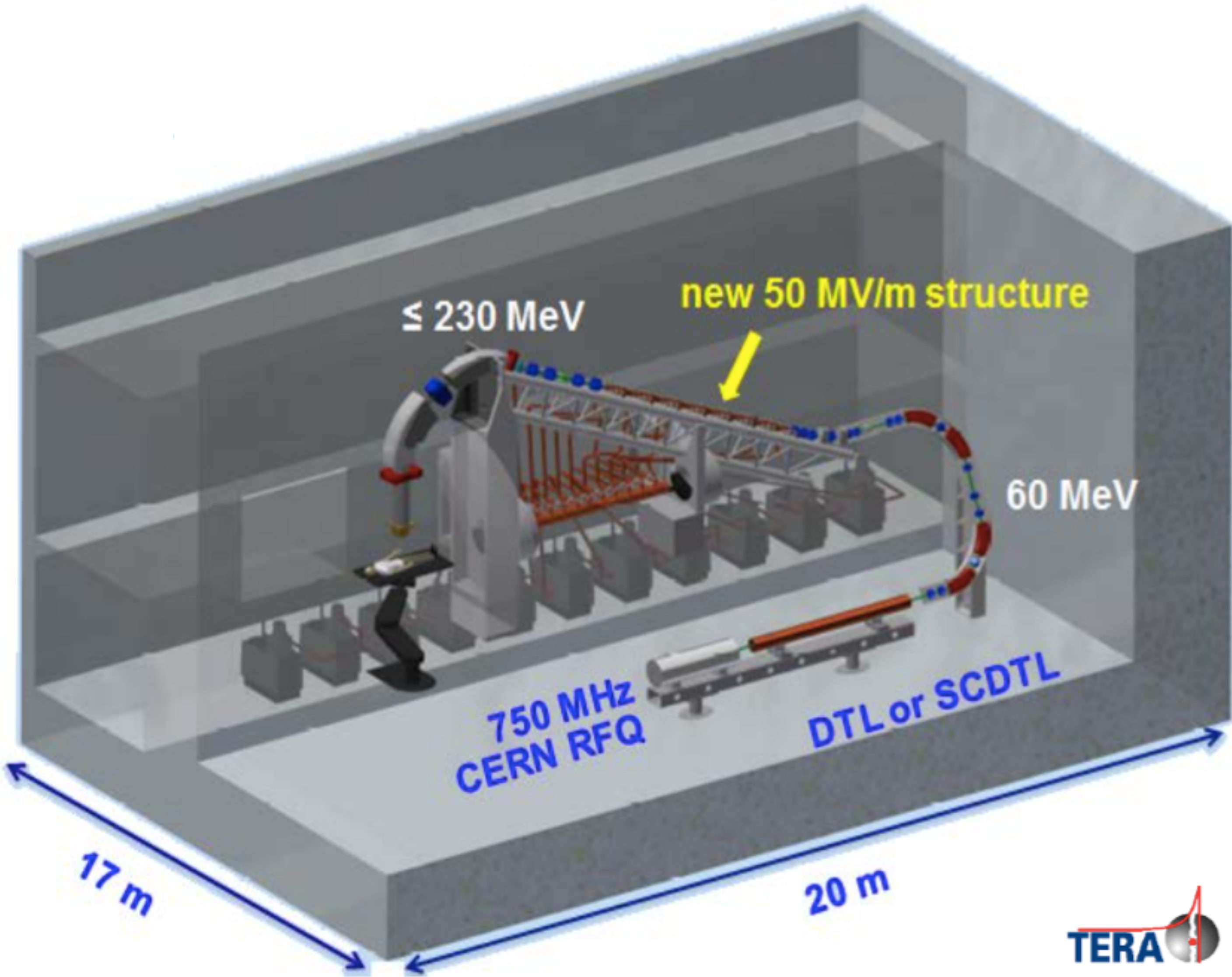
- tuning of 4-vane RFQs
  - tuning algorithm / matrix inversion SVD
  - tuning procedure / tuner tooling
- frequency tuning
- Q-values (multiple power couplers)
- antenna calibration

# Status



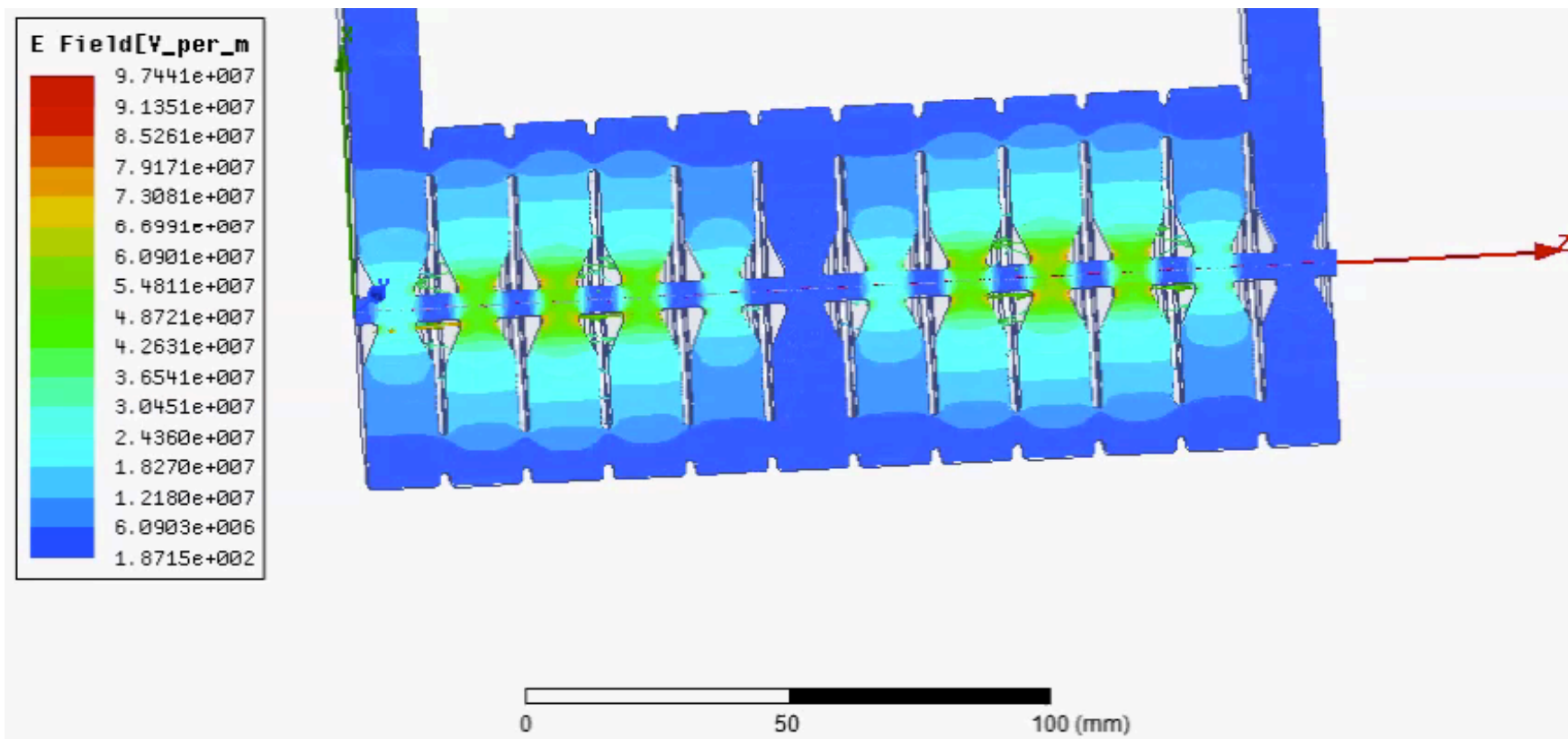
- tuning of 4-vane RFQs
    - tuning algorithm / matrix inversion SVD
    - tuning procedure / tuner tooling
  - frequency tuning
  - Q-values (multiple power couplers)
  - antenna calibration
- 
- RFQ does accelerate protons to 5 MeV
  - measured transverse beam properties match expectations from simulations

# Tera Foundation - TULIP



short linac requires  
high gradient & high frequency

- 3 GHz BTW structure
- max gradient of about 50 MV/m
- 20 cm long structure
- 10 MeV energy gain



# S-Band BTW Structure - Conditioning

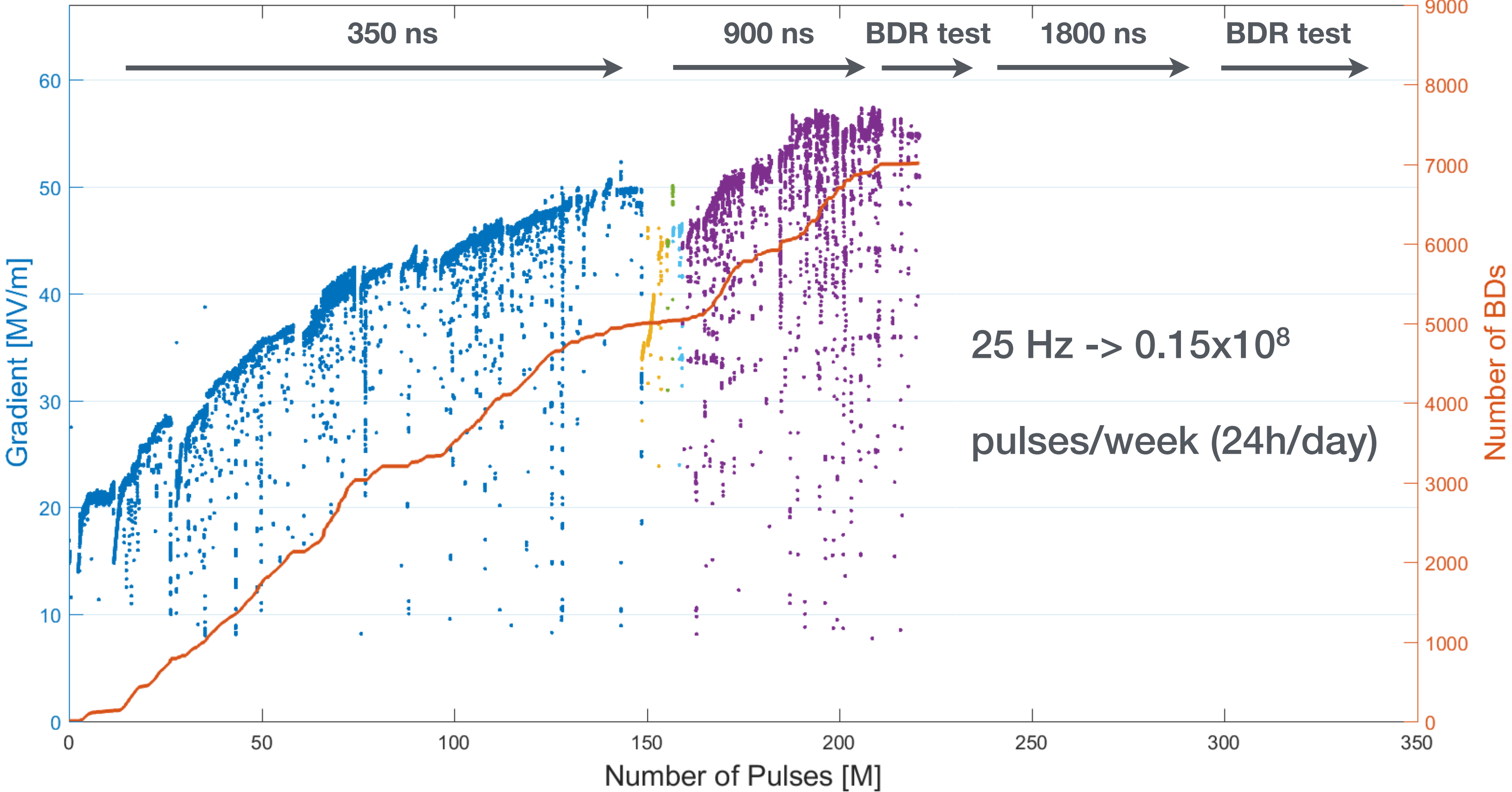


Stefano Benedetti

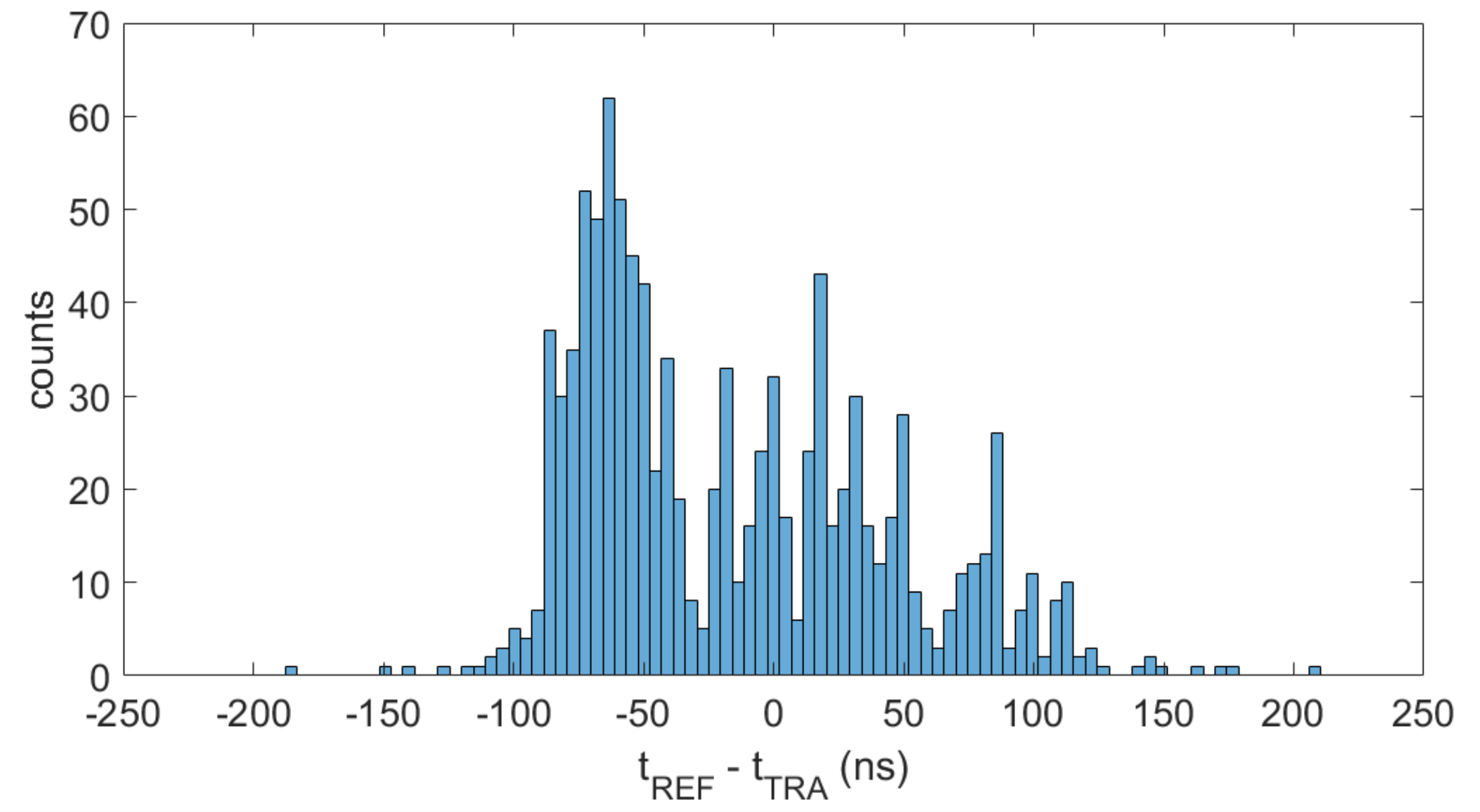
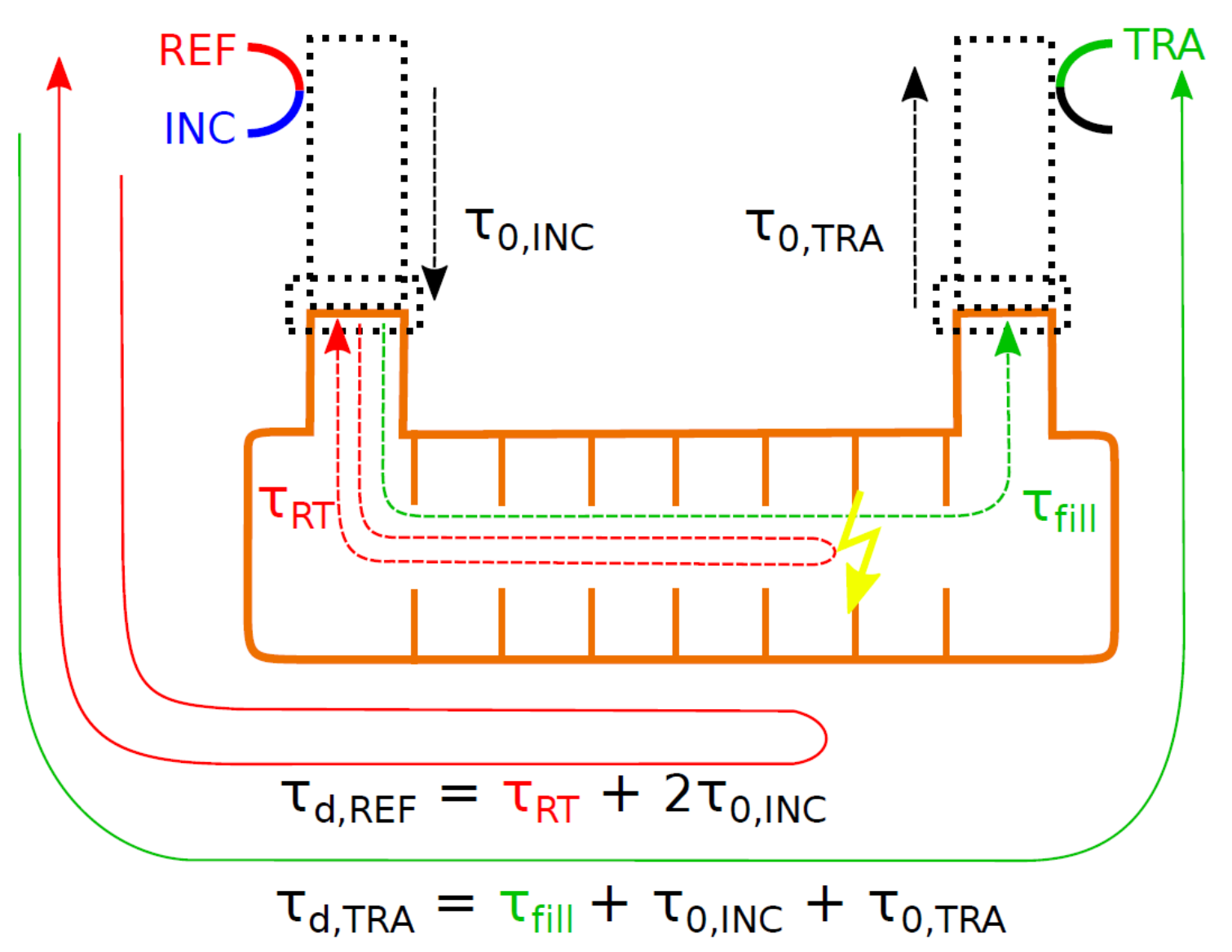
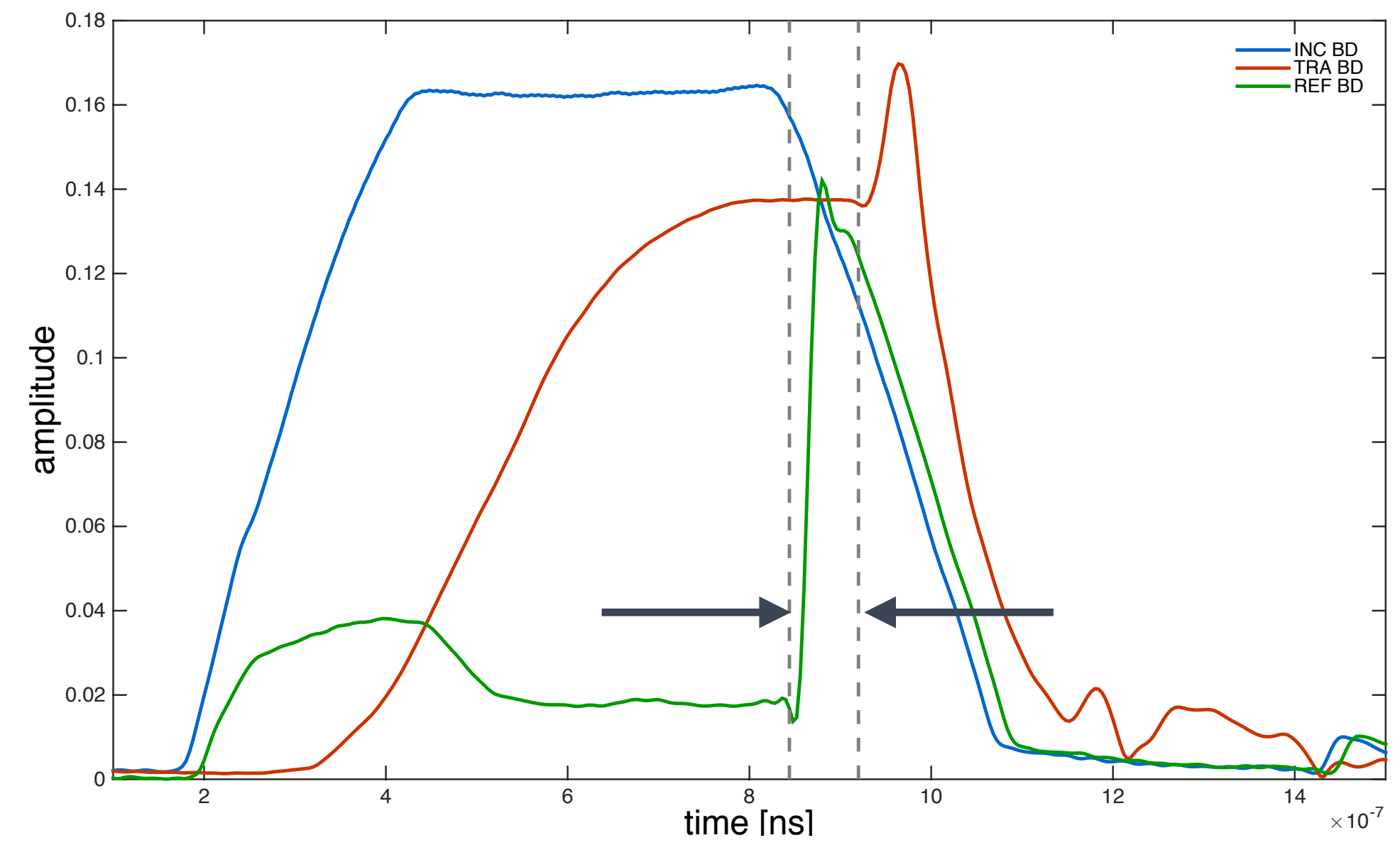
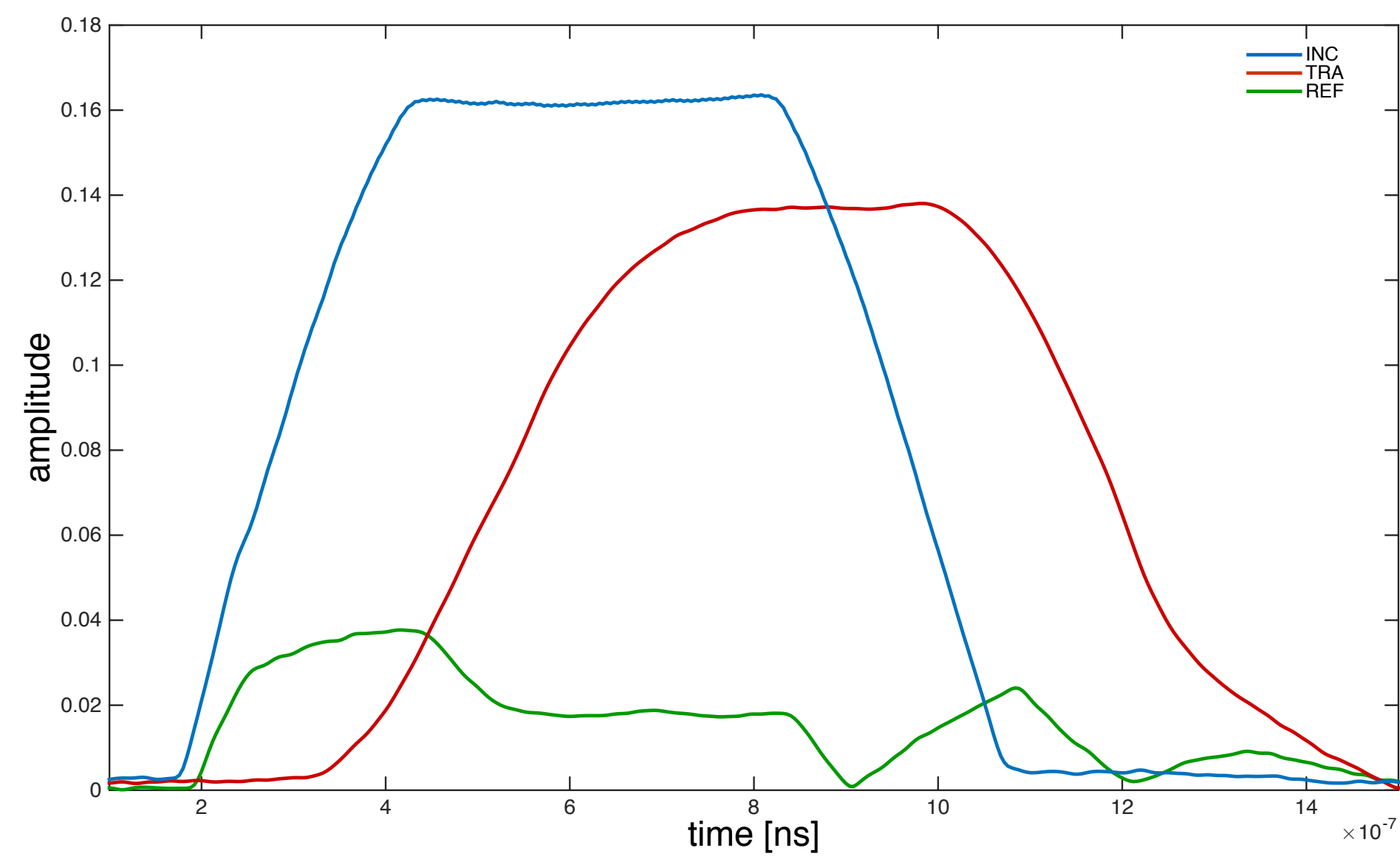
Conditioning of the structure  
Breakdown studies  
Data analysis



define high gradient  
limits of S-band cavities  
in terms of BDs



# S-Band BTW - breakdown location



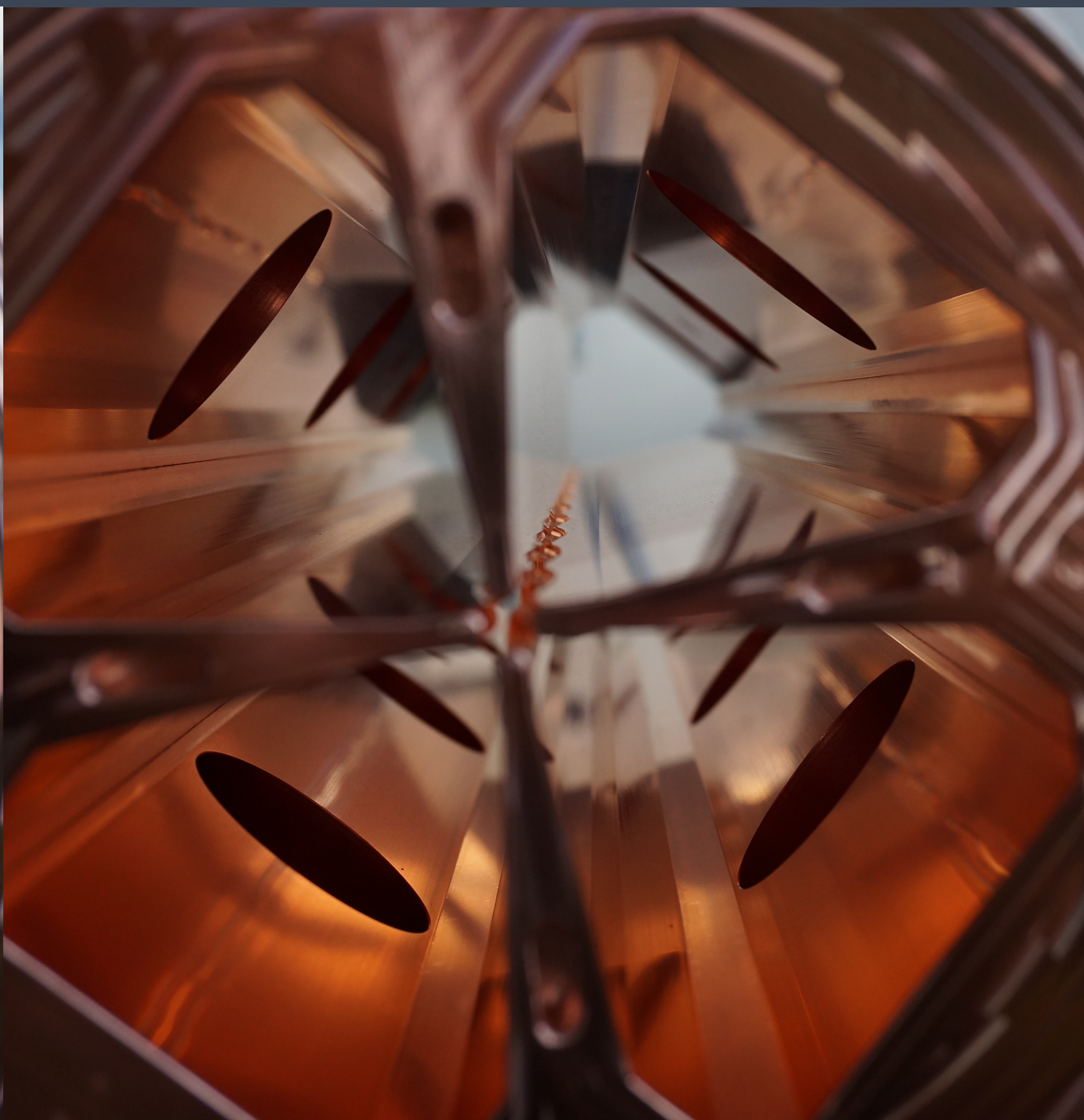


Thank you very much  
for your attention!



# Extra Slides

# Modulation

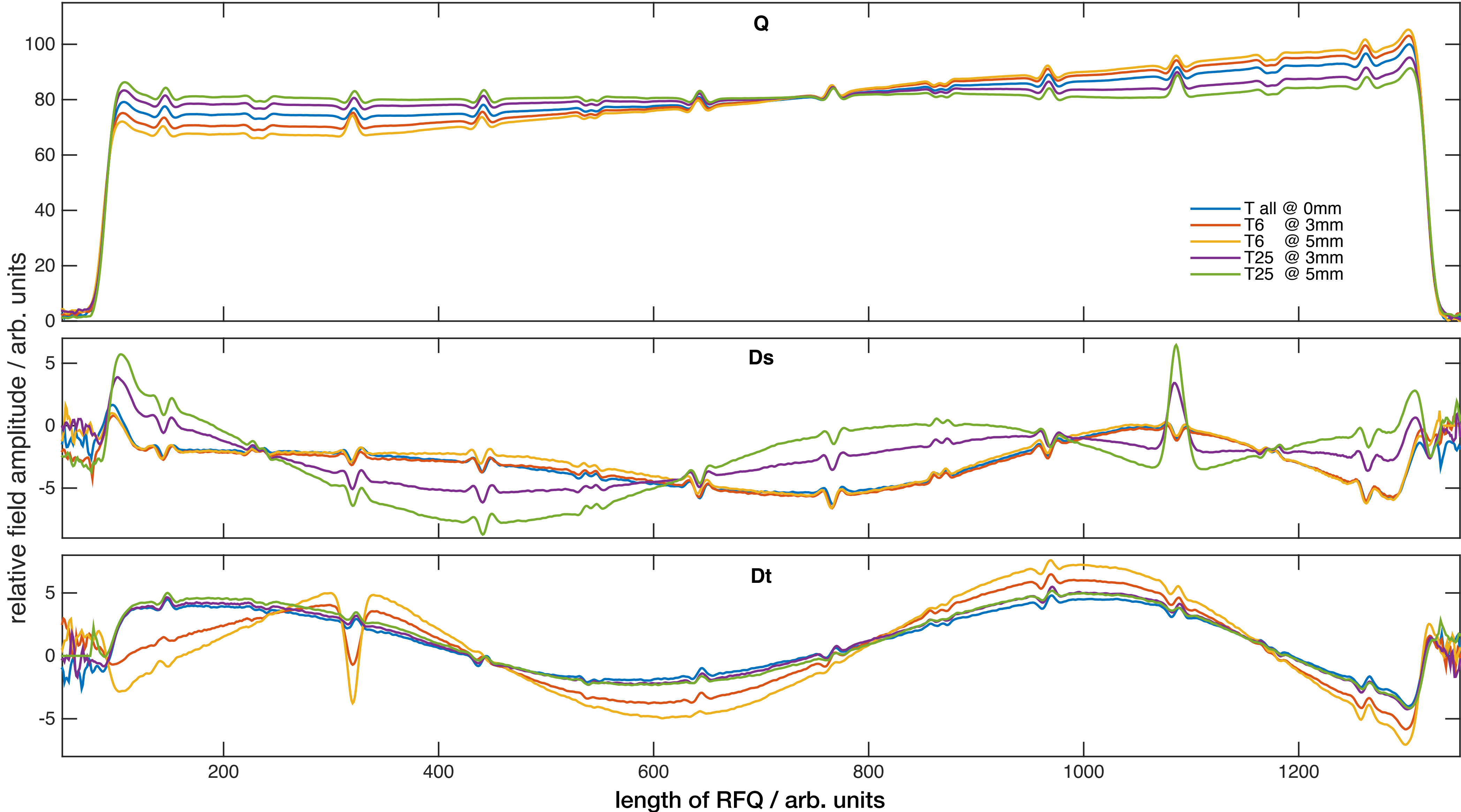


# Other Applications

<b>Application</b>	<b>Hadrontherapy Injector</b>	<b>Compact PET Isotope Production</b>	<b>99mTc &amp; Brachytherapy Production</b>	<b>IBA Ion Beam Analysis</b>
<b>General Design</b>	1 RFQ (4 modules)	2 RFQ	2 RFQ + 1 DTL	1 RFQ
<b>Particles</b>	p+	p+	p+ / d+ / $\alpha$	p+ / $\alpha$
<b>Frequency</b>	750 MHz	750MHz	704 MHz	750 MHz
<b>Output Energy</b>	5 MeV	10 MeV	18 MeV	3 MeV
<b>Total Length</b>	2 m	4 m	10 m	1 m
<b>Peak Power</b>	400 kW	800 kW	1.5 MW	average current 0.1 mA
<b>RF system</b>	IOT (x4)	solid state amplifier / magnetron	klystrons	

# Tuner Influence on Different Components

T6 → q2  
T25 → q1



# SVD - Singular Value Decomposition

- T1
- T2
- T3
- T4
- T5
- T6
- T7
- T8
- T9
- T10
- T11
- T12
- T13
- T14
- T15
- T16
- T17
- T18
- T19
- T20
- T21
- T22
- T23
- T24
- T25
- T26
- T27
- T28
- T29
- T30
- T31
- T32

$$\vec{V}_{svdi} \approx \vec{V}$$

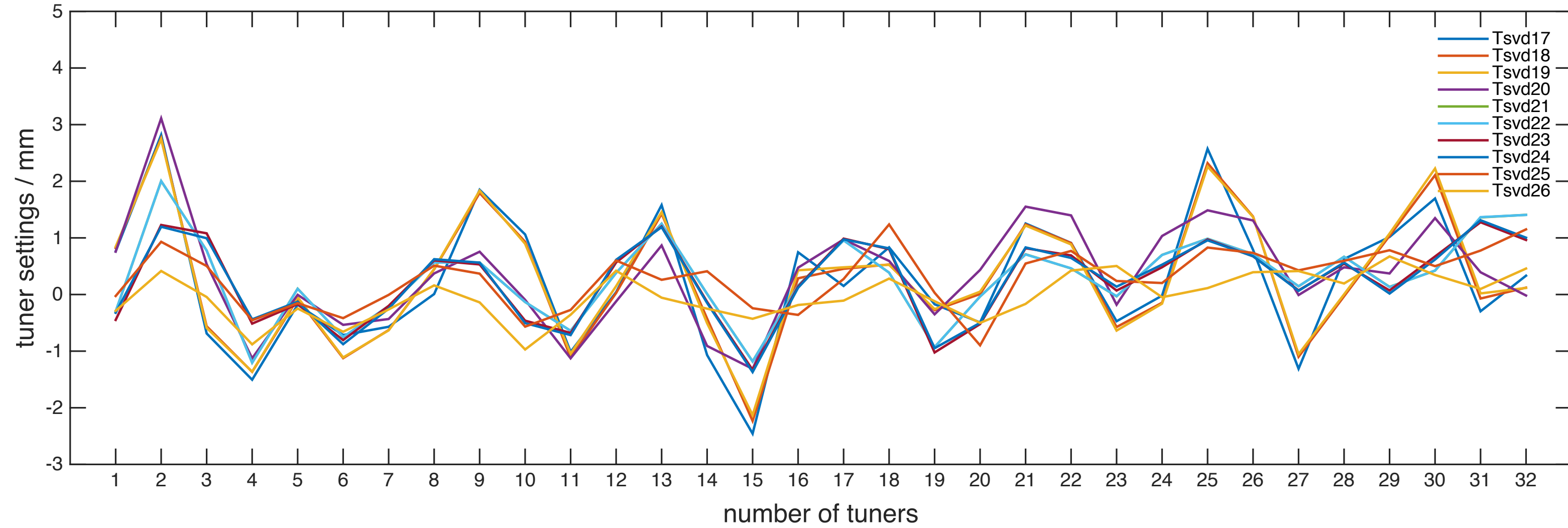
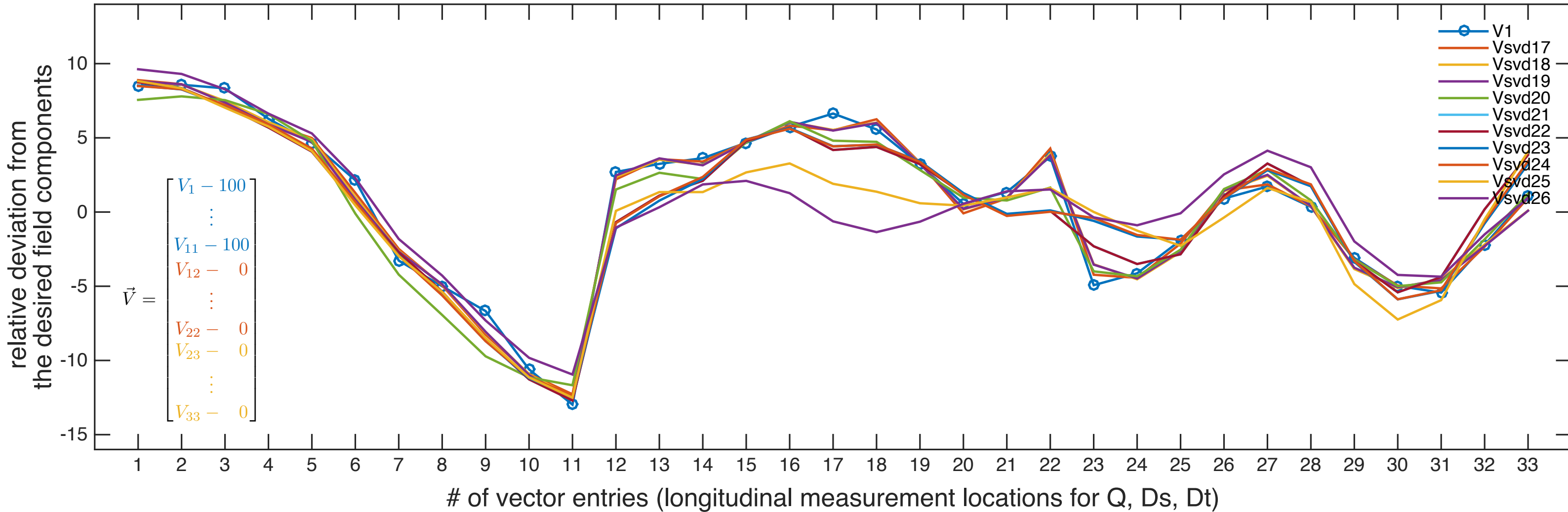
$$\vec{T}_{svdi} \gg \text{tuning range}$$

$$\vec{V}_{svdi} \approx \vec{V}$$

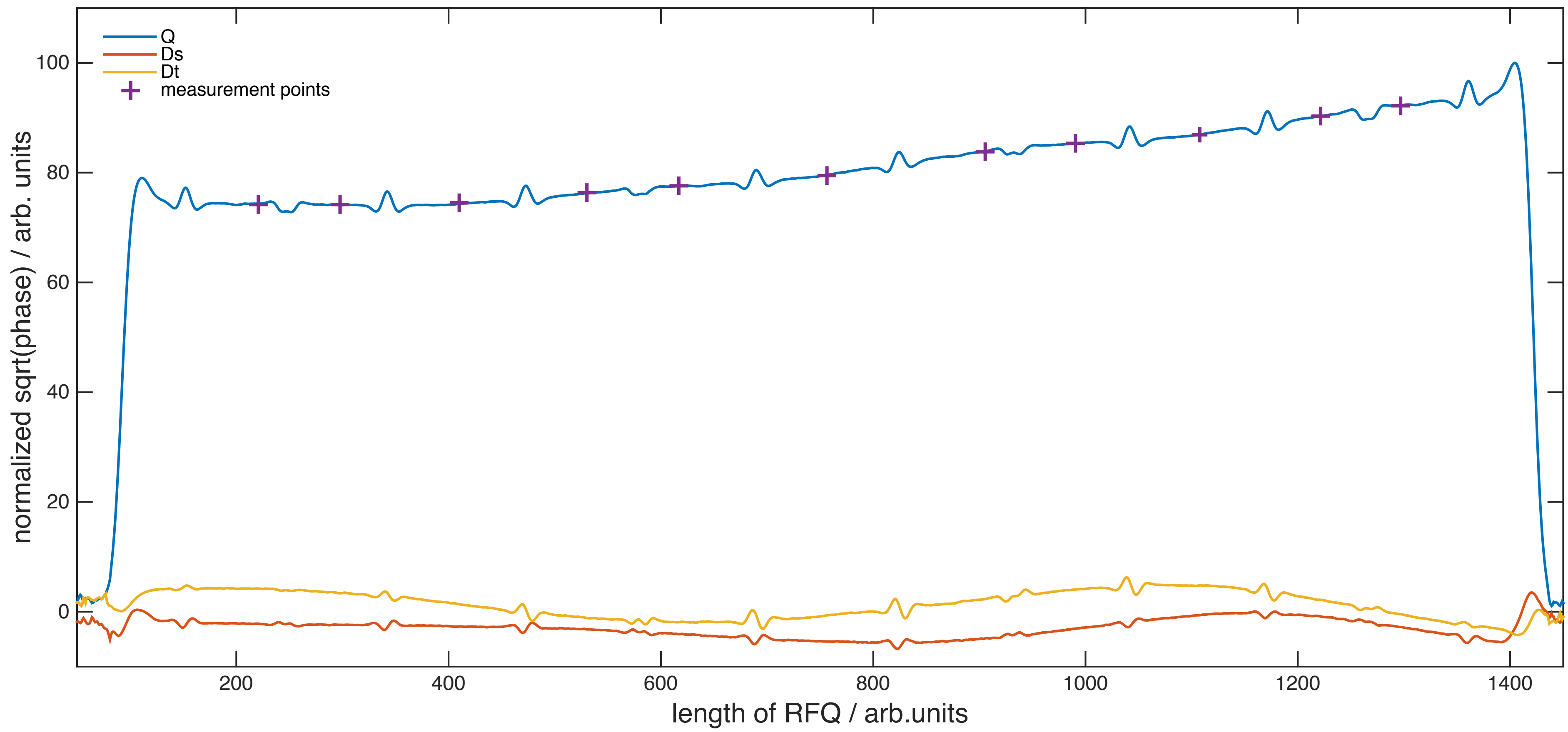
$$\vec{T}_{svdi} = \text{ok}$$

$$\vec{V}_{svdi} \neq \vec{V}$$

$$\vec{T}_{svdi} = \text{ok}$$

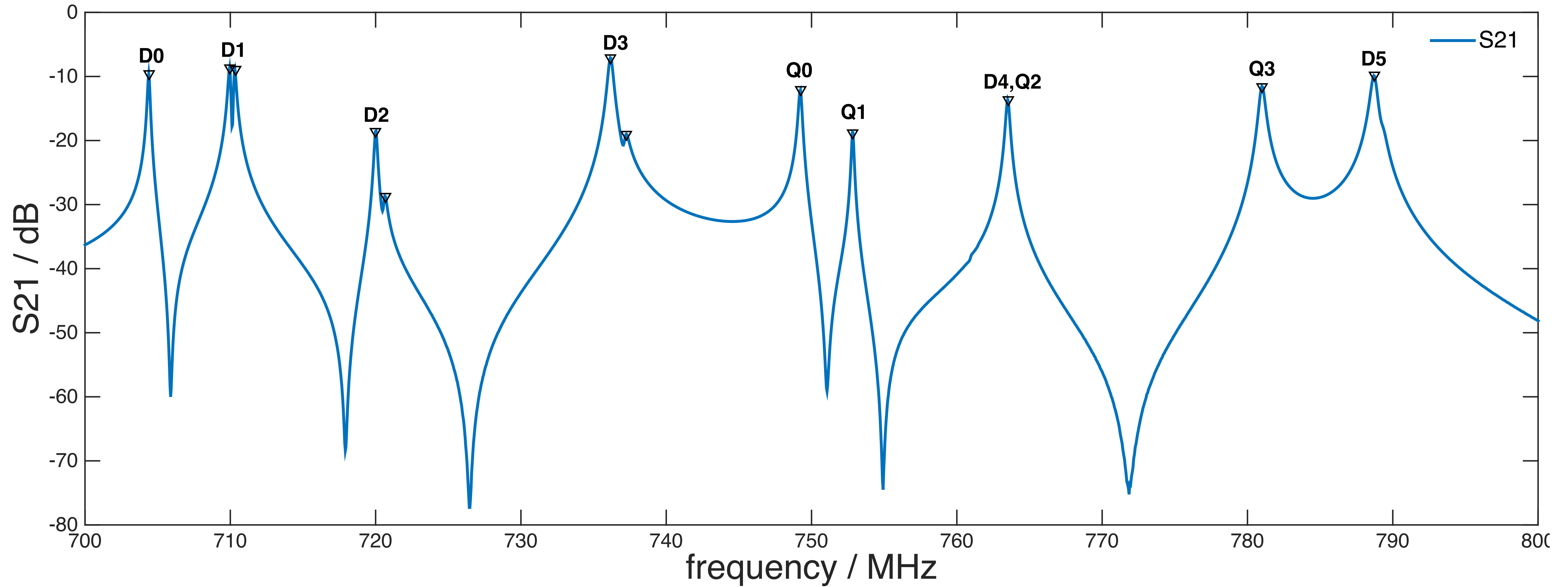


# Field Tuning



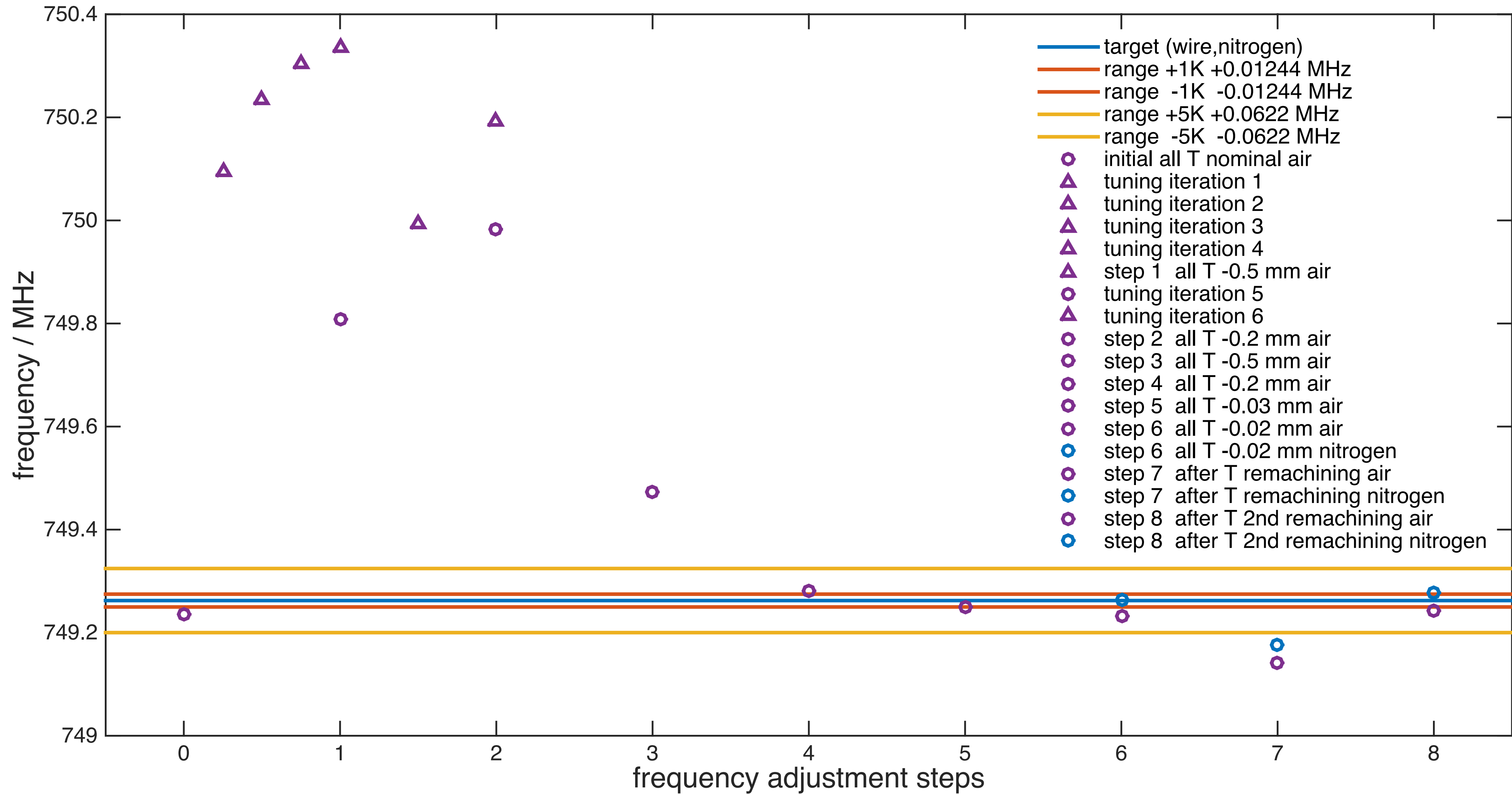
Component	Initial
Q	$\pm 10.8\%$
Ds	$\pm 3.0\%$
Dt	$\pm 3.6\%$

# Mode Spectra





# Frequency Tuning



# Dipole Stabiliser Rods / Modulation

