

# Gravitational waves from protoneutron stars and nuclear EOS

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collaborated with

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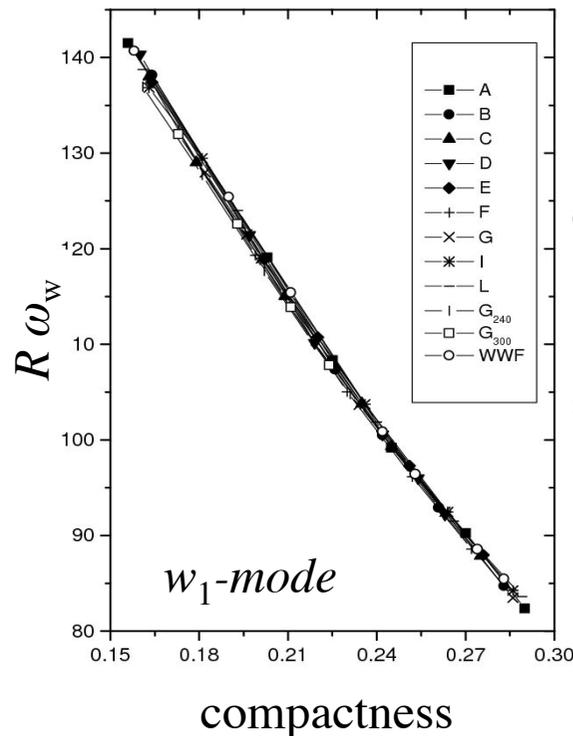
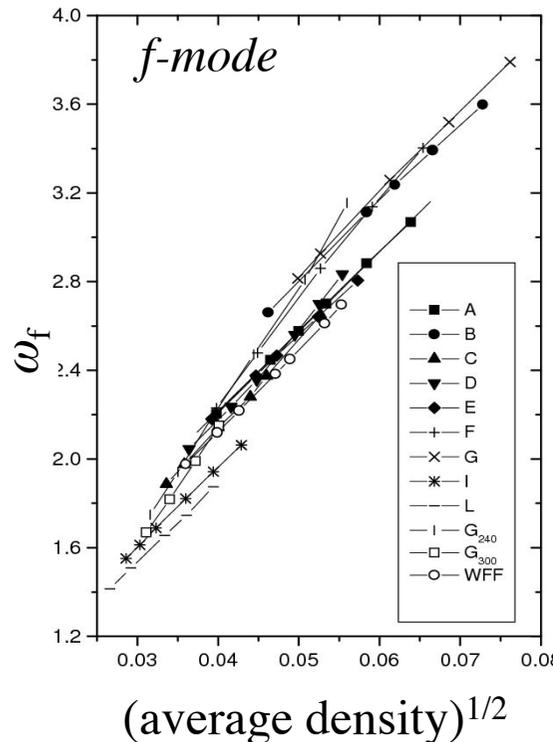
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# eigenfrequencies

- f- (and p<sub>i</sub>-) modes:  
acoustic (pressure) waves  
~ density ~  $M/R^3$
- w<sub>i</sub>-modes:  
spacetime oscillations ~  $M/R$

# Asteroseismology on Cold NSs

- via the observations of GW frequencies, one might be able to see the properties of NSs ---> [GW asteroseismology](#)



$$\omega_f \approx 0.78 + 1.64 \left[ \left( \frac{M}{1.4M_\odot} \right) \left( \frac{10\text{km}}{R} \right)^3 \right]^{1/2}$$

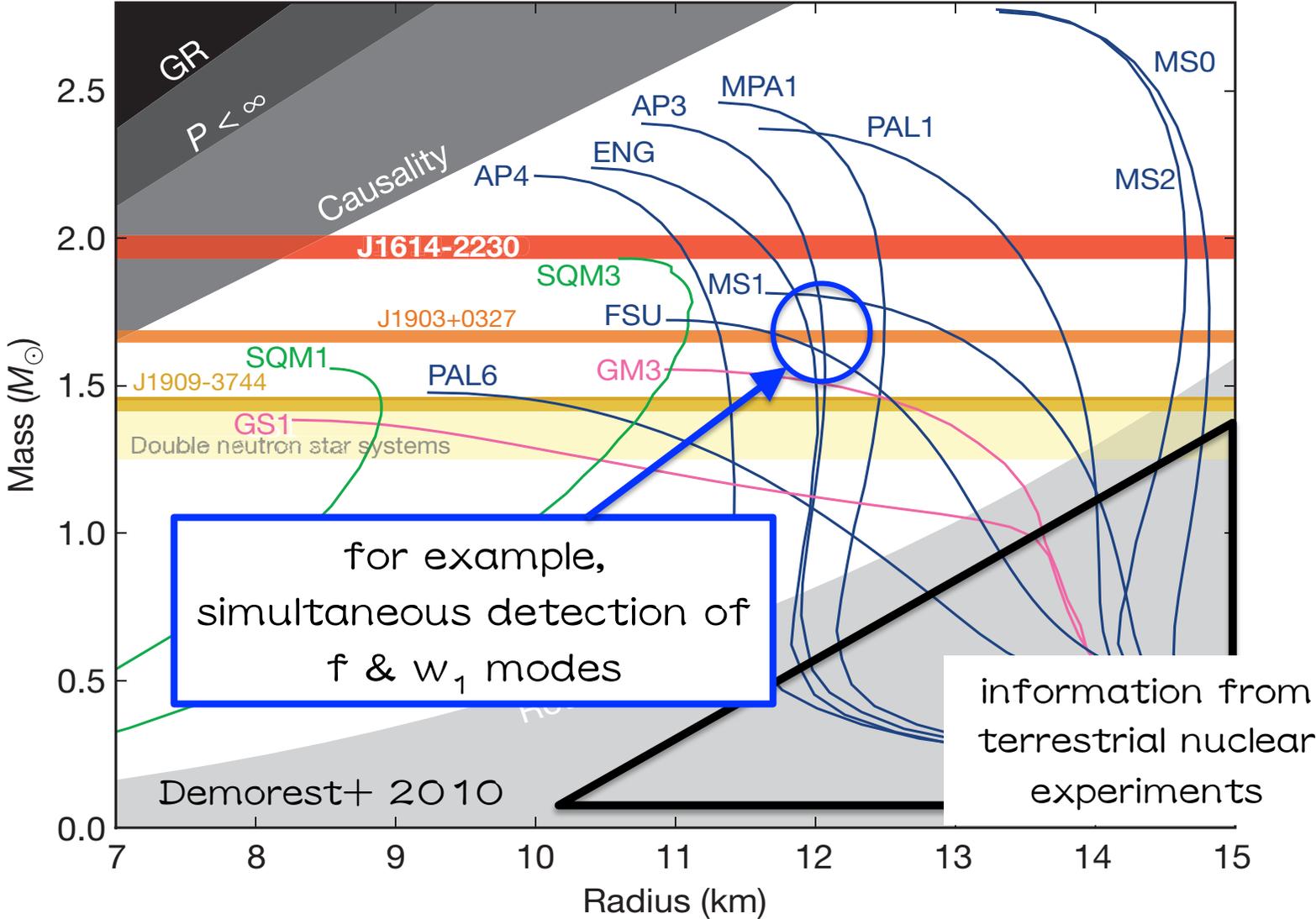
$$\omega_w \approx \left( \frac{10\text{km}}{R} \right) \left[ 20.92 - 9.14 \left( \frac{M}{1.4M_\odot} \right) \left( \frac{10\text{km}}{R} \right) \right]$$



determination of (M, R)

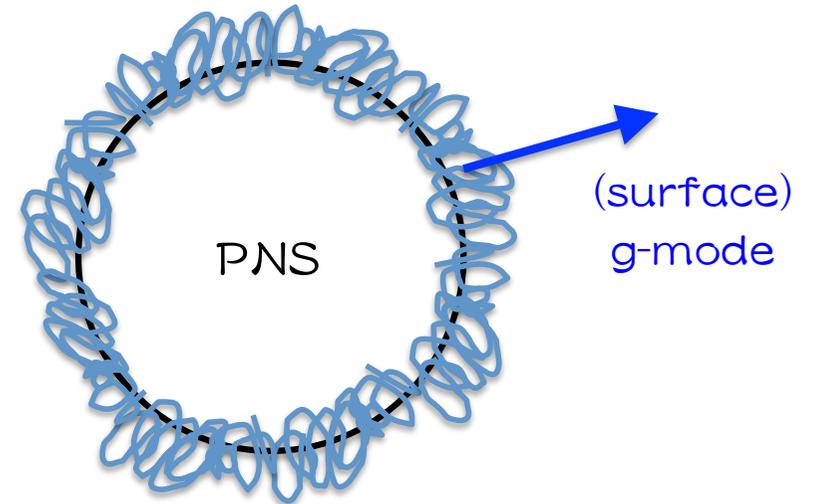
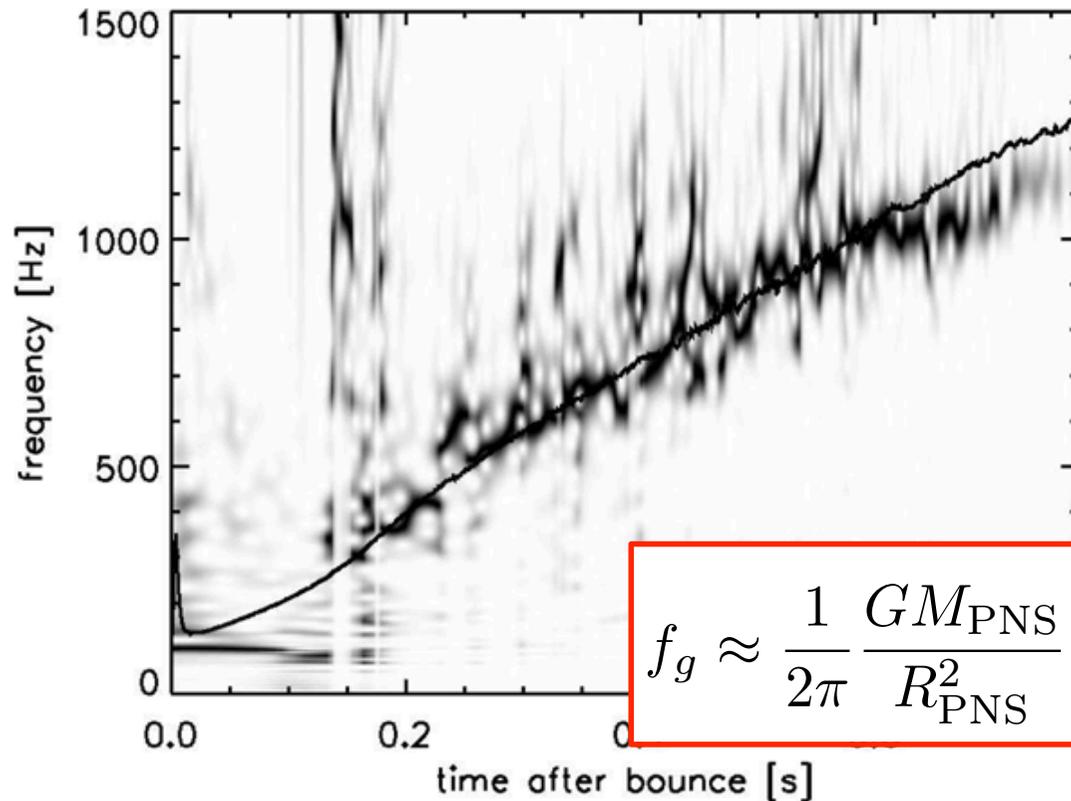
Andersson & Kokkotas (1998)

# Cold NS & EOS



# g-mode oscillations?

- 2D non-rotation with convection by Muller et al. (2013)  
 → excitations of specific frequency

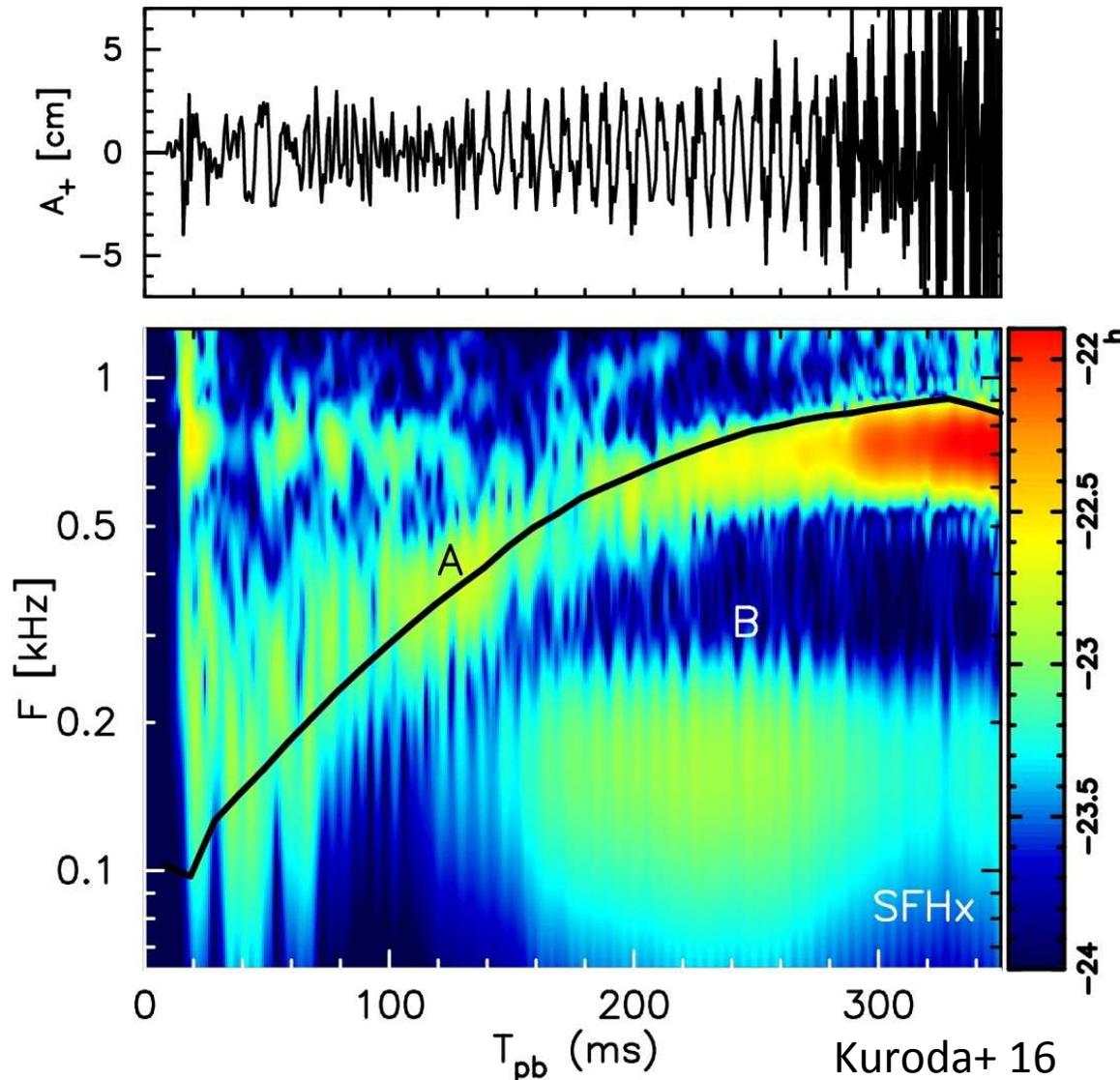


the convection & the standing accretion-shock instability

$$f_g \approx \frac{1}{2\pi} \frac{GM_{\text{PNS}}}{R_{\text{PNS}}^2} \left( \frac{1.1m_n}{\langle E_{\bar{\nu}_e} \rangle} \right)^{1/2} \left( 1 - \frac{GM_{\text{PNS}}}{c^2 R_{\text{PNS}}} \right)^2$$

BV frequency @  $r = R_{\text{PNS}}$

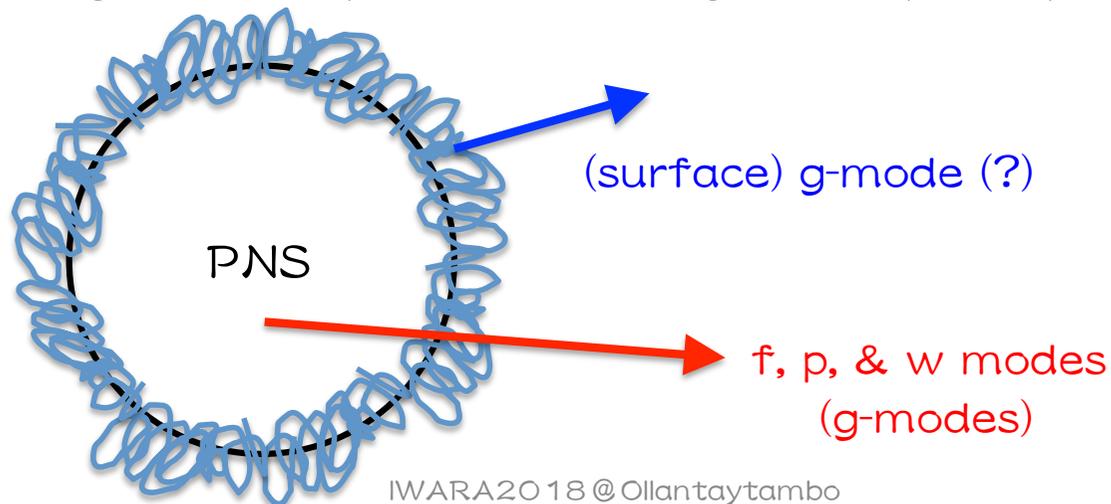
# GW from PSNs



- Numerical simulations tell us the GW spectra.
- difficult
  - to extract physics of PNS and/or SN mechanism
  - to make a long-term numerical calculations
- We adopt the **perturbation approach** to determine the freq. from PNS.

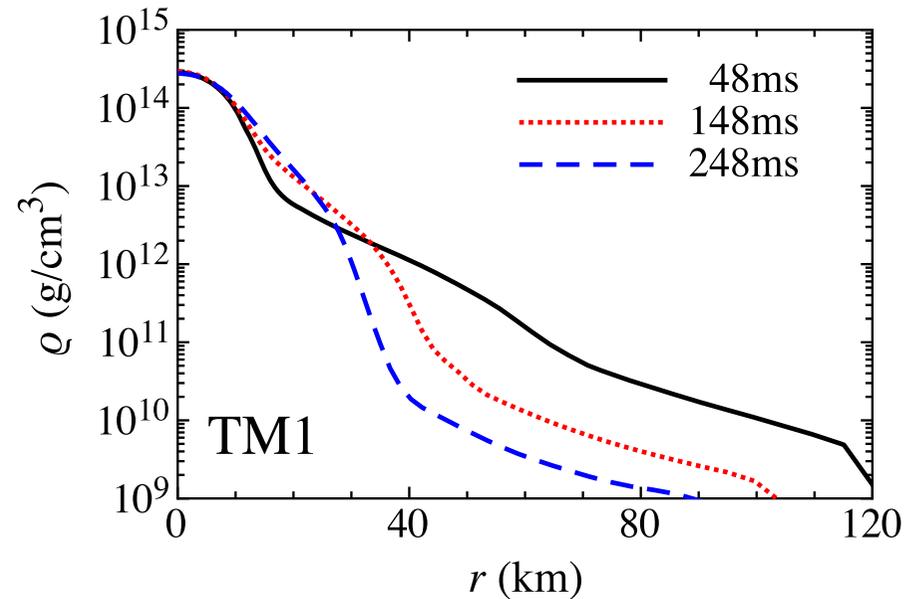
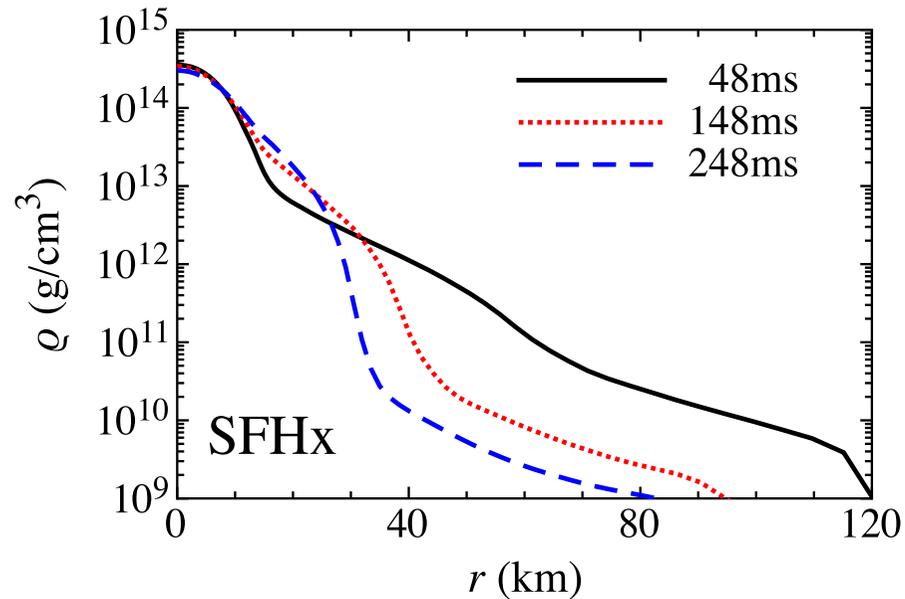
# asteroseismology in PNS

- background PNS models:
  - assuming that the PNS models are static spherically symmetric at each time step
  - adopting the numerical results of GR3D by Kuroda et al. (2016)
- add perturbations:
  - we particularly focus on
    - f, p-modes : with relativistic Cowling approximation, i.e.,  $\delta g_{\mu\nu} = 0$
    - w-modes : axial type oscillations with metric perturbation
- solve the eigenvalue problem  $\rightarrow$  eigenfrequency at each time



# PNS models

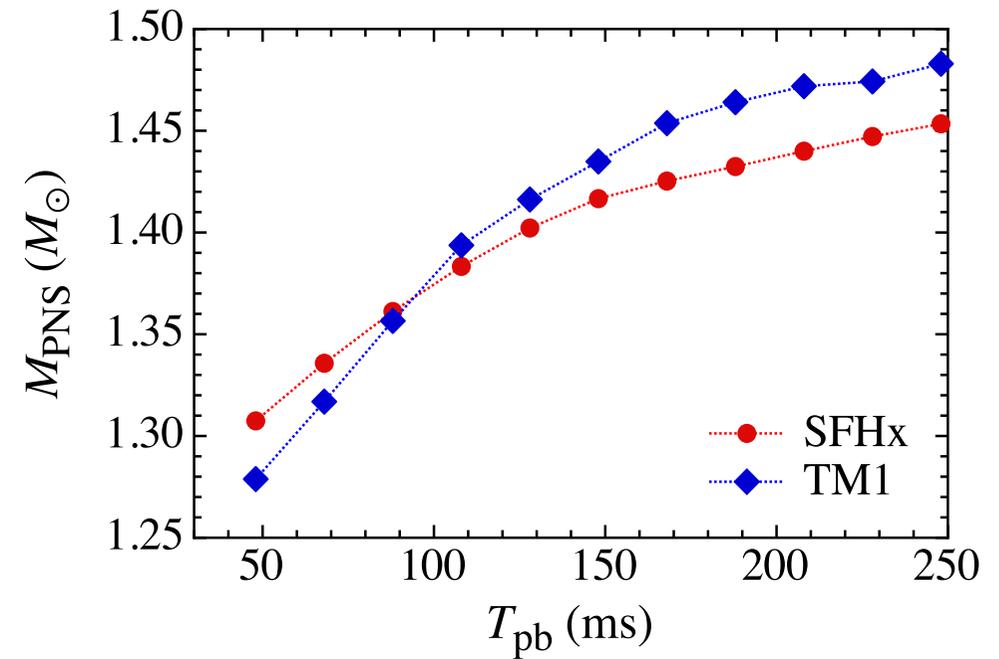
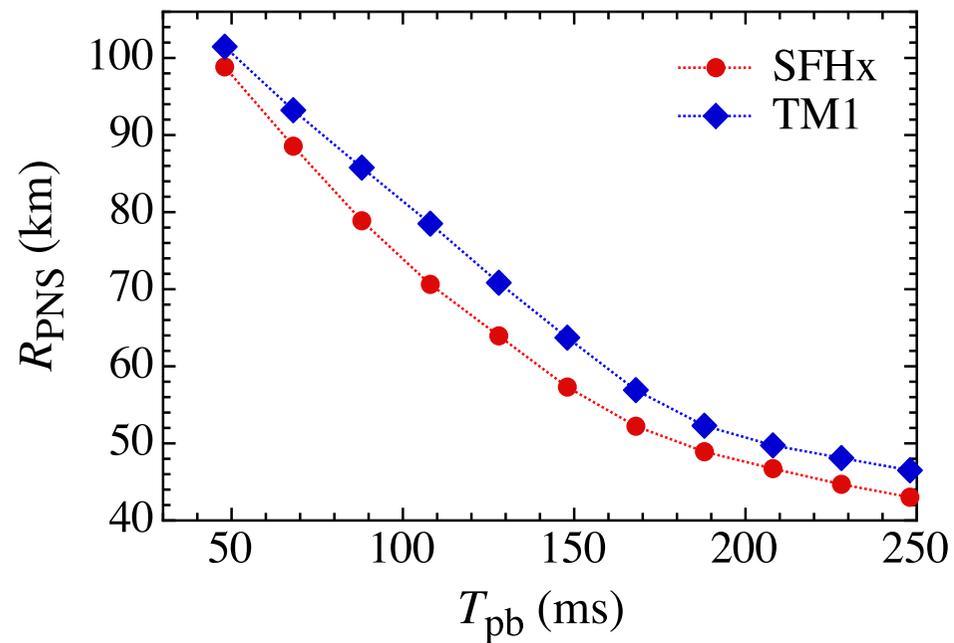
- we adopt the results of 3D-GR simulations of core-collapse supernovae (Kuroda et al. 2016)
  - progenitor mass =  $15M_{\odot}$
  - EOS : SFHx ( $2.13M_{\odot}$ ) & TM1 ( $2.21M_{\odot}$ )



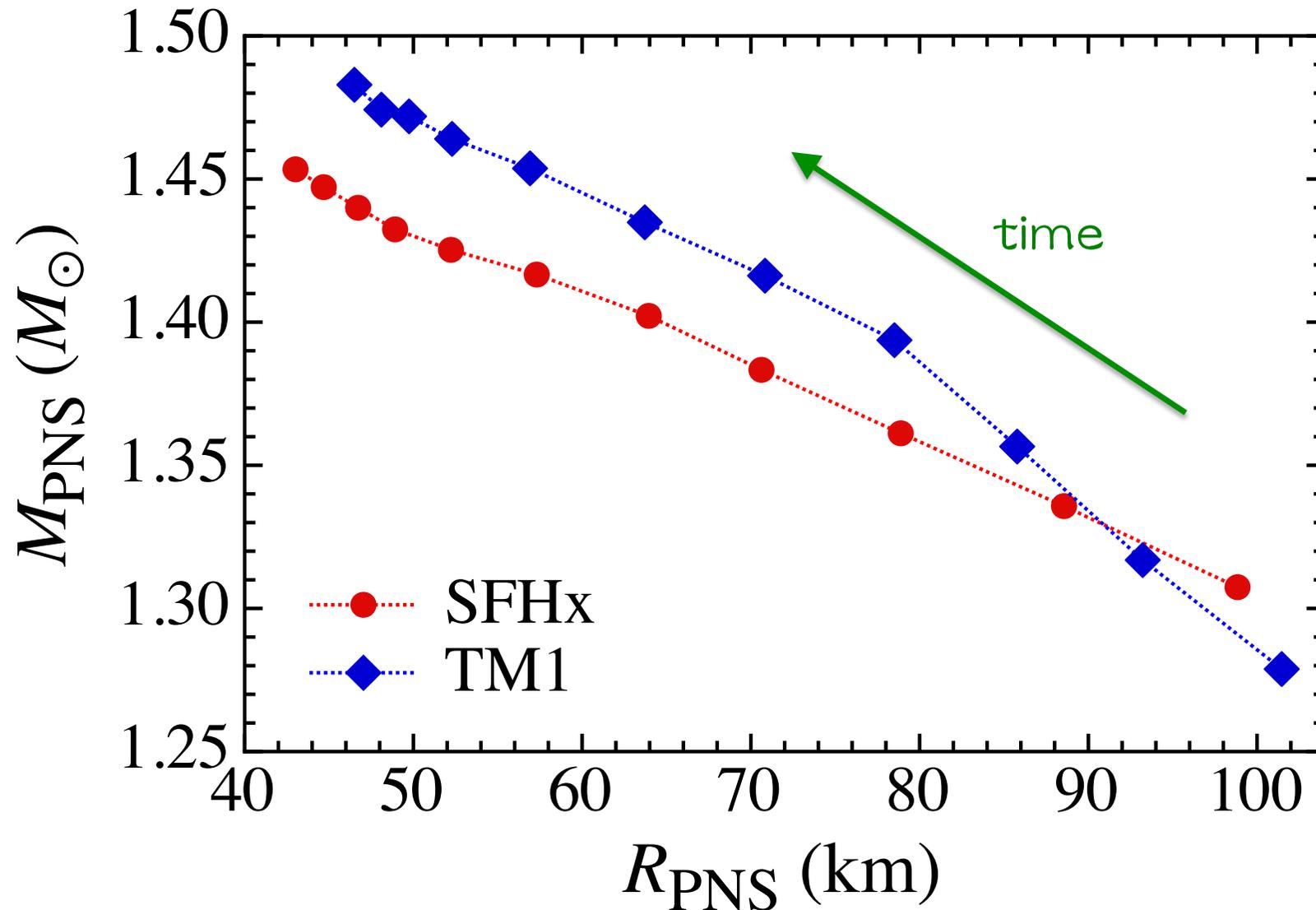
- $R_{\text{PNS}}$  is defined with  $\rho_s = 10^{10}$  g/cm<sup>3</sup>
- using the radial profiles as a background PNS model, the eigenfrequencies are determined.

# Mass & Radius

- $R_{\text{PNS}}$  is decreasing due to the cooling
- $M_{\text{PNS}}$  is increasing by mass accretion



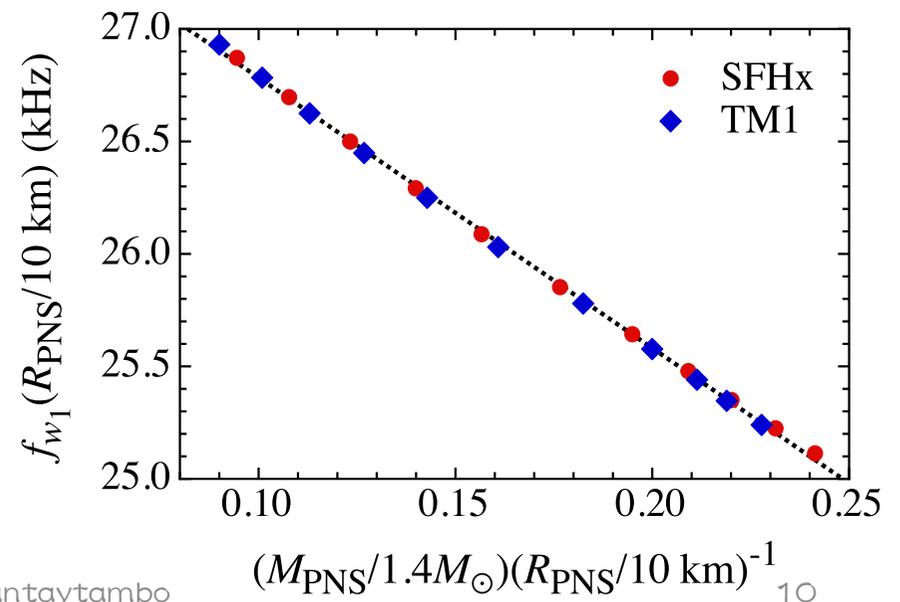
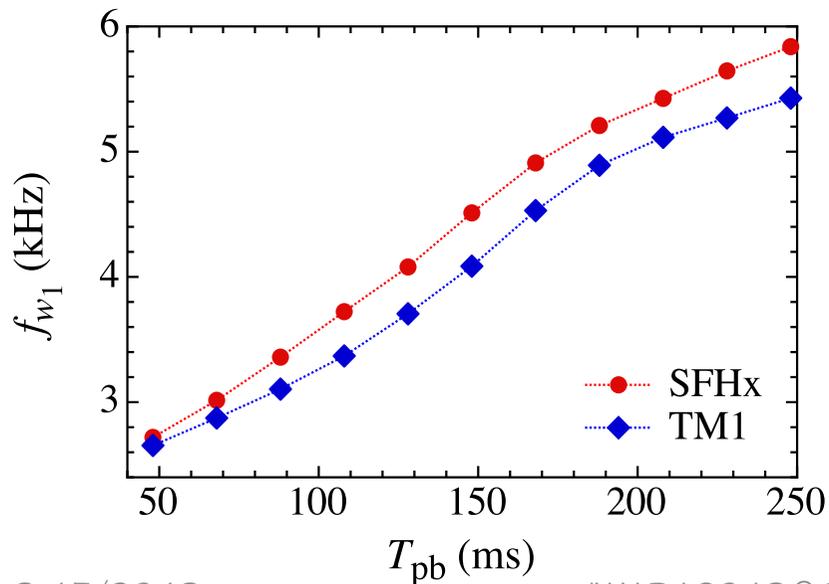
# M-R evolution after core-bounce



# evolution of $w_1$ -modes

- frequencies depend on the EOS.
  - increasing with time
  - can be characterized well by  $M_{\text{PNS}}/R_{\text{PNS}}$
- as for cold NS, we can get the fitting formula, almost independent from EOS

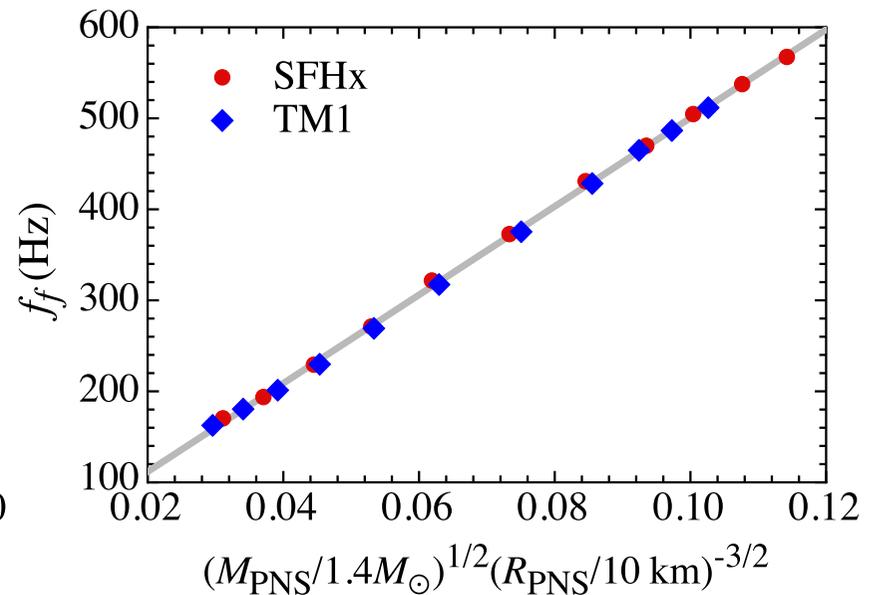
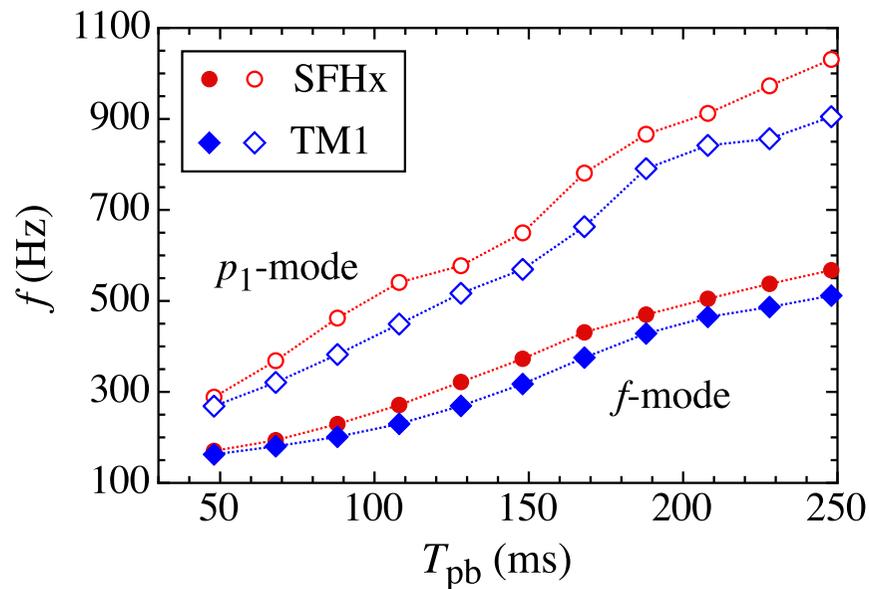
$$f_{w_1}^{(\text{PNS})} (\text{kHz}) \approx \left[ 27.99 - 12.02 \left( \frac{M_{\text{PNS}}}{1.4 M_{\odot}} \right) \left( \frac{R_{\text{PNS}}}{10 \text{ km}} \right)^{-1} \right] \times \left( \frac{R_{\text{PNS}}}{10 \text{ km}} \right)^{-1}$$



# evolution of f-mode

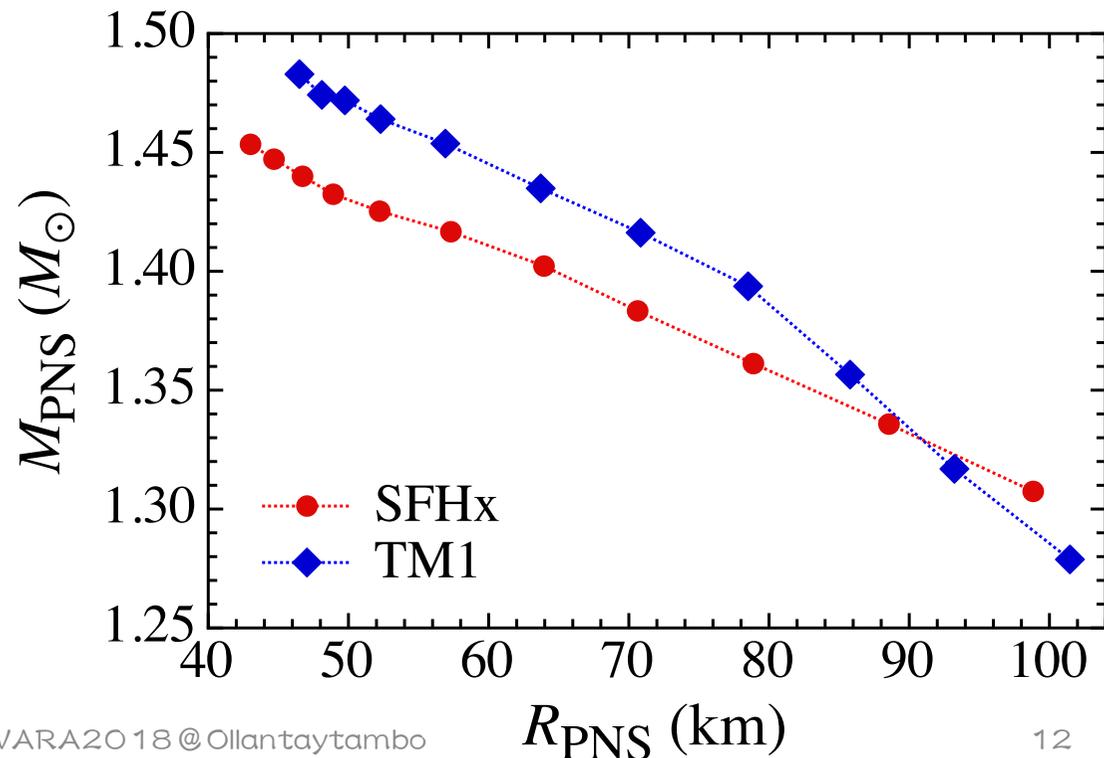
- frequencies can be expressed well by the average density independent of the EOS (and progenitor mass)
- we derive the fitting formula as a function of  $M_{\text{PNS}}/R_{\text{PNS}}^3$

$$f_f^{(\text{PNS})} (\text{Hz}) \approx 14.48 + 4859 \left( \frac{M_{\text{PNS}}}{1.4 M_{\odot}} \right)^{1/2} \left( \frac{R_{\text{PNS}}}{10 \text{ km}} \right)^{-3/2}$$



# determination of EOS

- GW spectra evolutions  $f_f(t)$  &  $f_{w1}(t)$   
→ evolutions of  $M_{\text{PNS}}/R_{\text{PNS}}^3$  &  $M_{\text{PNS}}/R_{\text{PNS}}$
- one can determine  $(M_{\text{PNS}}, R_{\text{PNS}})$  at each time after core bounce  
→ determination of the EOS
- unlike cold NS cases, in principle one can determine the EOS even with ONE GW event !



# detectability of $w_1$ -modes

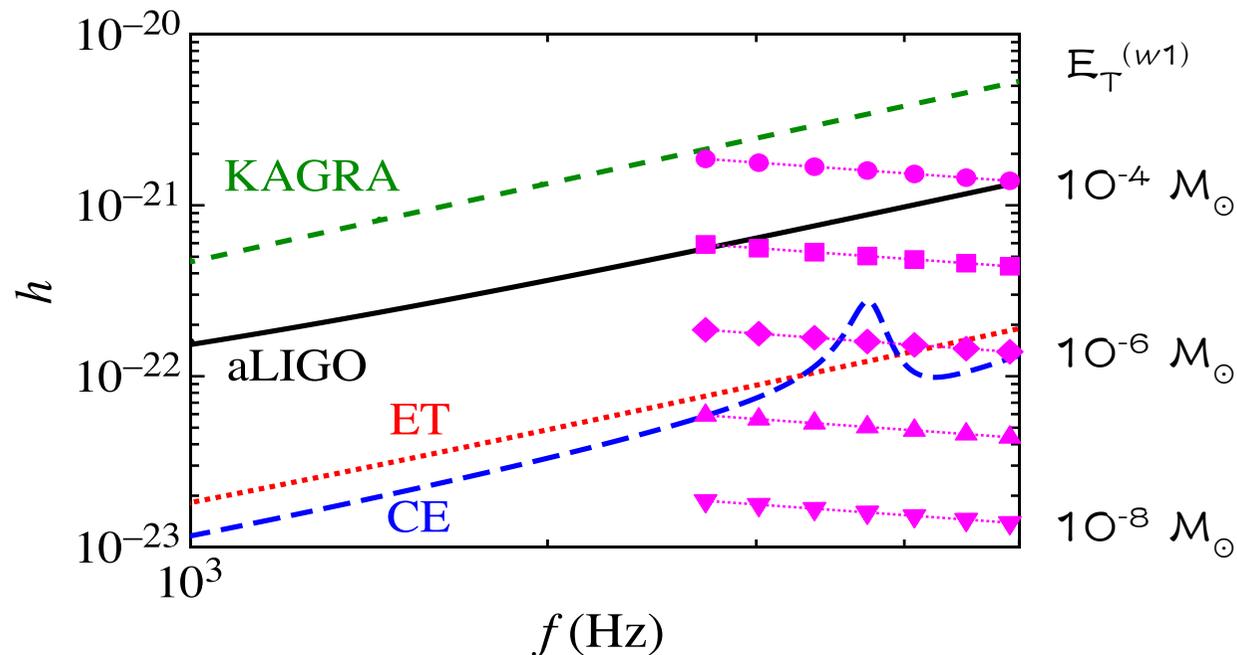
- effective amplitude of  $w_1$ -modes

$$h_{\text{eff}}^{(w_1)} \sim 7.7 \times 10^{-23} \left( \frac{E_{w_1}}{10^{-10} M_\odot} \right)^{1/2} \left( \frac{4 \text{ kHz}}{f_{w_1}} \right)^{1/2} \left( \frac{10 \text{ kpc}}{D} \right)$$

Andersson & Kokkotas (1996, 1998)

$$\frac{E_{w_1}}{E_T^{(w_1)}} \approx \frac{\tau_{w_1}}{T_{w_1}}$$

$E_{w_1}$  : energy for each time step  
 $E_T^{(w_1)}$  : total radiation energy in  $w_1$ -modes



# conclusion

- Asteroseismology could be powerful technique for extracting the interior information
- We examine the frequencies of gravitational waves radiating from PNS after bounce.

$$f_{w_1}^{(\text{PNS})} (\text{kHz}) \approx \left[ 27.99 - 12.02 \left( \frac{M_{\text{PNS}}}{1.4 M_{\odot}} \right) \left( \frac{R_{\text{PNS}}}{10 \text{ km}} \right)^{-1} \right] \times \left( \frac{R_{\text{PNS}}}{10 \text{ km}} \right)^{-1}$$

$$f_f^{(\text{PNS})} (\text{Hz}) \approx 14.48 + 4859 \left( \frac{M_{\text{PNS}}}{1.4 M_{\odot}} \right)^{1/2} \left( \frac{R_{\text{PNS}}}{10 \text{ km}} \right)^{-3/2}$$



$(M_{\text{PNS}}, R_{\text{PNS}})$  at each time after core bounce

- in principle, even with ONE GW event from supernova, one could determine the EOS for high density region.