

Molecules of hadrons bound by pion exchange: application to LHCb pentaquarks

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[T.B., Eur.Phys.J. A51, 152 (2015), 1509.02460]

[T.B. & E.Swanson (ongoing)]

$P_c(4380)$ and $P_c(4450)$

	$P_c(4380)^+$	$P_c(4450)^+$
Mass	$4380 \pm 8 \pm 29$	$4449.8 \pm 1.7 \pm 2.5$
Width	$205 \pm 18 \pm 86$	$35 \pm 5 \pm 19$
Assignment 1	$3/2^-$	$5/2^+$
Assignment 2	$3/2^+$	$5/2^-$
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$\Sigma_c^{*+} \bar{D}^0$ $(udc)(u\bar{c})$	4382.3 ± 2.4	
$\Sigma_c^+ \bar{D}^{*0}$ $(udc)(u\bar{c})$		4459.9 ± 0.5
$\Lambda_c^+(1P) \bar{D}^0$ $(udc)(u\bar{c})$		4457.09 ± 0.35
χ_{c1P} $(udu)(c\bar{c})$		4448.93 ± 0.07

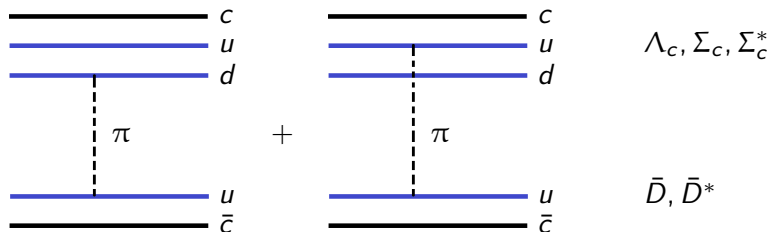
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Hidden-charm molecules

- ▶ Yang, Sun, He, Liu, Zhu (2011)
- ▶ Wu, Molina, Oset, Zou, Xiao, Nieves, Uchino, Liang, Roca, Magas, Feijoo, Ramos, ... (2010-2016)
- ▶ Karliner, Rosner (2015)
- ▶ He (2015)
- ▶ Shimizu, Suenaga, Harada (2016)
- ▶ Chen, Liu, Li, Zhu (2015)
- ▶ Yamaguchi, Santopinto (2016)
- ▶ Huang, Deng, Ping, Wang (2015)
- ▶ Yang, Ping (2015)
- ▶ Ortega, Entem, Fernandez (2016)
- ▶ ...

One-pion exchange potential



Potential mixes particles and angular momenta, e.g.

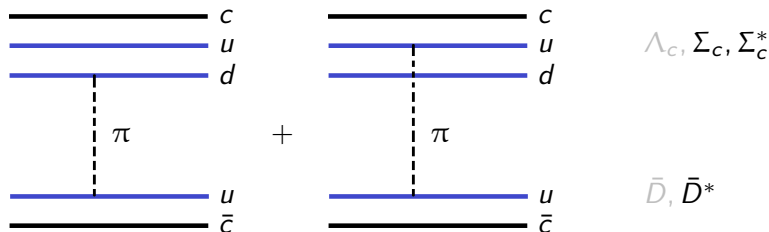
$$\blacktriangleright \Lambda_c \bar{D}({}^2S_{1/2}) \rightarrow \Sigma_c \bar{D}^*({}^4D_{1/2})$$

but the pattern is driven by diagonal blocks of fixed particles.

Note

- $\blacktriangleright \Lambda_c \Lambda_c \pi$ vertex is forbidden (isospin)
- $\blacktriangleright \bar{D} \bar{D} \pi$ vertex is forbidden (spin-parity)

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Quark models and heavy-quark chiral Lagrangians give

$$V(\vec{r}) = [V_C(r)\vec{\Sigma}_1 \cdot \vec{\Sigma}_2 + V_T(r)S_{12}(\hat{r})] \vec{T}_1 \cdot \vec{T}_2$$

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Coefficients are model-independent; e.g. $\Sigma_c \bar{D}^*$ in $1/2(3/2^-)$:

$$\begin{array}{l} \langle {}^4S_{3/2} | \\ \langle {}^2D_{3/2} | \\ \langle {}^4D_{3/2} | \end{array} \begin{array}{ccc} | {}^4S_{3/2} \rangle & | {}^2D_{3/2} \rangle & | {}^4D_{3/2} \rangle \\ -\frac{8}{3}V_C & -\frac{8}{3}V_T & -\frac{16}{3}V_T \\ -\frac{8}{3}V_T & +\frac{16}{3}V_C & +\frac{8}{3}V_T \\ -\frac{16}{3}V_T & +\frac{8}{3}V_T & -\frac{8}{3}V_C \end{array}$$

and relative strengths fixed by HQ symmetry.

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$\langle^4S_{3/2} $	$-\frac{8}{3}V_C$	$-\frac{8}{3}V_T$	$-\frac{16}{3}V_T$
$\langle^2D_{3/2} $	$-\frac{8}{3}V_T$	$+\frac{16}{3}V_C$	$+\frac{8}{3}V_T$
$\langle^4D_{3/2} $	$-\frac{16}{3}V_T$	$+\frac{8}{3}V_T$	$-\frac{8}{3}V_C$

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Central and tensor potentials with form factor cutoff

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and relative strengths fixed by HQ symmetry.

Central and tensor potentials with form factor cutoff

Larger isospin \implies weaker potential; e.g. $V_{I=3/2} = -\frac{1}{2}V_{I=1/2}$

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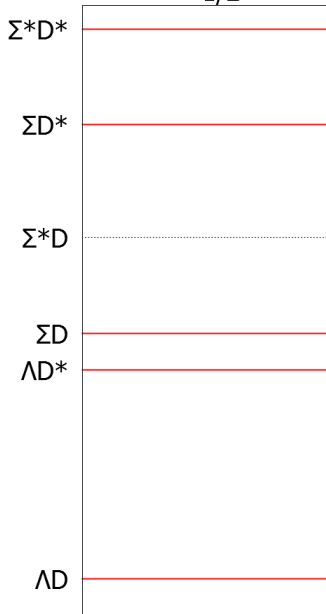
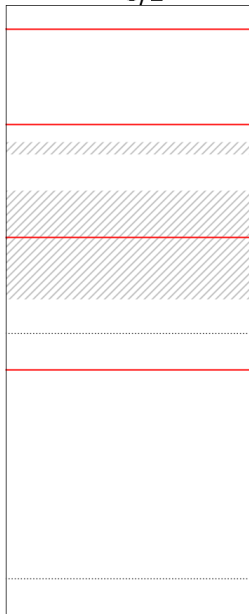
	$ ^4S_{3/2}\rangle$	$ ^2D_{3/2}\rangle$	$ ^4D_{3/2}\rangle$
$\langle^4S_{3/2} $	$-\frac{8}{3}V_C$	$-\frac{8}{3}V_T$	$-\frac{16}{3}V_T$
$\langle^2D_{3/2} $	$-\frac{8}{3}V_T$	$+\frac{16}{3}V_C$	$+\frac{8}{3}V_T$
$\langle^4D_{3/2} $	$-\frac{16}{3}V_T$	$+\frac{8}{3}V_T$	$-\frac{8}{3}V_C$

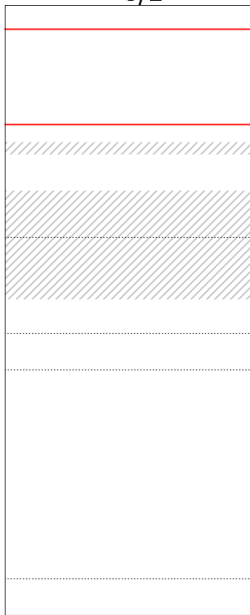
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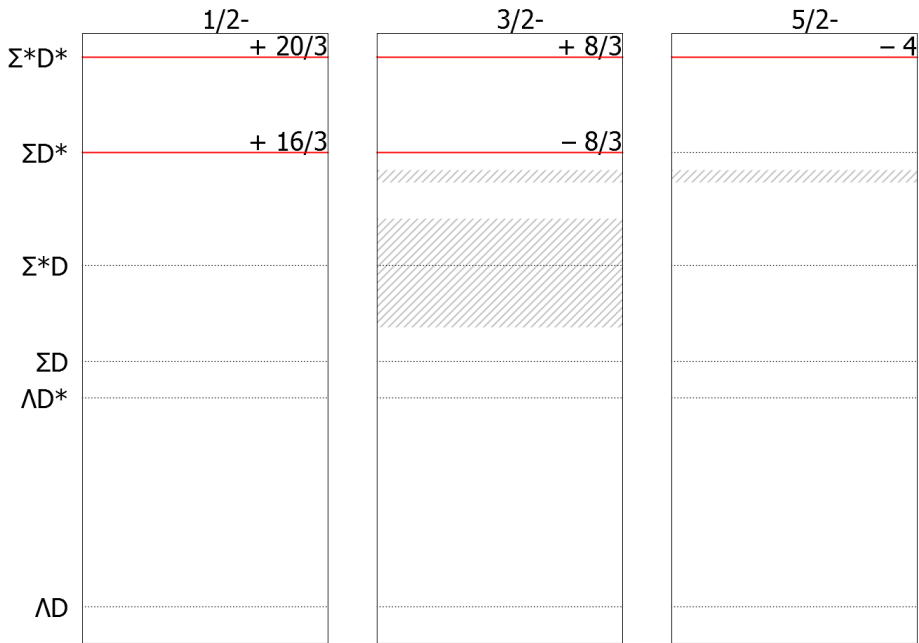
Central and tensor potentials with form factor cutoff

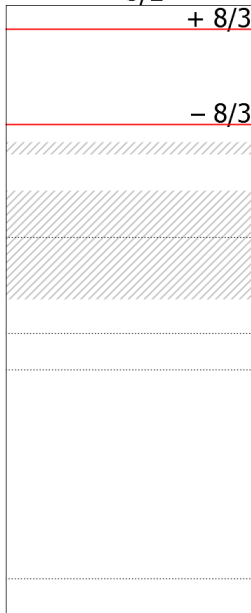
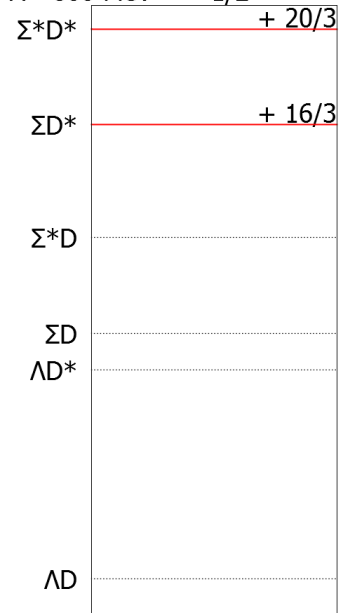
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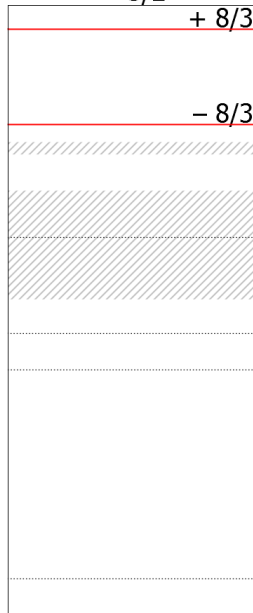
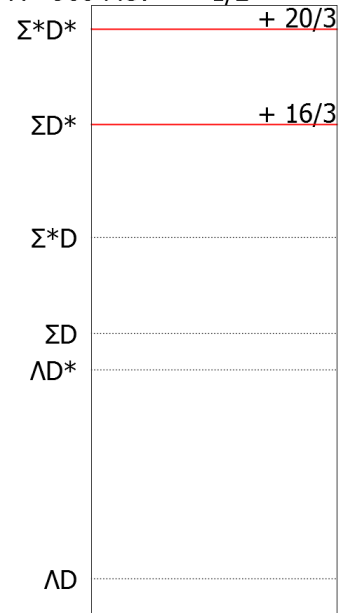
For channels with S-waves, binding is driven by coefficient of $V_C(r)$
(and unlike for NN , this can be positive...)

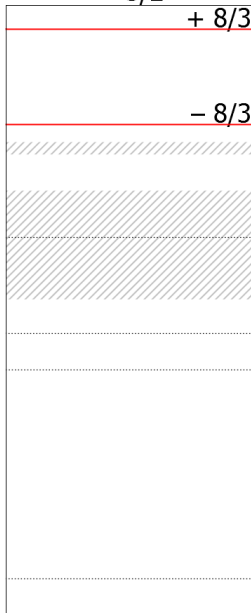
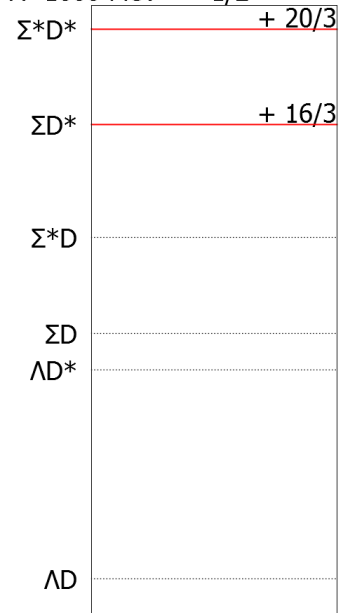
$1/2^-$  $3/2^-$  $5/2^-$ 

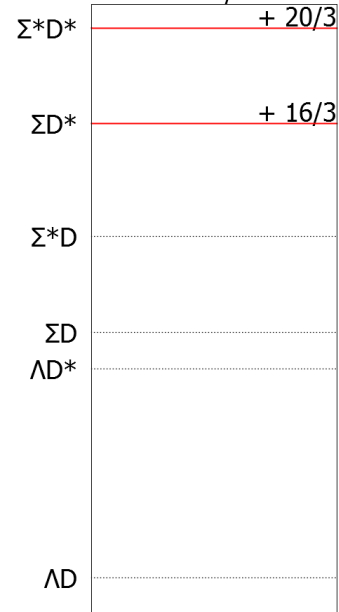
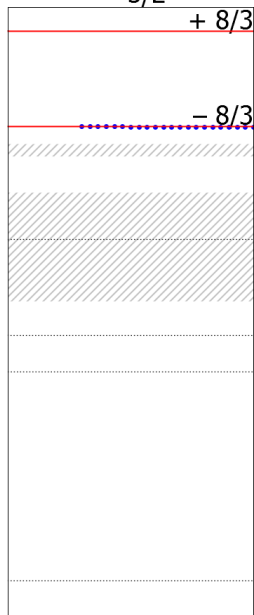
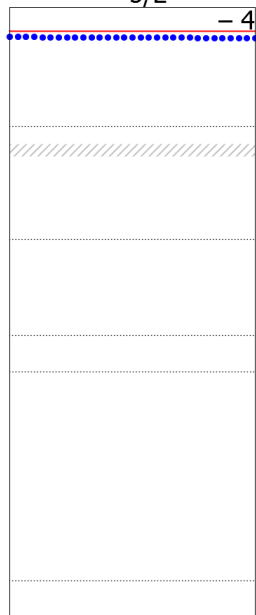
$1/2^-$ Σ^*D^* ΣD^* Σ^*D ΣD ΛD^* ΛD  $3/2^-$  $5/2^-$ 

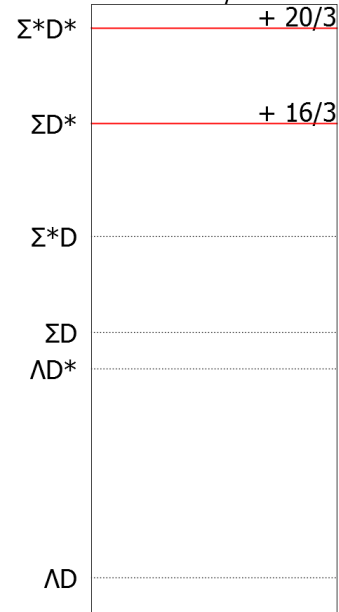
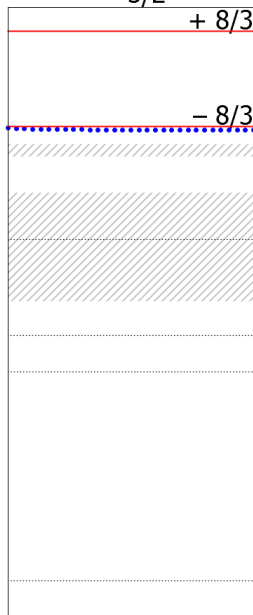


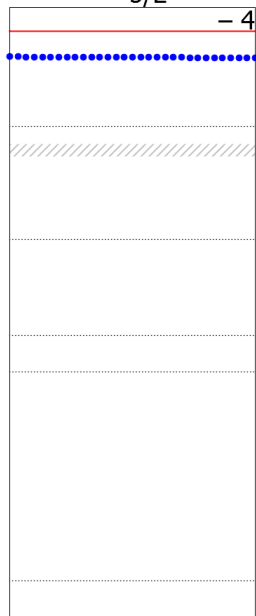
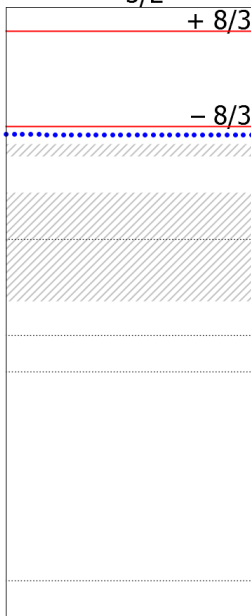
$\Lambda = 800 \text{ MeV}$ $1/2^-$ $3/2^-$ $5/2^-$ 

$\Lambda = 900 \text{ MeV}$ $1/2^-$ $3/2^-$ $5/2^-$ 

$\Lambda=1000 \text{ MeV}$ $1/2^-$ $3/2^-$ $5/2^-$ 

$\Lambda=1100$ MeV $1/2^-$  $3/2^-$  $5/2^-$ 

$\Lambda=1200$ MeV $1/2^-$  $3/2^-$  $5/2^-$ 

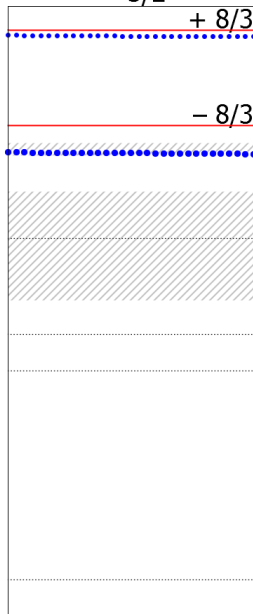
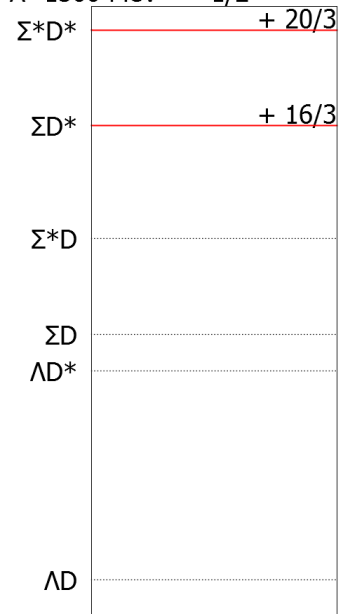
$\Lambda=1300$ MeV $1/2^-$ Σ^*D^* $+ 20/3$ ΣD^* $+ 16/3$ Σ^*D ΣD ΛD^* ΛD $3/2^-$ $+ 8/3$ $- 8/3$ $5/2^-$ $- 4$ 

$\Lambda=1500$ MeV

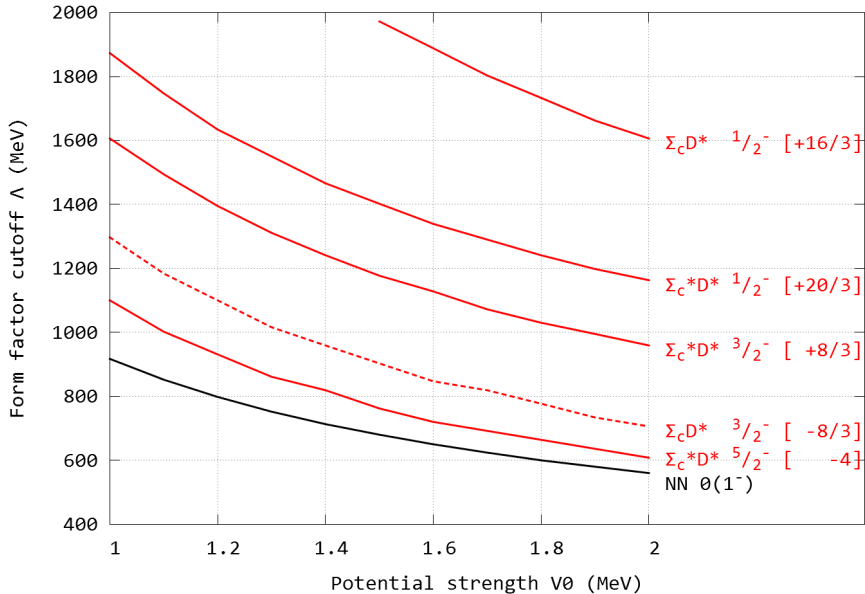
$1/2^-$

$3/2^-$

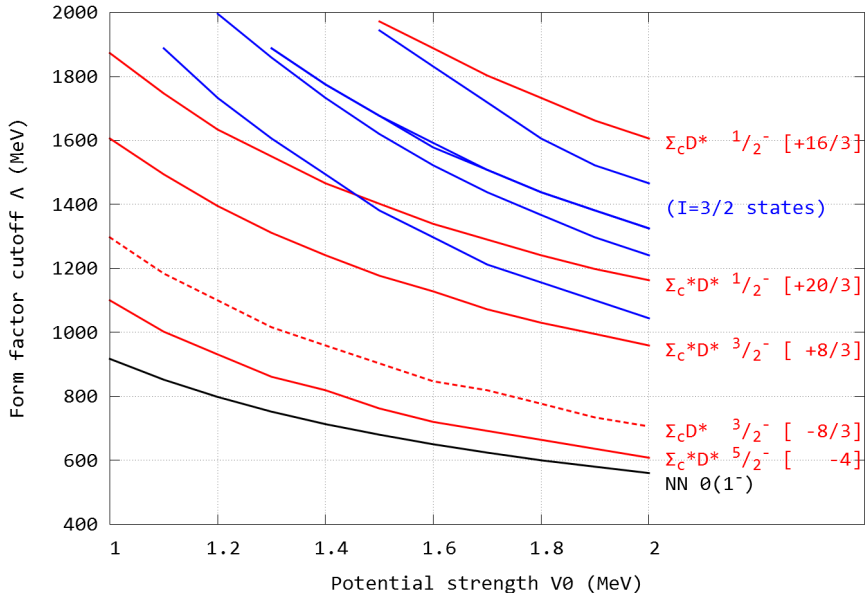
$5/2^-$



Critical form factor



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Conventional wisdom

“Molecules exist close to S-wave thresholds”

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- ▶ Only for certain quantum numbers
- ▶ “Few” states exist \Leftrightarrow all are “near” threshold
- ▶ “Many” states exist \Leftrightarrow some are more deeply bound
- ▶ Pattern is driven by coefficient of V_C , due to π exchange, and understood in fixed-particle basis. . . but is more general.

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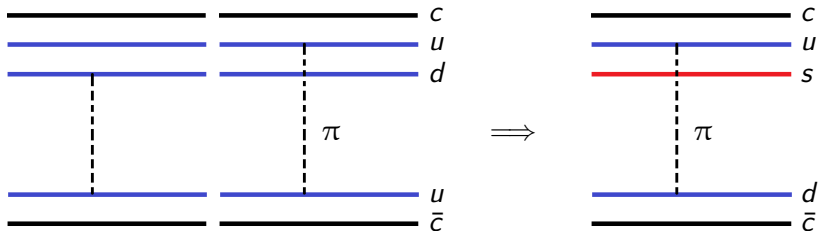
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P-wave states? (e.g $1/2^+$, $3/2^+$, $5/2^+$)

- ▶ Possible, but with much larger cut-off, implying many more states overall
- ▶ Pattern is driven by coefficient of V_T .
- ▶ States near wrong thresholds for $P_c(4380)$, $P_c(4450)$.

$\Xi_c^* \bar{D}^*$ molecules

$$\begin{aligned} \Lambda_c &= ((ud)_0 c)_{1/2} & \implies & \Xi_c = ((us)_0 c)_{1/2} \\ \Sigma_c &= ((ud)_1 c)_{1/2} & \implies & \Xi'_c = ((us)_1 c)_{1/2} \\ \Sigma_c^* &= ((ud)_1 c)_{3/2} & \implies & \Xi_c^* = ((us)_1 c)_{3/2} \end{aligned}$$



The potential matrices (central + tensor) are directly related.

Predict loosely bound $0(5/2^-)$ $\Xi_c^* \bar{D}^*$ state, observable in $\Lambda_b \rightarrow J/\psi \Lambda \eta$, and $\Xi_b \rightarrow J/\psi \Lambda K^-$ (LHCb run II).

Isospin mixing: $P_c(4380)$ and $P_c(4450)$

$$uudc\bar{c} = \begin{cases} (udc)(u\bar{c}) = \Sigma_c^+ \bar{D}^0 \\ (uuc)(d\bar{c}) = \Sigma_c^{++} D^- \end{cases}$$

Isospin-conserving interactions give $|I, I_3\rangle$ eigenstates,

$$\begin{pmatrix} |\frac{1}{2}, \frac{1}{2}\rangle \\ |\frac{3}{2}, \frac{1}{2}\rangle \end{pmatrix} = \begin{pmatrix} -\sqrt{\frac{1}{3}} & \sqrt{\frac{2}{3}} \\ \sqrt{\frac{2}{3}} & \sqrt{\frac{1}{3}} \end{pmatrix} \begin{pmatrix} |\Sigma_c^+ \bar{D}^0\rangle \\ |\Sigma_c^{++} D^-\rangle \end{pmatrix}$$

but only if the masses $\Sigma_c^+ = \Sigma_c^{++}$ and $\bar{D}^0 = D^-$.

Otherwise, isospin is not a good quantum number.

Isospin mixing: $P_c(4380)$ and $P_c(4450)$

$$P_c(4380) = 4380 \pm 8 \pm 29 \quad P_c(4450) = 4449 \pm 1.7 \pm 2.5$$

$$\Sigma_c^{*+} \bar{D}^0 = 4382.3 \pm 2.4 \quad \Sigma_c^+ \bar{D}^{*0} = 4459.9 \pm 0.5$$

$$\Sigma_c^{*++} D^- = 4387.5 \pm 0.7 \quad \Sigma_c^{++} D^{*-} = 4464.24 \pm 0.23$$

The P_c states have mixed isospin:

$$|P_c\rangle = \cos \phi \left| \frac{1}{2}, \frac{1}{2} \right\rangle + \sin \phi \left| \frac{3}{2}, \frac{1}{2} \right\rangle$$

They should decay also into $J/\psi \Delta^+$ and $\eta_c \Delta^+$, with weights:

$$J/\psi p : J/\psi \Delta^+ : \eta_c \Delta^+ = 2 \cos^2 \phi : 5 \sin^2 \phi : 3 \sin^2 \phi \quad [P_c(4380)]$$

$$J/\psi p : J/\psi \Delta^+ : \eta_c \Delta^+ = \cos^2 \phi : 10 \sin^2 \phi : 6 \sin^2 \phi \quad [P_c(4450)]$$

Isospin mixing: predicted $5/2^-$ states

$$\Sigma_c^* \bar{D}^* \quad 1/2(5/2^-)$$

$$\Sigma_c^{*+} \bar{D}^{*0} = 4524.4 \pm 2.4$$

$$\Sigma_c^{*++} D^{*-} = 4528.2 \pm 0.7$$

Mixed isospin:

$$|P\rangle = \cos \phi \left| \frac{1}{2}, \frac{1}{2} \right\rangle + \sin \phi \left| \frac{3}{2}, \frac{1}{2} \right\rangle$$

Decays:

→ $J/\psi p$: D-wave, spin flip

Reason for absence at LHCb?

→ $J/\psi \Delta$: S-wave, spin cons.

⇒ $I = 3/2$ decay enhanced.

Isospin mixing: predicted $5/2^-$ states

$$\Sigma_c^* \bar{D}^* 1/2(5/2^-)$$

$$\Xi_c^* \bar{D}^* 0(5/2^-)$$

$$\Sigma_c^{*+} \bar{D}^{*0} = 4524.4 \pm 2.4$$

$$\Xi_c^{*0} \bar{D}^{*0} = 4652.9 \pm 0.6$$

$$\Sigma_c^{*++} D^{*-} = 4528.2 \pm 0.7$$

$$\Xi_c^{*+} D^{*-} = 4656.2 \pm 0.7$$

Mixed isospin:

$$|P\rangle = \cos \phi |\frac{1}{2}, \frac{1}{2}\rangle + \sin \phi |\frac{3}{2}, \frac{1}{2}\rangle$$

Mixed isospin:

$$|P\rangle = \cos \phi |0, 0\rangle + \sin \phi |1, 0\rangle$$

Decays:

$\rightarrow J/\psi p$: D-wave, spin flip

Reason for absence at LHCb?

Decays:

$\rightarrow J/\psi \Lambda$: D-wave, spin flip

e.g. $\Lambda_b^0 \rightarrow J/\psi \Lambda \eta, J/\psi \Lambda \phi$

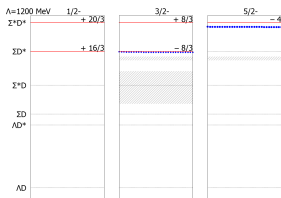
$\rightarrow J/\psi \Delta$: S-wave, spin cons.

$\implies I = 3/2$ decay enhanced.

$\rightarrow J/\psi \Sigma^*$: S-wave, spin cons.

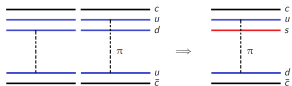
$\implies I = 1$ decay enhanced.

Conclusions

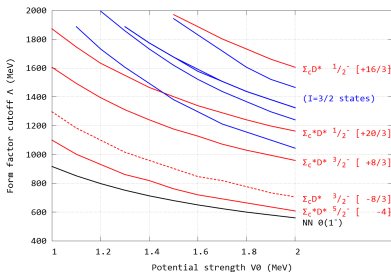


Pattern is

- ▶ easily understood
- ▶ parameter insensitive
- ▶ generic



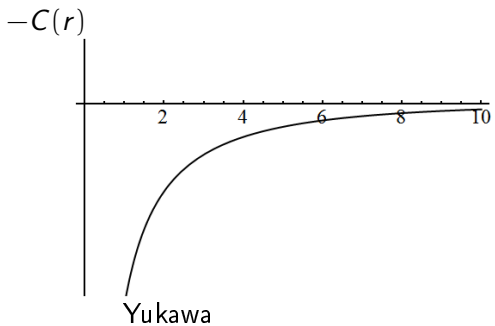
- ▶ Binding in certain $I(J^P)$ only
- ▶ $3/2^- \Sigma_c \bar{D}^* = P_c(4450)?$
- ▶ $5/2^- \Sigma_c^* \bar{D}^*$ with D-wave decay



- ▶ Predict $\Xi_c^* \bar{D}^* 0(5/2^-)$ partner
- ▶ All states are isospin mixtures

Backup slides

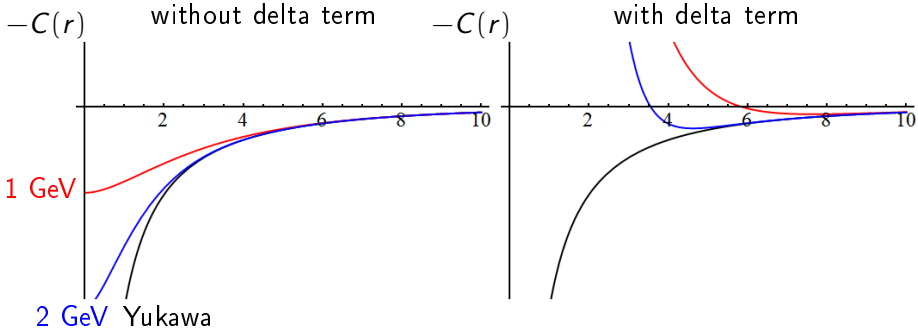
Central potential



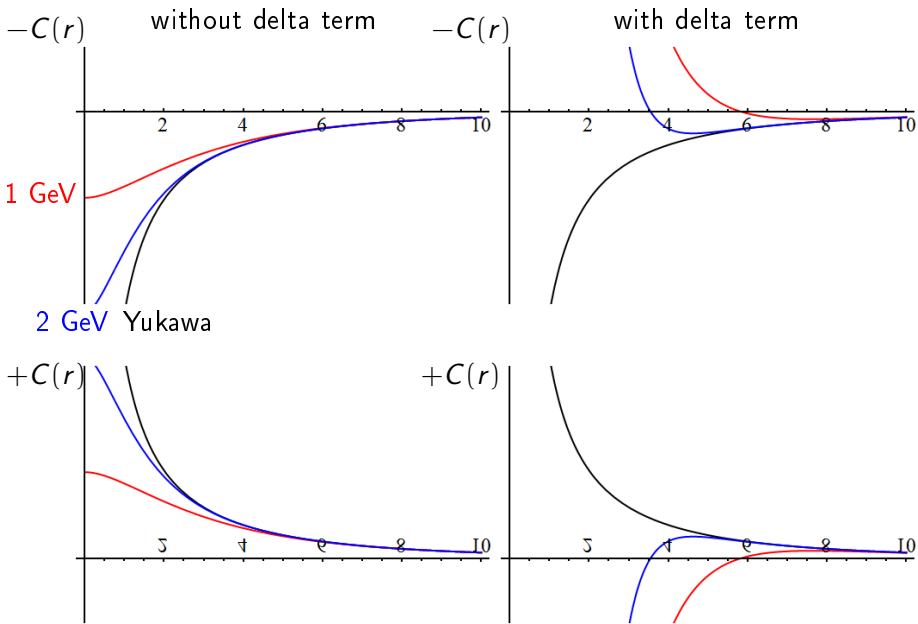
Central potential

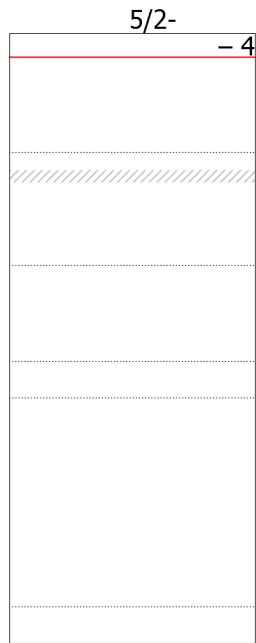
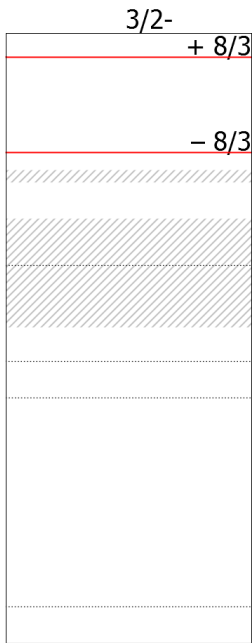
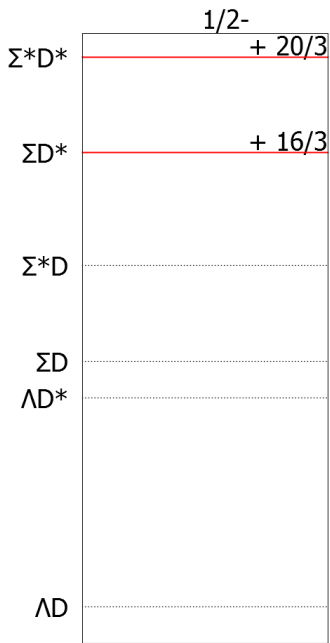
without delta term

with delta term



Central potential





$\Lambda = 600 \text{ MeV}$

$1/2^-$

Σ^*D^* $+ 20/3$

ΣD^* $+ 16/3$

Σ^*D

ΣD

ΛD^*

ΛD

$3/2^-$

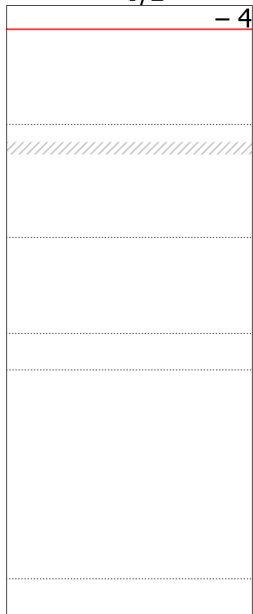
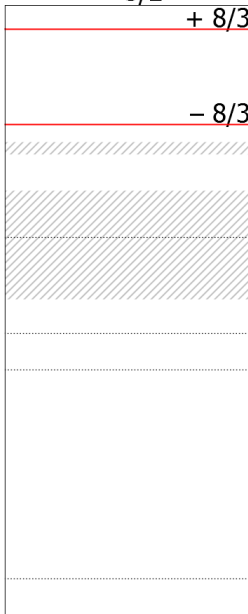
$+ 8/3$

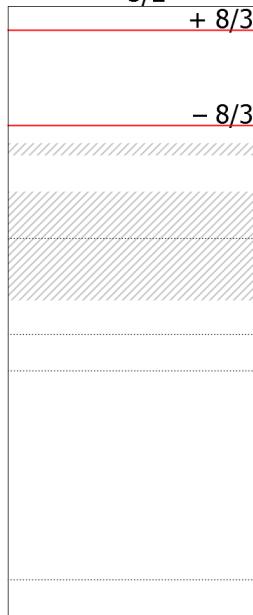
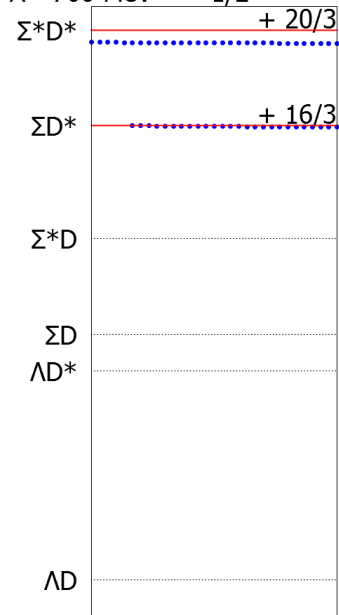
$- 8/3$

$5/2^-$

$- 4$

$- 4$



$\Lambda = 700 \text{ MeV}$ $1/2^-$ $3/2^-$ $5/2^-$ 

$\Lambda = 800 \text{ MeV}$

$1/2^-$

Σ^*D^* $+ 20/3$

ΣD^* $+ 16/3$

Σ^*D

ΣD

ΛD^*

ΛD

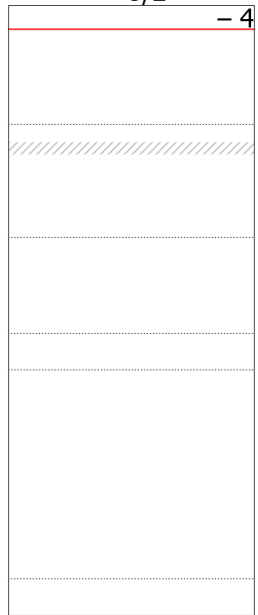
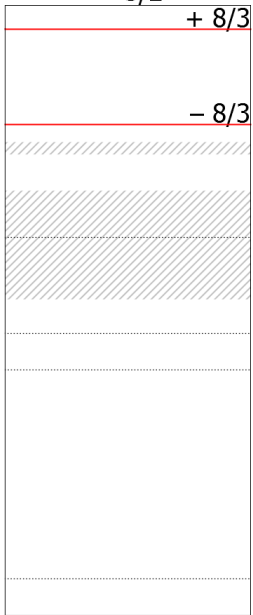
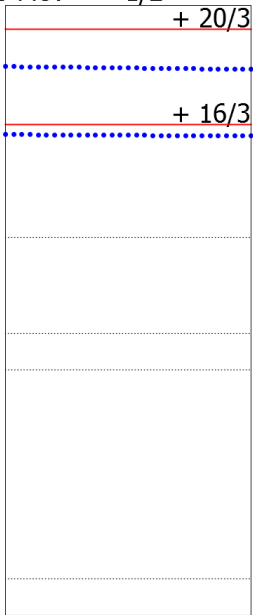
$3/2^-$

$+ 8/3$

$- 8/3$

$5/2^-$

$- 4$

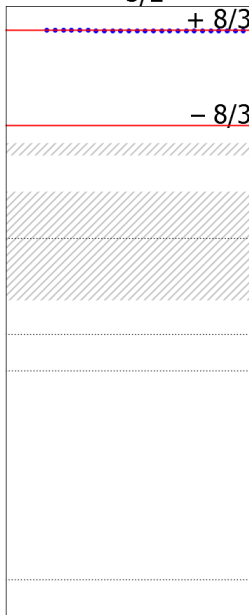
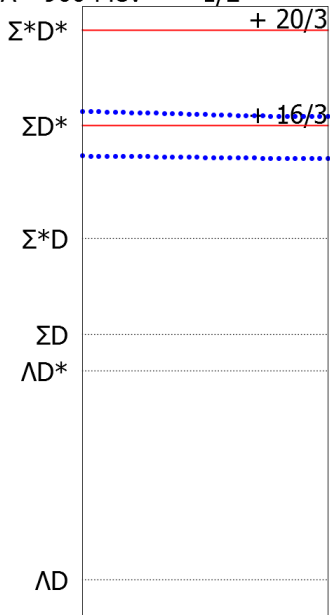


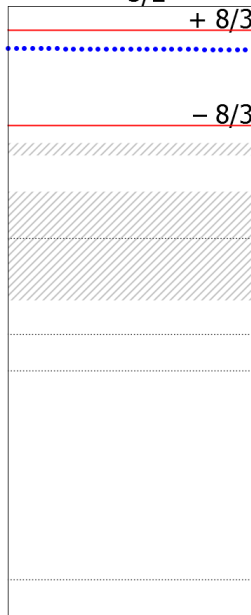
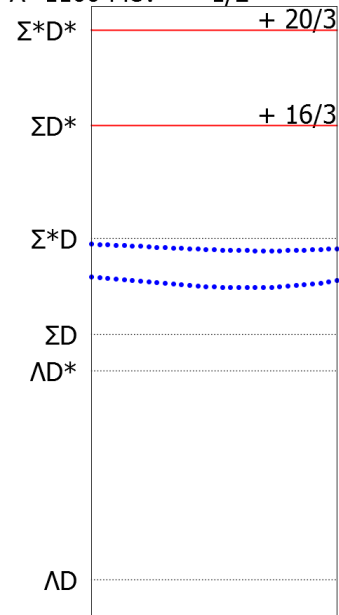
$\Lambda = 900 \text{ MeV}$

$1/2^-$

$3/2^-$

$5/2^-$



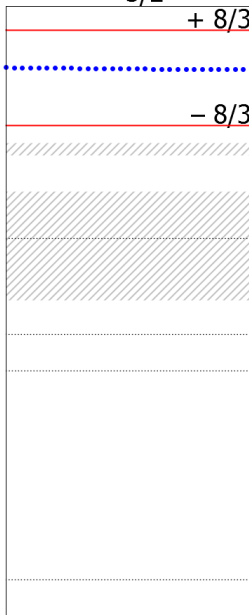
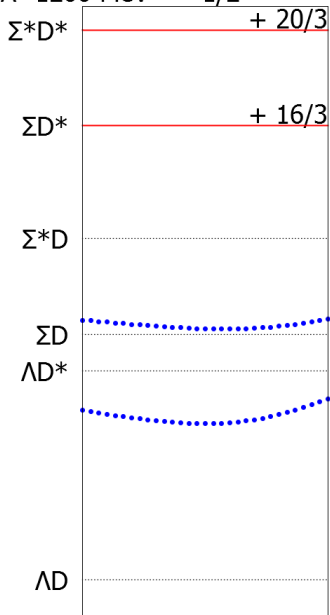
$\Lambda=1100$ MeV $1/2^-$ $3/2^-$ $5/2^-$ 

$\Lambda=1200$ MeV

$1/2^-$

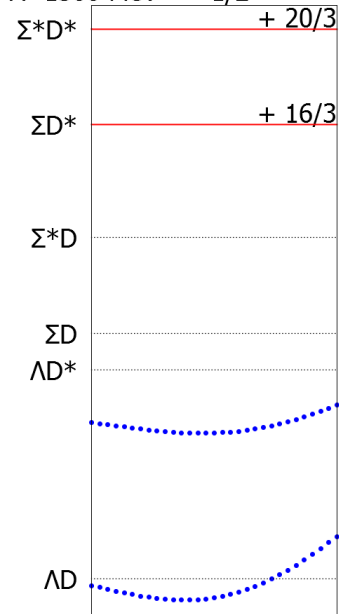
$3/2^-$

$5/2^-$

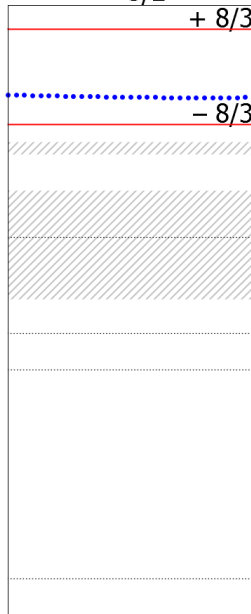


$\Lambda=1300$ MeV

$1/2^-$

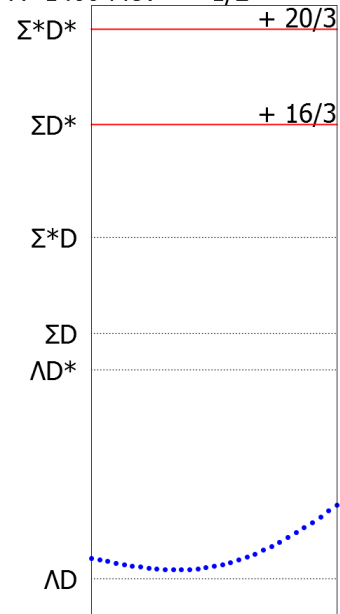
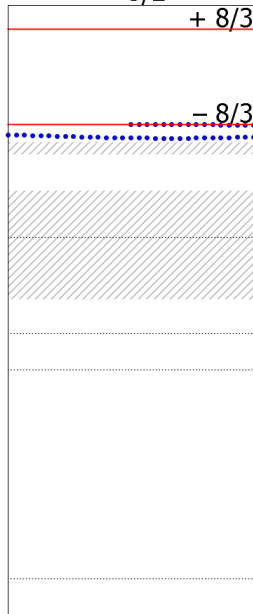


$3/2^-$



$5/2^-$



$\Lambda=1400$ MeV $1/2^-$  $3/2^-$  $5/2^-$ 

$\Lambda = 1500 \text{ MeV}$ $1/2^-$ $3/2^-$ $5/2^-$ $\Sigma^* D^*$ $+ 20/3$ $+ 8/3$ $- 4$ ΣD^* $+ 16/3$ $- 8/3$ $\Sigma^* D$ ΣD ΛD^* ΛD 