

# Charm CPV

[In practice: CPV, mixing and related]

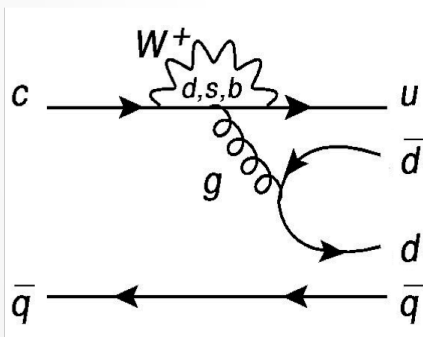
Jolanta Brodzicka, INP PAS (Krakow)  
on behalf of LHCb

Implications Workshop  
CERN, November 2017

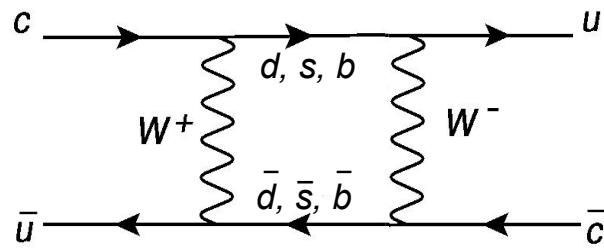


# Charm: unique, complementary but difficult

- Unique access to up-type quarks  
(flavour physics with top quark limited)
- $d, s, b$  quarks in loops: different NP particles/couplings?  
⇒ complementary to strange and beauty
- Loops very suppressed in charm  
⇒ CPV, mixing, rare decays suppressed in SM



Needed for CPV



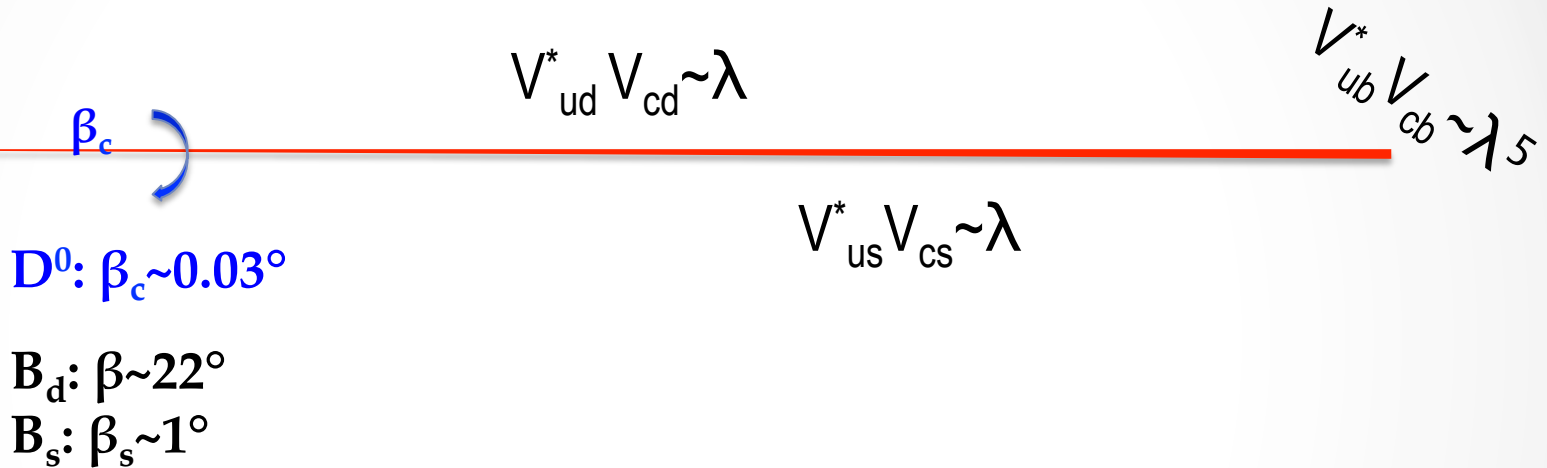
$D^0$ - $\bar{D}^0$  mixing @ short distance

- b loop  $\sim V_{ub} V_{cb} (m_b/m_W)^2$
- s & d: GIM suppressed, cancel in U-spin limit

- Large non-perturbative corrections ( $\sim 1/m_c$ ) ⇒ difficult to calculate

# Theoretical reality, in short

- Openness of charm Unitarity Triangle  $\Rightarrow$  CPV expected in SM



- Direct CPV (in decays)
  - $O(10^{-3})$  in SCS decays w/ penguin contribution
  - $O(10^{-2})$  wherever penguin increased:  $D^0 \rightarrow K_S K_S, K^{*0} K^{*0}, \rho\gamma, \varphi\gamma$
- Indirect CPV (mixing related)  $\sim O(10^{-4})$

# Experimental reality, in short

HFLAV Nov2016

- $D^0$ - $\bar{D}^0$  mixing

- established

No-mixing hypothesis excluded by  $>11\sigma$

- $x$  still not significant

- CPV

- not observed yet

- becoming sensitive to SM

- indirect CPV precision:  $O(10^{-4})$

- direct CPV precision: down to  $O(10^{-3})$

- Rare decays

- looking for signals, precision down to  $O(10^{-8})$

- not there yet to go beyond (asymmetries, LFU, polarisations)

## Mixing frequencies

$$x = (0.32 \pm 0.14)\%$$

$$y = (0.69^{+0.06}_{-0.07})\%$$

## Indirect CPV parameters

$$|q/p| = 0.89^{+0.08}_{-0.07}$$

$$\phi = \arg(q/p) = -13^{+10}_{-9} \text{ deg}$$

CPV if  $|q/p| \neq 1$  or  $\phi \neq 0$

# This year news

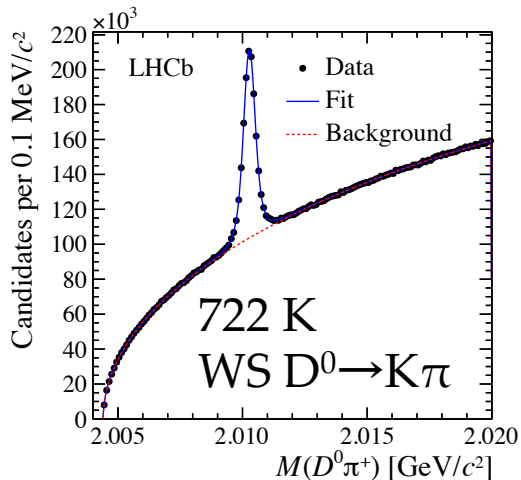
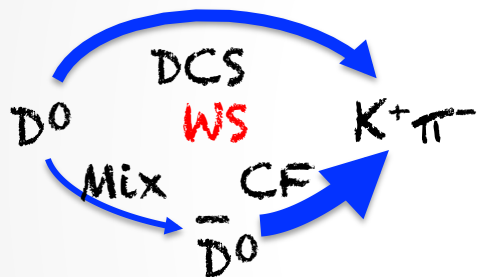
- WS/RS  $D^0 \rightarrow K\pi$  time evolution  
Run1+Run2, prompt charm from  $pp \rightarrow D^{*\pm} X$  New
- $A_\Gamma$  from  $D^0 \rightarrow K^+K^-, \pi^+\pi^-$  PRL 118, 261803 (2017)  
Run1, prompt charm
- $\Delta A_{CP}$  for  $\Lambda_c \rightarrow p\pi^+\pi^-$  and  $\Lambda_c \rightarrow pK^+K^-$  New  
Run1, secondary charm from  $\Lambda_b \rightarrow \Lambda_c \mu \nu$
- Amplitude Analysis of  $D^0 \rightarrow K^\pm \pi \pi \pi$ , New  
Run1, secondary charm from  $B \rightarrow D^{*\pm} \mu \nu$

# Mixing & Indirect CPV



# Time-evolution of (Wrong-Sign) $D^0 \rightarrow K^+ \pi^-$

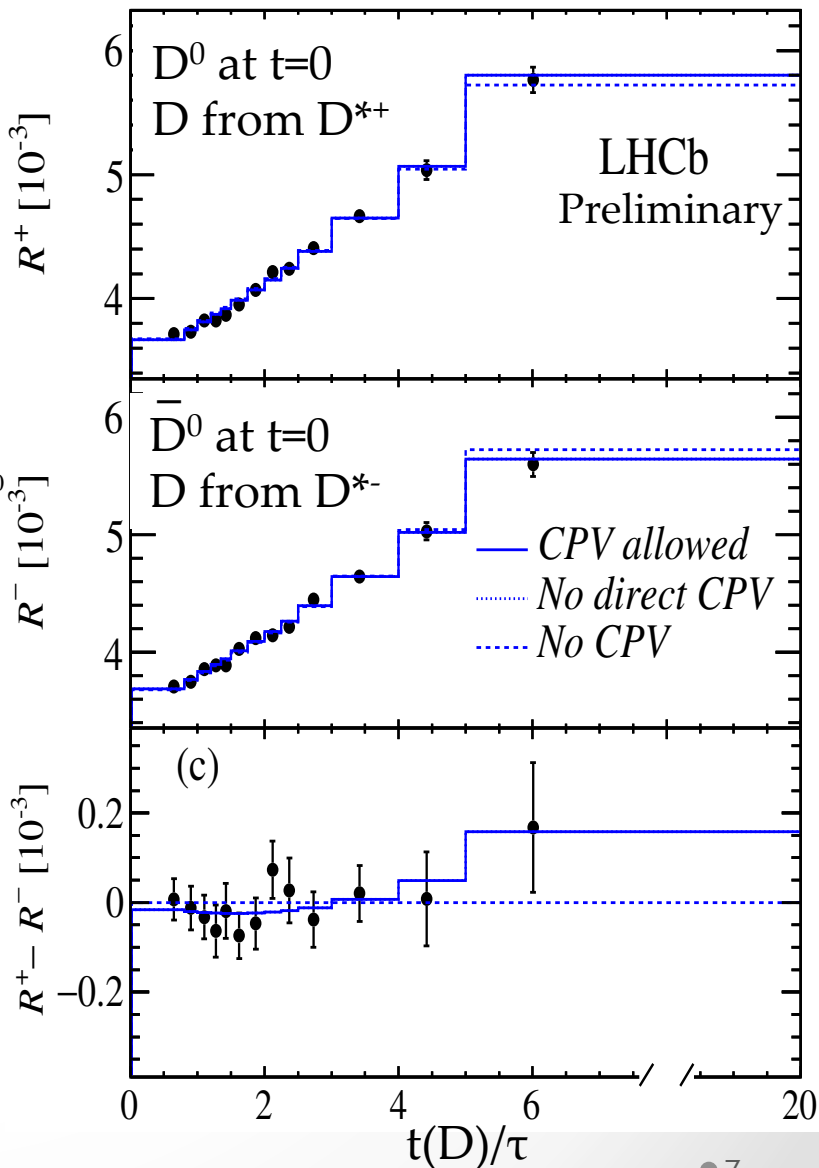
- 2011-2016 data prompt charm



$$R(t) = \frac{N_{WS}(t)}{N_{RS}} \approx R_D + \sqrt{R_D y'} \frac{t}{\tau} + \frac{x'^2 + y'^2}{4} \left(\frac{t}{\tau}\right)^2$$

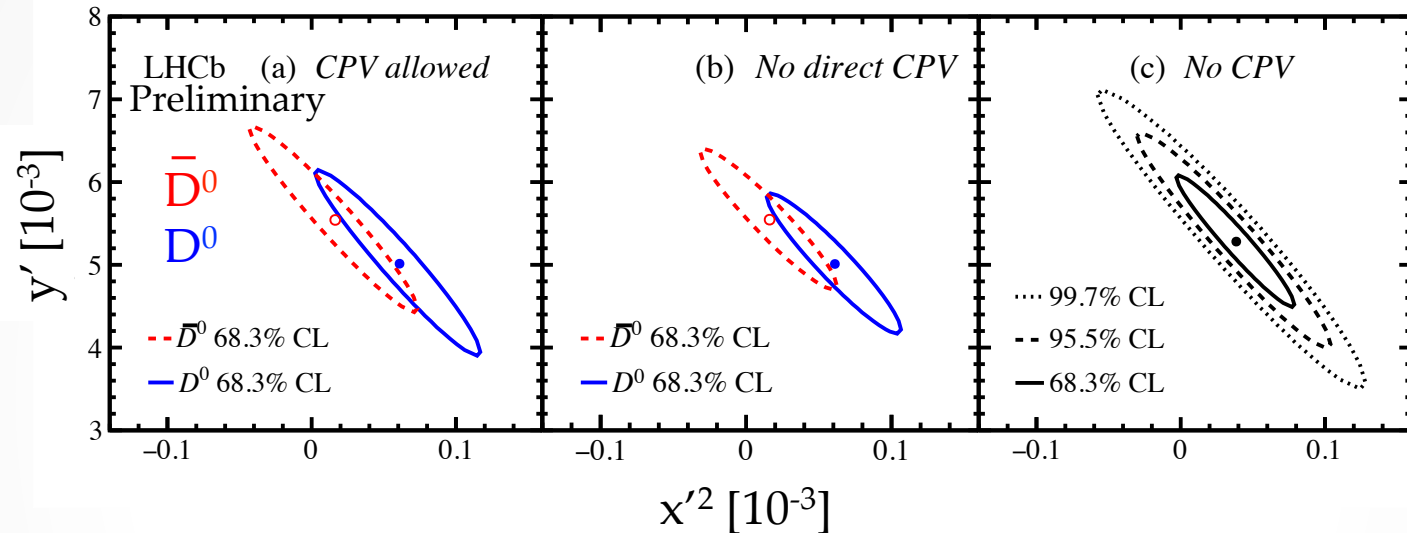
**Decay Interference Mixing**

- $R^\pm(t)$  for D from  $D^{*\pm} \Rightarrow$  measure CPV



# WS $D^0 \rightarrow K^+ \pi^-$ : results

- Confidence-level contours on  $(x'^2, y')$



- This study (2011-2016)

$$y' = (5.28 \pm 0.45 \pm 0.27) \times 10^{-3}$$

$$x'^2 = (3.9 \pm 2.3 \pm 1.4) \times 10^{-5}$$

$$1.00 < |q/p| < 1.35 \text{ @68\% CL}$$

- LHCb (2011-2012) PRL111, 251801 (2013)

$$y' = (4.8 \pm 0.8 \pm 0.5) \times 10^{-3}$$

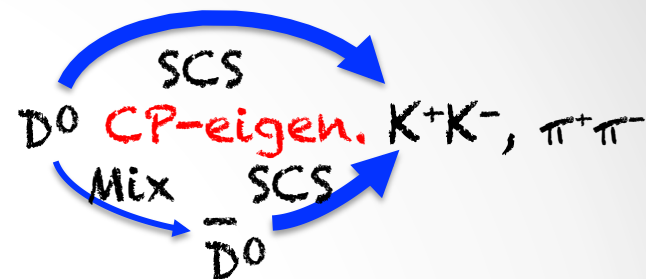
$$x'^2 = (5.5 \pm 4.2 \pm 2.6) \times 10^{-5}$$

- Direct CPV in DCS  $D^0 \rightarrow K^+ \pi^-$   $A_{CP}^{direct} = \frac{R_D^+ - R_D^-}{R_D^+ + R_D^-} = (-0.01 \pm 0.81 \pm 0.42)\%$



# $A_\Gamma$ : quest for indirect CPV

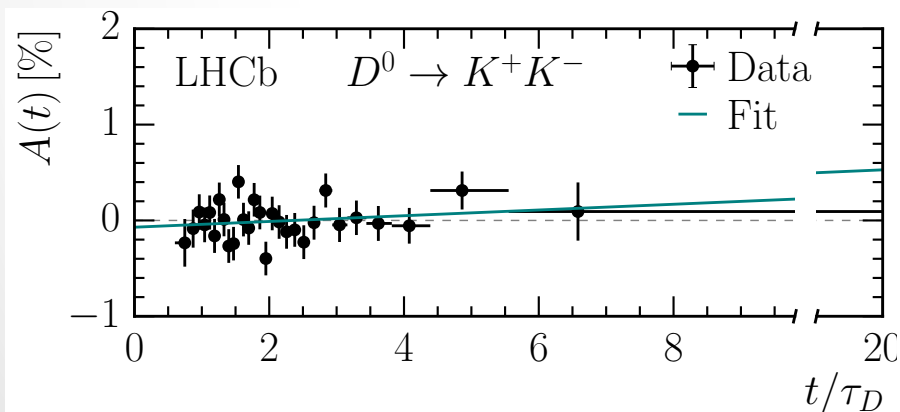
- Does mixing affect  $D^0$  and  $\bar{D}^0$  differently?
- Easiest access via  $A_\Gamma$



$$A_\Gamma = \frac{\tau(\bar{D}^0 \rightarrow h^+h^-) - \tau(D^0 \rightarrow h^+h^-)}{\tau(\bar{D}^0 \rightarrow h^+h^-) + \tau(D^0 \rightarrow h^+h^-)} \simeq -A_{CP}^{\text{indirect}}$$

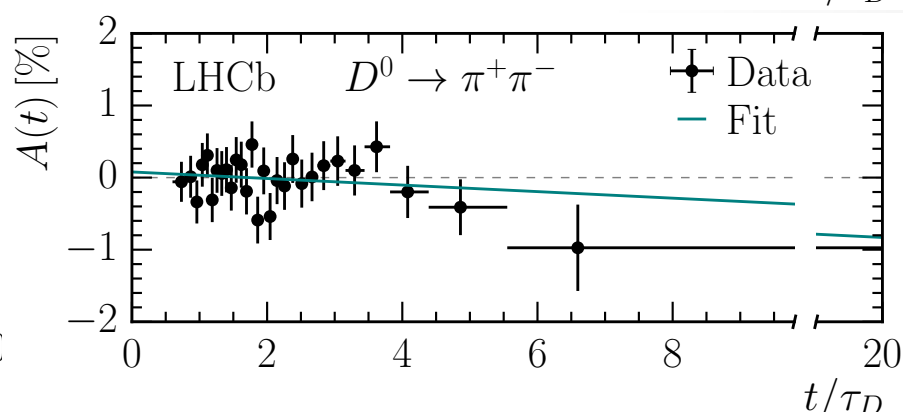
- Asymmetry of yields in  $t(D)$  bins:  $A_{CP}(t) \simeq A_{CP}^{\text{direct}} - A_\Gamma \frac{t}{\tau_D}$
- 2011+2012 data, prompt charm

$D^0 \rightarrow K^+K^-$  ~10M



$$A_\Gamma(KK) = (-0.030 \pm 0.032 \pm 0.010)\%$$

$D^0 \rightarrow \pi^+\pi^-$  ~3M



$$A_\Gamma(\pi\pi) = (+0.046 \pm 0.058 \pm 0.012)\%$$

# $A_\Gamma$ : entering SM area

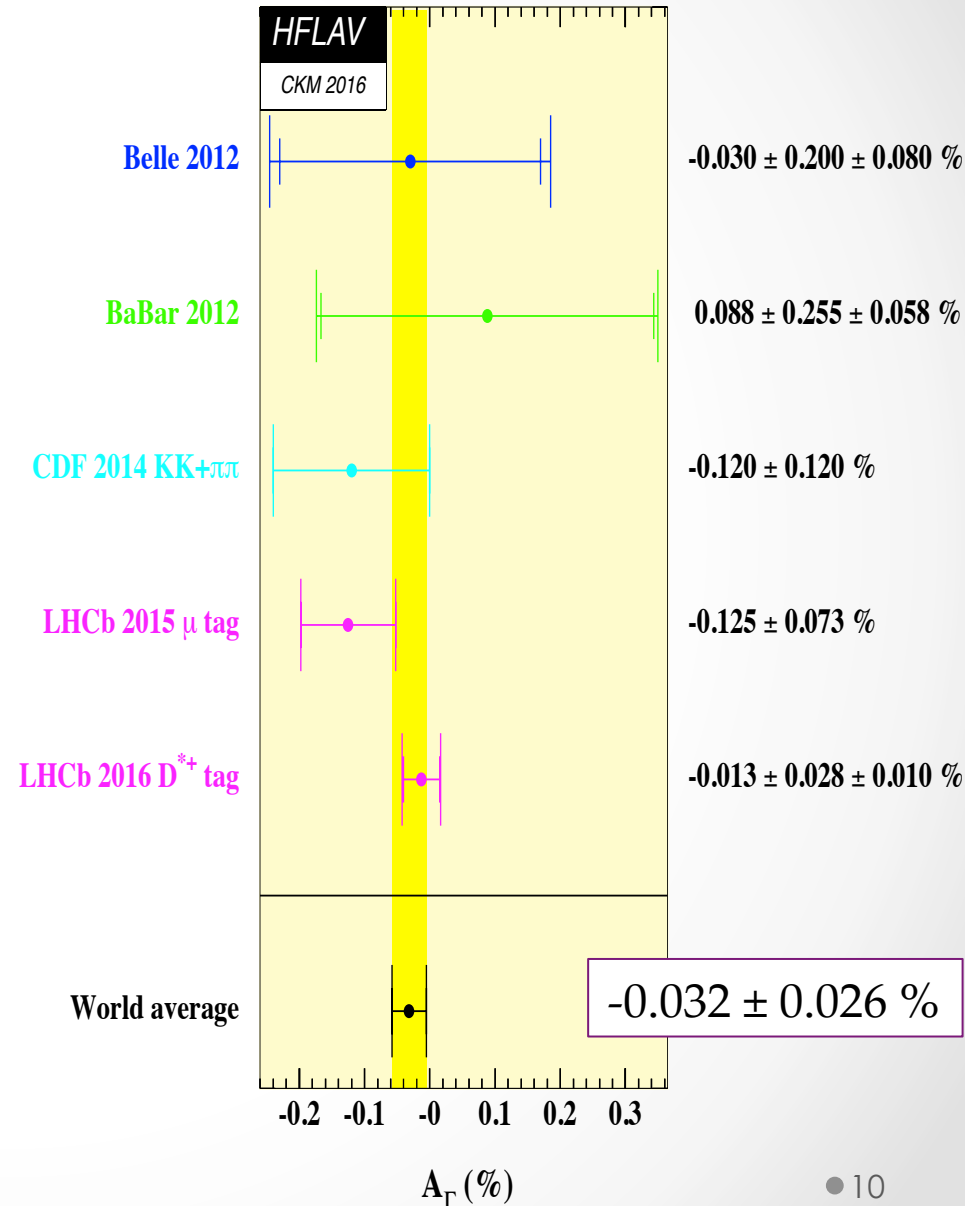
- Sensitivity:  $O(10^{-4})$   
Limited by statistics
- Indirect CPV in SM  $\sim 10^{-4}$

- $A_\Gamma$  in terms of basic parameters

$$A_\Gamma = \frac{1}{2} \left[ \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) y \cos \phi - \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) x \sin \phi \right]$$

CPV in mixing in mixing-  
interference

⇒ sensitivity to  $q/p$  depends on  $x$



# Multi-body decays are the (high)way

- Measure how phase space evolves with time [t-dep. Dalitz]

✓ **Direct access to  $x, y, |q/p|, \phi$**

✓ Access to amplitudes & phases  $\Rightarrow$  no external input

✓ No dilution from coherence factor

✗ Need model to describe resonances

- Sensitivity from  $D^0 \rightarrow f$  &  $D^0 \rightarrow \bar{f}$  interferences  
(large 'local' coherence factors are best)

- Golden modes

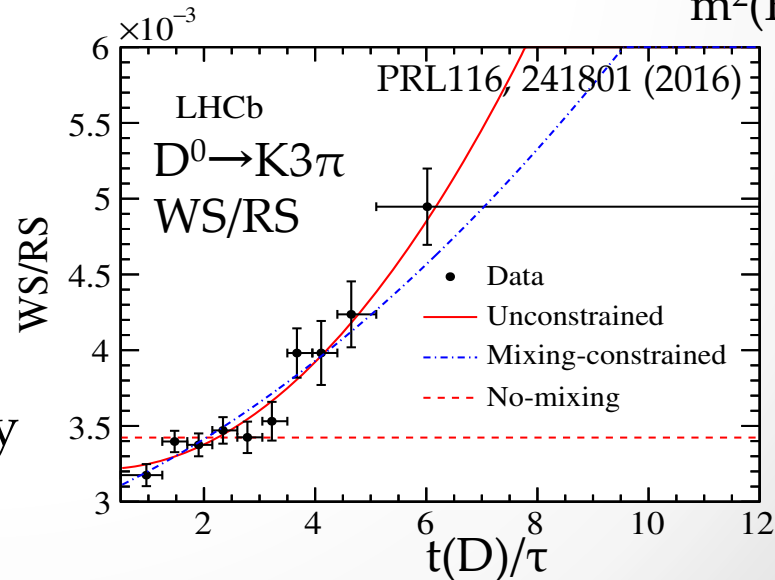
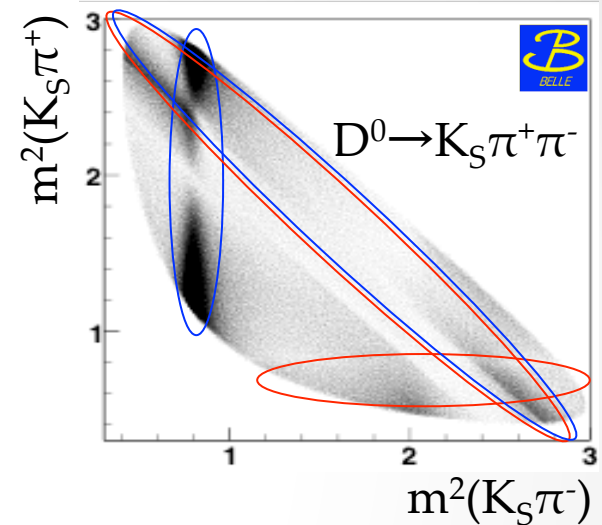
-  $D^0 \rightarrow K_S \pi^+ \pi^-$

Expect significant  $x$  with Run1+2

-  $D^0 \rightarrow K \pi \pi \pi$

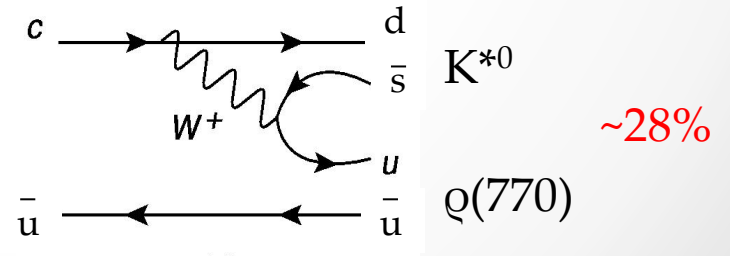
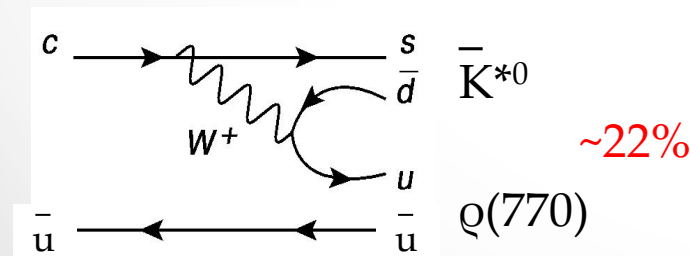
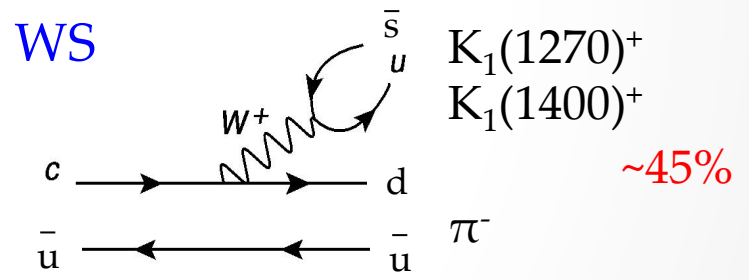
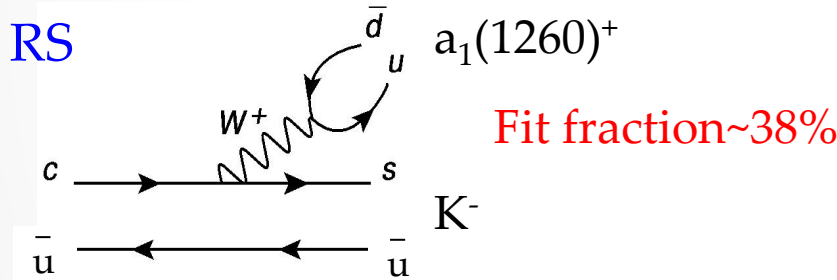
Needed for  $q/p$

So far phase-space integrated study



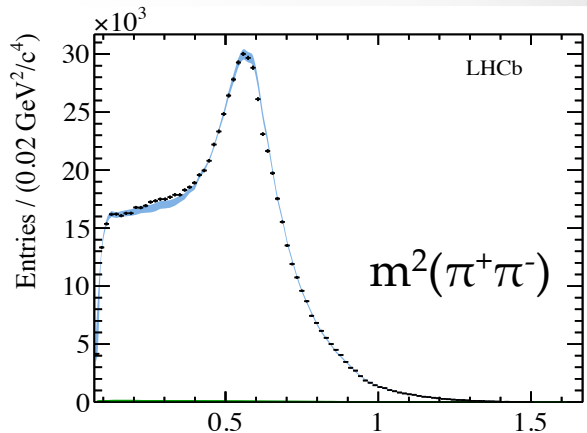
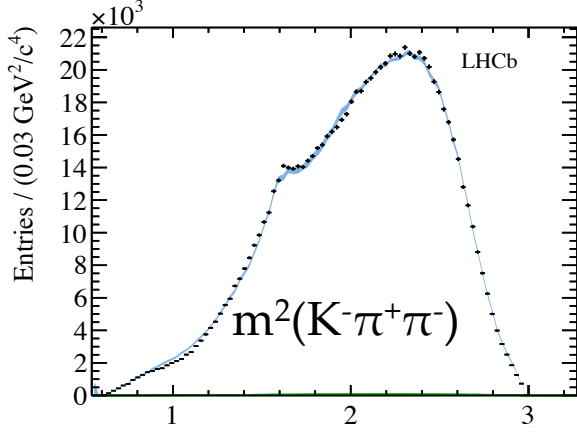
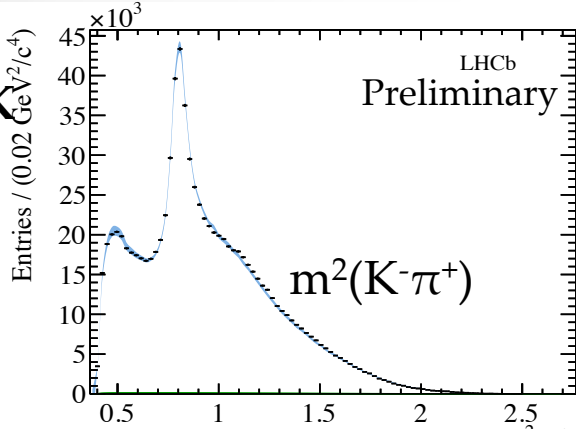
# Amplitude Analysis of $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$ (RS) & $K^+ \pi^- \pi^+ \pi^-$ (WS)

- 2011-2012 data,  $D^0$  from  $B \rightarrow D^{*\pm} \mu \nu$
- 1<sup>st</sup> analysis for WS, improved for RS
- time-integrated study (ignoring D-mixing)
- RS decays  $\approx$  CF  $c \rightarrow s \bar{d} u$  WS decays  $\approx$  DCS  $c \rightarrow d \bar{s} u$
- $\Rightarrow$  different dynamics
- Dominating contributions:

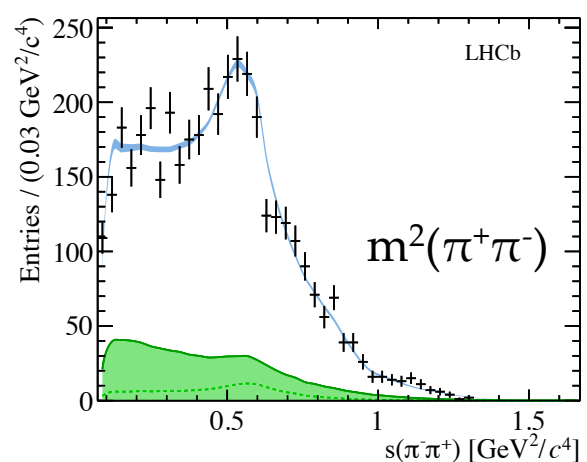
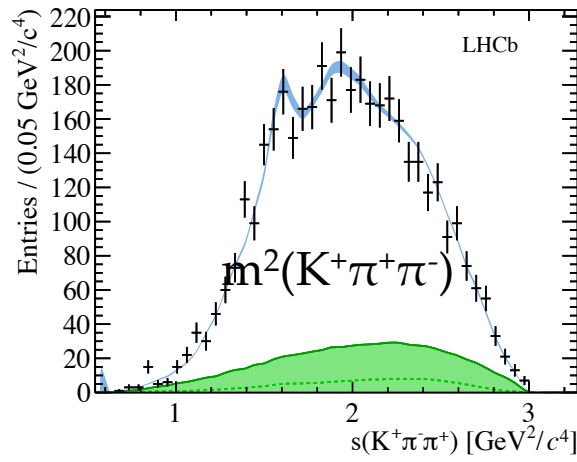
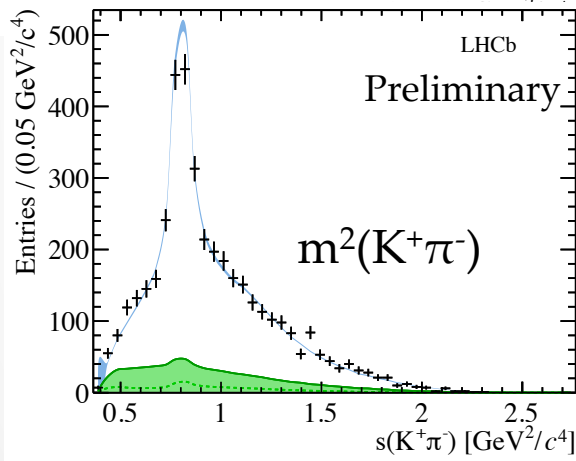


# Amplitude Analysis of $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$ (RS) & $K^+ \pi^- \pi^+ \pi^-$ (WS)

**RS**  
900K



**WS**  
3K



• Fit qualities:

RS  $\chi^2/\text{ndf} = 40483/32701 = 1.24$

WS  $\chi^2/\text{ndf} = 350/239 = 1.46$

**background**  
**model uncertainty**

# $D^0 \rightarrow K3\pi$ toward mixing

- Coherence factor  
(interference between DCS and CF)

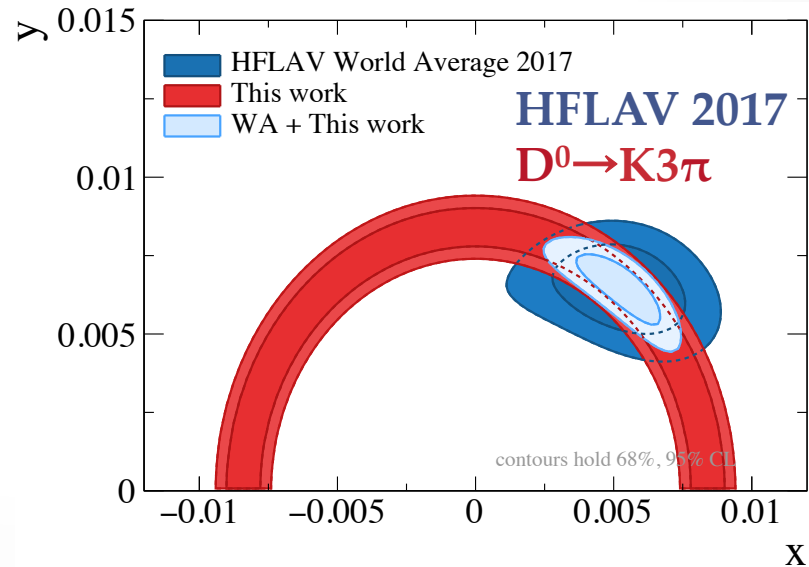
$$\int A_{K-3\pi}(\mathbf{r}) A_{K+3\pi}(\mathbf{r}) d\mathbf{r} \Rightarrow R_{coh} e^{-i\delta_{K3\pi}}$$

- 5-dim bins of equal strong phase
- Large 'local' coherence factors

- Add t-dependence  
for charm mixing & CPV
- Sensitivity study with prompt  
 $D^0 \rightarrow K3\pi$  from 2015+2016  
(PhD by Dominik Müller)

Bin	$R_{K3\pi}$	$\delta_{K3\pi} [^\circ]$
Global	$0.454 \pm 0.020$	128
1	$0.701 \pm 0.017$	$169 \pm 3$
2	$0.691 \pm 0.016$	$151 \pm 1$
3	$0.726 \pm 0.010$	$133 \pm 1$
4	$0.742 \pm 0.008$	$117 \pm 1$
5	$0.783 \pm 0.005$	$102 \pm 2$
6	$0.764 \pm 0.007$	$84 \pm 3$
7	$0.424 \pm 0.013$	$26 \pm 3$
8	$0.473 \pm 0.030$	$-149 \pm 7$

Preliminary



# Direct CPV



Most precise  
Very important

# $A_{CP}$ in two-body decays w/ penguin

	LHCb	Belle	BaBar	BESIII
Mode	$A_{CP}$ [%]			
$D^0 \rightarrow K^+ K^-$	$+0.04 \pm 0.12 \pm 0.10$	$-0.32 \pm 0.21 \pm 0.09$	$+0.00 \pm 0.34 \pm 0.13$	
$D^0 \rightarrow \pi^+ \pi^-$	$+0.07 \pm 0.14 \pm 0.11$	$+0.55 \pm 0.36 \pm 0.09$	$-0.24 \pm 0.52 \pm 0.22$	
$D^0 \rightarrow K_s K_s$	$-2.9 \pm 5.2 \pm 2.2$	$+0.00 \pm 1.53 \pm 0.17$		
$D^0 \rightarrow \pi^0 \pi^0$		$-0.03 \pm 0.64 \pm 0.10$		
$D^0 \rightarrow K_s \eta$		$+0.54 \pm 0.51 \pm 0.16$		
$D^0 \rightarrow K_s \eta'$		$+0.98 \pm 0.67 \pm 0.14$		
$D^+ \rightarrow K_s K^+$	$+0.03 \pm 0.17 \pm 0.14$	$+0.08 \pm 0.28 \pm 0.14$	$+0.46 \pm 0.36 \pm 0.25$	$-1.5 \pm 2.8 \pm 1.6$
$D^+ \rightarrow K_L K^+$				$-3.0 \pm 3.2 \pm 1.2$
$D^+ \rightarrow \phi \pi^+$	$-0.04 \pm 0.14 \pm 0.14$	$+0.51 \pm 0.28 \pm 0.05$		
$D^+ \rightarrow \eta \pi^+$		$+1.74 \pm 1.13 \pm 0.19$		
$D^+ \rightarrow \eta' \pi^+$	$-0.61 \pm 0.72 \pm 0.55 \pm 0.12$	$-0.12 \pm 1.12 \pm 0.17$		
$D_s^+ \rightarrow K_s \pi^+$	$+0.38 \pm 0.46 \pm 0.17$	$+5.45 \pm 2.50 \pm 0.33$	$+0.3 \pm 2.0 \pm 0.3$	
$D_s^+ \rightarrow \eta' \pi^+$	$-0.82 \pm 0.36 \pm 0.24 \pm 0.27$			



$$\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^+ K^-) - A_{CP}(D^0 \rightarrow \pi^+ \pi^-)$$

- Simple & sensitive

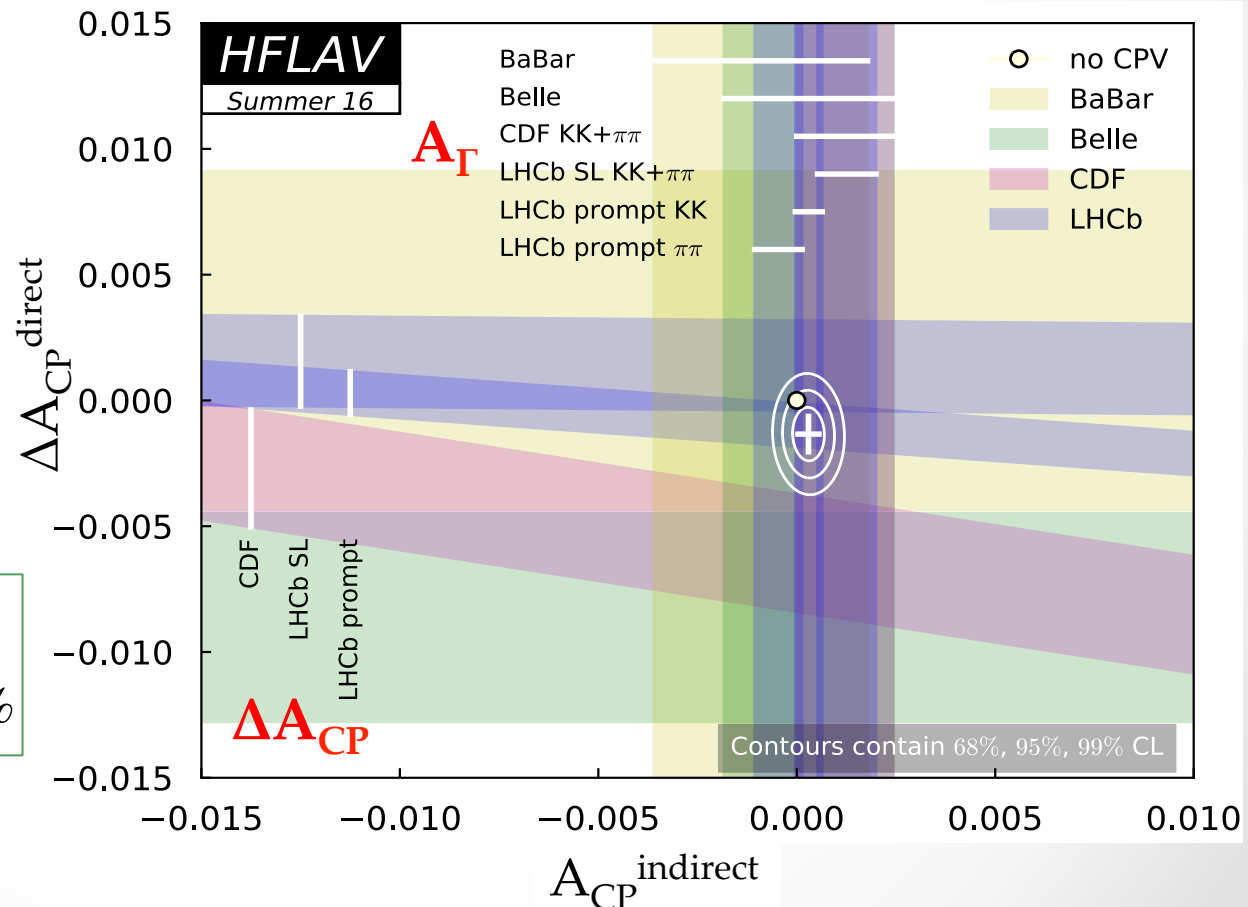
$$\Delta A_{CP} \simeq \left[ A_{CP}^{\text{direct}}(KK) - A_{CP}^{\text{direct}}(\pi\pi) \right] + \frac{\Delta \langle t \rangle}{\tau_D} A_{CP}^{\text{indirect}}$$

- In SM:  $|\Delta A_{CP}^{\text{direct}}| \leq 0.6\%$

- HFLAV average

$$\Delta A_{CP}^{\text{direct}} = (-0.13 \pm 0.07)\%$$

$$A_{CP}^{\text{indirect}} = (0.030 \pm 0.026)\%$$



# Prospects for direct CPV searches

Precision down to  $O(10^{-3})$ , still no evidence

- Will improve by 6-7 times with LHCb 50/fb (in  $\sim 10$  years)
- Important Belle2 input:  $D^0 \rightarrow \pi^0 \pi^0$ ,  $D^0 \rightarrow K_S K_S$ ,  $D^+ \rightarrow \pi^+ \pi^0$

Exploit correlations,  $A_{CP}$  not enough

- Between modes related via Isospin or U-spin
- Model independent test of SM, model dependent test of NP
- e.g. SM sum rules:

$$A(D^+ \rightarrow \pi^+ \pi^0) - \bar{A}(D^+ \rightarrow \pi^+ \pi^0) = 0$$

$$\frac{1}{\sqrt{2}} A(\pi^+ \pi^-) + A(\pi^0 \pi^0) - \frac{1}{\sqrt{2}} \bar{A}(\pi^+ \pi^-) - \bar{A}(\pi^0 \pi^0) = 0$$

Look at DCS decays (strongly advertised by I.Bigi)

Explore charm baryons

- Nothing published yet!
- 1<sup>st</sup> evidence for CPV in baryons (in  $\Lambda_b \rightarrow p 3\pi$ ) Nature Phys. 13, 391-396 (2017)

# $\Delta A_{CP}$ for $\Lambda_c \rightarrow pK^+K^-$ and $\Lambda_c \rightarrow p\pi^+\pi^-$

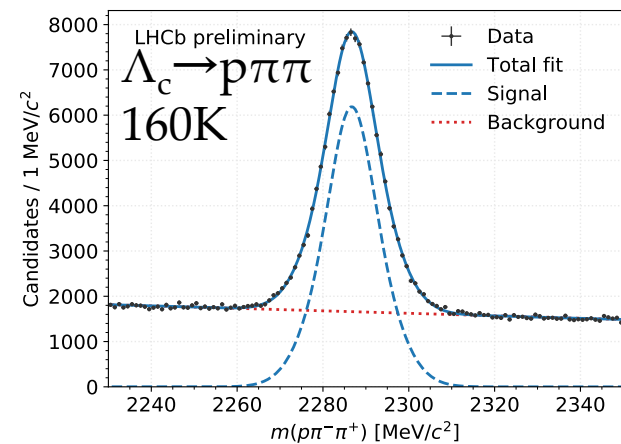
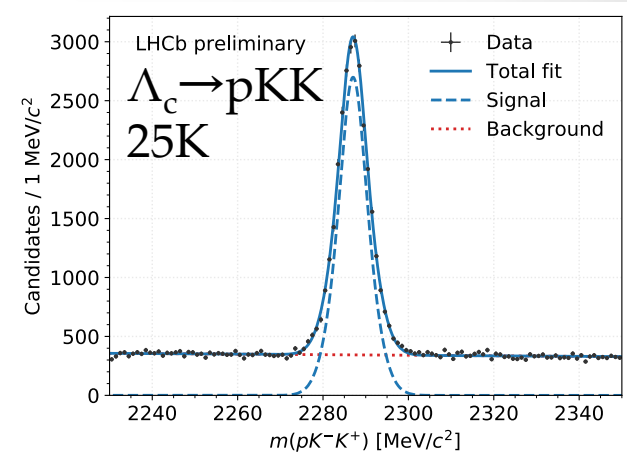
- SCS decays with penguin
- 2011-2012 data,  $\Lambda_c$  from  $\Lambda_b^0 \rightarrow \Lambda_c^- \mu^+ \nu$
- Global asymmetry

$$\Delta A_{CP} = A_{CP}^{\text{Raw}}(pK^-K^+) - A_{CP}^{\text{Raw}}(p\pi^-\pi^+) \\ \approx A_{CP}(pK^-K^+) - A_{CP}(p\pi^-\pi^+)$$

- Asymmetries in  $\Lambda_b$  production & detection of  $p/\bar{p}$ ,  $\mu^-/\mu^+$  cancel out

$$\Delta A_{CP} = (0.30 \pm 0.91 \pm 0.61)\%$$

- 1<sup>st</sup> CPV measurement for charm baryons
- Systematics dominated by MC size



$$A_{CP}^{\text{Raw}}(pK^-K^+) = (3.72 \pm 0.78)\%$$

$$A_{CP}^{\text{Raw}}(p\pi^-\pi^+) = (3.42 \pm 0.47)\%$$

# More with $\Lambda_c \rightarrow ph^+h^-$ ?

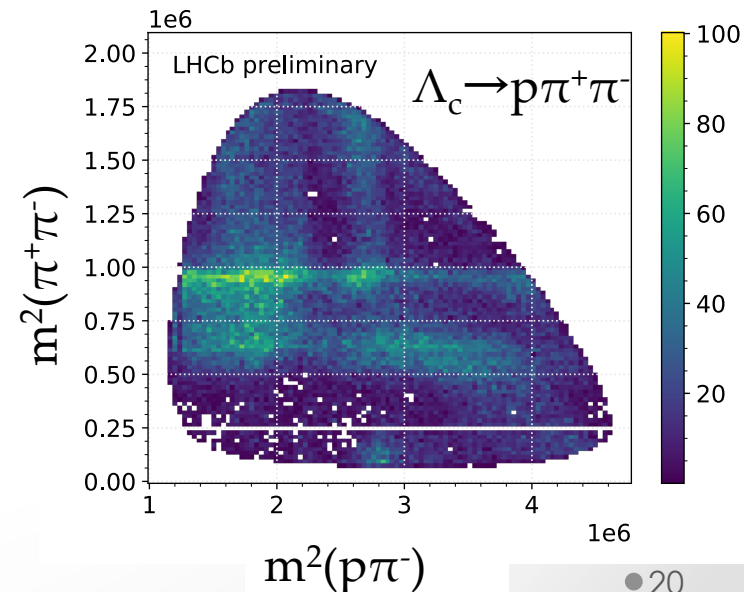
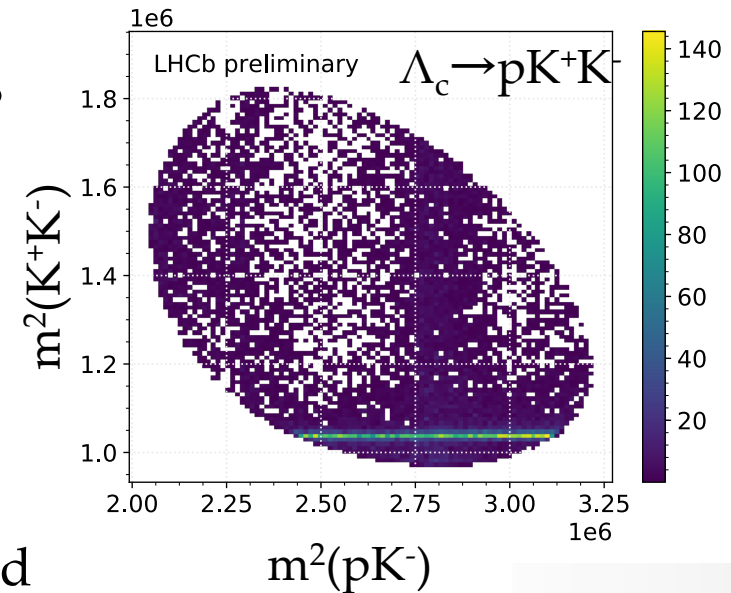
- How about  $\Delta A_{CP}$  in Phase-Space regions?
- CPV 'localised' through resonance interferences  $\Rightarrow$  better sensitivity, but difficult interpretation
- 5D phase space, reduces to Dalitz plot if  $\Lambda_c$  unpolarised
- Rich dynamics, amplitude analysis needed
- For now BF's for SCS and DCS decays

$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-K^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)} = (1.70 \pm 0.03 \pm 0.03) \%,$$

$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow p\pi^-\pi^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)} = (7.44 \pm 0.08 \pm 0.18) \%,$$

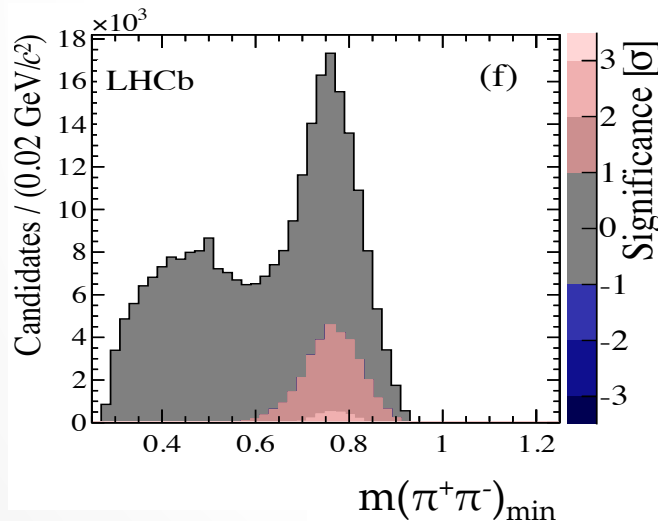
$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow p\pi^-K^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)} = (0.165 \pm 0.015 \pm 0.005) \%,$$

arXiv:1711.01157



# P behind CP violation

- 2&3-body hadronic D decays: only P-even ampl.  $\Rightarrow$  CPV via C-violation
- 4-body D decays: also P-odd amplitudes  $\Rightarrow$  CPV via P-violation
- CPV P-even:  $A_{CP} \sim \sin\Delta\phi_{\text{weak}} \sin\Delta\phi_{\text{strong}}$   
 P-odd:  $A_{CP} \sim \sin\Delta\phi_{\text{weak}} \cos\Delta\phi_{\text{strong}}$   $\leftarrow$  complementary
- $D^0 \rightarrow \pi^+\pi^-\pi^+\pi^-$ : P-odd CPV with  $2.7\sigma$  significance ( $>3\sigma$  for some scenarios)



- P-odd:  $D^0 \rightarrow \rho^0\rho^0$  in P-wave ( $\sim 6\%$ )
- Increased CPV significance points to  $\rho^0 \rightarrow \pi^+\pi^-$

PLB 769 (2017) 345-356

- $\Lambda_c$  decays: P-odd amplitudes already in 2 & 3-body channels!

# Going rare

More by Simone Bifani  
on Wednesday

- The larger penguin contribution, the larger CPV

## Radiative decays: there are signals to explore

- $A_{CP}(D^0 \rightarrow \rho^0 \gamma) \leq 10\%$  de Boer, Hiller arXiv:1701.06392
- Full Belle data PRL118, 051801 (2017)

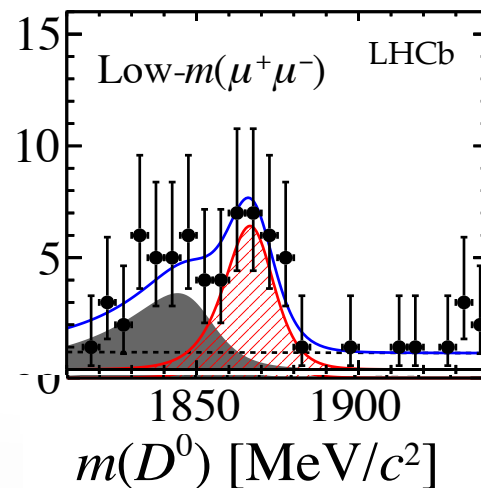
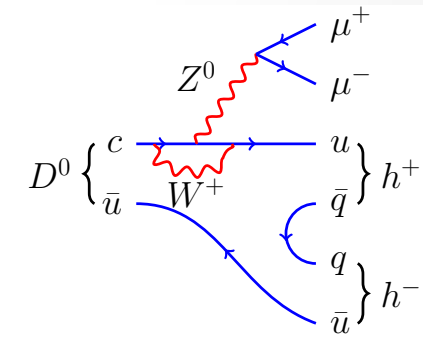
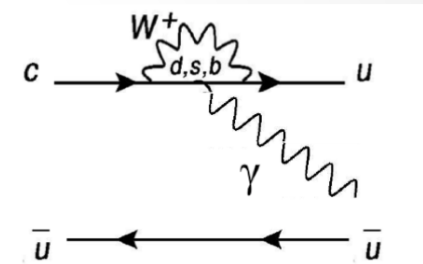
$$A_{CP}(D^0 \rightarrow \phi \gamma) = (-9.4 \pm 6.6 \pm 0.1)\%$$

$$A_{CP}(D^0 \rightarrow \rho^0 \gamma) = (+5.6 \pm 15.1 \pm 0.6)\%$$

- LHCb Run2: at least double Belle signals

## Leptonic decays: first signal!

- $D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$   
with  $m(\mu^+ \mu^-) < 525 \text{ MeV}$   
 $S = 27 \pm 6 (5.4\sigma)$   
PRL119, 181805 (2017)



signal  
 $D^0 \rightarrow 4\pi$

# Summary

- Pinning down the D-mixing frequencies
- Have a chance to get significant  $x$  with Run2 data
- CPV in charm still awaits discovery
- With Run2 data we are entering SM regime
- Observation first, then interpretation...
- With rare charm decays, we will take B-brother path ASAP  
 $P_5'$  for  $D \rightarrow hh \mu^+ \mu^-$ ? In  $\sim 10$  years...

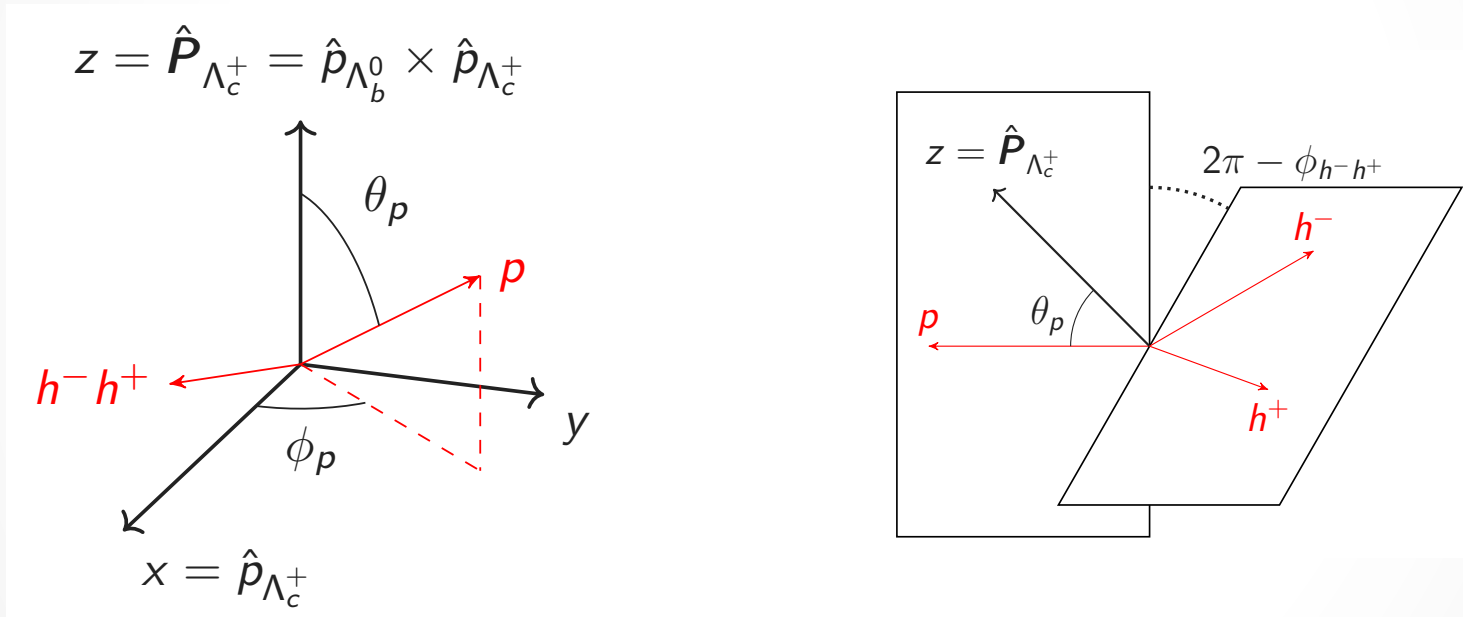
# Backups

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# $\Delta A_{CP}$ for $\Lambda_c \rightarrow ph^+h^-$

- 5D phase space describing  $\Lambda_c \rightarrow ph^+h^-$  dynamics:  
 $m^2(ph^-)$ ,  $m^2(h^+h^-)$ , 3 angles in a coordinate system defined as:  
 $z$ :  $\Lambda_c$  polarisation axis (perp. to production plane),  $x$ :  $\Lambda_c$  flight direction in lab



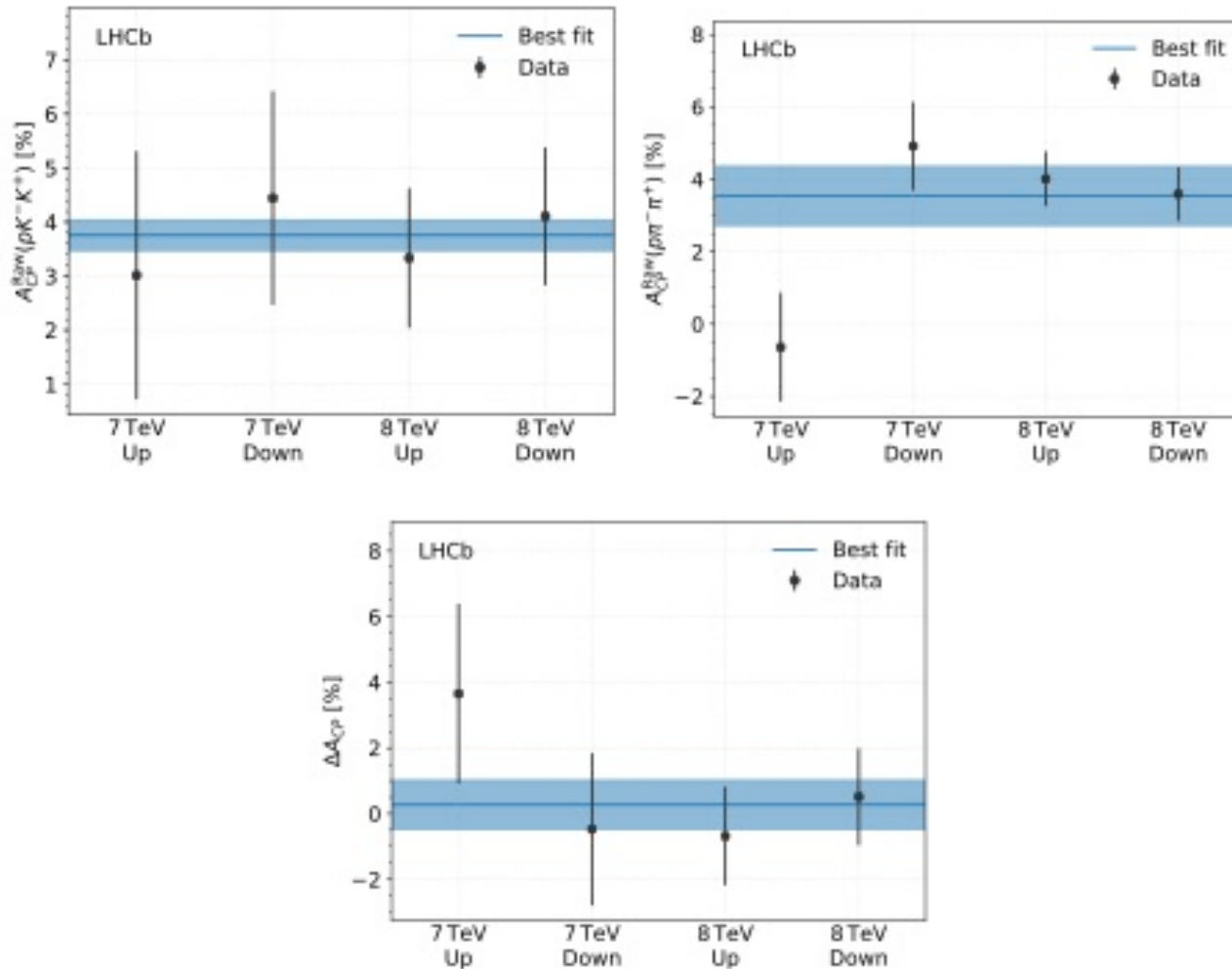
$\theta_p, \phi_p$ : proton polar and azimuthal angles

$\phi_{hh}$ : acoplanarity angle

- for unpolarised  $\Lambda_c$  PS reduces to the two inv. masses

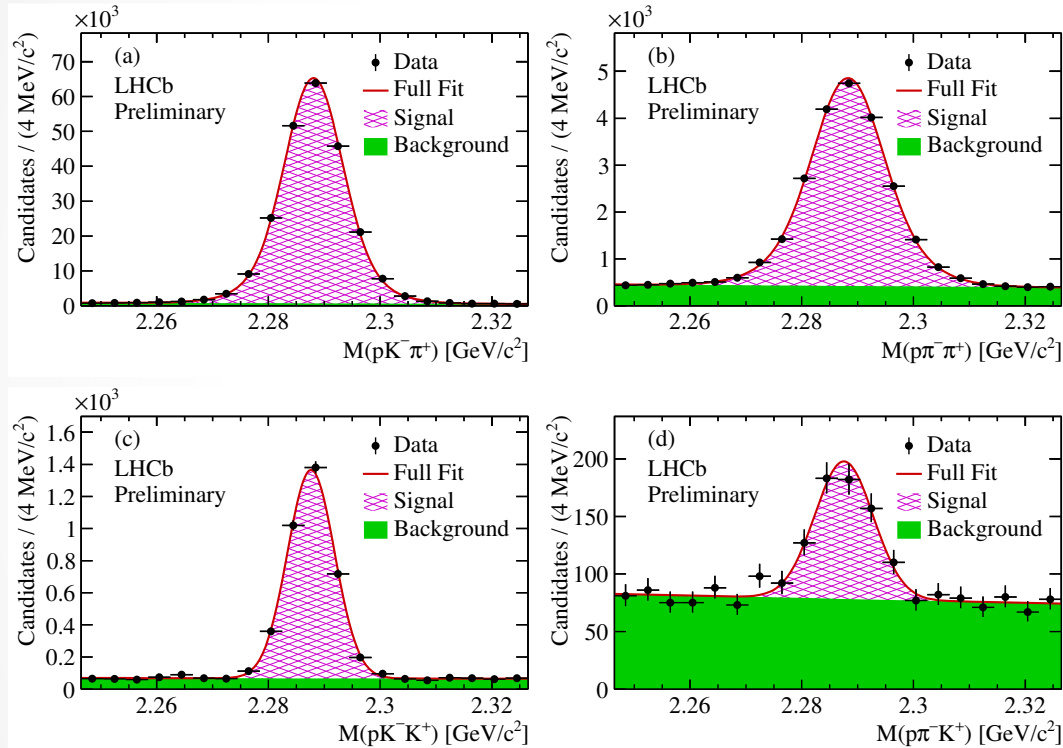
# $\Delta A_{CP}$ for $\Lambda_c \rightarrow ph^+h^-$

- Extra asymmetries:  $A_{CP}^{\text{Raw}}(f) \approx A_{CP}(f) + A_P^{\Lambda_b^0} + A_D^\mu + A_D^f$



# BF of $\Lambda_c \rightarrow ph^+h^-$

- 2011 data,  $\Lambda_c$  from  $\Lambda_b^0 \rightarrow \Lambda_c^- \mu^+ \nu$  (prompt charm as x-check)



	Mode	Yield
SL	$\Lambda_c^+ \rightarrow pK^- \pi^+$	$226851 \pm 522$
	$\Lambda_c^+ \rightarrow p\pi^- \pi^+$	$19584 \pm 207$
	$\Lambda_c^+ \rightarrow pK^- K^+$	$3420 \pm 62$
	$\Lambda_c^+ \rightarrow p\pi^- K^+$	$392 \pm 35$
Prompt	$\Lambda_c^+ \rightarrow pK^- \pi^+$	$58115 \pm 1561$
	$\Lambda_c^+ \rightarrow p\pi^- \pi^+$	$7480 \pm 328$
	$\Lambda_c^+ \rightarrow pK^- K^+$	$766 \pm 61$

SL analysis systematic [%]	$\Lambda_c^+ \rightarrow p\pi^- \pi^+$	$\Lambda_c^+ \rightarrow pK^- K^+$	$\Lambda_c^+ \rightarrow p\pi^- K^+$
PID selection efficiency ratio	2.0	1.4	2.0
Unknown $\Lambda_c^+ \rightarrow phh'$ decay structure	1.1	0.7	1.7
Finite simulation statistics	0.3	0.3	0.3
Trigger efficiency ratio	0.6	0.8	0.3
<b>Total</b>	<b>2.4</b>	<b>1.8</b>	<b>2.7</b>

# $D^0 \rightarrow K3\pi$ Amplitude Analysis

•  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  (RS)

	Fit Fraction [%]
$K^*(892)^0 \rho(770)^0$	$7.34 \pm 0.08 \pm 0.47$
$[K^*(892)^0 \rho(770)^0]^{L=1}$	$6.03 \pm 0.05 \pm 0.25$
$[K^*(892)^0 \rho(770)^0]^{L=2}$	$8.47 \pm 0.09 \pm 0.67$
$\rho(1450)^0 K^*(892)^0$	$0.61 \pm 0.04 \pm 0.17$
$[\rho(1450)^0 K^*(892)^0]^{L=1}$	$1.98 \pm 0.03 \pm 0.33$
$[\rho(1450)^0 K^*(892)^0]^{L=2}$	$0.46 \pm 0.03 \pm 0.15$
$\rho(770)^0 [K^- \pi^+]^{L=0}$	$0.93 \pm 0.03 \pm 0.05$
$\alpha_{3/2}$	
$K^*(892)^0 [\pi^+ \pi^-]^{L=0}$	$2.35 \pm 0.09 \pm 0.33$
$f_{\pi\pi}$	
$\beta_1$	
$a_1(1260)^+ K^-$	$38.07 \pm 0.24 \pm 1.38$
$K_1(1270)^- \pi^+$	$4.66 \pm 0.05 \pm 0.39$
$K_1(1400)^- [K^*(892)^0 \pi^-] \pi^+$	$1.15 \pm 0.04 \pm 0.20$
$K_2^*(1430)^- [K^*(892)^0 \pi^-] \pi^+$	$0.46 \pm 0.01 \pm 0.03$
$K(1460)^- \pi^+$	$3.75 \pm 0.10 \pm 0.37$
$[K^- \pi^+]^{L=0} [\pi^+ \pi^-]^{L=0}$	$22.04 \pm 0.28 \pm 2.09$

$D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$  (WS)

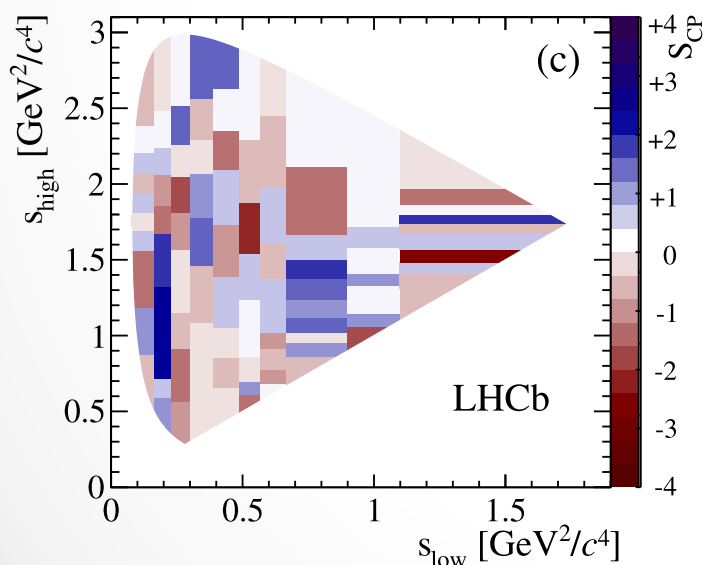
	Fit Fraction [%]
$K^*(892)^0 \rho(770)^0$	$9.62 \pm 1.58 \pm 1.03$
$[K^*(892)^0 \rho(770)^0]^{L=1}$	$8.42 \pm 0.83 \pm 0.57$
$[K^*(892)^0 \rho(770)^0]^{L=2}$	$10.19 \pm 1.03 \pm 0.79$
$\rho(1450)^0 K^*(892)^0$	$8.16 \pm 1.24 \pm 1.69$
$K_1(1270)^+ \pi^-$	$18.15 \pm 1.11 \pm 2.30$
$K_1(1400)^+ [K^*(892)^0 \pi^+] \pi^-$	$26.55 \pm 1.97 \pm 2.13$
$[K^+ \pi^-]^{L=0} [\pi^+ \pi^-]^{L=0}$	$20.90 \pm 1.30 \pm 1.50$

# Direct CPV in multibody decays

- Strong phases vary in Phase Space  $\Rightarrow$  **Local CPV asymmetries**
- **Model dependent**:  $A_{CP}$  for resonances (amplitude analysis)
- **Model independent**: test data consistency with no-CPV, give p-value

binned  $\chi^2$  ( $S_{CP}$  method)

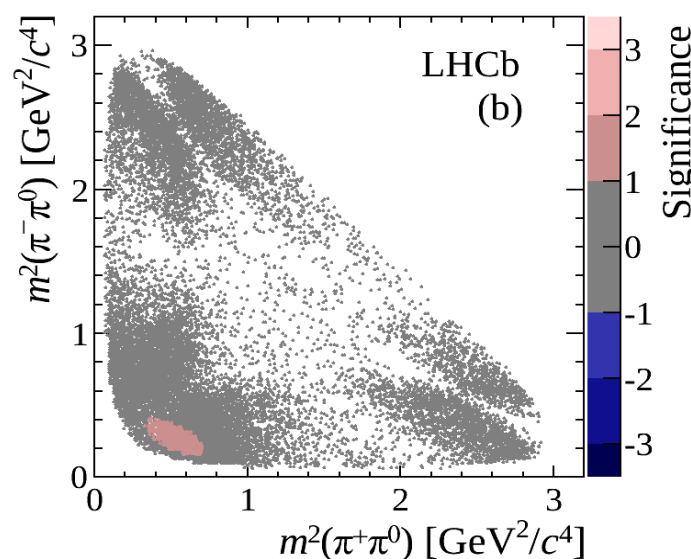
$D^+ \rightarrow \pi^+ \pi^+ \pi^-$  p-value = 50 ÷ 100%



Significance of asymmetry in Dalitz bins


unbinned (Energy Test)

$D^0 \rightarrow \pi^+ \pi^- \pi^0$  p-value = 2 ÷ 5%



Significance of asymmetry for each event

# Direct CPV in 4-body decays

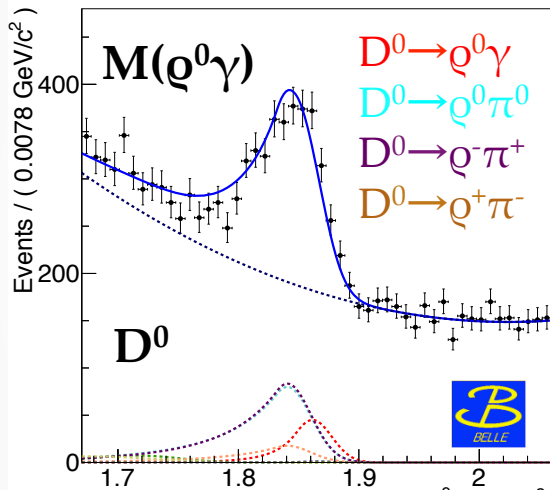
- **Access to P-odd amplitudes**  $\Rightarrow$  CPV via P-violation  
[P-odd amplitude e.g.  $D \rightarrow VV$  in P-wave]
- 2&3-body D decays: P-even ampl. only  $\Rightarrow$  CPV via C-violation  
[Baryons: P-odd also in 2&3-body decays]
- CPV in P-even ampl:  $A_{CP} \sim \sin \Delta \phi_{\text{weak}} \sin \Delta \phi_{\text{strong}}$   
P-odd ampl:  $A_{CP} \sim \sin \Delta \phi_{\text{weak}} \cos \Delta \phi_{\text{strong}}$   complementary
- Triple-product method (aka T-odd): sensitive to P-odd CPV **only**

Mode	$A_{CP}^{\text{P-odd}} [10^{-3}]$	Exp	Ref
$D^0 \rightarrow K_S \pi^+ \pi^- \pi^0$	$-0.3 \pm 1.4^{+0.2}_{-0.8}$	Belle	arXiv:1703.05721
$D^0 \rightarrow K^+ K^- \pi^+ \pi^-$	$1.8 \pm 2.9 \pm 0.4$	LHCb	JHEP10 (2014) 005
$D^+ \rightarrow K_S K^+ \pi^+ \pi^-$	$-12 \pm 10 \pm 5$	Babar	PRD84 031103(2011)

Triple product:  
 $C_T \equiv \vec{p}_1 \cdot (\vec{p}_2 \times \vec{p}_3)$

# Decays with photon(s)

- Theory problem: LongDistance  $\sim 10^3 \times$  ShortDistance
- NP probes:  $A_{CP}$ ,  $\gamma$  polarisation (t-dep. analysis or polarised  $\Lambda_c \rightarrow p\gamma$ )
- Experimental problem:  $\pi^0$  background



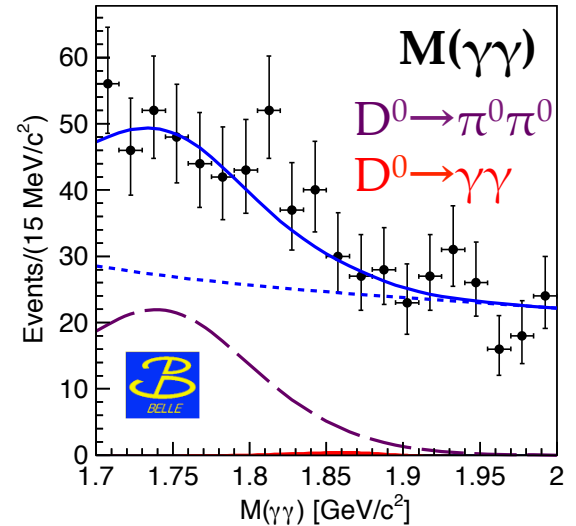
$$A_{CP}(D^0 \rightarrow \bar{K}^{*0} \gamma) = (-0.3 \pm 2.0 \pm 0.0)\%$$

$$A_{CP}(D^0 \rightarrow \phi \gamma) = (-9.4 \pm 6.6 \pm 0.1)\%$$

$$A_{CP}(D^0 \rightarrow \rho^0 \gamma) = (+5.6 \pm 15.1 \pm 0.6)\%$$

**No CPV**

$$BF(D^0 \rightarrow q\gamma) = (1.8 \pm 0.3 \pm 0.1) \times 10^{-5}$$

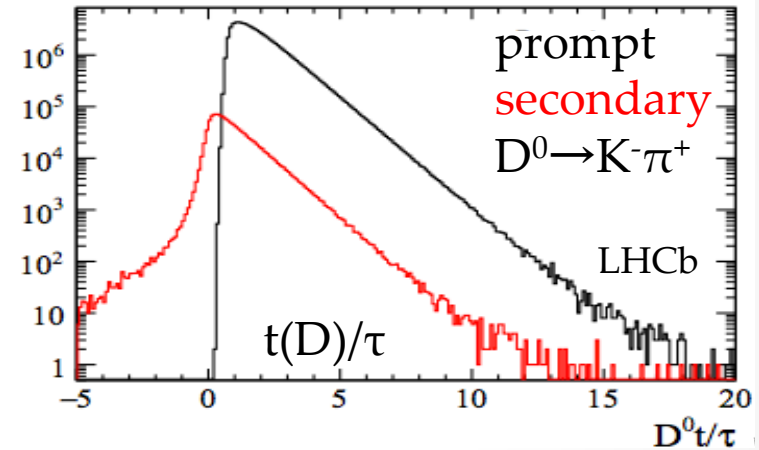
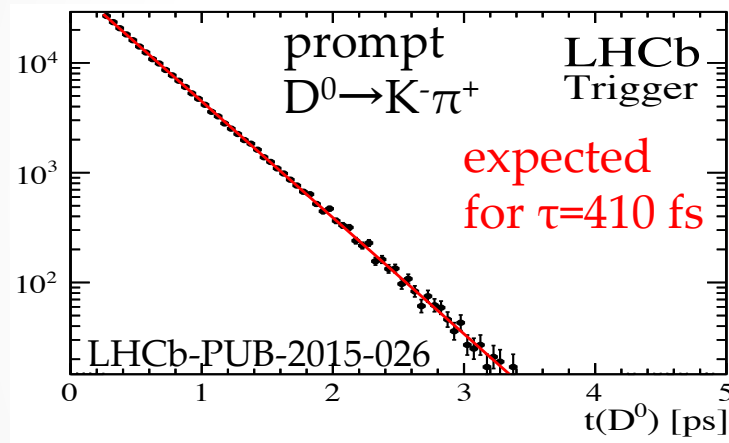


$$BF(D^0 \rightarrow \gamma\gamma) < 8.5 \times 10^{-7}$$

- LHCb competitive in  $D^0 \rightarrow q\gamma, \phi\gamma, K^*\gamma$
- Belle2 dominated:  $D^0 \rightarrow \gamma\gamma, D^+ \rightarrow q^+\gamma, \Lambda_c \rightarrow p\gamma$
- Belle2 wrt Belle: merged  $\pi^0, \gamma \rightarrow e^+e^-$  conversion
- LHCb upgrade: improved ECAL(?)

# Experimental aspects & prospects

- **t-acceptance:** LHCb triggers distort prompt charm
- Prompt + sec charm  $\Rightarrow$  full coverage of decay time
- Lifetime-unbiased triggers in Run-2

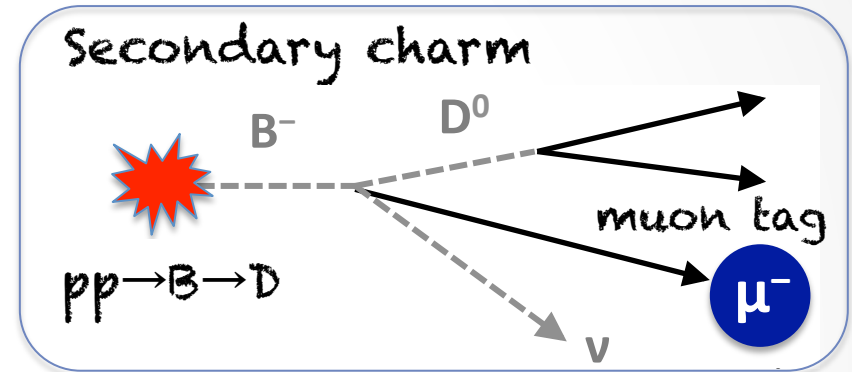
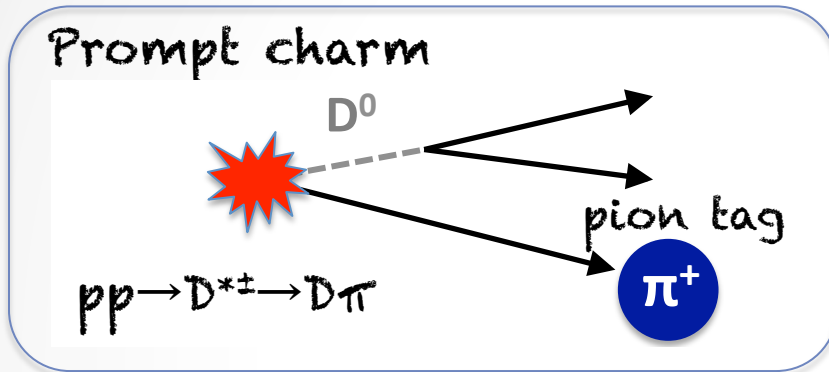


- **t-resolution**
- good at LHCb:  $\sim 50$ fs
- improved at Belle2 wrt Belle:  $\sim 250$ fs  $\rightarrow$   $\sim 150$ fs

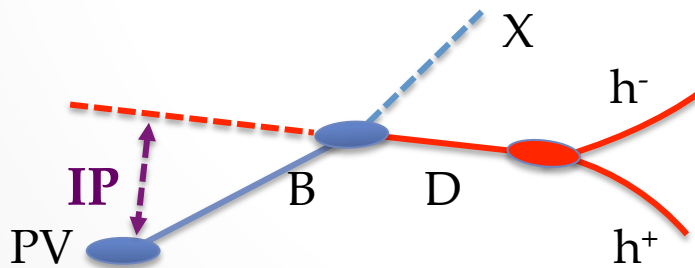


# Experimental aspects & prospects

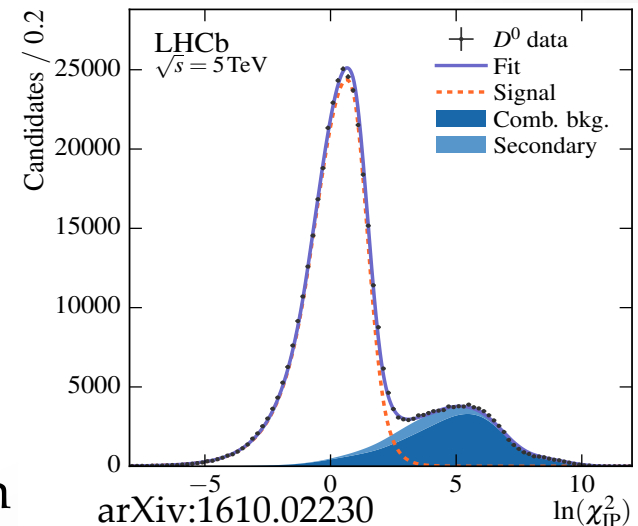
- flavour tagging at  $t=0$ . Defines charm samples



- LHCb uses both; Belle prompt
- prompt/sec separation, nontrivial at LHCb



- Lifetime biasing; may need better approach



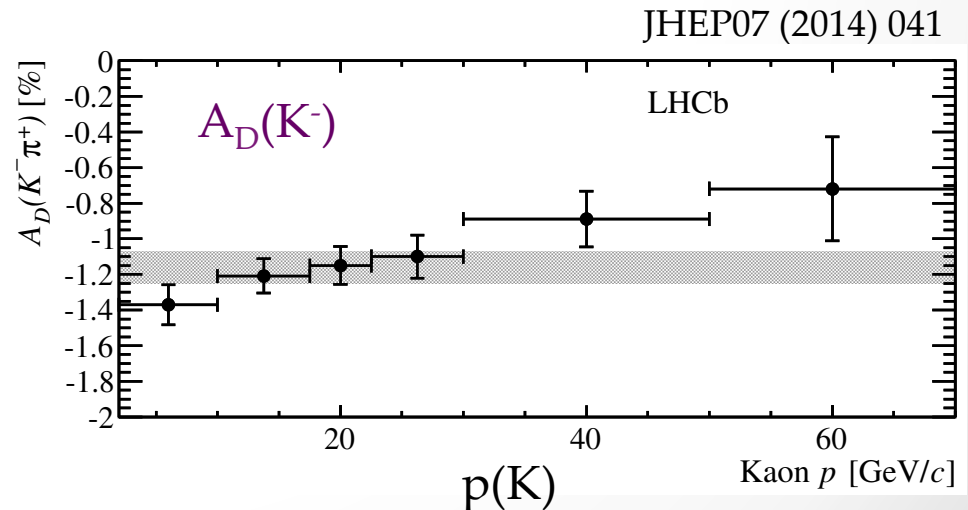
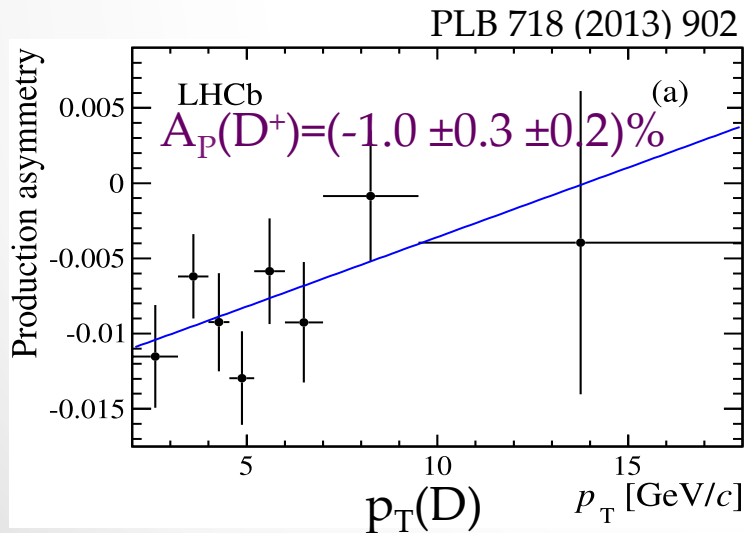
# 'Extra' asymmetries to account for

## Production asymmetry

- $e^+e^- \rightarrow \gamma/Z^*$  interference  $\Rightarrow$  FB asymmetry;  
easy to disentangle from CPV
- pp:  $\sigma(\Lambda_c^+) > \sigma(\Lambda_c^-) \Rightarrow \sigma(D^+) < \sigma(D^-)$  to compensate (Asym  $\sim 1\%$ )

## Detection asymmetries ( $K^+$ vs $K^-$ , $\pi^+$ vs $\pi^-$ )

- different interactions with detector material:  $\sigma(pK^-) > \sigma(pK^+)$
- depend on particle momentum

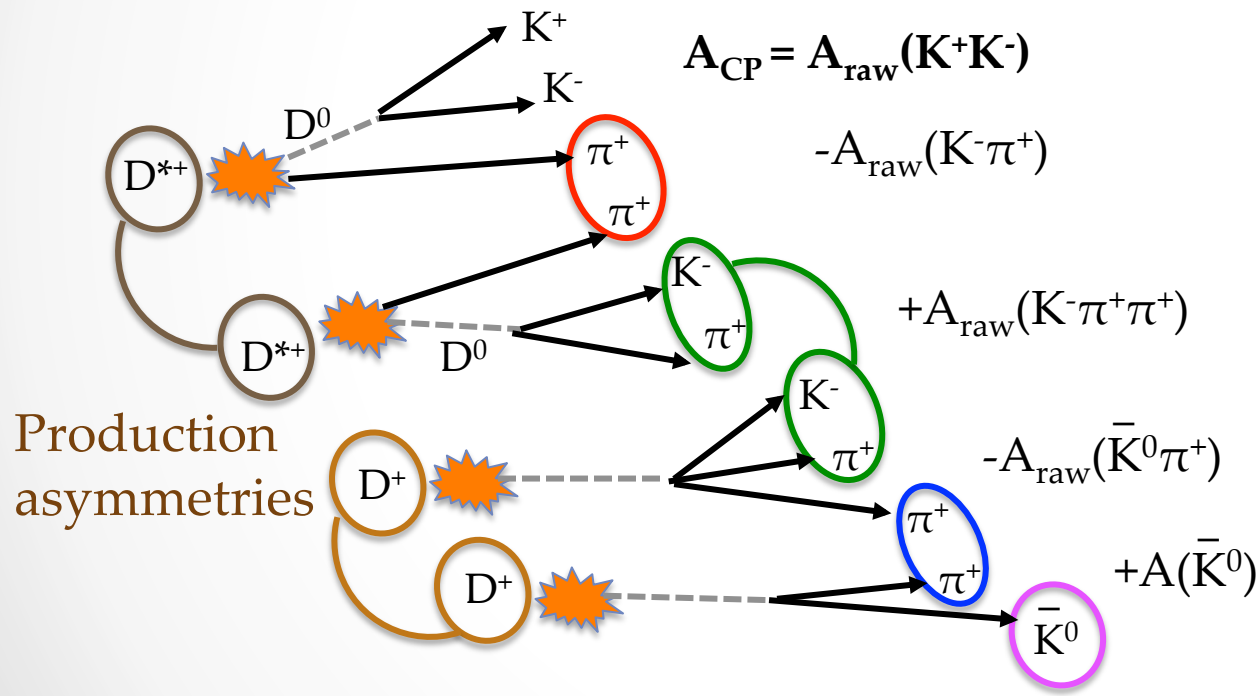


# From raw asymmetry to CP asymmetry

## Correct with CF control modes

- Overconstrain system with additional channels
- $A_{CP}(D^0 \rightarrow K^+K^-)$  case

$$A_{raw} = \frac{N(D) - N(\bar{D})}{N(D) + N(\bar{D})}$$



Multi-dim reweighting to match kinematics of signal & control modes

Calculated from known  $K^0/\bar{K}^0$  interactions with detector + K-mixing/CPV

- Assume no CPV in CF or include related uncertainty?

# $D^0$ - $\bar{D}^0$ mixing & Indirect CPV: basics

- Flavour eigenstates  $D^0$  [ $cu$ ]  $\bar{D}^0$  [ $\bar{c}\bar{u}$ ]  $\Leftrightarrow$  mass eigenstates  $D_1$   $D_2$  [ $m_{1,2}$   $\Gamma_{1,2}$ ]

$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle \quad |p|^2 + |q|^2 = 1$$

- Mixing frequencies  $x, y$

$$x = \frac{m_2 - m_1}{\Gamma} \quad y = \frac{\Gamma_2 - \Gamma_1}{2\Gamma} \quad \Gamma = \frac{\Gamma_1 + \Gamma_2}{2}$$

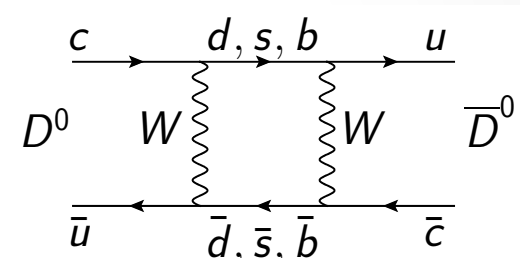
- CPV related to mixing (Indirect CPV)

$$|q/p| \neq 1 \quad \phi = \arg(q/p) \neq 0$$

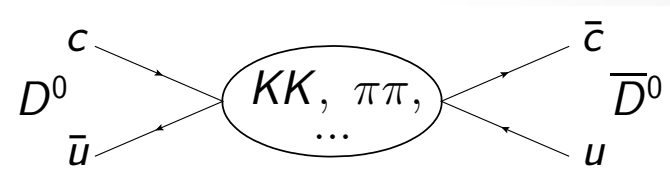
- SM:

$x, y \sim \mathcal{O}(10^{-2})$  with large uncertainty

Indirect CPV universal,  $\sim 10^{-4}$



$x \sim 10^{-5}$

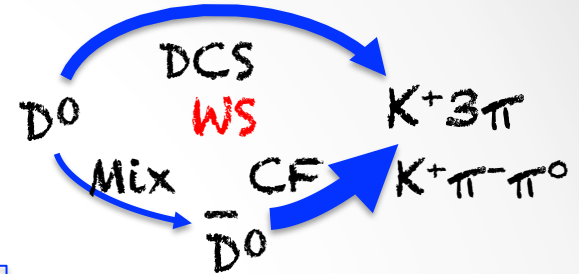


$x, y \sim 1\%$

difficult to calculate

# Wrong Sign Decays: $D^0 \rightarrow K3\pi$

- Rates integrated over Phase Space
- ⇒ averaged strong phase & coherence factor
- ⇒ dilution of sensitivity



$$R(t) = \frac{N_{WS}}{N_{RS}}(t) \simeq R_D^{K3\pi} + \sqrt{R_D^{K3\pi} R_{coh}} y'' \frac{t}{\tau} + \frac{x''^2 + y''^2}{4} \left(\frac{t}{\tau}\right)^2$$

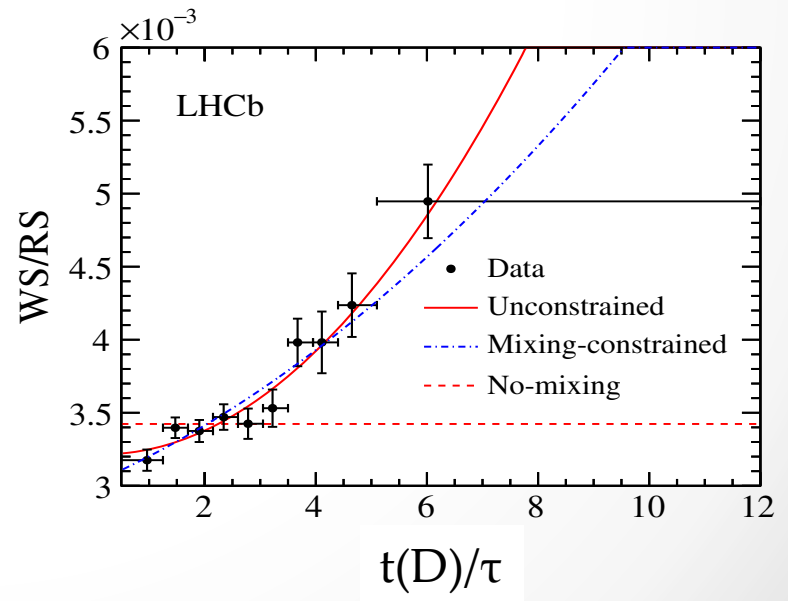
- $R_{coh} \sim 0$  phase variation;  $R_{coh} \sim 1$  resonances in phase

$$\int A_{K-3\pi}(\mathbf{r}) A_{K+3\pi}(\mathbf{r}) d\mathbf{r} \Rightarrow R_{coh} e^{-i\delta_{K3\pi}}$$

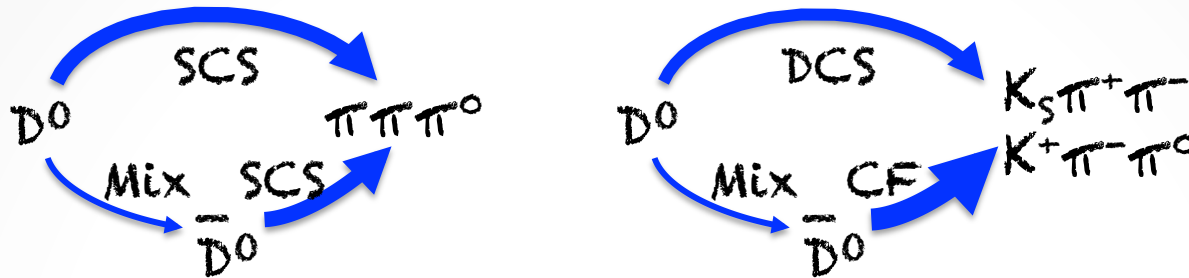
$$R_{coh} y'' = (0.3 \pm 1.8) \times 10^{-3}$$

$$(x''^2 + y''^2)/4 = (4.8 \pm 1.8) \times 10^{-5}$$

- Measurement w/o PS integration expected to have large sensitivity



# Multibody decays: time evolution of Dalitz



- ✓ Direct access to  $x, y, q/p$
- ✗ Need model to describe resonances
- ✓ Access to amplitudes & phases  $\Rightarrow$  no external input
- ✓ No dilution from coherence factor

$$\begin{aligned}
 \mathcal{P}[D^0(\text{Dalitz}; t)] \propto e^{-\Gamma t} \{ & |A_f|^2 [\cosh(y\Gamma t) + \cos(x\Gamma t)] \quad \leftarrow \text{decay } D^0 \rightarrow f \\
 & + \left| \frac{q}{p} \bar{A}_f \right|^2 [\cosh(y\Gamma t) - \cos(x\Gamma t)] \quad \leftarrow \text{mixing } D^0 \rightarrow \bar{D}^0 \rightarrow f \\
 & - 2\Re\left(\frac{q}{p} A_f^* \bar{A}_f\right) \sinh(y\Gamma t) - 2\Im\left(\frac{q}{p} A_f^* \bar{A}_f\right) \sin(x\Gamma t) \} \quad \leftarrow \text{interference of both}
 \end{aligned}$$

- Sensitivity depends on resonance interference

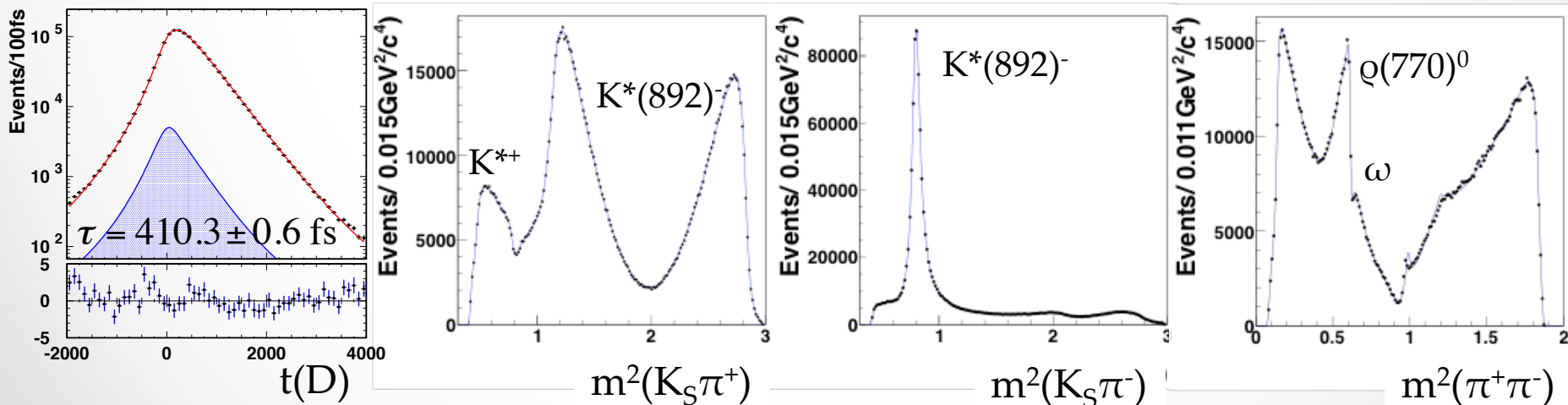
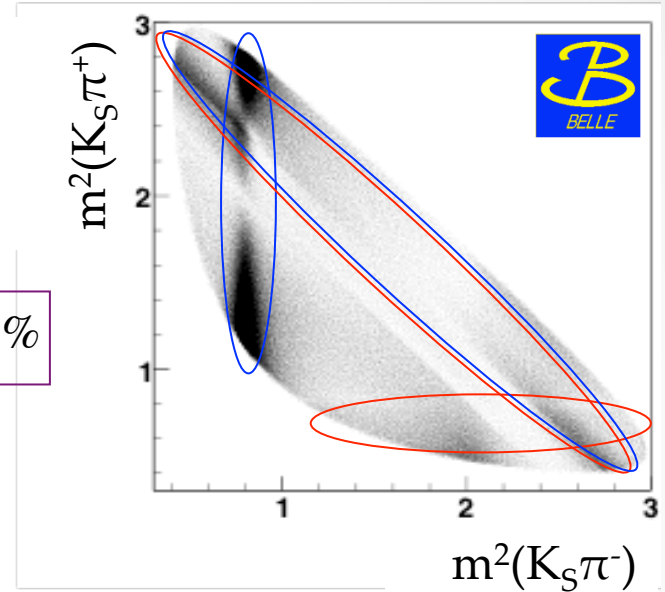
# Dalitz(t) of $D^0 \rightarrow K_S \pi^+ \pi^-$ golden mode

- Large statistics and rich dynamics
- Significant  $D^0 \rightarrow f$  &  $D^0 \rightarrow \bar{f}$  interferences
- Most precise  $x$  so far

$$x = \left( 0.56 \pm 0.19 \begin{matrix} +0.04 & +0.06 \\ -0.08 & -0.08 \end{matrix} \right) \% \quad y = \left( 0.30 \pm 0.15 \begin{matrix} +0.04 & +0.03 \\ -0.05 & -0.07 \end{matrix} \right) \%$$

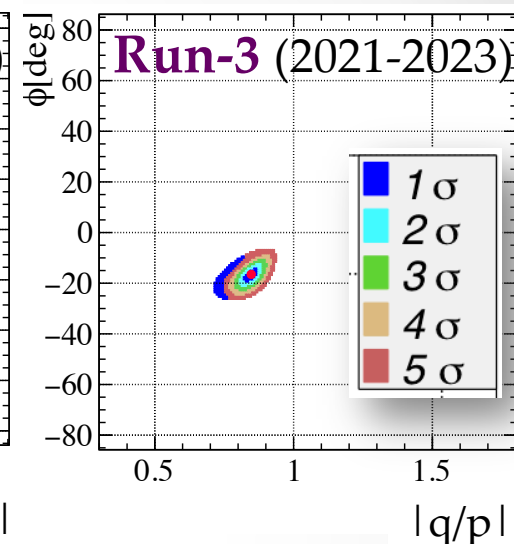
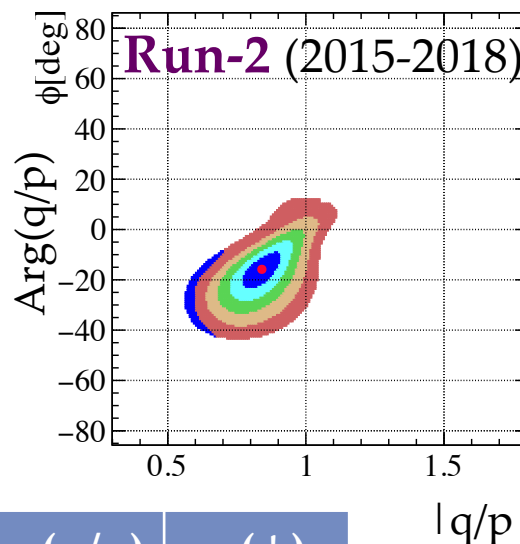
$$|q/p| = 0.90 \begin{matrix} +0.16 & +0.05 & +0.06 \\ -0.15 & -0.04 & -0.05 \end{matrix} \quad \phi = \left( -6 \pm 11 \pm 3 \begin{matrix} +3 \\ -4 \end{matrix} \right)^\circ$$

- Belle: 1.2M signal events
- LHCb: 2M in Run1. Significant  $x$  with Run1+2?

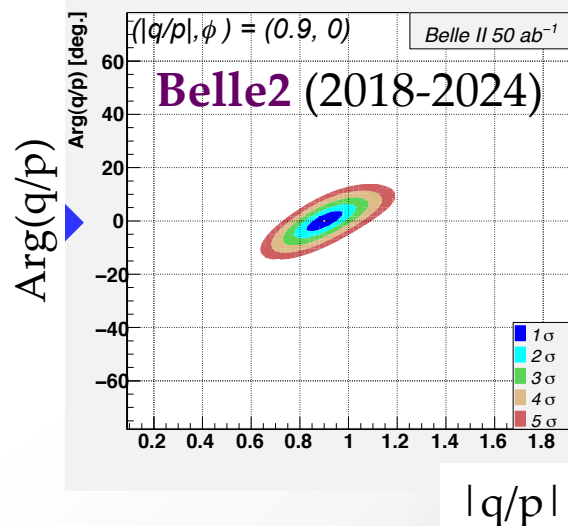


# Future of mixing & ICPV

- Dominated by LHCb
- Significant x with Run1+2?



	$\sigma(x)$ [ $10^{-3}$ ]	$\sigma(y)$ [ $10^{-3}$ ]	$\sigma(q/p)$ [ $10^{-3}$ ]	$\sigma(\phi)$ [mrad]
HFAG 2016	1.4	0.7	80	173
Run-1 (2011 - 2012)	1.1	0.8	65	119
Run-2 (2015 - 2018)	0.8	0.6	47	83
Run-3 (2021 - 2023)	0.3	0.2	17	32



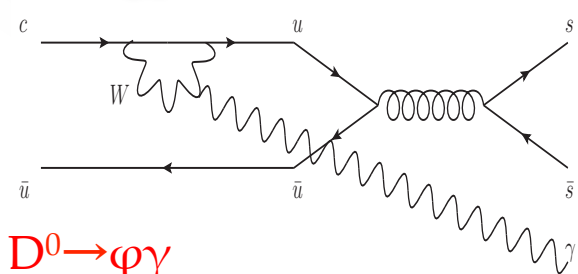
- LHCb:  $\sqrt{N}$  scaling of stat & syst
- Belle: includes irreducible syst



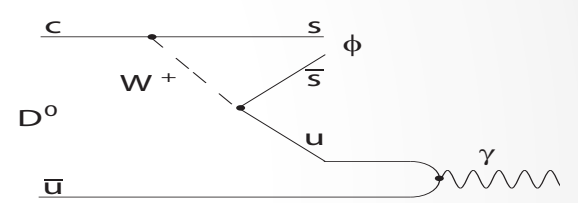


# $D^0 \rightarrow K^{*0} \gamma, \phi \gamma, \rho^0 \gamma$ : BF & $A_{CP}$

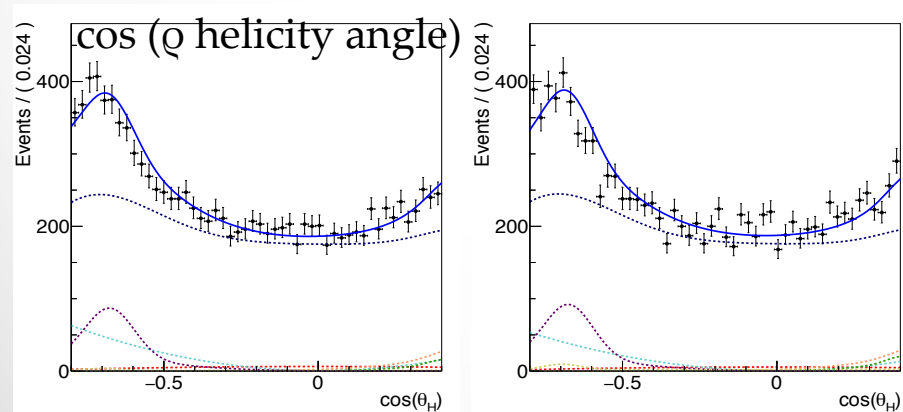
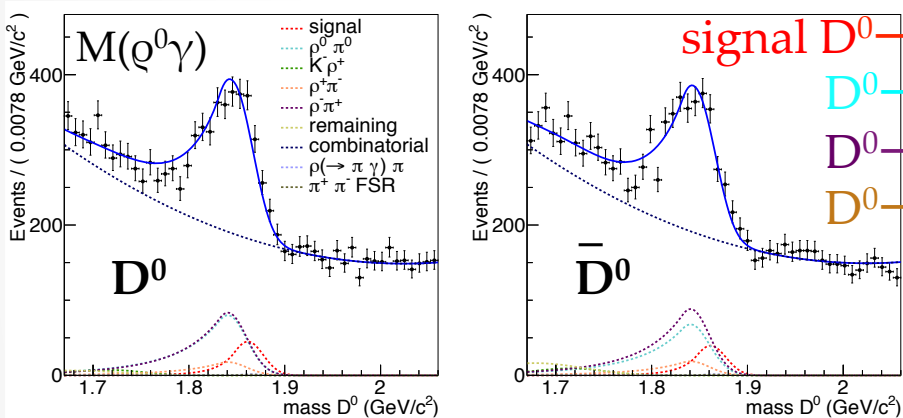
- BF's poorly measured. No CPV analysis before
- Large CPV within SM, up to a few %
- First observation of  $D^0 \rightarrow \rho(770) \gamma$



$D^0 \rightarrow \phi \gamma$   
Short distance contribution



Long distance via Vector Meson Dominance



$$\mathcal{B}(D^0 \rightarrow \bar{K}^{*0} \gamma) = (4.66 \pm 0.21 \pm 0.18) \times 10^{-4}$$

$$\mathcal{B}(D^0 \rightarrow \phi \gamma) = (2.76 \pm 0.20 \pm 0.08) \times 10^{-5}$$

$$\mathcal{B}(D^0 \rightarrow \rho^0 \gamma) = (1.77 \pm 0.30 \pm 0.08) \times 10^{-5}$$

$$A_{CP}(D^0 \rightarrow \bar{K}^{*0} \gamma) = (-0.3 \pm 2.0 \pm 0.0)\%$$

$$A_{CP}(D^0 \rightarrow \phi \gamma) = (-9.4 \pm 6.6 \pm 0.1)\%$$

$$A_{CP}(D^0 \rightarrow \rho^0 \gamma) = (+5.6 \pm 15.1 \pm 0.6)\%$$

No CPV

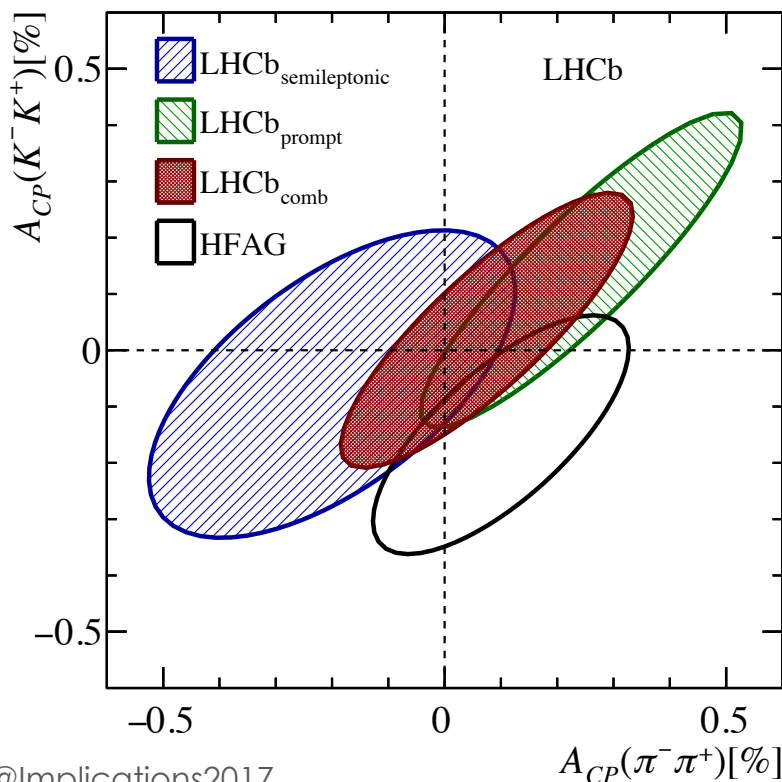
$$A_{CP}(D^0 \rightarrow K^+ K^-) \text{ \& } A_{CP}(D^0 \rightarrow \pi^+ \pi^-)$$

- Individual  $A_{CP}(KK)$ , pion-tagged sample

$$A_{CP}(K^+ K^-) = (0.14 \pm 0.15 \pm 0.10)\%$$

- Combine with  $\Delta A_{CP} \Leftrightarrow$

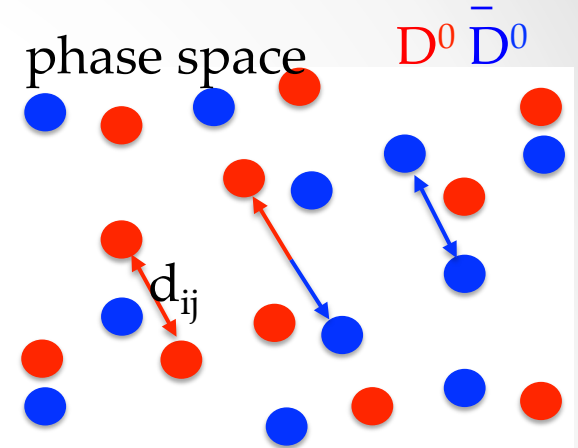
$$A_{CP}(\pi^+ \pi^-) = A_{CP}(K^+ K^-) - \Delta A_{CP} = (0.24 \pm 0.15 \pm 0.11)\%$$



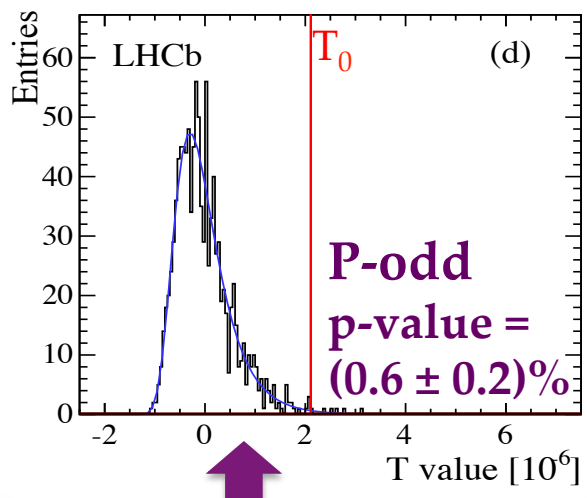
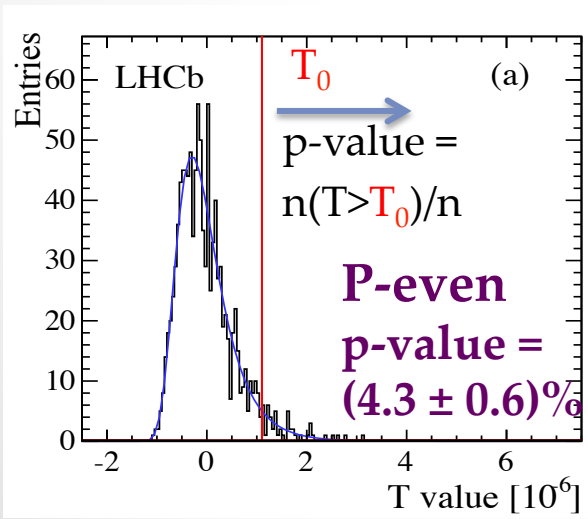
- Combine with results from **muon-tagged sample**  
JHEP07, 041 (2014)  
 $\Leftrightarrow$  **LHCb combination**
- Both  $A_{CP}$ 's consistent with zero

# Search for CPV in $D^0 \rightarrow 4\pi$ with Energy Test

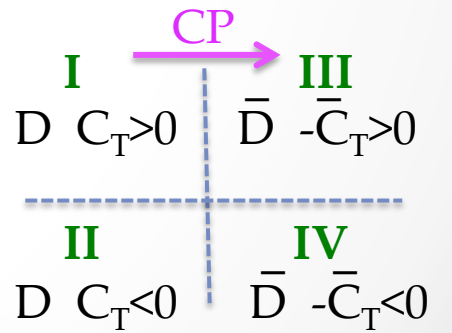
- Statistical comparison of two distributions
- Test statistics: based on distances of event pairs
- Compare with T distribution for no CPV case (randomize D flavour)
- 5-dim phase space:  $m^2(\pi\pi), m^2(\pi\pi\pi) \Rightarrow$  **P-even**
- Use triple-product sign to access **P-odd** CPV



$$T = \langle d_{ij} \rangle_{DD} + \langle d_{ij} \rangle_{\bar{D}\bar{D}} - \langle d_{ij} \rangle_{D\bar{D}}$$



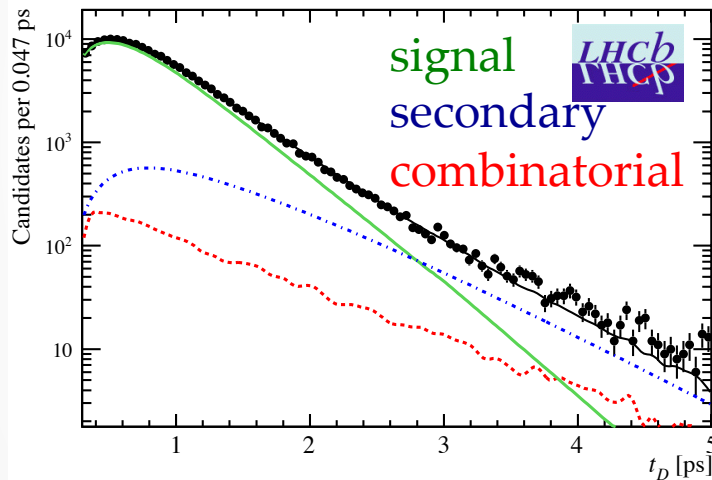
Marginally consistent with no CPV ( $\sim 2.7\sigma$ )



$$C_T \equiv \vec{p}\pi^+ \cdot (\vec{p}\pi^+ \times \vec{p}\pi^-)$$

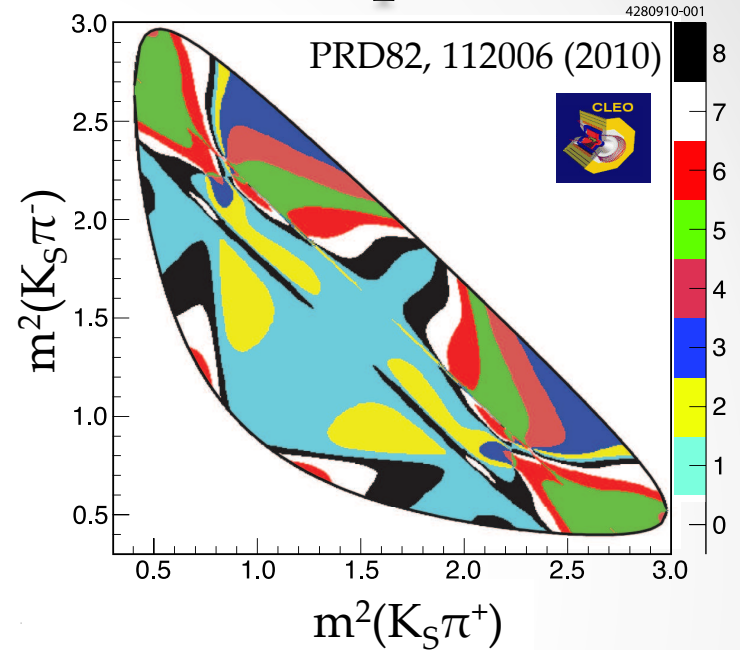
# $D^0 \rightarrow K_S \pi \pi$ , t-dep. Dalitz, model independent

- $D^0 \rightarrow K_S \pi \pi$  is a golden mode for mixing
- Binned approach to Dalitz
- Strong phases & fractions from Cleo-c
- Fit  $t(D)$  with data driven acceptance



$$\begin{aligned}
 x &= (-0.86 \pm 0.53 \pm 0.17)\% \\
 y &= (+0.03 \pm 0.46 \pm 0.13)\% \\
 \tau_D &= (410.9 \pm 1.1) \text{ fs}
 \end{aligned}$$

- This is with 2011 data: 180K signal  
 $K_S$  decayed inside vertex detector
- Ongoing for 2012 data: ~2M prompt+sec  
Also  $K_S$  decayed outside vertex detector



Belle: 1.2M signal

$$\begin{aligned}
 x &= (0.56 \pm 0.19^{+0.04 +0.06}_{-0.08 -0.08})\% \\
 y &= (0.30 \pm 0.15^{+0.04 +0.03}_{-0.05 -0.07})\%
 \end{aligned}$$

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