

# HL/HE Questions in Charm (Flavor Physics)

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# LHCb Upgrades

	LHC Run	Period	$\mathcal{L}_{\max}$ cm <sup>2</sup> s	$\int \mathcal{L} dt / \text{fb}$
Current	1&2	2010-2012, 2015-2018	$4 \times 10^{32}$	8
Phase-I	1&2	2021-2023, 2026-2029	$4 \times 10^{32}$	50
Phase-II	1&2	2031-2033, 2035-	$4 \times 10^{32}$	300

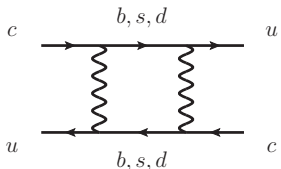
[LHCb report CERN-LHCC-2017-003]

- This corresponds to (hundreds of) billions of charmed hadrons

[LHCb-CONF-2016-005]

# D-Meson Physics – Introduction

- SM FCNC flavor dynamics determined by interplay between loop functions and CKM matrix elements



The diagram shows a charm quark loop. The top horizontal line is labeled 'c' at the left end and 'u' at the right end, with an arrow pointing right. The bottom horizontal line is labeled 'u' at the left end and 'c' at the right end, with an arrow pointing left. Two vertical wavy lines connect the top and bottom lines, each labeled 'b, s, d'.

$$= V_{cq} V_{uq}^* V_{cq'} V_{uq'}^* \times f\left(\frac{m_q^2}{M_W^2}, \frac{m_{q'}^2}{M_W^2}\right)$$

$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| & |V_{ts}| & |V_{tb}| \end{pmatrix} \approx \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}, \quad \lambda \approx 0.23$$

- “Two-generation dominance” and efficient GIM mechanism
  - SM contribution to FCNC effects in charm is small.
- Large long-distance contributions make SM predictions difficult.
- Search for new physics in the up-quark sector!

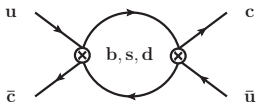
Why should we do  $D$  physics. . .

Why should we do  $D$  physics. . .

. . .if  $B$  and  $K$  physics is under better theoretical control?

I: Mixing is small

# $D^0 - \bar{D}^0$ mixing



$$i \frac{d}{dt} \begin{pmatrix} |D(t)\rangle \\ |\bar{D}(t)\rangle \end{pmatrix} = \left( M - i \frac{\Gamma}{2} \right) \begin{pmatrix} |D(t)\rangle \\ |\bar{D}(t)\rangle \end{pmatrix}$$

Diagonalize to get eigenstates

$$|D_{H,L}\rangle = p|D^0\rangle \mp q|\bar{D}^0\rangle$$

$$\Gamma_D \equiv \frac{\Gamma_H + \Gamma_L}{2}, \quad x \equiv \frac{M_H - M_L}{\Gamma_D}, \quad y \equiv \frac{\Gamma_H - \Gamma_L}{2\Gamma_D}.$$

# $D^0 - \bar{D}^0$ mixing – SM estimates

“Inclusive approach”:

- OPE expansion in powers of “ $\Lambda/m_c$ ”
- LO gives  $x \sim 10^{-5}$ ,  $y \sim 10^{-7}$
- Higher order  $x \sim y \lesssim 10^{-3}$   
[Georgi hep-ph/9209291, Ohl et al. hep-ph/9301212, 1993; Bigi et al. hep-ph/0005089]
- Cannot exclude  $y \sim 10^{-2}$  ( $V_{ub} \neq 0$ ) [Bobrowski et al. 1002.4794]

“Exclusive approach”:

- Sum over on-shell intermediate states
- Mainly  $D \rightarrow PP, PV$  leads to  $x \sim y \lesssim 10^{-3}$  [Cheng et al. 1005.1106]
- $SU(3)_F$  breaking in phase space  $y \sim 10^{-2}$  [Falk et al. hep-ph/0110317]
- Get  $x \sim 10^{-2}$  from a dispersion relation [Falk et al. hep-ph/0402204]

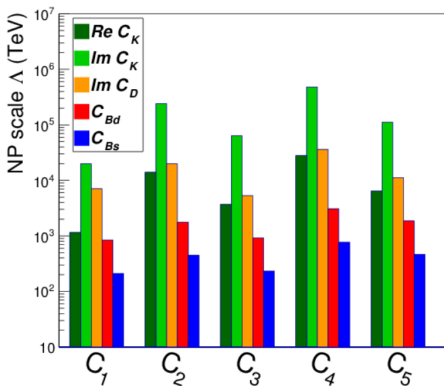
Large uncertainties; use experimental values to set upper bounds



# $D^0 - \bar{D}^0$ Mixing – NP

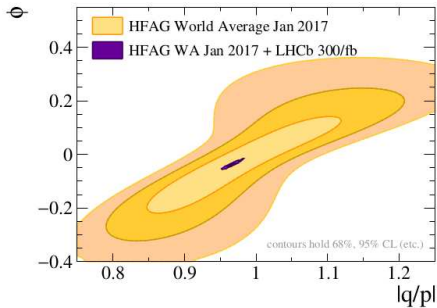
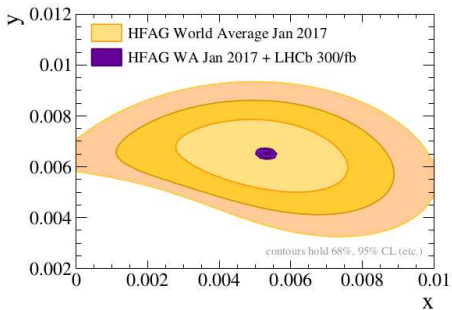
- Local NP contributions can be predicted very precisely
- Operator matrix elements from lattice QCD

[Carrasco et al. 1403.7302, Bazavov et al. 1706.04622]



[Silvestrini 1510.05797]

# $D^0 - \bar{D}^0$ Mixing



[LHCb report CERN-LHCC-2017-003]

## II: CP violation is small

# Three types of $CP$ violation

I  $|\bar{A}_{\bar{f}}/A_f| \neq 1$  ( $CP$  violation in decay)

$$a_f^d := \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})} = \frac{|A_f|^2 - |\bar{A}_{\bar{f}}|^2}{|A_f|^2 + |\bar{A}_{\bar{f}}|^2}$$

II  $|q/p| \neq 1$  ( $CP$  violation in mixing)

$$a_{sl} := \frac{\Gamma(\bar{D}^0(t) \rightarrow \ell^+ X) - \Gamma(D^0(t) \rightarrow \ell^- X)}{\Gamma(\bar{D}^0(t) \rightarrow \ell^+ X) + \Gamma(D^0(t) \rightarrow \ell^- X)} = \frac{|p/q|^2 - |q/p|^2}{|p/q|^2 + |q/p|^2}$$

III  $\text{Im}(\lambda_f) \equiv \text{Im}\left(\frac{q}{p} \frac{\bar{A}_f}{A_f}\right) \neq 0$  (interference-type  $CP$  violation)

$$a_{f_{CP}} := \frac{\Gamma(\bar{D}^0(t) \rightarrow f_{CP}) - \Gamma(D^0(t) \rightarrow f_{CP})}{\Gamma(\bar{D}^0(t) \rightarrow f_{CP}) + \Gamma(D^0(t) \rightarrow f_{CP})}$$

# Size of CPV in $D$ mixing

- Define  $\lambda_q \equiv V_{cq} V_{uq}^*$
- Eliminate  $\lambda_d$  via unitarity:  $\lambda_d + \lambda_s + \lambda_b = 0$
- $\lambda_s$  can be chosen real
- CPV naively suppressed by  $r = \text{Im}\lambda_b/\lambda_s \sim 6.5 \times 10^{-4}$

- The mixing amplitude is

$$\mathcal{A} = \lambda_s^2(f_{dd} + f_{ss} - 2f_{ds}) + 2\lambda_s\lambda_b(f_{dd} + f_{bs} - f_{bd} - f_{sd}) + \mathcal{O}(\lambda_b^2)$$

- In terms of  $U$ -spin contributions this is [Silvestrini 1510.05797]

$$\mathcal{A} = \lambda_s^2(\Delta U = 2) + 2\lambda_s\lambda_b(\Delta U = 1 + \Delta U = 2) + \mathcal{O}(\lambda_b^2) \sim \lambda_s^2\epsilon + 2\lambda_s\lambda_b\epsilon^2$$

- For nominal  $U$ -spin breaking,  $\epsilon \approx 30\%$ , expect CPV at order  $r/\epsilon \sim 10^{-3}$
- More detailed analysis

[Grossman et al., work in progress; see also talk by L. Silvestrini at this workshop]

# Size of CPV in $D$ decay

- Wilson coefficients can be computed **perturbatively**
- Hadronic matrix elements  $\langle K\pi | \mathcal{H}_{\text{eff}} | D \rangle$  dominated by **nonperturbative** QCD
- QCD factorization expected to work badly ( $\Lambda_{\text{QCD}}/m_c \lesssim 1$ )
- **Ultimately rely on lattice QCD**
  - Recent progress in  $K \rightarrow \pi\pi$  matrix element  
[E.g. Bai et al. 1505.07863]
  - Multiple-channel generalization of Lellouch-Lüscher formula  
[E.g. Polejaeva, Rusetsky 1203.1241; Hansen, Sharpe 1211.0511; Briceño, Davoudi 1212.3398]
- **Until then:**  $SU(3)$  flavor symmetry plus assumptions  
(Naive factorization, large- $N$ , “ $\epsilon^2$ ” sum rules, . . . )  
[E.g. Jung et al. 1410.8396, Müller et al. 1506.04121, Nierste et al. 1708.03572, Grossman et al. 1211.3361]
  - For instance,  $\Delta\mathcal{A}_{CP}$  has taught us that DCPV can be of order  $\gtrsim 10^{-3}$   
[E.g. Brod et al. 1111.5000, 1203.6659, Pirtskhalava et al. 1112.5451, Feldmann et al. 1202.3795]

# III: Null tests and rare decays

# Isospin sum rules

- Tree-level  $\mathcal{H}_{\text{eff}}$  for  $D \rightarrow \pi\pi$  has both  $\Delta I = 1/2$  and  $\Delta I = 3/2$ :

$$Q_T \sim (\bar{d}c)(\bar{u}d)$$

- QCD penguin operators are purely  $\Delta I = 1/2$ :

$$Q_P \sim (\bar{c}u) \otimes (\bar{u}u + \bar{d}d + \bar{s}s)$$

- $\Delta I = 3/2$  direct  $CP$ -violating transitions are absent in SM.

$$A_{\pi^+\pi^-} = \frac{1}{\sqrt{6}}\mathcal{A}_{3/2} + \frac{1}{\sqrt{3}}\mathcal{A}_{1/2},$$

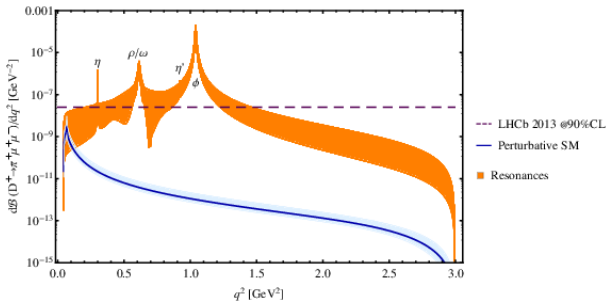
$$A_{\pi^0\pi^0} = \frac{1}{\sqrt{3}}\mathcal{A}_{3/2} - \frac{1}{\sqrt{6}}\mathcal{A}_{1/2},$$

$$A_{\pi^+\pi^0} = \frac{\sqrt{3}}{2}\mathcal{A}_{3/2}.$$

- $D^+ \rightarrow \pi^+\pi^0$  purely  $\Delta I = 3/2 \Rightarrow$  any  $CP$  asymmetry would be NP
- Can write down sum rules also for  $D \rightarrow \rho\pi$ ,  $D \rightarrow K^{(*)}\bar{K}^{(*)}\pi(\rho)$ ,  
 $D_s^+ \rightarrow K^*\pi(\rho)$  [Grossman et al. 1204.3557]



$$D^+ \rightarrow \pi^+ \mu^+ \mu^- \text{ and } D^0 \rightarrow P^+ P^- \mu^+ \mu^-$$



[Updated plot thanks to  
Stefan de Boer]

- Angular observables and CP asymmetries are (approximate) SM null tests [de Boer et al. 1510.00311]
  - Fit hadronic contributions
  - Asymmetries can be enhanced by resonances
- Also rare leptonic decays  $D \rightarrow \ell\ell$  [See, e.g., Fajfer 1509.01997]
  - Radiative decays  $D \rightarrow V\gamma$  relevant for Belle II

Why should we do  $D$  physics. . .

# Why should we do $D$ physics...

...if the up- and down sectors are related via weak isospin?

# I: Disentangle UV flavor structure

## $D$ mixing versus $K$ mixing

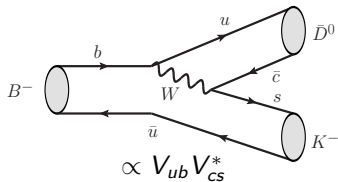
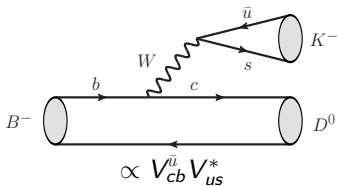
- Consider NP that couples to the LH quark doublets, e.g.,  $Q_{L,2} \sim (c_L, s_L)^T$
- SM plus NP:

$$\mathcal{L} \supset \overline{Q_{L,i}} Y_{ij}^d d_{R,j} H + \overline{Q_{L,i}} Y_{ij}^u u_{R,j} \tilde{H} + \frac{1}{\Lambda^2} (\overline{Q_{L,i}} X_{ij} Q_{L,j}) (\overline{Q_{L,i}} X_{ij} Q_{L,j})$$

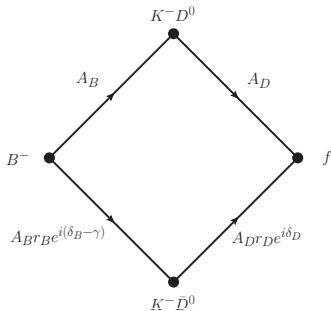
- Can always choose a basis where either  $Y^d$  or  $Y^u$  are diagonal
- Can always “adjust” NP to have vanishing contribution to *either*  $K$  mixing *or*  $D$  mixing, but not both
- Combining  $D$  and  $K$  mixing allows to test the UV flavor structure of NP  
[Blum et al. 0903.2118]

## II: Implications for $B$ physics

# $\gamma$ from tree decays – general idea



- $b \rightarrow c\bar{u}s, b \rightarrow u\bar{c}s$
- pure tree-level transition
- interference from common  $D^0, \bar{D}^0$  final states



# Including direct CP violation in $D$ decays

[Martone et al. 1212.0165, Zupan 1212.0165; see also Wang 1211.4539, Bhattacharya et al. 1301.5631, Bondar et al. 1303.6305]

- $B$  decay amplitude gets modified:

$$A(B^\pm \rightarrow f_D K^\pm) = A_B A_f^T [1 + r_B^\pm e^{i(\delta'_B \pm \gamma \pm \delta\gamma)}]$$

- What is the size of the effect?

$$\delta\gamma = \mathcal{O}(r_f/r_B), \quad \delta'_B - \delta_B = \mathcal{O}(r_f/r_B), \quad r_B^\pm - r_B = \mathcal{O}(r_f)$$

- $r_B(DK) = \mathcal{O}(10\%)$ ,  $\delta\gamma = \mathcal{O}(\text{few } \%)$
- $r_B(D\pi) = \mathcal{O}(0.5\%)$ ,  $\delta\gamma = \mathcal{O}(1)$

$$A_{CP}(B \rightarrow f_D K) = 2r_B \sin \delta_B \sin \gamma - a_f^{\text{dir}}$$



# Including direct CP violation

- Unknowns:  $2n_{SCS} + 3n_B + 1$
- Observables:  $2n_B(n_{CA} + n_{SCS})$
- Shift symmetry  $\gamma \rightarrow \gamma + \phi$ ,  $\alpha_f \rightarrow \alpha_f - \phi$ :

$$|A(B^\pm \rightarrow f_D K^\pm)|^2 = |A_B|^2 [ |A_f|^2 + 2r_B |A_f| |\bar{A}_f| \cos(\delta_B \pm \gamma \pm \alpha_f) + \dots ]$$

- $\alpha_f \equiv \arg(A_f/\bar{A}_f) = -a_f^{\text{dir}} \cot \delta_f$
- Cannot extract  $\gamma$  from  $B \rightarrow DK$  alone without assumptions
- Measure  $\delta_f$  at charm factories, or extract from  $D - \bar{D}$  mixing

Why should we do  $D$  physics. . .

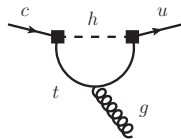
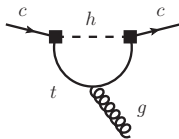
Why should we do  $D$  physics. . .

. . .if we can test the up-sector in top-quark decays?

# Disentangle UV flavor structure

# CP and flavor violating Higgs couplings

- Direct searches for  $h \rightarrow cu$  lead to  $\mathcal{O}(10\%)$  bounds
- Chromoelectric dipole leads to neutron EDM
- It also leads to CPV contribution in  $D$  decays and  $D - \bar{D}$  mixing



Observable	Coupling	Present bound	Future sensitivity
$d_n$	$ \text{Im}(Y_{tc} Y_{ct}) $	$5.0 \times 10^{-4}$	$1.7 \times 10^{-6}$
$d_n$	$ \text{Im}(Y_{tu} Y_{ut}) $	$4.3 \times 10^{-7}$	$1.5 \times 10^{-9}$
$\Delta\mathcal{A}_{CP}$	$ \text{Im}(Y_{ut}^* Y_{ct}) $	$4.0 \times 10^{-4}$	–
$D - \bar{D}$	$\sqrt{ \text{Im}(Y_{tc}^* Y_{ct} Y_{ut}^* Y_{tu}) }$	$4.1 \times 10^{-4}$	$1.3 \times 10^{-4}$

[Gorbahn et al. 1404.4873]

# Summary

- Charm physics is theoretically and experimentally challenging
- Some observables in principle very sensitive to NP
  - Test for NP in the up sector
  - Disentangle NP flavor structure
  - Future theory progress needed
  - Devise SM “null tests”
- Important input for  $B$  physics
- Charm flavor physics will play a prominent role also at future LHCb upgrades