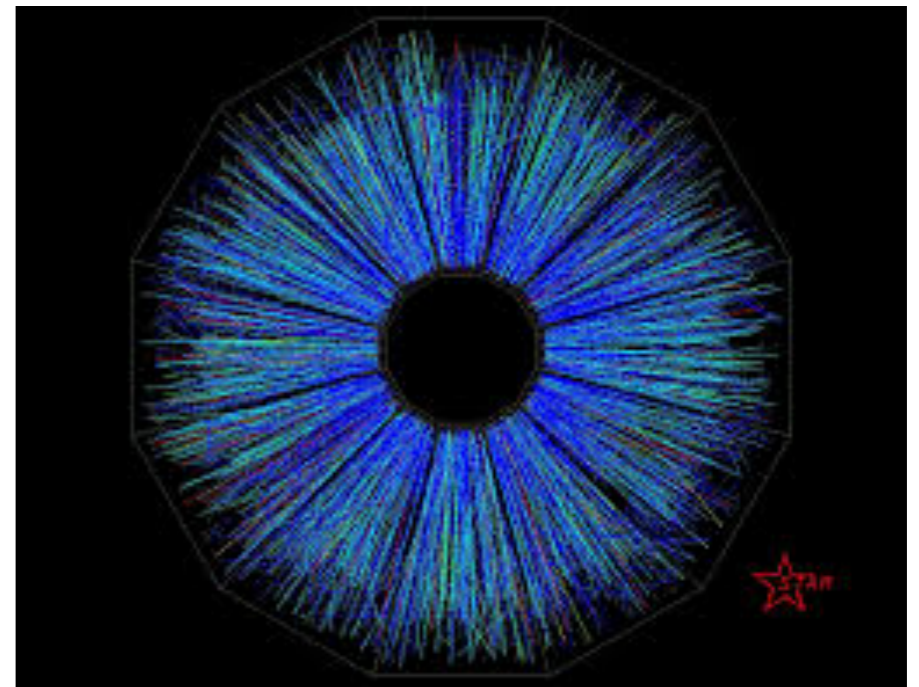
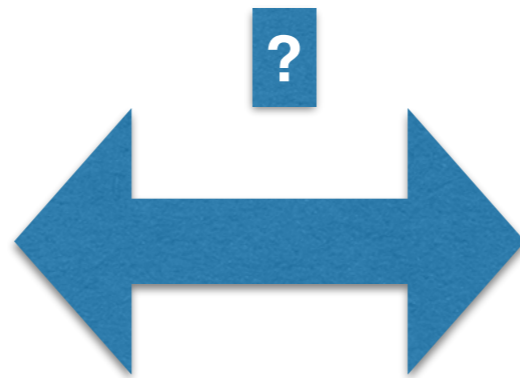


# Confinement, Instanton-dyons and Monopoles

Edward Shuryak  
Stony Brook University



topology, semiclassicals, instantons



Heavy ion collisions, QGP

Quark confinement and hadron spectrum,  
Aug.3, 2018, Maynooth, Ireland

# outline

Instanton-dyons  $\Leftrightarrow$  Monopoles  
Euclidean semiclassical theory  $\Leftrightarrow$  time-dependent dynamics

- **Confinement=Bose-Einstein condensation of monopoles. Kinetic coefficients -viscosity, jet quenching parameter, can be explained by “dual QGP” with monopoles. But, what are these monopoles in QCD?**
- **instanton-dyons  $\Rightarrow$  confinement, chiral symmetry breaking and nontrivial quark periodicity**
- **Relation between instanton-dyons and monopoles**
- **Chiral symmetry breaking with monopoles**



# Particle - monopoles and their dynamics: classics



- Dirac explained how magnetic charges may coexist with quantum mechanics (1934)
- 't Hooft and Polyakov discovered **monopoles** in Non-Abelian gauge theories (1974)
- 't Hooft and Mandelstam suggested “**dual superconductor mechanism for confinement (1976)**”
- Seiberg and Witten shown how it works, in the **N=2 Super - Yang-Mills theory (1994)**

# matter composition, by d.o.f.

**quarks**

## Role of QCD monopoles in jet quenching

Adith Ramamurti, Edward Shuryak (SUNY, Stony Brook). Aug 14, 2017. 16 pp.

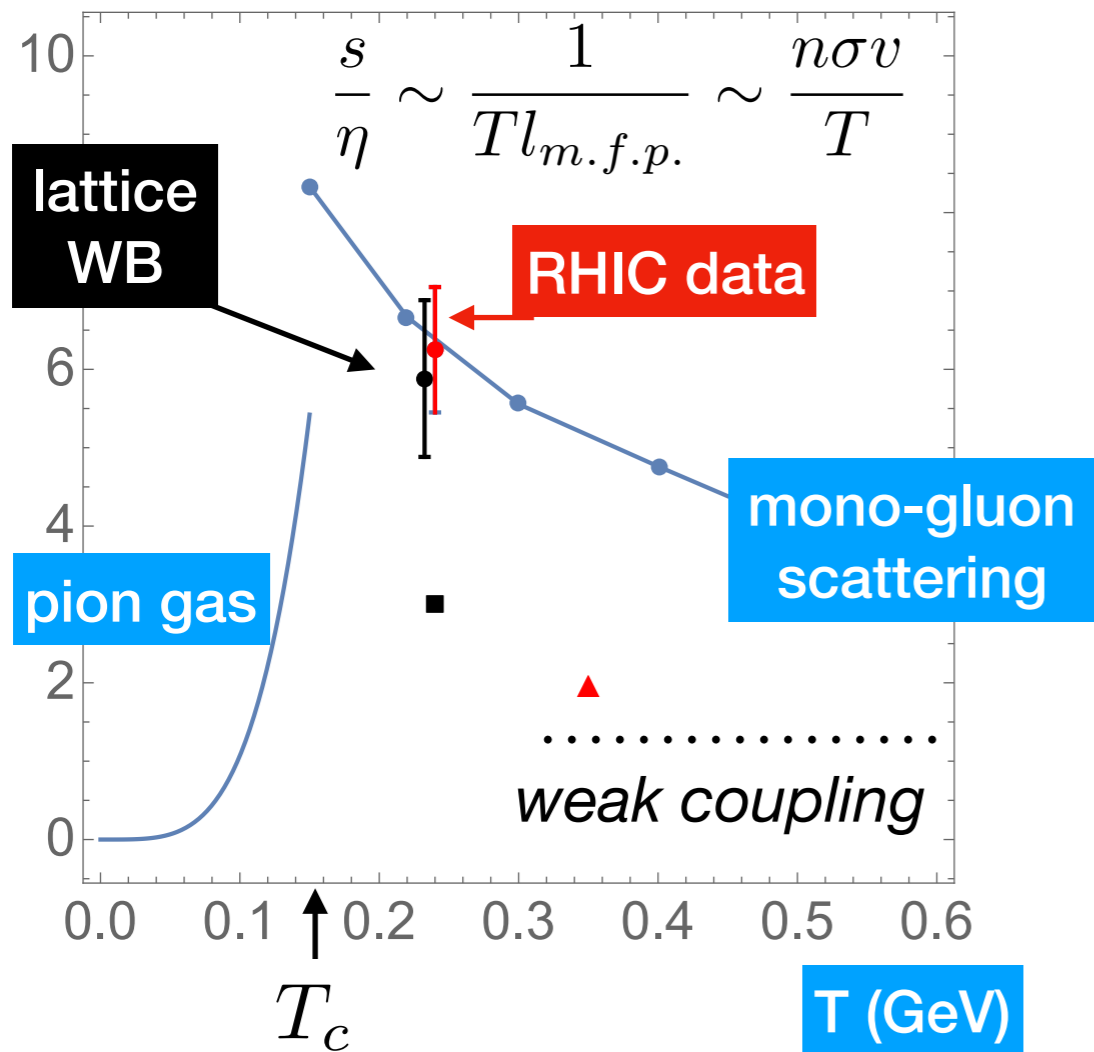
Published in *Phys.Rev. D97* (2018) no.1, 016010

monopoles

gluons

Strongly coupled quark-gluon plasma in heavy ion collisions

Edward Shuryak *Rev.Mod.Phys.* 89 (2017) 035001





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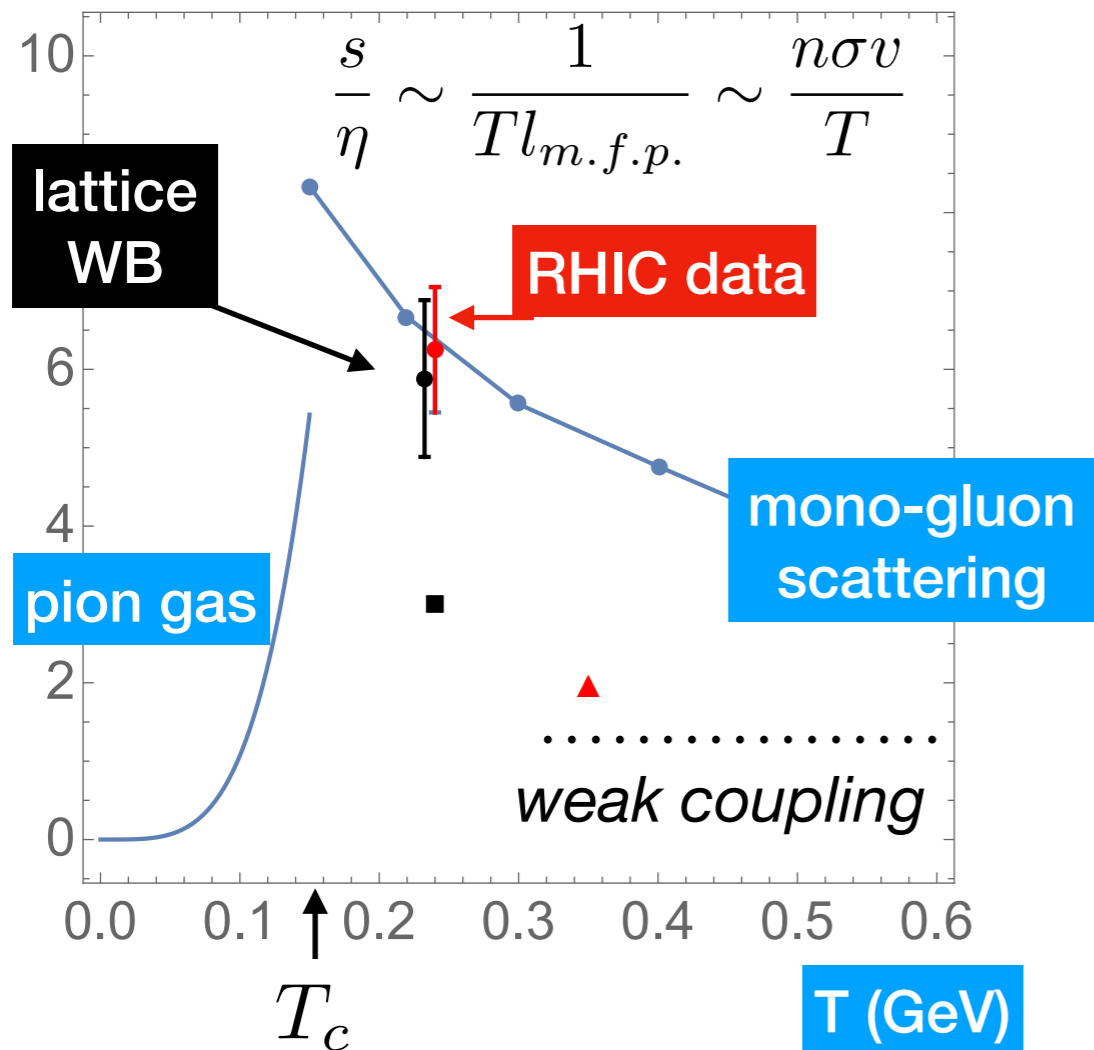
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Xu, J., J. Liao, and M. Gyulassy (2015),  
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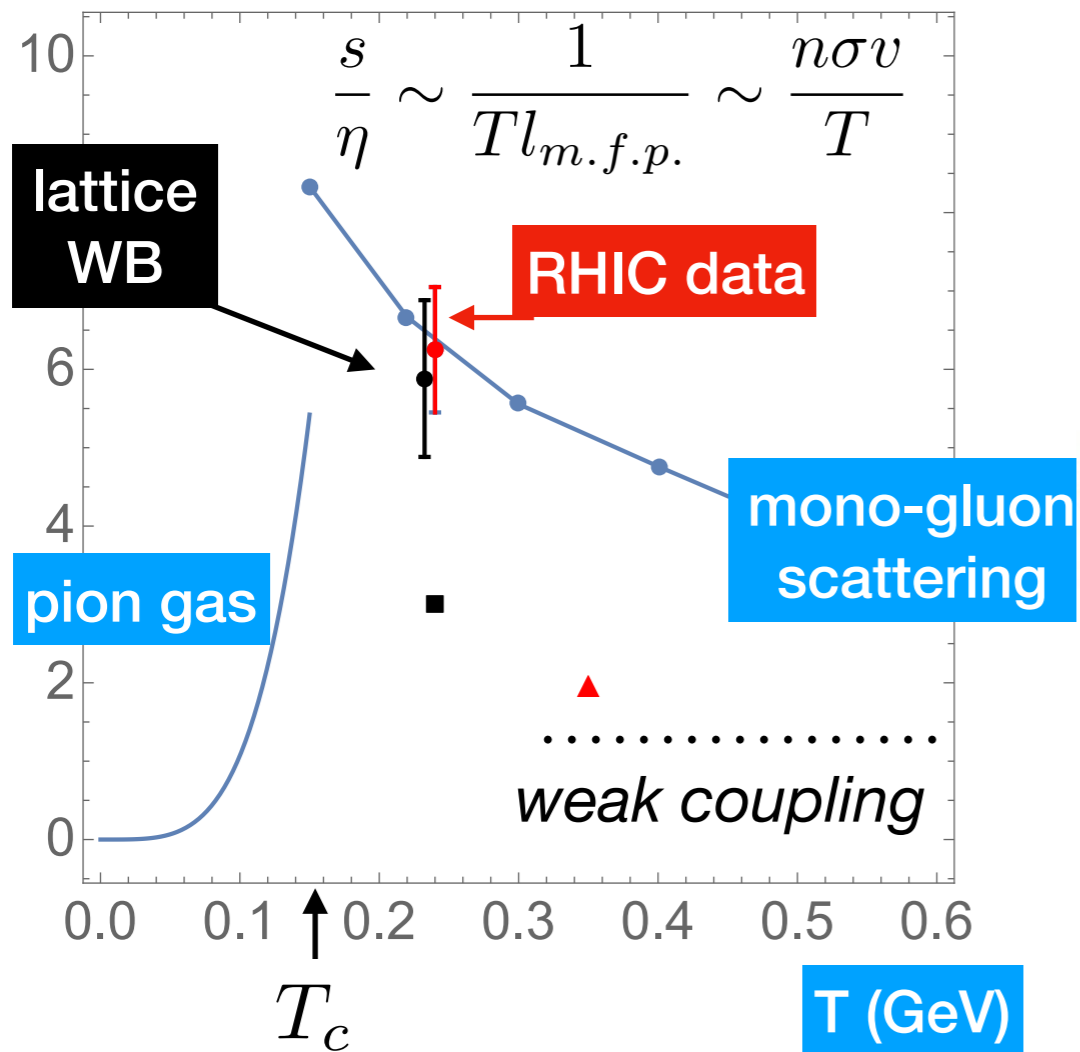
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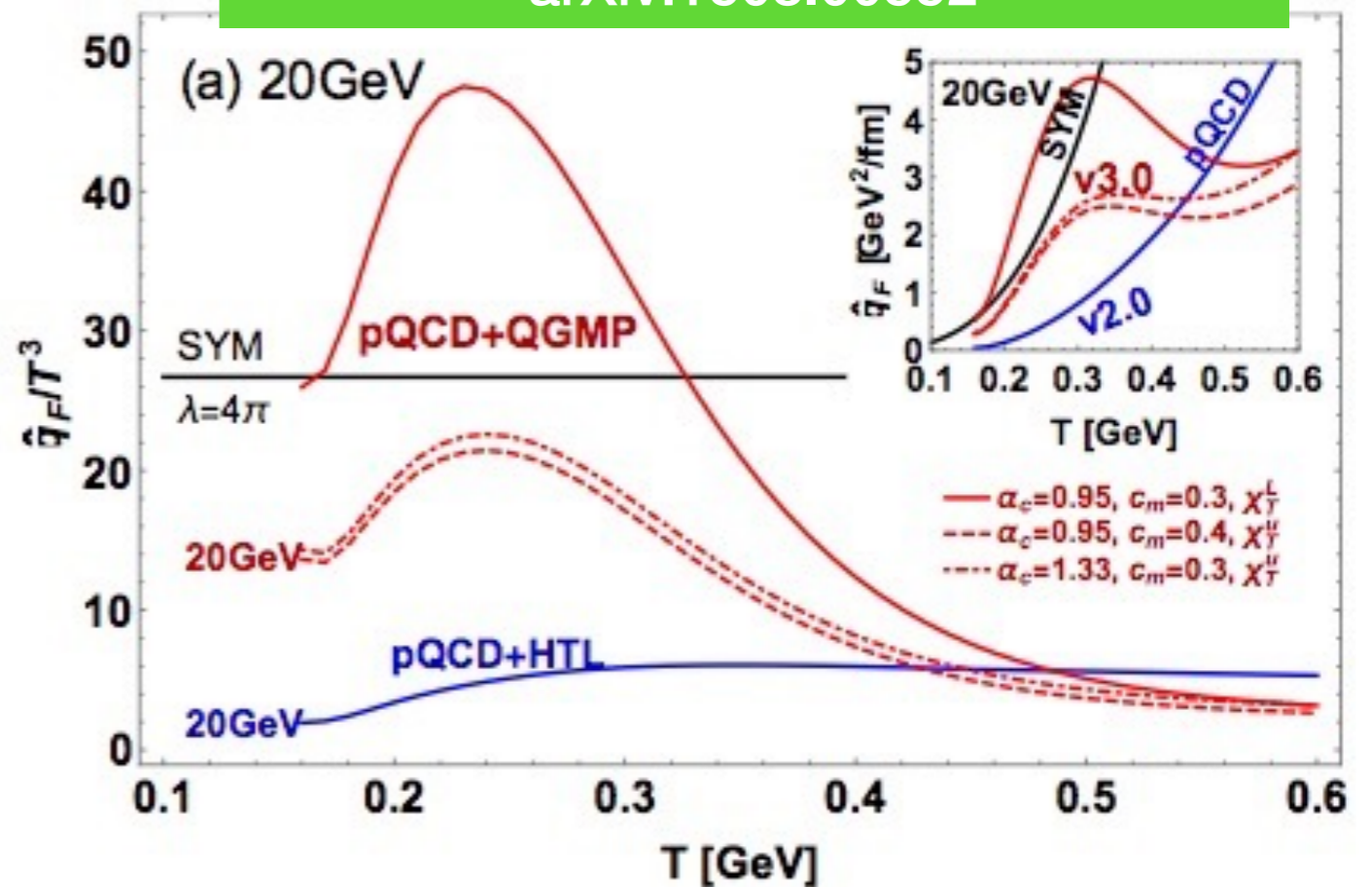
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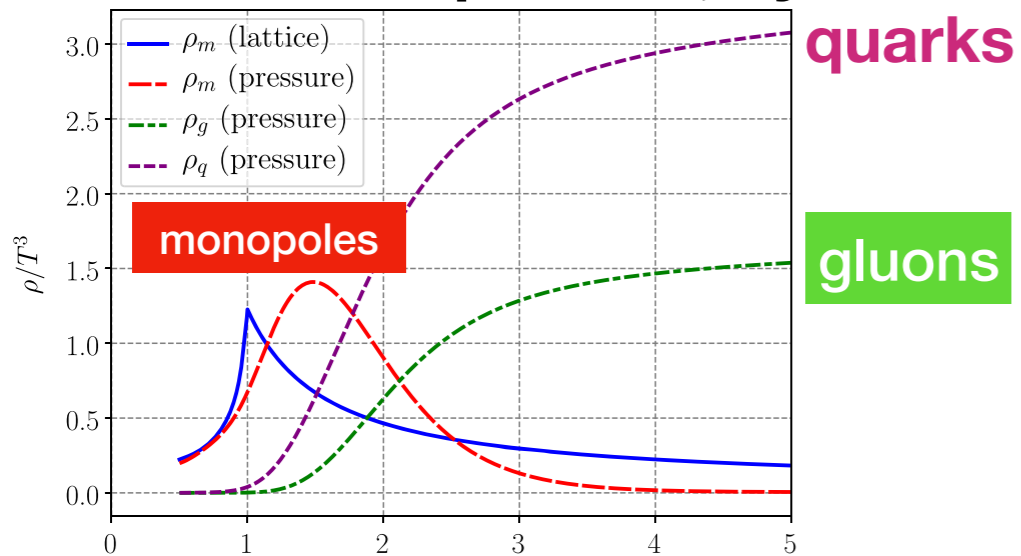
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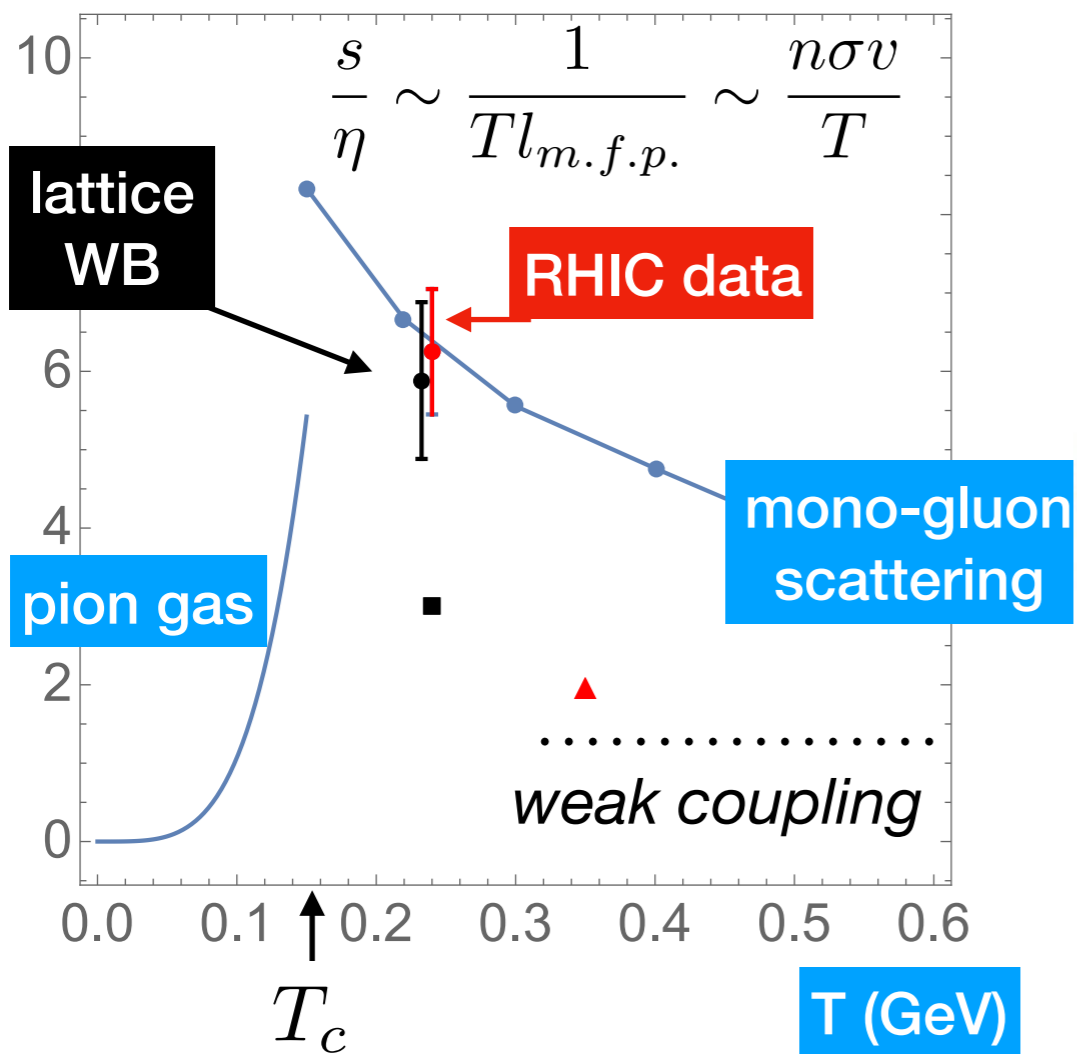


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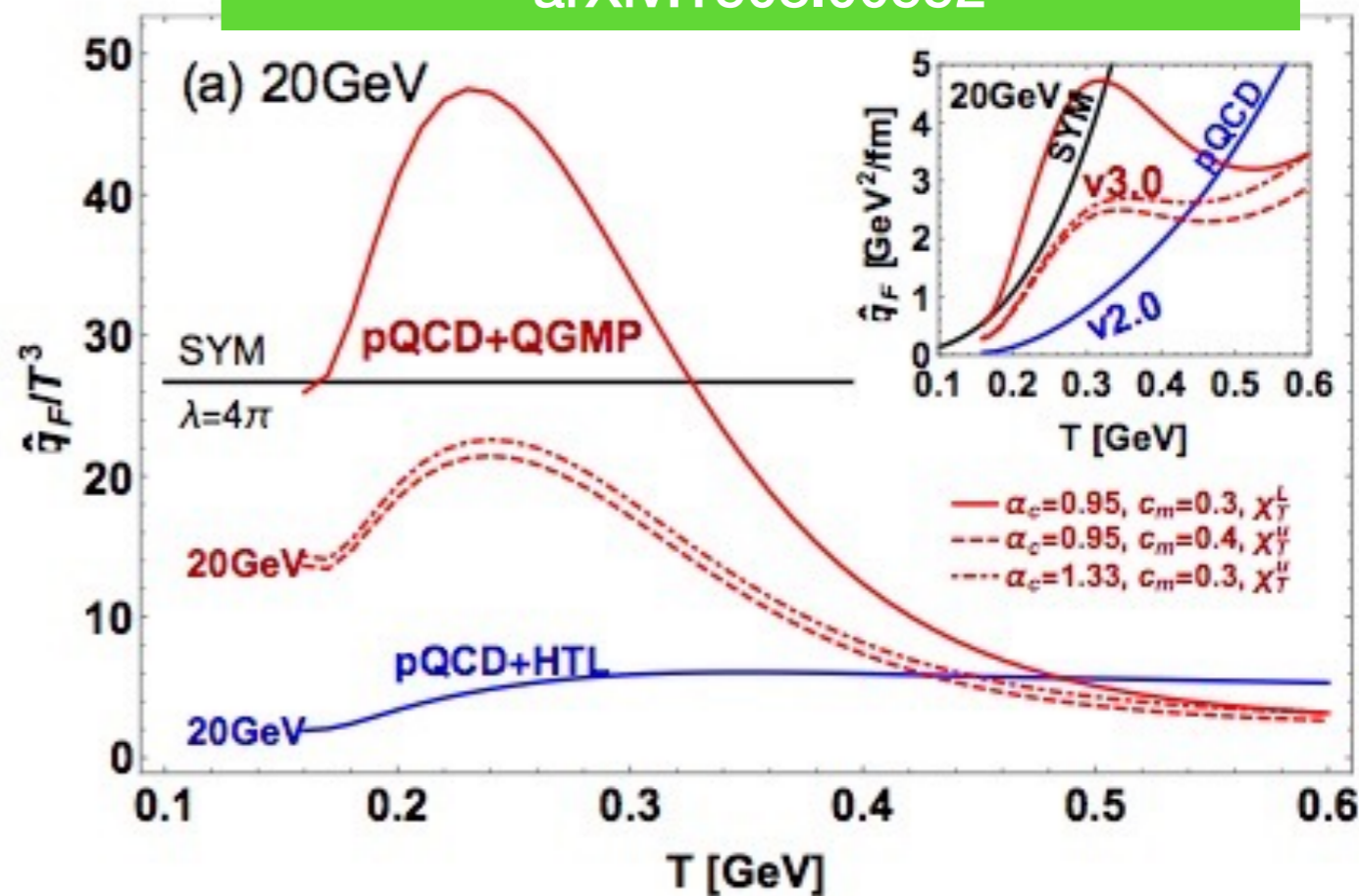
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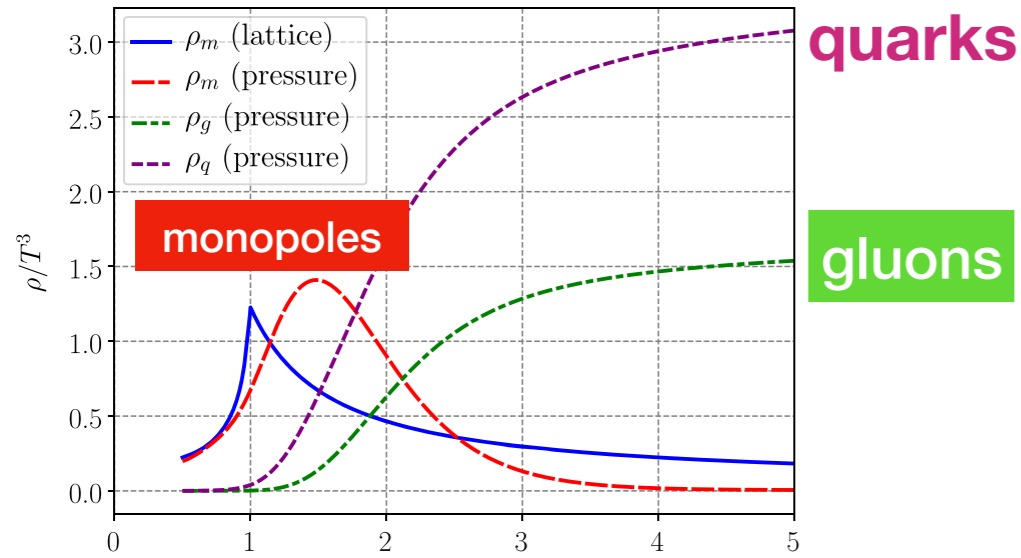
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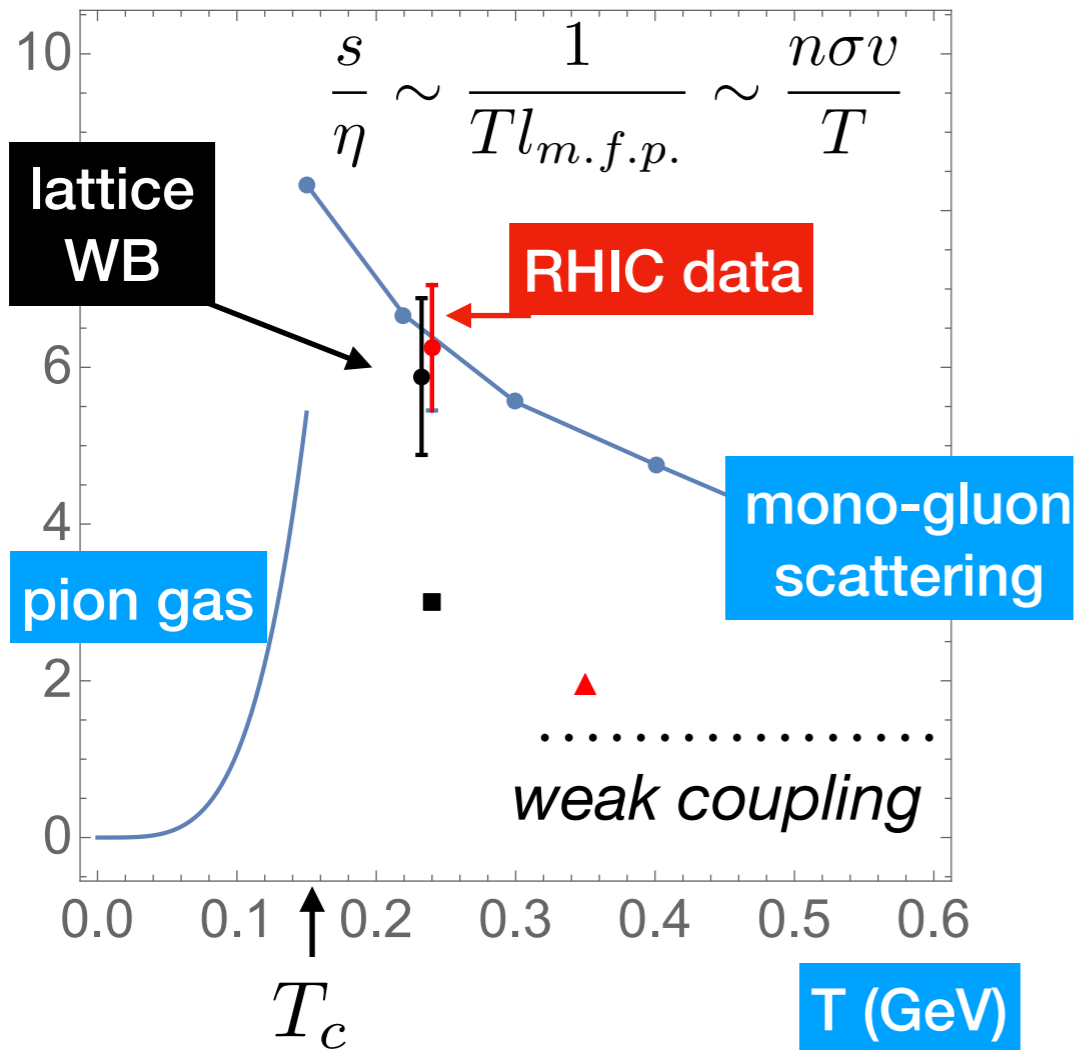
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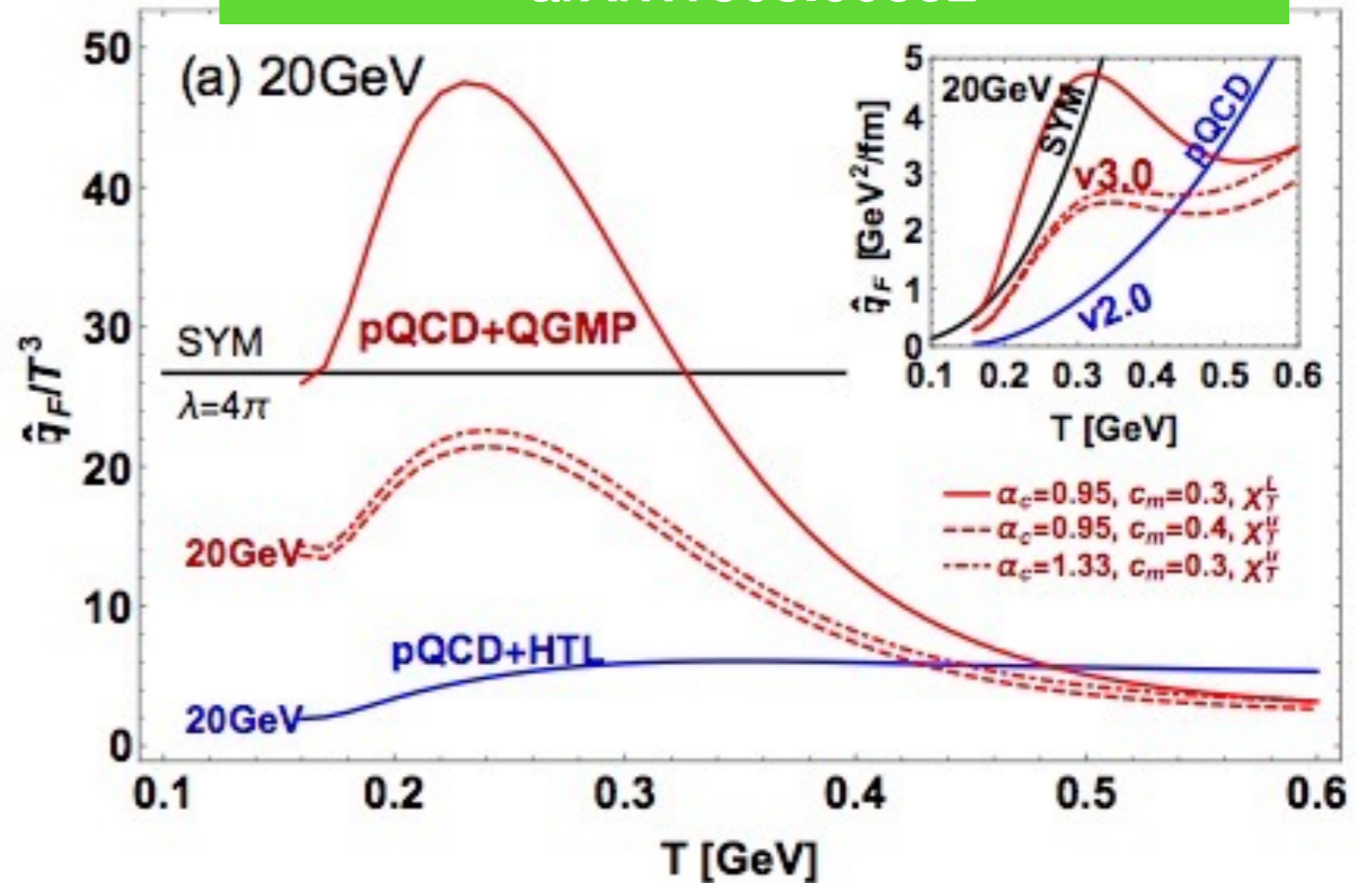
**only the monopole density peaks near  $T_c$ !**

## Strongly coupled quark-gluon plasma in heavy ion collisions

Edward Shuryak Rev.Mod.Phys. 89 (2017) 035001



Xu, J., J. Liao, and M. Gyulassy (2015), arXiv:1508.00552





# Are there monopoles in QCD?

- they are **not** 't Hooft-Polyakov monopoles because we do **not** have adjoint scalars
- Yes, lattice people learned how to find and trace them
- but one would want some analytic control

We do have **instantons** and **instanton-dyons** with good semiclassical control ( $S \gg \hbar$ )

*but*

- those are Euclidean objects,  
which cannot be taken out of Matsubara time
- for example we cannot calculate rescattering of  
quasiparticles or jets



Non-zero Polyakov line splits instantons  
into  $N_c$  instanton-dyons  
(Kraan, van Baal, Lee, Lu 1998)

Explained mismatch of quark condensate in SUSY QCD

V.Khoze (jr) et al 2001

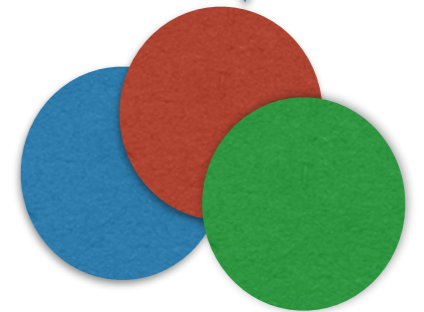
Explained confinement by back reaction to free energy

D.Diakonov 2012, Larsen+ES, Liu, Zahed+ES 2016

Explain chiral symmetry breaking in QCD  
and in setting with **modified fermion periodicities**

R.Larsen+ES 2017, Unsal et al 2017

BPST



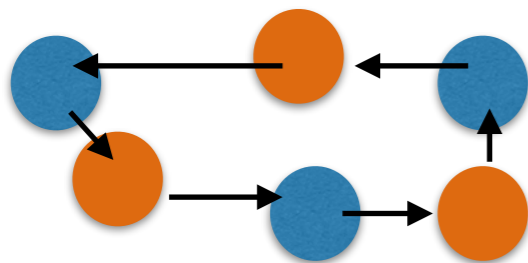
# Instanton-dyon Ensemble with two Dynamical Quarks: the Chiral Symmetry Breaking

Rasmus Larsen and Edward Shuryak

Department of Physics and Astronomy, Stony Brook University, Stony Brook NY 11794-3800, USA

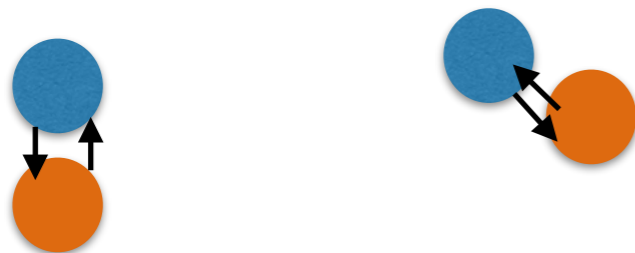
This is the second paper of the series aimed at understanding of the ensemble of the instanton-dyons, now with two flavors of light dynamical quarks. The partition function is appended by the fermionic factor,  $(\det T)^{N_f}$  and Dirac eigenvalue spectra at small values are derived from the numerical simulation of 64 dyons. Those spectra show clear chiral symmetry breaking pattern at high dyon density. Within current accuracy, the confinement and chiral transitions occur at very similar densities.

$$|\langle \bar{\psi}\psi \rangle| = \pi \rho(\lambda)_{\lambda \rightarrow 0, m \rightarrow 0, V \rightarrow \infty}$$



collectivized  
zero mode zone

dip near zero is  
a finite size effect



low density  
unbroken chiral sum

extracting condensate  
is far from trivial...

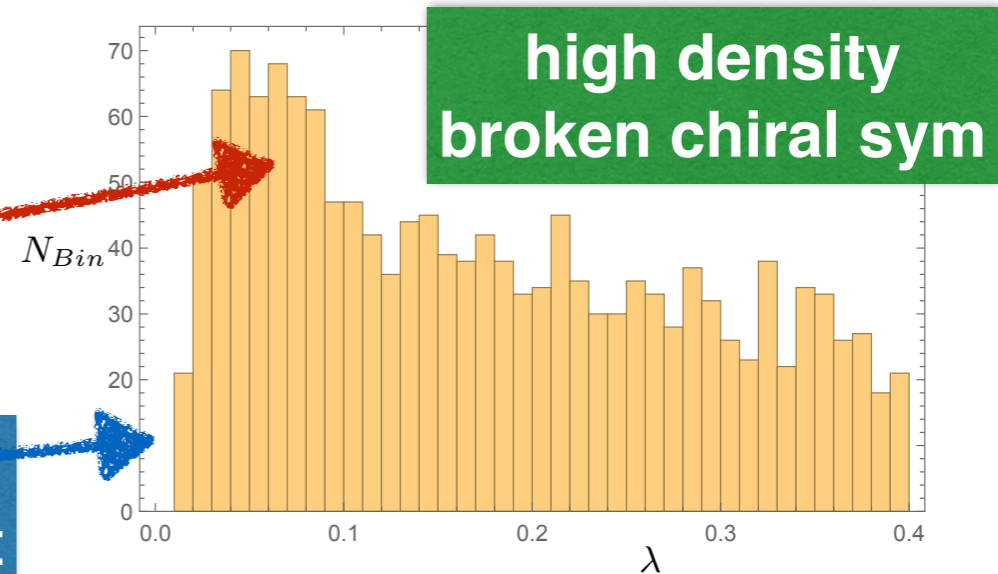


FIG. 1: Eigenvalue distribution for  $n_M = n_L = 0.47$ ,  $N_F = 2$  massless fermions.

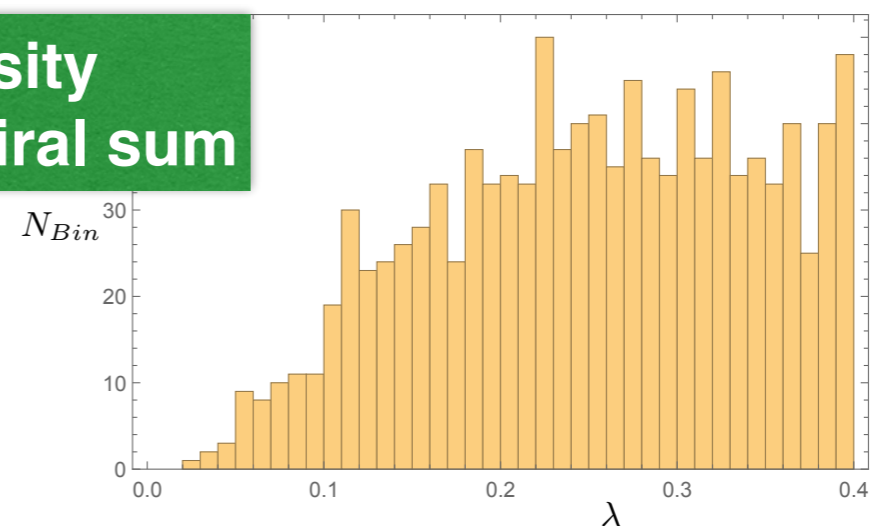
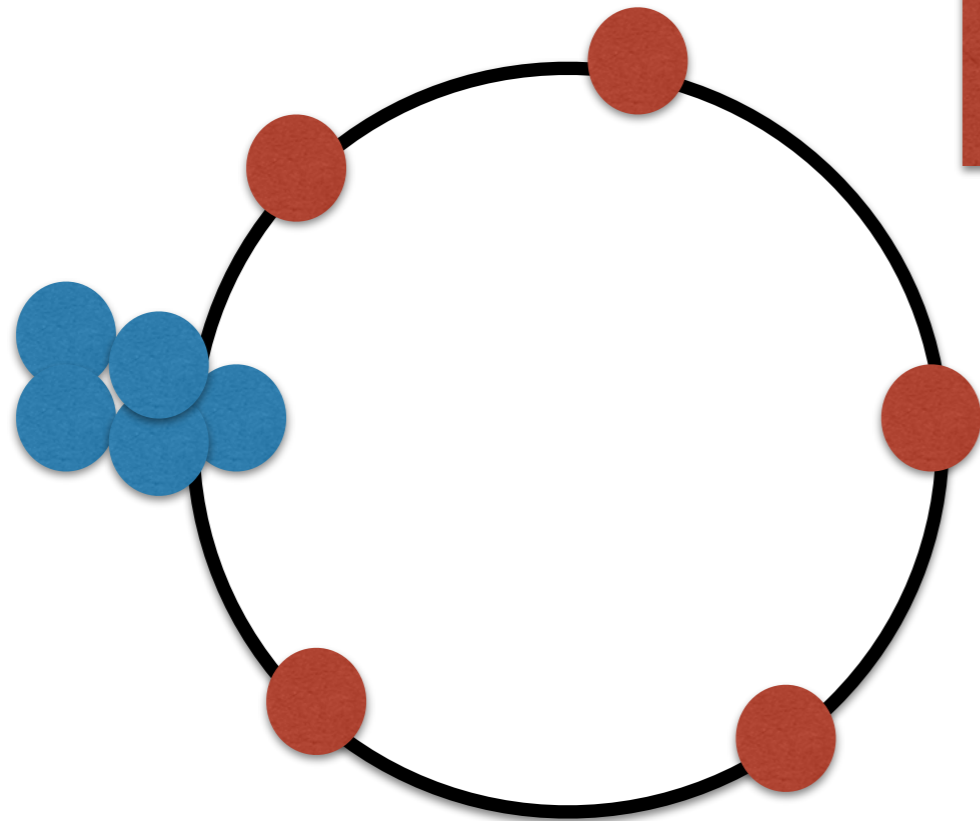


FIG. 2: Eigenvalue distribution for  $n_M = n_L = 0.08$ ,  $N_F = 2$  massless fermions.

# Ordinary $N_c=N_f=5$ QCD



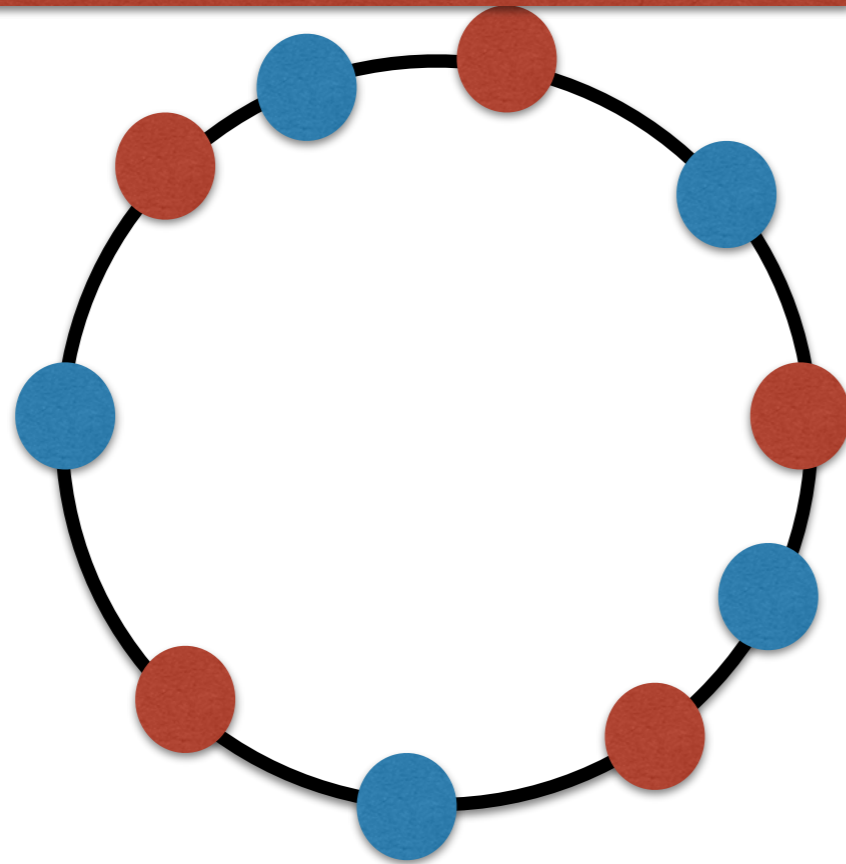
**P without a trace  
is a diagonal unitary matrix  
 $\Rightarrow N_c$  phases (red dots)**

**quark periodicity  
phases  $\Rightarrow N_f$  blue dots  
are in this case all  $=\pi$   
quarks are fermions**

**as a consequence,  
out of 5 types of instanton-dyons  
only one L has zero modes**

still  $N_c=N_f=5$  but with  
“most democratic” arrangement  
ZN-symmetric QCD

H. Kouno, Y. Sakai, T. Makiyama, K. Tokunaga, T.  
Sasaki and M. Yahiro, J. Phys. G 39, 085010 (2012).



quark periodicity  
phases  $\Rightarrow$   $N_f$  blue dots  
are in this case  
flavor-dependent

**In this case each dyon type has  
one zero mode  
with one quark flavor  
 $\Rightarrow$   $N$  independent topological ZMZ's!**



# Both transitions are dramatically different!

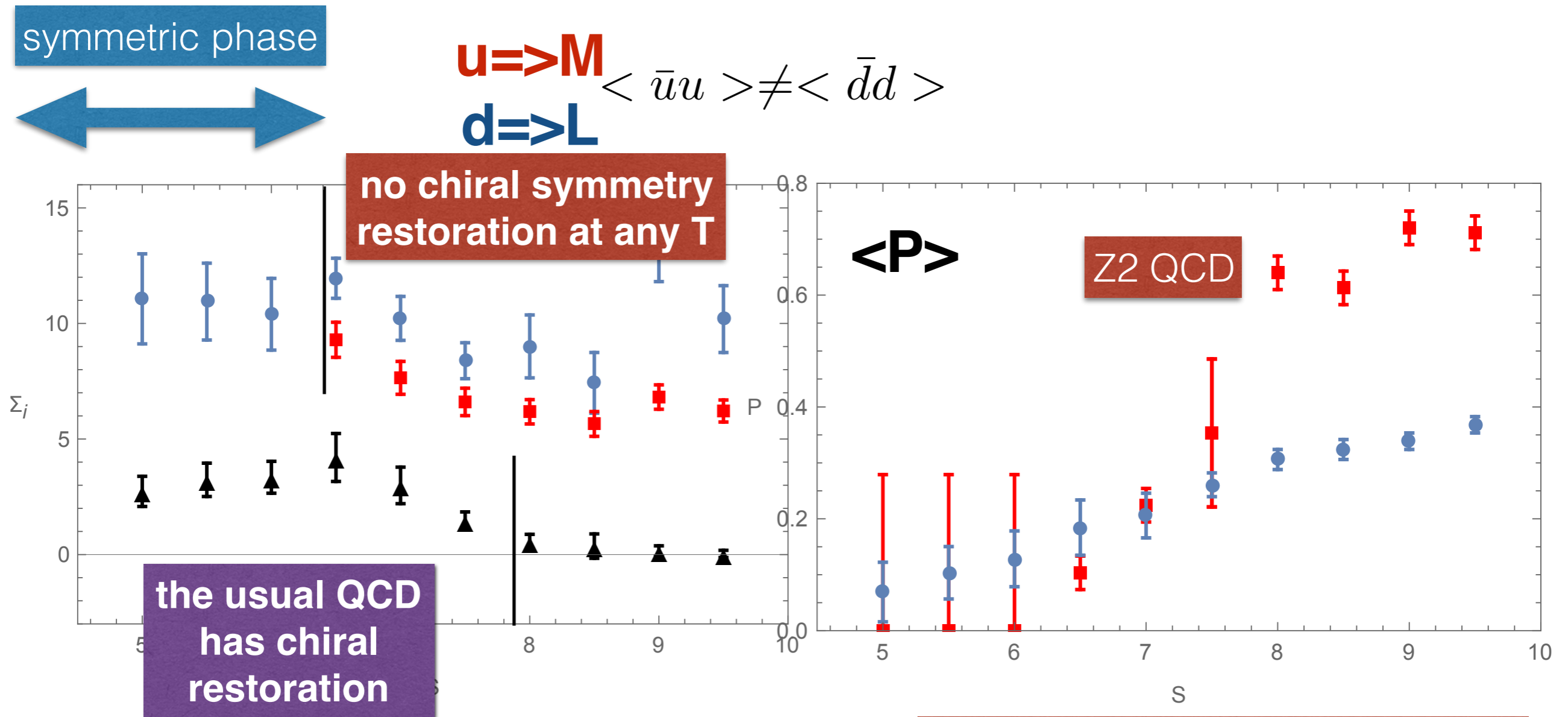


FIG. 6: Chiral condensate generated by  $u$  quarks and  $L$  dyons (red squares) and  $d$  quarks interacting with  $M$  dyons (blue circles) as a function of action  $S$ , for the  $Z_2$ -symmetric model. For comparison we also show the results from II for the usual QCD-like model with  $N_c = N_f = 2$  by black triangles.

**Note that the condensate is much larger for Z2QCD**

**confining phase gets much more robust: strong first order mixed phase (flat F) is observed at medium densities**



**Are instanton-dyons  
related to monopoles?**

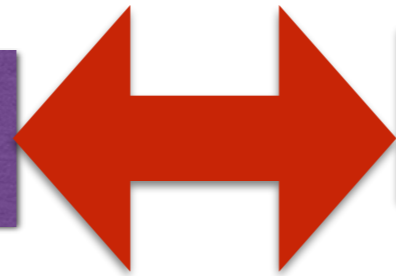
One can however start in the theory  
in which there is a complete theoretical control  
**on both** and **compare two approaches directly**

N.Dorey and A.Parnachev  
JHEP 0108, 59 (2001)  
hep-th/0011202]

N=4 extended supersymmetry  
with Higgsed scalar  
compactified on a circle

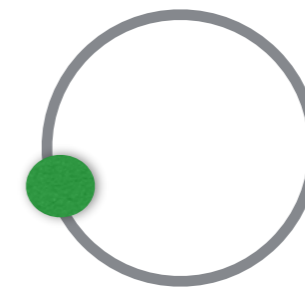
Partition function calculated in  
terms of **monopoles**

Partition function calculated in  
terms of **instanton-dyons**



Configurations are obviously very different  
Zs also look different,  
and yet they are related  
by the **Poisson summation formula**  
and thus are the same!!!

# Is there any relation between the semiclassical instanton-dyons and QCD monopoles?



Adith Ramamurti,<sup>\*</sup> Edward Shuryak,<sup>†</sup> and Ismail Zahed<sup>‡</sup>

The same phenomenon in much simpler setting:  
quantum particle on a circle at finite T

$$Z_1 = \sum_{l=-\infty}^{\infty} \exp\left(-\frac{l^2}{2\Lambda T} + il\omega\right)$$

moment of inertia

Aharonov-Bohm phase

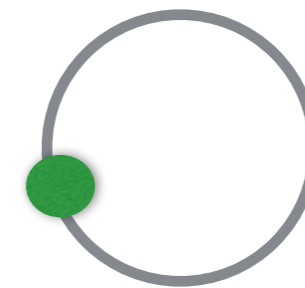
$$Z_2 = \sum_{n=-\infty}^{\infty} \sqrt{2\pi\Lambda T} \exp\left(-\frac{T\Lambda}{2}(2\pi n - \omega)^2\right).$$

Matsubara winding number

based on classical paths

$$\alpha_n(\tau) = 2\pi n \frac{\tau}{\beta},$$

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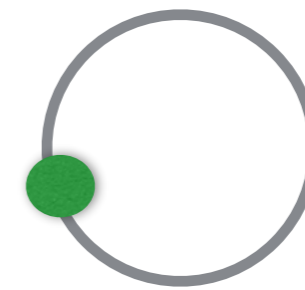
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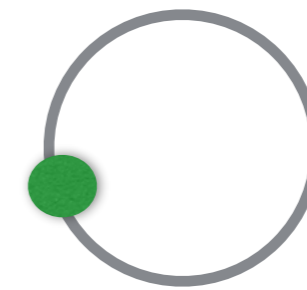
based on classical paths

And yet, they are the same!  
 (elliptic theta function of the 3 type)

$$Z_1 = Z_2 = \theta_3\left(-\frac{\omega}{2}, \exp\left(-\frac{1}{2\Lambda T}\right)\right)$$



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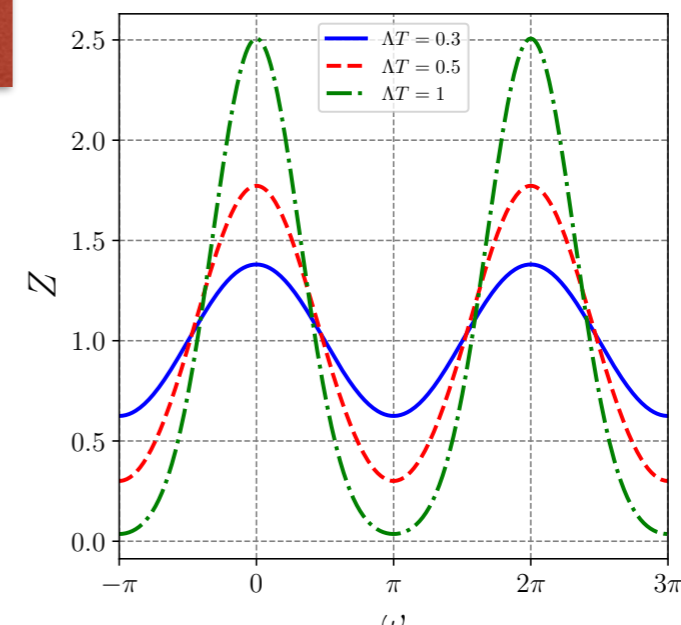
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Adith Ramamurti,<sup>\*</sup> Edward Shuryak,<sup>†</sup> and Ismail Zahed<sup>‡</sup>

$$\sum_{n=-\infty}^{\infty} f(\omega + nP) = \sum_{l=-\infty}^{\infty} \frac{1}{P} \tilde{f}\left(\frac{l}{P}\right) e^{i2\pi l\omega/P}$$

## instanton-dyons with winding number n

The twisted solution is obtained in two steps. The first is the substitution

$$v \rightarrow n(2\pi/\beta) - v, \quad (13)$$

and the second is the gauge transformation with the gauge matrix

$$\hat{\Omega} = \exp\left(-\frac{i}{\beta} n\pi\tau\hat{\sigma}^3\right), \quad (14)$$

where we recall that  $\tau = x^4 \in [0, \beta]$  is the Matsubara time. The derivative term in the gauge transformation adds a constant to  $A_4$  which cancels out the unwanted  $n(2\pi/\beta)$  term, leaving  $v$ , the same as for the original static monopole. After “gauge combing” of  $v$  into the same direction, this configuration – we will call  $L_n$  – can be combined with any other one. The solutions are all

$$S_n = (4\pi/g^2) |2\pi n/\beta - v|$$

Poisson summation formula can be used to derive the monopole sum

$$Z_{\text{inst}} = \sum_n e^{-\left(\frac{4\pi}{g_0^2}\right) |2\pi n - \omega|}$$

$$Z_{\text{mono}} \sim \sum_{q=-\infty}^{\infty} e^{iq\omega - S(q)}$$



$$S(q) = \log\left(\left(\frac{4\pi}{g_0^2}\right)^2 + q^2\right)$$

$$\approx 2\log\left(\frac{4\pi}{g_0^2}\right) + q^2 \left(\frac{g_0^2}{4\pi}\right)^2 + \dots$$

**q is angular momentum of rotating monopole, so it is electric charge**

**Can chiral symmetry breaking  
be understood  
via monopoles?**

# Chiral symmetry breaking and monopoles in gauge theories

Adith Ramamurti\* and Edward Shuryak†

*Department of Physics and Astronomy,*

*Stony Brook University,*

*Stony Brook, NY 11794, USA*

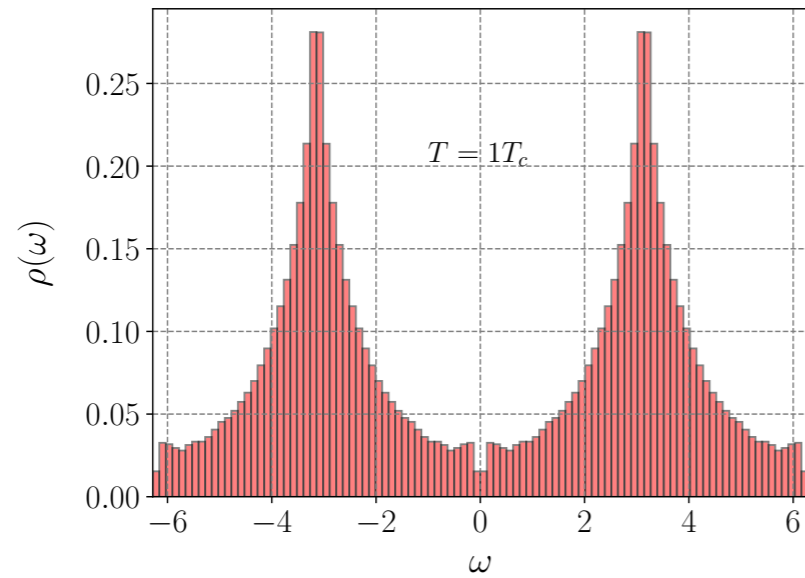
(Dated: January 23, 2018)

**Fermionic zero modes of monopoles are in 3d  
So they are q-m bound states**

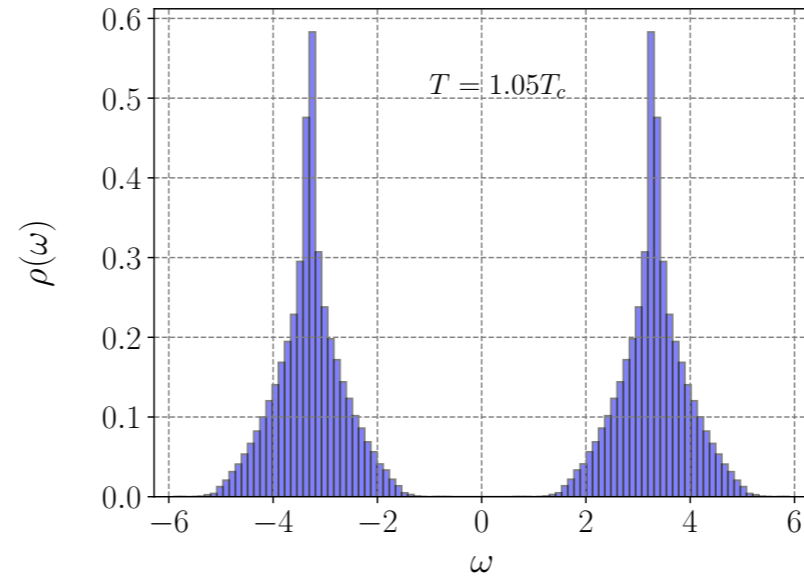
**Chiral symmetry breaking is based on 4d near-zero eigenmodes**

**Monopole mode leaves out the tau dependence  
And with anti-periodic quarks, it leads to Matsubara eigenvalues  $\pm \pi T$   
Can collectivization of eigenstates fill in the gap?**

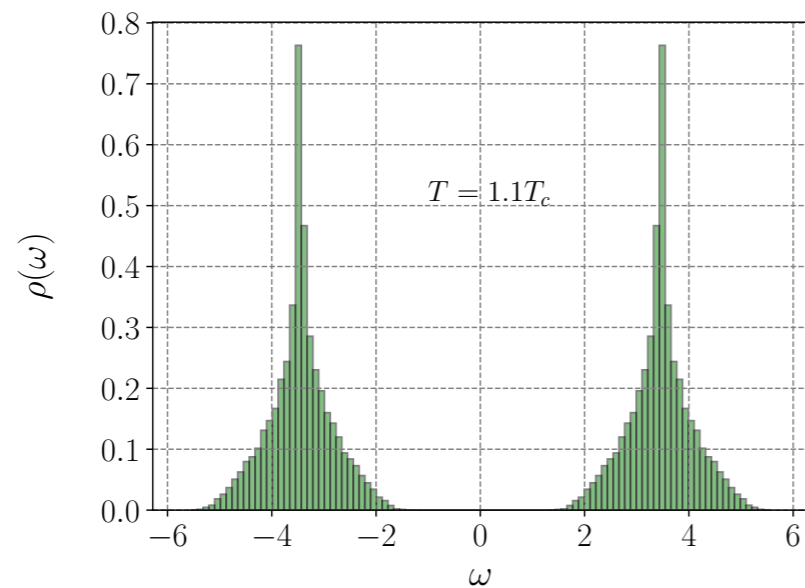
$$U = \oint_{\beta} d\tau e^{iH\tau} = -\mathbb{1}. \quad \lambda_i + \omega_{i,n} = \left( n + \frac{1}{2} \right) \frac{2\pi}{\beta},$$



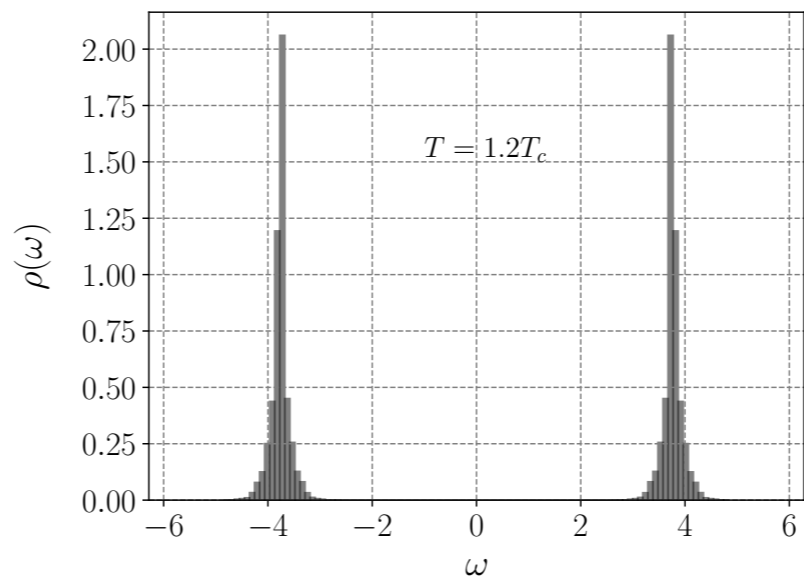
(a)  $T = 1T_c$



(b)  $T = 1.05T_c$



(c)  $T = 1.1T_c$



(d)  $T = 1.2T_c$

FIG. 4: Distributions of Dirac eigenvalues for  $T/T_c =$  (a) 1 , (b) 1.05 , (c) 1.1, and (d) 1.2, respectively.

**Yes, the gap at zero can be filled  
And this happens exactly at  $T_c$ !**

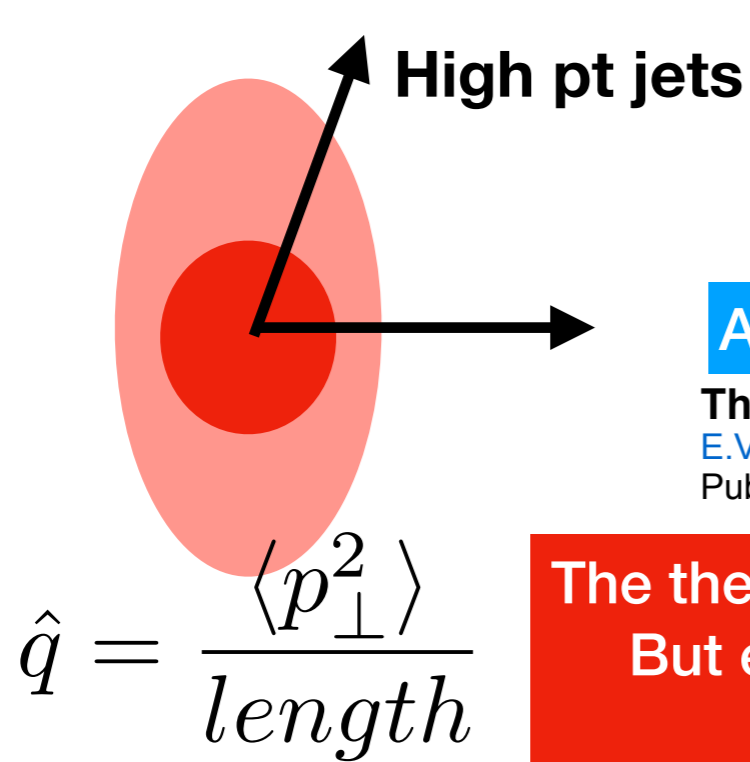


## Summary

- Instanton-dyons and monopoles look different but lead to **the same** partition function. **High and low T series.**
- Chiral condensate is due to collectivization of topological zero modes, for monopole as well
- sQGP is unusual because it is a **dual plasma**, with both electrically and magnetically charged quasiparticles
- As T cools, and electric coupling **increases**, the magnetic coupling **decreases**
- **As monopoles get lighter, their density grows till BEC (confinement)**

Extra slides

# A relatively recent story: the angular distribution of jet quenching and monopoles



$$\frac{dN}{dyd^2p_{\perp}} \sim [1 + 2v_2(p_{\perp})\cos(2\phi)]$$

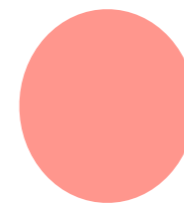
A jet in shorter x direction suffers less quenching by matter

The Azimuthal asymmetry at large  $p_{\perp}$  seem to be too large for a 'jet quenching'  
E.V. Shuryak (SUNY, Stony Brook). Dec 2001. 3 pp.  
Published in Phys.Rev. C66 (2002) 027902

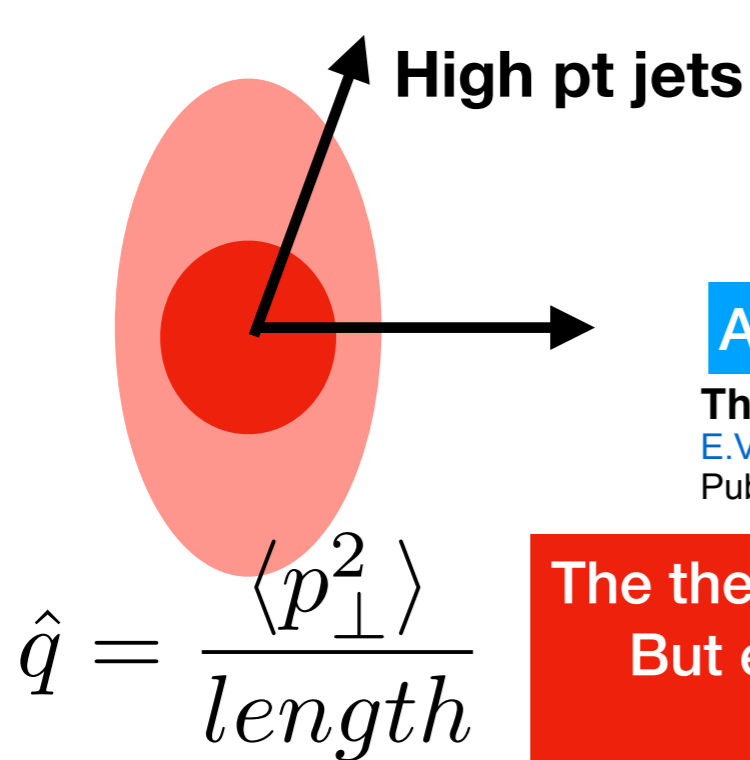
The theory gave reasonably good description of quenching itself  
But experiment stubbornly gave  $v_2$  about twice larger than  
all theories predicted

Angular Dependence of Jet Quenching Indicates Its Strong Enhancement Near the QCD Phase Transition

Jinfeng Liao, Edward Shuryak Phys.Rev.Lett. 102 (2009) 202302



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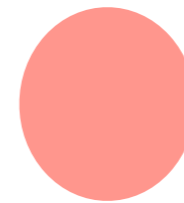
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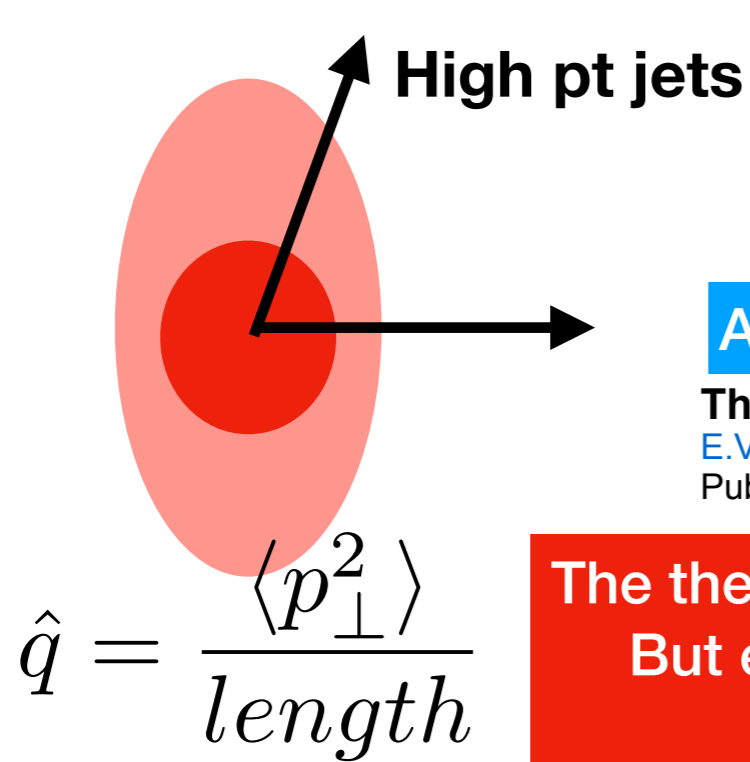
Jinfeng Liao, Edward Shuryak *Phys.Rev.Lett.* 102 (2009) 202302

An explanation proposed: in these theories  
the quenching is proportional to the **density**.  
And the most dense region (shown by the dark red)  
is much "more round" than less dense (pink) region.  
Perhaps quenching peaks at intermediate density?





# A relatively recent story: the angular distribution of jet quenching and monopoles



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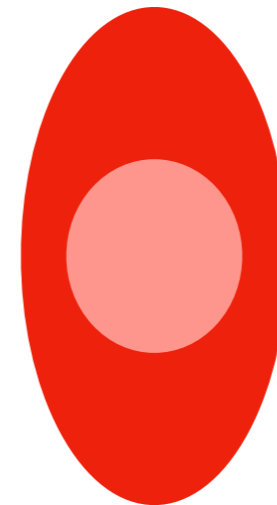
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 But experiment stubbornly gave  $v_2$  about twice larger than  
 all theories predicted

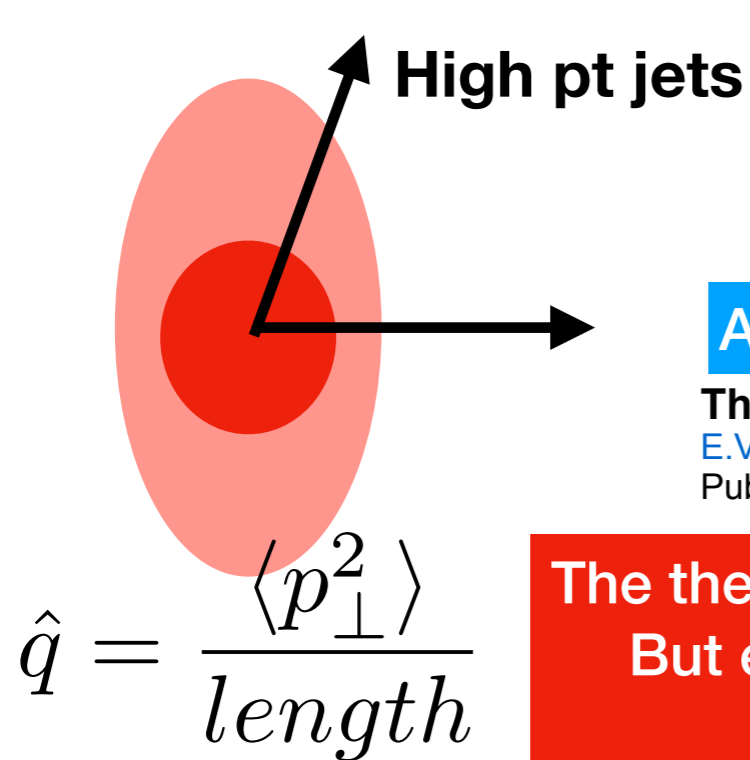
## Angular Dependence of Jet Quenching Indicates Its Strong Enhancement Near the QCD Phase Transition

Jinfeng Liao, Edward Shuryak Phys.Rev.Lett. 102 (2009) 202302

An explanation proposed: in these theories  
 the quenching is proportional to the **density**.  
 And the most dense region (shown by the dark red)  
 is much "more round" than less dense (pink) region.  
 Perhaps quenching peaks at intermediate density?



# A relatively recent story: the angular distribution of jet quenching and monopoles



$$\frac{dN}{dyd^2p_{\perp}} \sim [1 + 2v_2(p_{\perp})\cos(2\phi)]$$

A jet in shorter x direction suffers less quenching by matter

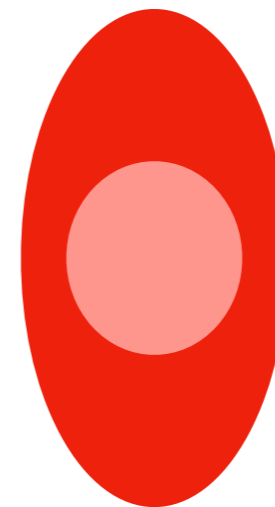
The Azimuthal asymmetry at large  $p_{\perp}$  seem to be too large for a 'jet quenching'  
 E.V. Shuryak (SUNY, Stony Brook). Dec 2001. 3 pp.  
 Published in Phys.Rev. C66 (2002) 027902

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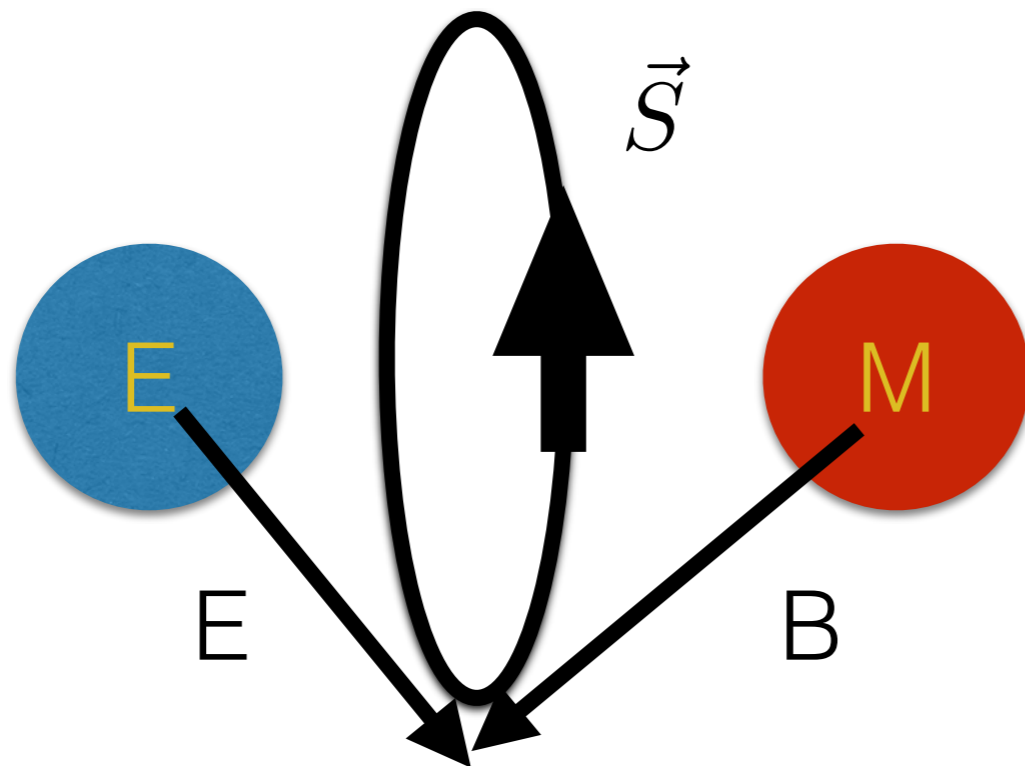
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 the quenching is proportional to the **density**.  
 And the most dense region (shown by the dark red)  
 is much "more round" than less dense (pink) region.  
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this reproduces  
 the azimuthal distribution of jet quenching.  
**BUT WHY ?**

# a monopole and a charge: classical motion

hints from  
the 19-th cent.



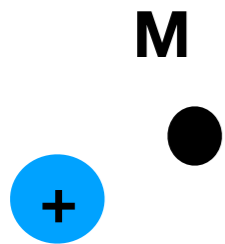
$$\vec{S} = [\vec{E} \times \vec{B}]$$

Pointing vector rotates

Observation by J.J.Thompson:  
even static charge+monopole  
lead to **rotating** electromagnetic field

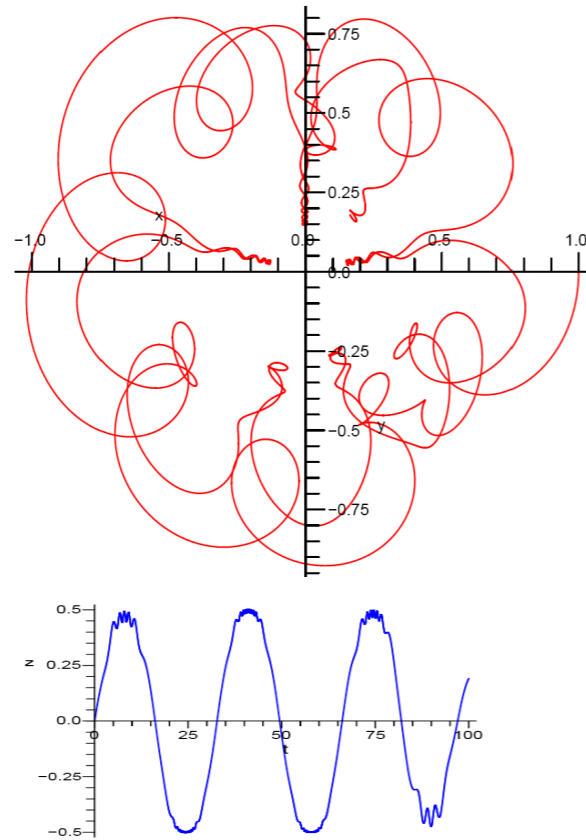
A.Poincare:  
angular momentum of the particle  
**plus that of the field** is conserved =>  
motion on a cone, not plane as usual

H. Poincaré, C. R. Acad. Sci. Ser. B. 123, 530 (1896).

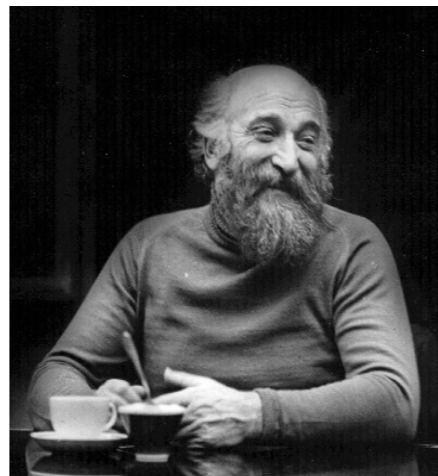
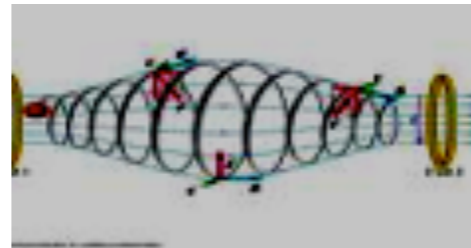


**two charges** play ping-pong  
with a **monopole** without  
even moving!

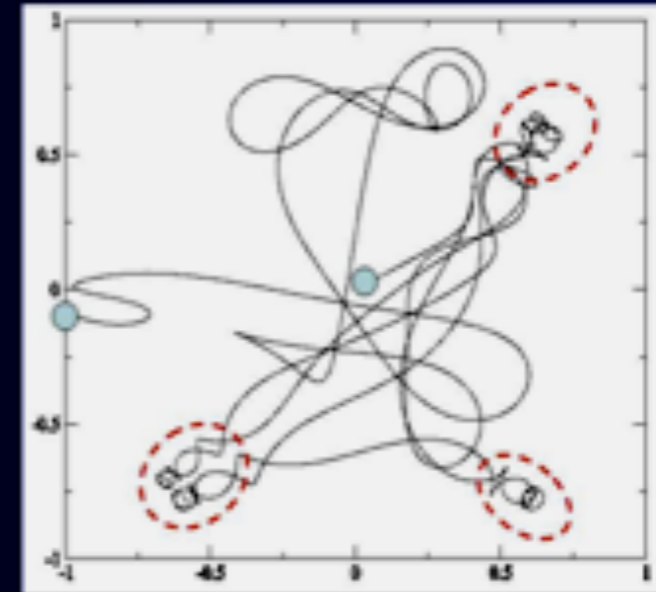
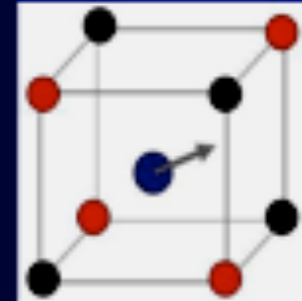
Indeed, collisions are much more frequent than in cascades



Dual to Budker's magnetic bottle



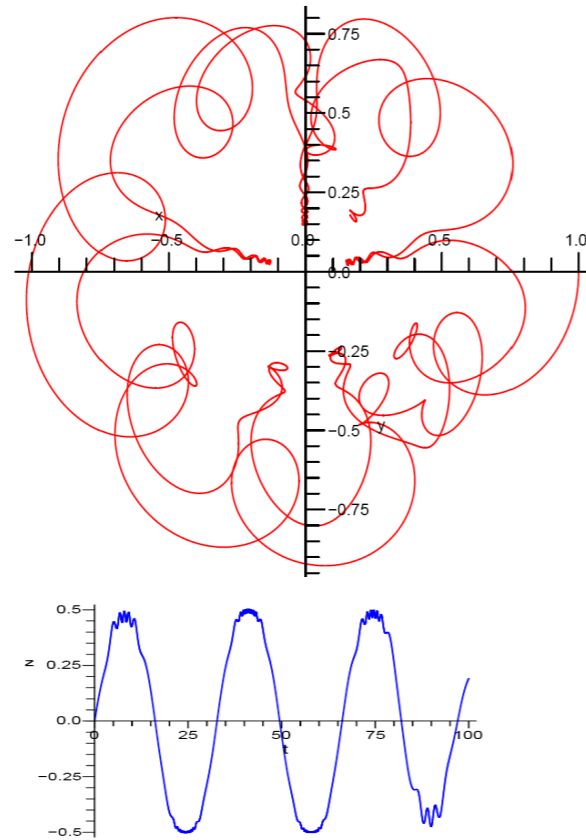
MQP in the field of a cube with alternating charges at corners.



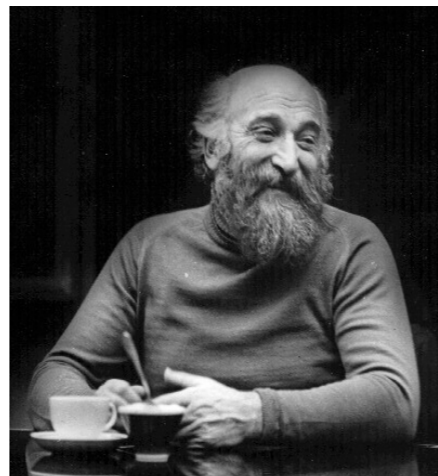
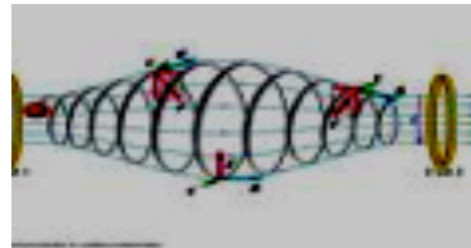
M  
+ ●

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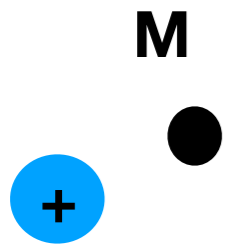


■ MQP in the field of a cube with alternating charges at corners.

The diagram shows a cube with alternating charges at the corners. A central particle trajectory is shown, with a blue dot indicating the particle's position. The plot below shows a complex trajectory in a cube with alternating charges at the corners, with axes ranging from -1 to 1.

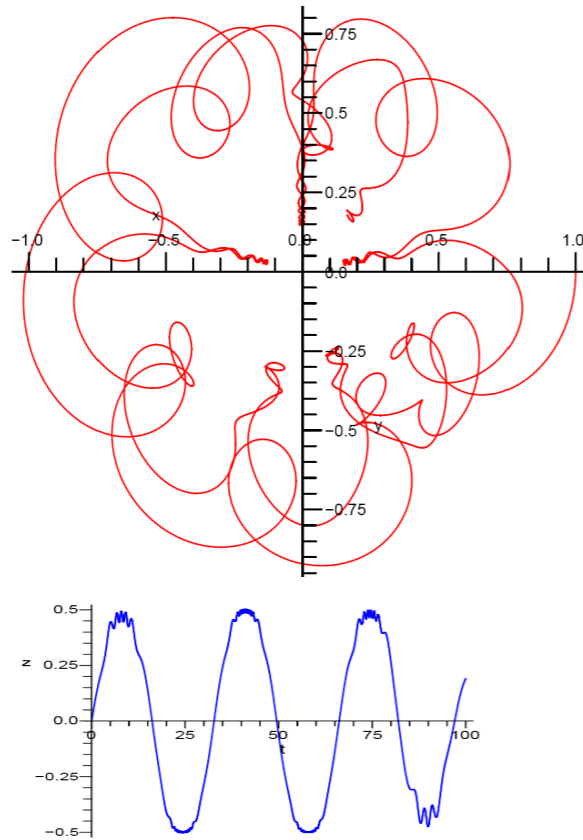
like a proverbial drunkard cannot go home colliding with few lamp posts



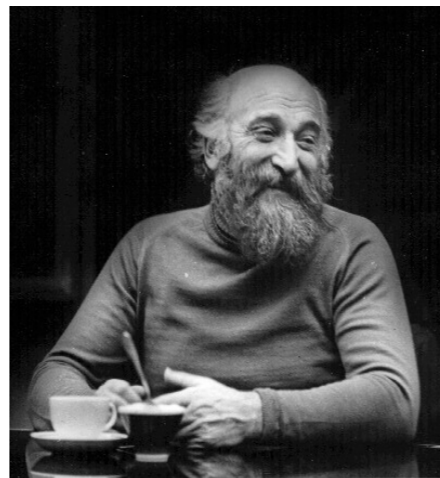
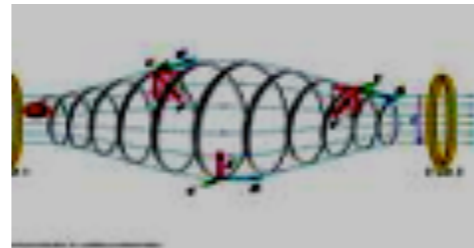


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Dual to Budker's  
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like a proverbial drunkard cannot go home  
colliding with few lamp posts

classical kinetics of the “dual plasma”, with E and M charges  
was simulated by molecular dynamics,  
diffusion coefficient and viscosity calculated

# Quantum-mechanical problem of a charge-monopole scattering (should belong to QM textbooks but is not there)

$$e \cdot g \equiv n \text{ integer}$$

$$\delta_j = \pi j'$$

$$j'(j' + 1) = j(j + 1) - n^2$$

is the only parameter  
It is dimensionless  
so the scattering phase  
cannot depend on momenta



Both  $j$  (total orbital mom.)  
and  $n$  (that of the field) are integers  
**but  $j'$  is not!!!! Thus complicated  
angular distribution**

Unlike in a standard scattering problem  
Y<sub>lm</sub> angular functions cannot be used:  
At large  $l, m \gg 1$  those describe a scattering plane  
But we know in classical limit it is the Poincare cone

D. G. Boulware, L. S. Brown, R. N. Cahn, S. D. Ellis, and C. k. Lee,  
Phys. Rev. D 14, 2708 (1976).  
J. S. Schwinger, K. A. Milton, W. Y. Tsai, L. L. DeRaad, and D. C. Clark,  
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**Note that  $d\delta/dk=0$**

**So no new states and thus no  
corrections to thermodynamics,  
Only to kinetics**

# quantum scattering of quarks and gluons on monopoles and viscosity of strongly coupled QGP

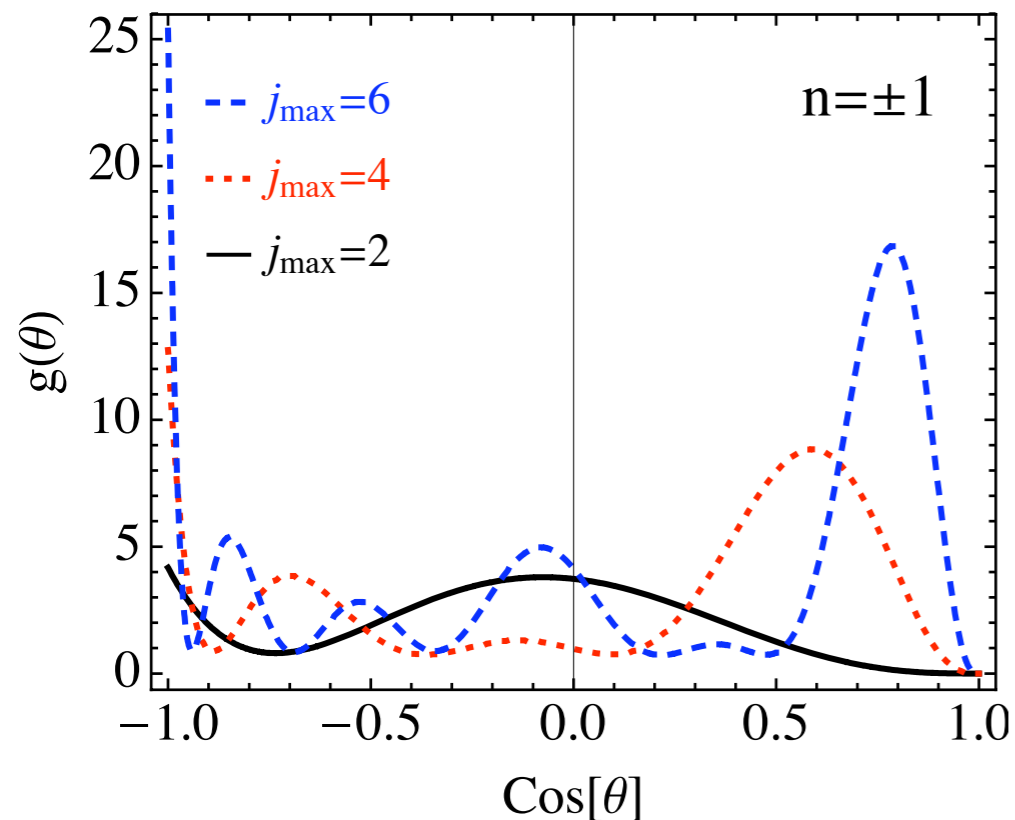
## gluon-monopole scattering explains small viscosity!

PHYSICAL REVIEW D **80**, 034004 (2009)

### Role of monopoles in a gluon plasma

Claudia Ratti and Edward Shuryak\*

backward peak  
important for transport  
cross section



### Not surprising, large correction to transport

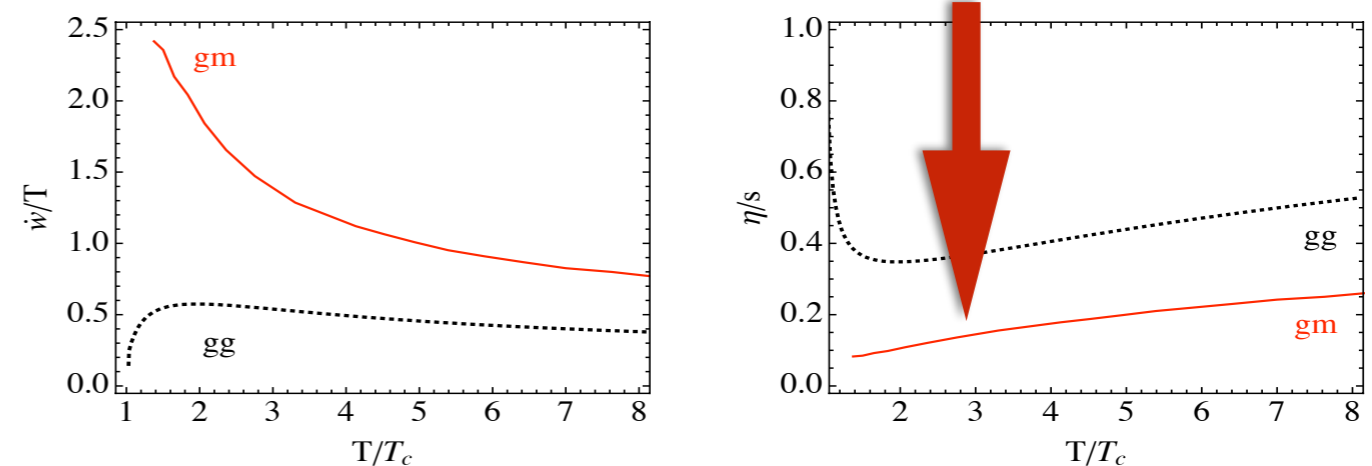


Figure 14: Left panel: gluon-monopole and gluon-gluon scattering rate. Right panel: gluon-monopole and gluon-gluon viscosity over entropy ratio,  $\eta/s$ .

- **RHIC:  $T/T_c < 2$ , LHC  $T/T_c < 4$** : we predict hydro will still be there, with  $\eta/s$  about .2



Spring 2008

A. D'Alessandro and M. D'Elia

Dipartimento di Fisica, Università di Genova and INFN, Sezione di Genova,  
Via Dodecaneso 33, I-16146 Genova, Italy

**x-Correlations  
show it is a liquid  
=> Magnetic  
Coulomb coupling**

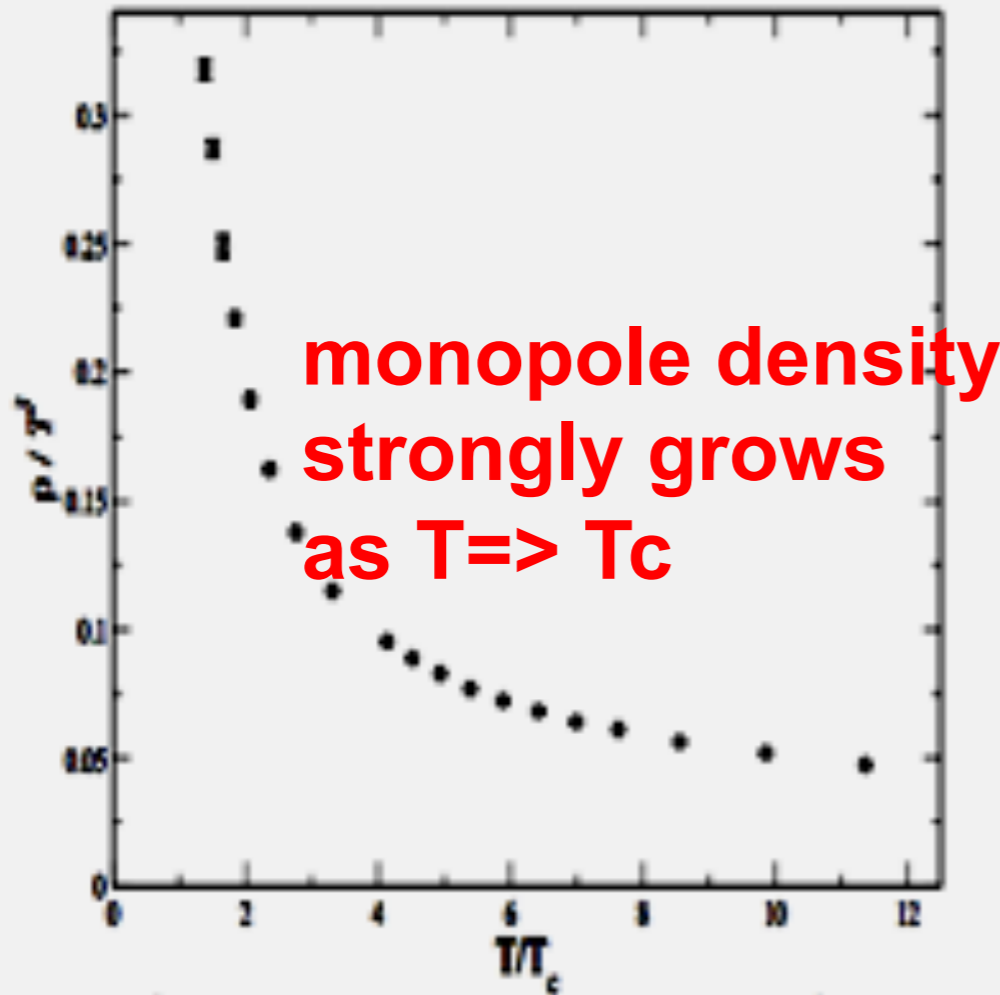


FIG. 3.  $\rho(T)/T^3$  as a function of  $T/T_c$ . Data have been obtained on a  $48^3 \times L_t$  lattice, with variable  $L_t$  and at  $\beta = 2.75$  (first 9 points), and variable  $\beta$  at  $L_t = 4$  (last 10 points).

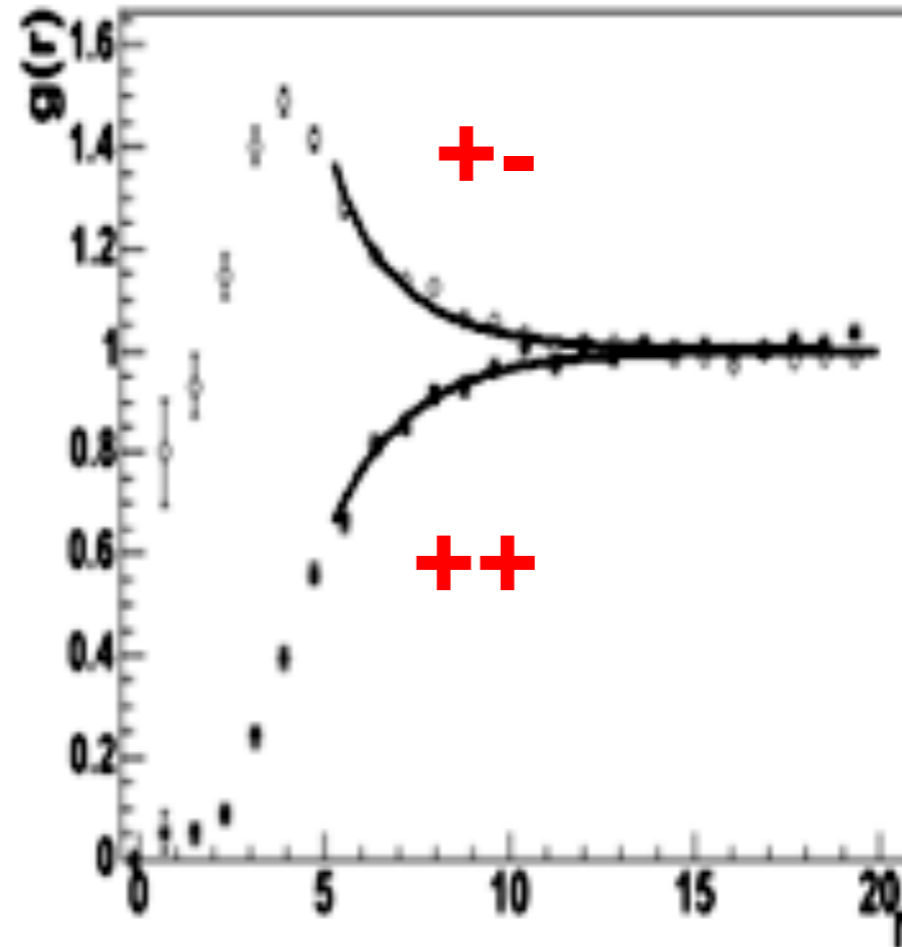


FIG. 5.  $g(r)$  for the monopole-monopole (stars) and monopole-antimonopole (circles) case on  $10^3 \times 5$  lattice at  $\beta = 2.7$  ( $T \simeq 2.85 T_c$ ). The reported curves correspond to fits according to  $\langle \dots \rangle = \exp(-V(r)/T)$  with  $V(r)$  a Yukawa potential [see Eqs. (2.9) and (2.10)].

Lattice SU(2) gauge theory, monopoles found and followed by Min.Ab.gauge



## Magnetic Component of Quark-Gluon Plasma is also a Liquid!

Jinfeng Liao and Edward Shuryak

Department of Physics and Astronomy, State University of New York, Stony Brook, NY 11794

(April 1, 2008)

The so called magnetic scenario recently suggested in [1] emphasizes the role of monopoles in strongly coupled quark-gluon plasma (sQGP) near/above the deconfinement temperature, and specifically predicts that they help reduce its viscosity by the so called “magnetic bottle” effect. Here we present results for monopole-(anti)monopole correlation functions from the same classical molecular dynamics simulations, which are found to be in very good agreement with recent lattice results [2]. We show that the magnetic Coulomb coupling does run in the direction *opposite* to the electric one, as expected, and it is roughly inverse of the asymptotic freedom formula for the electric one. However, as  $T$  decreases to  $T_c$ , the magnetic coupling never gets weak, with the plasma parameter always large enough ( $\Gamma > 1$ ). This nicely agrees with empirical evidences from RHIC experiments, implying that magnetic objects cannot have large mean free path and should also form a good liquid

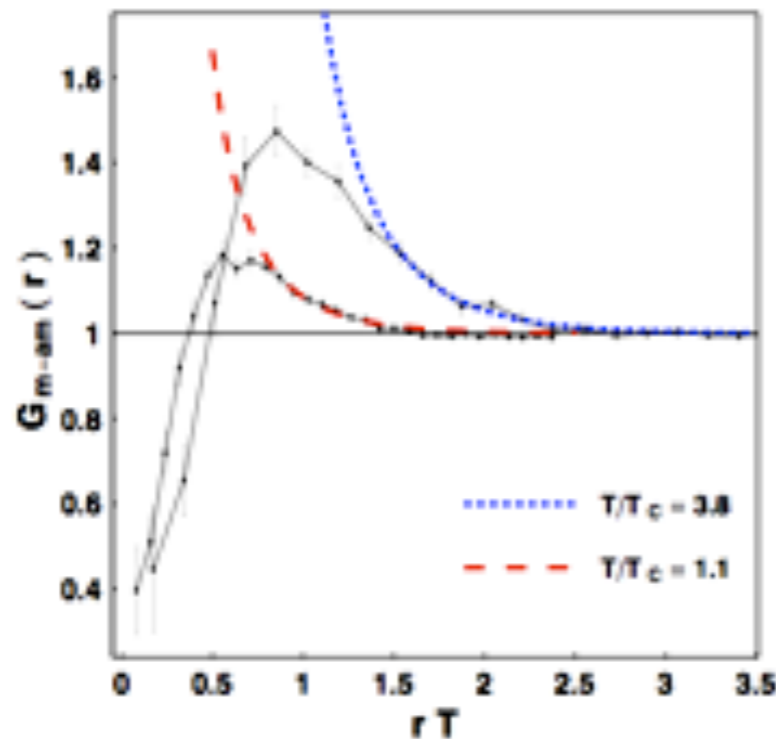
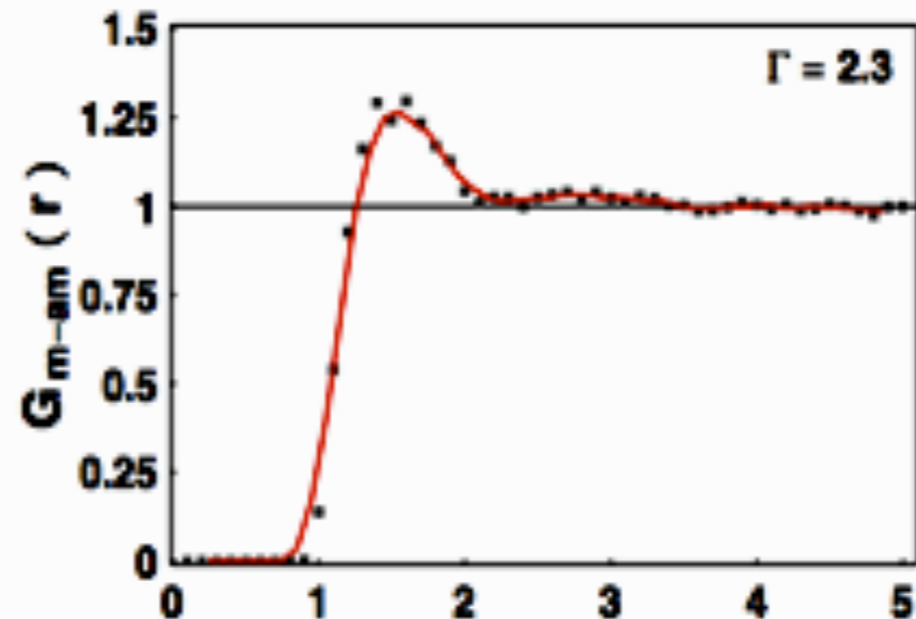


FIG. 2. (color online) Monopole-antimonopole correlators versus distance: points are lattice data [2], the dashed lines are our fits.

Our MD for 50-50 MQP/EQP

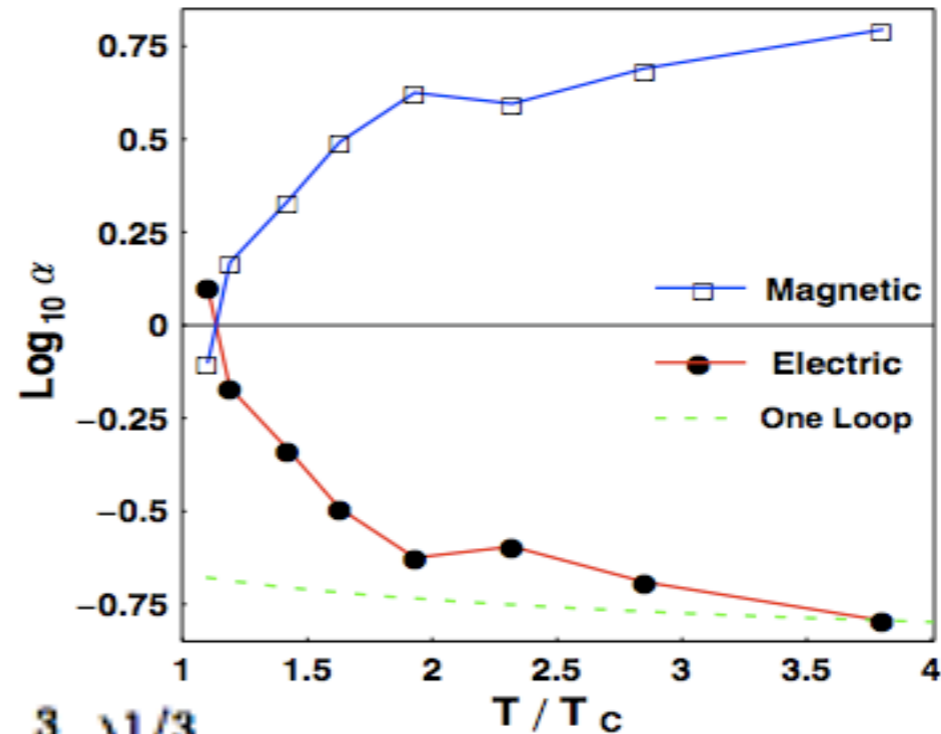


I would not bother you with this plot  
If not one observation:  
The correlation increases with T

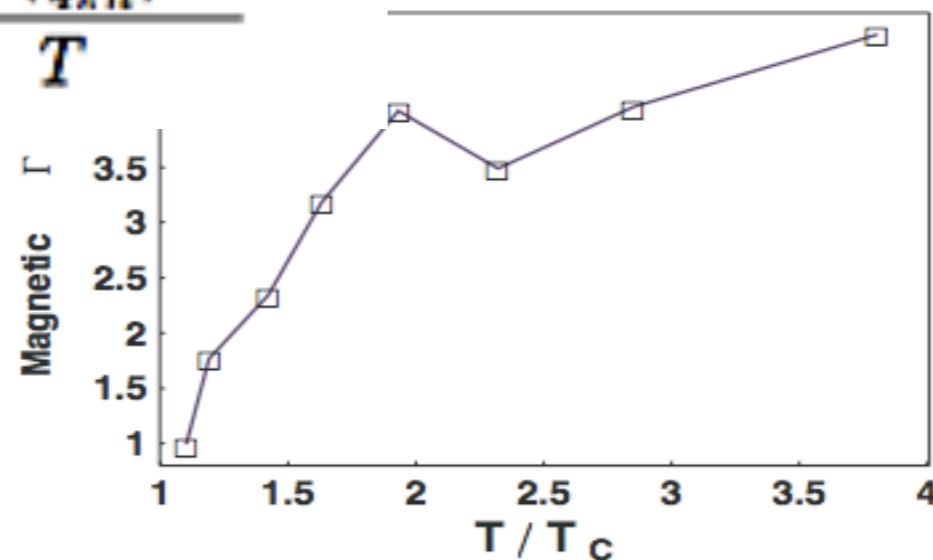
$\alpha_s(\text{electric})$  and  $\alpha_s(\text{magnetic})$

do run in opposite directions!

- Squares: fitted magnetic coupling, circles: its inverse compared to asymptotic freedom (dashed)
- Effective plasma parameter (here for magnetic)
- So, the monopoles are **never weakly coupled!**
- **(just enough to get Bose-condensed)**



$$\Gamma \equiv \frac{\alpha_C / (\frac{3}{4\pi n})^{1/3}}{T}$$



“magnetic scenario”: Liao, ES hep-ph/0611131, Chernodub+Zakharov

Old good Dirac condition

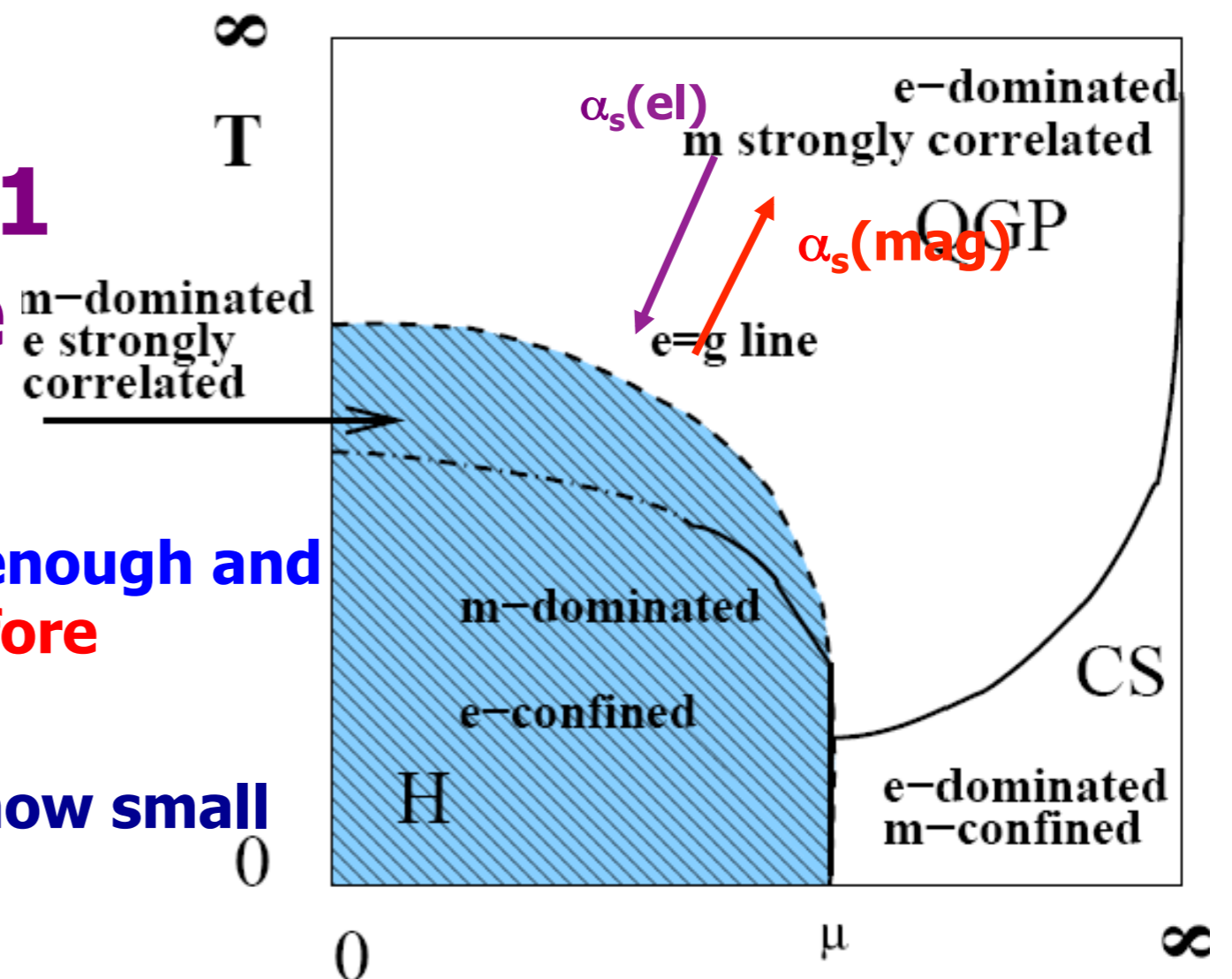
$$\alpha_s(\text{electric}) \quad \alpha_s(\text{magnetic}) = 1$$

=> electric/magnetic couplings (e/g) must run in the opposite directions!

the “equilibrium line”  
 $\alpha_s(\text{el}) = \alpha_s(\text{mag}) = 1$   
 needs to be in the plasma phase

monopoles should be dense enough and sufficiently weakly coupled before deconfinement to get BEC

=>  $\alpha_s(\text{mag}) < \alpha_s(\text{el})$ : how small can  $\alpha_s(\text{mag})$  be?





Static  $\bar{Q}Q$  potentials and the magnetic component of QCD plasma near  $T_c$ 

and earlier works

Jinfeng Liao<sup>1,2,\*</sup> and Edward Shuryak<sup>3,†</sup>

Flux tubes can exist even without “dual superconductor”

At  $T > T_c$ 

E.g. there are plenty of flux tubes on the Sun

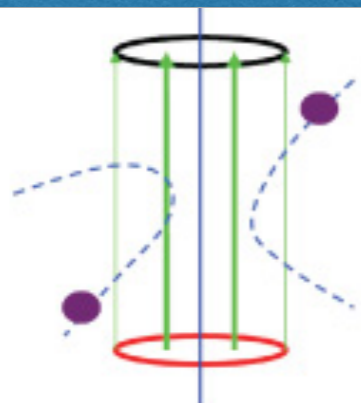
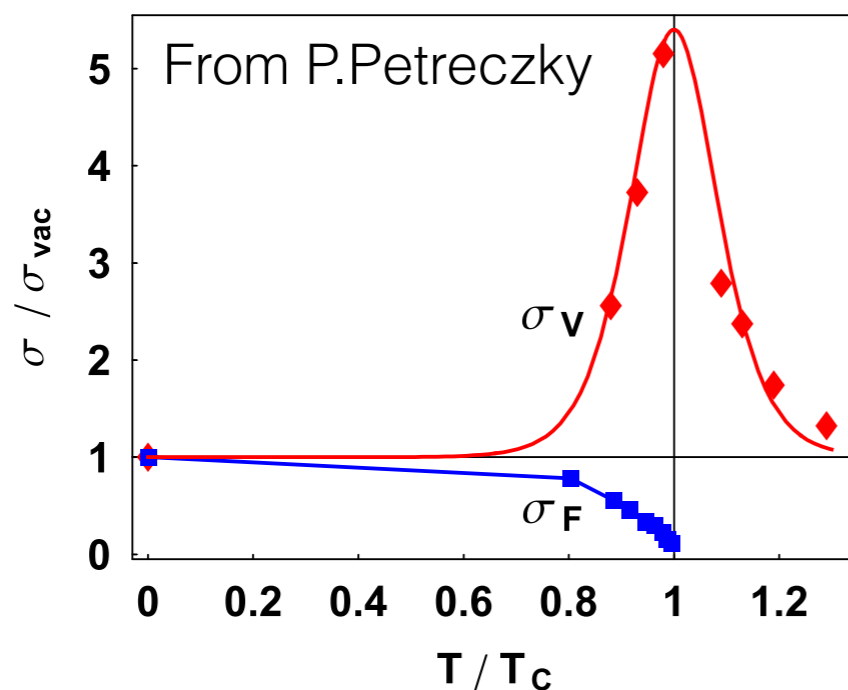
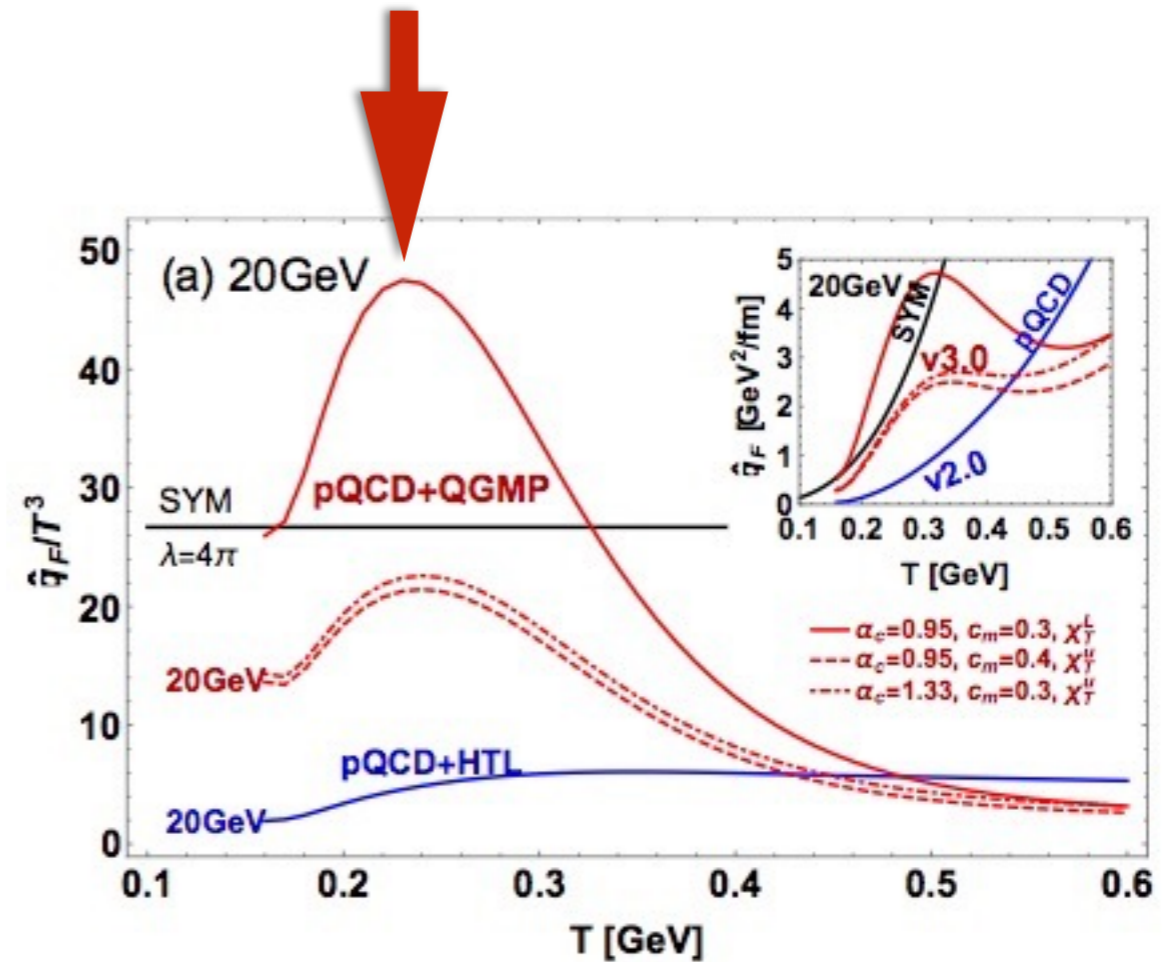
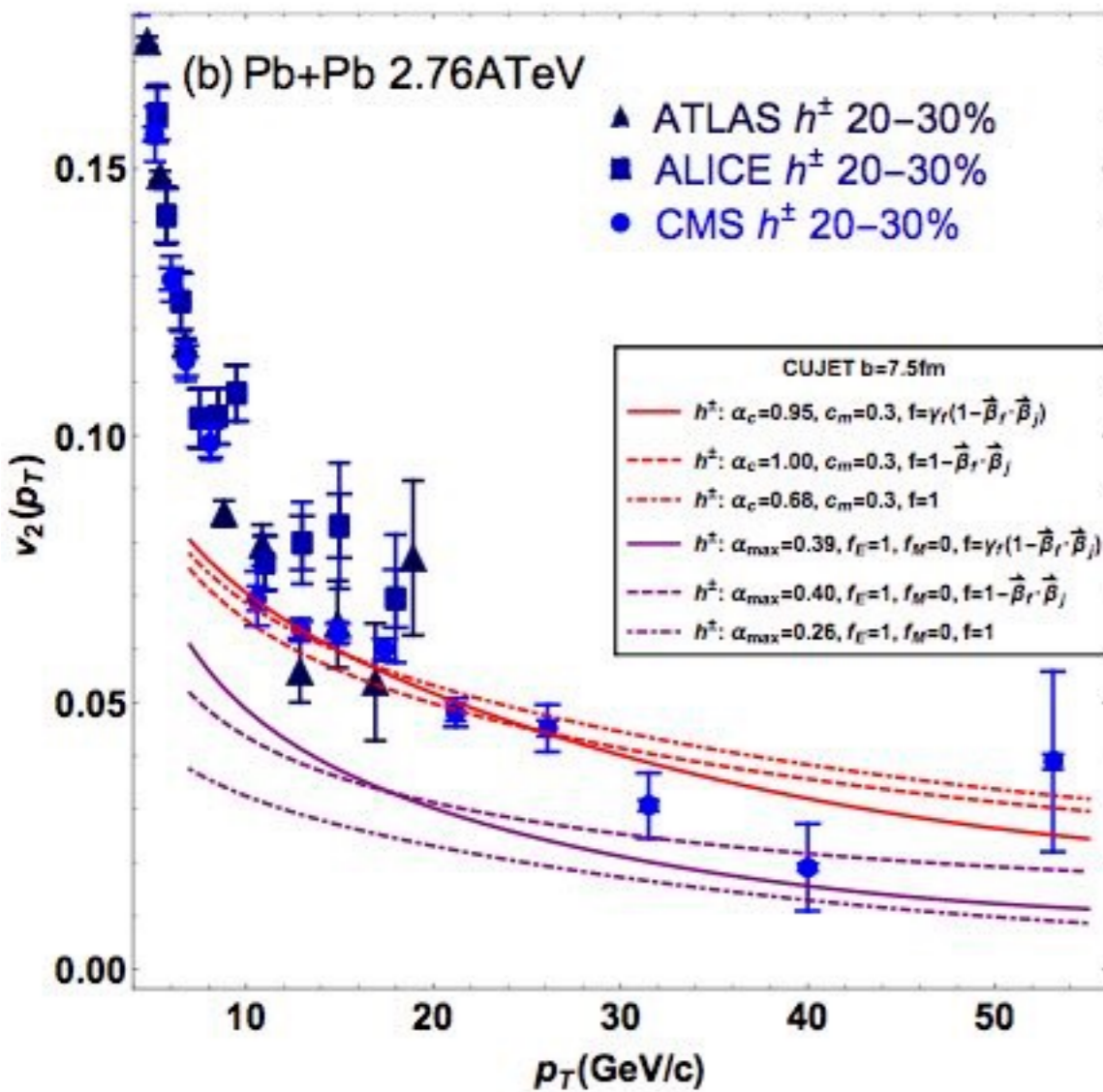
Some density of monopoles  
is enough to provide pressure  
On the electric flux tubeThe only difference is such flux tubes  
are not stable forever  
Because of Ohmic losseson the lattice one cannot study  
unstable objects  
But one can have string tension  
For free energy and potential energyWe argued that free energy corresponds  
To very slow processes, while in quarkonia  
One should use potential energy

FIG. 2 (color online). Effective string tensions in the free energy  $\sigma_F(T)$  (from [4]) and the internal energy  $\sigma_V(T)$  (extracted from [3]).

peak of the density of monopoles at  $T_c$  explains not only a **dip in viscosity (m.f.p.)** but also other things such as jet quenching



Xu, J., J. Liao, and M. Gyulassy (2015),  
arXiv:1508.00552