

Are thermal conductivity or bulk viscosity important in neutron star mergers?

Prof. Mark Alford
Washington University in St. Louis

Alford, Bovard, Hanauske, Rezzolla, Schwenzer

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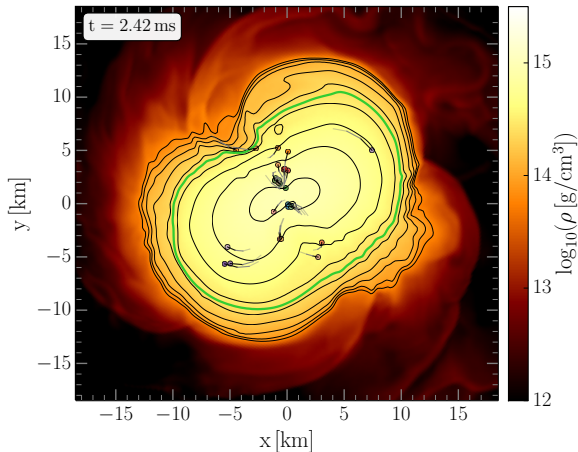
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Outline

- ▶ Neutron star mergers
- ▶ Thermal conductivity
- ▶ Bulk viscosity
- ▶ Conclusions

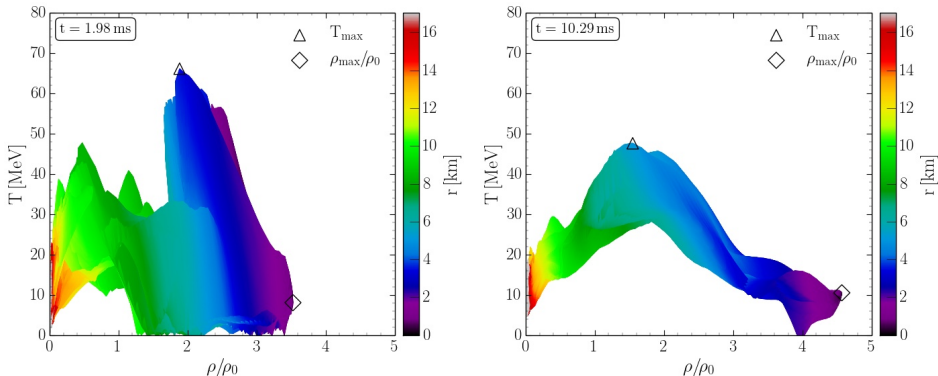
Neutron star mergers

Mergers probe the properties of nuclear/quark matter at high density (up to $\sim 4n_{\text{sat}}$) and temperature (up to ~ 60 MeV)



In developing signatures for **quark matter**, we must include all the relevant physics for **nuclear matter**.

Nuclear material in a neutron star merger



M. Hanauske, Rezzolla group, Frankfurt

Significant spatial/temporal variation in:

temperature
fluid flow velocity
density

so we need to allow for
thermal conductivity
shear viscosity
bulk viscosity

Role of transport in mergers

We can estimate the equilibration times for various forms of dissipation, to decide which is the most important.

- ▶ **Thermal equilibration:** If neutrinos are trapped, and there are short-distance temperature gradients then thermal transport might be fast enough to play a role.

$$\tau_{\kappa}^{(\nu)} \approx 700 \text{ ms} \left(\frac{z_{\text{typ}}}{1 \text{ km}} \right)^2 \left(\frac{T}{10 \text{ MeV}} \right)^2 \left(\frac{0.1}{x_p} \right)^{1/3} \left(\frac{m_n^*}{0.8 m_n} \right)^3 \left(\frac{\mu_e}{2\mu_\nu} \right)^2$$

- ▶ **Shear viscosity:** similar conclusion.
- ▶ **Bulk viscosity:** If Direct Urca processes remain suppressed at the relevant densities and temperatures, bulk viscosity will quickly damp density oscillations

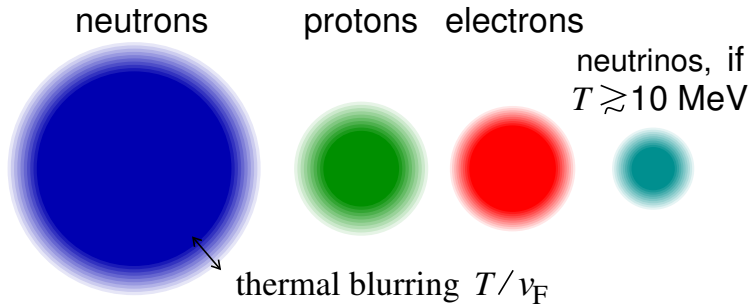
$$\tau_{\zeta}^{\text{min}} \approx 3 \text{ ms} \left(\frac{t_{\text{comp}}}{1 \text{ ms}} \right) \left(\frac{K}{250 \text{ MeV}} \right) \left(\frac{0.25 \text{ MeV}}{Y_{\zeta}} \right)$$

Nuclear material constituents

Temperature: 5 to 20 MeV

Density: up to $4 n_{\text{sat}}$

Fermi
surfaces:



neutrons: $\sim 90\%$ of baryons

$$p_{Fn} \sim 350 \text{ MeV}$$

protons: $\sim 10\%$ of baryons

$$p_{Fp} \sim 150 \text{ MeV}$$

electrons: same density as protons

$$p_{Fe} = p_{Fp}$$

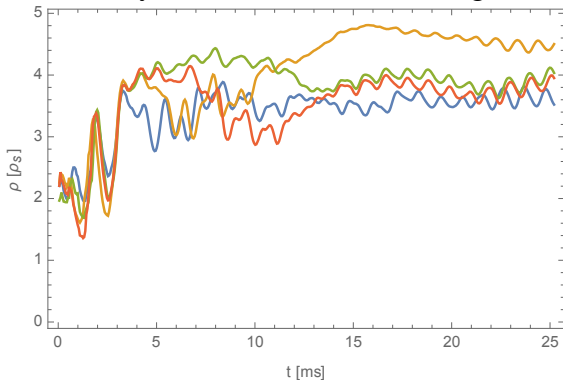
neutrinos: only present if mfp $\lesssim 1 \text{ km}$

$$p_{F\nu} \sim \frac{1}{2} p_{Fe}$$

Bulk viscosity: compression dissipation

Bulk viscosity turns compression energy of density oscillations into heat.

Density vs time for tracers in merger



Tracers (co-moving fluid elements) show dramatic density oscillations especially in the first 5 ms.

Amplitude: up to 50%
Period: ~ 2 ms

- ▶ What is the largest bulk viscosity ζ_{\max} we could expect?
- ▶ What is the equilibration time τ_{ζ} ?
le how long does it take for bulk viscosity to dissipate a good fraction of the energy of a density oscillation?

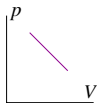
Bulk viscosity: phase lag in system response

Some component in the material is equilibrating slowly.

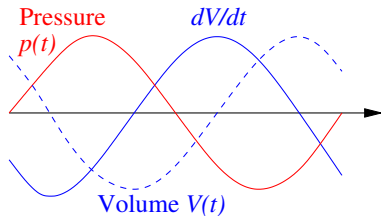
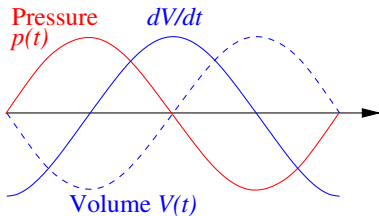
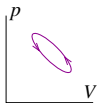
Baryon density n and hence fluid element volume V gets out of phase with applied pressure p :

$$\text{Dissipation} = - \int p dV = - \int p \frac{dV}{dt} dt$$

No phase lag.
Dissipation = 0



Some phase lag.
Dissipation > 0



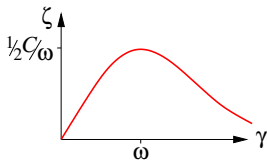
Bulk viscosity: a resonant phenomenon

Bulk viscosity is maximum when

(internal equilibration rate) \sim (freq of density oscillation)

γ ω

$$\zeta = C \frac{\gamma}{\gamma^2 + \omega^2}$$



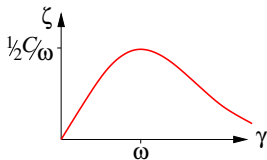
What quantity would equilibrate on the timescale of the density oscillations in neutron star mergers (milliseconds)?

Bulk viscosity: a resonant phenomenon

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What quantity would equilibrate on the timescale of the density oscillations in neutron star mergers (milliseconds)?

Flavor, via weak interactions

Bulk viscosity and flavor equilibration

When you compress nuclear matter, the proton fraction wants to change.

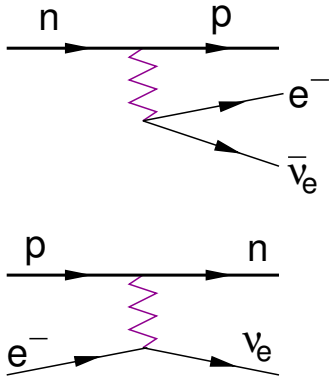
Weak interactions convert $n \leftrightarrow p$

But exactly what is the timescale?

Is it similar to the millisecond timescale of density oscillations in neutron star mergers?

Flavor equilibration processes

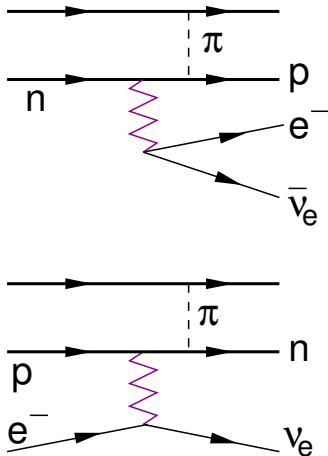
Direct Urca



Only occurs if proton density is high enough: $p_{Fn} < p_{Fe} + p_{Fp}$

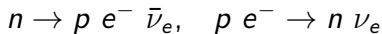
$$\text{Rate } \gamma_D \sim T^4$$

Modified Urca



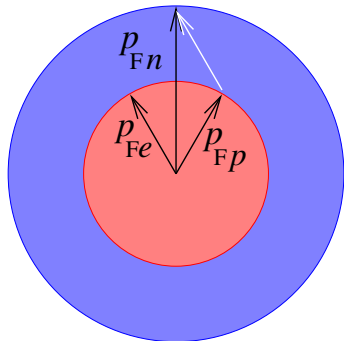
$$\gamma_M \sim T^6$$

When can Direct Urca happen?



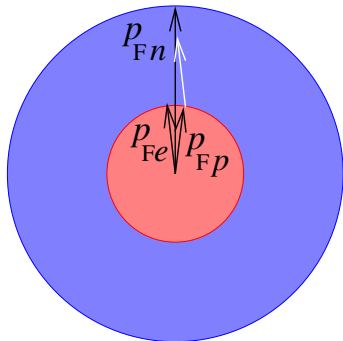
For $T = 0$ and the case of no neutrino trapping ($\mu_\nu = 0$)

High proton fraction:
Direct Urca open



$\vec{p}_n = \vec{p}_p + \vec{p}_e$ is possible
because $p_{Fn} < p_{Fp} + p_{Fe}$

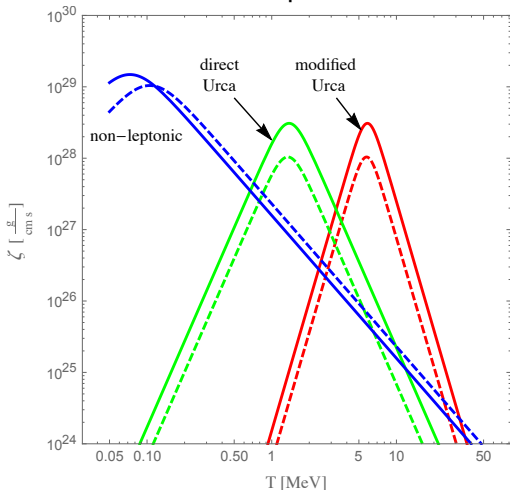
Low proton fraction:
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$\vec{p}_n = \vec{p}_p + \vec{p}_e$ is impossible
because $p_{Fn} > p_{Fp} + p_{Fe}$

Bulk viscosity: resonant peak

For oscillations of freq $\omega = 2\pi \times 1$ kHz



Bulk visc reaches maximum when flavor equilibration rate $\gamma(T) = \omega$.

Direct Urca is faster, so $\gamma_D(T) = \omega$ at $T \sim 1$ MeV
 ζ suppressed at $T \gtrsim 5$ MeV

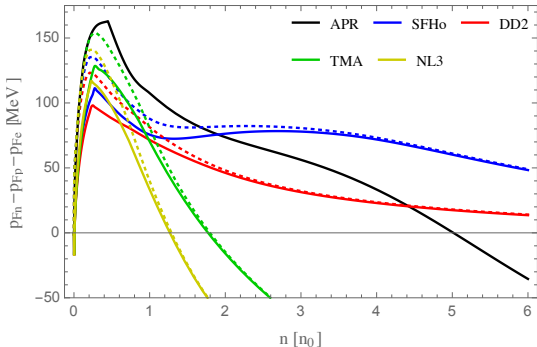
Modified Urca is slower, so $\gamma_M(T) = \omega$ at $T \sim 7$ MeV

ζ_{\max} is determined by EoS, indep of equilibration rate

Typical temperature in first 5ms of post-merger (where density oscillations are large) is 5-20 MeV, so we expect strong bulk viscosity if the Direct Urca channel is suppressed (proton density low).

Does Direct Urca occur?

Direct Urca happens when $\rho_{Fn} < \rho_{Fe} + \rho_{Fp}$
i.e. when $\rho_{Fn} - \rho_{Fe} - \rho_{Fp} < 0$



At $T = 0$, there is no consensus among candidate nuclear matter equations of state about the threshold density for Direct Urca.

Need to consider:

- Thermal effects
- Interaction effects
- Gradual opening of Direct Urca phase space
- Effects of ν_e trapping

The amount of bulk visc dissipation is a probe of the nuclear EoS

Bulk viscosity equilibration time

Density oscillation of amplitude Δn on timescale t_{comp} :

$$n(t) = \bar{n} + \Delta n \cos(2\pi t/t_{\text{comp}})$$

Energy of density oscillation: $\mathcal{E}_{\text{comp}} = \frac{K}{18} \bar{n} \left(\frac{\Delta n}{\bar{n}} \right)^2$

Compression dissipation rate: $W_{\text{comp}} = \frac{2\pi^2 \zeta}{t_{\text{comp}}^2} \left(\frac{\Delta n}{\bar{n}} \right)^2$

Damping Time: $\tau_{\zeta} = \frac{\mathcal{E}_{\text{comp}}}{W_{\text{comp}}} = \frac{K \bar{n} t_{\text{comp}}^2}{36\pi^2 \zeta}$
--

Bulk visc is important if $\tau_{\zeta} \lesssim 10 \text{ ms}$

Is bulk visc big enough to matter?

There are high-amplitude density oscillations with $f \sim 1$ kHz in regions at $T \sim 5$ to 10 MeV

Suppose Direct Urca processes are suppressed at those temperatures and densities.

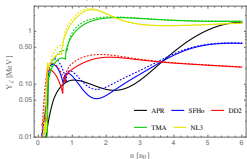
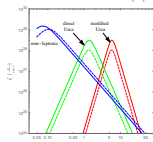
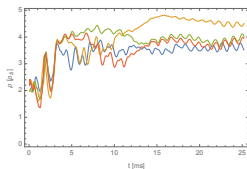
Then flavor equilibration via modified Urca will achieve its maximum value

Max bulk visc from flavor equilibration is

$$\zeta_{\max} = Y_{\zeta} \bar{n} t_{\text{comp}}$$

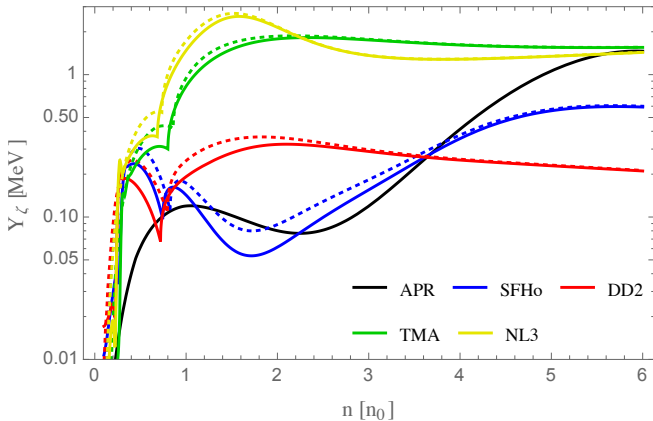
$$\tau_{\zeta}^{\min} = \left(\frac{K}{36\pi^2 Y_{\zeta}} \right) t_{\text{comp}}$$

$$\approx \boxed{3 \text{ ms}} \left(\frac{t_{\text{comp}}}{1 \text{ ms}} \right) \left(\frac{K}{250 \text{ MeV}} \right) \left(\frac{0.25 \text{ MeV}}{Y_{\zeta}} \right)$$

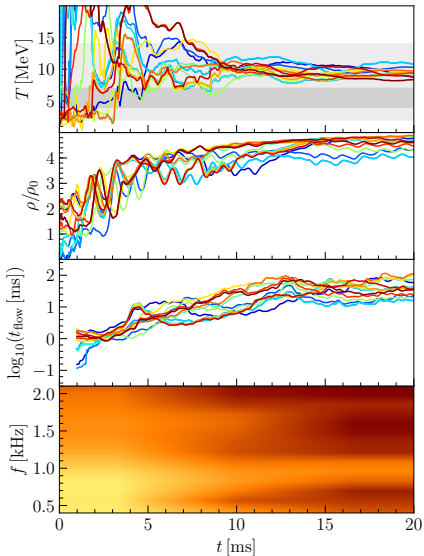


Max bulk visc “Y” factor

Typical value is in the 0.1 to 1 MeV range



State of post-merger matter



Temperature is in the range that maximizes bulk viscosity.
(assuming Modified Urca only)

Large amplitude ~ 1 kHz density oscillations during the first 5-10 ms

Density oscillation freq in kHz range

Summary

It is useful to have estimates of the equilibration times for various forms of dissipation, to decide which is the most important.

- ▶ **Thermal equilibration:** If neutrinos are trapped, and there are short-distance temp gradients then thermal transport might be fast enough to play a role.

$$\tau_{\kappa}^{(\nu)} \approx 700\text{ms} \left(\frac{z_{\text{typ}}}{1\text{ km}}\right)^2 \left(\frac{T}{10\text{ MeV}}\right)^2 \left(\frac{0.1}{x_p}\right)^{1/3} \left(\frac{m_n^*}{0.8 m_n}\right)^3 \left(\frac{\mu_e}{2\mu_\nu}\right)^2$$

- ▶ **Shear viscosity:** similar conclusion.
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The Future

- ▶ Incorporate bulk viscosity in numerical simulations
- ▶ Understand neutrino trapping. At what temp/density is there neutrino domination of thermal and shear viscous transport? Does neutrino trapping affect bulk viscosity?
- ▶ What density and temperature range allows Direct Urca?
- ▶ Are there short-range gradients ($z_{\text{typ}} \sim 0.1 \text{ km}$) that would lead to rapid shear viscous or thermal equilibration?
- ▶ Explore the role of dissipation in the collapse of a single star to a denser “third family” or “twin star” configuration