Normalization states

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Motivation

- At proton colliders such as the LHC, the presence of large uncertainties regarding absolute trigger and production efficiencies implies that only ratios of branching fractions can be measured at a precise level.
- For each $R(X_c)$ measurement, one therefore has to choose a normalization channel whose yield will be measured together with the signal channel under consideration to determine such a ratio.
- In the case of 3-prong $\tau \rightarrow 3\pi v_{\tau}$ we measure e.g.

$$K(D^*) = \frac{Br(B^0 \to D^*\tau\nu)}{Br(B^0 \to D^*3\pi)} = \frac{N_{\text{sig}}}{N_{\text{norm}}} \times \frac{\varepsilon_{\text{norm}}}{\varepsilon_{\text{sig}}},$$

• and get $R(D^*) = K(D^*) \times Br(B^0 \rightarrow D^*3\pi)/Br(B^0 \rightarrow D^*\mu\nu)$.

The ideal normalization channel

[Disclaimer: 3-prong measurements from now on]

- its final state is exactly the same as the signal channel
- its production dynamics and decay kinematics are the same as the signal channel
- 3. its absolute branching fraction is known with an uncertainty negligible with respect to other sources.

In practice...

- $B^0 \rightarrow D^{*-}\tau^+\nu_{\tau}$: the decay channel $B^0 \rightarrow D^{*-}\pi^+\pi^-\pi^+$ matches criteria 1 and 3 but only partially criterion 2, since the two extra neutrinos present in the signal final state affect (slightly) trigger and selection efficiencies.
- $B_c \rightarrow J/\psi \ \tau^+ \nu_\tau$: the $B_c \rightarrow J/\psi \ \pi^+ \pi^- \pi^+$ channel matches criteria 1 (fully) and 2 (partially), but it does not match at all criterion 3, since its branching fraction is unknown.
 - Normalizing to $B_c \rightarrow J/\psi \ \mu^+ \nu_{\mu}$ would violate criterion 1 and 2 (to some extent)
- Similar situation for D⁰, D⁻, D_s⁻, Λ_c^{-} : branching fractions are known at a precision level above 10%

Summary of measurements

Channel	Branching fraction	Notes
$B^0 \rightarrow D^{*} 3\pi$	(7.21 ± 0.29) 10 ⁻³	Dominated by Babar measurement
$B^0 \rightarrow D^-3\pi$	$(6.0 \pm 0.7) \ 10^{-3}$	CLEO 1992 + PDG fit
$B^+ \rightarrow D^0 3\pi$	(5.7 ± 2.2) 10 ⁻³	CLEO 1992 + PDG fit
$B_s \rightarrow D_s 3\pi$	(6.1 ± 1.0) 10 ⁻³	CDF + PDG fit. Measured relative to $B^0 \rightarrow D^-3\pi$
$\Lambda_b \rightarrow \Lambda_c 3\pi$	(7.7 ± 1.1) 10 ⁻³	 CDF, relative to Λ_cπ. The uncertainty on the latter is dominated by 2 LHCb measurements, both dominated by knowledge of f_{baryon}/f_d and 1. BR(B⁰→D⁻π⁺) 2. Obtained using the branching fraction of Λ+_c→pK⁻π⁺ decay.
$B_c \rightarrow J/\psi 3\pi$	seen	

Badly needed measurements of B mesons could be easily done at Belle-II / Belle /Babar!

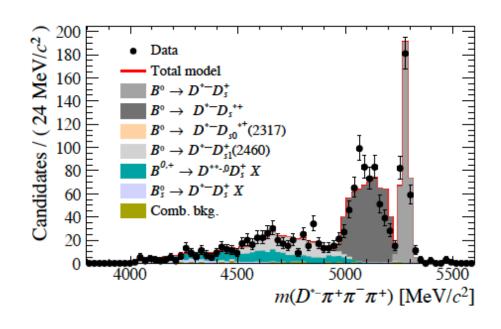
In the baryon (and B_c) sectors we are (and will) be dominated by the knowledge of the hadronization fractions

Other normalization channels?

- Final states of the type $X_b \rightarrow X_c D_s$ are particularly interesting as normalization channels
 - In addition to the same topology as signal, they also have the same detached vertex topology, therefore uncertainties due to trigger and selection efficiencies will drop out in the K(X_c) measurement

Is it worth the effort?

- LHCb 3-prong R(D*)
- B \rightarrow D*D_s(\rightarrow 3 π)X control sample
- All analysis cuts
- ~300 candidates on Run1
- Cf. 1300 signal candidates
- ...but statistical errors are similar (~6%)



- Alternatively:
 - take $D_s \rightarrow KK\pi$ decays
 - 5x more candidates
- But: different final state!

Summary of $X_b \rightarrow X_c D_s$ decays

Channel	Branching fraction	Notes
$B^0 \rightarrow D^* - D_s$	$(8.0 \pm 1.1) \ 10^{-3}$	Babar + CLEO
$B^0 \rightarrow D^-D_s$	$(7.2 \pm 0.8) \ 10^{-3}$	Dominated by BELLE 2007
$B^+ \rightarrow D^0 D_s$	(9.0 ± 0.9) 10 ⁻³	Babar + CLEO. LHCb uses B^0 → D^-D_s
$B_s \rightarrow D_s D_s$	(4.4 ± 0.5) 10 ⁻⁴	BELLE on Y(5S). LHCb uses $B^0 \rightarrow D^-D_s$
$\Lambda_b \rightarrow \Lambda_c D_s$	$(1.1 \pm 0.1) \ 10^{-3}$	LHCb uses $B^0 \rightarrow D^-D_s$ and measured $Br(\Lambda_b \rightarrow \Lambda_c^+\pi^-)/Br(B^0 \rightarrow D^+\pi^-)$
$B_c \rightarrow J/\psi D_s$	seen	ATLAS+LHCb: 3.1± 0.5 relative to $B_c \rightarrow J/\psi \pi$

Measurements of B mesons could be easily done at Belle-II / Belle /Babar

In the baryon (and B_c) sectors we are (and will) be dominated by the knowledge of the hadronization fractions

Mixed approach?

• Combine theoretical predictions with experimental measurements, e.g.

$$R(\Lambda_c) = \frac{Br(\Lambda_b \to \Lambda_c \tau \nu)}{Br(\Lambda_b \to \Lambda_c \mu \nu)} = \frac{N(\Lambda_b \to \Lambda_c \tau \nu)}{N(\Lambda_b \to \Lambda_c 3\pi)} * \frac{N(\Lambda_b \to \Lambda_c 3\pi)}{N(B^0 \to D^{*-} 3\pi)} * \frac{Br(B^0 \to D^{*-} 3\pi)}{Br(B^0 \to D^{*-} \mu \nu)} * \frac{1}{Th}$$

$$Th = \operatorname{Br}(\Lambda_b^{\ 0} \to \Lambda_c^- \mu^+ \nu_\mu) / \operatorname{Br}(B^0 \to D^{*-} \mu^+ \nu_\mu),$$

- The first two ratios can be experimentally determined with a percent precision in LHCb because they involve channels with the same final state or the same trigger configuration. The third one is measured at B factories and Belle-2.
- Uncertainties due to the limited knowledge of the Λ_b production fractions or the Λ_b branching fractions in any observable state completely cancel in these ratios.

Meinel, semi-tauonic WS, Apr 2016

Another ratio, useful as a normalization factor in the LHCb measurement of $\Lambda_b \to \Lambda_c \tau \bar{\nu}_{\tau}$:

$$R = rac{\Gamma(\Lambda_b^0 o \Lambda_c^+ \, \mu^- ar{
u}_\mu)}{\Gamma(ar{B}^0 o D^+ \mu^- ar{
u}_\mu)}$$

Input	R
DLM+HPQCD	2.47 ± 0.26
DLM + Fermilab / MILC	2.30 ± 0.23
DLM+Fermilab/MILC+BaBar	2.45 ± 0.19
DLM + Fermilab / MILC + BaBar + Belle	2.37 ± 0.16

- [W. Detmold, C. Lehner, S. Meinel, PRD 92, 034503 (2015)]
- [J. A. Bailey et al., PRD 92, 034506 (2015)]
- [H. Na et al., PRD 92, 054510 (2015)]
- [B. Aubert et al. (BaBar), PRL 104, 011802 (2010)]
- [R. Glattauer et al. (Belle), PRD 93, 032006 (2016)]
- [C. DeTar, private communication]

Homework

- Estimate the precision level which can be reached in the approaches mentioned above to select the optimum normalization strategy,
 - This can involve two or more normalization channels per measurement.
- Measure the normalization channels at the most appropriate facility (B factories, LHCb or Belle-2).
- In addition to branching fractions, a full kinematic study allows to determine the impact on systematic uncertainties related to the imperfect cancellation of trigger and selection efficiencies between signal and normalization