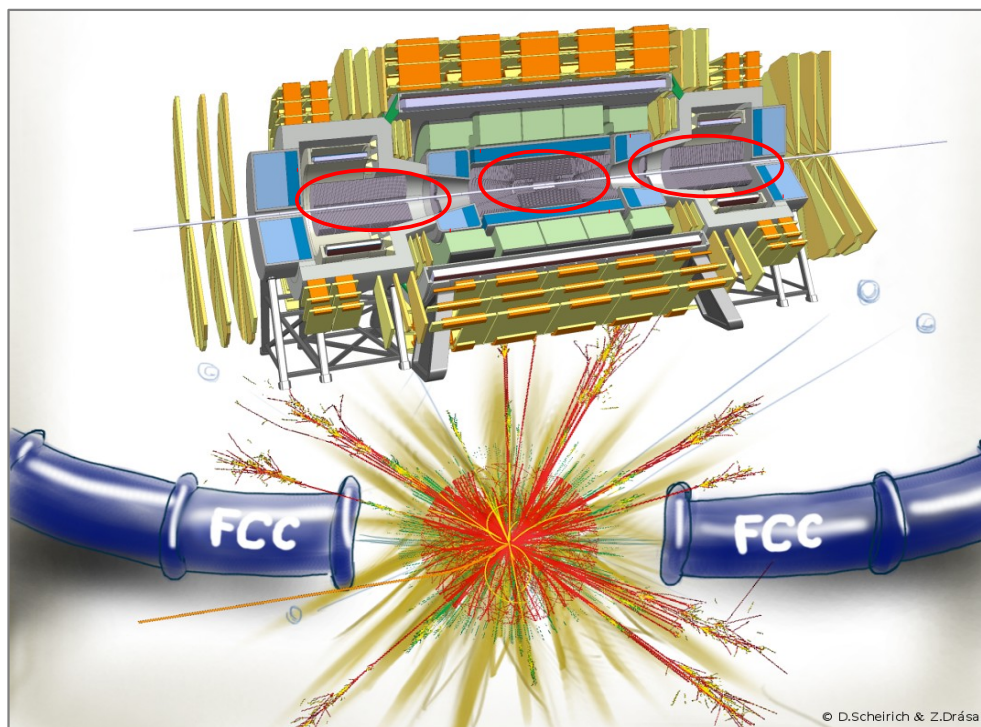


# FCC-hh: Pile-up & PU Mitigation Studies



Zbyněk Drásal  
CERN



# Overview

- Pile-up numbers: HL-LHC versus FCC-hh
- Effective pile-up rate & primary vertexing
  - Comparison CMS versus FCC v4.01
  - Effect of luminous region size
- Summary & Plans

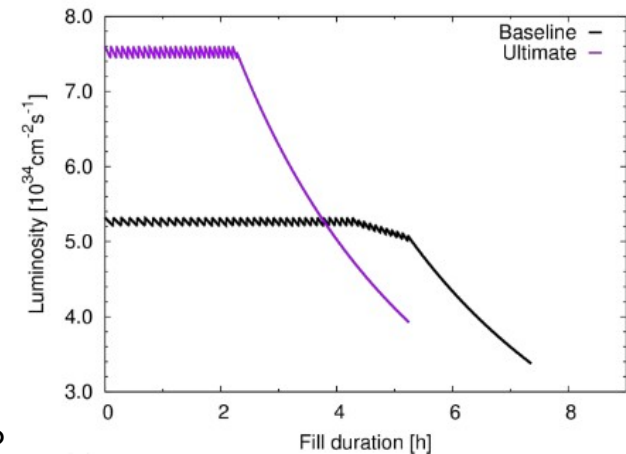
# Pile-up Numbers: HL-LHC

- How to estimate pile-up limits for FCC-hh?

→ numbers from G.Arduini's ECFA talk on HL-LHC luminous region

$$\langle \mu \rangle = \frac{\sigma_{inel} \cdot L}{n_B \cdot f_r}$$

- $\sigma_{inel} \sim 85\text{mb @ } 14\text{TeV HL-LHC}$
- **Tunnel length** = 26.659 km
- $n_B = 2748 \rightarrow$  N bunches (2808 for LHC)
- **Bunches fill-up factor**  $f_{up} = 2748/3554 \sim 77.3\%$
- $f_r = 11.245\text{kHz} \rightarrow$  revolution frequency (nominal LHC)
- **Baseline Luminosity** (levelled) =  $5.3 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- **Ultimate Luminosity** (levelled) =  $7.6 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$



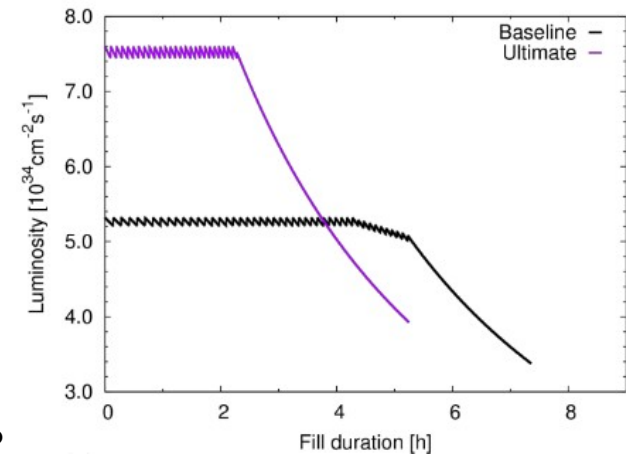
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- **Luminosity variations** between bunches  $\pm 8\%$  (see e.g. [ATL-PHYS-PUB-2013-014](#))
- **Pile-up:  $\mu$  is Poisson distributed** → quantify **limits** by 95% confidence interval ( $\sigma \sim 1.96\sqrt{N}$ )

→ **HL-LHC Baseline:**  $\langle \mu \rangle = (146 \pm 12) \pm 25$

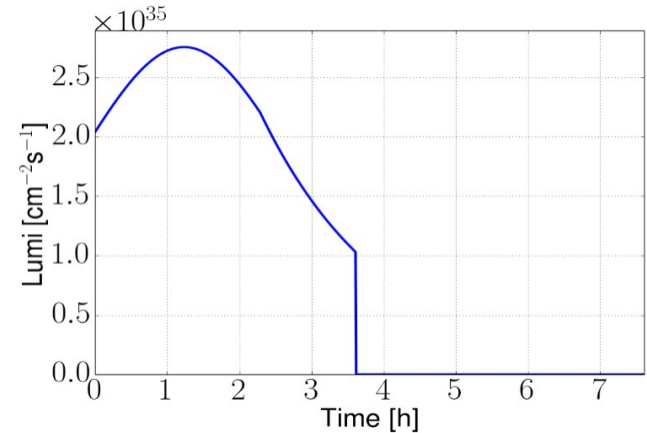
with  $\sigma_{inel} \sim 81\text{mb}$  (TOTEM),  $n_b \sim 2808$ ,  $L \sim 5 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$  →  $\langle \mu \rangle = [(128 \pm 10) \pm 23]$

→ **HL-LHC Ultimate:**  $\langle \mu \rangle = (209 \pm 17) \pm 29$  (with  $\sigma_{inel} \sim 81\text{mb}$  etc. →  $\langle \mu \rangle = [(184 \pm 15) \pm 28]$ )

# Pile-up Numbers: FCC-hh

- How to estimate pile-up limits for FCC-hh?

→ numbers extrapolated (plot from D.Schulte's talk at FCC Week)



$$\langle \mu \rangle = \frac{\sigma_{inel} \cdot L}{n_B \cdot f_r}$$

- $\sigma_{inel} \sim 108\text{mb}$  @ 100TeV FCC-hh
- **Tunnel length** = 97.500 km
- $n_B = 10050$  (using  $f_{up}$  factor)
- $f_r = 3.075\text{kHz}$  (assuming FCC tunnel)
- **Ultimate Luminosity**  $\sim 30 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- **Levelled luminosity (assuming loss in int. L  $\sim 20\%$ )**  $= 15 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$

– Assume the same luminosity variations between bunches  $\pm 8\%$

– **Pile-up Poisson distr.:** quantify **limits** by 95% confidence interval ( $\sigma \sim 1.96\sqrt{N}$ )

→ **FCC-hh Ultimate:**  $\langle \mu \rangle = [(1048 \pm 84) \pm 66] \rightarrow \text{Max } O(1200), \text{ Avg } \sim O(1000)$

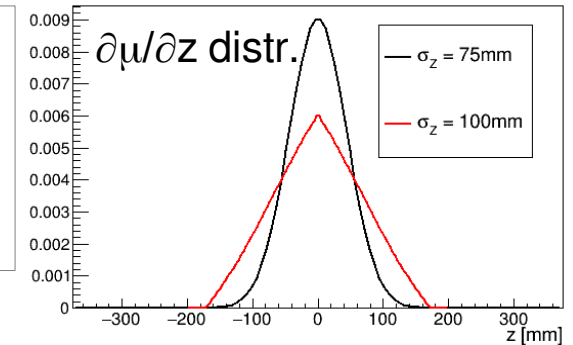
→ **FCC-hh Levelled:**  $\langle \mu \rangle = [(524 \pm 42) \pm 47] \rightarrow \text{Max } O(600)$

# Vertexing @ PU=1000 & Timing Information

- How the pile-up (PU)~1000 degrades primary vertexing? Does the timing info help?
  - Dependent on scenario for luminous region (Gauss, “rectangular”,...) → simulate **1000 PU** vertices according to Gaussian (HL-LHC) Line & Time PU densities (c.f.: [PhysRevSTAB.17.111001](#))

- Gauss. bunch:**  $\frac{1}{\sqrt{2\pi}\sigma_z} e^{-\frac{1}{2}\left(\frac{z}{\sigma_z}\right)^2}$ 
  - **Line PU:**  $\frac{\sqrt{1+\phi^2}}{\sqrt{\pi}\sigma_z} e^{-(1+\phi^2)\left(\frac{z}{\sigma_z}\right)^2}$
  - **Time PU:**  $\frac{\sqrt{1+\psi^2}}{\sqrt{\pi}\sigma_z} e^{-(1+\psi^2)\left(\frac{ct}{\sigma_z}\right)^2}$

Line PU distr.: gaussian versus rectangular shaped bunches



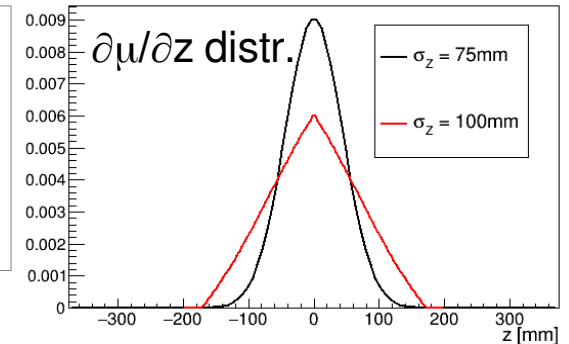
Piwinsky angle  $\Phi \sim 0.67$   
 Time Piw. angle  $\Psi \sim 0.40$   
 Luminous reg.  $\sim 44\text{mm}$

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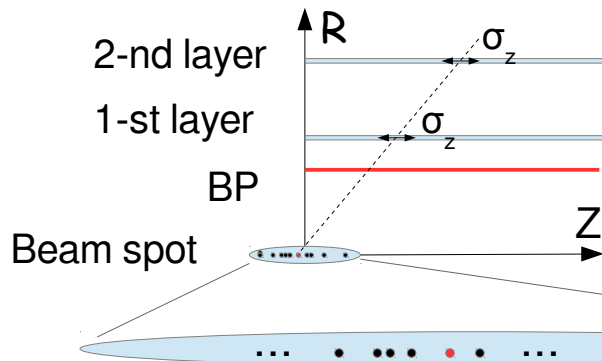
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- Study what fraction of tracks may be unambiguously assigned to the primary vertex @ 95% CL? Use 2D info (PV assumed to be “precisely” found from e.g. high  $p_T$  tracks)



**$\delta z_0$  &  $\delta t_0$  play the crucial role!**

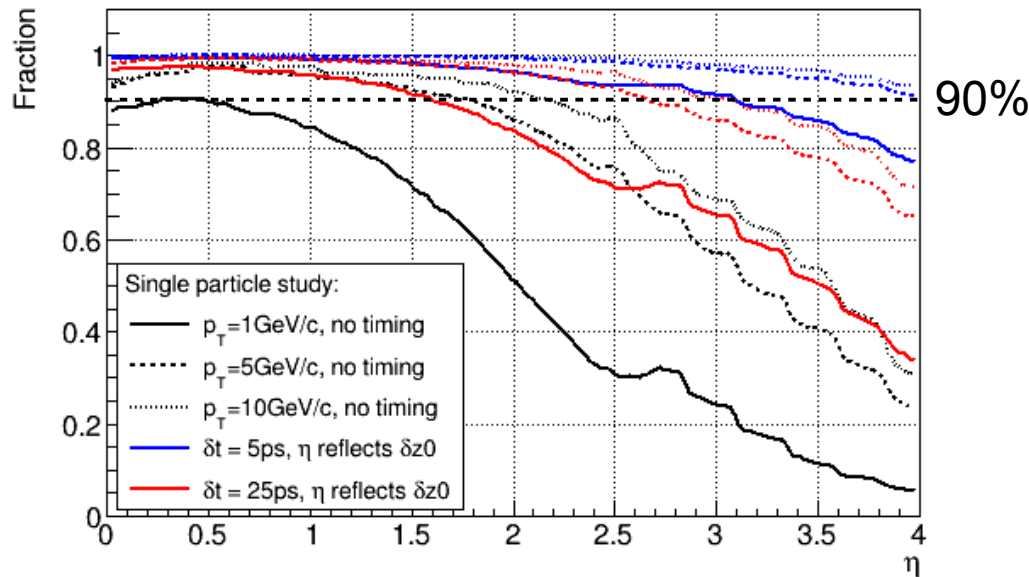
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# CMS Ph2: Effective PU Rate @ PU=140

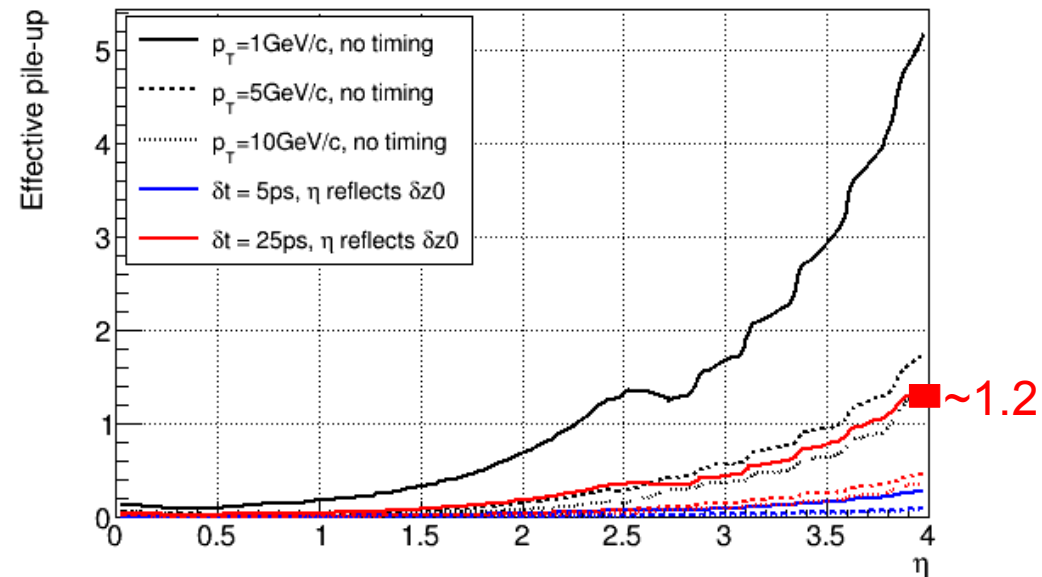
- Compare FCC-hh to HL-LHC conditions (PU~140), using e.g. CMS Ph2 upgrade layout

## HL-LHC scenario @ PU=140 CMS Ph2 Upgr. tracker

Fraction of tracks being unambiguously assigned to prim. vertex @95% CL:  $\sigma_z^{\text{Gauss}}=75\text{mm}$ ,  $\langle\mu_{\text{tot}}\rangle=140$



Effective pile-up confusing prim. vertexing @95% CL:  $\sigma_z^{\text{Gauss}}=75\text{mm}$ ,  $\langle\mu_{\text{tot}}\rangle=140$



### Comment:

- Error on TOF  $\sim 1.5 - 3\text{ps}$  ( $\eta$  dependent)  $\rightarrow$  negligible wrt 25ps (hence, not included into calculations)

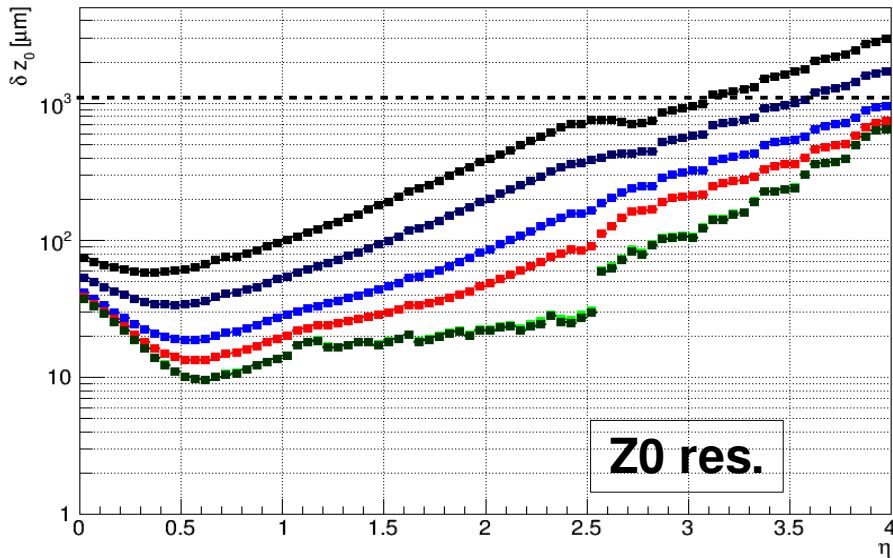


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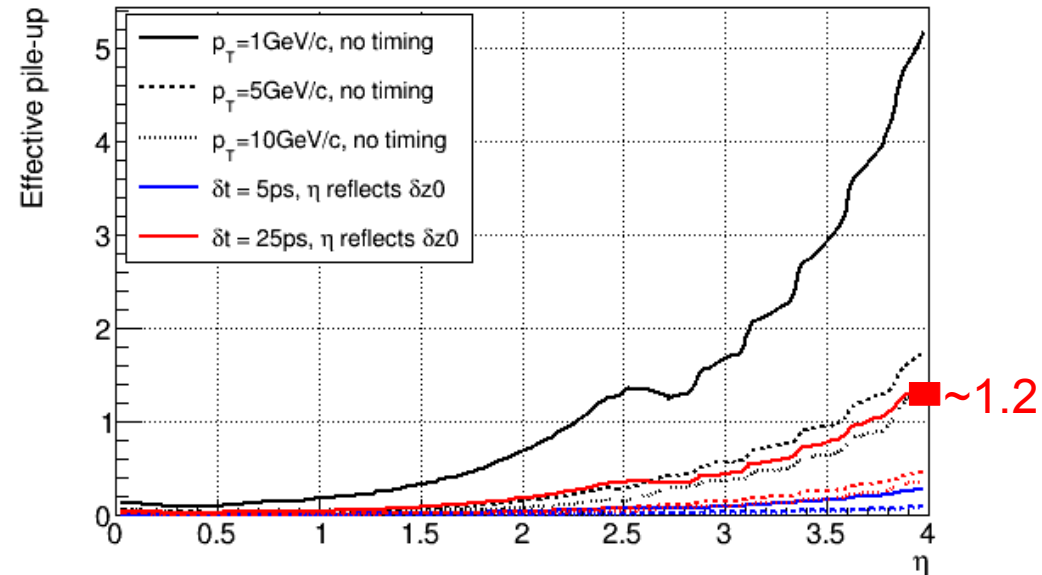
- Why such a shape of effective PU rate? Mostly driven by **z0 res.**

## HL-LHC scenario @ PU=140 CMS Ph2 Upgr. tracker

Longitudinal impact parameter error - const  $P_T$  across  $\eta$



Effective pile-up confusing prim. vertexing @95% CL:  $\sigma_z^{\text{Gauss}}=75\text{mm}$ ,  $\langle\mu_{\text{tot}}\rangle=140$

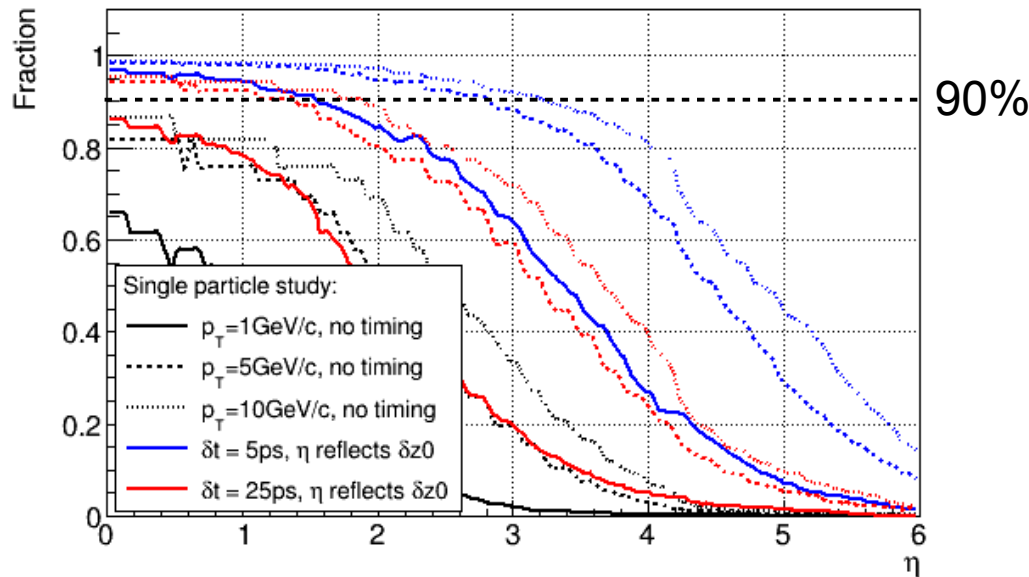


# FCC v4.01: Effective PU Rate @ PU=1000

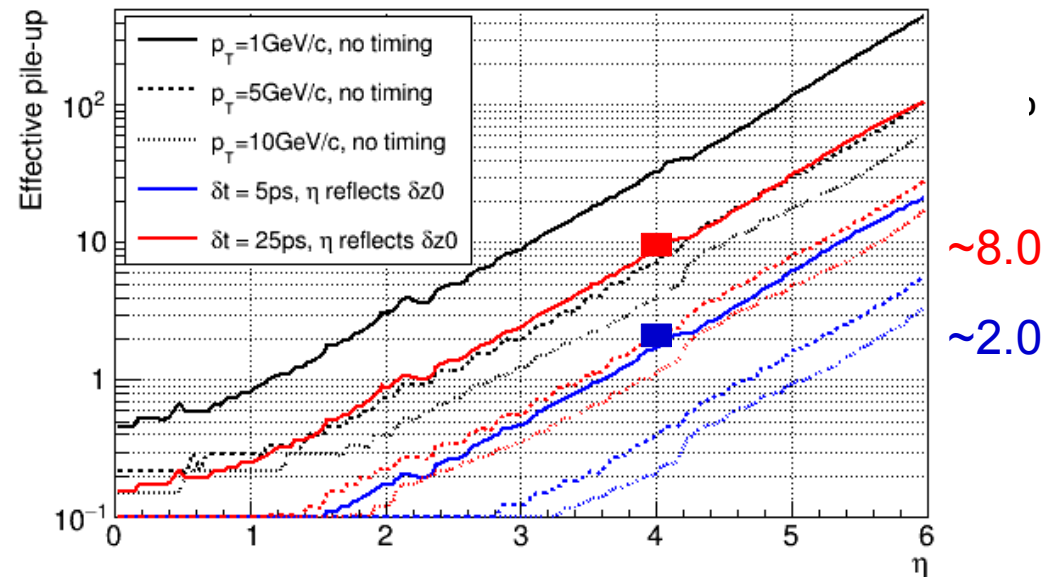
- Compared to FCC-hh (PU~1000)?

**FCC-hh scenario @ PU=1000**  
**Tilted layout**

Fraction of tracks being unambiguously assigned to prim. vertex @95% CL:  $\sigma_z^{\text{Gauss}}=75\text{mm}$ ,  $\langle\mu_{\text{tot}}\rangle=1000$



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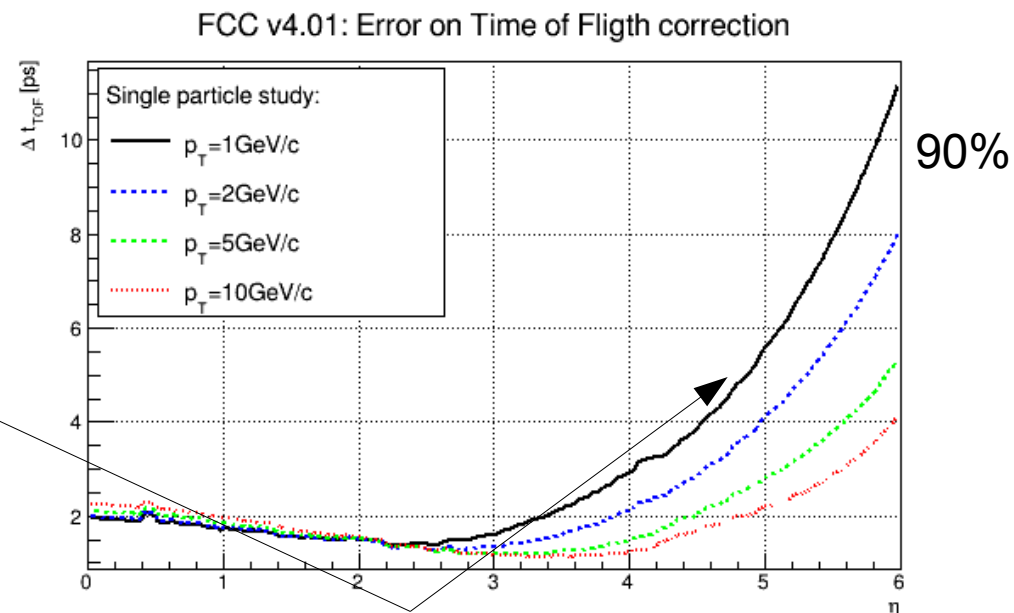
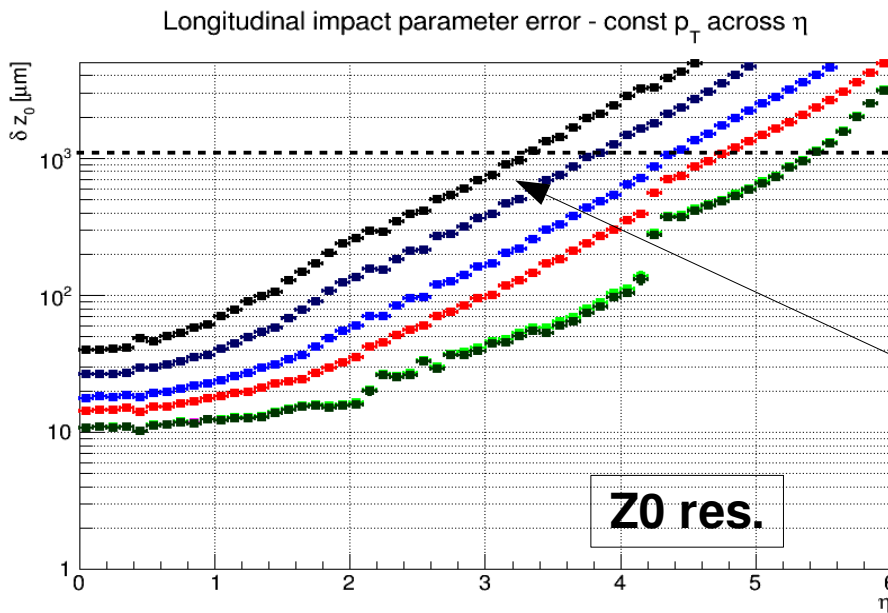
**Comment:** Not taken into account non-negligible error on time of flight correction (see other slide)

**Conclusion:** 2D vertexing (time & z) essential, but may not be sufficient to mitigate PU effect (even up-to  $\eta=4.0$ , unless  $\delta t_0 \sim 5\text{ps}$  assumed)!

# FCC v4.01: Effective PU Rate @ PU=1000

- What is the effect of TOF correction?

**FCC-hh scenario @ PU=1000**  
**Tilted layout**



**Error on TOF correction mostly due to z0 res.**

→ Non-negligible effect if one aims for  $t_0$  res.  $\sim 10$ ps (Remember: time must be propagated along track to vertex position) → **Several timing layers necessary to mitigate the error on TOF!**

# Pile-Up Mitigation

- How one can possibly mitigate the PU?
  - Improve vertexing performance:
    - **t0 res.** → hard, at the technology limits
    - **z0 res.** → hard, limited by beam-pipe material, namely at high eta → crossing @ shallow angle

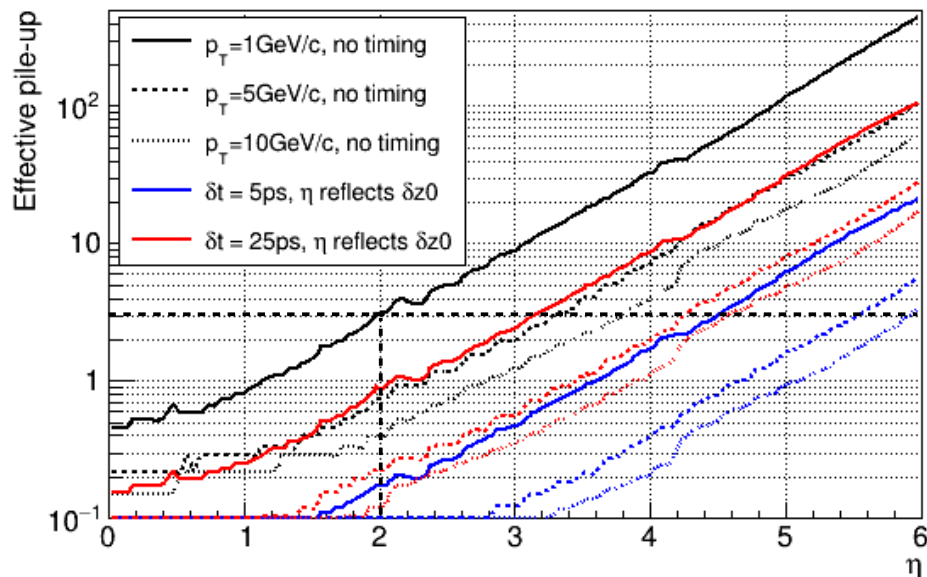
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  - **Extend luminous region** → PU vertices better separated in space & time, does it help? How much?

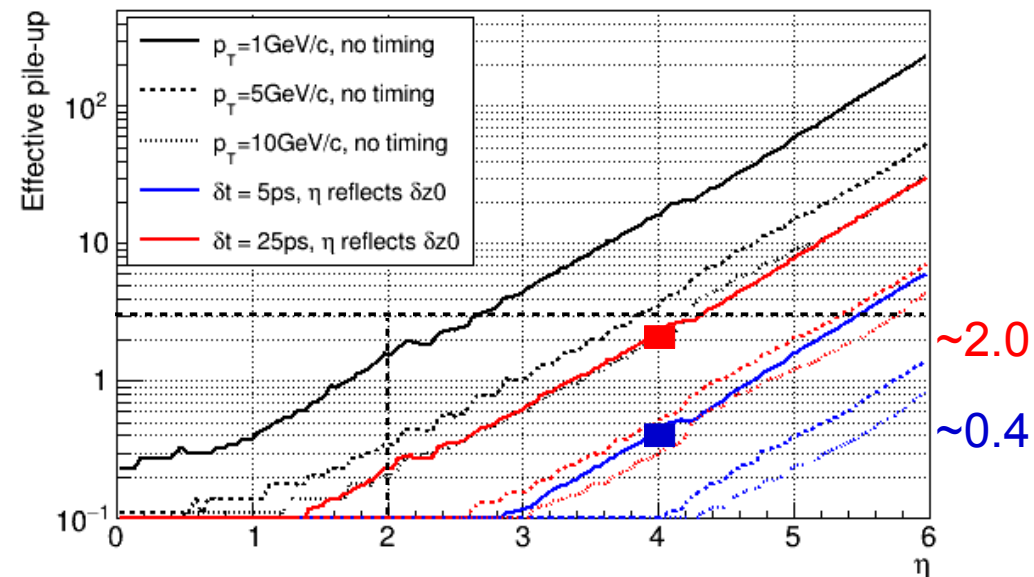
# Effect of Luminous Region Size on Effective PU

- Studied Gaussian distributed PU densities with bunch  $\sigma_z = 75\text{mm}$  versus  $150\text{mm}$ 
  - Does extension of luminous region decreases effective PU rate? **By how much?**
  - Lum. region size:  $\sigma_{\text{lum.region } z} \sim \sigma_z / \sqrt{2}$

Effective pile-up confusing prim. vertexing @95% CL:  $\sigma_z^{\text{Gauss}} = 75\text{mm}$ ,  $\langle \mu_{\text{tot}} \rangle = 1000$



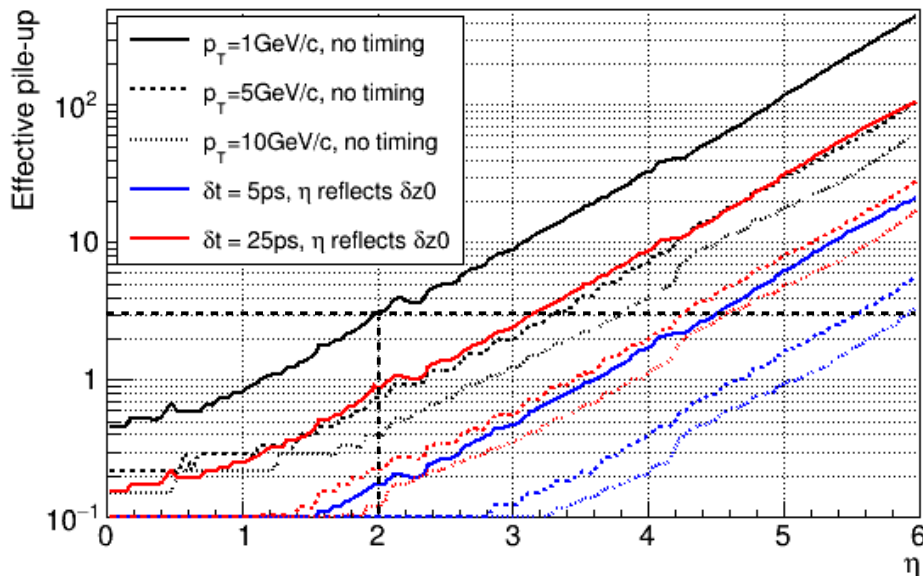
Effective pile-up confusing prim. vertexing @95% CL:  $\sigma_z^{\text{Gauss}} = 150\text{mm}$ ,  $\langle \mu_{\text{tot}} \rangle = 1000$



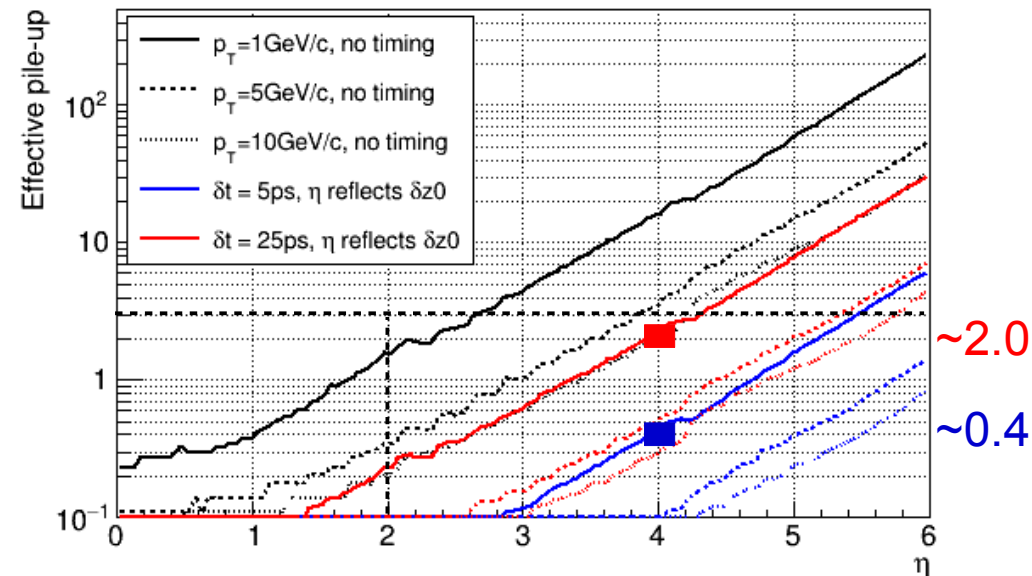
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Effective pile-up confusing prim. vertexing @95% CL:  $\sigma_z^{\text{Gauss}} = 150\text{mm}$ ,  $\langle \mu_{\text{tot}} \rangle = 1000$



→ Effective PU rate decreases by the same factor **f** as one increases  $\sigma_z$  if **z0 information used only**, **by  $f^2$  if both t0 & z0 used** (unless time & line PU correlated)!

# Summary & Plans

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  - Effective pile-up rate seems manageable only up-to  $\eta \sim 4$ , but just by using 2D vertexing (time & z). In addition, extreme timing res.  $\sim 5$ ps has to be assumed, **hence several timing layers necessary**
  - **Effective PU may be significantly decreased by increasing size of luminous region**, increase in size by factor **f** results in **a quadratic decrease ( $1/f^2$ ) in effective PU**, if **both timing & spatial information is being used**

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- **Plans:**
  - Study different PU scenarios (ultimate versus levelled)
  - To get more realistic estimates on effective PU & comparable plots to full simulations, convolve pT curves with min bias  $dpt/d\eta$  distr. & study 1 real physics case (e.g.  $Z' \rightarrow \mu\mu, t\bar{t}$ )
  - To understand the effect of size of luminous region on effective PU, several scenarios need to be modelled:
    - Gaussian versus rectangular shape of bunches
    - Different bunch sizes (75mm as a reference, 120mm as a current limit & 200mm as an ultimate limit)