

# Modern reanalysis of the reactor anomaly conversion method

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Leendert Hayen

SSP, Aachen, June 11th 2018

IKS, KU Leuven, Belgium



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# Introduction

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# Anomaly Introduction

What's it about in 3 steps:

**Where** is the anomaly?

Antineutrino's from  $\beta^-$  decay of reactor fission fragments



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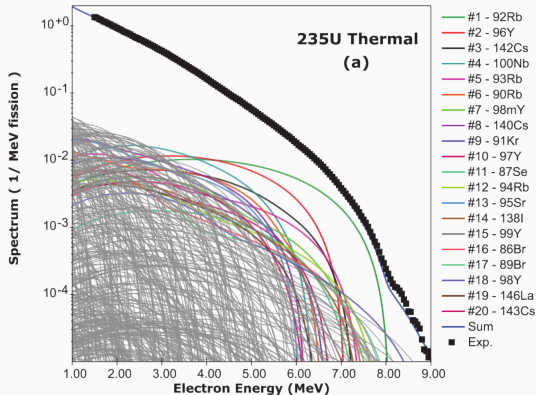
**How** should we interpret this?

Prediction error (mean,  $\sigma$ ) or sterile neutrino's, something else

When new physics lurks, look out for quirks!

# Antineutrino origin

Fission fragments from  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$  and  $^{241}\text{Pu}$  have many  $\beta^-$  branches, but can only measure **cumulative** spectrum.

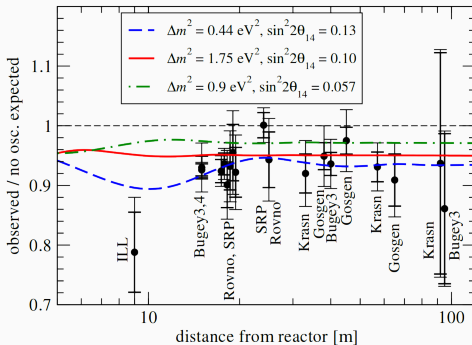


Conversion of all  $\beta$  branches is **tremendous** challenge

A. A. Sonzogni *et al.*, PRC **91** (2015) 011301(R)

# Deficiency and particle physics proposal

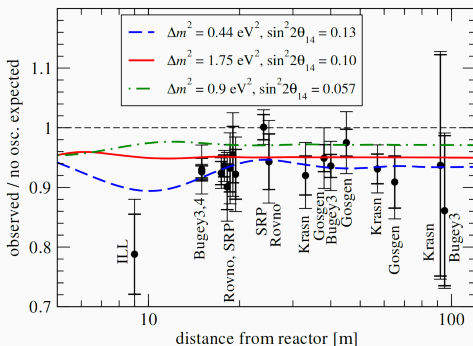
Current deficiency in neutrino count rate at 94% (2-3 $\sigma$ )



Very exciting, but... it is real?

# Deficiency and particle physics proposal

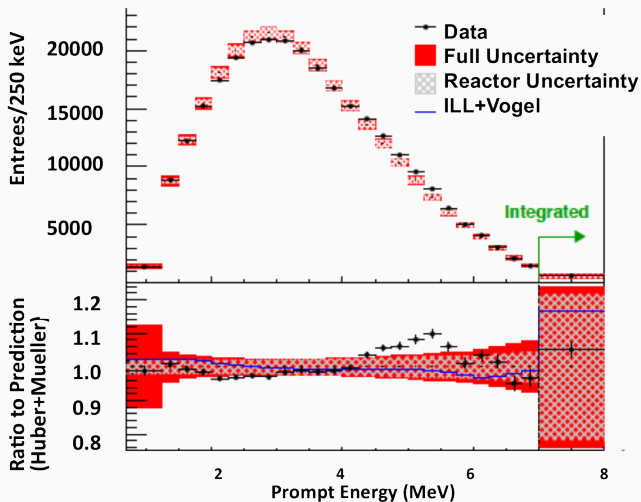
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Very exciting, but... it is real?

Understanding of all corrections & nuclear structure is **crucial!**

# Reactor bump



Something not understood, most likely **nuclear physics** problem

## **(Very) Short Baseline Experiments**

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Anomaly from 2011, bump from 2015(ish), what happened?

Anomaly from 2011, bump from 2015(ish), what happened?

### **Short baseline**

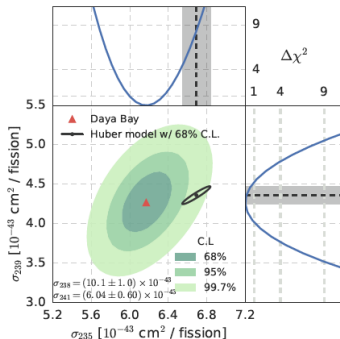
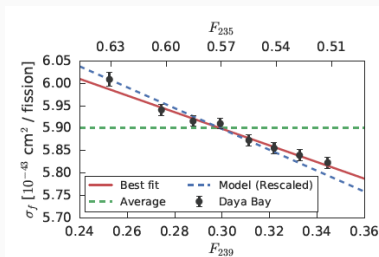
- Daya Bay
- Double Chooz
- RENO

Performing wonderfully, BUT anomaly & bump still with us

# Short baseline experiments

## New developments

Fuel dependence on measured count rate

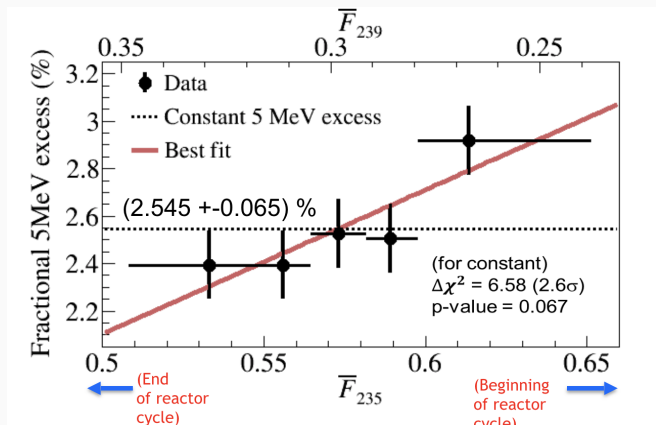


Usual Huber-Mueller model cannot reproduce correct slope!

**Confirmed by RENO**

## Short baseline experiments

RENO claims possible  $^{235}\text{U}$  dependence (I. Yu, Neutrino 2018)



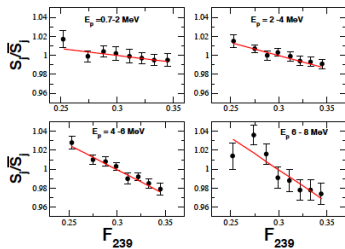
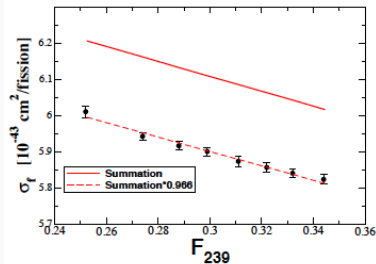
Interesting result, see how data evolves

## Short baseline experiments

Usual comparison to Huber-Mueller model, **however**

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Usual comparison to Huber-Mueller model, **however**



Database approach reproduces slope, but still allows for an anomaly

Uncertainties for summation are, will have to wait for experiment

## Very short baseline experiments

Since 2011, ~ 10 experiments started setting up

Several experiments came online late 2017/2018! Published data from

- DANNS (Russia) 1804.04046
- STEREO (France) 1806.02096
- PROSPECT (USA) 1806.02784
- NEOS (Korea) 1610.05134

Very exciting & more coming soon!

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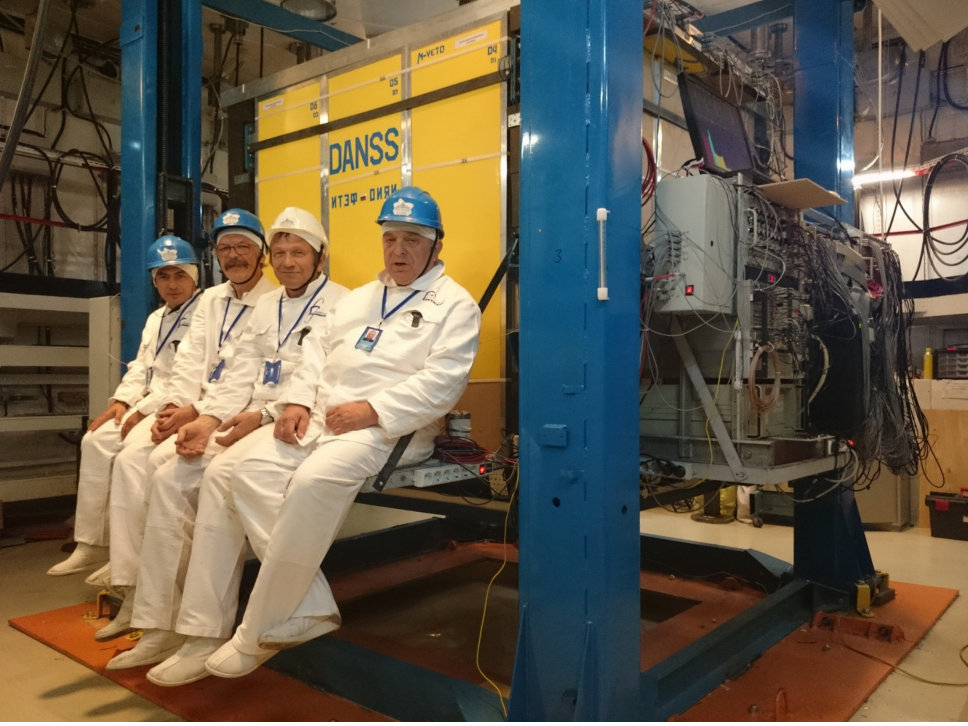
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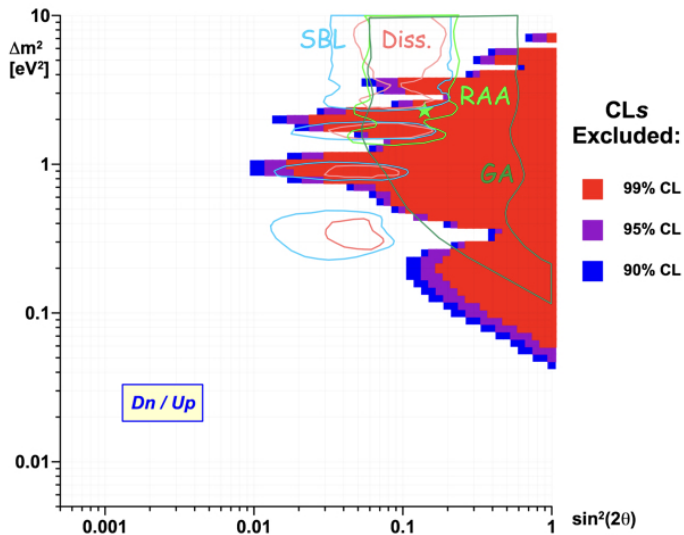
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Many results @ Neutrino 2018  $\rightarrow$  unceremoniously stole slides from V. Egorov, J. Lamblin, T. Langford & Y. Oh

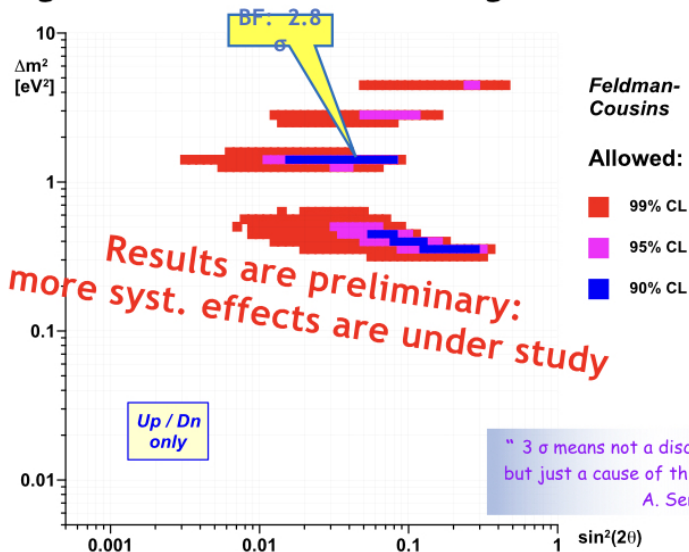
**Very grateful!**



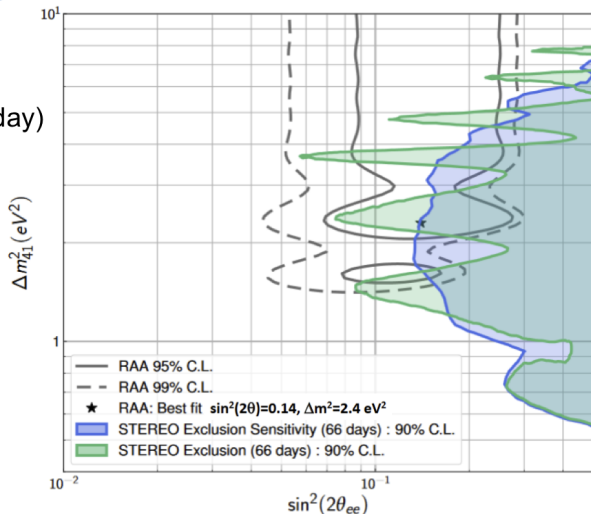




## Significance of the best regions



- 66 days ON ( $396 \pm 4 \bar{\nu}_e$  / day)
- Raster scan approach
- Generate pseudo-experiments to estimate the  $\Delta\chi^2$  pdf
- arXiv:1806.02096



→ Best fit value of the RAA rejected at 97.5% C.L.

Assembly in 30s (video)

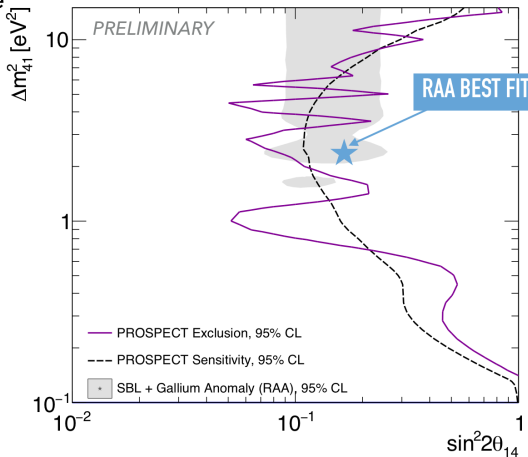
ASSEMBLY OF FIRST ROW



NOVEMBER 1, 2017  
YALE WRIGHT LAB

## OSCILLATION SEARCH RESULTS

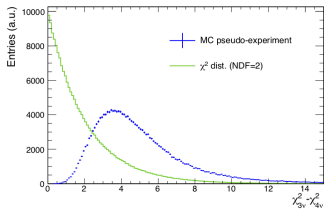
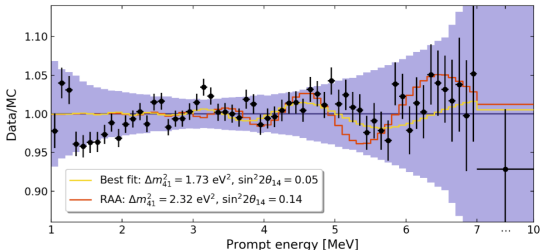
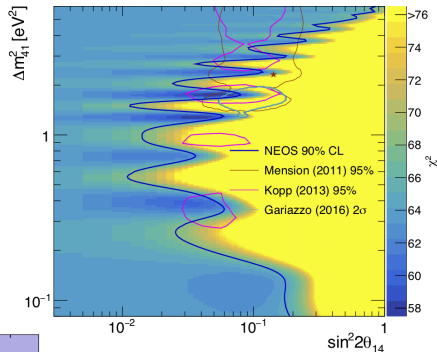
- ▶ Feldman-Cousins based confidence intervals for oscillation search
- ▶ Covariance matrices captures all uncertainties and energy/baseline correlations
- ▶ Critical  $\chi^2$  map generated from toy MC using full covariance matrix
- ▶ 95% exclusion curve based on 33 days Reactor On operation
- ▶ *Direct test of the Reactor Antineutrino Anomaly*



**Disfavors RAA best-fit point at >95% ( $2.3\sigma$ )**

# Active-to-sterile oscillation

- Normalized with the Daya Bay shape
- Best fits at:  
 $(1.73 \text{ eV}^2, 0.05)$ ,  $(1.30 \text{ eV}^2, 0.04)$   
 with  $\chi^2(3\nu) - \chi^2(4\nu) = 6.5$ ,  
 $p\text{-value} = 0.22$
- Fine structures in reactor  $\nu$  spectrum  
 or oscillation?



Great progress from all experiments

Several experiments are taking data

Best Reactor anomaly fit ( $\Delta m_{41}^2, \sin^2 \theta_{4e}$ ) excluded with  $\geq 3\sigma$  by several experiments

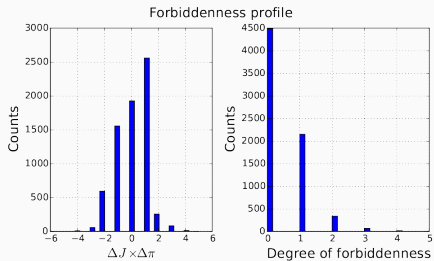
**Talk by C. Giunti**



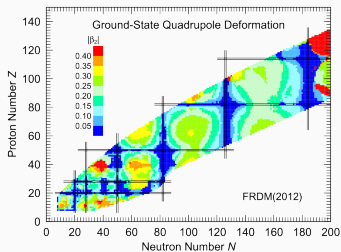
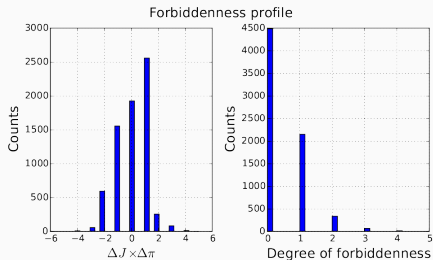
# Reactor anomaly analysis

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## Nuclear $\beta$ decay is complicated

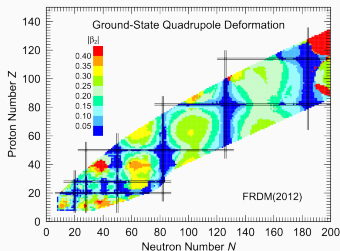
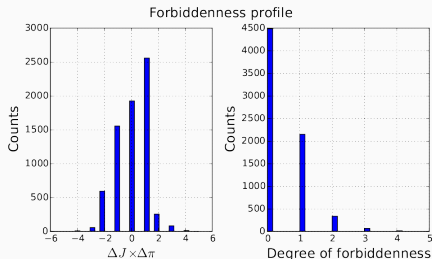


Nuclear  $\beta$  decay is complicated



Both greatly influence the spectrum shape!

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**Additional** lower order effects: Atomic, electrostatic, kinematic. . .

L.H. *et al.*, Rev. Mod. Phys. 90 (2018) 015008

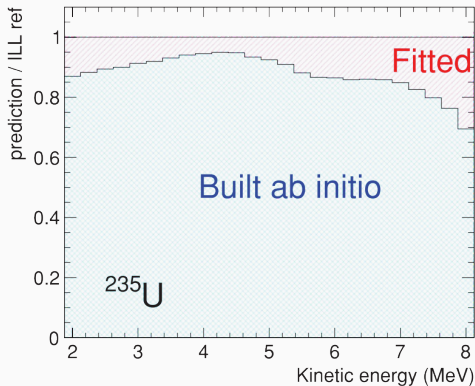
Approaches split up in 2:

1. **Huber** method: virtual  $\beta$  branch fits

# State of the art

Approaches split up in 2:

1. **Huber** method: virtual  $\beta$  branch fits
2. **Summation** method: Build from databases & extrapolate a la #1



Much of *ab initio* is based on same spectral assumptions

# Extrapolation & Virtual branches

## Current methods have many issues:

- Estimated average  $b/Ac$  from spherical mirrors, but highly transition and deformation dependent
- Incorrectly estimates  $(\alpha Z)^{n>1}$  effects,  $\text{RNA}(\langle Z \rangle^{n>1}) \neq \langle \text{RNA}(Z^{N>1}) \rangle!$
- Fixed endpoints on grid
- $^{239}\text{Pu}/^{235}\text{U}$  is wrong
- Only allowed transitions (dominant  $0^+ \leftrightarrow 0^-$  transitions)
- Quenching of  $g_A$  is absent
- ...

Predictions are **dubious**

An *et al.* (Daya Bay Collab.), PRL 118 (2017) 251801 & Hayes *et al.*,  
arXiv:1707.07728

## Forbidden transitions

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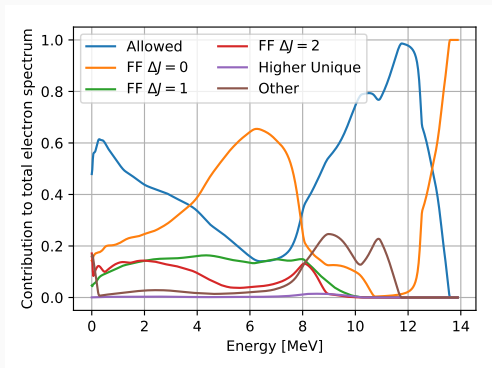


## Forbidden shape factors

Roughly  $\sim 30\%$  of 8000 transitions are forbidden, usually assumed of negligible importance

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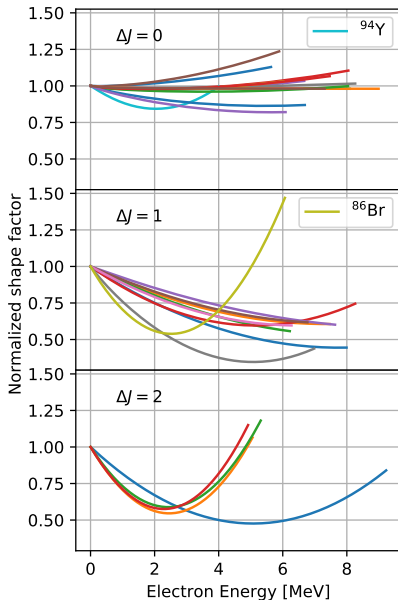
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Experimental region of interest (2-8 MeV) is **dominated** by forbidden decays

# Forbidden shape factors

Picked 29 dominant forbidden transitions, calculated shape factor in nuclear shell model



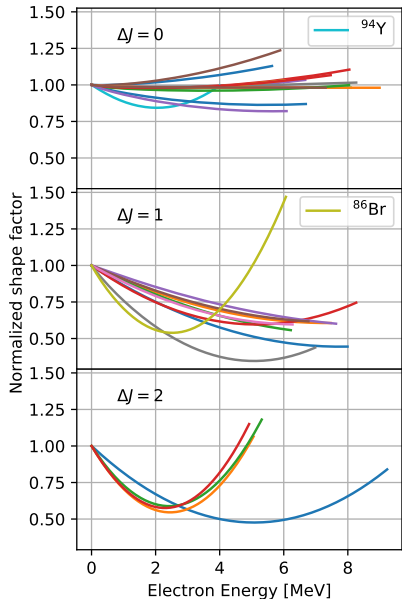
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$$\frac{dN}{dE} \propto pE(E_0 - E)^2 F(Z, E)$$
$$C(Z, E)$$

Allowed:  $C = 1$

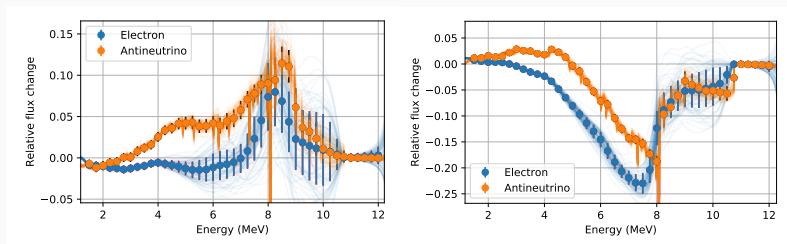
As expected,  
large spectral changes



# Forbidden spectral changes

Uniform behaviour for each  $\Delta J$  allows for parametrisation  
→ Use Monte Carlo for correction of **all** forbidden decays

Look at difference in cumulative spectrum shapes



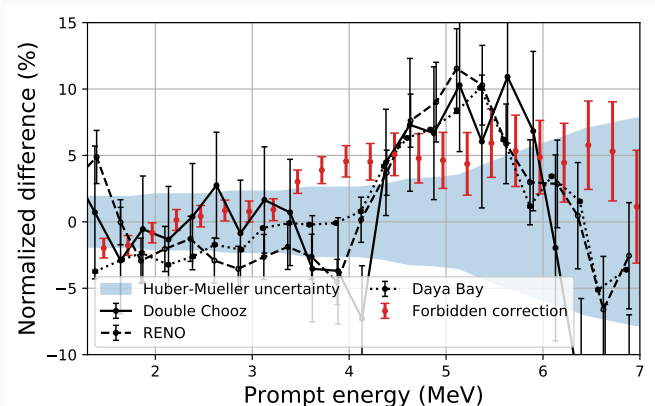
Allowed

Unique

Large spectral changes, downward trend  $\sim 5\%$  wrt Unique  
Monte Carlo allows for uncertainty estimation

# Forbidden transitions & the bump

Use spectrum changes with Schreckenbach correspondence



Bump **strongly mitigated**, still further research

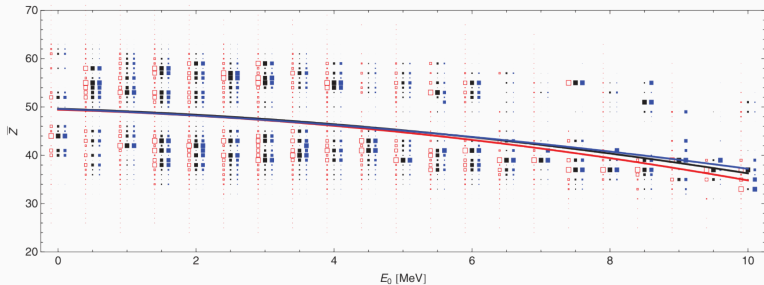
arXiv: 1805.12259, submitted to PRL

# Modern conversion analysis

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# Extrapolation & Virtual branches

How to construct these fictitious  $\beta$  branches?



Parametrised  $\bar{Z}(E_0)$  fit with simple polynomial

P. Huber, PRC **84** (2011) 024617



# Extrapolation & Virtual branches

Typical procedure

1. Make grid for  $E_0$  in  $[2, 12]$  MeV
2. Every gridpoint  $E_{0,i}$ , choose  $Z(E_{0,i})$
3. Assume allowed shape, extrapolate average nuclear matrix elements
4. Fit VB intensities to cumulative exp. spectrum

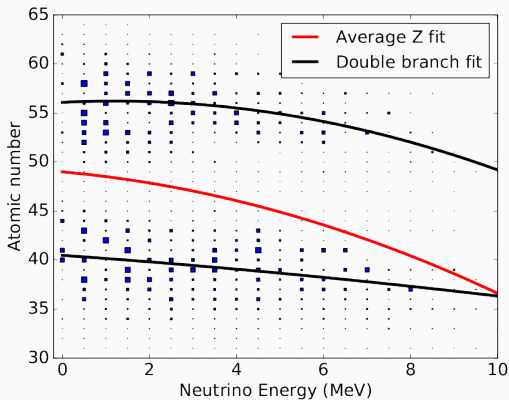
$$S(E_e) = \sum_i c_i S(E_e, \bar{Z}(E_{0,i}), E_{0,i})$$

5. Invert spectra using  $E_\nu = E_0 - E_e$

# Database extrapolation

Database contains much more information to use

Trivial extension  
to improve  
 $(\alpha Z)^2$  behaviour,  
fixed weights

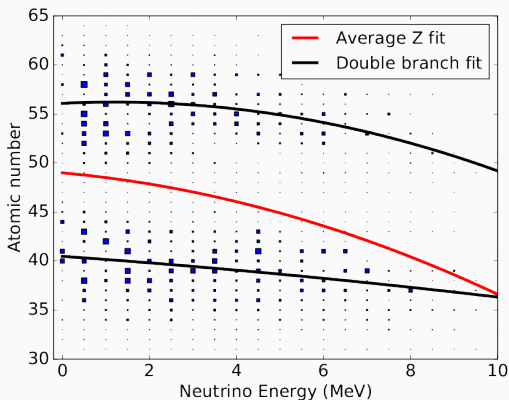


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Employ  
Machine Learning  
clustering  
algorithms to find  
better patterns



Nuclear  $\beta$  decays live in high-dimensional vector spaces

- $Z, A$
- Log  $ft$  values
- Branching Ratio,  $E_0$ , daughter excitation
- $\Delta J^{\Delta\pi}$  (forbiddenness, unique)
- Initial and final deformation
- ...

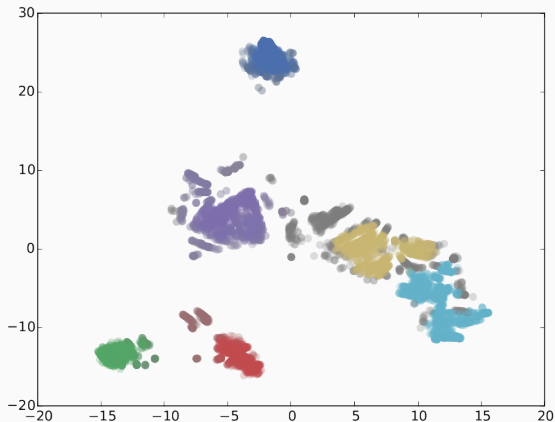
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Clusters in high dimensions are smeared in 2D projections

# Clustering visualisation

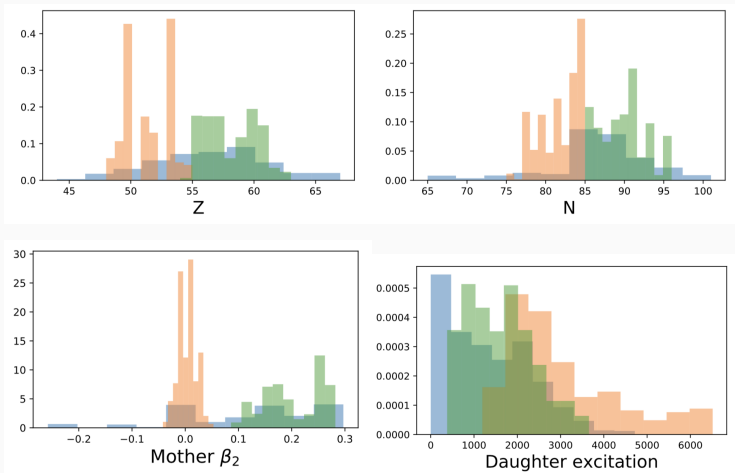
Use dimensional reduction (t-SNE) to visualise results



Clear clusters, intercluster distance irrelevant here

# Intercluster comparison

## Example comparison for 3 clusters



Large differences visible for simple histograms!

How to combine these results?

Instead of a single  $Z(E_0)$  fit, use

Multidimensional Cluster Markov Chain Monte Carlo (MC<sup>3</sup>)



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Multidimensional Cluster Markov Chain Monte Carlo (MC<sup>3</sup>)

Build a **distribution** of anomaly → better uncertainty estimate

## Virtual $\beta$ branch creation

### Procedure:

For each  $E_0$  bin, for each cluster, build sampling distribution

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Modification of prior allows for compensation/study of  
pandemonium

## MC<sup>3</sup> moving forward

Clusters contain nuclear structure information, can stochastically deduce matrix element corrections

Also relevant for *ab initio* approach!

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Done correctly, *realistic uncertainty & anomaly* including correlations

## Summary

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- Data coming in from VSBL

Expect results soon!

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Proper treatment of forbidden corrections is **essential**, can mitigate bump, trends towards anomaly removal

Nuclear  $\beta$  decays live in high-dimensional clusters, combine with Monte Carlo for proper anomaly determination