

# EFT parameterization for VBS

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**SMEFT** = Effective Field Theory with SM fields + symmetries

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$$

$$\mathcal{L}_n = \sum_i C_i Q_i^{d=n}$$

$C_i$  - free parameters ( Wilson coefficients )

$Q_i$  - gauge invariant operators that form a complete basis


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 any UV compatible with the SM in the low energy limit can be matched onto the SMEFT

 a convenient phenomenological approach: systematically classifies all the possible new physics signals

 allows to compute with no reference to the UV

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$$\mathcal{L}_n = \sum_i C_i \mathcal{Q}_i^{d=n}$$

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$\mathcal{Q}_i$  - gauge invariant operators that form a complete basis

We consider B, L conservation and only first order deviations → only  $\mathcal{L}_6$

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \mathcal{L}_6$$

$$\mathcal{L}_6 = \sum_i C_i \mathcal{Q}_i$$

there are 59 operators = 76 (2499) real parameters for 1 (3) generation(s)

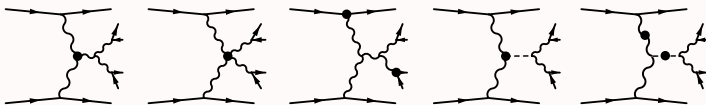
$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
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$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
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$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
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$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^m]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		

# Which operators are relevant for VBS?

## 1. Identify all the terms that can contribute

- (a) corrections to SM diagrams : TGC / QGC,  $hVV$ ,  $Vff$ ,  $\delta\Gamma_{Z,W,h}$ ,  $\delta m_W$ , (  $gqq$  )



- (b) BSM vertices that give new diagrams :  $VVff$ ,  $Vhff$ ,  $ffff$  ...



## 2. Verify which are phenomenologically relevant. Depends on:

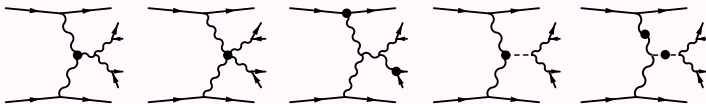
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Gzadkowski, Iskrzynski, Misiak, Rosiek 1008.4884

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$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

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$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^k)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jkmn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^m]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^m]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		

# Summary - most general case

## Corrections to SM couplings/propagators

Vff ( $\rightarrow \Gamma_W, \Gamma_Z$ )	$Q_{HD} Q_{HWB} Q_{II} Q_{HI}^3 Q_{HI}^1 Q_{Hq}^3 Q_{Hq}^1 Q_{He} Q_{Hu} Q_{Hd} Q_{Hud}$
Vff (dipole)	$Q_{eW} Q_{eB} Q_{uW} Q_{dB} Q_{dW} Q_{dB} (Q_{uG}, Q_{dG})$
TGC/QGC	$Q_{HD} Q_{HWB} Q_{II} Q_{HI}^3 Q_W Q_{\tilde{W}} Q_{H\tilde{W}B}$
hVV	$Q_{HD} Q_{HWB} Q_{II} Q_{HI}^3 Q_{HW} Q_{H\tilde{W}} Q_{HB} Q_{H\tilde{B}} Q_{H\tilde{W}B} Q_{H\Box}$
$m_W$	$Q_{HD} Q_{HWB} Q_{HI}^3 Q_{II}$
$\Gamma_h$	$Q_{HD} Q_{II} Q_{HI}^3 Q_{eH} Q_{dH} Q_{uH} Q_{H\Box}$

## Couplings giving new diagrams

VVff	$Q_{eW} Q_{eB} Q_{uW} Q_{dB} Q_{dW} Q_{dB} Q_{II}$
Vhff	$Q_{HI}^3 Q_{HI}^1 Q_{Hq}^3 Q_{Hq}^1 Q_{He} Q_{Hu} Q_{Hd} Q_{Hud}$
4-fermions	...

28 (30) operators and **254 (290)** parameters counting phases and flavor indices

+ four-fermion operators!

# Reducing the set – symmetries

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{\varphi}$	$(\varphi^{\dagger} \varphi)^3$	$Q_{e\varphi}$	$(\varphi^{\dagger} \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{\varphi \square}$	$(\varphi^{\dagger} \varphi) \square (\varphi^{\dagger} \varphi)$	$Q_{u\varphi}$	$(\varphi^{\dagger} \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$	$Q_{\varphi D}$	$(\varphi^{\dagger} D^{\mu} \varphi)^* (\varphi^{\dagger} D_{\mu} \varphi)$	$Q_{d\varphi}$	$(\varphi^{\dagger} \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^{\dagger} \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{l}_p \gamma^{\mu} l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^{\dagger} \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu}^I \varphi)(\bar{l}_p \tau^I \gamma^{\mu} l_r)$
$Q_{\varphi W}$	$\varphi^{\dagger} \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{e}_p \gamma^{\mu} e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^{\dagger} \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{q}_p \gamma^{\mu} q_r)$
$Q_{\varphi B}$	$\varphi^{\dagger} \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu}^I \varphi)(\bar{q}_p \tau^I \gamma^{\mu} q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^{\dagger} \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{u}_p \gamma^{\mu} u_r)$
$Q_{\varphi WB}$	$\varphi^{\dagger} \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{d}_p \gamma^{\mu} d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^{\dagger} \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^{\dagger} D_{\mu} \varphi)(\bar{u}_p \gamma^{\mu} d_r)$

# Reducing the set – symmetries

Assume CP conservation

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
		$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
		$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
		$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
		$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
		$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

# Reducing the set – symmetries

Assume CP conservation + approx.  $U(3)^5$  flavor sym

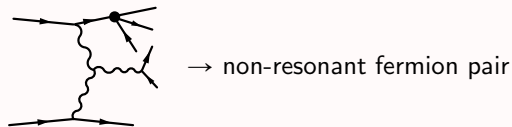
$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$		
		$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi) \Box (\varphi^\dagger \varphi)$		
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$		
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$			$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{l}_p \gamma^\mu l_r)$
				$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi) (\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$			$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{e}_p \gamma^\mu e_r)$
				$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$			$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi) (\bar{q}_p \tau^I \gamma^\mu q_r)$
				$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$			$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{d}_p \gamma^\mu d_r)$



# Reducing the set – selection cuts

Cuts can help removing (new) diagrams.

Examples:



4-fermion operators (apart from  $Q_{II}$ ) and new diagrams are likely to be negligible in resonant VBS



Simulation studies required to make solid statements

# Reducing the set – complementary constraints

Ideal statement: “the operator  $XX$  is very constrained from another measurement, so it can be neglected”

it's OK to use this argument to reduce the parameter set (for now)

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suppose I have a theory that produces  $(D^\mu W_{\mu\nu}^i)(i\Phi^\dagger \overleftrightarrow{D}^{i\nu} \Phi)$   
 $\Rightarrow$  deviations in processes with TGC/QGC

In the Warsaw basis it corresponds to a combination of  $C_{H\Box}$ ,  $C_{Hq}^{(3)}$ ,  $C_{HI}^{(3)}$ ,  $C_H$  + others

$$(D^\mu W_{\mu\nu}^i)(i\Phi^\dagger \overleftrightarrow{D}^{i\nu} \Phi) = g \left( 2\Phi^\dagger \Phi (D_\mu \Phi^\dagger D^\mu \Phi) + \frac{Q_{H\Box}}{2} + \frac{Q_{Hq}^{(3)} + Q_{HI}^{(3)}}{2} \right)$$

Grzadkowski et al:  $(\varphi^\dagger \varphi) [(D_\mu \varphi)^\dagger (D^\mu \varphi)] \stackrel{(5.1)}{=} \frac{1}{2} (\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi) + \boxed{\psi^2 \varphi^3} + \boxed{\varphi^6} + m^2 \boxed{\varphi^4} + \boxed{E}$ .

LEP measurements tell  $C_{Hq}^{(3)}, C_{HI}^{(3)} \ll 1 \rightarrow$  I remove them from the fit  
 $\rightarrow$  no parameter left to account for the deviation in processes with TGC/QGC!

# Reducing the set – complementary constraints

Ideal statement: “the operator  $XX$  is very constrained from another measurement, so it can be neglected”

it's OK to use this argument to reduce the parameter set (for now)

**My skepticism:** this statement is basis dependent as the EFT is *not* intuitive

---

What this means:

- ▶ the operators in a basis don't capture only new physics contributing directly to them, but also to other invariants that were removed from the basis
- ▶ their physical interpretation is not obvious! ( $\sim$  no control on the structures that were removed)
- ▶ to my knowledge it is not possible to select a basis that “minimizes” this
- ▶ reducing the parameter set “intuitively” is ok as long as there is no deviation. If anything appears it is necessary to include *all* to interpret it correctly

# Operators relevant for VBS - minimal set

imposing CP +  $U(3)^5$  flavor symmetry, neglecting contributions  $\propto y_f$ ,  $f \neq b, t$   
and assuming non-standard diagrams give negligible impact

## Corrections to SM couplings/propagators

$\mathcal{Q}_{HD} = (H^\dagger D_\mu H)^*(H^\dagger D^\mu H)$	● ● ● ●	$\mathcal{Q}_{Hl}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{l}\gamma^\mu l)$	●
$\mathcal{Q}_{H\Box} = (H^\dagger H)(H^\dagger \Box H)$	●	$\mathcal{Q}_{Hl}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^i H)(\bar{l}\sigma^i \gamma^\mu l)$	● ● ● ●
$\mathcal{Q}_W = \varepsilon_{ijk} W_{\mu\nu}^i W^{j\nu\rho} W_\rho^{k\mu}$	●	$\mathcal{Q}_{Hq}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{q}\gamma^\mu q)$	●
$\mathcal{Q}_{HB} = (H^\dagger H)B_{\mu\nu}B^{\mu\nu}$	●	$\mathcal{Q}_{Hq}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^i H)(\bar{q}\sigma^i \gamma^\mu q)$	●
$\mathcal{Q}_{HW} = (H^\dagger H)W_{\mu\nu}^i W^{i\mu\nu}$	●	$\mathcal{Q}_{He} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{e}\gamma^\mu e)$	●
$\mathcal{Q}_{HWB} = (H^\dagger \sigma^i H)W_{\mu\nu}^i B^{\mu\nu}$	● ● ● ●	$\mathcal{Q}_{Hu} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}\gamma^\mu u)$	●
$\mathcal{Q}_{ll} = (\bar{l}\gamma_\mu l)(\bar{l}\gamma^\mu l)$	● ● ●	$\mathcal{Q}_{Hd} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{d}\gamma^\mu d)$	●

● = Vff ( $\Gamma_{W,Z}$ )   
 ● = TGC/QGC   
 ● = hVV ( $\Gamma_h$ )   
 ● =  $m_W$

14 operators and **14** parameters

# HEFT = Non-linear EFT = EW chiral Lagrangian

Main idea: the Higgs does not need to be in a doublet

$h$

treated as a singlet  
with arbitrary couplings

$$\mathcal{F}(h) = 1 + 2a\frac{h}{b} + b\frac{h^2}{v^2} + \dots$$
$$H = \frac{v+h}{\sqrt{2}} \mathbf{U} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

independent

$\mathbf{U} = e^{i\pi^l \sigma^l / v}$

adimensional  
↓  
derivative expansion  $\sim \chi$ PT

→ a **very general** EFT



contains the linear as a particular limit

→ matches composite Higgs models + other UVs with significant nonlinear effects in the EWSB sector

# HEFT operators for VBS - minimal set

restricting to CP +  $U(3)^5$  and neglecting 4-fermion interactions

29 operators

$$\mathcal{P}_C = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \mathcal{F}_C$$

$$\mathcal{P}_B = B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B$$

$$\mathcal{P}_1 = B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \mathcal{F}_1$$

$$\mathcal{P}_3 = \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3$$

$$\mathcal{P}_5 = \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5$$

$$\mathcal{P}_{11} = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}$$

$$\mathcal{P}_{13} = i \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}$$

$$\mathcal{P}_{17} = \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}$$

$$\mathcal{P}_{23} = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}$$

$$\mathcal{P}_{26} = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}$$

$$\mathcal{N}_1^{\mathcal{Q}} = i \bar{Q}_L \gamma_\mu \mathbf{V}^\mu Q_L \mathcal{F}$$

$$\mathcal{N}_5^{\mathcal{Q}} = i \bar{Q}_L \gamma_\mu \{ \mathbf{V}^\mu, \mathbf{T} \} Q_L \mathcal{F}$$

$$\mathcal{N}_7^{\mathcal{Q}} = i \bar{Q}_L \gamma_\mu \mathbf{T} \mathbf{V}^\mu \mathbf{T} Q_L \mathcal{F}$$

$$\mathcal{N}_2^\ell = i \bar{L}_R \gamma_\mu \mathbf{U}^\dagger \{ \mathbf{V}^\mu, \mathbf{T} \} \mathbf{U} L_R \mathcal{F}$$

$$R_2^\ell = (\bar{L}_L \gamma_\mu L_L) (\bar{L}_L \gamma^\mu L_L) \mathcal{F}$$

$$\mathcal{P}_T = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \mathcal{F}_T$$

$$\mathcal{P}_W = W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W$$

$$\mathcal{P}_2 = B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2$$

$$\mathcal{P}_4 = B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4$$

$$\mathcal{P}_6 = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6$$

$$\mathcal{P}_{12} = (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}$$

$$\mathcal{P}_{14} = \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}$$

$$\mathcal{P}_{18} = \text{Tr}(\mathbf{T} [\mathbf{V}_\mu, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18}$$

$$\mathcal{P}_{24} = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}$$

$$\mathcal{P}_{WWW} = \frac{\varepsilon_{abc}}{\Lambda^2} W_\mu^{a\nu} W_\nu^{b\rho} W_\rho^{c\mu} \mathcal{F}_{WWW}$$

$$\mathcal{N}_2^{\mathcal{Q}} = i \bar{Q}_R \gamma_\mu \mathbf{U}^\dagger \mathbf{V}^\mu \mathbf{U} Q_R \mathcal{F}$$

$$\mathcal{N}_6^{\mathcal{Q}} = i \bar{Q}_R \gamma_\mu \mathbf{U}^\dagger \{ \mathbf{V}^\mu, \mathbf{T} \} \mathbf{U} Q_R \mathcal{F}$$

$$\mathcal{N}_8^{\mathcal{Q}} = i \bar{Q}_R \gamma_\mu \mathbf{U}^\dagger \mathbf{T} \mathbf{V}^\mu \mathbf{T} \mathbf{U} Q_R \mathcal{F}$$

$$R_5^\ell = (\bar{L}_L \gamma_\mu \mathbf{T} L_L) (\bar{L}_L \gamma^\mu \mathbf{T} L_L) \mathcal{F}$$

$$\mathbf{T} = U \sigma^3 \mathbf{U}^\dagger$$

$$\mathbf{V}_\mu = D_\mu \mathbf{U} \mathbf{U}^\dagger$$

Quick dictionary:

$$\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \rightarrow Z_\mu$$

$$\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \rightarrow Z_\mu Z_\nu + W_\mu^+ W_\mu^-$$

$$\mathcal{F}_i \rightarrow 1 + h/v + \dots$$

basis of 1604.06801



# HEFT operators for VBS - minimal set

restricting to CP +  $U(3)^5$  and neglecting 4-fermion interactions

29 operators

$$\mathcal{P}_C = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \mathcal{F}_C$$

$$\mathcal{P}_B = B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B$$

$$\mathcal{P}_1 = B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \mathcal{F}_1$$

$$\mathcal{P}_3 = \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3$$

$$\mathcal{P}_5 = \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5$$

$$\mathcal{P}_{11} = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11} \mathbf{F}_{S,1}$$

$$\mathcal{P}_{13} = i \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}$$

$$\mathcal{P}_{17} = \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}$$

$$\mathcal{P}_{23} = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23} \mathbf{F}_{S,0}$$

$$\mathcal{P}_{26} = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}$$

$$\mathcal{N}_1^{\mathcal{Q}} = i \bar{Q}_L \gamma_\mu \mathbf{V}^\mu Q_L \mathcal{F}$$

$$\mathcal{N}_5^{\mathcal{Q}} = i \bar{Q}_L \gamma_\mu \{ \mathbf{V}^\mu, \mathbf{T} \} Q_L \mathcal{F}$$

$$\mathcal{N}_7^{\mathcal{Q}} = i \bar{Q}_L \gamma_\mu \mathbf{T} \mathbf{V}^\mu \mathbf{T} Q_L \mathcal{F}$$

$$\mathcal{N}_2^\ell = i \bar{L}_R \gamma_\mu \mathbf{U}^\dagger \{ \mathbf{V}^\mu, \mathbf{T} \} \mathbf{U} L_R \mathcal{F}$$

$$R_2^\ell = (\bar{L}_L \gamma_\mu L_L) (\bar{L}_L \gamma^\mu L_L) \mathcal{F}$$

$$\mathcal{P}_T = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \mathcal{F}_T$$

$$\mathcal{P}_W = W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W$$

$$\mathcal{P}_2 = B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2$$

$$\mathcal{P}_4 = B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4$$

$$\mathcal{P}_6 = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6 \mathbf{F}_{S,0}$$

$$\mathcal{P}_{12} = (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}$$

$$\mathcal{P}_{14} = \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}$$

$$\mathcal{P}_{18} = \text{Tr}(\mathbf{T} [\mathbf{V}_\mu, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18} \mathbf{F}_{S,0}$$

$$\mathcal{P}_{24} = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24} \mathbf{F}_{S,0}$$

$$\mathcal{P}_{WWW} = \frac{\varepsilon_{abc}}{\Lambda^2} W_\mu^{a\nu} W_\nu^{b\rho} W_\rho^{c\mu} \mathcal{F}_{WWW}$$

$$\mathcal{N}_2^{\mathcal{Q}} = i \bar{Q}_R \gamma_\mu \mathbf{U}^\dagger \mathbf{V}^\mu \mathbf{U} Q_R \mathcal{F}$$

$$\mathcal{N}_6^{\mathcal{Q}} = i \bar{Q}_R \gamma_\mu \mathbf{U}^\dagger \{ \mathbf{V}^\mu, \mathbf{T} \} \mathbf{U} Q_R \mathcal{F}$$

$$\mathcal{N}_8^{\mathcal{Q}} = i \bar{Q}_R \gamma_\mu \mathbf{U}^\dagger \mathbf{T} \mathbf{V}^\mu \mathbf{T} \mathbf{U} Q_R \mathcal{F}$$

$$R_5^\ell = (\bar{L}_L \gamma_\mu \mathbf{T} L_L) (\bar{L}_L \gamma^\mu \mathbf{T} L_L) \mathcal{F}$$

$$\mathbf{T} = U \sigma^3 \mathbf{U}^\dagger$$

$$\mathbf{V}_\mu = D_\mu \mathbf{U} \mathbf{U}^\dagger$$

Quick dictionary:

$$\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \rightarrow Z_\mu$$

$$\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \rightarrow Z_\mu Z_\nu + W_\mu^+ W_\mu^-$$

$$\mathcal{F}_i \rightarrow 1 + h/v + \dots$$

correspond to  $d \geq 8$   
in the SMEFT

basis of 1604.06801

Analysis @ d=6: we can restrict to a minimal set of 14 parameters

1. preliminary study: which diagrams are negligible?  
can L/T polarizations be distinguished?  
any sensitivity to CP violation?  
which input scheme ( $\{\alpha_{em}, m_Z, G_f\}$  or  $\{m_W, m_Z, G_f\}$ )?
2. start with a feasible subset of parameters if 14 are too many.
3. tools: compare available codes for SMEFT predictions
4. including more parameters: possibility of combining / comparing with other datasets

Later extensions:

1. switch to a HEFT analysis
2. including some d=8 operators

**Extra slides**

# TGC vs QGC in the SMEFT

## TGC

$$-ig_{WWV} \left[ g_1^V \left( W_{\mu\nu}^+ W^{-\mu} V^\nu - W_{\mu\nu}^- W^{+\mu} V^\nu \right) + \kappa_V W_\mu^+ W_\nu^- V^{\mu\nu} \right] - i\lambda_V V^{\mu\nu} W_\nu^{+\rho} W_{\rho\mu}^-$$

$$\begin{array}{l|l} g_1^\gamma & 1 \\ \kappa_\gamma & 1 + \frac{v^2}{t_\theta} C_{HWB} \\ \lambda_\gamma & 6C_{W s_\theta} \end{array} \quad \begin{array}{l|l} g_1^Z & 1 - \frac{v^2}{4c_{2\theta}} \left( C_{HD} + 4C_{HI}^{(3)} - 2C_{II} + 4t_\theta C_{HWB} \right) \\ \kappa_Z & 1 - \frac{v^2}{4c_{2\theta}} \left( C_{HD} + 4C_{HI}^{(3)} - 2C_{II} + 4s_{2\theta} C_{HWB} \right) \\ \lambda_Z & 6C_{W c_\theta} \end{array}$$

## QGC

$$g^2/2 \left[ g_{WW}^{(1)} \left( (W_\mu^+ W_\nu^-)^2 - (W_\mu^+ W^{-\mu})^2 \right) + g_{VV'}^{(1)} \left( W^{+\mu} W^{-\nu} \frac{V_\mu V'_\nu + V_\nu V'_\mu}{2} - W_\mu^+ W^{-\mu} V_\nu V'^\nu \right) \right]$$

$$\begin{array}{l|l} g_{WW}^{(1)} & 1 - \frac{v^2 c_\theta^2}{2c_{2\theta}} \left( C_{HD} + 4C_{HI}^{(3)} - 2C_{II} + 4t_\theta C_{HWB} \right) \\ g_{Z\gamma}^{(1)}/s_{2\theta} & 1 - \frac{v^2}{4c_{2\theta}} \left( C_{HD} + 4C_{HI}^{(3)} - 2C_{II} + 4t_\theta C_{HWB} \right) \\ g_{ZZ}^{(1)}/c_\theta^2 & 1 - \frac{v^2}{2c_{2\theta}} \left( C_{HD} + 4C_{HI}^{(3)} - 2C_{II} + 4t_\theta C_{HWB} \right) \end{array} \quad \begin{array}{l|l} g_{\gamma\gamma}^{(1)}/s_\theta^2 & 1 \end{array}$$

+ structures from  $C_{W \in IJK} W_{\mu\nu}^I W^{J\nu\rho} W_\rho^{K\mu}$

	$\alpha_{\text{em}}$ scheme	$m_W$ scheme
$\delta g_1^\gamma$	0	$\frac{v^2}{4} \left( -c_{HD} \frac{c_\theta^2}{s_\theta^2} - 4c_{H\ell}^{(3)} + 2c_{II} - 4c_{HWB} \frac{c_\theta}{s_\theta} \right)$
$\delta g_1^Z$	$-\frac{v^2}{4c_{2\theta}} \left( c_{HD} + 4c_{H\ell}^{(3)} - 2c_{II} + 4\frac{s_\theta}{c_\theta} c_{HWB} \right)$	$\frac{v^2}{4} \left( c_{HD} - 4c_{H\ell}^{(3)} + 2c_{II} + 4\frac{s_\theta}{c_\theta} c_{HWB} \right)$
$\delta \kappa_\gamma$	$v^2 \frac{c_\theta}{s_\theta} c_{HWB}$	$\frac{v^2}{4} \left( -c_{HD} \frac{c_\theta^2}{s_\theta^2} - 4c_{H\ell}^{(3)} + 2c_{II} \right)$
$\delta \kappa_Z$	$-\frac{v^2}{4c_{2\theta}} \left( c_{HD} + 4c_{H\ell}^{(3)} - 2c_{II} + 4s_{2\theta} c_{HWB} \right)$	$\frac{v^2}{4} \left( c_{HD} - 4c_{H\ell}^{(3)} + 2c_{II} \right)$
$\delta \lambda_\gamma$	$6c_W s_\theta$	$6c_W s_\theta$
$\delta \lambda_Z$	$6c_W c_\theta$	$6c_W c_\theta$

$$\begin{aligned} \mathcal{L}_{WWV} = & -ig_{WWW} \left\{ g_1^V \left( W_{\mu\nu}^+ W^{-\mu} V^\nu - W_\mu^+ V_\nu W^{-\mu\nu} \right) + \kappa_V W_\mu^+ W_\nu^- V^{\mu\nu} \right. \\ & - ig_5^V \varepsilon^{\mu\nu\rho\sigma} \left( W_\mu^+ \partial_\rho W_\nu^- - W_\nu^- \partial_\rho W_\mu^+ \right) V_\sigma + \\ & \left. + g_6^V \left( \partial_\mu W^{+\mu} W^{-\nu} - \partial_\mu W^{-\mu} W^{+\nu} \right) V_\nu \right\} \end{aligned}$$

$$g_{WWZ} = g \cos \theta, \quad g_{WW\gamma} = e$$

1311.1823

	Coeff. $\times e^2/s_\theta^2$	Chiral
$\Delta\kappa_\gamma$	1	$-2c_1 + 2c_2 + c_3 - 4c_{12} + 2c_{13}$
$\Delta g_6^\gamma$	1	$-c_9$
$\Delta g_1^Z$	$\frac{1}{c_\theta^2}$	$\frac{s_\theta^2}{4e^2 c_{2\theta}} c_T + \frac{2s_\theta^2}{c_{2\theta}} c_1 + c_3$
$\Delta\kappa_Z$	1	$\frac{s_\theta^2}{e^2 c_{2\theta}} c_T + \frac{4s_\theta^2}{c_{2\theta}} c_1 - \frac{2s_\theta^2}{c_{2\theta}^2} c_2 + c_3 - 4c_{12} + 2c_{13}$
$\Delta g_5^Z$	$\frac{1}{c_\theta^2}$	$c_{14}$
$\Delta g_6^Z$	$\frac{1}{c_\theta^2}$	$s_\theta^2 c_9 - c_{16}$

$$\begin{aligned} \mathcal{L}_{4X} \equiv & g^2 \left\{ g_{ZZ}^{(1)} (Z_\mu Z^\mu)^2 + g_{WW}^{(1)} W_\mu^+ W^{+\mu} W_\nu^- W^{-\nu} - g_{WW}^{(2)} (W_\mu^+ W^{-\mu})^2 \right. \\ & + g_{VV'}^{(3)} W^{+\mu} W^{-\nu} (V_\mu V'_\nu + V'_\mu V_\nu) - g_{VV'}^{(4)} W_\nu^+ W^{-\nu} V^\mu V'_\mu \\ & \left. + i g_{VV'}^{(5)} e^{\mu\nu\rho\sigma} W_\mu^+ W_\nu^- V_\rho V'_\sigma \right\} \end{aligned}$$

1311.1823

	Coeff. $\times e^2/4s_\theta^2$	Chiral
$\Delta g_{WW}^{(1)}$	1	$\frac{s_\theta^2}{e^2 c_{2\theta}} C_T + \frac{8s_\theta^2}{c_{2\theta}} C_1 + 4C_3 + 2C_{11} - 16C_{12} + 8C_{13}$
$\Delta g_{WW}^{(2)}$	1	$\frac{s_\theta^2}{e^2 c_{2\theta}} C_T + \frac{8s_\theta^2}{c_{2\theta}} C_1 + 4C_3 - 4C_6 - \frac{v^2}{2} C_{Ch} - 2C_{11} - 16C_{12} + 8C_{13}$
$\Delta g_{ZZ}^{(1)}$	$\frac{1}{c_\theta}$	$C_6 + \frac{v^2}{8} C_{Ch} + C_{11} + 2C_{23} + 2C_{24} + 4C_{26}$
$\Delta g_{ZZ}^{(3)}$	$\frac{1}{c_\theta^2}$	$\frac{s_\theta^2 c_\theta^2}{e^2 c_{2\theta}} C_T + \frac{2s_\theta^2}{c_{2\theta}} C_1 + 4C_\theta^2 C_3 - 2s_\theta^4 C_9 + 2C_{11} + 4s_\theta^2 C_{16} + 2C_{24}$
$\Delta g_{ZZ}^{(4)}$	$\frac{1}{c_\theta^2}$	$\frac{2s_\theta^2 c_\theta^2}{e^2 c_{2\theta}} C_T + \frac{4s_\theta^2}{c_{2\theta}} C_1 + 8C_\theta^2 C_3 - 4C_6 - \frac{v^2}{2} C_{Ch} - 4C_{23}$
$\Delta g_{\gamma\gamma}^{(3)}$	$s_\theta^2$	$-2C_9$
$\Delta g_{\gamma Z}^{(3)}$	$\frac{s_\theta}{c_\theta}$	$\frac{s_\theta^2}{e^2 c_{2\theta}} C_T + \frac{8s_\theta^2}{c_{2\theta}} C_1 + 4C_3 + 4s_\theta^2 C_9 - 4C_{16}$
$\Delta g_{\gamma Z}^{(4)}$	$\frac{s_\theta}{c_\theta}$	$\frac{2s_\theta^2}{e^2 c_{2\theta}} C_T + \frac{16s_\theta^2}{c_{2\theta}} C_1 + 8C_3$
$\Delta g_{\gamma Z}^{(5)}$	$\frac{s_\theta}{c_\theta}$	$8C_{14}$