



Studies for the measurement of the $t\bar{t} + \gamma$ process with ATLAS at LHC

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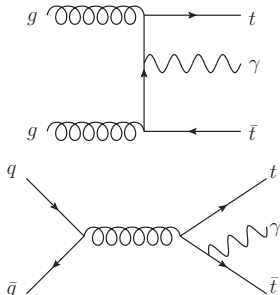
Why is $pp \rightarrow t\bar{t}\gamma$ interesting?

- sensitive to the electromagnetic coupling of the top quark \rightarrow direct charge measurement
- sensitive to vertex structure (in differential measurements) \rightarrow test of the Standard Model and possible clues to physics beyond the Standard Model

$$\begin{aligned} \Gamma^\mu(q^2) = & -iQ_t e \gamma^\mu \left(F_1^V(q^2) + F_1^A(q^2) \gamma_5 \right) \\ & - iQ_t e i \frac{\sigma^{\mu\nu} q_\nu}{2m_t} \left(F_2^V(q^2) + F_2^A(q^2) \gamma_5 \right) \end{aligned}$$

Precision measurements:

- possible background: charged hadrons that are misidentified as photons and photons from hadron decays

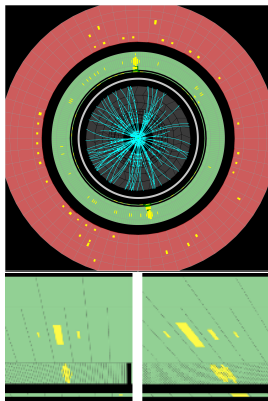


photons deposit energy mostly in the electromagnetic calorimeter:

- searching for energy clusters in the electromagnetic calorimeter
- reconstruction and matching of the tracks, photon conversion?
- possibly: reconstruction of conversion vertex
- depending on the matching: (un)converted photon or electron

Photon identification with high signal efficiency and high background rejection is required. Photon identification is based on cuts on discriminating variables that characterize:

- hadronic leakage
- lateral and longitudinal shower development
- energy ratios



Variables and Position

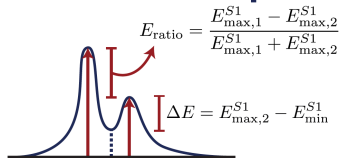
	Strips	2nd	Had.
Ratios	f_1, f_{side}	R_{η}^*, R_{ϕ}	$R_{\text{Had.}}^*$
Widths	$w_{s,3}, w_{s,\text{tot}}$	$w_{\eta,2}^*$	-
Shapes	$\Delta E, E_{\text{ratio}}$	* Used in PhotonLoose.	

Energy Ratios

$$R_{\eta} = \frac{E_{3 \times 7}^{S2}}{E_{7 \times 7}^{S2}} \quad R_{\phi} = \frac{E_{3 \times 3}^{S2}}{E_{3 \times 7}^{S2}} \quad R_{\text{Had}} = \frac{E_T^{\text{Had}}}{E_T}$$

$$f_1 = \frac{E_{S1}}{E_{\text{Tot.}}} \quad f_{\text{side}} = \frac{E_7^{S1} - E_3^{S1}}{E_3^{S1}}$$

Shower Shapes



Widths

$$w_{\eta,2} = \sqrt{\frac{\sum E_i \eta_i^2}{\sum E_i} - \left(\frac{\sum E_i \eta_i}{\sum E_i} \right)^2}$$

Width in a 3×5 ($\Delta\eta \times \Delta\phi$) region of cells in the second layer.

$$w_s = \sqrt{\frac{\sum E_i (i - i_{\text{max}})^2}{\sum E_i}}$$

$w_{s3} = w_s$, uses 3 strips in η ;
 w_{stot} is defined similarly, but uses 20 strips.

Prompt Photons

A prompt photon is a photon originating from the matrix element, the parton shower or the hadronisation.

Hadron fake

A hadron fake is either a hadron misidentified as photon or a photon from the hadron decay.

Data modelling

hadron fakes:

- based on dijet events
- e.g. $g + g \rightarrow g + g$
- final state gluons create jets
- some hadrons of these jets will be detected as photons

prompt photons:

- based on inclusive photon samples
- primarily events where $g + q \rightarrow \gamma + q$ via t-channel scattering (QCD-Compton)

High amount of hadronic fakes for $t\bar{t}\gamma$ -processes (about 30 % at $\sqrt{s} = 7$ TeV).
At $\sqrt{s} = 7$ TeV discrimination using discriminating variables e.g. p_T^{iso} .

The photon track-isolation variable p_T^{iso} ...

... is defined as the scalar sum of the transverse momenta of selected tracks in a cone of $\Delta R = 0.2$ around the photon candidate.

p_T^{iso} -distribution of signal and background is simulated with templates. The templates are fitted to the data using a likelihood fit.

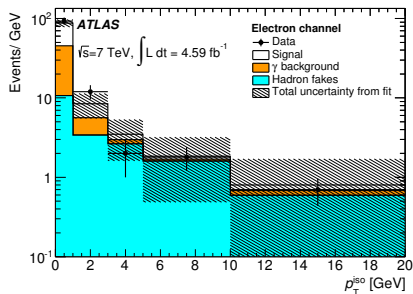


Figure: ²Results of the combined likelihood fit using the track-isolation (p_T^{iso}) distributions as the discriminating variable for the electron channel.

²Phys.Rev.D 91:072007

- check distributions of the shower shape variables for differences
- use differences to discriminate between hadron fakes and prompt photons
- use information about conversion

$$s = \frac{1}{2} \sum_{i \in \text{bins}} \frac{(s_i - b_i)^2}{(s_i + b_i)}$$

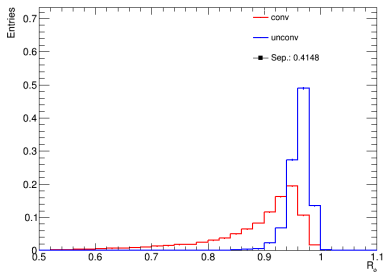


Figure: Comparison of R_ϕ between tight-ID converted and unconverted photons.

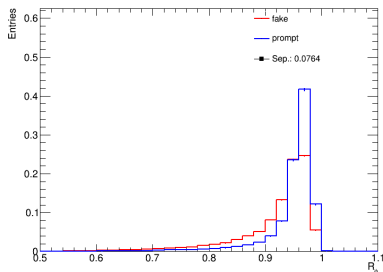


Figure: Comparison of R_ϕ between tight-ID prompt photons and fakes.

Table: Comparison of separations between prompt photons and hadron fakes for different variables and conversion types.

	all	converted	unconverted	N_{bins}	x_{min}	x_{max}
R_{η}	0.0531	0.0462	0.0279	30	0.85	1.05
R_{ϕ}	0.0764	0.0344	0.0507	30	0.5	1.1
$w_{\eta 2}$	0.0232	0.0153	0.0091	30	0.004	0.016
f_{side}	0.0778	0.0332	0.0809	30	0	0.7
$w_{\eta 1}$	0.0464	0.0262	0.0321	30	0.4	0.85
w_{stot}	0.0484	0.0350	0.0391	30	0	4
R_{had}	0.0310	0.0354	0.0238	30	-0.2	0.25
R_{had_1}	0.0291	0.0368	0.0224	30	-0.05	0.06
E_{ratio}	0.0234	0.0286	0.0209	30	0.75	1.02
ΔE	0.0029	0.0052	0.0016	30	-25 GeV	300 GeV

BDT uses an ensemble of weak learners to create one strong learner. Models have form:

$$F(x) = \sum_{m=1}^M \gamma_m h_m(x)$$

$h_m(x)$ are called weak learners, we use decision trees. The model is build iterative:

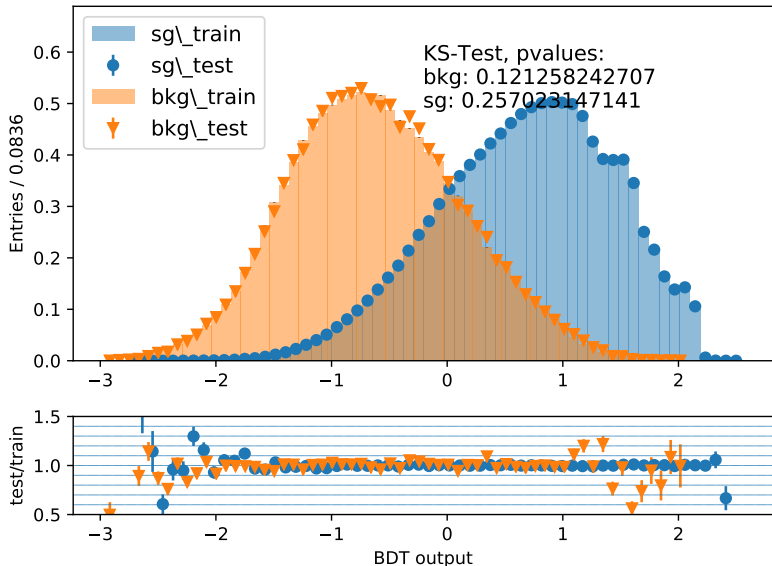
$$F_m(x) = F_{m-1}(x) + \gamma_m h_m(x)$$

$h_m(x)$ is chosen so that the loss function L will be minimized:

$$F_m(x) = F_{m-1}(x) + \arg \min_h \sum_{i=1}^n L(y_i, F_{m-1}(x_i) - h(x))$$

Use learning rate ν to scale step length:

$$F_m(x) = F_{m-1}(x) + \nu \gamma_m h_m(x)$$



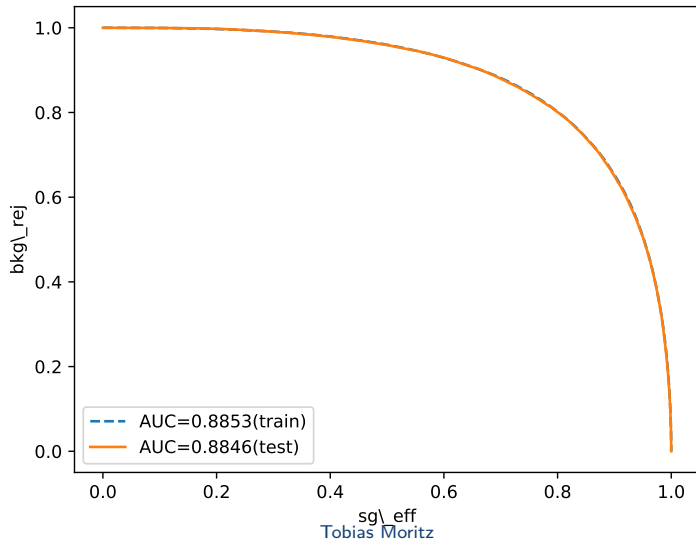


Table: Comparison of AUC-values

	no conversion	converted	unconverted	conversion as feature
AUC-test	0.8829	0.8780	0.8761	0.8838
AUC-train	0.8840	0.8803	0.8805	0.8864

Table: Comparison AUC-values for exponential loss function

	no conversion	converted	unconverted	conversion as feature
AUC-test	0.8829	0.8784	0.8774	0.8846
AUC-train	0.8839	0.8811	0.8798	0.8853

Summary

- can use differences in shower shapes to discriminate between prompt photons and hadron fakes
- training two different BDTs for converted and unconverted photons does not improve performance
- increase in performance when using conversion as feature

Outlook

- studies of systematics
- optimization of BDT parameters
- comparison with other MVA-algorithms (e.g. neural network)



Thank you for your attention.



Backup

Gradient Tree Boosting

- number of single trees = 120, maximum depth of trees = 3, learning rate = 0.1, subsample = 0.5
- loss function: $L = -2(yP - \log(1 + \exp(P)))$, where P is the log-odds
- train size: 0.8, test size: 0.2
- features: R_η , R_ϕ , $w_{\eta 2}$, f_{side} , $w_{\eta 1}$, w_{stot} , R_{had} , R_{had_1} , E_{ratio} , ΔE , (see appendix)

- uses a set of decision rules to perform classification on a dataset
- training vectors $x_i \in \mathbb{R}^l$, $i = 1, \dots, n$
- label vector $y_i \in \mathbb{R}$, $i = 1, \dots, n$
- n samples and l features
- data at node m represented by Q
- split candidates $\theta = (j, t_m)$ with feature j and threshold t_m
- data is split into two subsets $Q_{\text{left}}(\theta)$ and $Q_{\text{right}}(\theta)$:

$$Q_{\text{left}}(\theta) = \left\{ (x_i, y_i) \mid x_i^j \leq t_m \right\}$$
$$Q_{\text{right}}(\theta) = Q \setminus Q_{\text{left}}$$

- x_i^j is the value of the i -th sample for the j -th feature
- impurity at node m is calculated for impurity function $H()$:

$$G(Q, \theta) = \frac{n_{\text{left}}}{N_m} H(Q_{\text{left}}(\theta)) + \frac{n_{\text{right}}}{N_m} H(Q_{\text{right}}(\theta))$$

- the parameters that minimize the impurity are chosen:

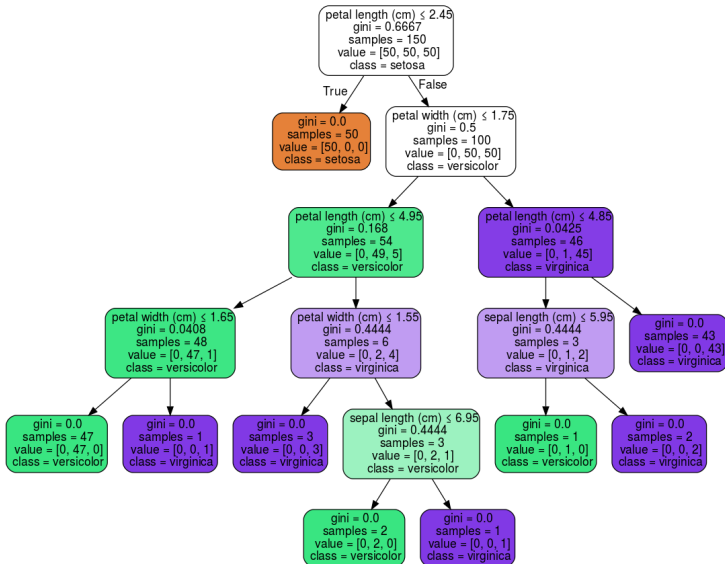
$$\theta^* = \arg \min_{\theta} G(Q, \theta)$$

- recurse for $Q_{\text{left}}(\theta^*)$ and $Q_{\text{right}}(\theta^*)$.
- possible measure for impurity is GINI:

$$H(X_m) = \sum_k p_{mk}(1 - p_{mk}),$$
$$p_{mk} = \frac{1}{N_m} \sum_{x_i \in R_m} I(y_i = k)$$

- p_{mk} is the proportion of class k in node m .

Example for a decision tree using the iris dataset



BDT uses an ensemble of decision trees. Models have form:

$$F(x) = \sum_{m=1}^M \gamma_m h_m(x)$$

$h_m(x)$ are called weak learners, we use decision trees. The model is build iterative:

$$F_m(x) = F_{m-1}(x) + \gamma_m h_m(x)$$

$h_m(x)$ is chosen so that the loss function L will be minimized:

$$F_m(x) = F_{m-1}(x) + \arg \min_h \sum_{i=1}^n L(y_i, F_{m-1}(x_i) - h(x))$$

Use learning rate ν to scale step length:

$$F_m(x) = F_{m-1}(x) + \nu \gamma_m h_m(x)$$

General idea of MVA implementation and training procedure

- learn some properties of a data set and apply them to new data
- split data into training set and testing set
- train MVA algorithm using the training set
- test algorithm on testing set

Signal

- based on inclusive photon samples
- primarily events where $g + q \rightarrow \gamma + q$ via t-channel scattering (QCD-Compton)
- `/eos/atlas/atlascerngroupdisk/perf-egamma/InclusivePhotons/v12/v12_01/PyPt17_inf_mc15c_v12_PIDuse.root`

Background

- based on dijet events
- e.g. $g + g \rightarrow g + g$
- final state gluons create jets
- some hadrons of these jets will be detected as photons
- `/eos/atlas/atlascerngroupdisk/perf-egamma/InclusivePhotons/v12/v12_01/Py8_jetjet_mc15c_v12_PIDuse.root`

Normalised hadronic leakage

$$R_{\text{had}} = \frac{E_{\text{T}}^{\text{had}}}{E_{\text{T}}}$$

The transverse energy deposited in the hadronic calorimeter $E_{\text{T}}^{\text{had}}$ in a window of $\Delta\eta \times \Delta\phi = 0.24 \times 0.24$ behind the photon cluster, normalized to the total transverse energy E_{T}

Normalised hadronic leakage in first layer

$$R_{\text{had}_1} = \frac{E_{\text{T}}^{\text{had},1}}{E_{\text{T}}}$$

The transverse energy deposited in the first layer of the hadronic calorimeter $E_{\text{T}}^{\text{had},1}$ in a window of $\Delta\eta \times \Delta\phi = 0.24 \times 0.24$ behind the photon cluster, normalized to the total transverse energy E_{T}

Middle η energy ratio

$$R_{\eta} = \frac{E_{3 \times 7}^{S2}}{E_{7 \times 7}^{S2}}$$

The ratio of the sum of the energy $E_{3 \times 7}^{S2}$ in a rectangle of 3×7 calorimeter cells in the second layer, to the sum of the energies $E_{7 \times 7}^{S2}$ in a 7×7 rectangle, centred around the cluster seed.

Middle ϕ energy ratio

$$R_{\phi} = \frac{E_{3 \times 3}^{S2}}{E_{3 \times 7}^{S2}}$$

The ratio of the sum of the energy $E_{3 \times 3}^{S2}$ in a rectangle of 3×3 calorimeter cells in the second layer, to the sum of the energies $E_{3 \times 7}^{S2}$ in a 3×7 rectangle, centred around the cluster seed.

Middle lateral width

$$w_{\eta 2} = \sqrt{\frac{\sum E_i \eta_i^2}{\sum E_i} - \left(\frac{\sum E_i \eta_i}{\sum E_i}\right)^2}$$

Measures the lateral width of the shower in the second layer of the electromagnetic calorimeter in a window of $\eta \times \phi = 3 \times 5$ cells. E_i is the energy deposited in each cell and η_i the η position of the cell.

Front side energy ratio

$$F_{\text{side}} = \frac{E(\pm 3) - E(\pm 1)}{E(\pm 1)}$$

Measures the lateral containment of the shower in η . $E(\pm n)$ is the energy in the $\pm n$ strips around the strip with the highest energy.

Front lateral width (3 strips)

$$w_{s3} = \sqrt{\frac{\sum E_i (i - i_{\max})^2}{\sum E_i}}$$

Measures the width of the shower in η using three strip cells centred on the strip with the highest energy. i is the strip identification number, i_{\max} identifies the strip with the highest energy and E_i is the energy deposited in each strip.

Front lateral width (total)

$w_{s\text{tot}}$ measures the width of the shower in η using all cells in a window of $\Delta\eta \times \Delta\phi = 0.0625 \times 0.196$, approximately 20×2 strip cells. $w_{s\text{tot}}$ is computed as w_{s3} .

Front second maximum energy difference

$$\Delta E = [E_{2^{\text{nd}}\text{max}}^{S1} - E_{\text{min}}^{S1}]$$

The difference between the energy of the strip cell with the second largest energy $E_{2^{\text{nd}}\text{max}}^{S1}$ and the energy of the cell with the lowest energy found between the largest and the second largest energy E_{min}^{S1} . If there is no second maximum $\Delta E = 0$.

Front maxima relative energy ratio

$$E_{\text{ratio}} = \frac{E_{1^{\text{st}}\text{max}}^{S1} - E_{2^{\text{nd}}\text{max}}^{S1}}{E_{1^{\text{st}}\text{max}}^{S1} + E_{2^{\text{nd}}\text{max}}^{S1}}$$

The relative difference between the energy of the strip with the highest energy $E_{1^{\text{st}}\text{max}}^{S1}$ and the energy of the strip with the second highest energy $E_{2^{\text{nd}}\text{max}}^{S1}$. If there is no second maximum $E_{\text{ratio}} = 1$

Table: Comparison of separations between converted and unconverted photons for different variables for all photons, prompts and hadron fakes

	all	prompt	fake	N_{bins}	x_{min}	x_{max}
R_{η}	0.0891	0.0608	0.0830	30	0.85	1.05
R_{ϕ}	0.4148	0.3930	0.4035	30	0.5	1.1
$w_{\eta 2}$	0.0996	0.0831	0.0974	30	0.004	0.016
f_{side}	0.1195	0.1643	0.0748	30	0	0.7
$w_{\eta 1}$	0.1266	0.1288	0.1091	30	0.4	0.85
w_{stot}	0.0820	0.0808	0.0707	30	0	4
R_{had}	0.0104	0.0051	0.0087	30	-0.2	0.25
$R_{\text{had}1}$	0.0060	0.0030	0.0052	30	-0.05	0.06
E_{ratio}	0.0059	0.0060	0.0060	30	0.75	1.02
ΔE	0.0033	0.0035	0.0034	30	-25 GeV	300 GeV

Separation:

$$s = \frac{1}{2} \sum_{i \in \text{bins}} \frac{(s_i - b_i)^2}{(s_i + b_i)}$$

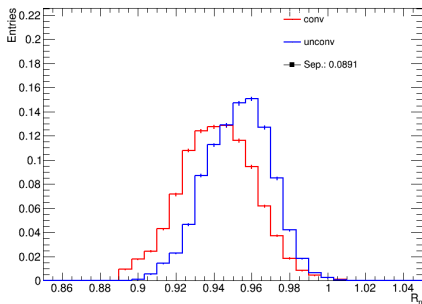


Figure: Comparison of R_η between tight-ID converted and unconverted photons.

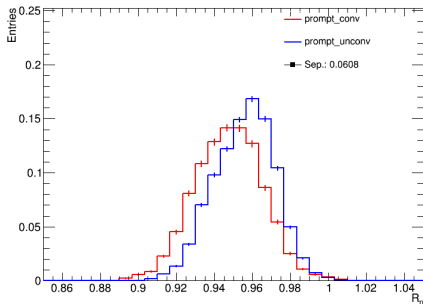


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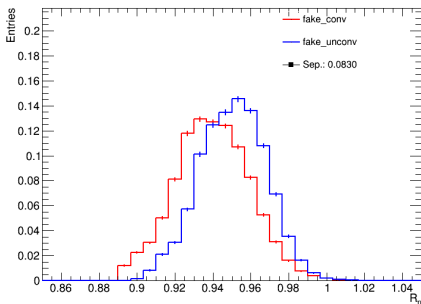


Figure: Comparison of R_η between tight-ID converted and unconverted fake photons.

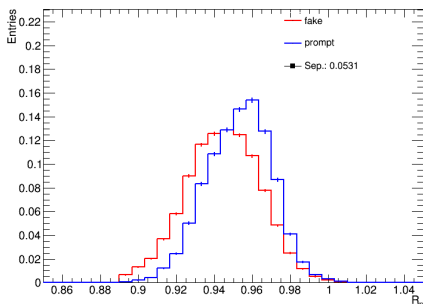


Figure: Comparison of R_η between tight-ID prompt photons and fakes.

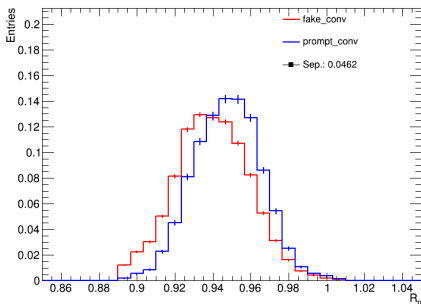


Figure: Comparison of R_η between tight-ID converted prompt photons and fake photons.

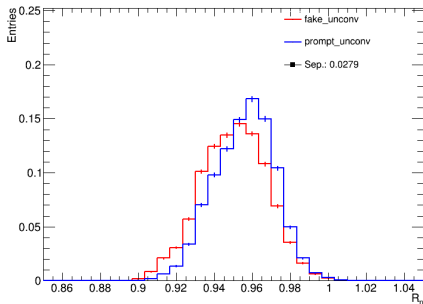


Figure: Comparison of R_η between tight-ID unconverted prompt photons and fake photons.

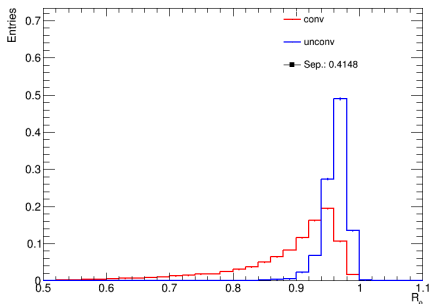


Figure: Comparison of R_ϕ between tight-ID converted and unconverted photons.

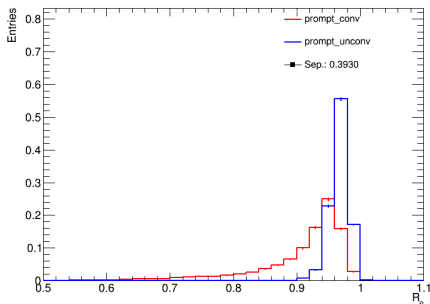


Figure: Comparison of R_ϕ between tight-ID converted and unconverted prompt photons.

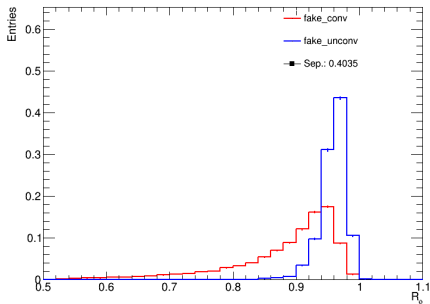


Figure: Comparison of R_ϕ between tight-ID converted and unconverted fake photons.

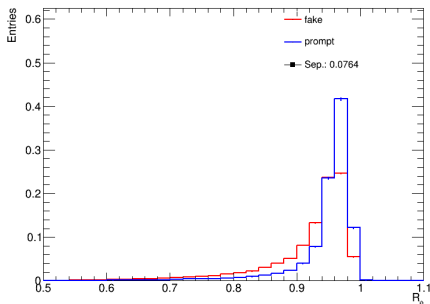


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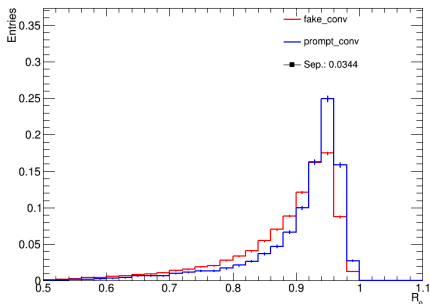


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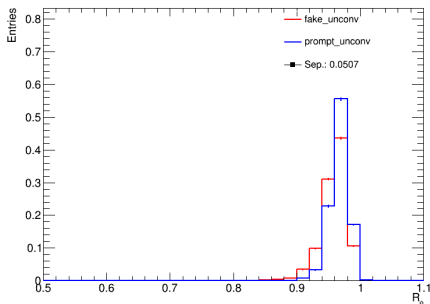


Figure: Comparison of R_ϕ between tight-ID unconverted prompt photons and fake photons.

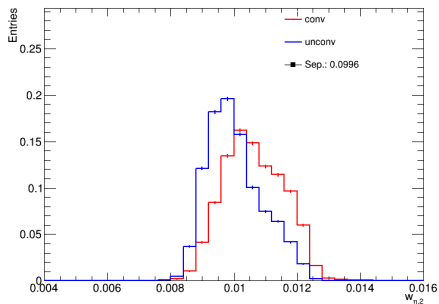


Figure: Comparison of $w_{\eta 2}$ between tight-ID converted and unconverted photons.

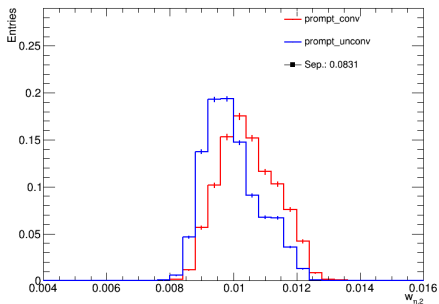


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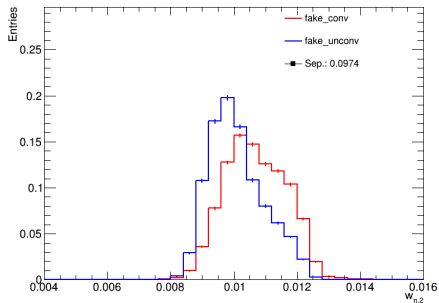


Figure: Comparison of $w_{\eta 2}$ between tight-ID converted and unconverted fake photons.

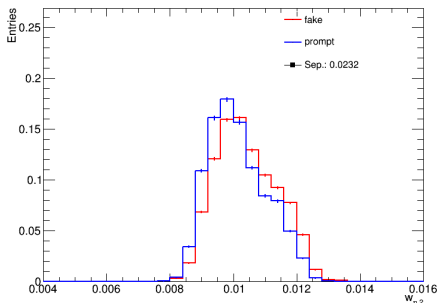


Figure: Comparison of $w_{\eta 2}$ between tight-ID prompt photons and fakes.

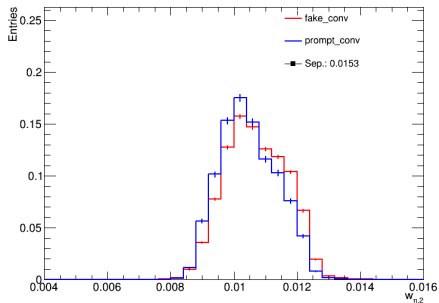


Figure: Comparison of $w_{\eta 2}$ between tight-ID converted prompt photons and fake photons.

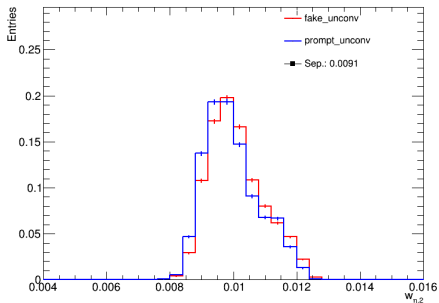


Figure: Comparison of $w_{\eta 2}$ between tight-ID unconverted prompt photons and fake photons.

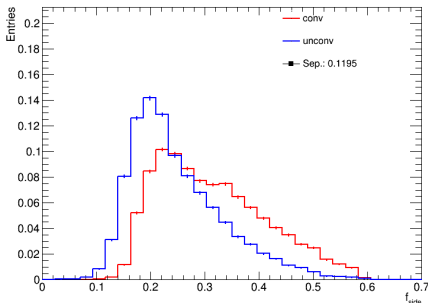


Figure: Comparison of f_{side} between tight-ID converted and unconverted photons.

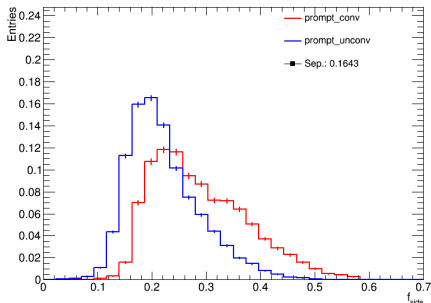


Figure: Comparison of f_{side} between tight-ID converted and unconverted prompt photons.

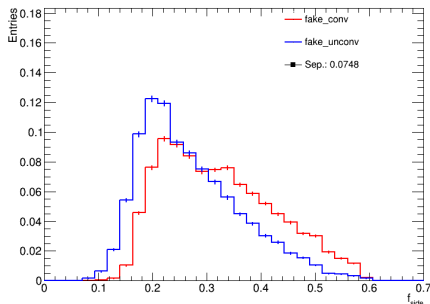


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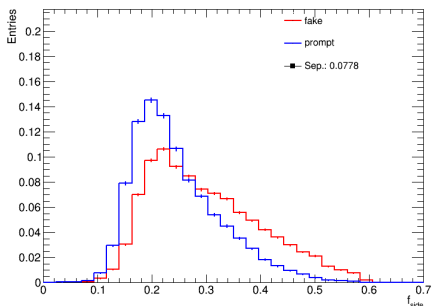


Figure: Comparison of f_{side} between tight-ID prompt photons and fakes.

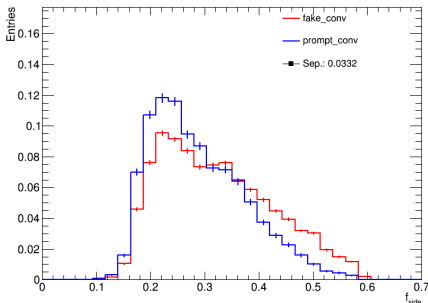


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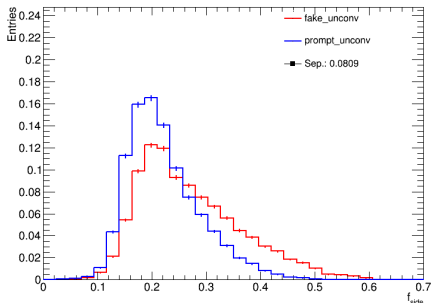


Figure: Comparison of f_{side} between tight-ID unconverted prompt photons and fake photons.

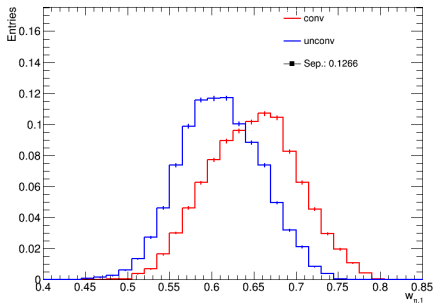


Figure: Comparison of $w_{\eta 1}$ between tight-ID converted and unconverted photons.

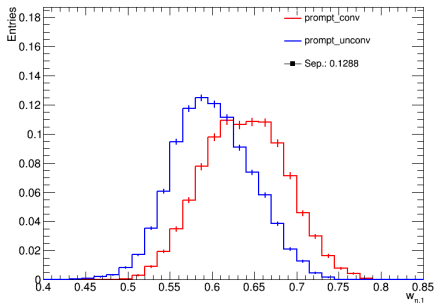


Figure: Comparison of $w_{\eta 1}$ between tight-ID converted and unconverted prompt photons.

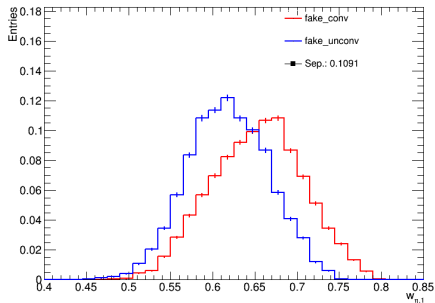


Figure: Comparison of $w_{\eta 1}$ between tight-ID converted and unconverted fake photons.

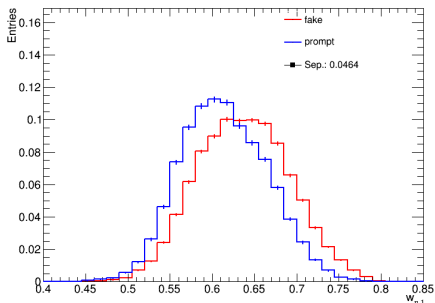


Figure: Comparison of $w_{\eta 1}$ between tight-ID prompt photons and fakes.

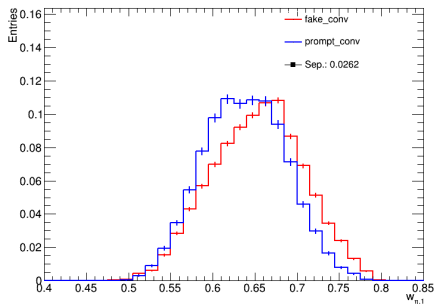


Figure: Comparison of $w_{\eta 1}$ between tight-ID converted prompt photons and fake photons.

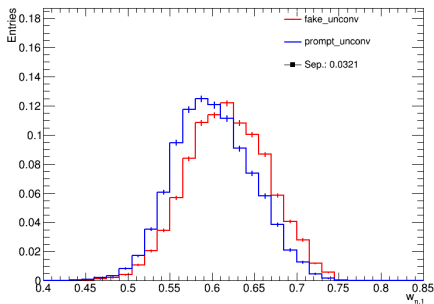


Figure: Comparison of $w_{\eta 1}$ between tight-ID unconverted prompt photons and fake photons.

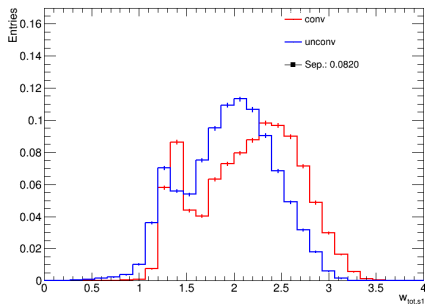


Figure: Comparison of $w_{\text{tot},s1}$ between tight-ID converted and unconverted photons.

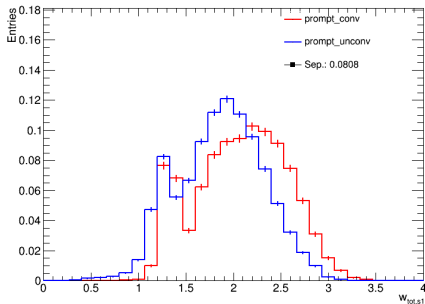


Figure: Comparison of $w_{\text{tot},s1}$ between tight-ID converted and unconverted prompt photons.

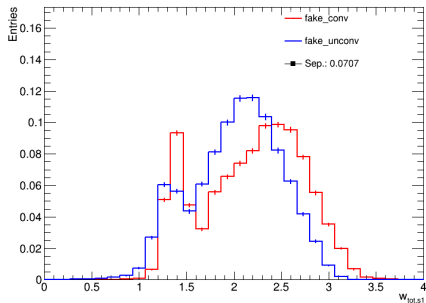


Figure: Comparison of $w_{\text{tot},s1}$ between tight-ID converted and unconverted fake photons.

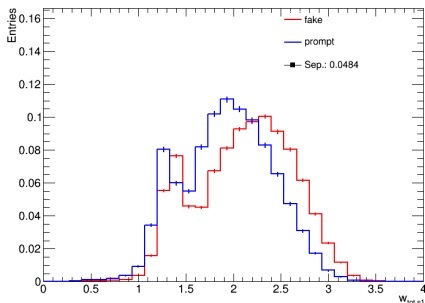


Figure: Comparison of $w_{\text{tot},s1}$ between tight-ID prompt photons and fakes.

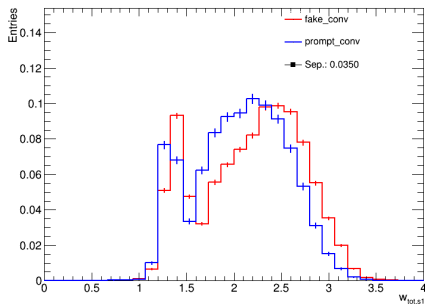


Figure: Comparison of $w_{\text{tot},s1}$ between tight-ID converted prompt photons and fake photons.

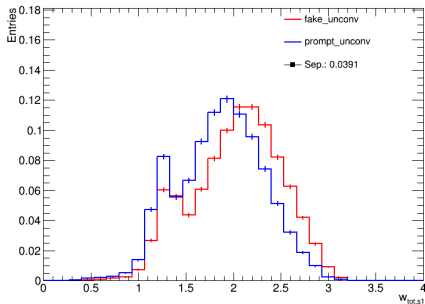


Figure: Comparison of $w_{\text{tot},s1}$ between tight-ID unconverted prompt photons and fake photons.

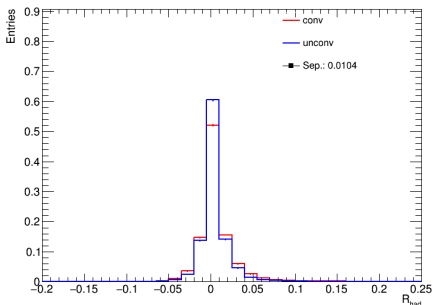


Figure: Comparison of R_{had} between tight-ID converted and unconverted photons.

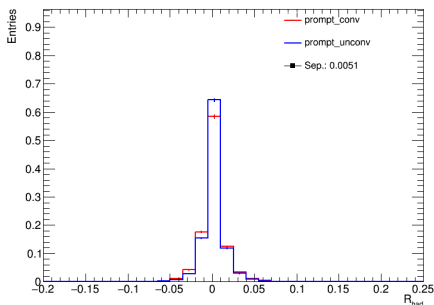


Figure: Comparison of R_{had} between tight-ID converted and unconverted prompt photons.

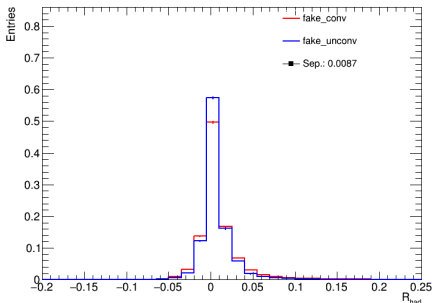


Figure: Comparison of R_{had} between tight-ID converted and unconverted fake photons.

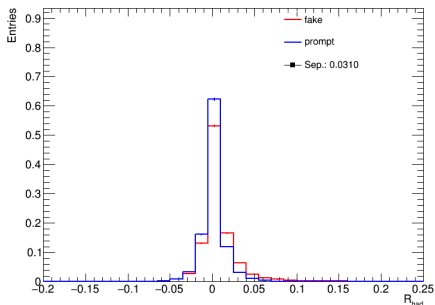


Figure: Comparison of R_{had} between tight-ID prompt photons and fakes.

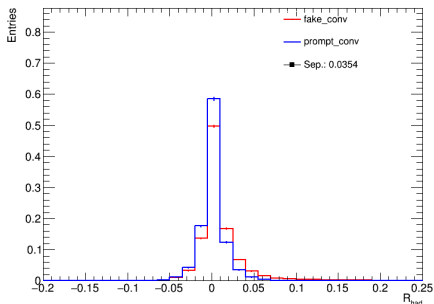


Figure: Comparison of R_{had} between tight-ID converted prompt photons and fake photons.

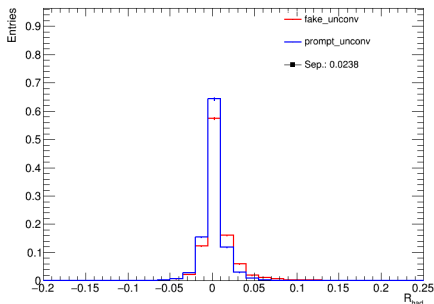


Figure: Comparison of R_{had} between tight-ID unconverted prompt photons and fake photons.

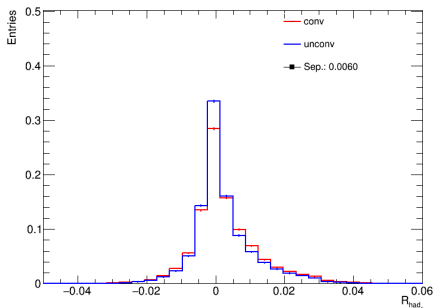


Figure: Comparison of R_{had_1} between tight-ID converted and unconverted photons.

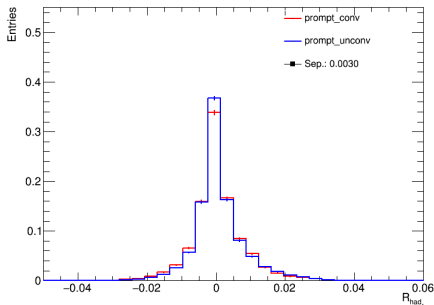


Figure: Comparison of R_{had_1} between tight-ID converted and unconverted prompt photons.

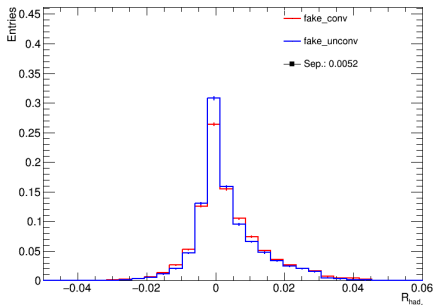


Figure: Comparison of R_{had_1} between tight-ID converted and unconverted fake photons.

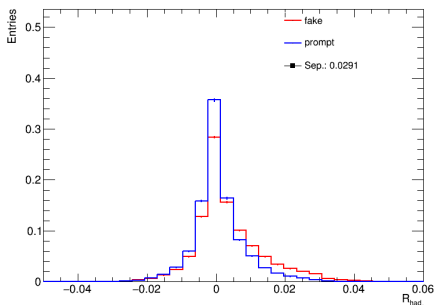


Figure: Comparison of R_{had_1} between tight-ID prompt photons and fakes.

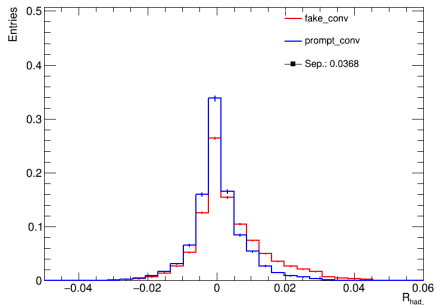


Figure: Comparison of R_{had_1} between tight-ID converted prompt photons and fake photons.

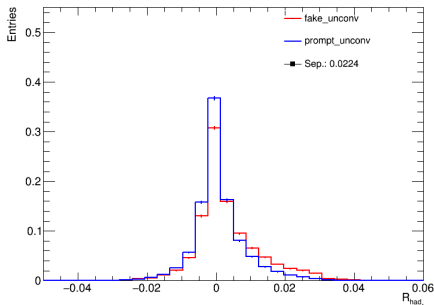


Figure: Comparison of R_{had_1} between tight-ID unconverted prompt photons and fake photons.

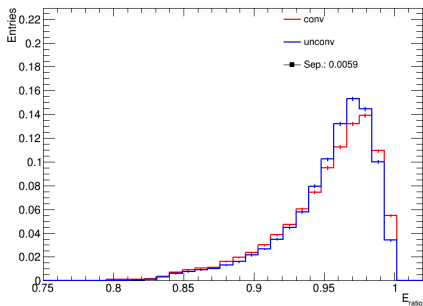


Figure: Comparison of E_{ratio} between tight-ID converted and unconverted photons.

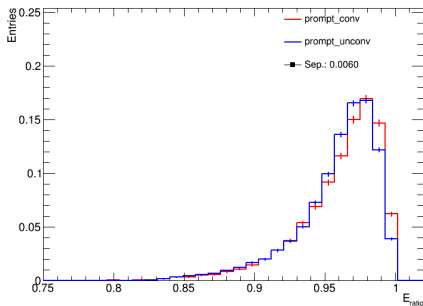


Figure: Comparison of E_{ratio} between tight-ID converted and unconverted prompt photons.

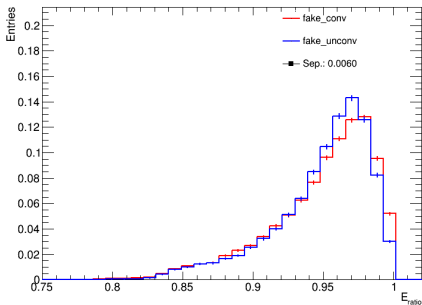


Figure: Comparison of E_{ratio} between tight-ID converted and unconverted fake photons.

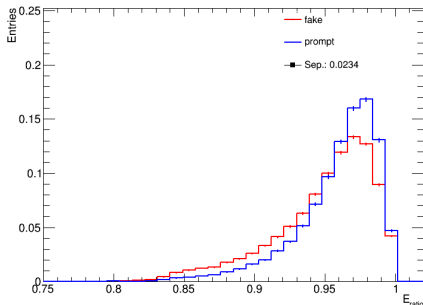


Figure: Comparison of E_{ratio} between tight-ID prompt photons and fakes.

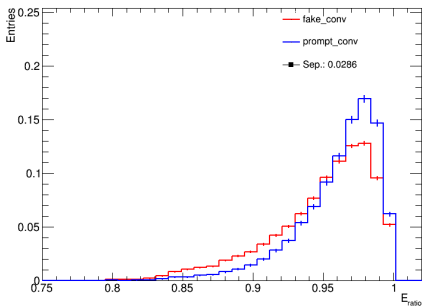


Figure: Comparison of E_{ratio} between tight-ID converted prompt photons and fake photons.

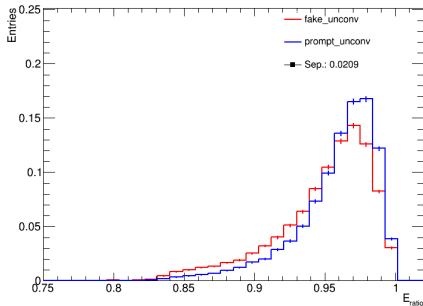


Figure: Comparison of E_{ratio} between tight-ID unconverted prompt photons and fake photons.

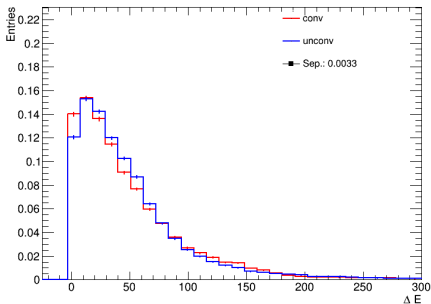


Figure: Comparison of ΔE between tight-ID converted and unconverted photons.

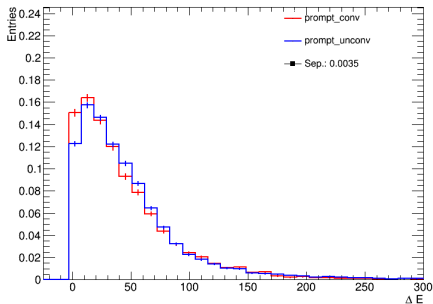


Figure: Comparison of ΔE between tight-ID converted and unconverted prompt photons.

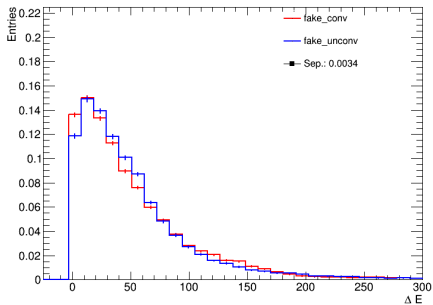


Figure: Comparison of ΔE between tight-ID converted and unconverted fake photons.

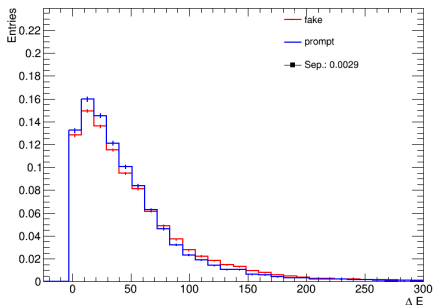


Figure: Comparison of ΔE between tight-ID prompt photons and fakes.

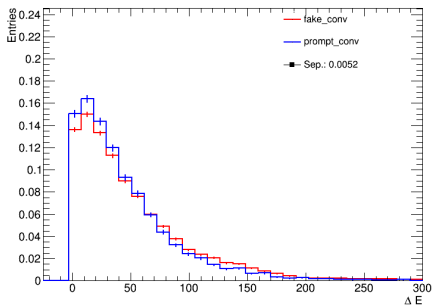


Figure: Comparison of ΔE between tight-ID converted prompt photons and fake photons.

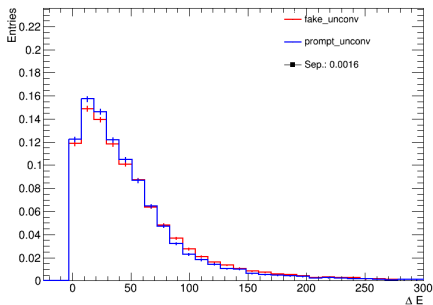


Figure: Comparison of ΔE between tight-ID unconverted prompt photons and fake photons.