

Axions beyond DFSZ/KSVZ

Flavour and Dark Matter workshop
Universität Heidelberg - 26.09.17

Luca Di Luzio



Based on

Redefining the Axion Window, LDL, F. Mescia, E. Nardi
Phys. Rev. Lett. 118 (2017) no.3, 031801, arXiv:1610.07593 [hep-ph]

Window for preferred axion models, LDL, F. Mescia, E. Nardi
to appear in Phys. Rev. D, arXiv:1705.05370 [hep-ph]

The Nucleophobic Axion, LDL, F. Mescia, E. Nardi, P. Panci, M. Redi, R. Ziegler
In preparation

Outline

- The QCD axion
- Experimental axion searches
- Axion couplings beyond DFSZ/KSVZ benchmarks

The strong CP problem

- CP violation in QCD

$$\mathcal{L}_{\text{QCD}} = \sum_q \bar{q} (i\not{D} - \textcolor{red}{m}_q e^{i\theta_q}) q - \frac{1}{4} G_a^{\mu\nu} G_{\mu\nu}^a - \textcolor{red}{\theta} \frac{\alpha_s}{8\pi} G_a^{\mu\nu} \tilde{G}_{\mu\nu}^a \quad \left(\tilde{G}_{\mu\nu}^a = \frac{1}{2} \epsilon_{\mu\nu\rho\sigma} G^{a,\rho\sigma} \right)$$

- $\bar{\theta} = \theta - \sum_q \theta_q$ invariant under a chiral transformation ($q \rightarrow e^{i\gamma_5 \alpha} q$)

- exp. limit from neutron EDM  $|\bar{\theta}| \lesssim 10^{-10}$ why so small ?

- Qualitatively different from other “small value” problems of the SM

- $\bar{\theta} \propto J_{\text{CKM}} \log \Lambda_{\text{UV}}$ radiatively stable (unlike $m_H^2 \ll \Lambda_{\text{UV}}^2$) [Ellis, Gaillard NPB 150 (1979)]

- it evades explanations based on environmental selection (unlike $y_{e,u,d} \sim 10^{-6} \div 10^{-5}$)

[Ubbaldi, 0811.1599]

The QCD axion

- PQ mechanism

[Peccei, Quinn PRL 38 (1977), PRD 16 (1977)]

- assume a global $U(1)_{\text{PQ}}$: i) QCD anomalous and ii) spontaneously broken

- axion: PGB of $U(1)_{\text{PQ}}$ breaking


[Weinberg PRL 40 (1978), Wilczek PRL 40 (1978)]

$$a(x) \rightarrow a(x) + \delta\alpha f_a$$


$$\mathcal{L}_{\text{eff}} = \underbrace{\left(\bar{\theta} + \frac{a}{f_a} \right)}_{\text{effective theta}} \frac{\alpha_s}{8\pi} G_a^{\mu\nu} \tilde{G}_{\mu\nu}^a - \frac{1}{2} \partial^\mu a \partial_\mu a + \mathcal{L}(\partial_\mu a, \psi)$$

$\langle \theta_{\text{eff}}(x) \rangle \rightarrow 0$ (dynamically, via a QCD-induced axion potential)

Axion models (UV completions)

- PQWW axion
 - axion identified with the phase of the Higgs in a 2HDM ($f_a \sim v$, ruled out long ago)
- Needs $f_a \gg v$  invisible axion (phase of a SM singlet)
 - DFSZ axion: [Zhitnitsky SJNP 31 (1980), Dine, Fischler, Srednicki PLB 104 (1981)]
SM quarks charged under PQ (requires 2HDM)
 - KSVZ axion: [Kim PRL 43 (1979), Shifman, Vainshtein, Zakharov NPB 166 (1980)]
new vector-like quarks charged under PQ

Axion models (UV completions)

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- DFSZ axion:

SM quarks charged under PQ (requires 2HDM)

- KSVZ axion:

new vector-like quarks charged under PQ



Here: focus on general DFSZ/KSVZ models

- Other variants: composite axion, heavy axion, axiflavor, etc.

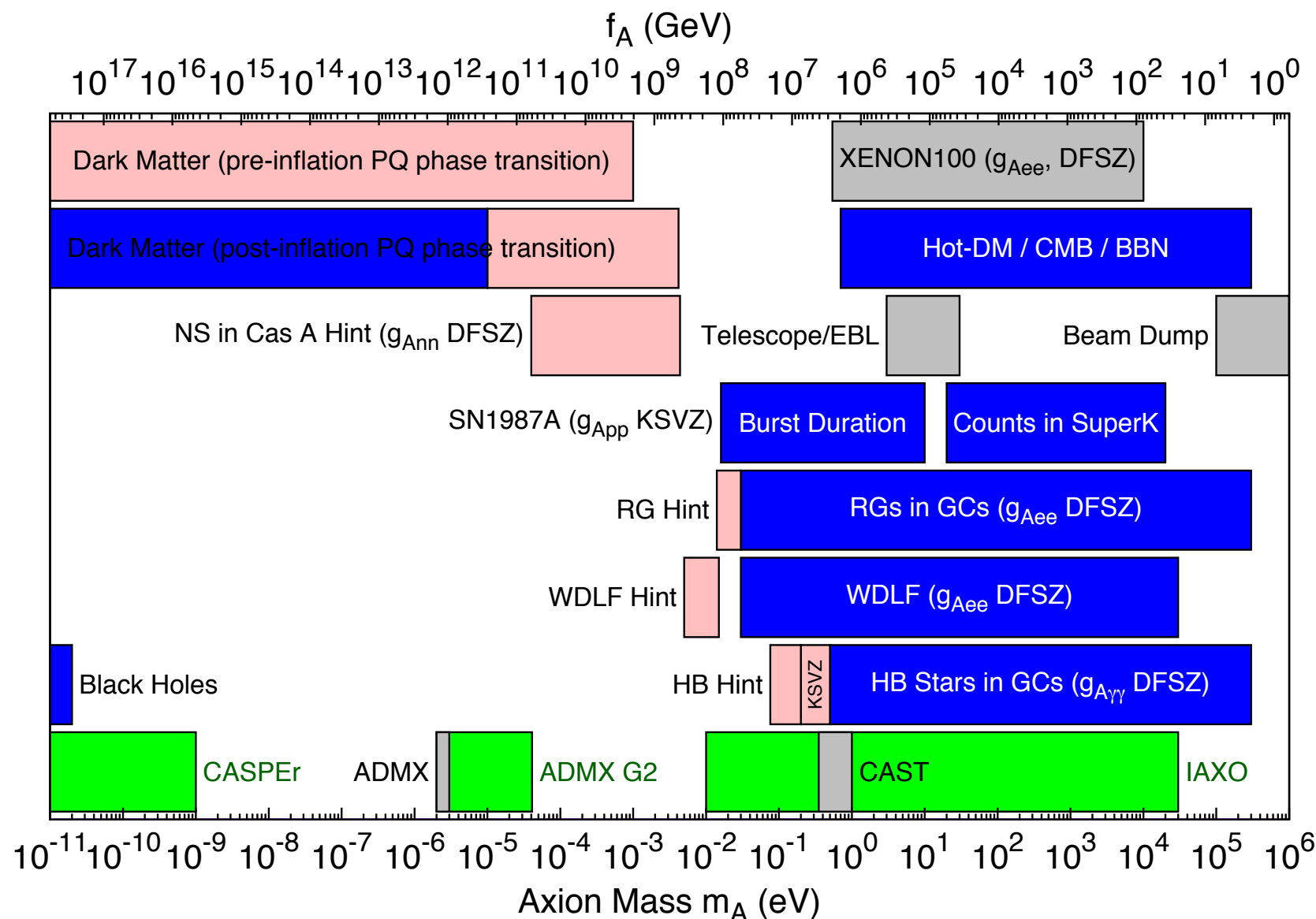
[Kim PRD 31 (1985), ...]

[Rubakov JETP 65 (1997), ...]

[Calibbi et al. 1612.08040, ...]

Axion landscape

- axion mass $m_a \simeq m_\pi \frac{f_\pi}{f_a} \simeq 6 \text{ meV} \frac{10^9 \text{ GeV}}{f_a}$
- axion couplings $\sim 1/f_a$



[Ringwald, Rosenberg, Rybka, Particle Data Group (2016)]

Astro/cosmo exclusions

Lab exclusions

Exp. sensitivities

DM explained / Astro Hints

Outburst of exp. proposals

PHYSICAL REVIEW X **4**, 021030 (2014)

Proposal for a Cosmic Axion Spin Precession Experiment (CASPER)

Dmitry Budker,^{1,5} Peter W. Graham,² Micah Ledbetter,³ Surjeet Rajendran,² and Alexander O. Sushkov⁴

PRL **113**, 161801 (2014) PHYSICAL REVIEW LETTERS week ending
17 OCTOBER 2014

Resonantly Detecting Axion-Mediated Forces with Nuclear Magnetic Resonance

Asimina Arvanitaki¹ and Andrew A. Geraci^{2,*}

PRL **117**, 141801 (2016) PHYSICAL REVIEW LETTERS week ending
30 SEPTEMBER 2016

Broadband and Resonant Approaches to Axion Dark Matter Detection

Yonatan Kahn,^{1,*} Benjamin R. Safdi,^{2,†} and Jesse Thaler^{2,‡}

PRL **118**, 091801 (2017) PHYSICAL REVIEW LETTERS week ending
3 MARCH 2017

Dielectric Haloscopes: A New Way to Detect Axion Dark Matter

Allen Caldwell,¹ Gia Dvali,^{1,2,3} Béla Majorovits,¹ Alexander Millar,¹ Georg Raffelt,¹ Javier Redondo,^{1,4}
Olaf Reimann,¹ Frank Simon,¹ and Frank Steffen¹
(MADMAX Working Group)

Searching for galactic axions through magnetized media: The QUAX proposal

R. Barbieri^{a,b}, C. Braggio^c, G. Carugno^c, C.S. Gallo^c, A. Lombardi^d, A. Ortolan^d, R. Pengo^d,
G. Ruoso^{d,*}, C.C. Speake^e

PHYSICAL REVIEW D **91**, 084011 (2015)

Discovering the QCD axion with black holes and gravitational waves

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Masha Baryakhtar[†] and Xinlu Huang[‡]

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(Received 16 December 2014; published 7 April 2015)

PHYSICAL REVIEW D **91**, 011701(R) (2015)

Search for dark matter axions with the Orpheus experiment

Gray Rybka,^{*} Andrew Wagner,[†] Kunal Patel, Robert Percival, and Katileiah Ramos
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CULTASK, The Coldest Axion Experiment at CAPP/IBS/KAIST in Korea

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Outburst of exp. proposals

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Yonatan Kahn,^{1,*} Benjamin R. Safdi,^{2,†} and Jesse Thaler^{2,‡}

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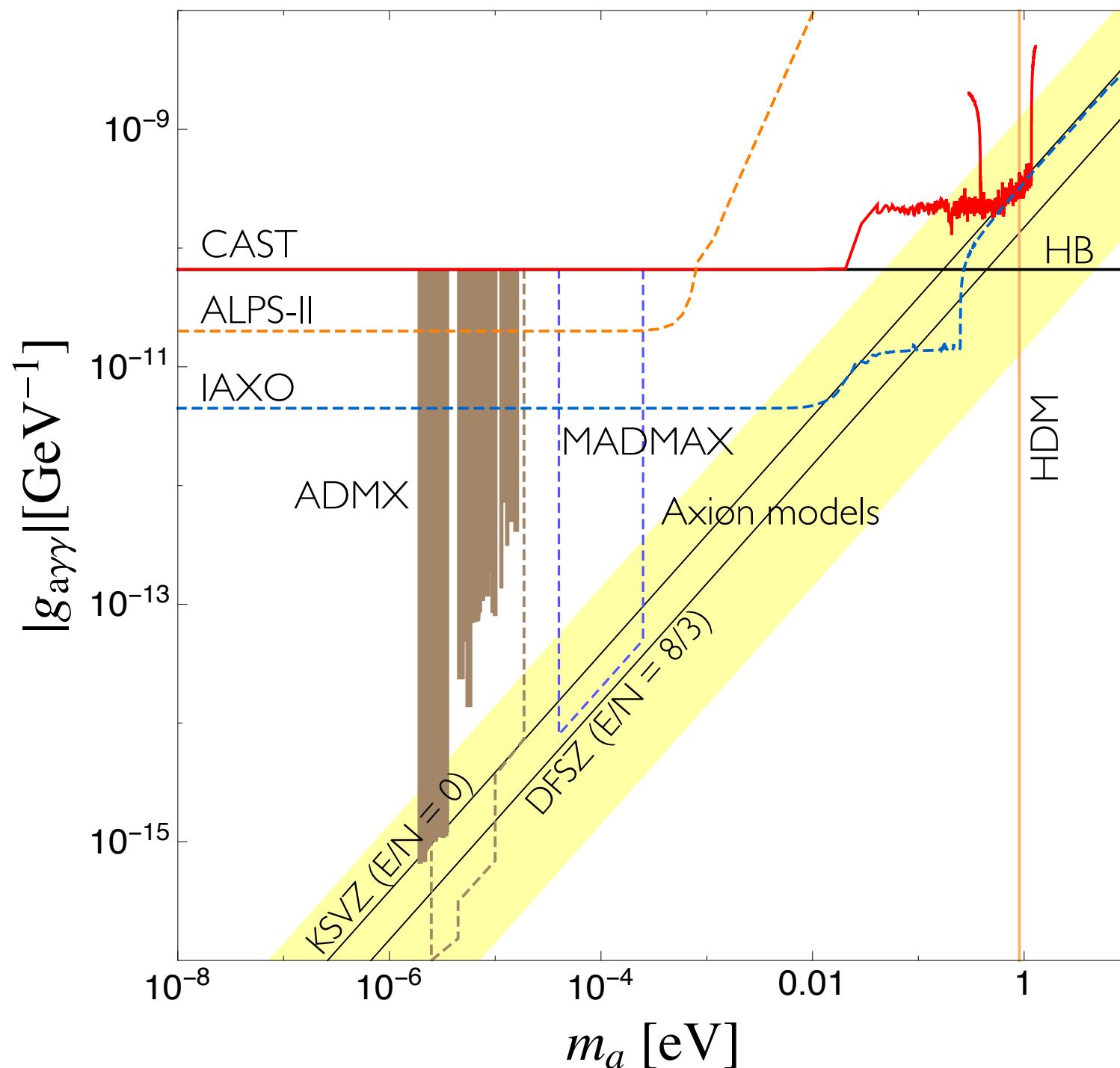
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g_aγγ

The “usual” axion window



$$g_{a\gamma\gamma} = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E}{N} - 1.92 \right)$$

E/N anomaly coefficients,
depend on UV completion

$$|E/N - 1.92| \in [0.07, 7]$$

[Axion band from PDG (since end of 90's).
Includes representative KSVZ/DFSZ models
e.g. from:

- Kaplan, NPB 260 (1985),
- Cheng, Geng, Ni, PRD 52 (1995),
- Kim, PRD 58 (1998)]

Hadronic axions

- Field content

Field	Spin	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_{PQ}$
Q_L	1/2	\mathcal{C}_Q	\mathcal{I}_Q	\mathcal{Y}_Q	\mathcal{X}_L
Q_R	1/2	\mathcal{C}_Q	\mathcal{I}_Q	\mathcal{Y}_Q	\mathcal{X}_R
Φ	0	1	1	0	1

- PQ charges carried by a vector-like quark $Q = Q_L + Q_R$
 - $Q \sim (3,1,0)$ in the original KSVZ model, but in general only $\mathcal{C}_Q \neq I$ required

$$\partial^\mu J_\mu^{PQ} = \frac{N\alpha_s}{4\pi} G \cdot \tilde{G} + \frac{E\alpha}{4\pi} F \cdot \tilde{F}$$

$$\left. \begin{aligned} N &= \sum_Q (\mathcal{X}_L - \mathcal{X}_R) T(\mathcal{C}_Q) \\ E &= \sum_Q (\mathcal{X}_L - \mathcal{X}_R) Q_Q^2 \end{aligned} \right\} \text{anomaly coeff.}$$

and a SM singlet Φ containing the “invisible” axion ($f_a \gg v$)

$$\Phi(x) = \frac{1}{\sqrt{2}} [\rho(x) + f_a] e^{ia(x)/f_a}$$

Hadronic axions

- Field content

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Q_R	1/2	\mathcal{C}_Q	\mathcal{I}_Q	\mathcal{Y}_Q	\mathcal{X}_R
Φ	0	1	1	0	1

- Lagrangian

$$\mathcal{L}_a = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{PQ}} - V_{H\Phi} + \mathcal{L}_{Qq} \quad |\mathcal{X}_L - \mathcal{X}_R| = 1$$

- $\mathcal{L}_{\text{PQ}} = |\partial_\mu \Phi|^2 + \bar{Q} i \not{D} Q - (y_Q \bar{Q}_L Q_R \Phi + \text{H.c.}) \quad \longrightarrow \quad m_Q = y_Q f_a / \sqrt{2}$
- $V_{H\Phi} = -\mu_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4 + \lambda_{H\Phi} |H|^2 |\Phi|^2 \quad \longrightarrow \quad m_\rho \sim f_a$
- \mathcal{L}_{Qq} d ≤ 4 mixing with SM quarks (depends in Q-gauge quantum numbers)

Q-stability issue

- Symmetry of the kinetic term

$$U(1)_{Q_L} \times U(1)_{Q_R} \times U(1)_\Phi \xrightarrow{y_Q \neq 0} U(1)_{PQ} \times U(1)_Q$$

$$\mathcal{L}_{PQ} = |\partial_\mu \Phi|^2 + \bar{Q} i \not{D} Q - (y_Q \bar{Q}_L Q_R \Phi + \text{H.c.})$$

- $U(1)_Q$ is the Q-baryon number. If exact, Q would be stable



issue with cosmology [see backup slides]

Q-stability issue

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- Q-decay possible if $U(1)_Q$ broken via:

- $\mathcal{L}_{Qq} \neq 0$

- Planck-suppressed op. $\mathcal{L}_{Qq}^{d>4}$

Selection criteria

- We require:

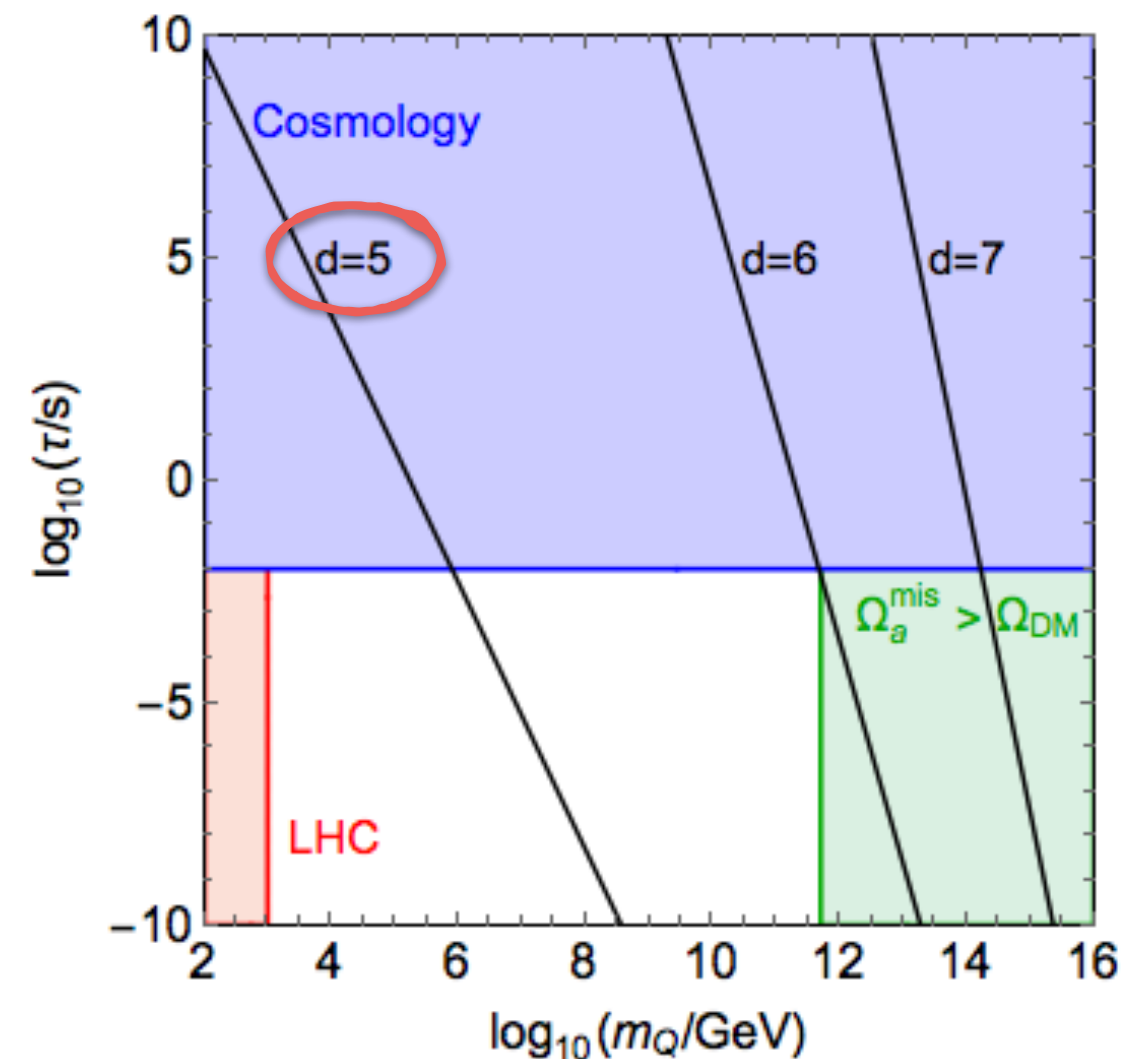
I. Q sufficiently short lived $\tau_Q \lesssim 10^{-2}$ s (applies only to $T_{\text{reheating}} > m_Q$)

- decays via $d=4$ op. fast enough
- decays via effective op.

$$\mathcal{L}_{Qq}^{d>4} = \frac{1}{M_{\text{Planck}}^{(d-4)}} \mathcal{O}_{Qq}^{d>4} + \text{h.c.}$$

$$\Gamma_{\text{NDA}} = \frac{1}{4(4\pi)^{2n_f-3}(n_f-1)!(n_f-2)!} \frac{m_Q^{2d-7}}{M_{\text{Planck}}^{2(d-4)}}$$

→ Q must allow for $d=4$ or 5 decay op.'s



Selection criteria

- We require:

1. Q sufficiently short lived $\tau_Q \lesssim 10^{-2} \text{ s}$ (*applies only to $T_{\text{reheating}} > m_Q$*)
2. No Landau poles below 10^{18} GeV
3. Absence of domain walls
4. Q -assisted unification

Phenomenologically preferred Q's

- Only 15 Q's survive to conditions 1. and 2.

$$g_{a\gamma\gamma} = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E}{N} - 1.92(4) \right)$$

$$\frac{E}{N} = \frac{\sum_Q \mathcal{Q}_Q^2}{\sum_Q T(\mathcal{C}_Q)}$$

R_Q	\mathcal{O}_{Qq}	$\Lambda_{\text{Landau}}^{2-\text{loop}} [\text{GeV}]$	E/N
$(3, 1, -1/3)$	$\bar{Q}_L d_R$	$9.3 \cdot 10^{38} (g_1)$	$2/3$
$(3, 1, 2/3)$	$\bar{Q}_L u_R$	$5.4 \cdot 10^{34} (g_1)$	$8/3$
$(3, 2, 1/6)$	$\bar{Q}_R q_L$	$6.5 \cdot 10^{39} (g_1)$	$5/3$
$(3, 2, -5/6)$	$\bar{Q}_L d_R H^\dagger$	$4.3 \cdot 10^{27} (g_1)$	$17/3$
$(3, 2, 7/6)$	$\bar{Q}_L u_R H$	$5.6 \cdot 10^{22} (g_1)$	$29/3$
$(3, 3, -1/3)$	$\bar{Q}_R q_L H^\dagger$	$5.1 \cdot 10^{30} (g_2)$	$14/3$
$(3, 3, 2/3)$	$\bar{Q}_R q_L H$	$6.6 \cdot 10^{27} (g_2)$	$20/3$
$(3, 3, -4/3)$	$\bar{Q}_L d_R H^{\dagger 2}$	$3.5 \cdot 10^{18} (g_1)$	$44/3$
$(\bar{6}, 1, -1/3)$	$\bar{Q}_L \sigma_{\mu\nu} d_R G^{\mu\nu}$	$2.3 \cdot 10^{37} (g_1)$	$4/15$
$(\bar{6}, 1, 2/3)$	$\bar{Q}_L \sigma_{\mu\nu} u_R G^{\mu\nu}$	$5.1 \cdot 10^{30} (g_1)$	$16/15$
$(\bar{6}, 2, 1/6)$	$\bar{Q}_R \sigma_{\mu\nu} q_L G^{\mu\nu}$	$7.3 \cdot 10^{38} (g_1)$	$2/3$
$(8, 1, -1)$	$\bar{Q}_L \sigma_{\mu\nu} e_R G^{\mu\nu}$	$7.6 \cdot 10^{22} (g_1)$	$8/3$
$(8, 2, -1/2)$	$\bar{Q}_R \sigma_{\mu\nu} \ell_L G^{\mu\nu}$	$6.7 \cdot 10^{27} (g_1)$	$4/3$
$(15, 1, -1/3)$	$\bar{Q}_L \sigma_{\mu\nu} d_R G^{\mu\nu}$	$8.3 \cdot 10^{21} (g_3)$	$1/6$
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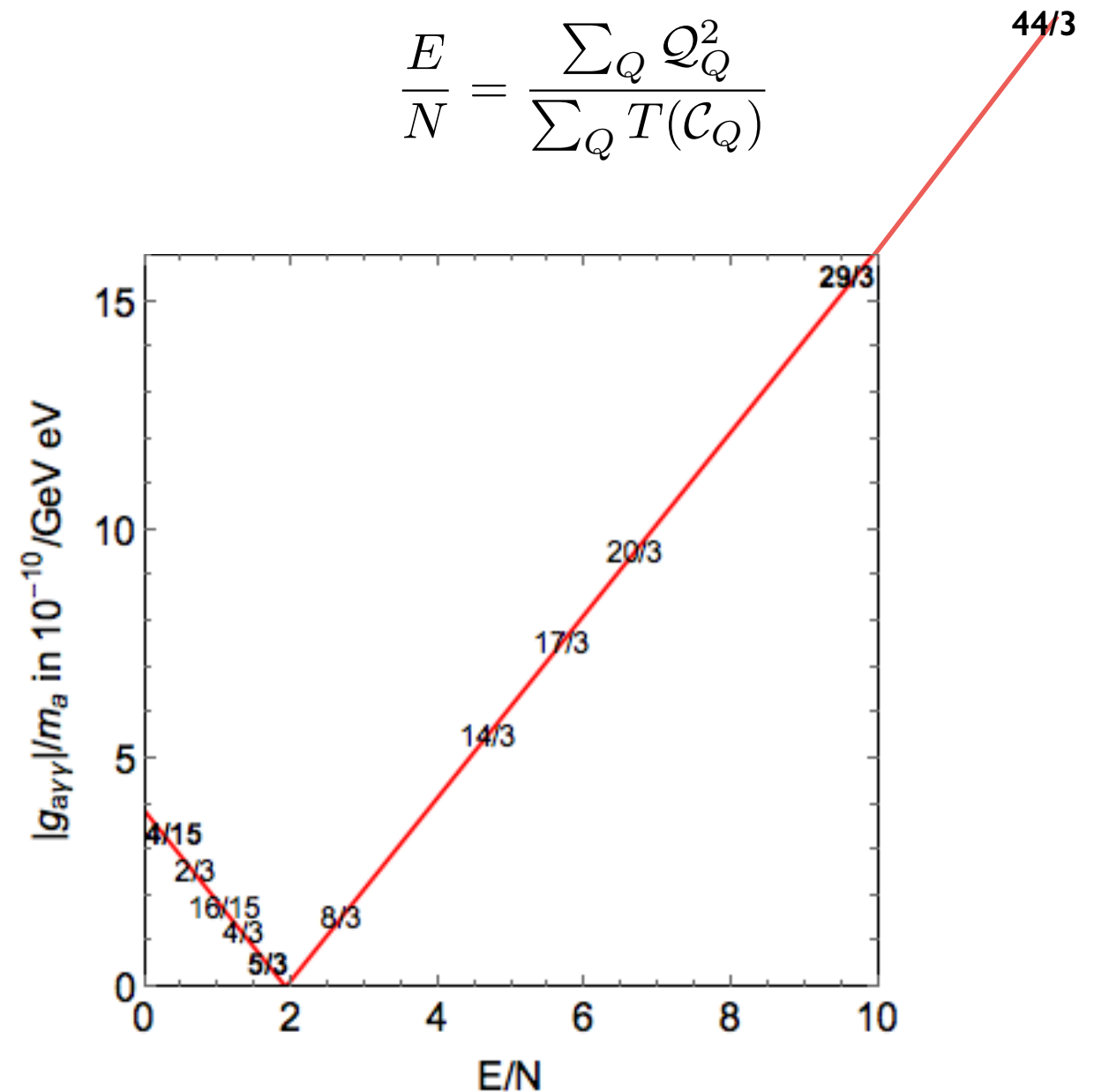
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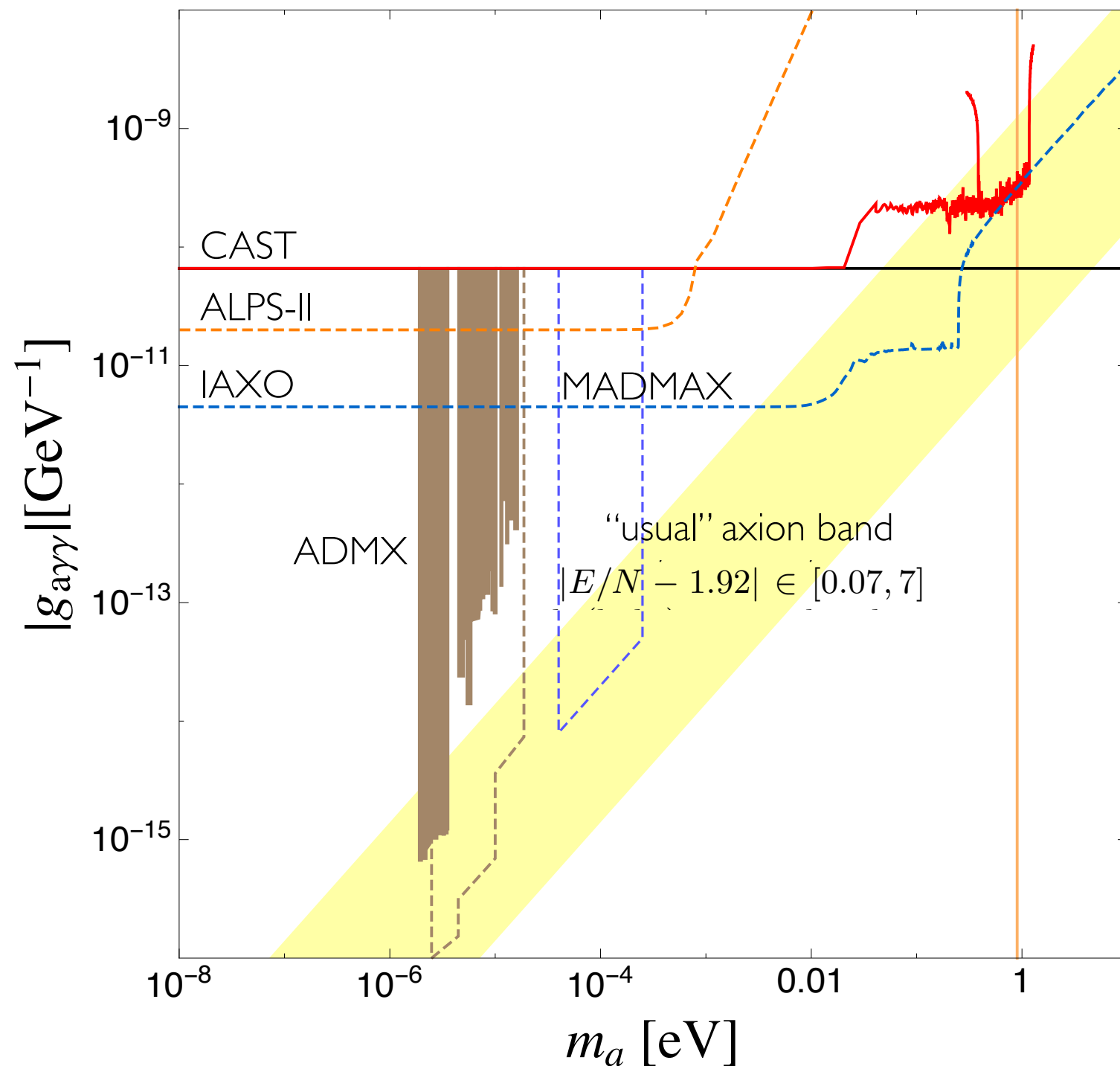
$$g_{a\gamma\gamma} = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E}{N} - 1.92(4) \right)$$

$$\frac{E}{N} = \frac{\sum_Q \mathcal{Q}_Q^2}{\sum_Q T(\mathcal{C}_Q)}$$

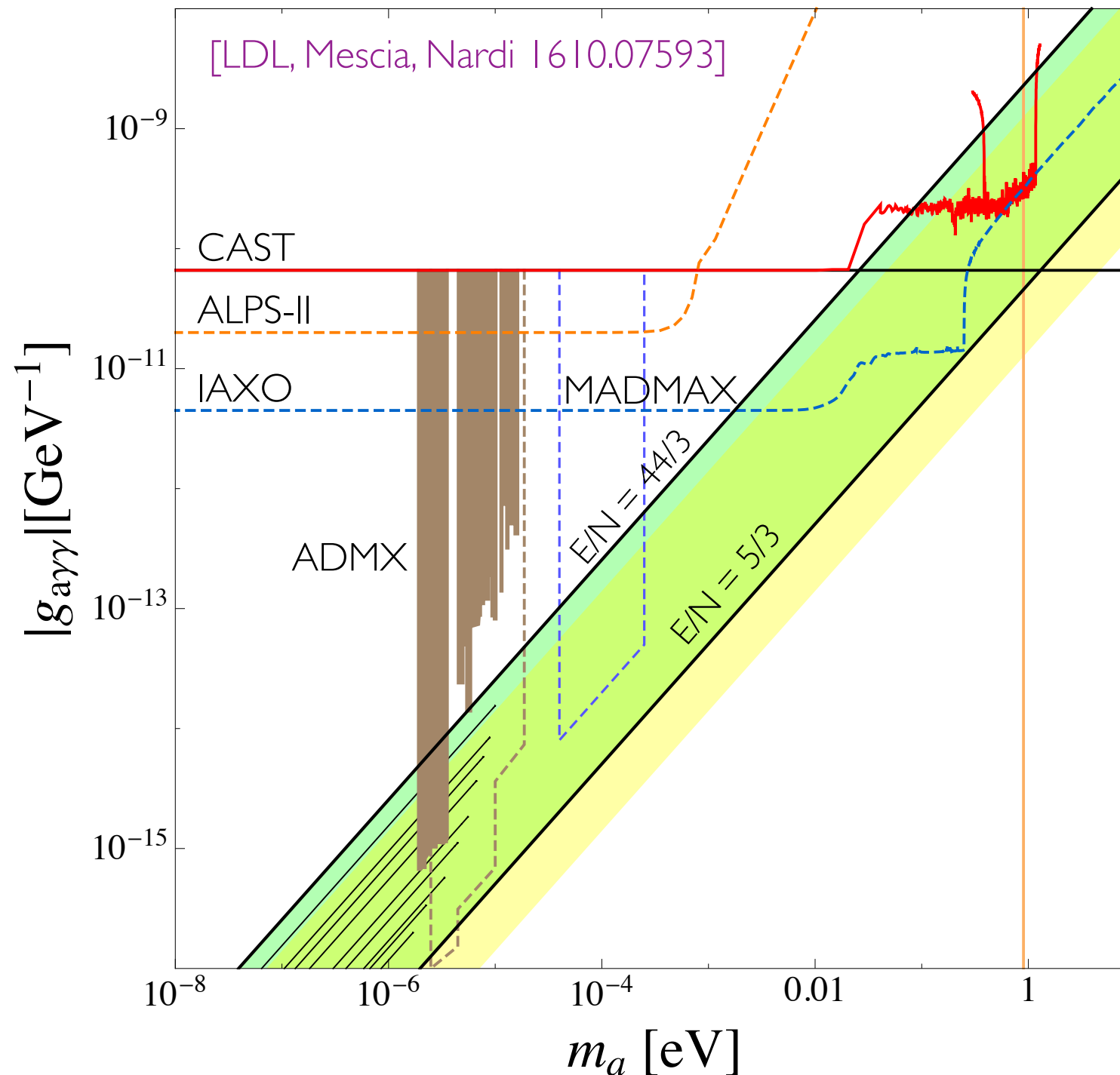
	R_Q	\mathcal{O}_{Qq}	$\Lambda_{\text{Landau}}^{2\text{-loop}} [\text{GeV}]$	E/N
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Redefining the axion window



Redefining the axion window



More Q's

- What happens for $N_Q > 1$?

- combined anomaly factor for $R_Q^1 + R_Q^2 + \dots$: $\frac{E_c}{N_c} = \frac{E_1 + E_2 + \dots}{N_1 + N_2 + \dots}$

- Strongest coupling (compatible with LP criterium)

$$(3, 3, -4/3) \oplus (3, 3, -1/3) \ominus (\bar{6}, 1, -1/3) \quad \longrightarrow \quad E_c/N_c = 170/3$$

- Complete decoupling within theoretical errors possible as well:

$$\left. \begin{array}{l} (3, 3, -1/3) \oplus (\bar{6}, 1, -1/3) \\ (\bar{6}, 1, 2/3) \oplus (8, 1, -1) \\ (3, 2, -5/6) \oplus (8, 2, -1/2) \end{array} \right\} \quad E_c/N_c = (23/12, 64/33, 41/21) \approx (1.92, 1.94, 1.95)$$

$$g_{a\gamma\gamma} = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E_c}{N_c} - 1.92(4) \right)$$

[Theoretical error from NLO χ PT
Grilli di Cortona et al., 1511.02867]

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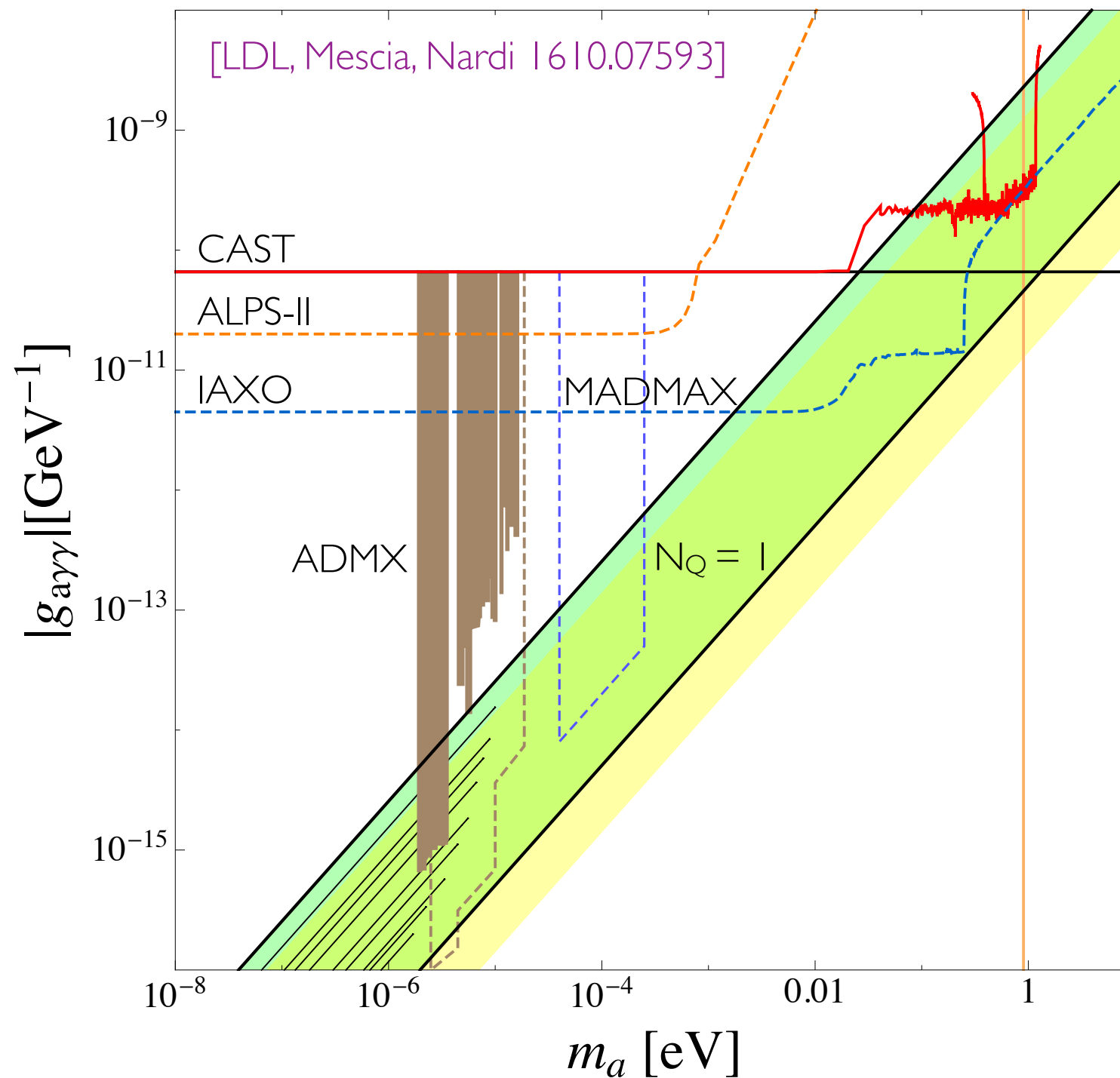
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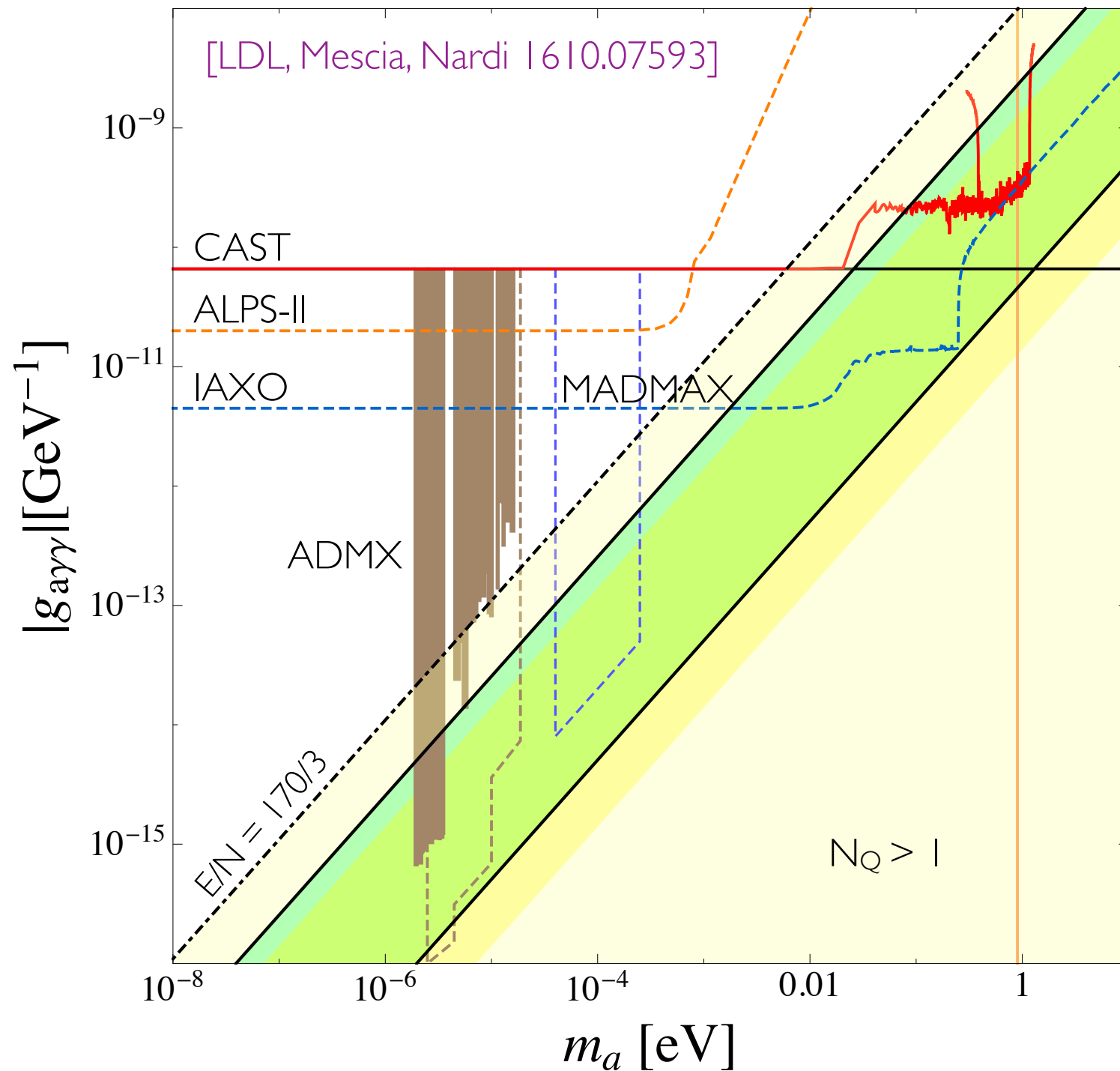
“such a cancellation is immoral, but not unnatural”

[D. B. Kaplan, (1985)]

More Q's



More Q's



DFSZ-like axions

- Potentially large E/N due to electron PQ charge

$$\frac{E}{N} = \frac{\sum_j \left(\frac{4}{3} X_u^j + \frac{1}{3} X_d^j + X_e^j \right)}{\sum_j \left(\frac{1}{2} X_u^j + \frac{1}{2} X_d^j \right)}$$

$$u_R^j \rightarrow \exp(i X_{uj}) u_R^j$$

$$d_R^j \rightarrow \exp(i X_{dj}) d_R^j$$

$$e_R^j \rightarrow \exp(i X_{ej}) e_R^j$$

- with n_H Higgs doublets and a SM singlet Φ , enhanced global symmetry

$$U(1)^{n_H+1} \rightarrow U(1)_{\text{PQ}} \times U(1)_Y$$

must be explicitly broken in the scalar potential via non-trivial invariants (e.g. $H_u H_d \Phi^2$)



non-trivial constraints on PQ charges of SM fermions

DFSZ-like axions

- Potentially large E/N due to electron PQ charge

$$\frac{E}{N} = \frac{\sum_j \left(\frac{4}{3} X_u^j + \frac{1}{3} X_d^j + X_e^j \right)}{\sum_j \left(\frac{1}{2} X_u^j + \frac{1}{2} X_d^j \right)}$$

$$\mathcal{L}_Y = Y_u \bar{Q}_L u_R H_u + Y_d \bar{Q}_L d_R H_d + Y_e \bar{L}_L e_R H_e + \text{h.c.}$$

- With 2 or 3 Higgs doublets, DFSZ remains within $N_Q = 1$ KSVZ window

- $n_H = 2$

DFSZ-I : $X_e = X_d$ $E/N = 8/3$

DFSZ-II : $X_e = -X_u$ $E/N = 2/3$

- $n_H = 3$

DFSZ-III : $X_e \neq X_{u,d}$ $E/N_{(\text{max})} = -4/3$

DFSZ-like axions

- Potentially large E/N due to electron PQ charge

$$\frac{E}{N} = \frac{\sum_j \left(\frac{4}{3} X_u^j + \frac{1}{3} X_d^j + X_e^j \right)}{\sum_j \left(\frac{1}{2} X_u^j + \frac{1}{2} X_d^j \right)}$$

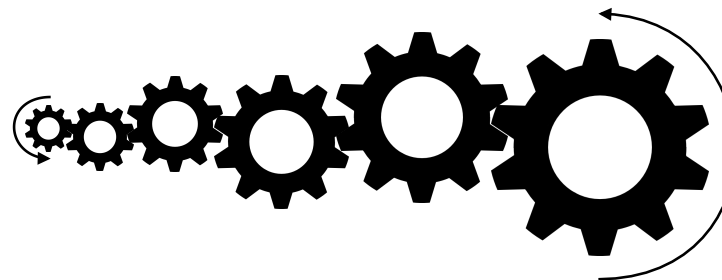
$$\mathcal{L}_Y = Y_u \bar{Q}_L u_R H_u + Y_d \bar{Q}_L d_R H_d + Y_e \bar{L}_L e_R H_e + \text{h.c.}$$

- With 2 or 3 Higgs doublets, DFSZ remains within $N_Q = 1$ KSVZ window
- Clockwork-like scenarios allow to **boost** E/N
 - n up-type doublets which *do not couple* to SM fermions ($n \lesssim 50$ from LP condition)

$$(H_u H_d \Phi^2)$$

$$(H_k H_{k-1}^*)(H_{k-1}^* H_d^*)$$

$$(H_e H_n)(H_n H_d)$$



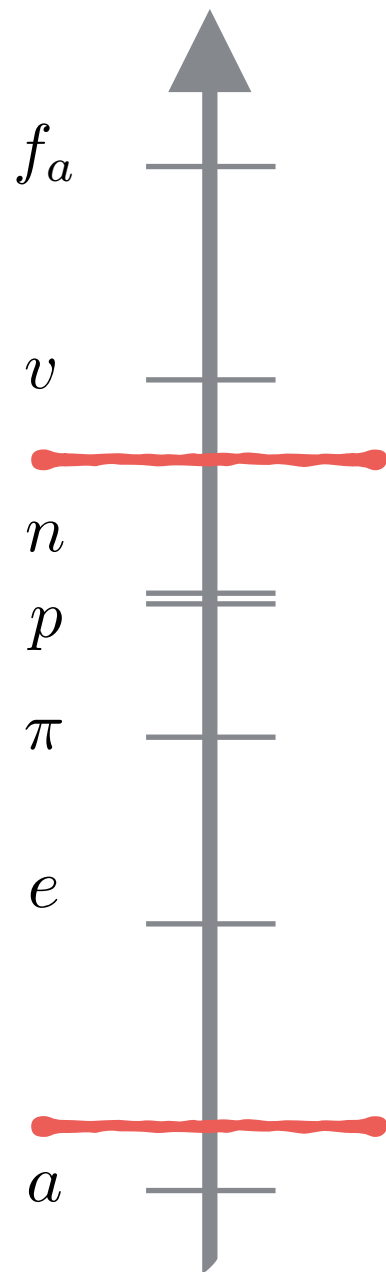
$$E/N \sim 2^n$$

[See also Farina et al. 1611.09855, for KSVZ clockwork]

Axion couplings to matter

- Axion-nucleons couplings

[Kaplan NPB 260 (1985), Srednicki NPB 260 (1985), ...
Grilli di Cortona et al. I511.02867]



$$\mathcal{L}_a \supset \frac{a}{f_a} \frac{\alpha_s}{8\pi} G_{\mu\nu} \tilde{G}^{\mu\nu} + \frac{\partial_\mu a}{2f_s} c_q^0 \bar{q} \gamma^\mu \gamma_5 q$$

$$c_q^0 = 0 \quad (\text{KSVZ})$$

$$c_{u,c,t}^0 = \frac{1}{3} \sin^2 \beta = \frac{1}{3} - c_{d,s,b}^0 \quad (\text{DFSZ})$$

EFT-I: quarks and gluons

$$\mathcal{L}_N \supset \bar{N} v^\mu D_\mu N + 2g_A A_\mu^i \bar{N} S^\mu \sigma^i N + 2g_0^{u+d} \hat{A}_\mu^{u+d} \bar{N} S^\mu N$$

$$A_\mu^3 = c_{(u-d)/2} \frac{\partial_\mu a}{2f_a} \quad (\text{iso-vector})$$

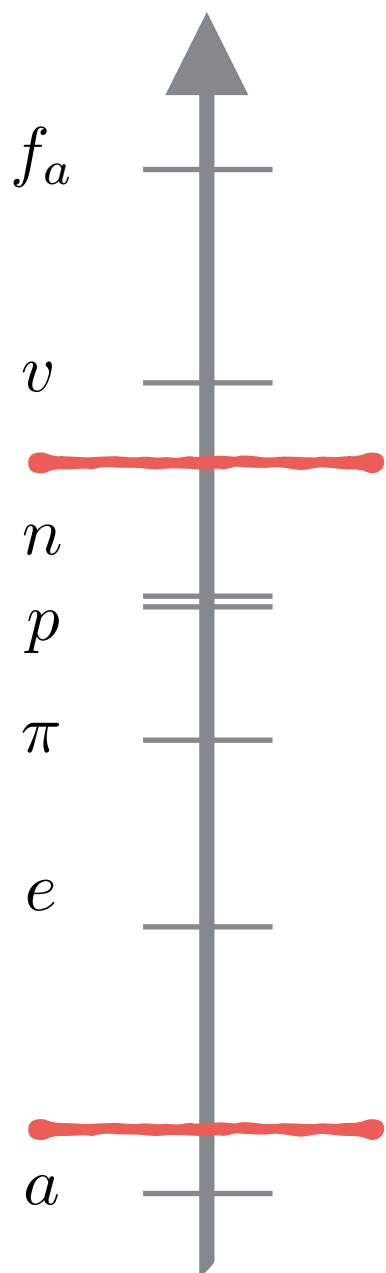
$$\hat{A}_\mu^{u+d} = c_{(u+d)/2} \frac{\partial_\mu a}{2f_a} \quad (\text{iso-scalar})$$

EFT-II: non-relativistic nucleons (Galilean group + isospin)

Axion couplings to matter

- Axion-nucleons couplings

[Kaplan NPB 260 (1985), Srednicki NPB 260 (1985), ...
Grilli di Cortona et al. I511.02867]



Matching over a single-nucleon state

$$\langle p | \mathcal{L}_a | p \rangle = \langle p | \mathcal{L}_N | p \rangle$$



$$s^\mu \Delta q \equiv \langle p | \bar{q} \gamma_\mu \gamma_5 | p \rangle$$

$$g_A = \Delta u - \Delta d = 1.2723(23) \quad (\beta\text{-decay})$$

$$g_0^{u+d} = \Delta u + \Delta d = 0.541(50) \quad (\text{Lattice})$$

$$\frac{\partial_\mu a}{2f_a} c_N \bar{N} \gamma^\mu \gamma_5 N$$

$$c_p = -0.47(3) + 0.88(3)c_u^0 - 0.39(2)c_d^0 - 0.038(5)c_s^0$$

$$- 0.012(5)c_c^0 - 0.009(2)c_b^0 - 0.0035(4)c_t^0,$$

$$c_n = -0.02(3) + 0.88(3)c_d^0 - 0.39(2)c_u^0 - 0.038(5)c_s^0$$

$$- 0.012(5)c_c^0 - 0.009(2)c_b^0 - 0.0035(4)c_t^0,$$

model-independent

The Nucleophobic axion

- Is it possible to suppress simultaneously both c_p and c_n ?

$$\frac{\partial_\mu a}{2f_a} c_N \bar{N} \gamma^\mu \gamma_5 N \quad \begin{aligned} c_p + c_n &= (c_u^0 + c_d^0 - 1) (\Delta u + \Delta d) && \text{(2-flavours, no-running)} \\ c_p - c_n &= (c_u^0 - c_d^0 + \underbrace{\frac{m_u - m_d}{m_u + m_d}}_{-0.35}) (\Delta u - \Delta d) \end{aligned}$$

- KSVZ: $c_{u,d}^0 = 0$

- DFSZ: $c_u^0 + c_d^0 = \frac{1}{N_f} \quad (N_f = 3)$

→ theorem: nucleophobia requires non-universal DFSZ

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→ theorem: nucleophobia requires non-universal DFSZ

- Some applications: *[work in progress]*

- Relaxation of SN bound (improved sensitivity @ IAXO)

- Low $f_a \sim 10^8$ GeV can help in explaining stellar cooling anomalies [Giannotti et al. 1708.02111]

- Interplay with flavour observables (e.g. $K \rightarrow \pi a$)

Conclusions

- The QCD axion is a well-motivated BSM scenario
 - solves the strong CP problem
 - provides an excellent DM candidate
 - Healthy experimental program
 - experiments are entering now the preferred window for the QCD axion
 - outburst of ideas in the recent years
- *Take home message: axion couplings might sizeably deviate from the standard DFSZ/KSVZ benchmarks (relevant when confronting exp. sensitivities and bounds)*

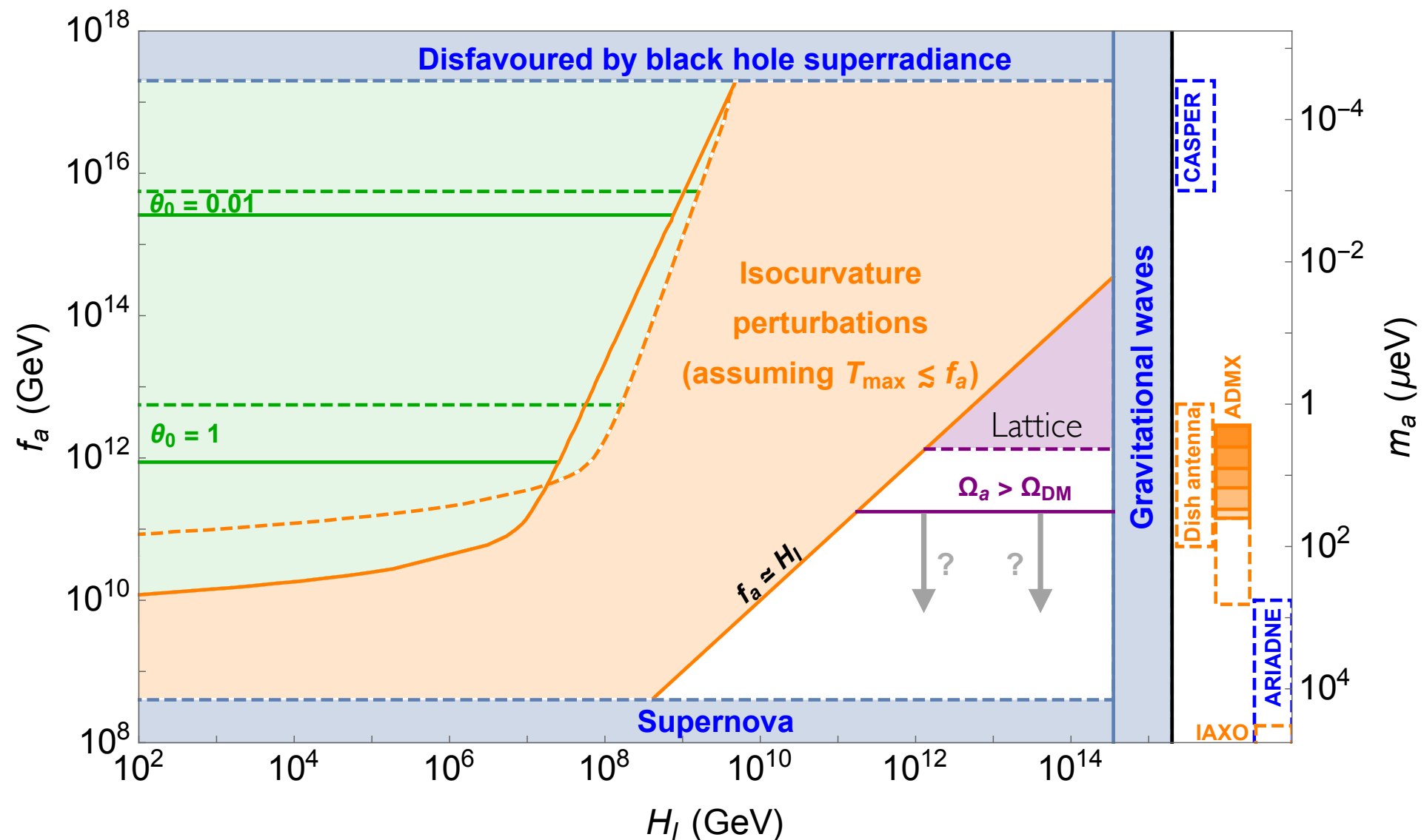
Backup slides

Pre-inflationary scenarios

- What about $T_{\text{reheating}} < m_Q$?
 - condition on Q decay is relaxed, but Landau pole still applies
- $m_Q \sim y_Q f_a < 5 \cdot 10^{11} \text{ GeV}$
 - $N_Q = 1$: $(E/N)_{\text{max(pre)}} = 2.5 (E/N)_{\text{max(post)}}$
 - $N_Q > 1$: $(E/N)_{\text{max(pre)}} = 1.2 (E/N)_{\text{max(post)}}$
 - ➔ *axion-photon coupling well-described by post-inflationary axion window*
- $f_a \gg 5 \cdot 10^{11} \text{ GeV}$ (requires $\theta_0 \ll 1$)
 - ➔ *arbitrarily large axion-photon coupling at the cost of tuning initial mis. condition*

Relic abundance from mis. mechanism

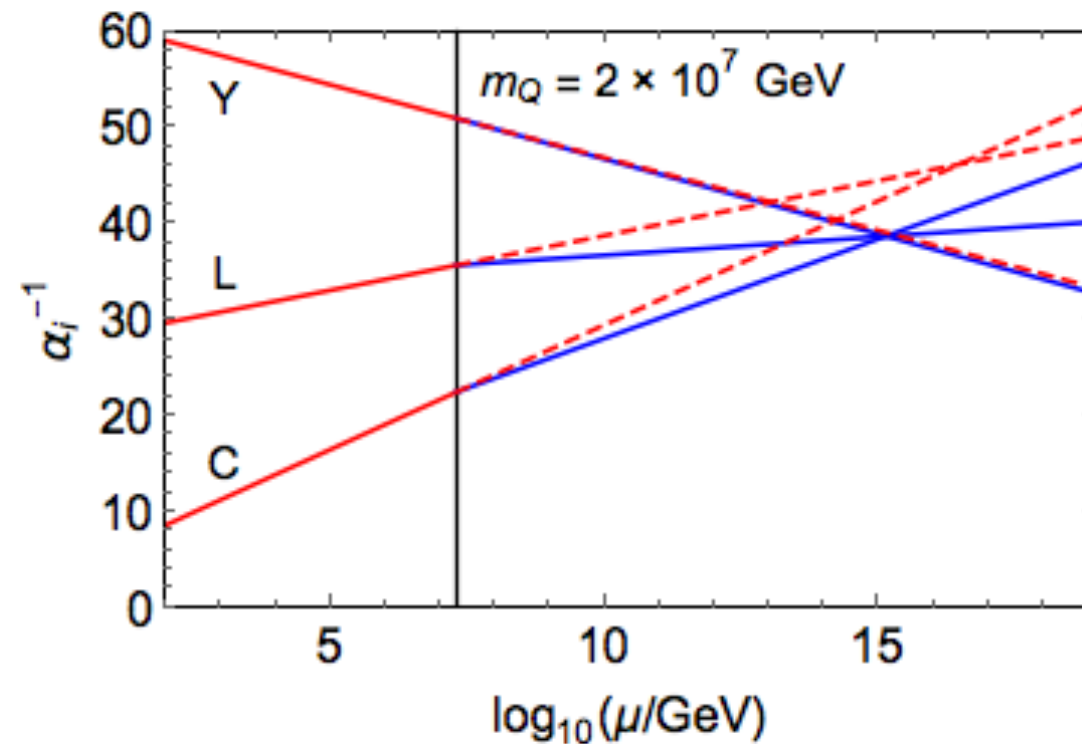
- Upper limit from recent lattice QCD calculations: $f_a \lesssim 10^{11 \div 12}$ GeV for $\theta_0 = \mathcal{O}(1)$



[Grilli di Cortona et al. 1511.02867]

Unificaxion

- Some Q's might improve gauge coupling unification [Giudice, Rattazzi, Strumia, 1204.5465]
 - out of all our 15 cases, just one works well: $Q \sim (3, 2, 1/6)$



Unificaxion

- Some Q 's might improve gauge coupling unification [Giudice, Rattazzi, Strumia, 1204.5465]
 - out of all our 15 cases, just one works well: $Q \sim (3, 2, 1/6)$
- Conceiving a UV model remains, however, a non-trivial challenge
 - $Q \in \psi_{\text{GUT}}$
 - $m_Q \lesssim f_a \ll M_{\text{GUT}}$

$$[\text{PQ}, \text{GUT}] = 0$$

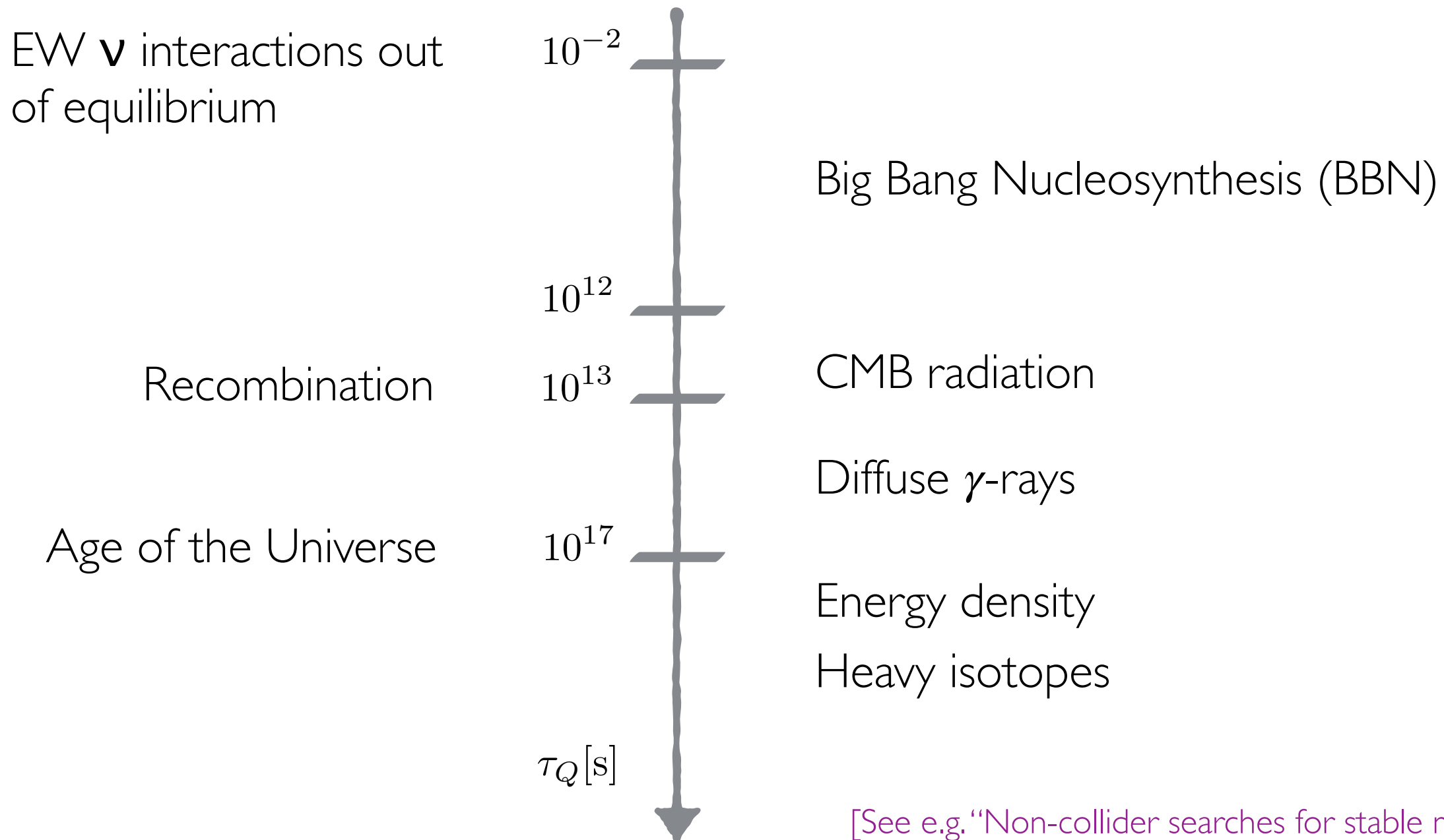


$$m_{\psi_{\text{GUT}}} = \mathcal{O}(f_a)$$

- a complete GUT multiplet doesn't help !

Cosmological constraints

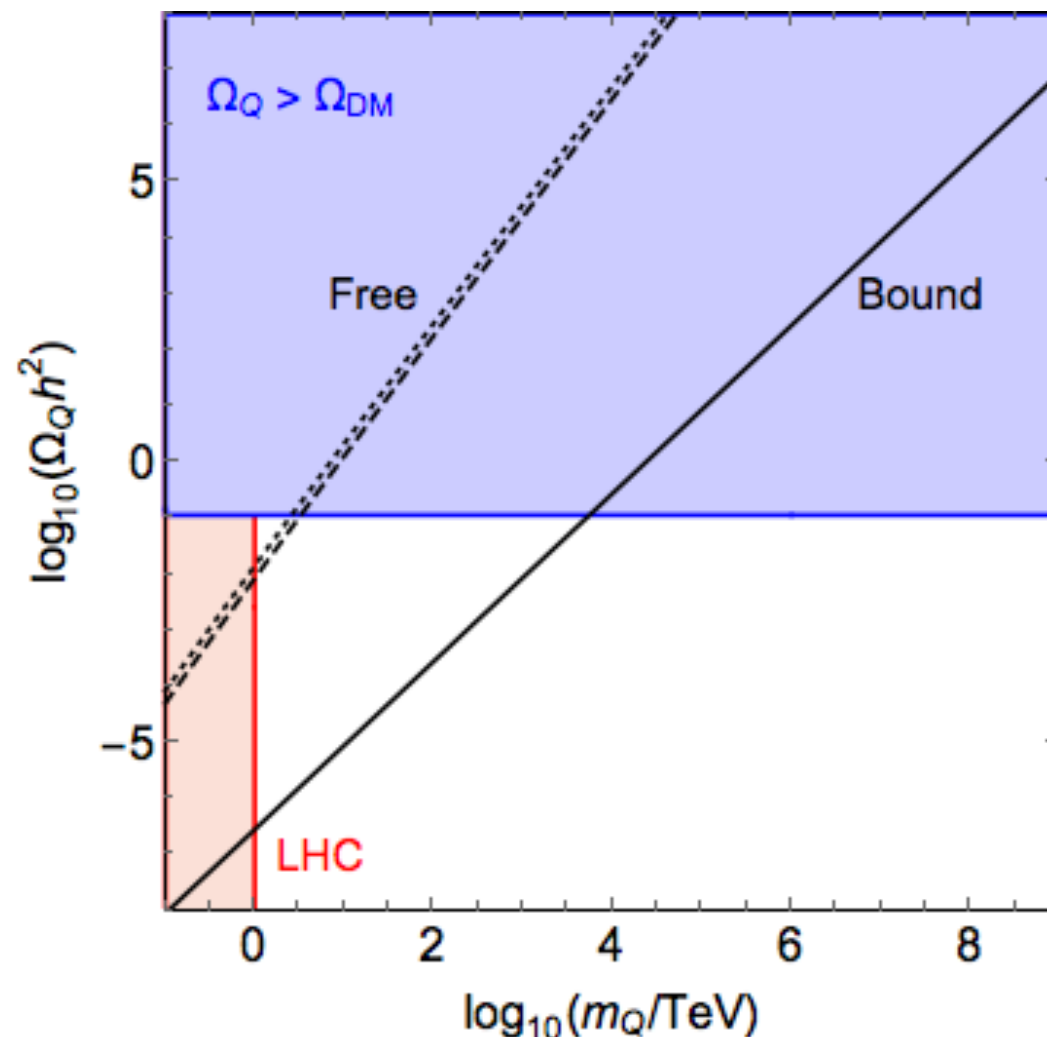
- Long-lived and strongly-interacting particles are severely bounded by cosmology



[See e.g. “Non-collider searches for stable massive particles”,
Burdin et al. Physics Reports 582 (2015) 1–52]

Heavy Q's relic density

- $T_{\text{reheating}} > m_Q$ (thermal distribution of Q's as initial condition)
- Reliable estimates on Ω_Q remain an **open issue**, but Q abundances too high



[Rich literature: e.g.
Dover, Gaiser, Steigman PRL 42 (1979),
Nardi, Roulet PLB 245 (1990),
Arvanitaki et al., hep-ph/0504210,
Kang, Luty, Nasri, hep-ph/0611322,
Jacob, Nussinov, 0712.2681
Kusakabe, Takesako, 1112.0860]

Axion coupling to photons

- Axion effective Lagrangian

See e.g. 1511.02867

$$\mathcal{L}_a = \frac{1}{2}(\partial_\mu a)^2 + \frac{a}{f_a} \frac{\alpha_s}{8\pi} G_{\mu\nu} \tilde{G}^{\mu\nu} + \frac{1}{4} a g_{a\gamma\gamma}^0 F_{\mu\nu} \tilde{F}^{\mu\nu} \quad g_{a\gamma\gamma}^0 = \frac{\alpha_{em}}{2\pi f_a} \frac{E}{N}$$

- field depended chiral transformation to eliminate aGGtilde $q = \begin{pmatrix} u \\ d \end{pmatrix} \rightarrow e^{i\gamma_5 \frac{a}{2f_a} Q_a} \begin{pmatrix} u \\ d \end{pmatrix}$

$$\text{tr } Q_a = 1$$



$$\mathcal{L}_a = \frac{1}{2}(\partial_\mu a)^2 + \frac{1}{4} a g_{a\gamma\gamma} F_{\mu\nu} \tilde{F}^{\mu\nu} - \bar{q}_L M_a q_R + h.c.$$

$$M_a = e^{i\frac{a}{2f_a} Q_a} M_q e^{i\frac{a}{2f_a} Q_a}, \quad M_q = \begin{pmatrix} m_u & 0 \\ 0 & m_d \end{pmatrix}, \quad Q = \begin{pmatrix} \frac{2}{3} & 0 \\ 0 & -\frac{1}{3} \end{pmatrix}$$

$$Q_a = \frac{M_q^{-1}}{\langle M_q^{-1} \rangle} \quad (\text{no axion-pion mixing})$$

$$g_{a\gamma\gamma} = \frac{\alpha_{em}}{2\pi f_a} \left[\frac{E}{N} - 6 \text{tr} (Q_a Q^2) \right] = \frac{\alpha_{em}}{2\pi f_a} \left[\frac{E}{N} - \frac{2}{3} \frac{4m_d + m_u}{m_d + m_u} \right] = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E}{N} - 1.92(4) \right)$$