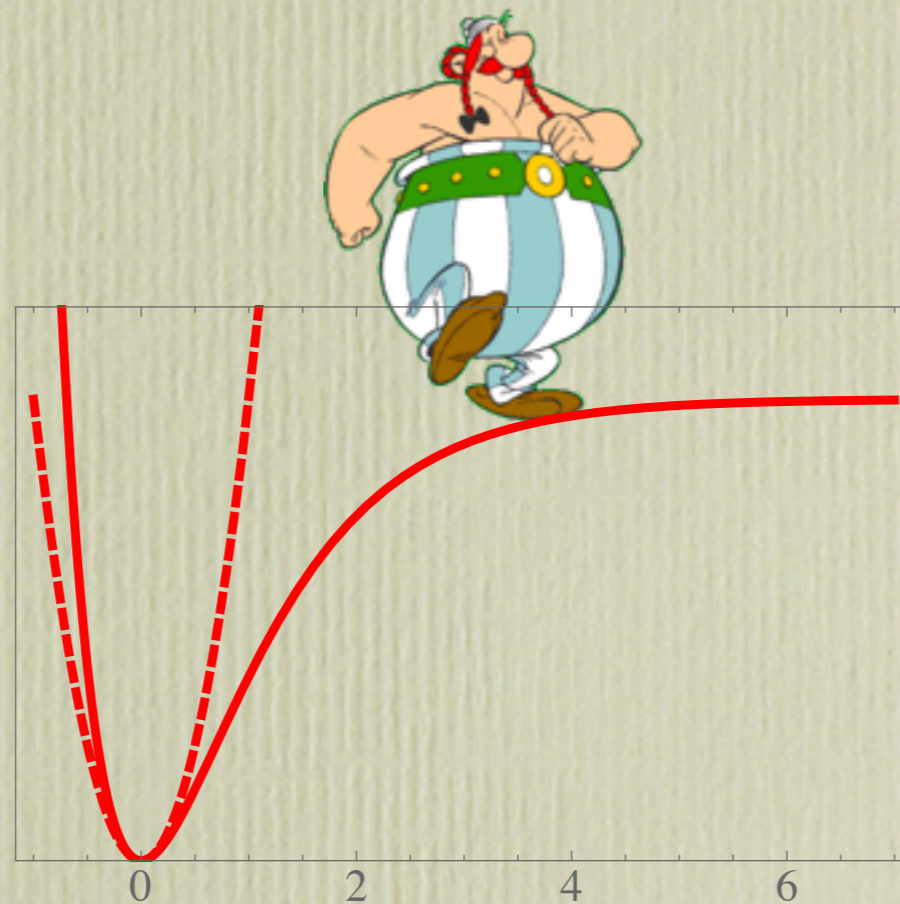


The Flattened Road to Acceleration in String Theory

with J. Moritz, A. Retolaza [1707.05830]

with R. Kallosh, A. Linde, D. Roest, Y. Yamada [1707.08678]



And work with: I. Ben-Dayana, W. Buchmüller, E. Dudas, K. Dutta, R. Flauger, L. Heurtier, E. Pajer, F. Pedro, F. Rühle, E. Silverstein, A. Uranga, C. Wieck, M. Winkler, T. Wrase, G. Xu

Alexander Westphal
(DESY)



slow-roll inflation ...

[Guth, Linde, Albrecht, Steinhardt '80s]

$$\cancel{\ddot{\phi}} + 3H\dot{\phi} = -\partial_{\phi}V \equiv -V' \quad , \quad H^2 = \frac{1}{3} \left(\frac{1}{2} \cancel{\dot{\phi}^2} + V \right)$$

$$a \sim e^{Ht}$$

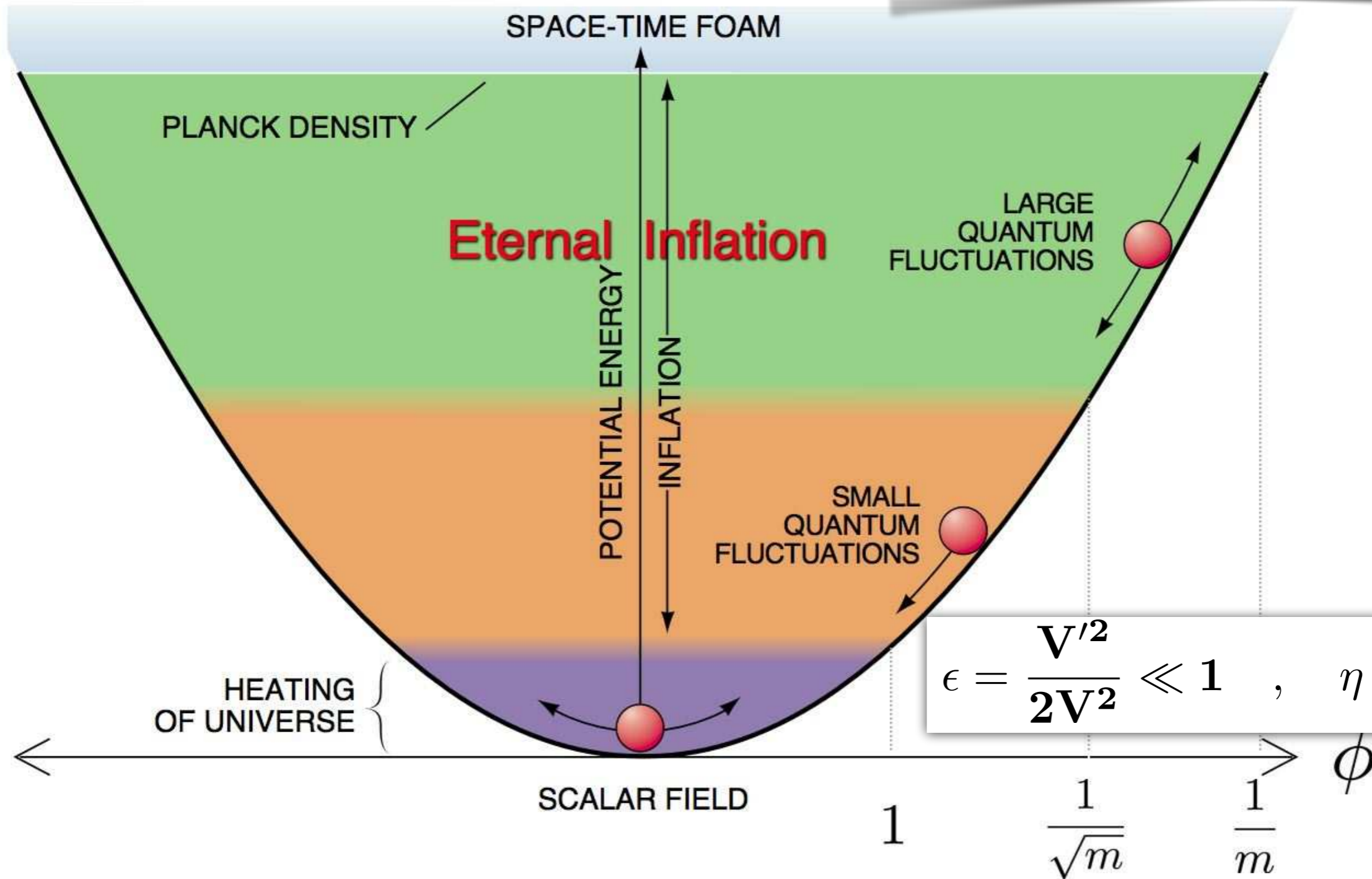
$$\epsilon = \frac{V'^2}{2V^2} \ll 1 \quad , \quad \eta = \frac{V''}{V} \ll 1$$

slow-roll inflation ...

[Guth, Linde, Albrecht, Steinhardt '80s]

$$V(\phi) = \frac{m^2}{2} \phi^2$$

$$3H\dot{\phi} \simeq -V' \quad , \quad H^2 \simeq \frac{1}{3}V$$



$$\epsilon = \frac{V'^2}{2V^2} \ll 1 \quad , \quad \eta = \frac{V''}{V} \ll 1$$

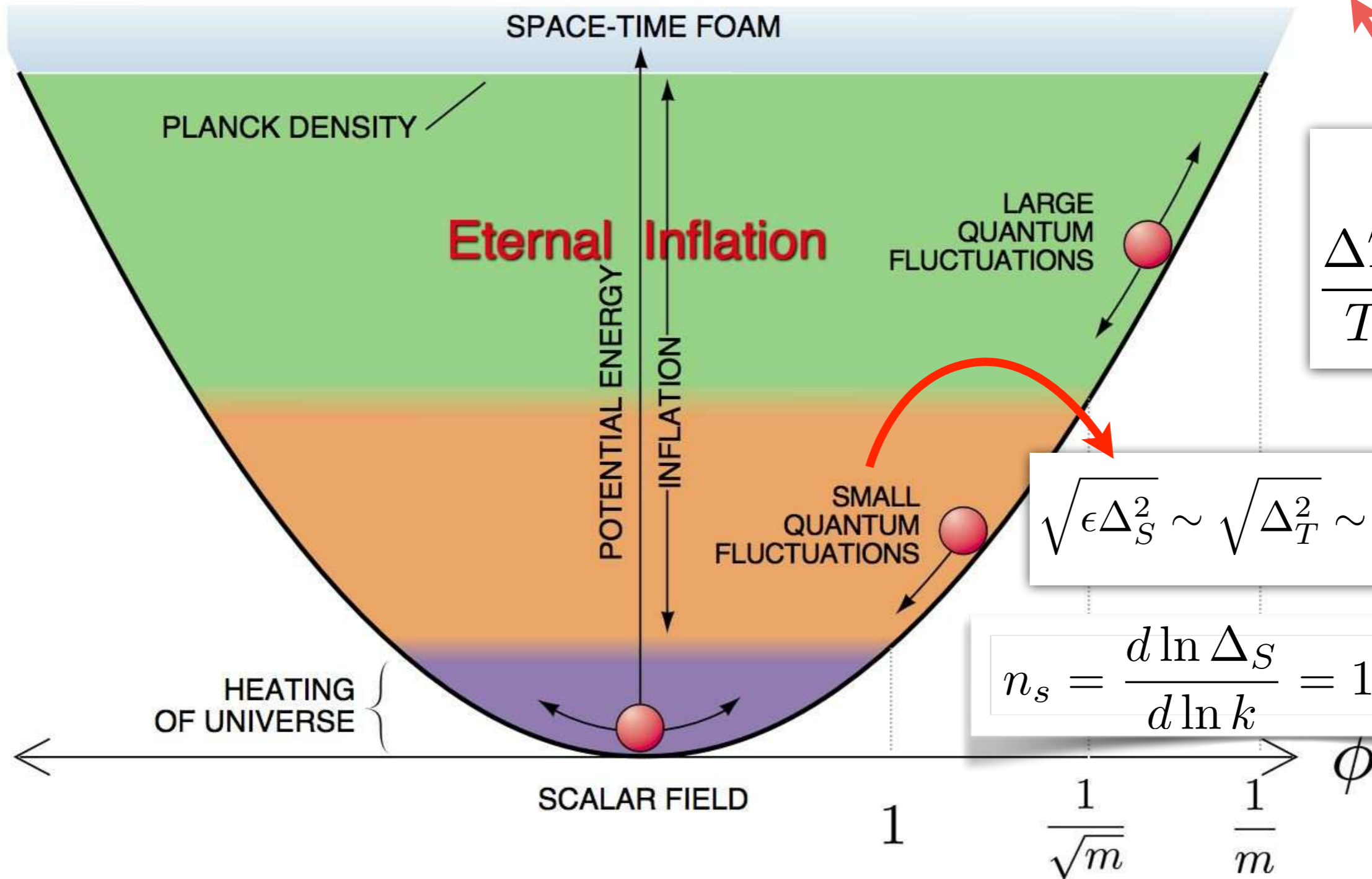
[picture from lecture notes: Linde '07]



slow-roll inflation ...

[Guth, Linde, Albrecht, Steinhardt '80s]

$$V(\phi) = \frac{m^2}{2} \phi^2 \quad m \sim 10^{13} \text{ GeV}$$



CMB:

$$\frac{\Delta T}{T} \sim 10^{-5}$$

$$\sqrt{\epsilon \Delta_S^2} \sim \sqrt{\Delta_T^2} \sim \frac{H}{M_P} \sim 10^{-5}$$

$$n_s = \frac{d \ln \Delta_S}{d \ln k} = 1 - 6\epsilon + 2\eta$$

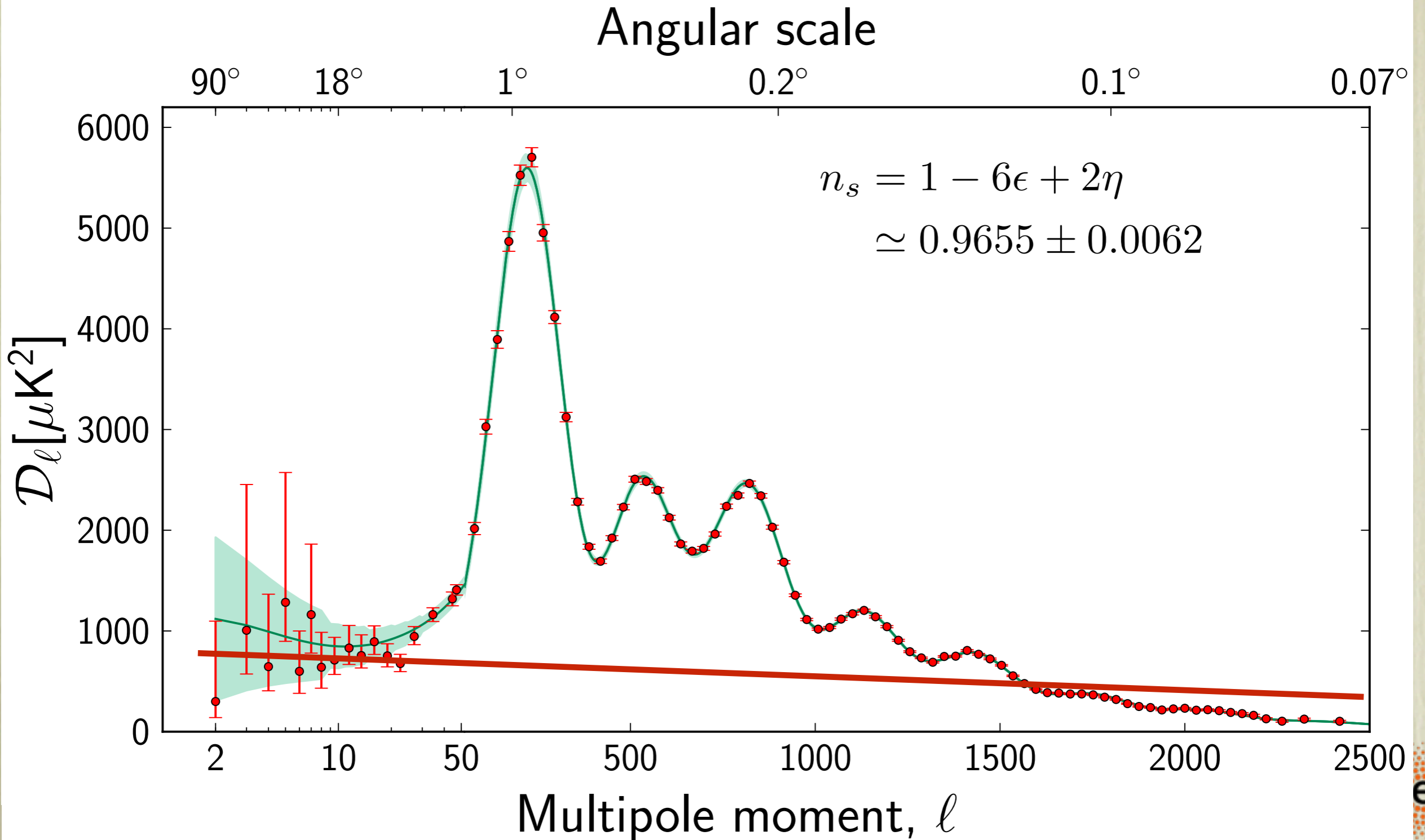
[picture from lecture notes: Linde '07]



slow-roll inflation ...

[Guth, Linde, Albrecht, Steinhardt '80s]

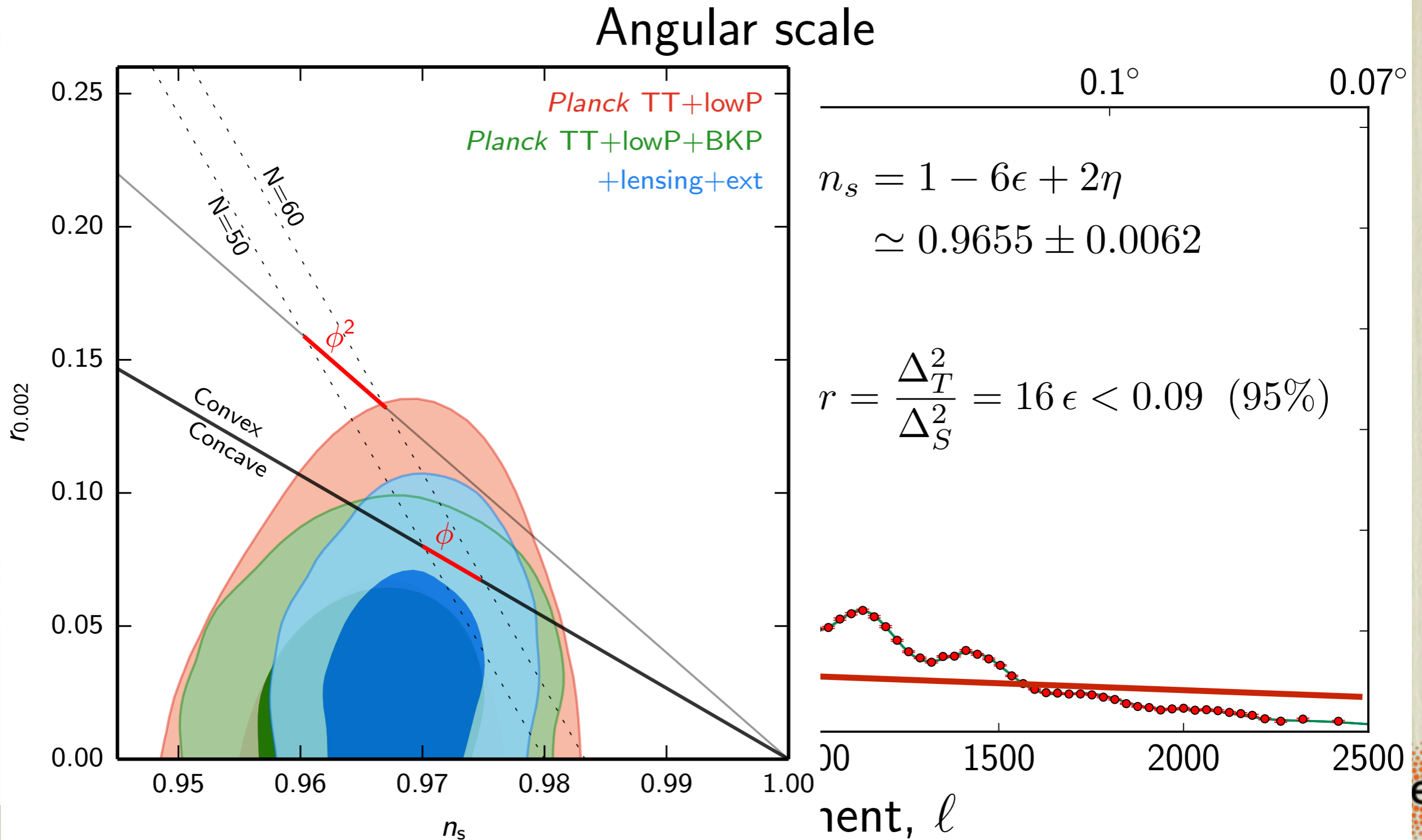
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slow-roll inflation ...

[Guth, Linde, Albrecht, Steinhardt '80s]

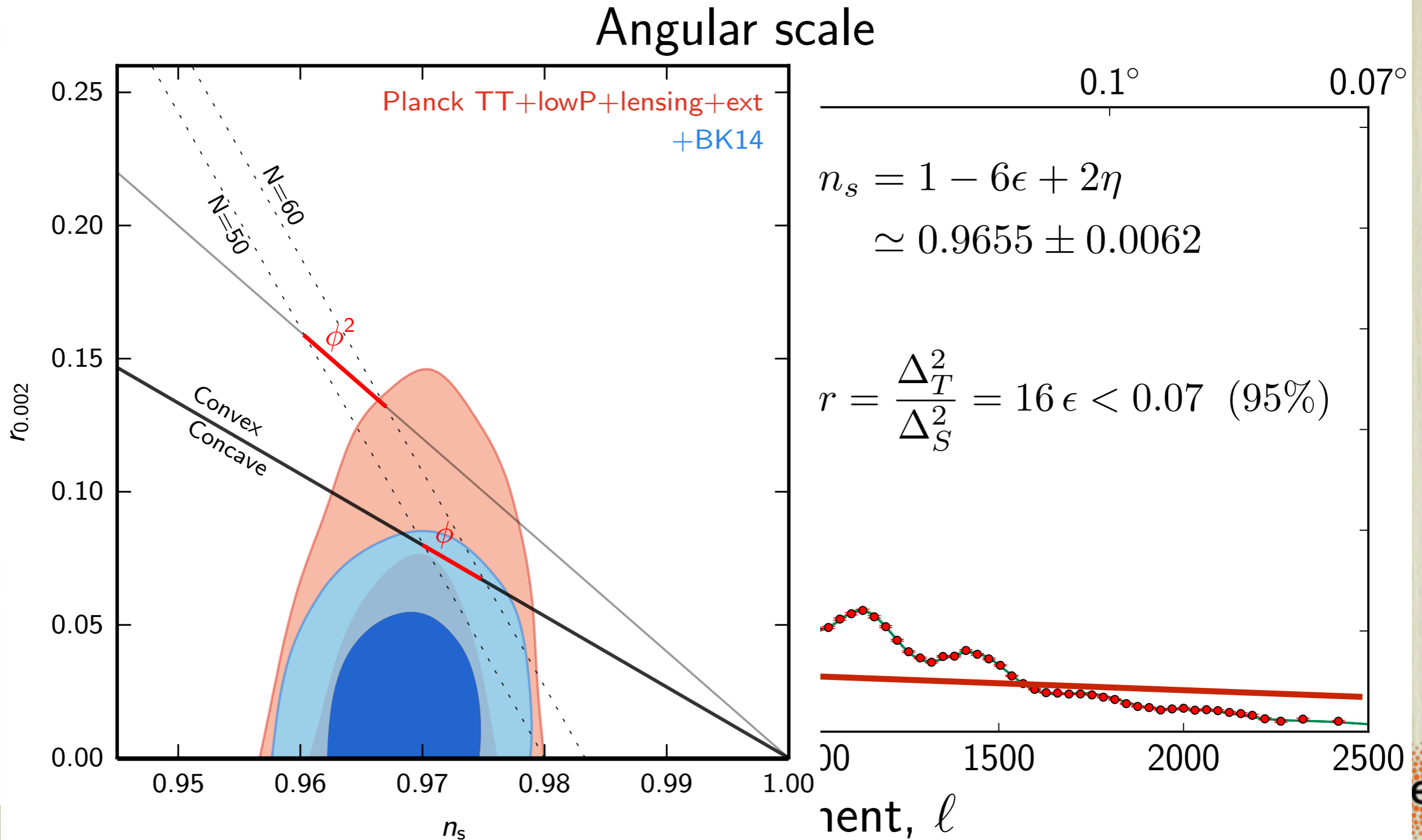
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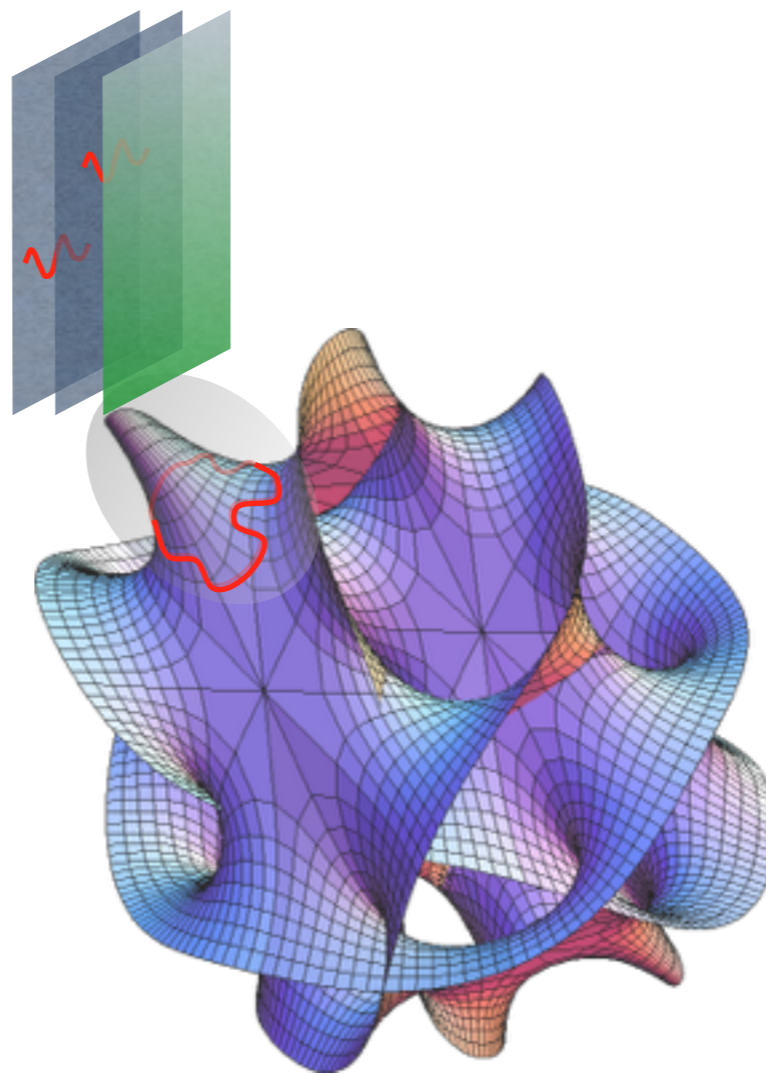
slow-roll inflation ...

[Guth, Linde, Albrecht, Steinhardt '80s]

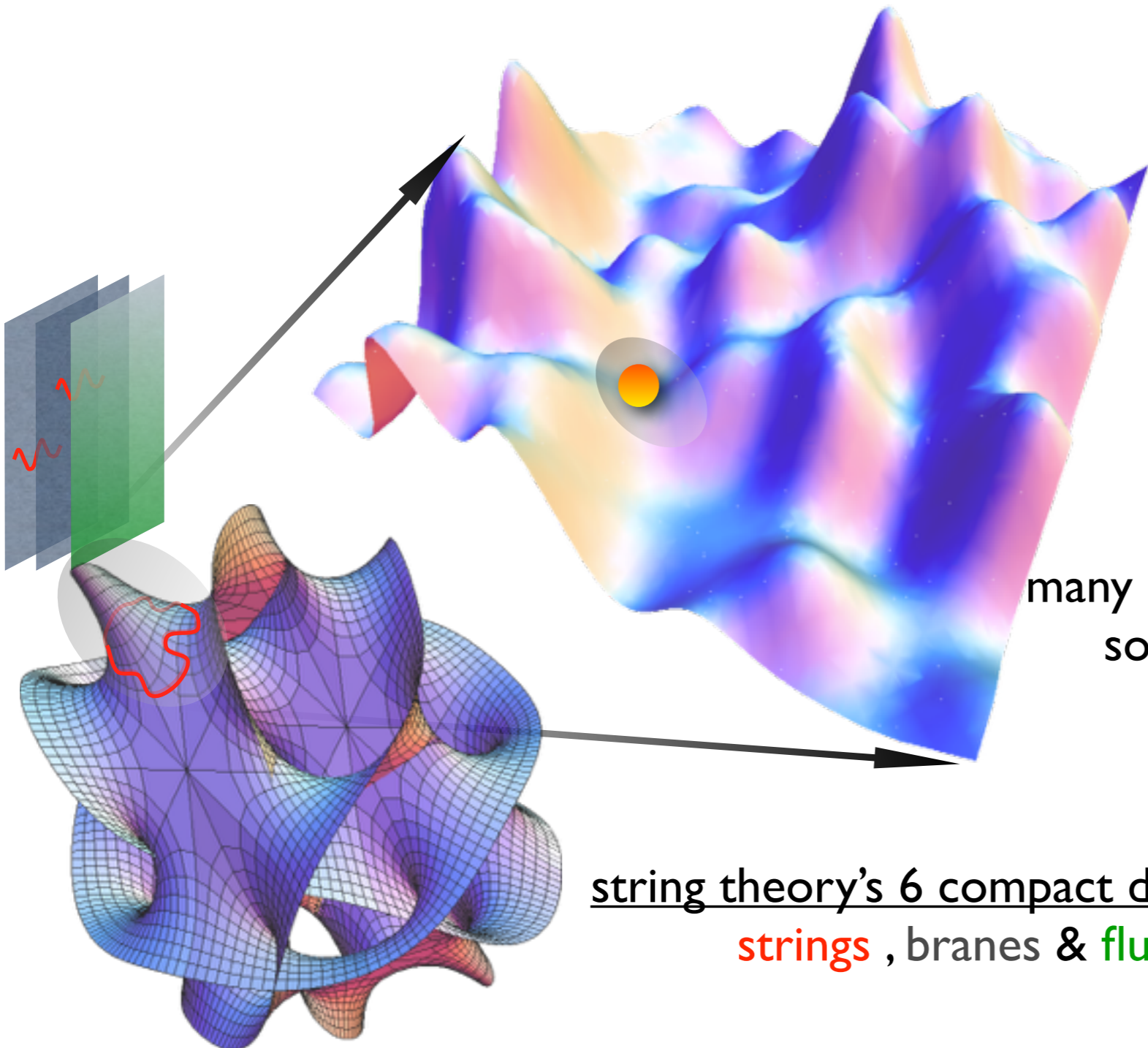
$$V(\phi) = \frac{m^2}{2} \phi^2$$



test string theory with inflation & CMB

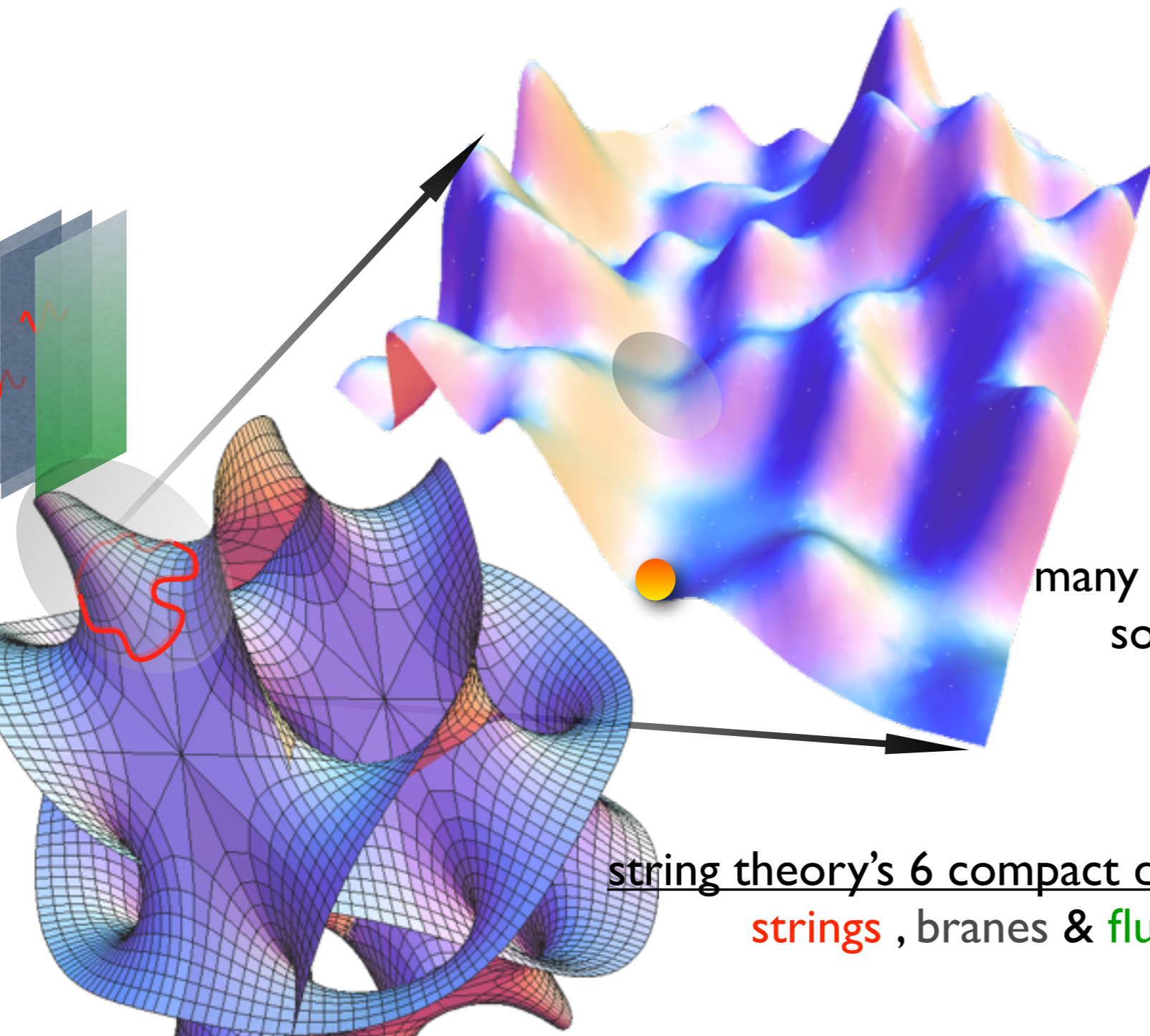


string theory's 6 compact dimensions:
strings , branes & **fluxes**



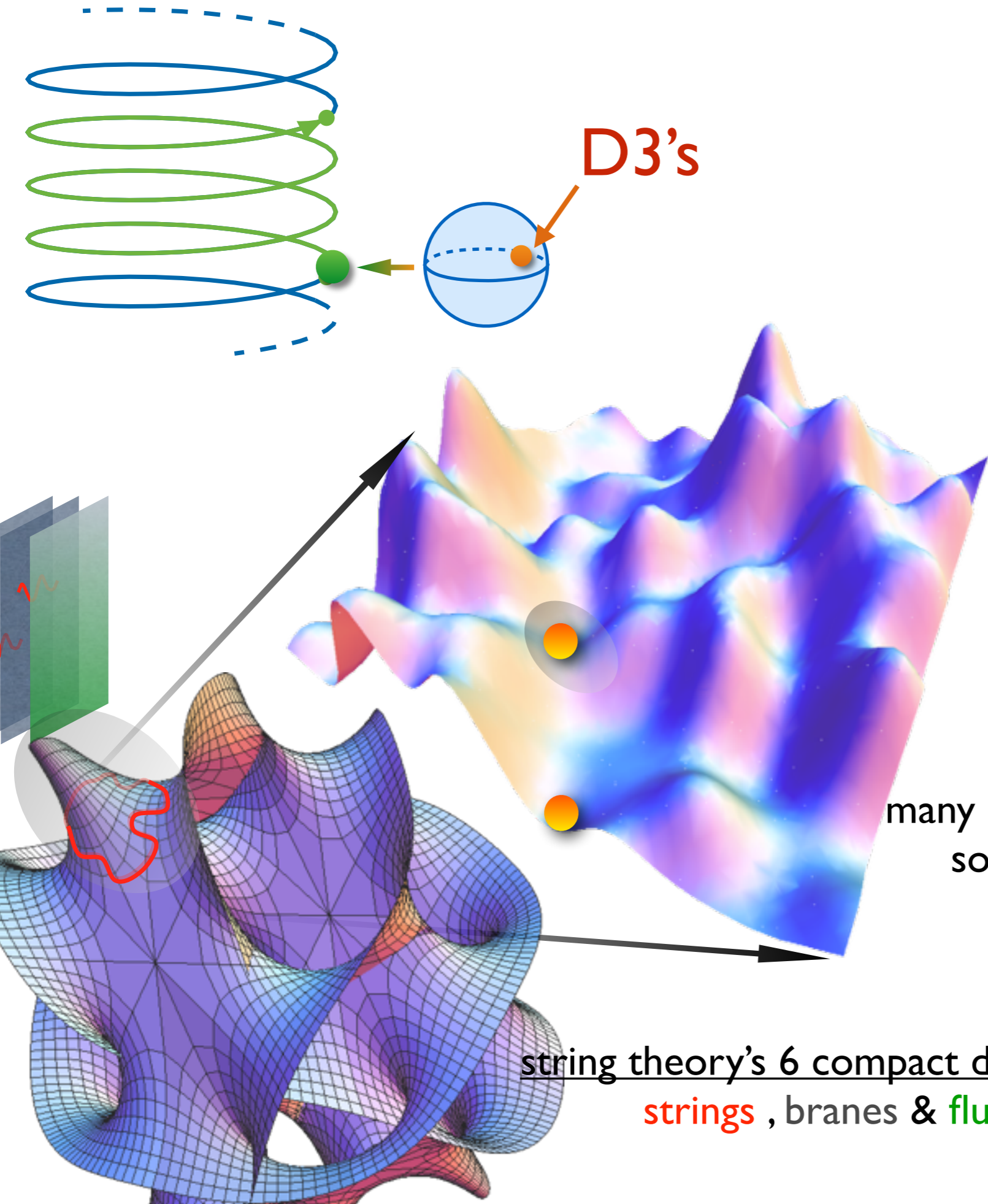
the string theory landscape:
many isolated *vacua*, connected by tunneling
some mountain slopes drive *inflation*

string theory's 6 compact dimensions:
strings , branes & **fluxes**



the string theory landscape:
many isolated *vacua*, connected by tunneling
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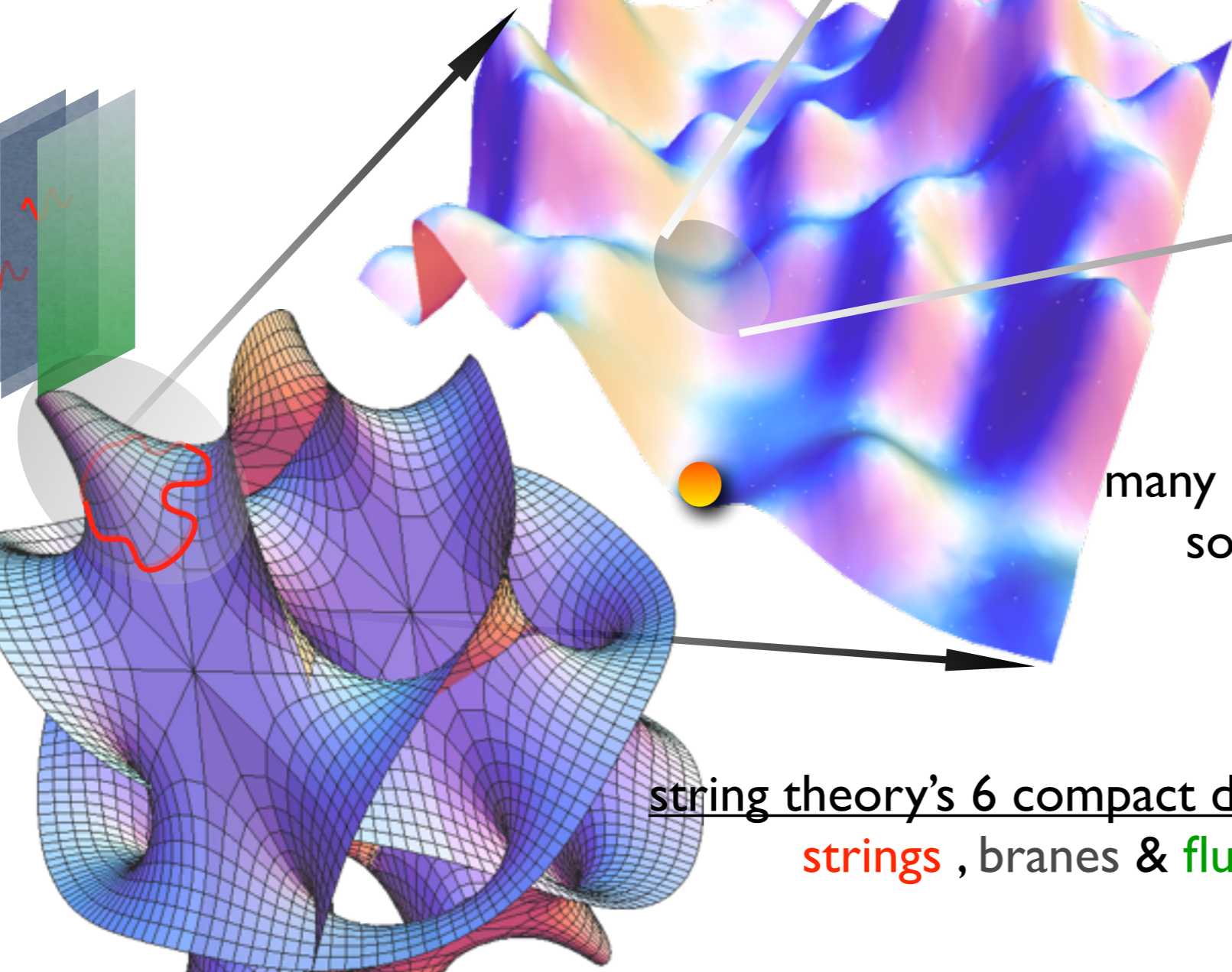
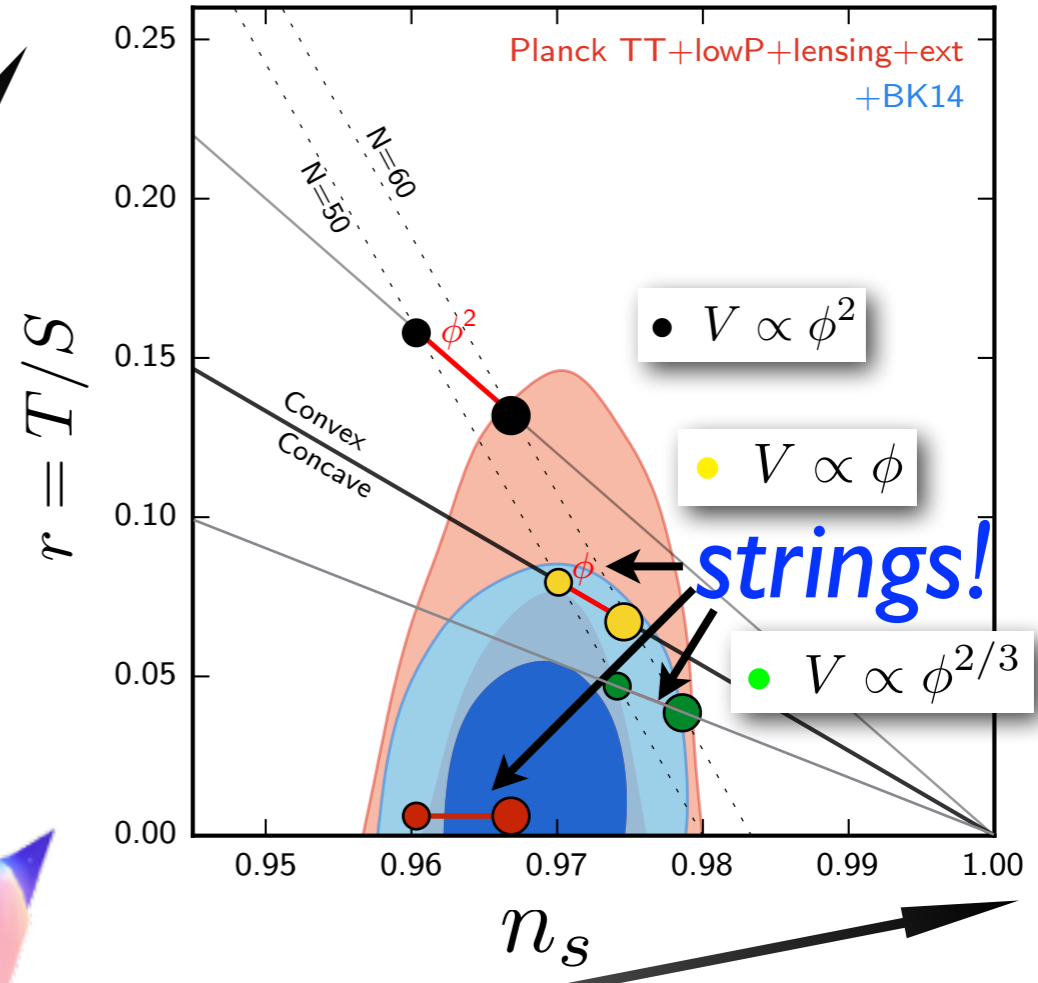
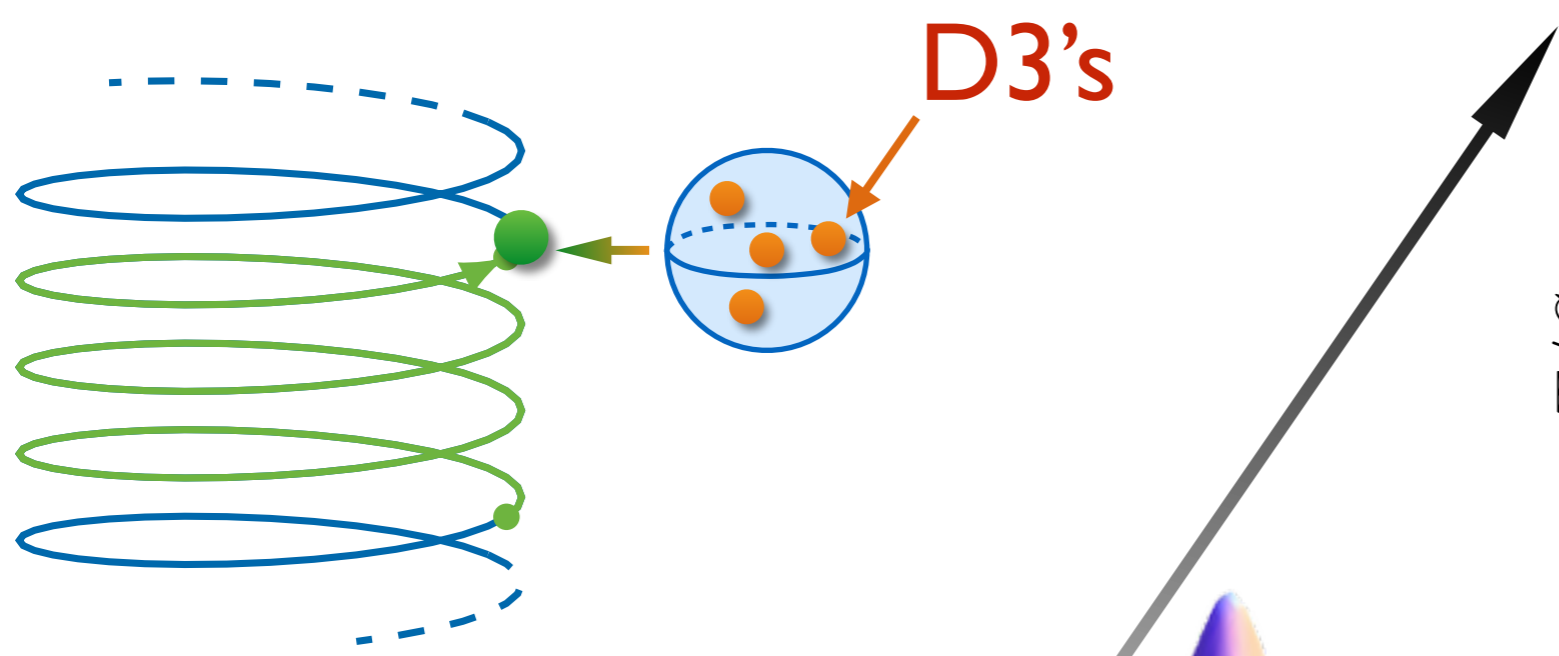
string theory's 6 compact dimensions:
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D3's

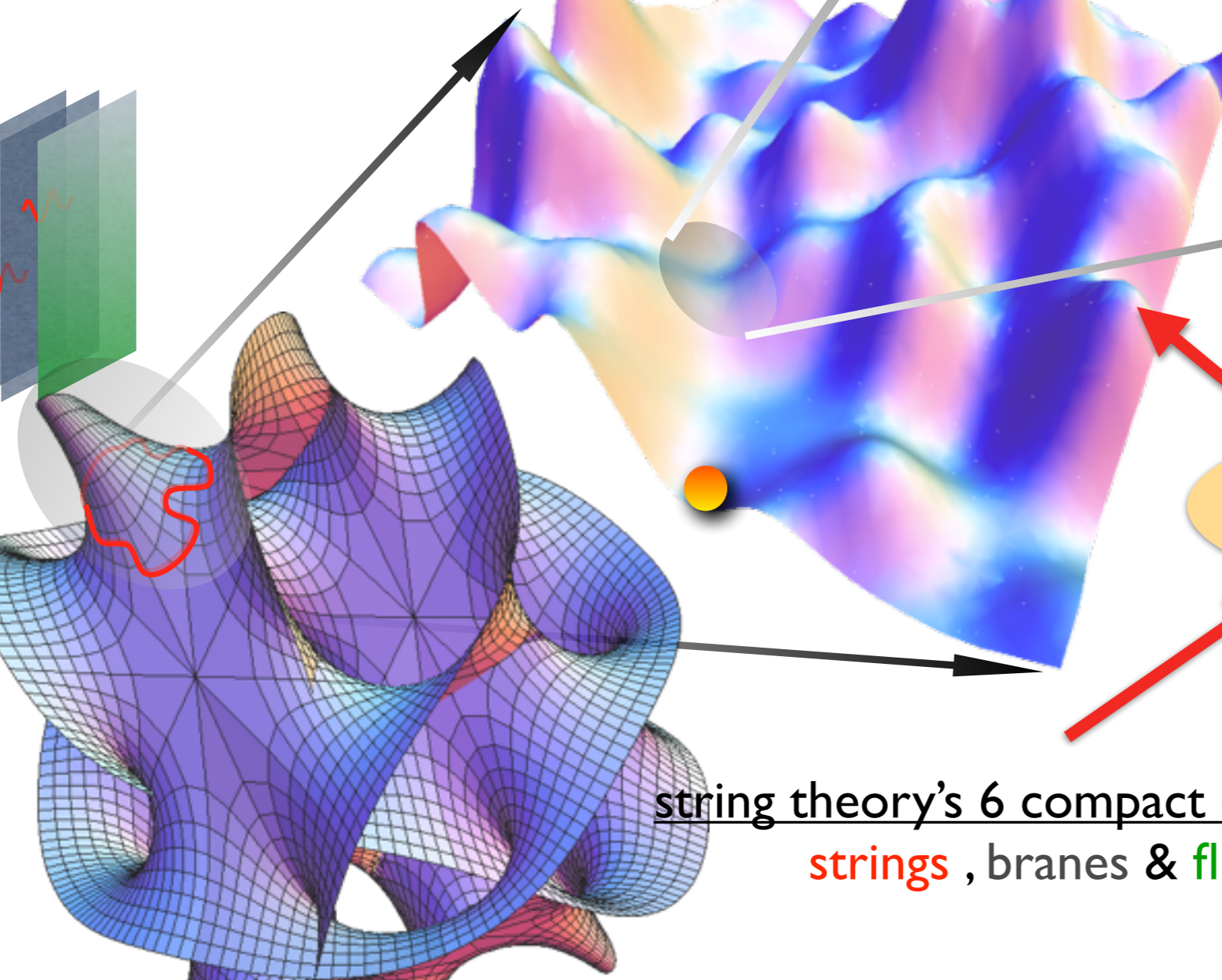
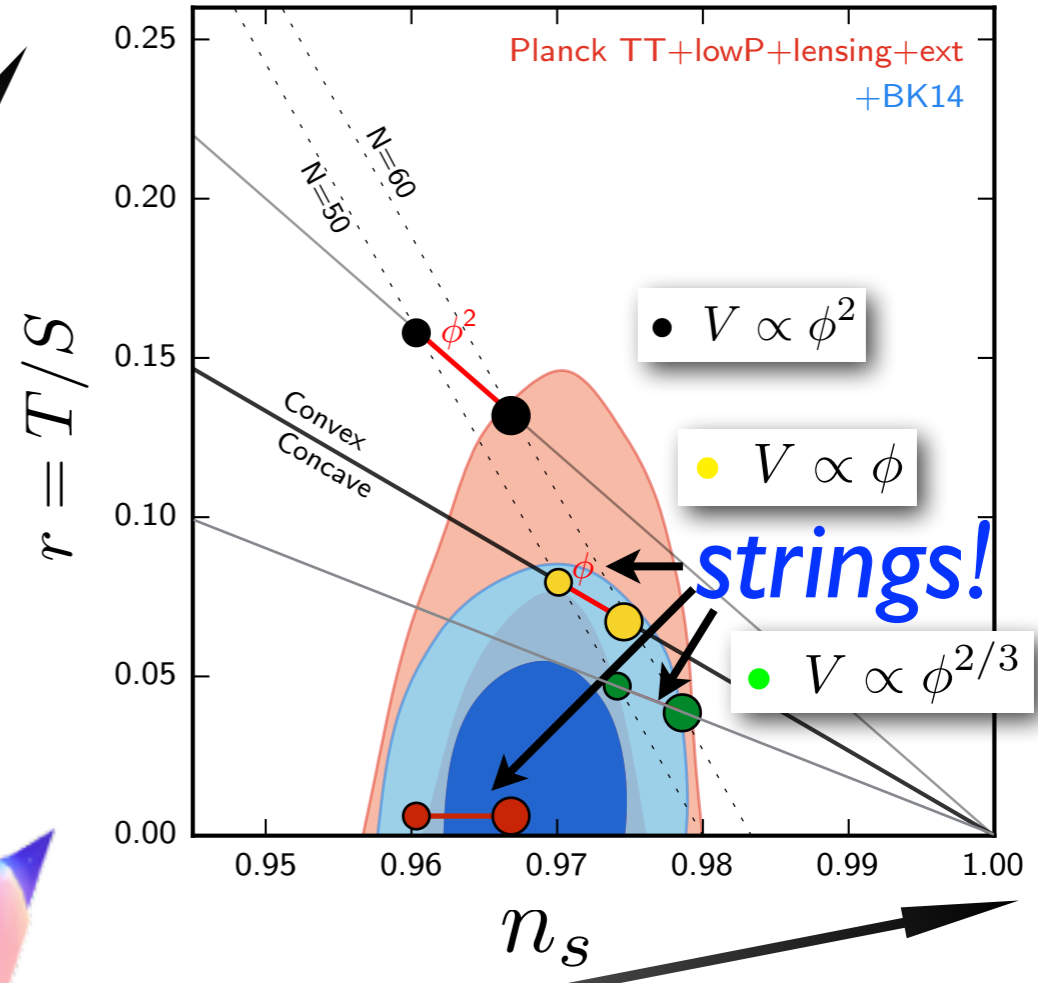
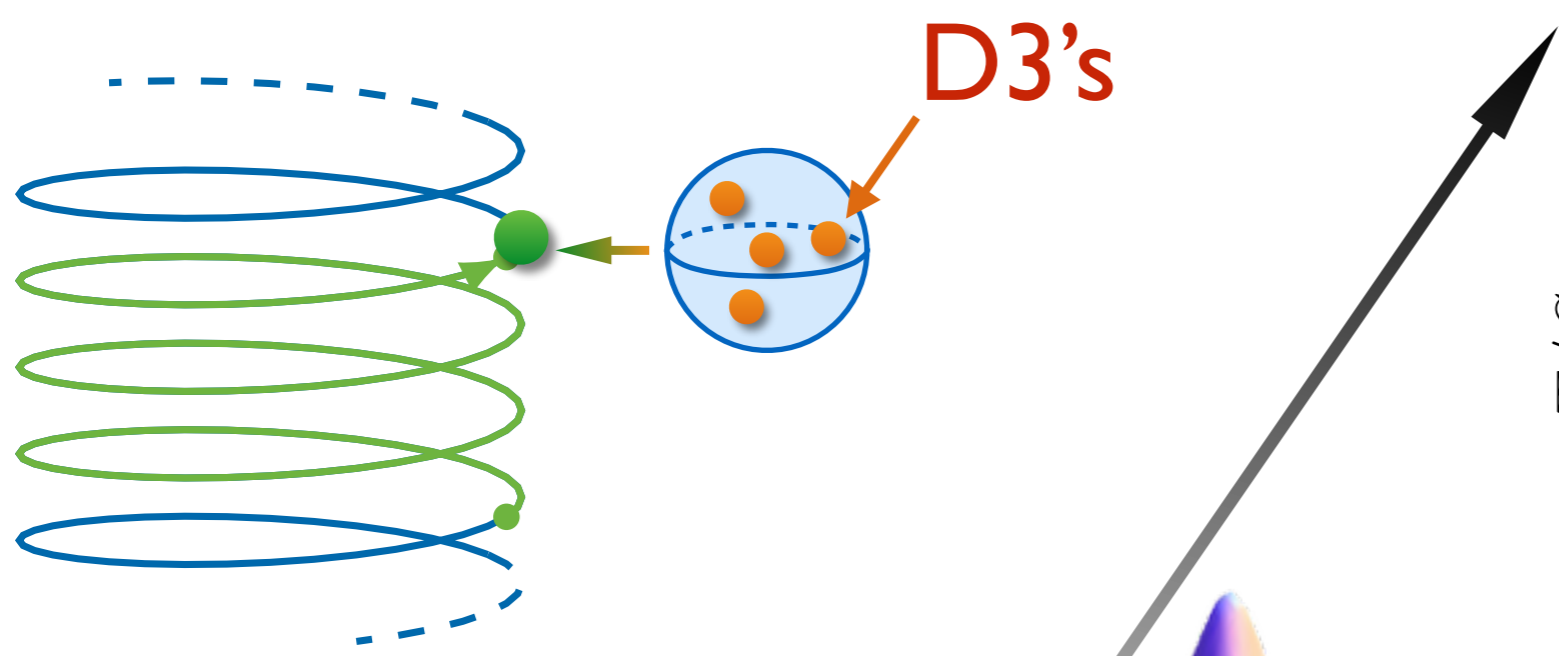
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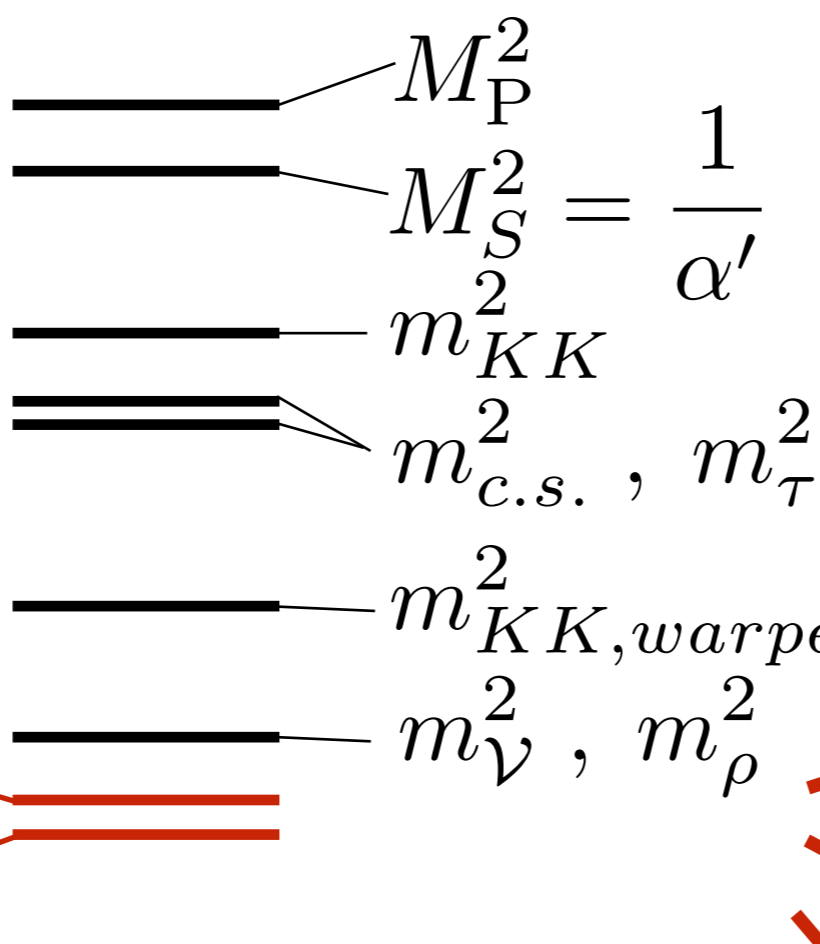


the string theory landscape:
many isolated *vacua*, connected by tunneling
some mountain slopes drive *inflation*

string theory's 6 compact dimensions:
strings, branes & fluxes



**moduli & axions:
light scalars ...**



$H^2, \Delta V,$
 $m_{3/2}^2 M_P^2, \dots$
 m_ϕ^2

inflation
 EW symmetry breaking
 dark energy

— $SM + axions$



flattened acceleration from slow-roll: inflation

[Dong, Horn, Silverstein & AW '10]

2-field system: $V(\phi, \chi) = g \phi^2 \chi^2 + M^2 (\chi - \chi_0)^2$

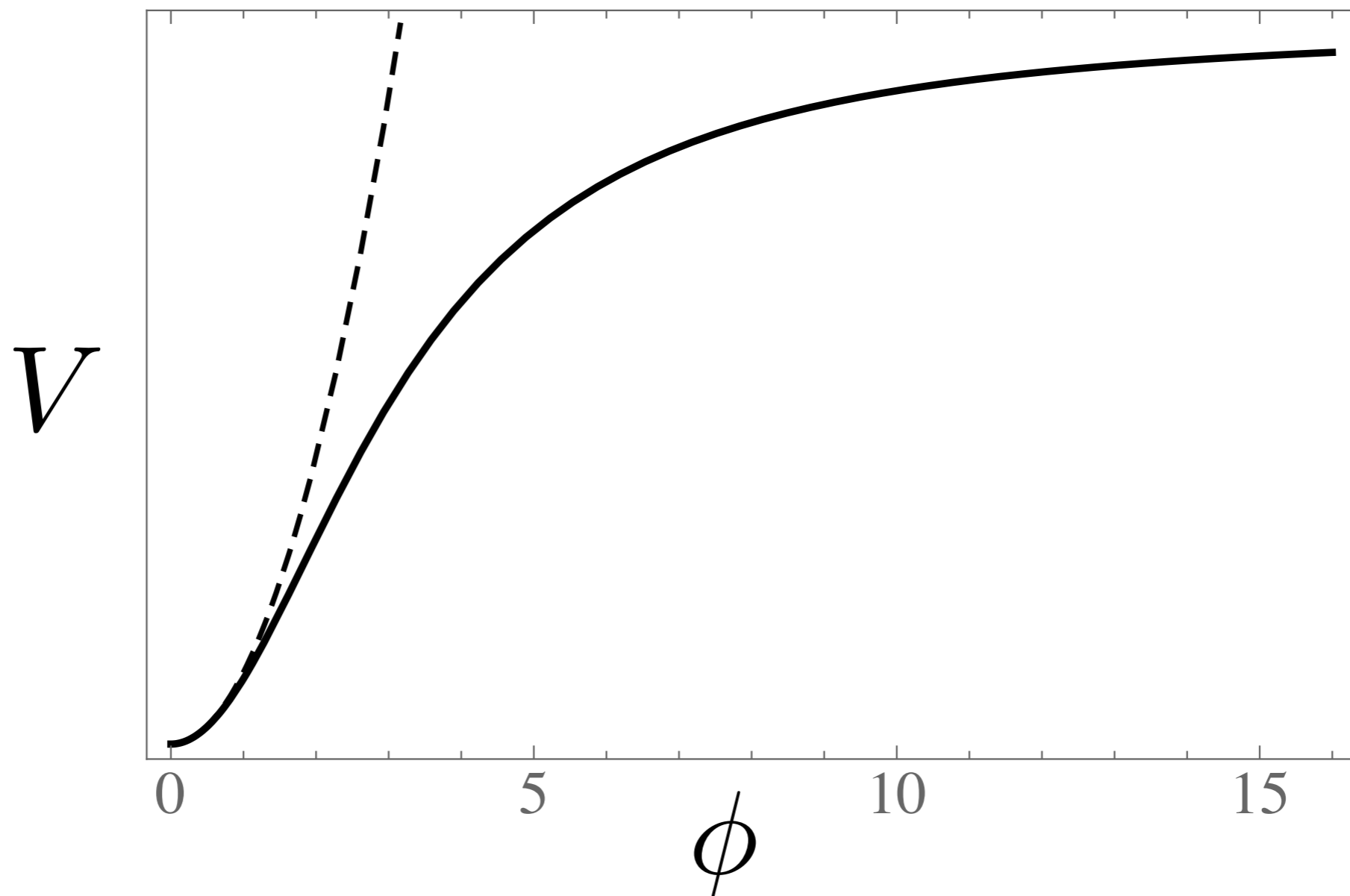
$$m_\phi^2 = g \chi_0^2 \sim \chi_0^2 \ll M^2 \quad (g \lesssim 1)$$

effective potential: $V_{eff.}(\phi) = M^2 \chi_0^2 \frac{g \phi^2}{M^2 + g \phi^2}$

$$= \frac{m_\phi^2 \phi^2}{1 + \frac{m_\phi^2}{M^2} \cdot \frac{\phi^2}{\chi_0^2}} \simeq \frac{m_\phi^2 \phi^2}{1 + \frac{\phi^2}{M^2}}$$


flattened acceleration from slow-roll: inflation

effective potential — flattened inflation !



slow-roll field \rightarrow **parameter (e.g. anti-brane tension)**

2-field system:

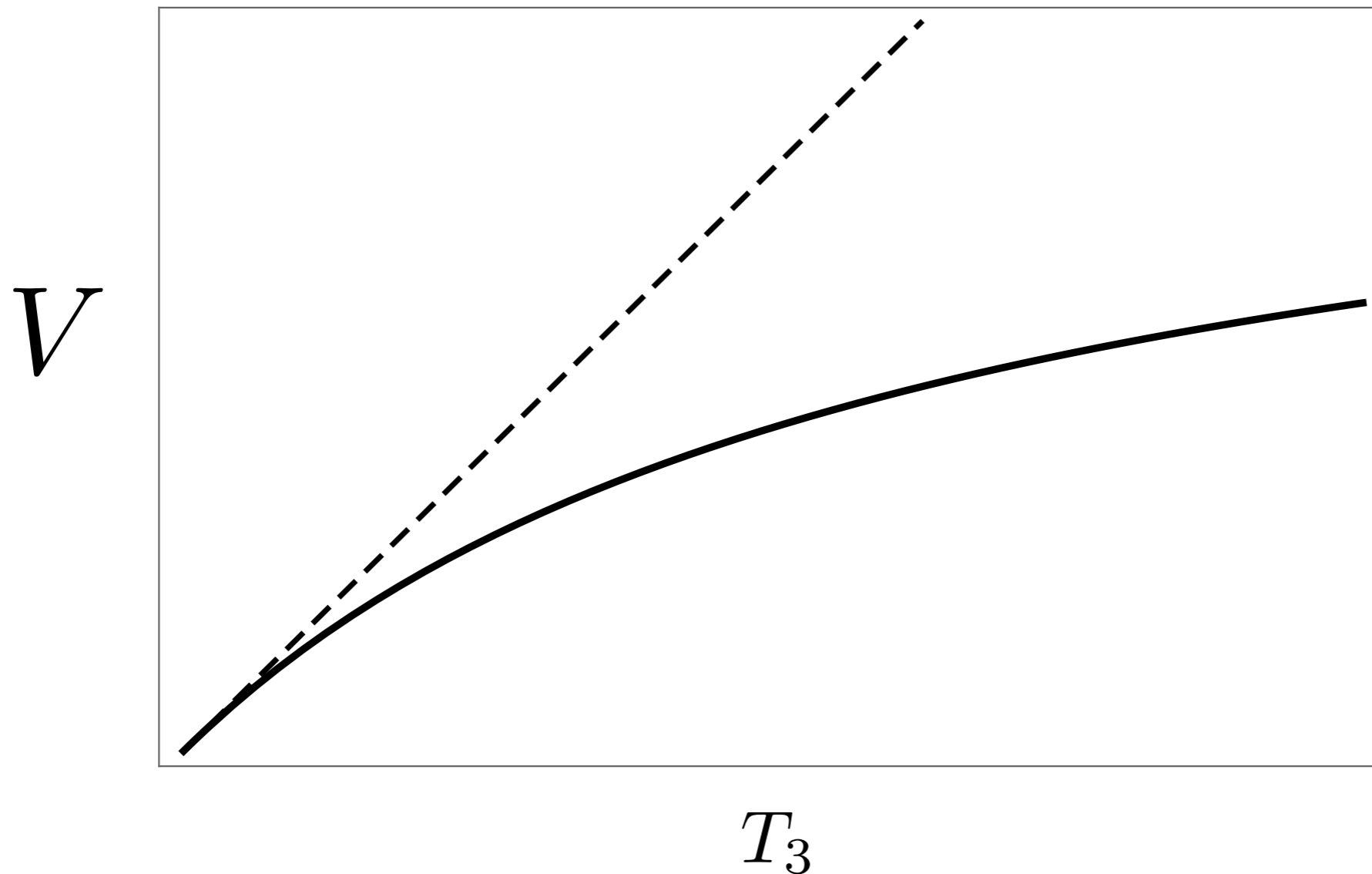
$$\phi^2 \rightarrow T_3$$


effective potential:

$$V \sim \frac{T_3}{1 + \frac{T_3}{M^2}}$$

flattened acceleration from slow-roll: inflation

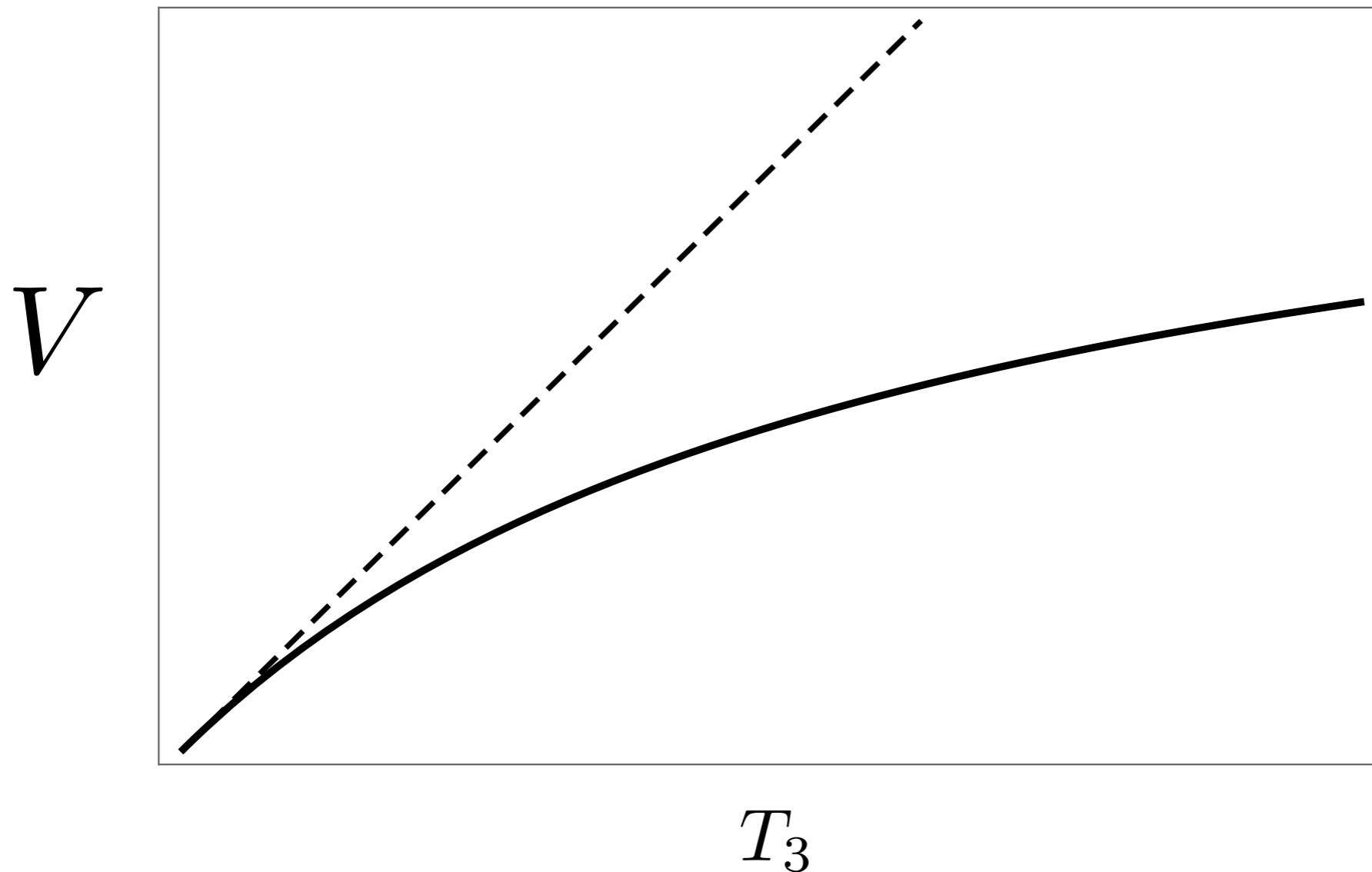
effective potential — flattened uplift ???



... ?

flattened acceleration from slow-roll: inflation

effective potential — flattened uplift ???



... ?
↓
yes !

axion monodromy — a summary

[Silverstein & AW; McAllister,
Silverstein & AW; Kaloper & Sorbo '08]
[Kaloper, Lawrence & Sorbo '11]

- 5D U(1) gauge symmetry — 4D Stueckelberg mech.

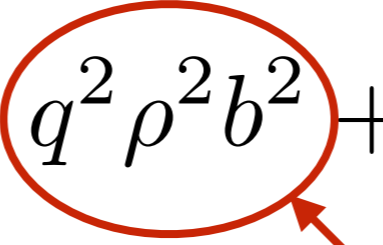
$$S = \int_{\mathcal{M}_4 \times S^1} d^5x \left(\frac{1}{4} F^{MN} F_{MN} - |(\partial_M + iqA_M)\phi|^2 + \lambda(|\phi|^2 - \rho^2)^2 \right)$$

$$\phi = \langle \phi \rangle = \rho e^{iC_0}$$

$$= \int_{\mathcal{M}_4} d^4x \int_{S^1} dy \left(\frac{1}{4} B^{MN} B_{MN} - q^2 \rho^2 |B_M|^2 \right), \quad B_M = A_M + \frac{1}{q} \partial_M C_0$$

$$A_M \rightarrow A_M + \partial_M \Lambda, \quad C_0 \rightarrow C_0 - q\Lambda \rightarrow B_M \rightarrow B_M$$

$$S = \int_{\mathcal{M}_4} d^4x \left(\frac{1}{2} (\partial_\mu b)^2 - q^2 \rho^2 b^2 + \dots \right), \quad b = \oint_{S^1} B_5$$

 axion mass term

Flattening 1: moduli backreact in axion monodromy

- bare bones monodromy: $\int d^{10}x \left(\frac{|dB|^2}{g_s^2} + |F_1|^2 + |F_3|^2 + |\tilde{F}_5|^2 \right)$

$$V = \frac{C_1}{\phi} + C_2 \phi^2 (\mu^2 + b^2) \quad \longrightarrow \quad \langle \phi \rangle = \langle \phi \rangle_0 (1 + b^2 / \mu^2)^{-1/3}$$

- 2 types of flattening — additive & multiplicative:

$$V_{eff.}(b) = V|_{\langle \phi \rangle} \sim \langle \phi \rangle_0^2 \frac{b^2}{(1 + b^2 / \mu^2)^{2/3}} \sim \begin{cases} b^2 - \frac{2}{3} \frac{b^4}{\mu^2} & , \quad \mu \gg 1 \\ b^{2/3} & , \quad \mu \ll 1 \end{cases}$$

- other powers as well: $\phi, \phi^{4/3}, \phi^2$

[McAllister, Silverstein, AW & Wrase '14]

[Hebecker et al. '14]

[Buchmüller, Dudas, Heurtier, AW, Wieck & Winkler '15]

Flattening 2: pole inflation/ α -attractors in string theory

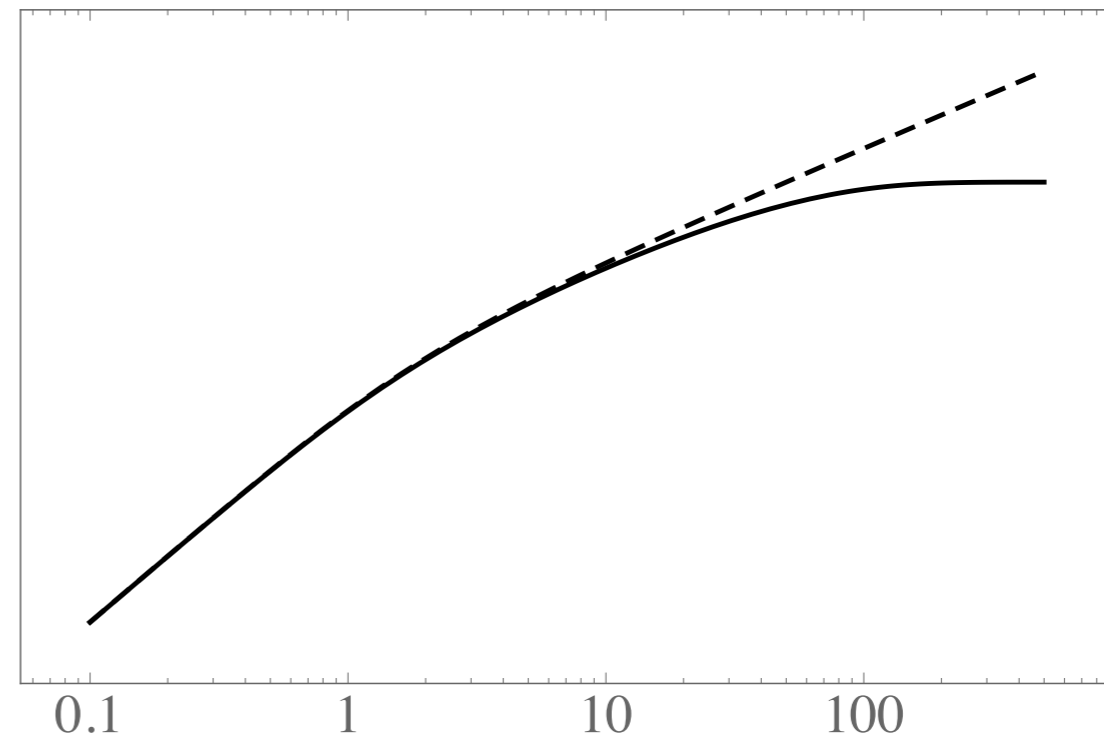
- backreaction for moduli & axions — singular kinetic terms:

$$\mathcal{L}_{kin} = \frac{1}{\phi^2} \left((\partial\phi)^2 + (\partial a)^2 \right) \quad V = V_0(\phi) - c(\phi) a + \dots$$

$$\phi = \phi_0 \rightarrow \phi_0 + \epsilon a \quad , \quad \epsilon \ll 1$$

$$\mathcal{L}_{kin} \rightarrow \frac{1}{\epsilon^2} \frac{(\partial a)^2}{a^2}$$

$$V \rightarrow V_0 - c e^{-\epsilon \varphi} + \dots$$



$\varphi [M_P]$



Flattening 2: pole inflation/ α -attractors in string theory

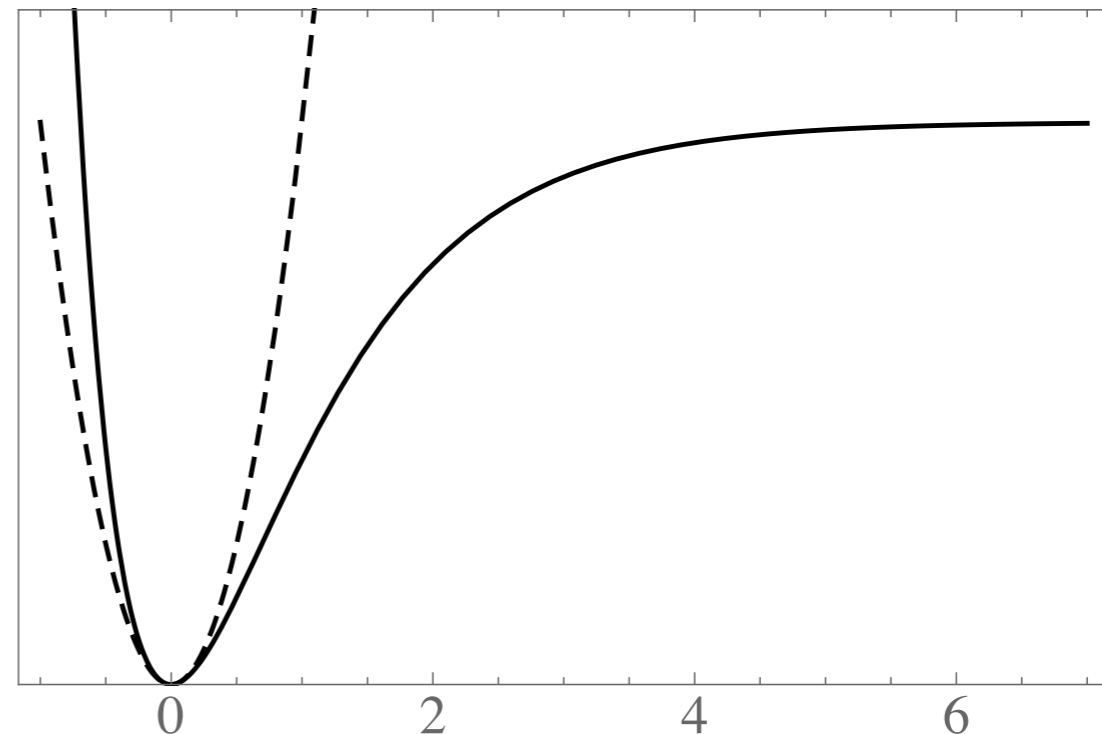
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Flattening 2: pole inflation/ α -attractors in string theory

[Burgess, Cicoli & Quevedo '08; and/or de Alwis, Broy, Ciupke, Diaz, Guidetti, Muia, Pedro, Shukla, AW, Williams '14-'17]

- string realization - 'fibre inflation':

[Kallosh, Linde, Roest, AW & Yamada '17]

$$\mathcal{L}_{kin} = \frac{(\partial\phi)^2}{4\phi^2} + \frac{(\partial\chi)^2}{2\chi^2}$$

supergravity +
extra dimensions

loop corrections

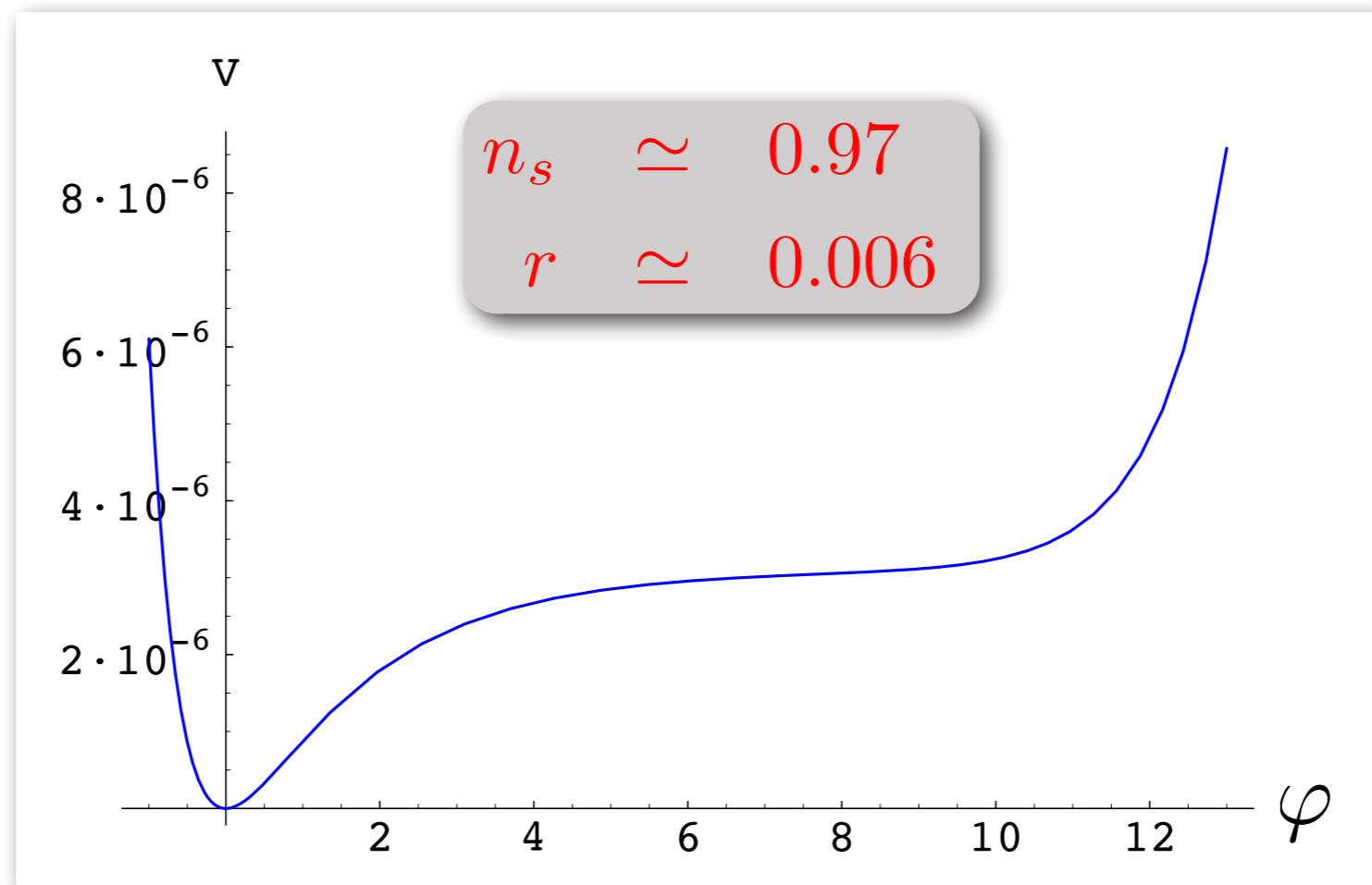
$$V = \left(\frac{1}{\sqrt{\phi\chi}} \right)^2 \cdot \left(V_0(\phi, \chi) - \left(\frac{c}{\chi} + \frac{\delta}{\phi^{p/2}} + \dots \right) \right)$$

$$\mathcal{V} = R^6 = const. \Rightarrow \phi \sim 1/\chi^2, \chi \rightarrow e^{-\varphi/\sqrt{3}}$$

Flattening 2: pole inflation/ α -attractors in string theory

[Burgess, Cicoli & Quevedo '08; and/or de Alwis, Broy, Ciupke, Diaz, Guidetti, Muia, Pedro, Shukla, AW, Williams '14-'17]

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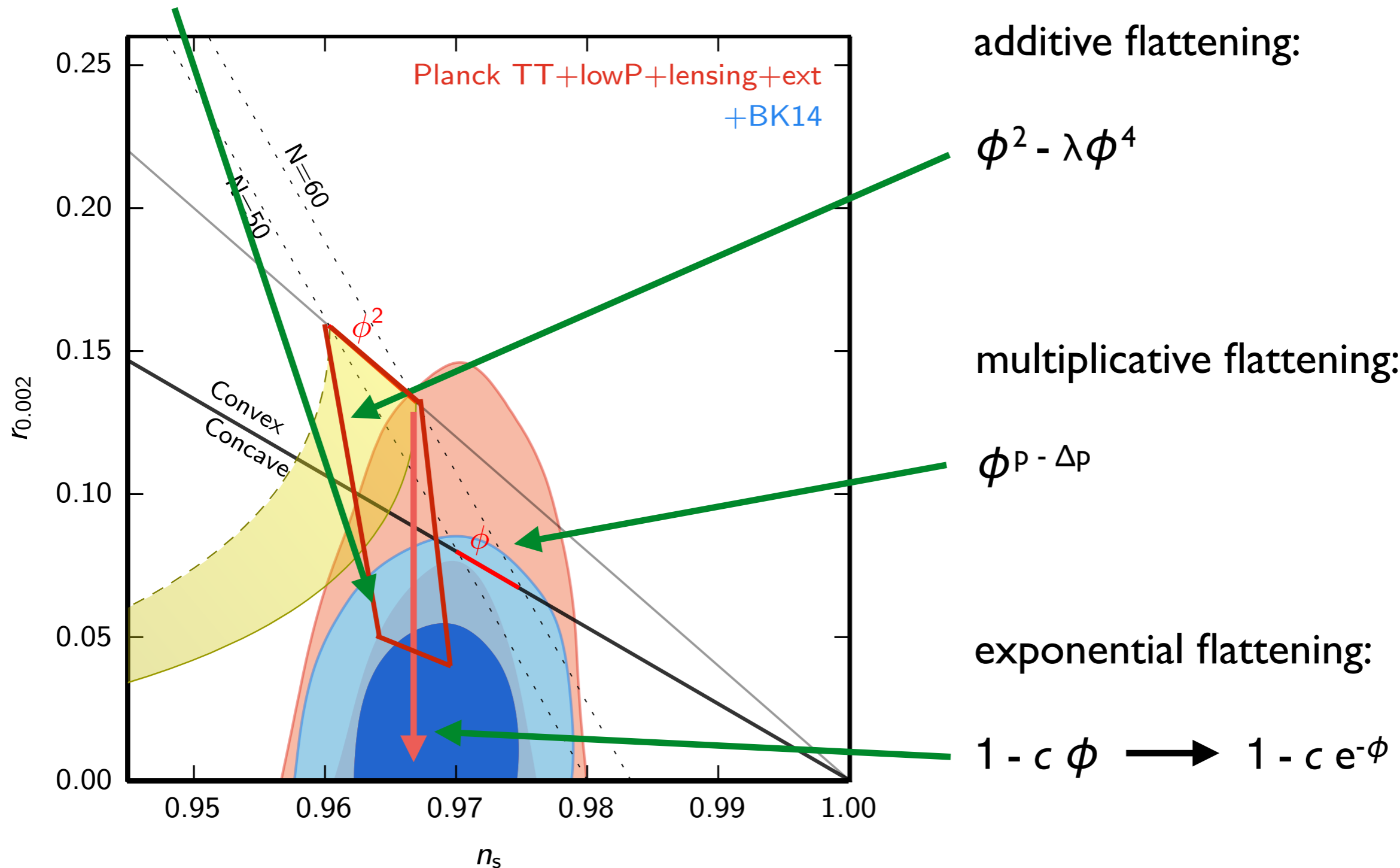


$$\rightarrow V = \frac{1}{\mathcal{V}^2} \cdot \left(V_0 - c e^{-\varphi/\sqrt{3}} + \delta e^{+p\varphi/\sqrt{3}} + \dots \right)$$

phenomenology ... flattening !

n_s - r limits Planck, TT + lowP + BICEP2/Keck/Planck joint analysis 2015

'flux flattening': [Landete, Marchesano, Shiu, Zoccarato '17]

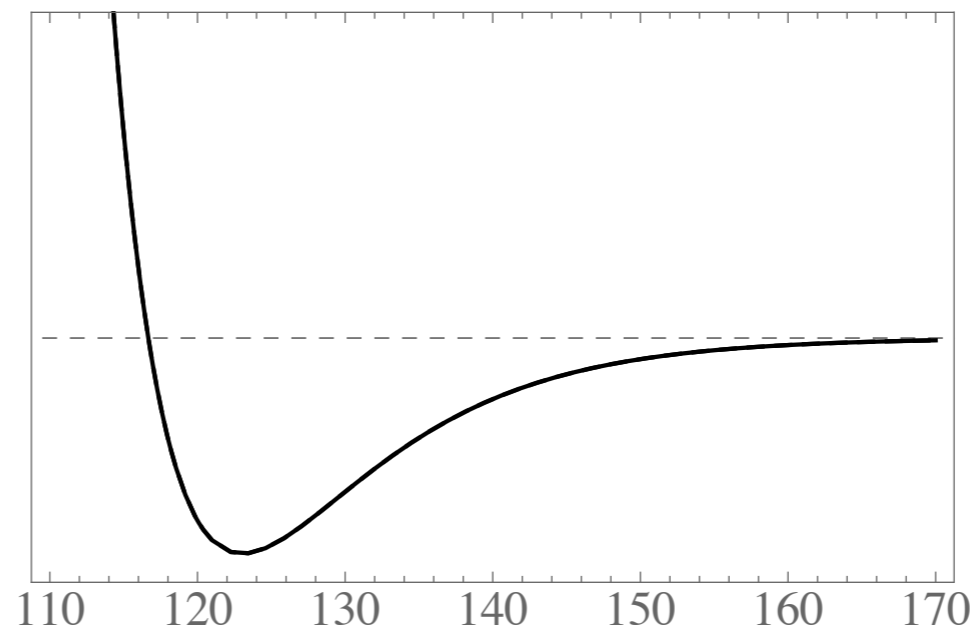


Flattening 3 - the CC : KKLT de Sitter vacua ? [KKLT '03]

KKLT - I: $K = -3 \ln(T + \bar{T})$, $W = W_0 + P e^{-aT}$

$$V = e^K (K^{T\bar{T}} |D_T W|^2 - 3|W|^2)$$

$$= -\frac{W_0}{\rho^2} e^{-a\rho} + \frac{1}{\rho} e^{-2a\rho}$$



Flattening 3 - the CC : KKLT de Sitter vacua ? [KKLT '03]

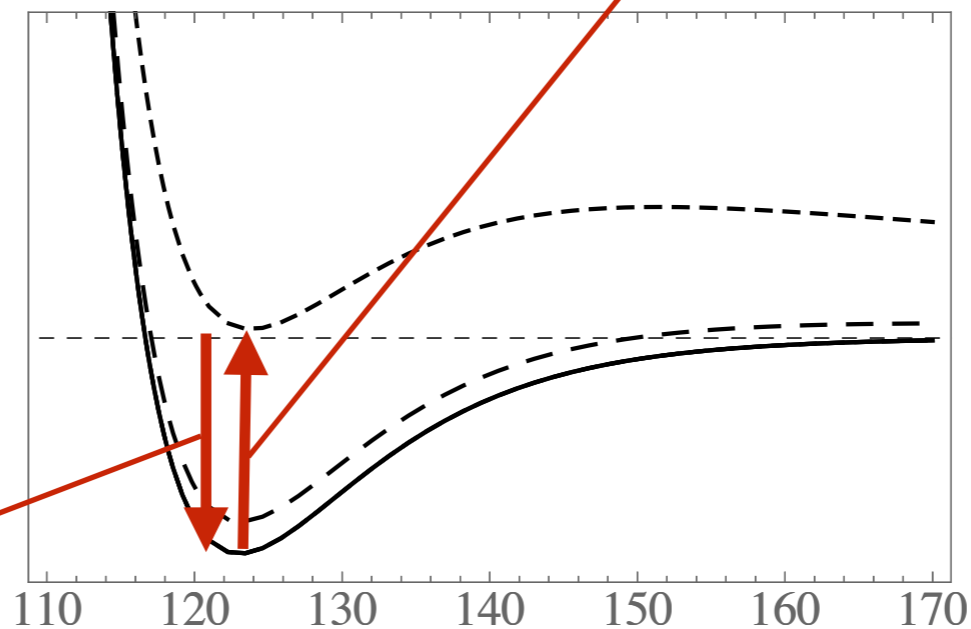
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$$V = e^K (K^{T\bar{T}} |D_T W|^2 - 3|W|^2)$$

$$= -\frac{W_0}{\rho^2} e^{-a\rho} + \frac{1}{\rho} e^{-2a\rho}$$

KKLT - 2: $V \rightarrow V + \delta V$, $\delta V = \frac{\epsilon T_3}{\rho^2}$ $\overline{D3}$ - brane [KPV '01]

$$V_{AdS} \sim -m_\rho^2 M_P^2$$



Flattening 3 - the CC : KKLT de Sitter vacua ?

[Moritz, Retolaza & AW '17]

uplift:

$$\epsilon \ll 1$$

usually: warping ...

$$\epsilon \sim e^{4A} = \text{const.} \ll 1$$

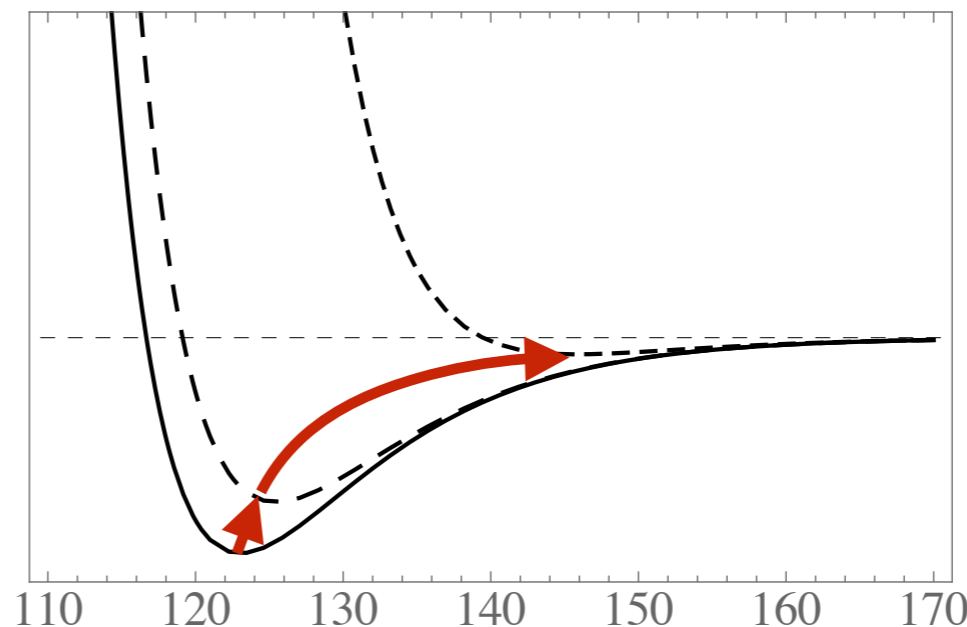
but: why not ... ?

$$\epsilon \sim e^{-2a\rho}$$

flattened uplift !!

once:

$$\delta V \gtrsim |V_{AdS}| \sim m_\rho^2 M_P^2$$



$V < 0 !!$

Flattening 3 - the CC : KKLT de Sitter vacua ?

[Volkov & Akulov '73; subsets of: Aalsma, Antoniadis, Bandos, Bergshoff, Dudas, Ferrara, Dasgupta, Garcia del Moral, Heller, Kallosh, Kuzenko, Linde, Martucci, McDonough, Parameswaran, van Proeyen, Quevedo, Quiroz, Roest, Scalisi, van der Schaar, Sorokin, Uranga, Vercnocke, Wrase, Yamada, Zavala '14-'17; ...]

- nilpotent superfield S parametrizes the nonlinear anti-D3-SUSY:

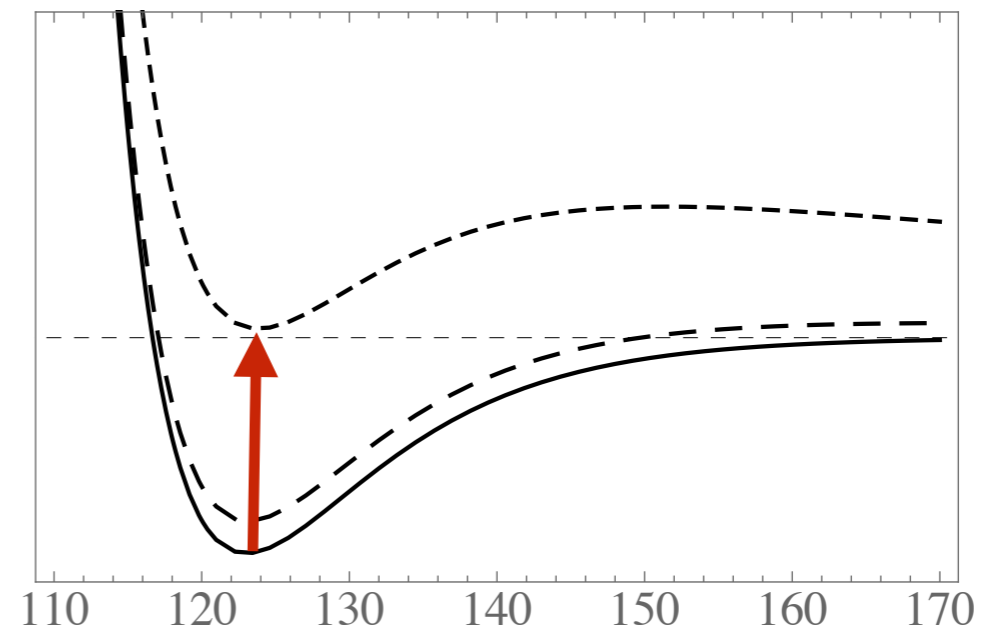
$$K = -3 \ln(T + \bar{T} - S\bar{S})$$

$$W = W_0 + P e^{-aT} + B S$$

$$B = e^{2A} \sqrt{T_3} \quad , \quad e^{2A} \sim \sqrt{\epsilon} \sim e^{-a\rho}$$



$$\delta V_F \sim e^{4A} \frac{T_3}{\rho^2}$$



Flattening 3 - the CC : KKLT de Sitter vacua ?

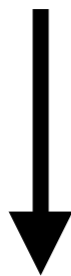
[Volkov & Akulov '73; subsets of: Aalsma, Antoniadis, Bandos, Bergshoff, Dudas, Ferrara, Dasgupta, Garcia del Moral, Heller, Kallosh, Kuzenko, Linde, Martucci, McDonough, Parameswaran, van Proeyen, Quevedo, Quiroz, Roest, Scalisi, van der Schaar, Sorokin, Uranga, Vercoocke, Wrase, Yamada, Zavala '14-'17; ...]

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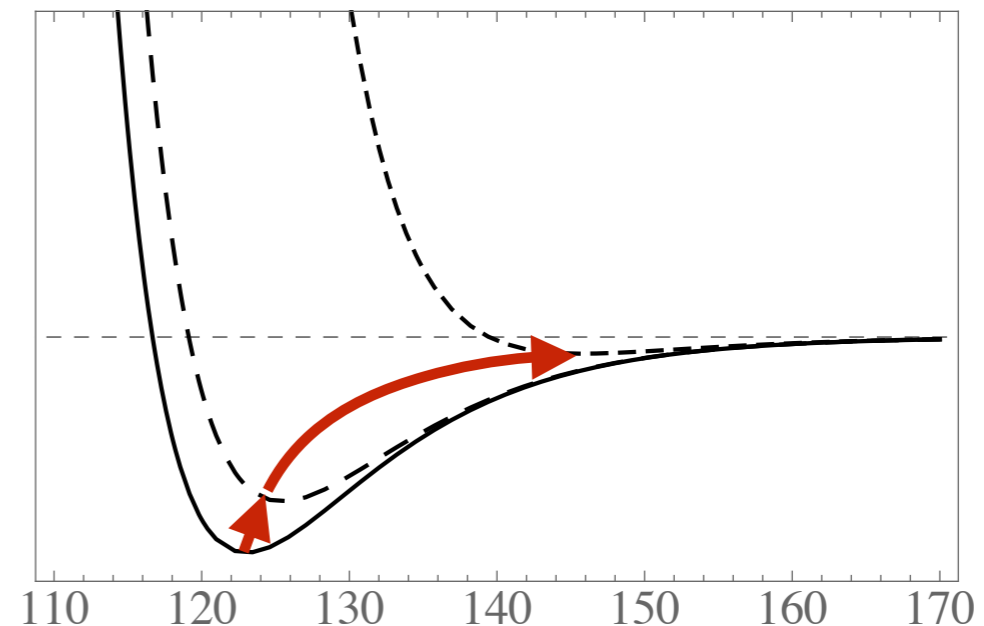
$$K = -3 \ln(T + \bar{T} - S\bar{S}) \quad [\text{Moritz, Retolaza \& AW '17}]$$

$$W = W_0 + (P + C S)e^{-aT} + B S$$

$$B = 0 \quad , \quad C = \mathcal{O}(1)\sqrt{T_3}$$



$$\delta V_F \sim e^{-2a\rho} \frac{T_3}{\rho^2}$$



Flattening 3 - the CC : KKLT de Sitter vacua ?

[Heidenreich, McAllister & Torroba; Dymarsky & Martucci '10]

[Moritz, Retolaza & AW '17]

- need 10D analysis to fix sign of 4D CC:
 - dim. reduction of 7-brane flux-condensate coupling
 - use flux e.o.m to find flux profiles encoding presence of condensate
 - Use 10D Einstein & Bianchi eq.s to determine sign of 4D curvature — assuming backreacted solution with anti-D3 brane exists !!

$$\tilde{\nabla}^2 \Phi^- = \tilde{R}_{4D} + e^{-6A} |\partial \Phi^-|^2 + e^{2A} \frac{\Delta^{flux+loc}}{2\pi}$$

Flattening 3 - the CC : KKLT de Sitter vacua ?

[Moritz, Retolaza & AW '17]

- extracting gaugino bilinear from D7-action & insert in flux e.o.m.:

$$\frac{e^{2A}}{2\pi} \Delta^{D7} = \int \frac{d^6 y \sqrt{g}}{8\pi^3 \mathcal{V}_w \tilde{\mathcal{V}}_w} \left(4 \left| \sum_{a=1}^n \frac{\langle \lambda \lambda \rangle_a}{16\pi^2} \nabla_i \nabla_j \Psi_a \right|^2 - 3 \sum_{a=1}^n \left| \frac{\langle \lambda \lambda \rangle_a}{16\pi^2} \nabla_i \nabla_j \Psi_a \right|^2 \right)$$

> 0 for $n = 1$!

Flattening 3 - the CC : KKLT de Sitter vacua ?

[Moritz, Retolaza & AW '17]

- this fixes sign of 4D CC:

$$\begin{aligned} \overline{D3}\text{-brane: } \Delta^{loc} &> 0 \\ D7\text{-brane: } \Delta^{D7} &> 0 \end{aligned} \quad \Rightarrow \quad \langle V \rangle \sim \int_{CY} \tilde{R}_4 < 0 \quad !!$$

- 10D input necessary to fix 4D EFT of KKLT — otherwise neglect of coupling:

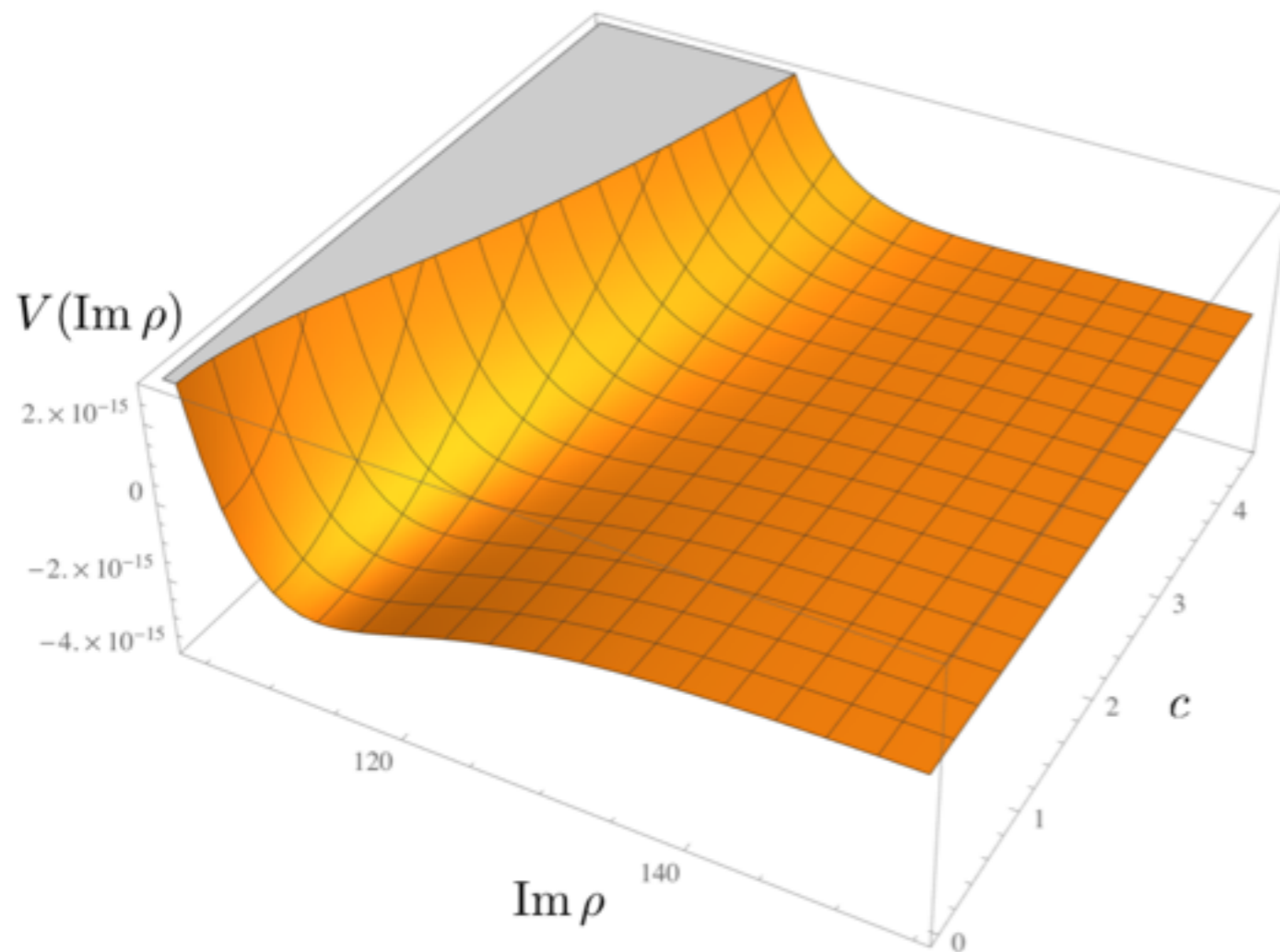
$$\mathcal{O}(1) \sqrt{T3} e^{-a\rho}$$

- simplest KKLT — ρ & 1 gaugino condensate — does not give dS !
- need racetrack: two $e^{-a\rho}$ - terms — can give dS !

all forms of positive vacuum energy in string theory
flatten below linearly adding up sources !



Thank You !



- single condensate

- racetrack

