# Studies on lepton-hadron interactions for precision neutrino physics

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## Discovery of neutrino oscillation

1996 Neutrino oscillation was discovered

at Super-Kamiokande



## Discovery of neutrino oscillation

1996 Neutrino oscillation was discovered





Neutrino oscillation and properties of neutrinos

Neutrino oscillations

- Non-zero neutrino mass states
  - $(m_1, m_2, m_3)$

Flavor mixing

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{PMNS} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

3 mixing angles  $(\theta_{12}, \theta_{23}, \theta_{13})$ 2 mass differences  $(\Delta m_{32}^2, \Delta m_{21}^2)$ 1 CP phase  $(\delta_{CP})$ 



$$U_{PMNS} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & C_{23} & S_{23} \\ 0 & -S_{23} & C_{23} \end{pmatrix} \cdot \begin{pmatrix} C_{13} & 0 & S_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -S_{13}e^{i\delta} & 0 & C_{13} \end{pmatrix} \cdot \begin{pmatrix} C_{12} & S_{12} & 0 \\ -S_{12} & C_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
$$c_{ij} = \cos \theta_{ij}$$
$$s_{ij} = \sin \theta_{ij}$$

#### Accelerator based long baseline neutrino oscillation experiments Produce $v_{\mu}$ / $\overline{v_{\mu}}$ beam using high intensity proton source. Baselines are a few hundreds to thousand km. Study $\nu_{\mu}$ disappearance. $\rightarrow \theta_{23}$ and $|\Delta m_{23}^2|$ Ash river (NOVA) ~ 810 km Study $v_e$ appearance. Soudan ( MINOS ) ~ 750km $\rightarrow \theta_{13}$ , CP violation and mass hierarchy. The NOvA experiment Typical $E_{\nu} \sim a$ few GeV The T2K experiment Typical $E_{\nu} \sim 600 MeV$ FermiLab Chicago J-PARC Main Ring Super-Kamiokande (ICRR, Univ. Tokyo) dE/dx ≈ 12.9 MeV/cm(MIP through cell v., Charged Current MC simulation Proton \*\*\*\*\*\*\*\*\*\*\* Flectron v. Charged Current

L. Suter(FNAL User meeting)

#### Determination of properties of neutrinos

Neutrino oscillation probability (survival probability) 2 Flavor case (simplified)

$$P(\nu_{\mu} \rightarrow \nu_{\mu}) = 1 - \sin^2 2\theta \cdot \sin^2 \left(\frac{1.27\Delta m^2 L}{E_{\nu}}\right)$$

 $\theta$  Mixing angle,  $\Delta m^2$  Squared mass difference (in eV<sup>2</sup>) L Distance (in km),  $E_{\nu}$  Energy of neutrino (in GeV)



#### **Properties of neutrinos**

All angles except for  $\delta_{CP}$  have been measured.

$$U_{PMNS} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & C_{23} & S_{23} \\ 0 & -S_{23} & C_{23} \end{pmatrix} \cdot \begin{pmatrix} C_{13} & 0 & S_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -S_{13}e^{i\delta} & 0 & C_{13} \end{pmatrix} \cdot \begin{pmatrix} C_{12} & S_{12} & 0 \\ -S_{12} & C_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

 $\begin{aligned} \sin^2\theta_{12} &= 0.307 \pm 0.013 & \sin^2\theta_{13} = 0.0210 \pm 0.0011 \\ \sin^2\theta_{23} &= 0.51 \pm 0.04 \text{ (normal hierarchy )} \end{aligned}$ 



Properties of neutrinos ~ Remaining questions 1) Is  $\theta_{23}$  really 45° or < 45° or >45°?  $\sin^2\theta_{23} = 0.51 \pm 0.04$  (normal hierarchy)

 $\rightarrow$  Precise measurement of  $\nu_{\mu}$  disappearance

2) Mass hierarchy ~ which is heavier ? Δm<sup>2</sup><sub>32</sub> > 0 or < 0 ?</li>
3) Is CP violated (δ<sub>CP</sub> = 0 or not) ? → Study difference between ν<sub>μ</sub> → ν<sub>e</sub> and ν<sub>μ</sub> → ν<sub>e</sub>

 $m^2$  $\Delta m_{32}^2 (10^{-3} eV^2)$ Normal Hierarchy 90% C.L Normal Hierarchy **Inverted Hierarchy**  NOvA 8.85×10<sup>20</sup> POT-equiv.  $m_3^2$ ···· T2K 2016  $m_{2}^{2}$ ----- MINOS 2014 NOvA Preliminary  $m_{1}^{2}$  $m_{2}^{2}$ Joint analysis  $m_{3}^{2}$ 2.0 0.4 0.5 0.6  $\sin^2 \theta_{23}$ 8

#### Determination of neutrino oscillation parameters

Neutrino oscillation probability ~ Appearance (3 flavor)

$$P(\nu_{\mu} \rightarrow \nu_{e}) = \frac{4\bar{4}C_{13}^{2}S_{23}^{2}S_{23}^{2}S_{23}^{2}S_{12}^{2}\Phi_{31}!}{+8C_{13}^{2}S_{12}S_{13}S_{23}(C_{12}C_{23}\cos\delta - S_{12}S_{13}S_{23})\cos\Phi_{32} \cdot \sin\Phi_{31} \cdot \sin\Phi_{21}}{+8C_{13}^{2}C_{12}C_{23}S_{12}S_{13}S_{23}(C_{12}C_{23}\cos\delta - S_{12}S_{13}S_{23})\cos\Phi_{32} \cdot \sin\Phi_{31} \cdot \sin\Phi_{21}}|$$
 **CP odd term**  
$$+4S_{12}^{2}C_{13}^{2}(C_{12}^{2}C_{23}^{2} + S_{12}^{2}S_{23}^{2}S_{13}^{2} - 2C_{12}C_{23}S_{12}S_{23}S_{13}\cos\delta)\sin^{2}\Phi_{21}}|$$
  
$$= 8C_{13}^{2}S_{13}^{2}S_{23}^{2}(1 - 2S_{13}^{2})\frac{dL}{4E_{\nu}}\cos\Phi_{32}\sin\Phi_{31}.|$$
 **Matter term**  
$$= 2\sqrt{2}G_{F}n_{e}E_{\nu} \quad c_{ij} = \cos\theta_{ij}, s_{ij} = \sin\theta_{ij}, \phi_{ij} = \frac{1.27\Delta m_{ij}^{2}L}{E_{\nu}}$$
  
For anti neutrinos,  $a \rightarrow -a, \delta \rightarrow -\delta$   
**Appearance probabilities could be different between**  $\nu_{\mu}$  and  $\overline{\nu_{\mu}}$ .  
$$= \sqrt{2}\sqrt{2}G_{F}n_{e}E_{\nu} \quad v_{ij} \rightarrow \overline{\nu_{e}} \qquad \frac{\sin^{2}2\theta_{13}=0.1}{\delta^{2}-1/2\pi}$$

 $E_{v}$  (GeV)

 $E_V$  (GeV)

Determination of neutrino oscillation parameters

Determination of mass hierarchy

using matter effects in atmospheric neutrino oscillation



It is also possible to determine mass hierarchy using neutrinos from accelerators.

Neutrino-nucleon/nucleus interactions above 100 MeV

Charged current quasi-elastic scattering (CCQE)

 $\nu + N \rightarrow l^- + N'$  $v_{\mu}$  cross-section/E<sub>v</sub>  $1fb = 10^{-39} cm^2$ (Oxygen, avg. nucleon) Neutral current elastic scattering nucleon)  $\nu + N \rightarrow \nu + N'$ NC + CC Total Single meson productions 10<sup>-38</sup>cm<sup>2</sup>/GeV/avg. .5  $\nu + N \rightarrow l^- + N' + \pi (\eta, K)$ CC Total Single photon productions CC QE  $\nu + N \rightarrow l^- + N' + \gamma$ CC DIS CC  $1\pi$ (radiative decay of resonance) Deep inelastic scattering д/б CC multi nucleor  $\nu + N \rightarrow l^- + N' + n \times \pi (\eta, K)$ 3 Neutrino energy (GeV)

Neutrino detectors ~ nucleus target Various "nuclear effects" have to be taken into account. Neutrino-nucleon/nucleus interactions above 100 MeV

Charged current quasi-elastic scattering (CCQE)

 $\nu + N \rightarrow l^- + N'$ 

Neutral current elastic scattering

 $\nu + N \rightarrow \nu + N'$ 

Single meson productions

 $\nu + N \rightarrow l^- + N' + \pi (\eta, K)$ Single photon productions

 $\nu + N 
ightarrow l^- + N' + \gamma$ 

( radiative decay of resonance ) Deep inelastic scattering

 $\nu + N \rightarrow l^- + N' + n \times \pi (\eta, K)$ 



Neutrino detectors ~ nucleus target Various "nuclear effects" have to be taken into account.

Case 1:  $E_v = 100 \text{MeV} \sim \text{a few GeV}$ 

 $v + N \rightarrow I + N'$  Charged current quasi-elastic scattering



Accelerator based experiment  $\rightarrow$  Known neutrino direction

#### Use direction and momentum of lepton

to reconstruct energy of neutrino

- Purity of the selected events
- Binding effects of target nucleus Fermi momentum, Binding energy etc.
- Contamination ~ Impurity Interactions other than genuine CCQE
- Multi-nucleon interaction?

#### Case 2: $E_v$ > several GeV

Charged current interactions,

#### mainly $\nu$ + N $\rightarrow$ / + N' + hadrons

(Charged current deep/shallow inelastic scattering)



Use direction and momentum of lepton together with the observed energy of hadrons to estimate the energy of neutrino. Event topologies of neutral current interactions and electron neutrino charged current interactions are quite similar in some detectors.

#### Case 2: $E_v$ > several GeV

Charged current interactions,

### mainly $\nu$ + N $\rightarrow$ / + N' + hadrons

Neutrino interaction / flavor identification using simulated data catalogues (MINOS)



#### Case 2: $E_v$ > several GeV

Charged current interactions,

### mainly $\nu$ + N $\rightarrow$ / + N' + hadrons

Neutrino flavor identification using neural network (NOvA)



equivalent to 30% more exposure

Precise simulation programs are required.

Determination of neutrino oscillation parameters

Neutrino-nucleus interactions

~ Major source of uncertainties in oscillation analyses

Dedicated neutrino detectors are located in the  $\nu$  beamline to measure  $\nu$  flux and interactions.

Systematic error for # of events ( for 1 ring events ) @ T2K



## Determination of neutrino oscillation parameters

Neutrino-nucleus interactions

~ Major source of uncertainties in oscillation analyses



Need to understand the neutrino-nucleus interaction. This will reduce the errors from neutrino-nucleus interactions and also, improve the accuracy of the flux measurements with the near detectors. Accelerator based neutrino oscillation experiments



# Difficulties in the neutrino oscillation experiments 1) Neutrino beam energy is not monochromatic



Energy of each observed "neutrino" is reconstructed from experimental observables

#### or

observables (distributions) are compared with the simulation using the "oscillated" neutrino flux. Difficulties in the neutrino oscillation experiments

2) Various kinds of interactions are contained in the sample. Exact energy transfer or momentum transfer values are not available.



Difficulties in the neutrino oscillation experiments

- 3) Understanding of neutrino-nucleus interactions are far from perfect.
  - Neutrino-nucleon scattering data
    - $D_2$  Bubble chamber data in '70s ~ '80s

Low statistics and large systematic errors.

 Recently, there are high quality neutrino-nucleus scattering data are available.

However, acceptances of low momentum nucleons

are insufficient.



Deep inelastic scatterings  $v + N \rightarrow I + hadrons$ Dominant interaction in the high energy region

$$\frac{d^2\sigma^{\nu}}{dxdy} = \frac{G_F^2 m_N E_{\nu}}{\pi} \left[ (1-y+\frac{1}{2}y^2+C_1)F_2(x) + y(1-\frac{1}{2}y+C_2)[xF_3(x)] \right]$$

We need to know F2 or xF3 (structure functions). Differential cross-section ( $d\sigma/dq^2$ ) has peak in small  $|q^2|$ . However, PDFs are not valid for small  $|q^2|$  and small W.

Bodek & Yang proposed low q<sup>2</sup> corrections for GRV98. (Fit various data to extract correction factors.)

Experiments use their correction in the simulation. <sup>1 2</sup> Better to have independent studies.



 $|q^{2}|(GeV^{2}/c^{2})$ 

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## How about xF<sub>3</sub>?

## Deep inelastic scatterings

 $v + N \rightarrow I + hadrons$ 

Structure function is known to have nuclear modifications

Recently, nuclear dependences of neutrino-nucleus differential cross-section was reported but the behavior seems to be different from electron scattering.



Theoretical studies of "nuclear PDF" have been started. *Further measurements and studies are necessary.* 25

## Inclusive neutrino-nucleus scattering measurements

MINERvA experiment measured the relation

between reconstructed 3 momentum transfer

and observed energy of hadrons.

However, their simulation program can not reproduce the distribution.



Due to multi-nucleon interactions (  $\nu + N_1 + N_2 \rightarrow l^- + N_1' + N_2''$  )  $2_6$ 

Charged current quasi-elastic scattering  $v + n \rightarrow l + p$ 

Extension from nucleon scattering to nucleus scattering: simple Fermi-gas model has been widely used. ( R. Smith and E. Moniz, Nucl. Phys. B43, 605 (1972) ).

Since K2K (~2000), several disagreements are found:

1) Forward going muon is larger than data

~ larger suppression in small q<sup>2</sup>

2) Larger # of "CCQE-like" events are observed

One solution is to increase  $M_A$  for CCQE by O(20%).



Charged current quasi-elastic scattering  $v + n \rightarrow t + p$ 

Cross-section of CCQE-like events Measured value is much larger than the simple model predictions

Due to the problem in the parameters measured in the old experiments? Is single nucleon scattering

with impulse approximation insufficient?



 Contribution from 2 nucleon interaction? Recent experiments did not measure low momentum nucleons.
 → It is not possible to discriminate single nucleon interaction from multi-nucleon interactions.

Interestingly, large suppression is observed in the forward ( small  $q^2$  ) region.

## Multi-nucleon interactions



If the discrepancies between CCQE prediction and CCQE-like observed events, are caused by bound nucleon scattering, reconstructed energy is shifted for those events.

The fraction of these events is less than ~ 20% of true CCQE ( if we assume naive model ) but the effects may be visible in precise experiments.



New experiments and theoretical studies to understand neutrino induced multi-nucleon scatterings have been started.

Nuclear effects ~ pion interaction in nucleus Pion interactions in nucleus is also important because these interactions affect determination of neutrino-nucleus interaction channel.



However, old data sets have  $\sim 30$  % errors. Also, a few data sets available above  $\Delta$  region.



Nuclear effects ~ pion interaction in nucleus DUET experiments used fiber tracker to measure pion absorption & charge-exchange cross-sections.



Almost back to back protons are observed after absorption. ( Correlated pair nucleon absorbed π<sup>+</sup> ?) Size of the error gets smaller.

#### Need higher precision measurements above delta region.

## Summary

Study of neutrino oscillation using atmospheric and accelerator neutrinos heavily rely on the neutrino-nucleus scattering Monte-Carlo simulation programs.

Uncertainties from neutrino-nucleus scattering is one of the largest source of systematic errors.

It is necessary to reduce the errors for the discovery and parameter measurements of CP violation, mass hierarchy determination and precise determination of neutrino oscillation parameters.

PDF for low q<sup>2</sup> and low W and nuclear corrections, multinucleon interactions and pion interactions in nucleus will be important topics to be understood for the next generation experiments.



15-19 October 2018 Gran Sasso Science Institute (GSSI) Europe/Zurich timezone

Search ...

https://indico.cern.ch/event/703880/

Since 2001, a series of workshop was started to discuss neutrino-nucleus interactions from both theoretical and experimental aspects.

This year, the 12<sup>th</sup> workshop will be held at Gran Sasso Science Institute in Italy. (October 15 ~ 19)

There will be a satellite meeting to discuss Shallow and Deep inelastic scattering. (October 11 ~ 13) Q

#### fin.