

WG6: Spin and 3D structure Summary

Yoshitaka Hatta, Kenichi Nakano, Sanghwa Park

Apologies for omissions and inaccuracies...

WG6: Scope

Spin {
Longitudinal spin – sum rules, gluon helicity
Transverse spin – transversity, single spin asymmetry

3D structure {
TMD – sign flip, linearly polarized gluon,
fragmentation function
GPD – Ji sum rule, twist three

18 theory talks, 15 experimental talks,
two joint sessions (with WG1 and WG7)


Longitudinal spin

The proton spin problem

Jaffe-Manohar decomposition

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L^q + L^g$$

Quarks' helicity Gluons' helicity Orbital angular Momentum



Quark helicity reasonably constrained $\Delta\Sigma = 0.25 \sim 0.3$

Gluon helicity nonzero!

But the uncertainty in the small-x is huge, need more effort

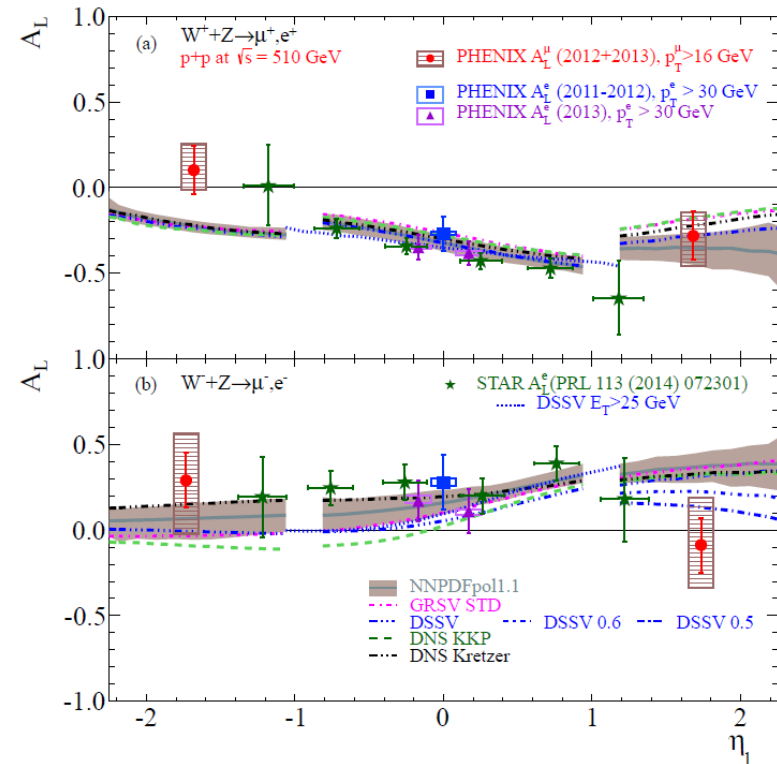
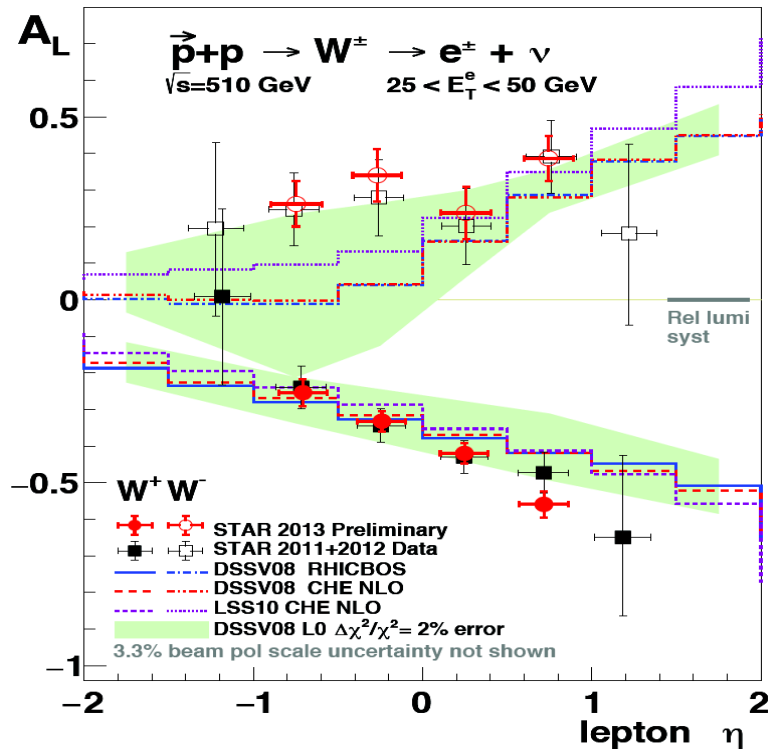
Little is known about orbital angular momentum

Longitudinal Single-Spin Asymmetry of W in pp at RHIC

Determination of $\Delta\bar{d}$ $\Delta\bar{u}$

B. Surrow

C. Kim



Improved accuracy with latest datasets & better W identification.

Also the ratio \bar{d}/\bar{u} can be determined from STAR measurement of W^+/W^- ratio.

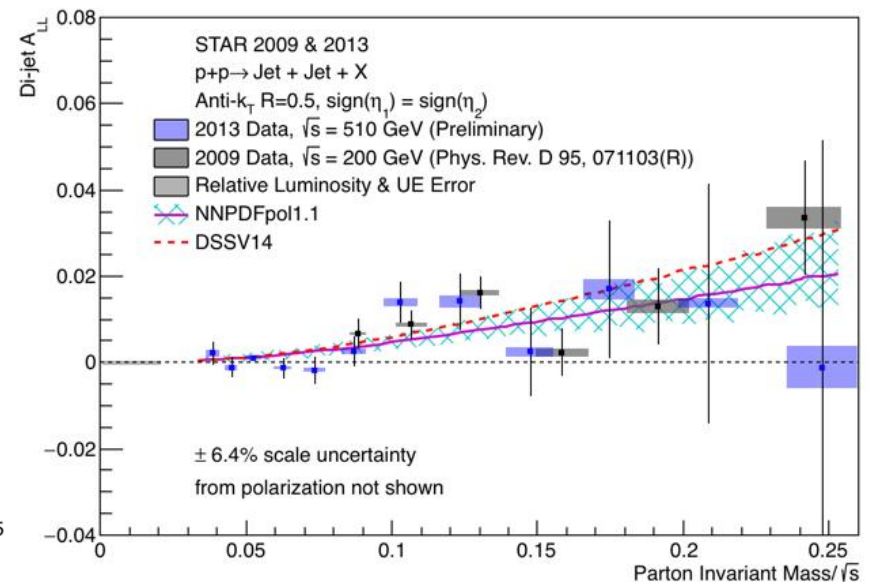
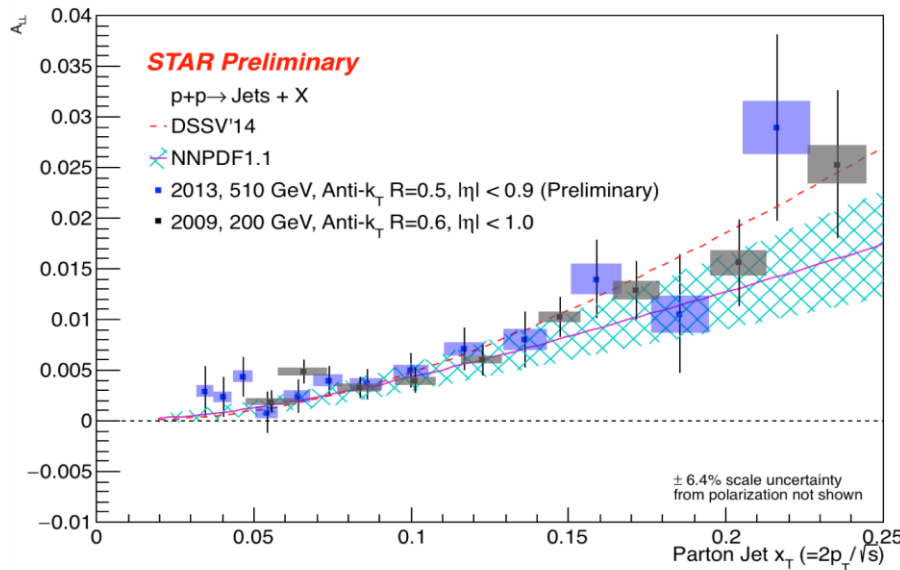
Gluon Polarization via Jets in pp at RHIC

Double helicity asymmetry A_{LL} of inclusive jets & di-jets at 200 & 510 GeV by STAR & PHENIX

A. Quintero

Z. Chang

M. Patel



Improved accuracy with latest datasets & better jet reconstruction.
Inclusive hadron (e.g. pion) productions were measured also.

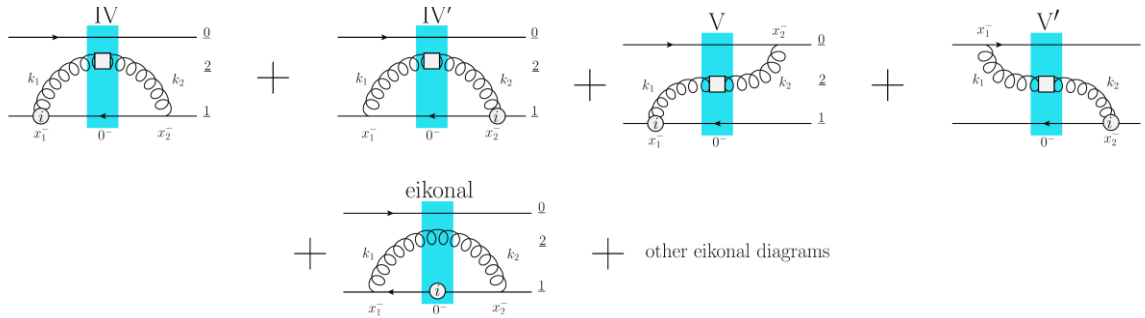
Helicity evolution at small-x

M. Sievert

Small-x evolution of the **polarized** dipole

$$G(x_{10}^2, z) = G^{(0)}(x_{10}^2, z) + \frac{\alpha_s N_c}{2\pi} \int_{\frac{1}{x_{10}^2 s}}^z \frac{dz'}{z'} \int_{\frac{1}{z' s}}^{x_{10}^2} \frac{dx_{21}^2}{x_{21}^2} [\Gamma(x_{10}^2, x_{21}^2, z') + 3G(x_{21}^2, z')]$$

$$\Gamma(x_{10}^2, x_{21}^2, z') = G^{(0)}(x_{10}^2, z') + \frac{\alpha_s N_c}{2\pi} \int_{\frac{1}{x_{10}^2 s}}^{z'} \frac{dz''}{z''} \int_{\frac{1}{z'' s}}^{\min[x_{10}^2, x_{21}^2 \frac{z'}{z''}]} \frac{dx_{32}^2}{x_{32}^2} [\Gamma(x_{10}^2, x_{32}^2, z'') + 3G(x_{32}^2, z'')]$$



Resummation of double logarithms $\alpha_s \ln^2 \frac{1}{x} \rightarrow \Delta f(x) \sim \left(\frac{1}{x}\right)^{\alpha_h}$

$$\alpha_h^{q,S} = \frac{4}{\sqrt{3}} \sqrt{\frac{\alpha_s N_c}{2\pi}}$$

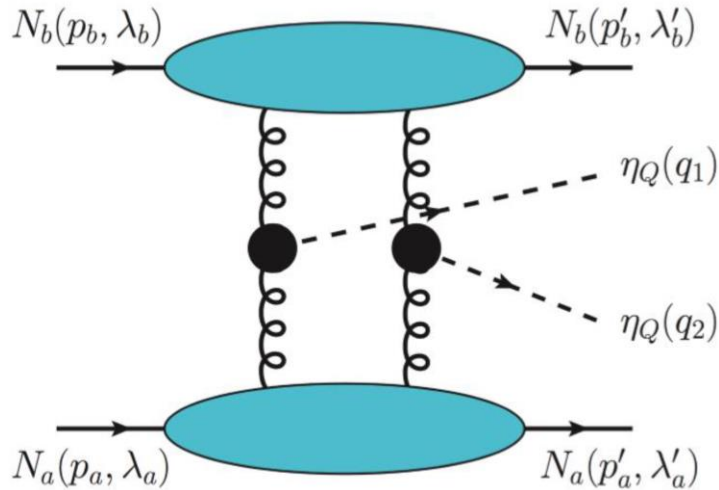
$$\alpha_h^{q,NS} = \sqrt{2} \sqrt{\frac{\alpha_s N_c}{2\pi}}$$

$$\alpha_h^G = \frac{13}{4\sqrt{3}} \sqrt{\frac{\alpha_s N_c}{2\pi}}$$

Parton orbital angular momentum

Double η_C - production in pp

S. Bhattacharya



$$\frac{1}{2}(\tau_{XY} - \tau_{YX})$$

$$\approx 2 \text{Re} \left\{ -\frac{1}{M^2} (\epsilon_{\perp}^{ij} \Delta q_{\perp}^i \Delta_{a\perp}^j) C[\vec{\beta}_{\perp} \cdot \vec{k}_{a\perp} F_{1,4}] \right\}$$

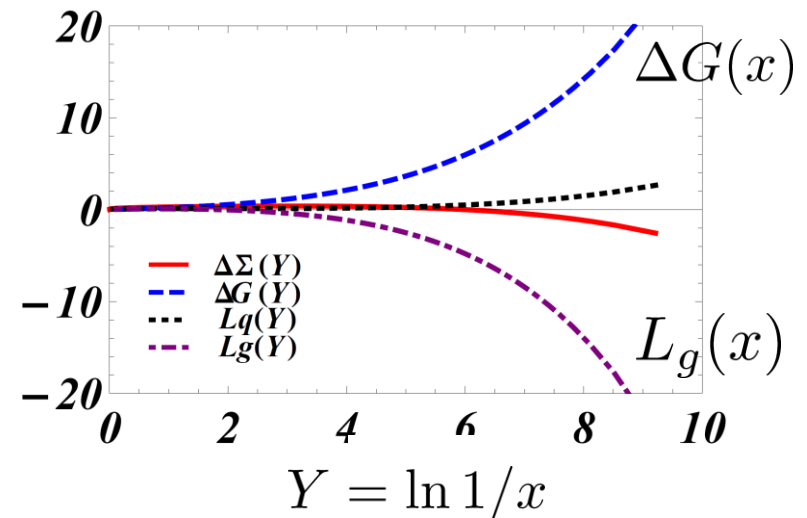
Moment of $F_{1,4}$

→ Gluon orbital angular momentum

Y. Hatta

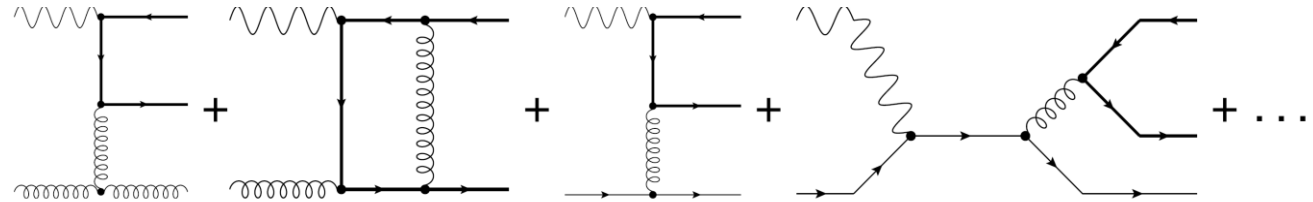
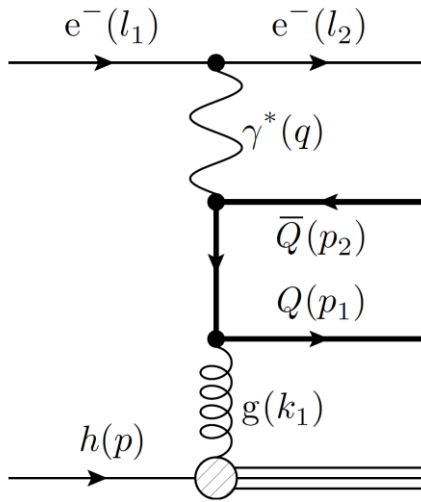
'DGLAP' evolution of OAM density $L_g(x)$

$$L_g(x) \approx -\Delta G(x) \text{ at small-}x$$



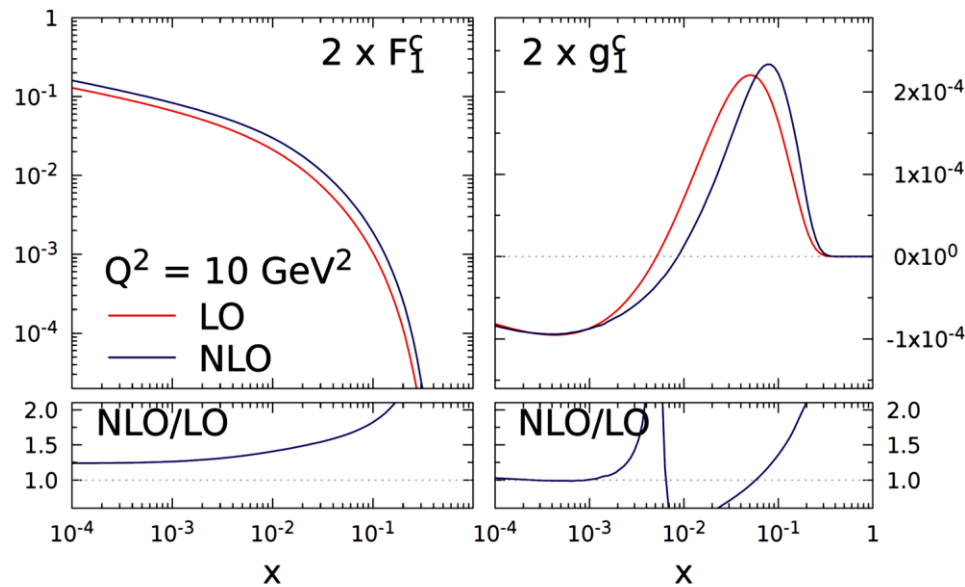
NLO heavy-flavor production in polarized DIS

F. Hekhorn



Full NLO analytical calculation.

NLO corrections large, both for unpolarized/polarized

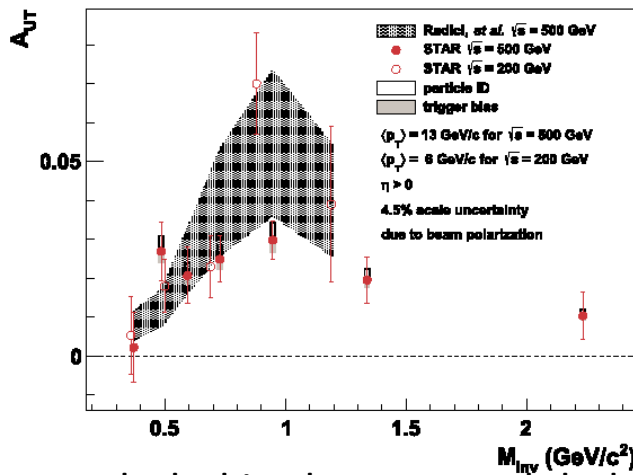


Transverse spin

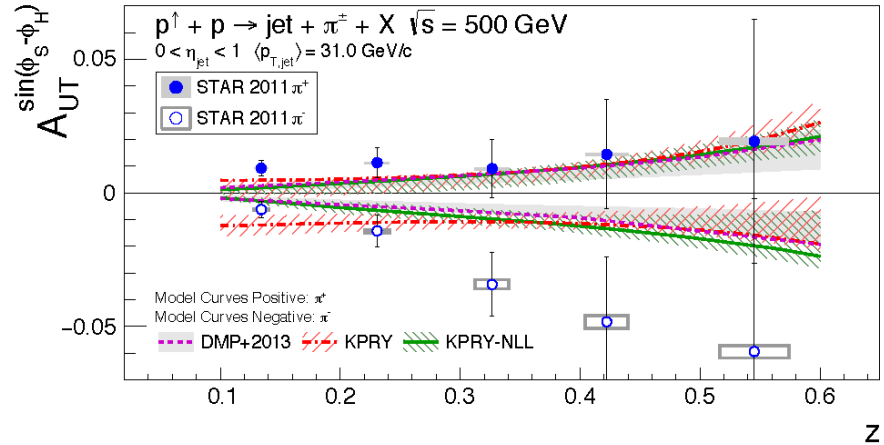
Transversity

C. Gagliardi

- STAR: Transversity via IFF and Collins FF



Included in the recent global analysis (Radici and Bacchetta)

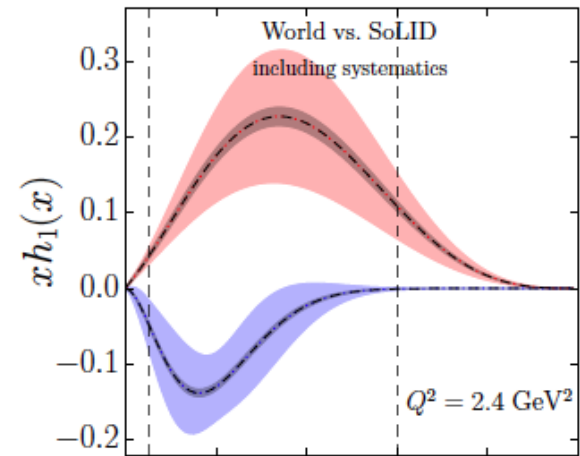


First Collins effect measurements in pp collisions

- Universality test of Collins FF
- TMD evolution effects appear to be small

- HERMES, COMPASS and JLab 6 GeV SIDIS data
- JLab 12 GeV upgrade and beyond

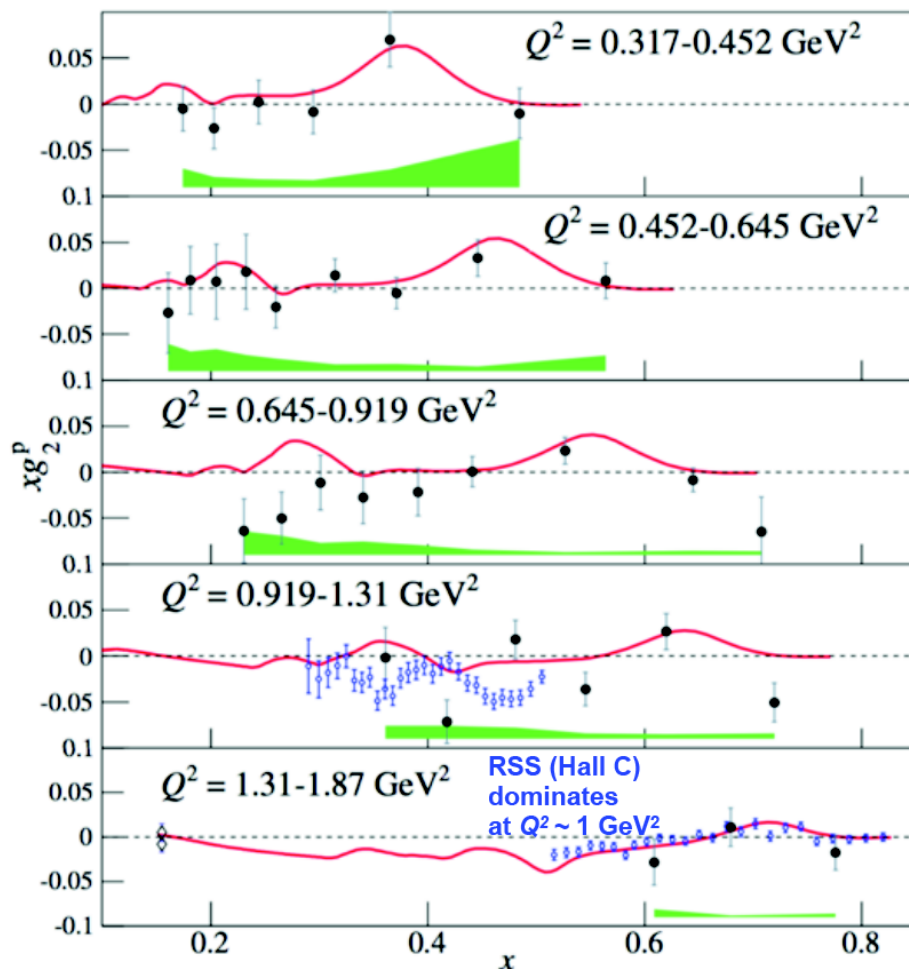
H. Gao



Measurement of $g_2(x)$ by CLAS

First extraction of g_2 from EG1 experiment.

R. Fersch

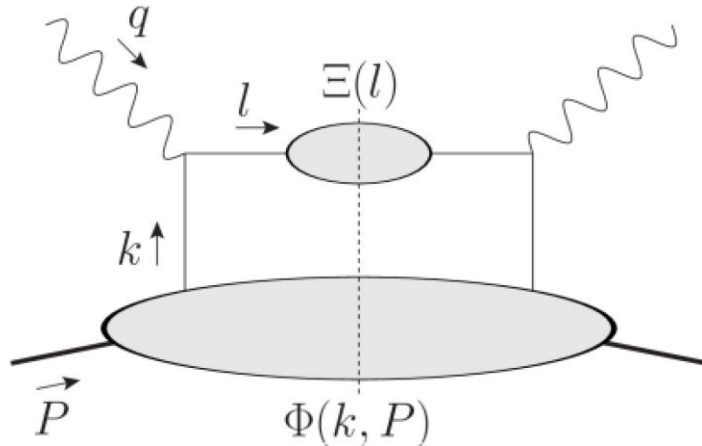


Little world data available!

Useful for extracting higher-twist matrix elements.

New contribution to $g_2(x)$

A. Accardi



Jet correlators

$$\Xi_{ij}(l, n_+) = F.T. \langle 0 | \mathcal{U}_{(+\infty, \eta)}^{n_+} \psi_i(\eta) \bar{\psi}_j(0) \mathcal{U}_{(0, +\infty)}^{n_+} | 0 \rangle$$

$$g_2(x_B) - g_2^{WW}(x_B) = \frac{1}{2} \sum_a e_a^2 \left(\underbrace{g_2^{q, \text{tw}3}(x_B)}_{\equiv g_2^{\text{quark}}} + \frac{m_q}{M} \left(\frac{h_1^q}{x} \right)^* (x_B) + \underbrace{\frac{M_q - m_q}{M} \frac{h_1^q(x_B)}{x_B}}_{\equiv g_2^{\text{jet}}} \right)$$

Color force distribution

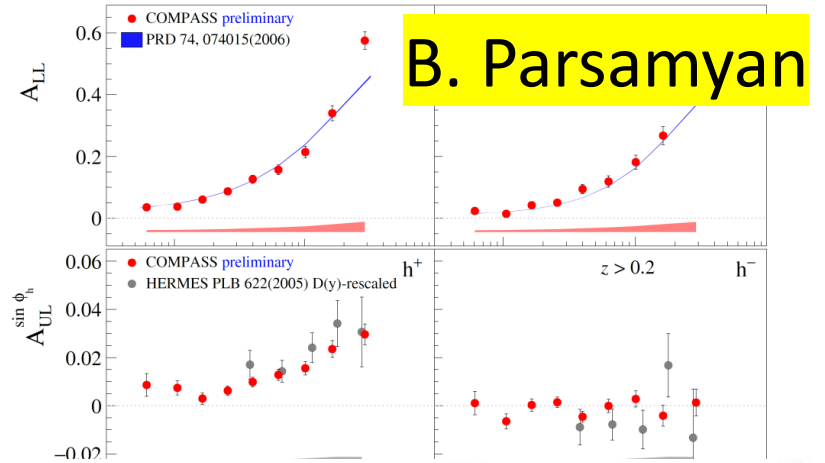
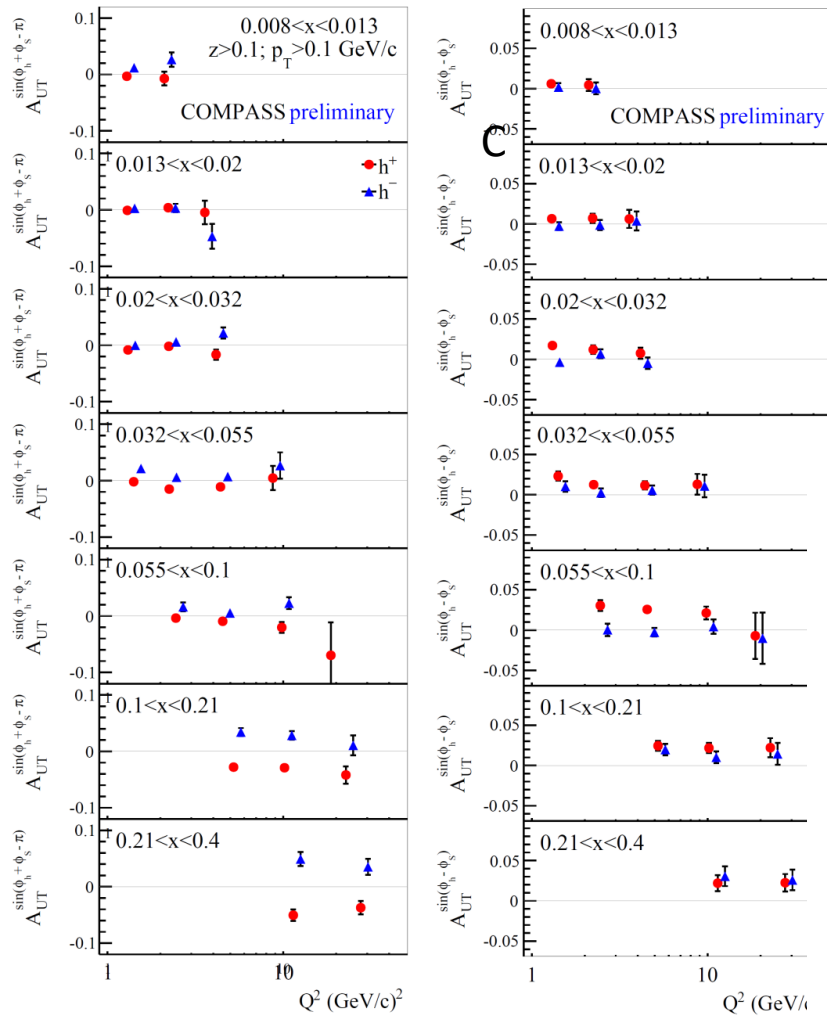
Transversity in inclusive DIS!

Burkardt-Cottingham

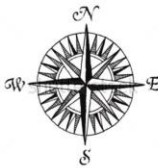
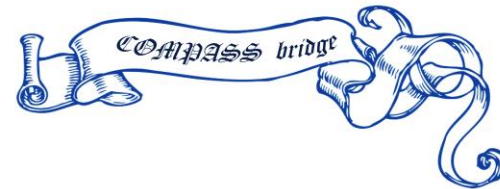
$$\int_0^1 g_2(x) = M_{\text{jet}} \int_0^1 dx \frac{h_1(x)}{x}$$

→ Broken by quark vacuum fluctuations!

Compass SIDIS Single Spin Asymmetries



B. Parsamyan



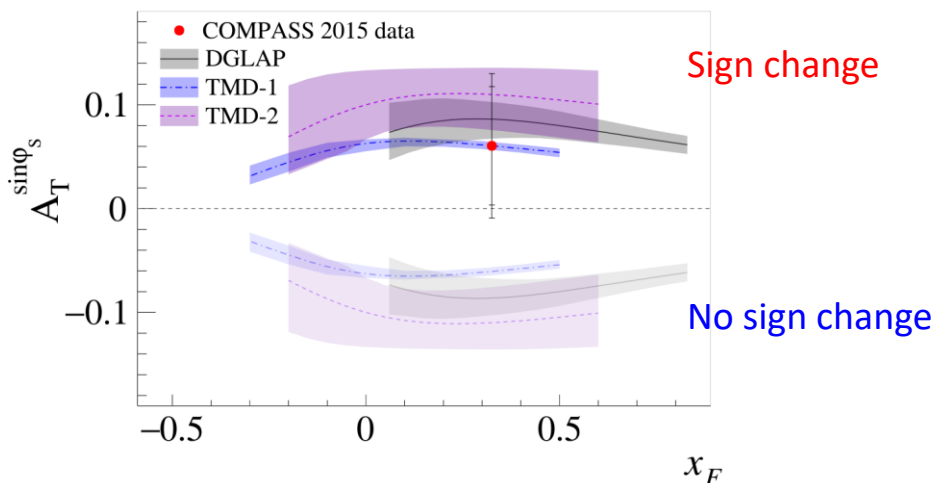
Drell-Van

SIDIS

Multidimensional analysis of SIDIS proton SSAs
No hints for significant Q²-dependences of
Sivers and Collins TSAs

Sign change of Sivers function

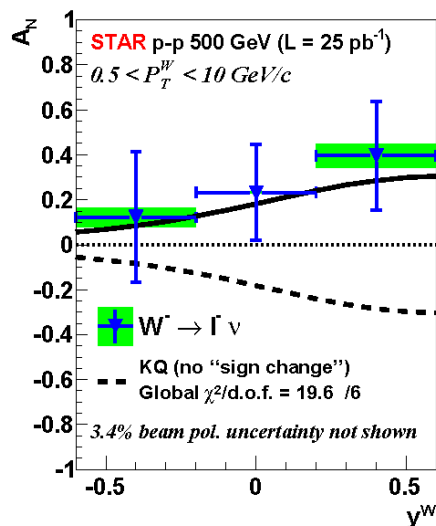
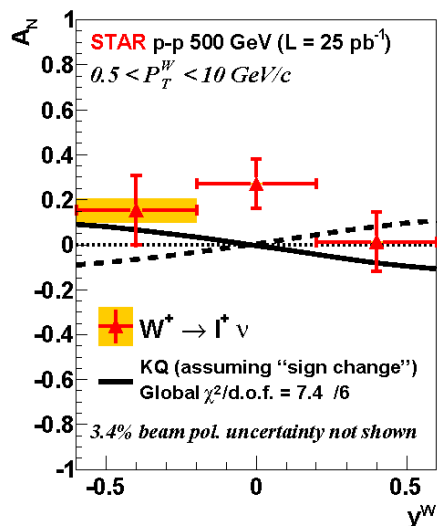
COMPASS DY Measurement



M. Chiosso

More data coming! - 2018 second year of polarized DY data taking

W, Z and DY measurement from STAR



C. Gagliardi

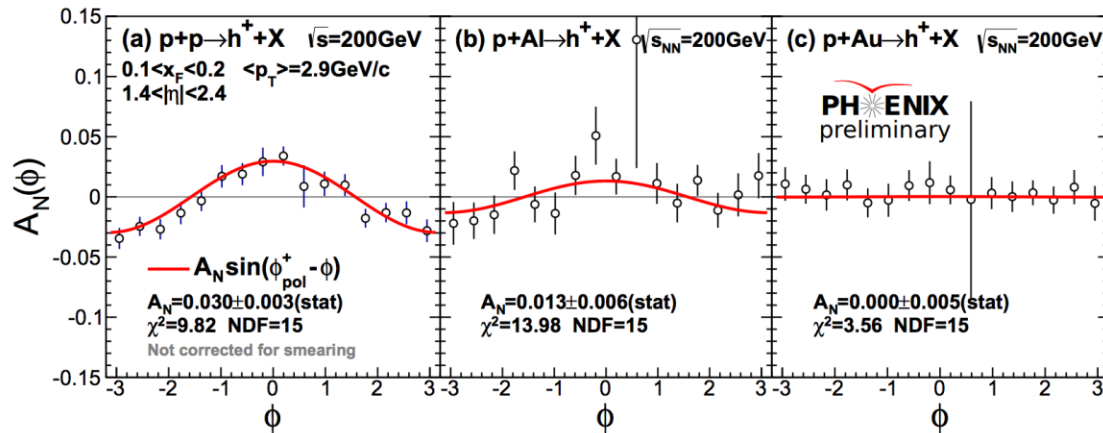
STAR data favors sign change if evolution effects are modest

High precision data from 2017 RHIC run under analysis

Nuclear dependence A_N

J. Bok

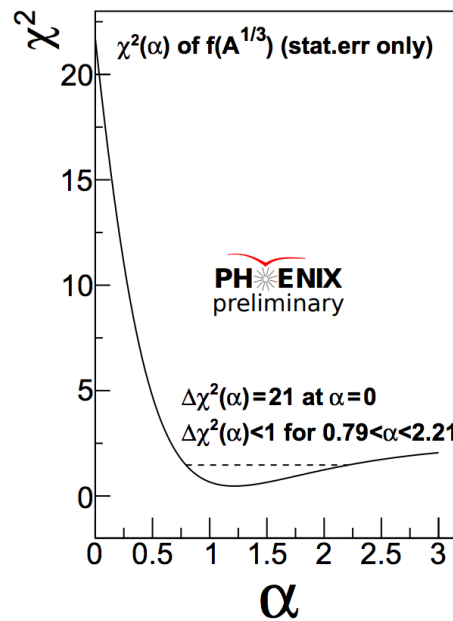
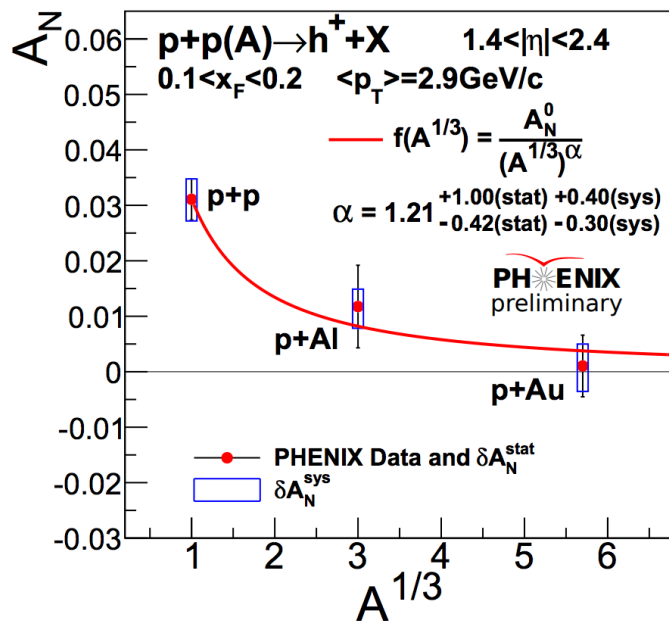
- PHENIX charged hadron A_N in polarized pA



A_N of charged pion and kaon mixture

Non-zero A_N observed for positively charged hadrons in p+p

Clear suppression in p+Au

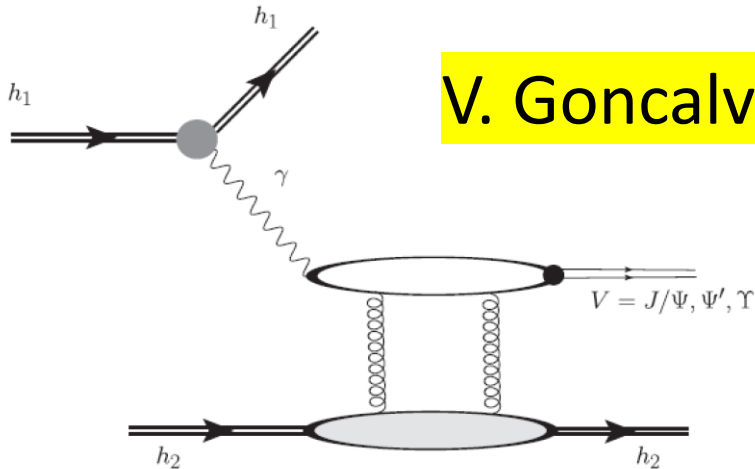


$A^{1/3}$ suppression by gluon saturation is expected

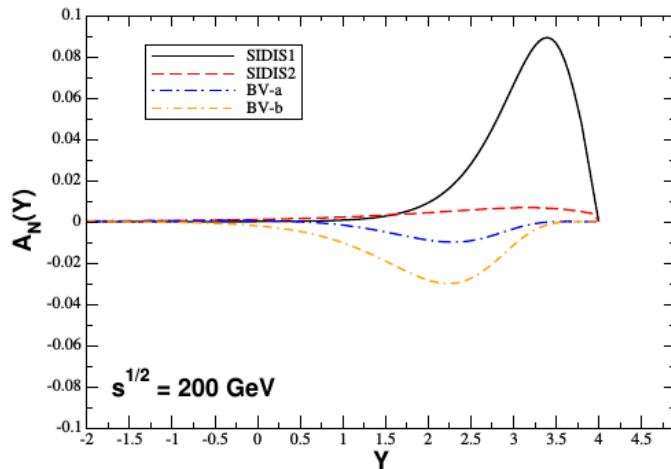
Data favors an A-dependence:
 $\Delta\chi^2 = 21$ at $\alpha = 0$ (NO A-dep), out of 4sigma

Single and Double Spin Asymmetry theory

A_N of J/ψ in UPC



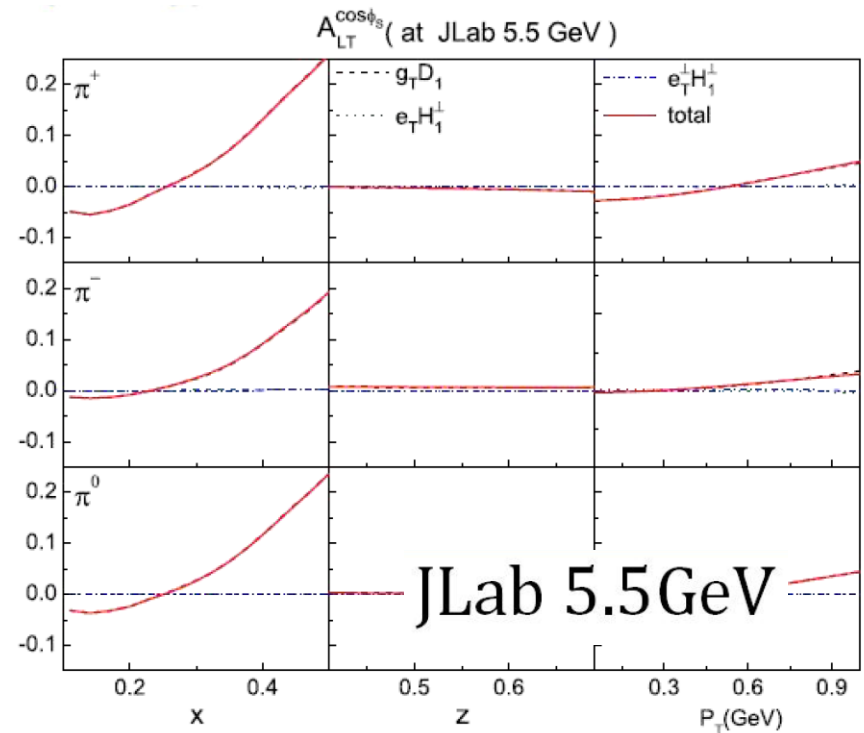
V. Goncalves



sensitive to gluon Sivers

A_{LT} in SIDIS in the collinear twist-three framework

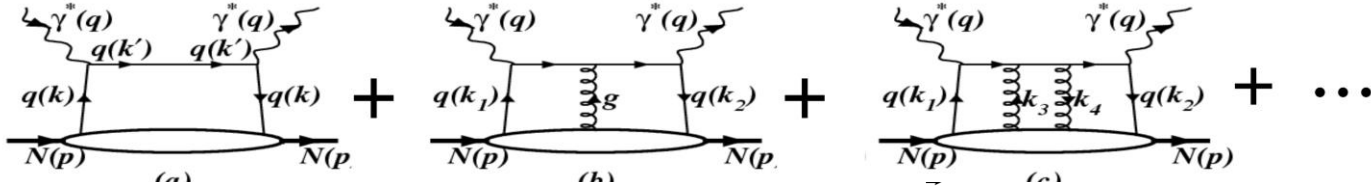
W. Mao



TMD

SIDIS theory

Z.-T. Liang



Complete results for structure functions up to twist-4

$$\kappa_M \equiv \frac{M}{Q}, \quad \bar{k}_\perp \equiv \frac{|\vec{k}_\perp|}{M}$$

$$W_{UU,T} = xf_1 + 4x^2 \kappa_M^2 f_{+3dd}, \quad W_{UU,L} = 8x^3 \kappa_M^2 f_3$$

$$W_{UU}^{\cos 2\phi} = -2x^2 \kappa_M^2 \bar{k}_\perp^2 f_{-3d}^\perp$$

$$W_{UL}^{\sin 2\phi} = 2x^2 \kappa_M^2 \bar{k}_\perp^2 f_{+3dL}^\perp$$

$$W_{LL} = xg_{1L} + 4x^2 \kappa_M^2 f_{+3ddL}$$

$$W_{UT,T}^{\sin(\phi-\phi_S)} = \bar{k}_\perp (xf_{1T}^\perp + 4x^2 \kappa_M^2 f_{+3ddT}), \quad W_{UT,L}^{\sin(\phi-\phi_S)} = 8x^3 \kappa_M^2 \bar{k}_\perp f_{3T}^\perp$$

$$W_{UU}^{\cos \phi} = -2x^2 \kappa_M \bar{k}_\perp f^\perp$$

$$W_{UL}^{\sin \phi} = -2x^2 \kappa_M \bar{k}_\perp f_L^\perp$$

$$W_{LU}^{\sin \phi} = 2x^2 \kappa_M \bar{k}_\perp g^\perp$$

$$W_{LL}^{\cos \phi} = -2x^2 \kappa_M \bar{k}_\perp g_L^\perp$$

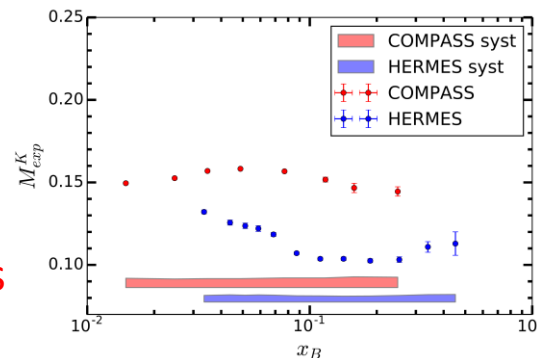
$$W_{UT}^{\sin \phi_S} = -2x^2 \kappa_M f_T$$

J. Guerrero

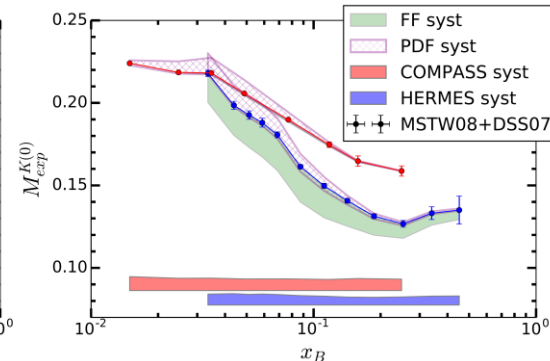
Kaon production in SIDIS,
sensitive to s-quark distribution

Tension between COMPASS and HERMES
Partly reconciled by **hadron mass effects**

Experimental Data



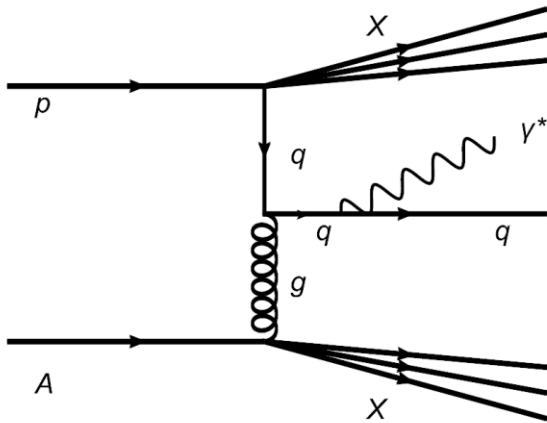
“Massless data” at same Q^2



Linearly polarized gluon distribution

$$\Phi_g^{\mu\nu}(x, \mathbf{k}_T, \zeta, \mu) = -\frac{1}{2x} \left\{ g_T^{\mu\nu} f_1^g(x, k_T, \mu) - \left(\frac{k_T^\mu k_T^\nu}{M_p^2} + g_T^{\mu\nu} \frac{k_T^2}{2M_p^2} \right) h_1^{\perp g}(x, k_T, \mu) \right\}.$$

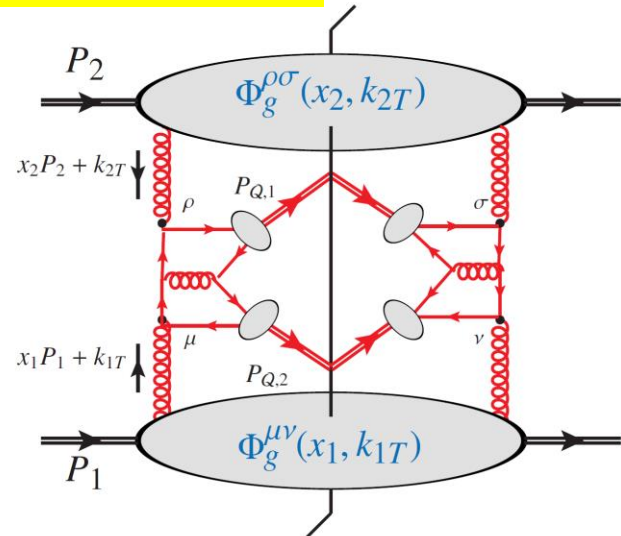
Y. Zhou



$\cos(2\phi)$ asymmetry for $pA \rightarrow \gamma^* \text{ jet } X$

TMD evolution effects significant

J. Lansberg



$\langle \cos 4\phi_{CS} \rangle$ in double J/ψ production

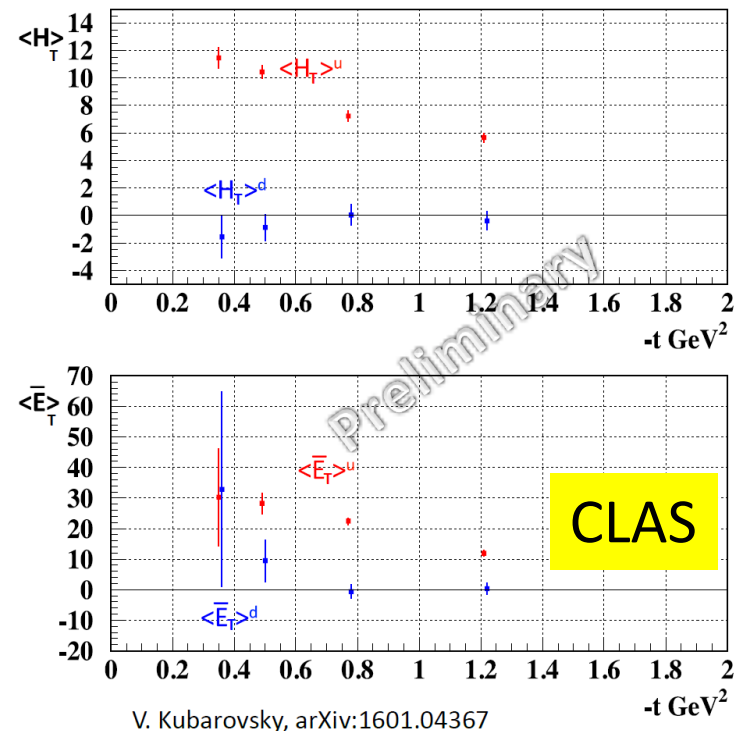
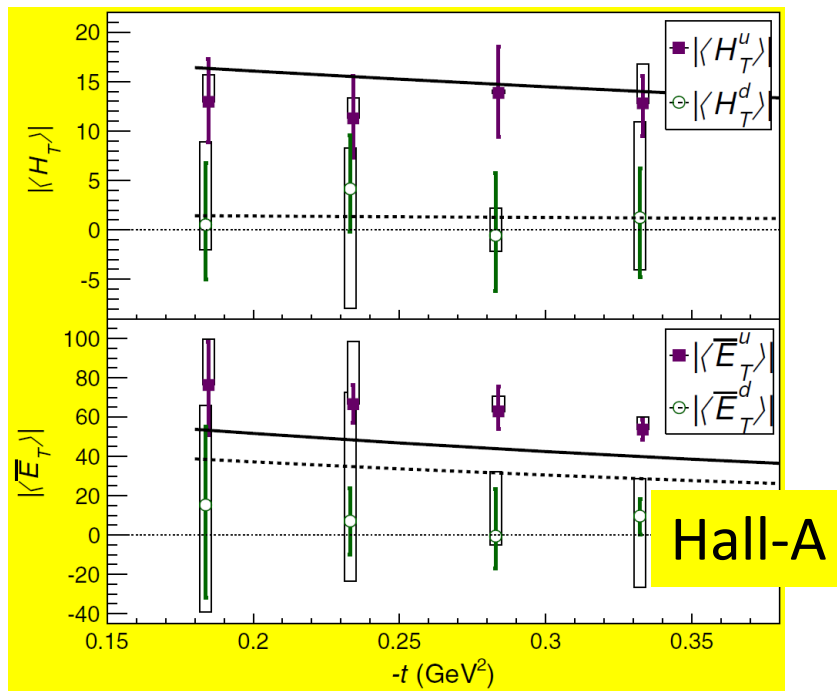
largest values ever predicted ! (up to 40 %)

GPD

GPD at JLab @ 6 GeV

C. Hyde
A. Kim

Measurement of transversity GPD (chiral odd) from
DVMP $D(e,e' \pi^0)pn$ $H(e,e' \pi^0)p$. First attempt at flavor separation

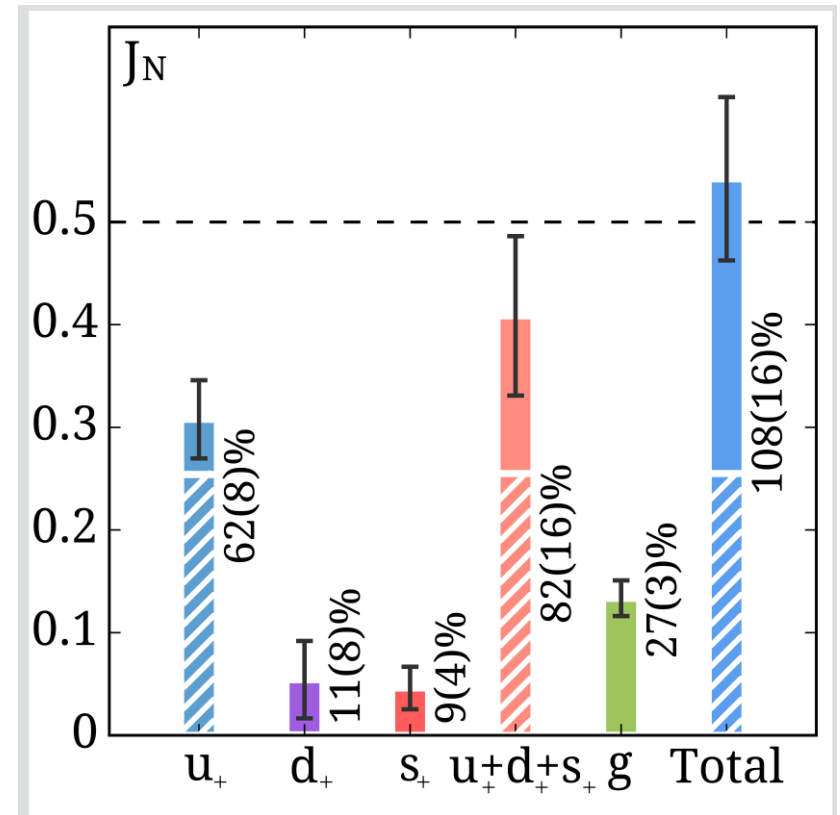
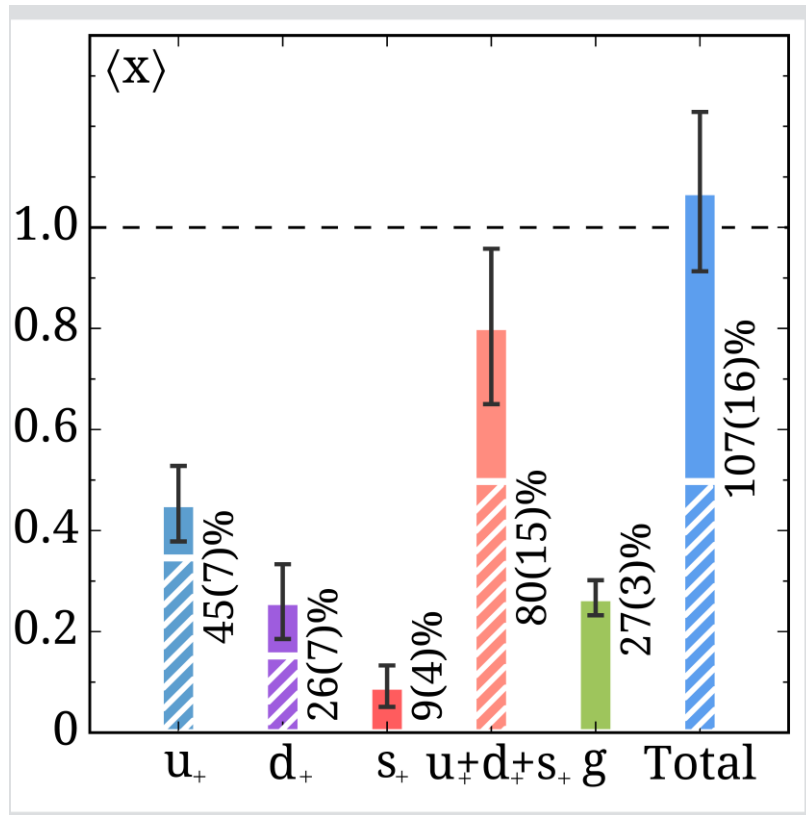


- My prediction: In 10 years, we will be confident in value of $J_{u,d}$

Lattice test of Ji sum rule

Simulations at the physical point!

K. Hadjiyiannakou



$$J_{u_++d_++s_++g}^N = 0.541(62)(49)$$

GPD theory developments

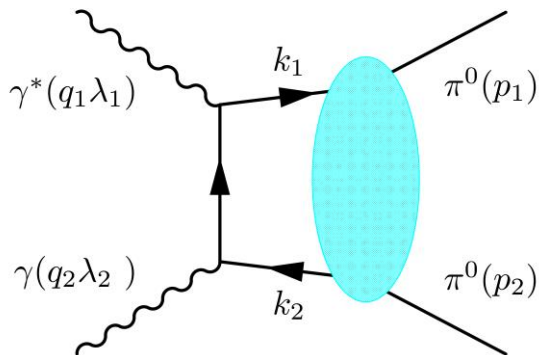
M. Burkardt

Twist-2 GPDs \rightarrow 3D imaging

Twist-3 GPDs \rightarrow Color Lorentz **force** (matrix element of $\bar{q}F^{+i}q$)

GPDs not just for the study of imaging but also for color force!

Q.-T. Song



Generalized distribution amplitude (GDA)

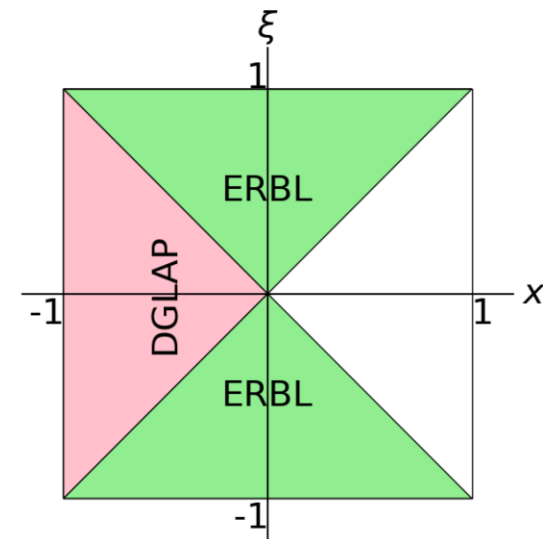
Extraction from Belle data $\gamma^* \gamma \rightarrow \pi^0 \pi^0$.

\rightarrow Mass radius of pion

N. Chouika

Knowledge of GPD $f(x, \xi, \Delta)$ in the DGLAP region $|x| > |\xi|$

\rightarrow Reconstruct the full GPD

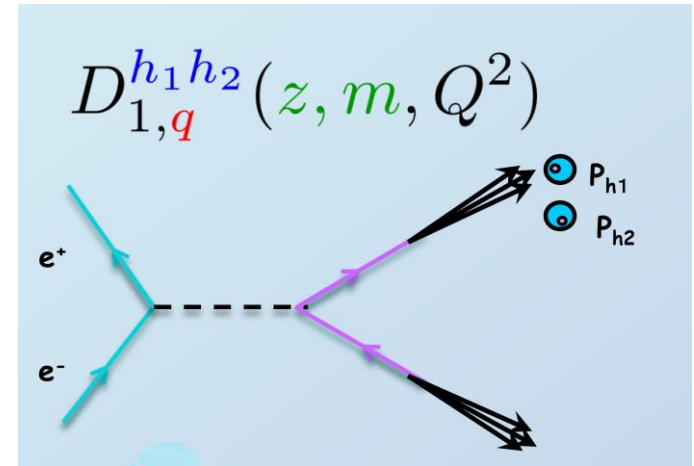
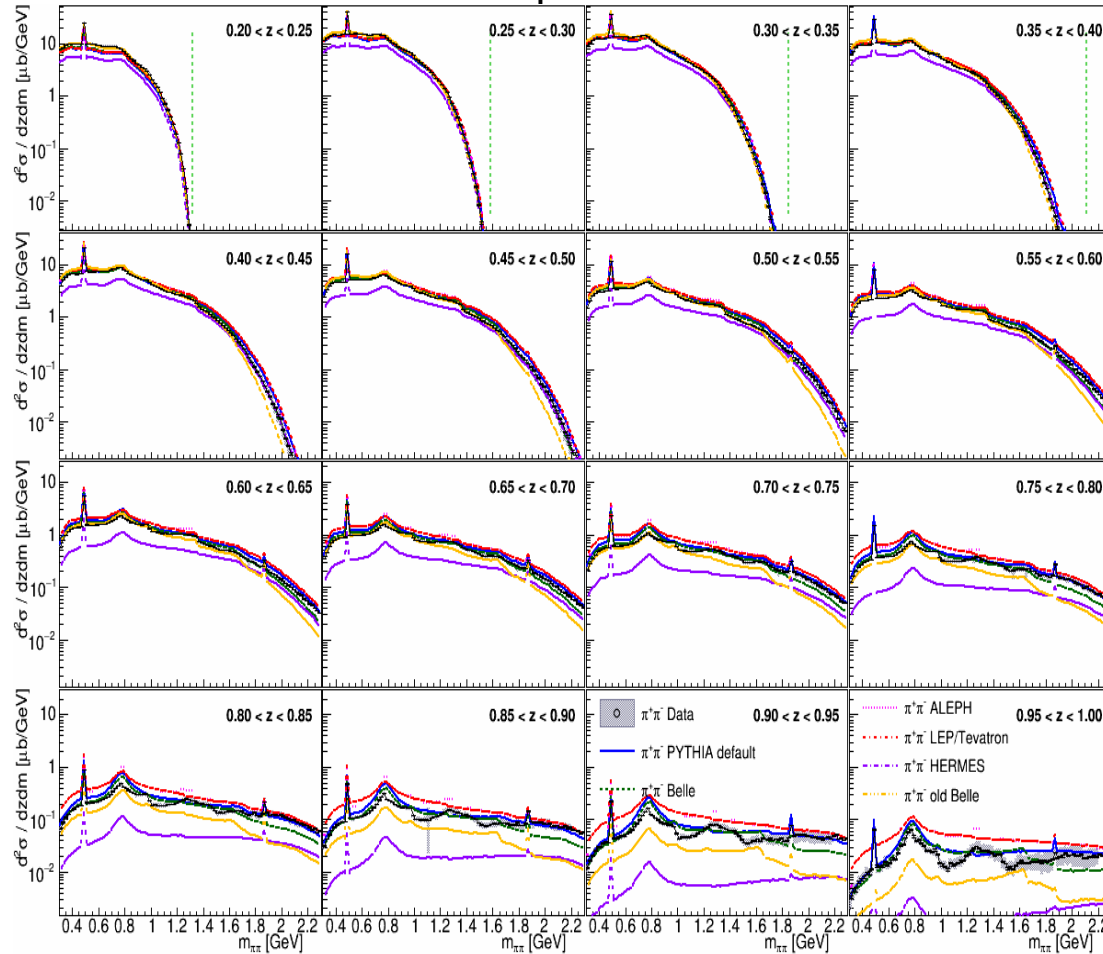


TMD fragmentation function

Fragmentation Functions from e^+e^- at Belle

R. Seidl

Di-hadrons in same hemisphere



Important input for transversity,
tensor charge extraction

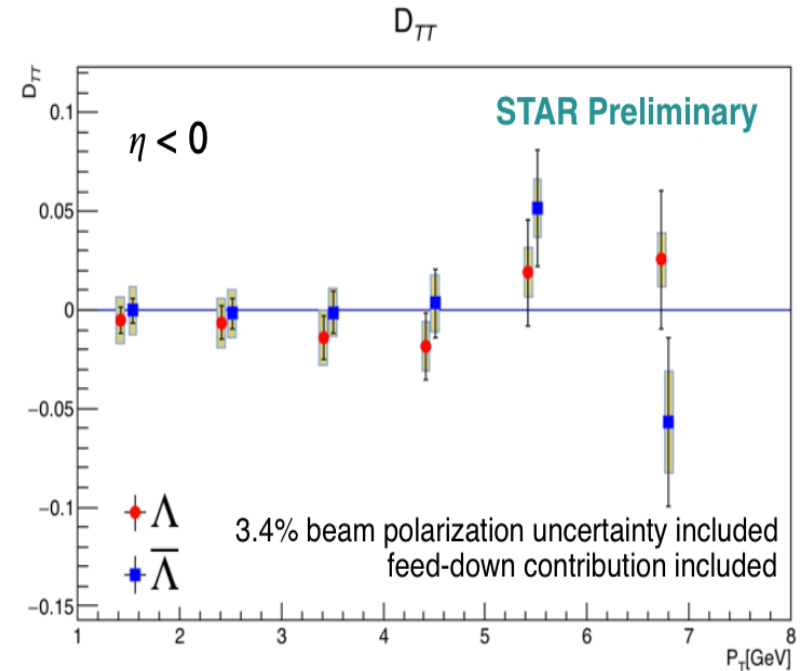
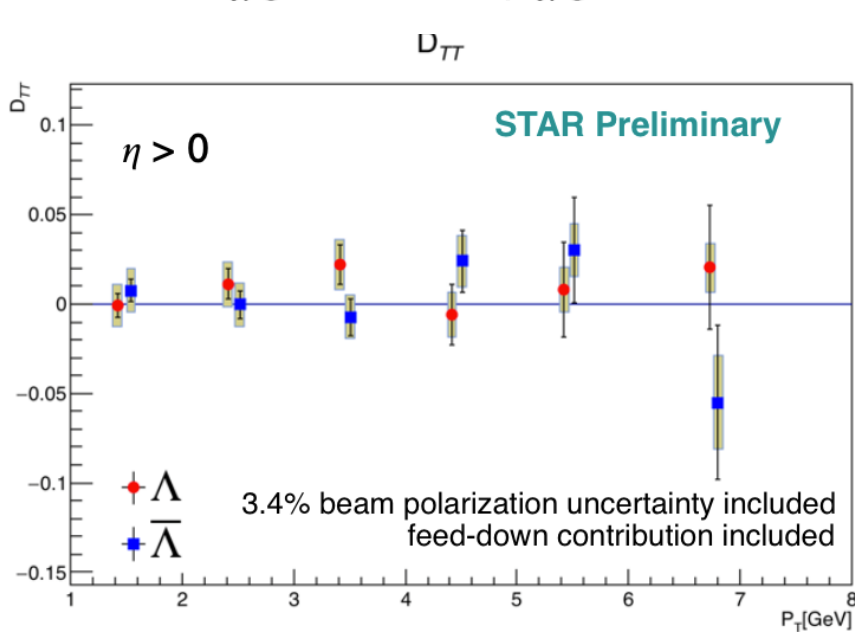
Various types (single hadron & di-hadron) of FFs (and more) were measured.

Transverse-Spin Transfer $p \rightarrow \Lambda$ in pp

$$D_{TT} \equiv \frac{d\sigma^{(p^\uparrow p \rightarrow H^\uparrow X)} - d\sigma^{(p^\uparrow p \rightarrow H^\downarrow X)}}{d\sigma^{(p^\uparrow p \rightarrow H^\uparrow X)} + d\sigma^{(p^\uparrow p \rightarrow H^\downarrow X)}}$$

measured by STAR at RHIC

Q. Xu

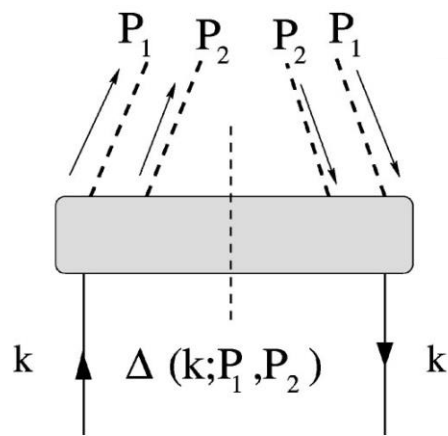


Λ spin \sim s quark's spin

Sensitive to strangeness transversity and transversely polarized fragmentation function.
To be improved in statistics and systematics.

Fragmentation function theory developments

H. Matevosyan



$$\Delta_{ij}(k; P_1, P_2) = \nabla \int d^4\zeta e^{ik \cdot \zeta} \langle 0 | \psi_i(\zeta) | P_1 P_2, X \rangle \langle P_1 P_2, X | \bar{\psi}_j(0) | 0 \rangle$$

related to "jet handedness"

$$\Delta^{\gamma^- \gamma_5] = \frac{\epsilon_T^{ij} R_{Ti} k_{Tj}}{M_h^2} G_1^\perp(z, \xi, \mathbf{k}_T^2, \mathbf{R}_T^2, \mathbf{k}_T \cdot \mathbf{R}_T)$$

New observable to access DiFFs in e+e-

→ **q_T -weighted asymmetry**

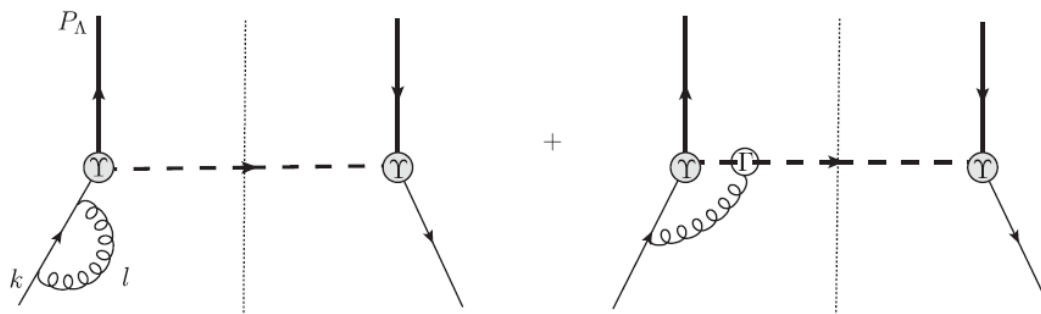
$$\left\langle \frac{q_T^2 (3 \sin(\varphi_q - \varphi_R) \sin(\varphi_q - \varphi_{\bar{R}}) + \cos(\varphi_q - \varphi_R) \cos(\varphi_q - \varphi_{\bar{R}}))}{M_h \bar{M}_h} \right\rangle$$

Y. Yang

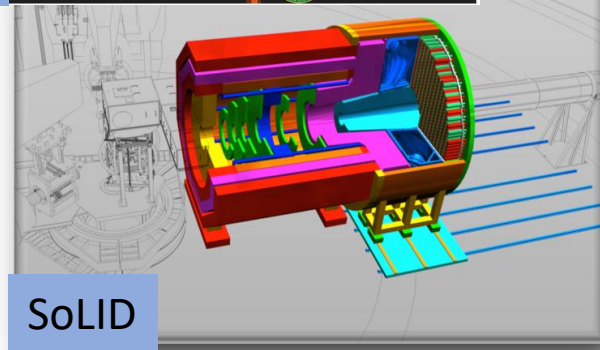
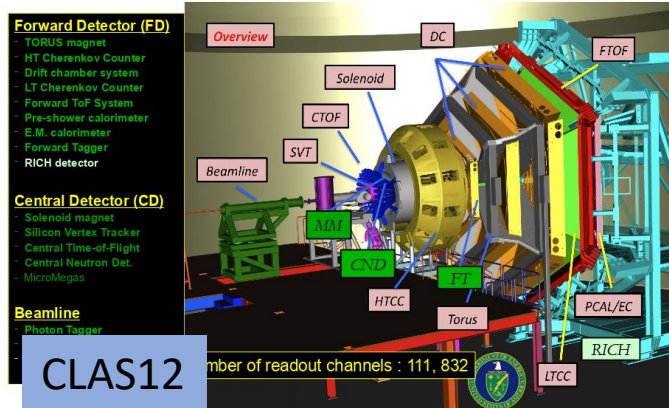
Unpolarized quark → transversely polarized Λ

T-odd. Need final state interaction
(loop corrections)

Calculated in the diquark model



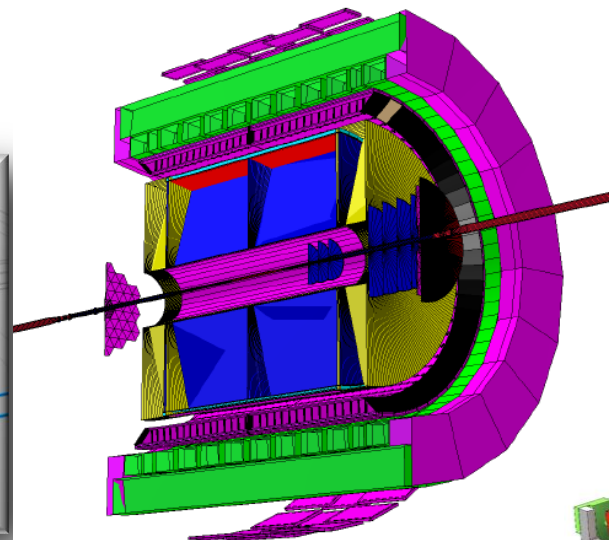
Future experiments



A. Kim
H. Gao

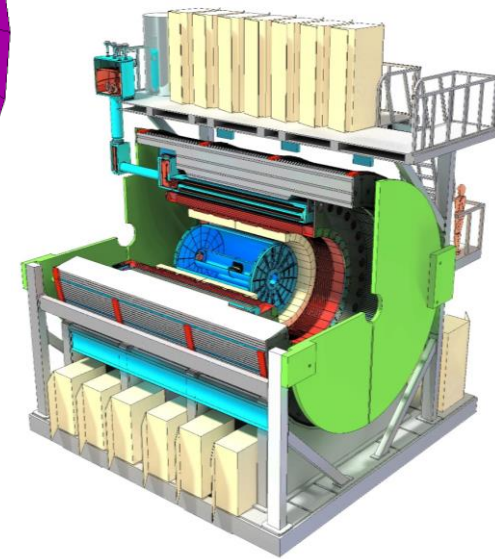
- JLab 12 GeV
Hall A, Hall C, CLAS12, SBS, SoLID, ..
Rich TMD and GPD program

- RHIC Cold QCD program
Jets at forward rapidity
Precision DY measurements



E. Aschenauer

fsPHENIX



- Future COMPASS
SIDIS measurements with transversely polarized deuteron target in 2021