



# Jet Correlation Measurements at ATLAS and the determination of the strong coupling constant

## DIS 2018

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Scattering and Related Subjects

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On behalf of the ATLAS Collaboration

**Why multi-jet cross section ratios?**

**The measured quantity**

**Measurement results**

**The strong coupling constant**

**Extraction procedure**

**Results**

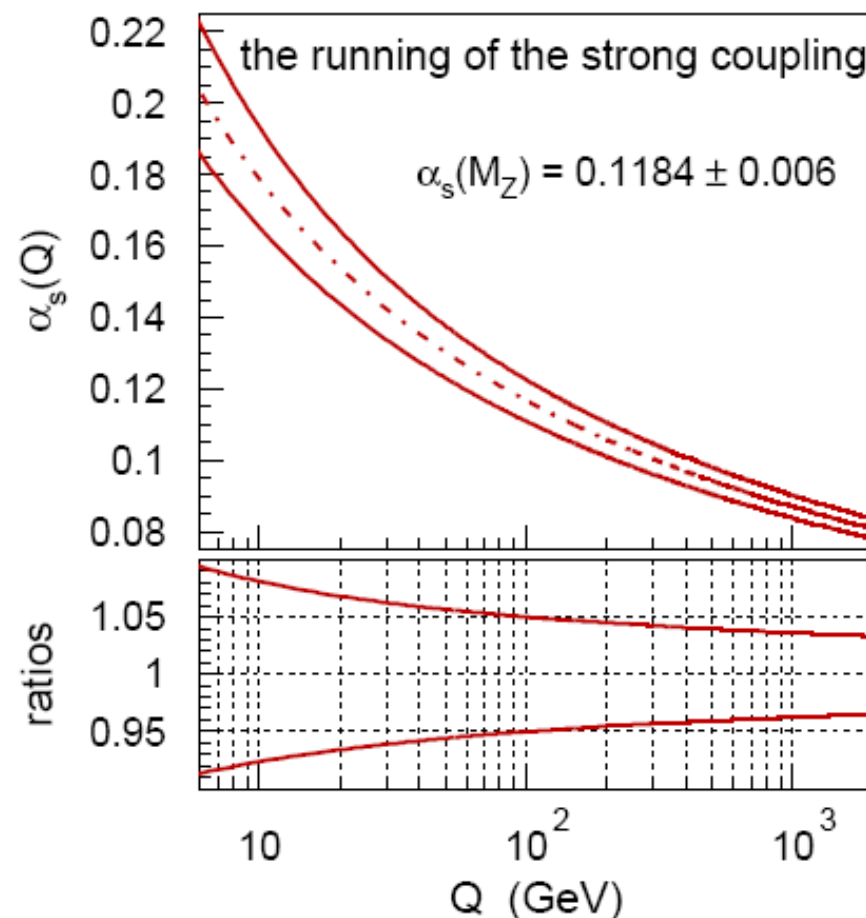
# The strong coupling and the RGE



$\alpha_s(\mu_R)$  depends on  
renormalization scale  $\mu_R$

$\mu_R$  dependence is predicted by  
Renormalization Group Equation  
(RGE)

Values of  $\alpha_s(\mu_R)$  are not predicted



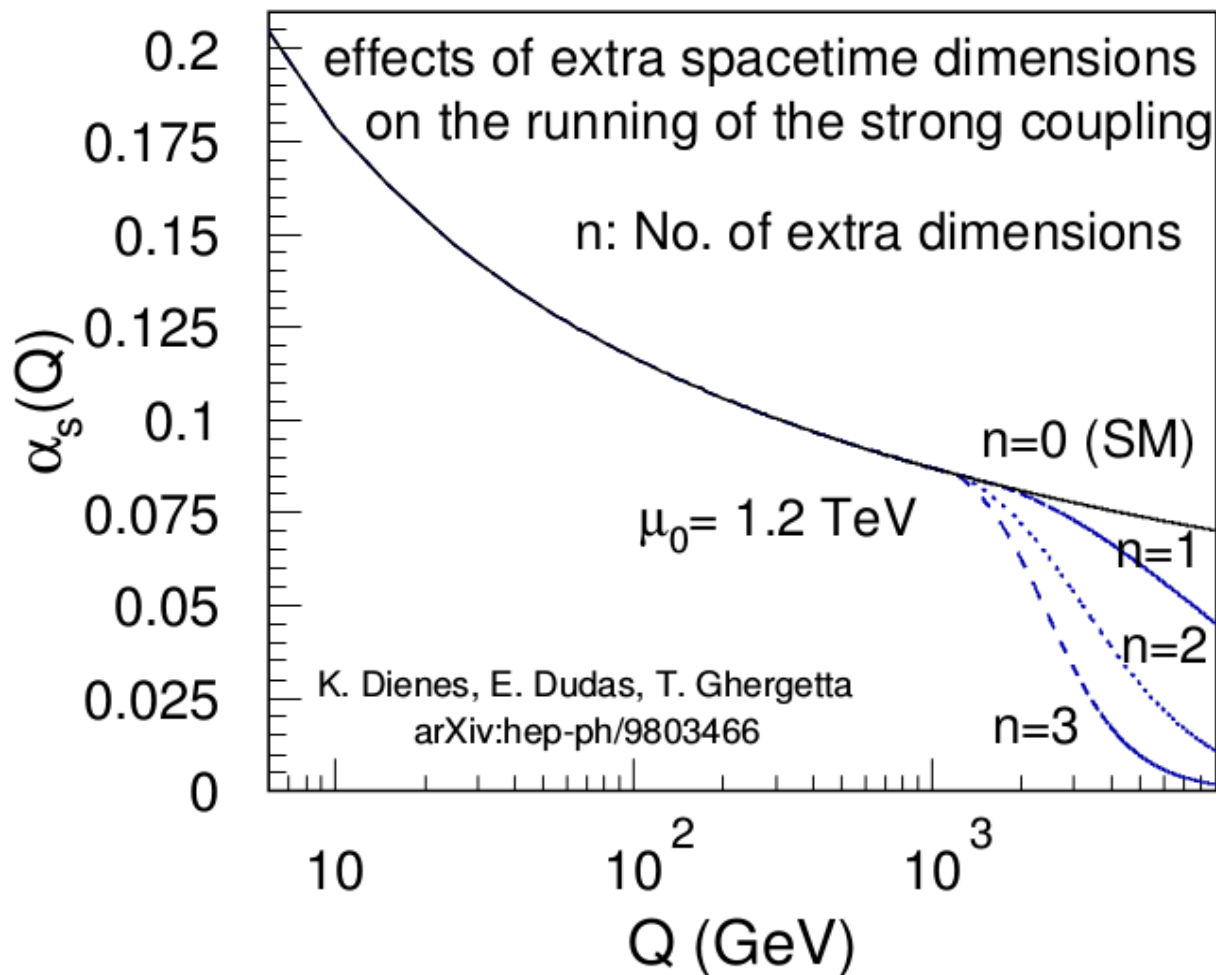
QCD tests  $\rightarrow$  2 aspects:

- Determine the value of  $\alpha_s \rightarrow \alpha_s(M_Z)$
- test the predictions for its running

# Why we care



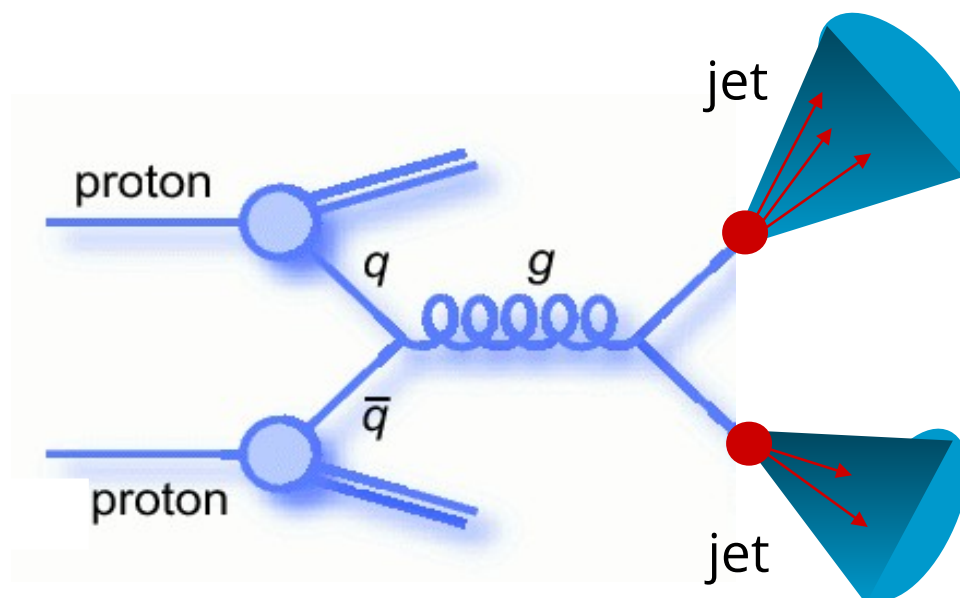
RGE of pQCD may not tell the full story



RGE may be modified  
by New Physics

e.g. effects from extra  
spacetime dimensions:  
→ Modified running of  
 $\alpha_s(Q)$  at high  $Q$

# Jet production at a hadron collider

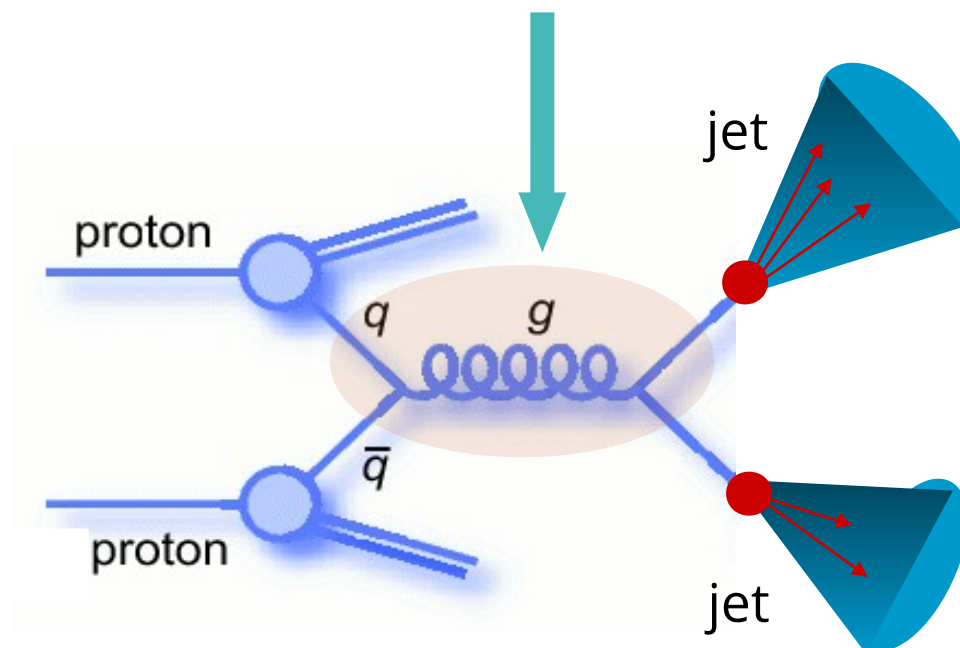


# Jet production at a hadron collider



## Matrix Elements

Standard Model or New Physics?



# Jet production at a hadron collider

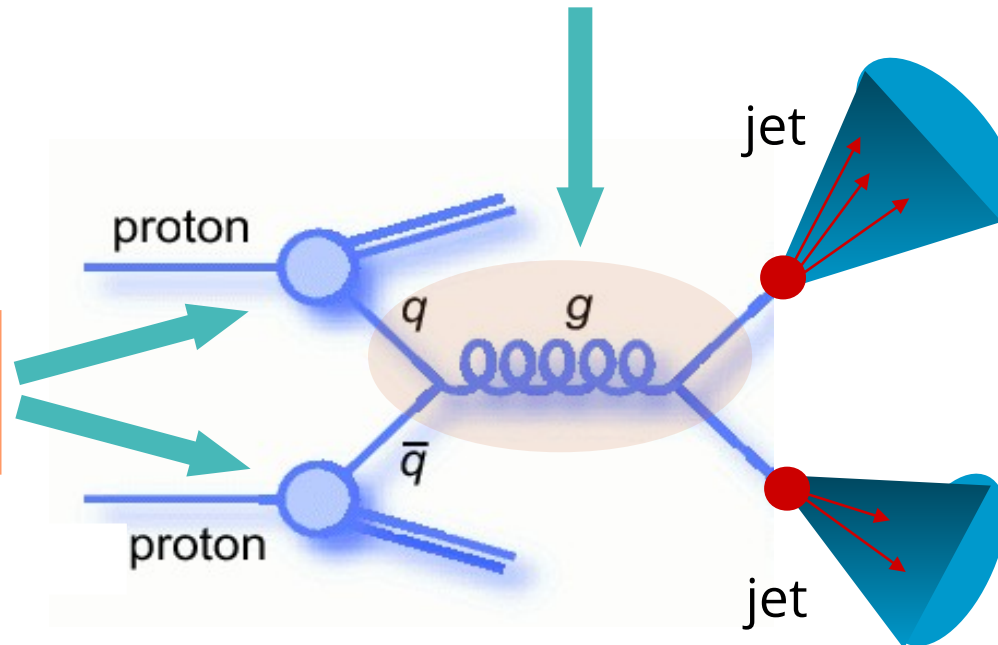


## Matrix Elements

Standard Model or New Physics?

## Parton distribution functions

Values? Evolution?  
Universality?



# Jet production at a hadron collider

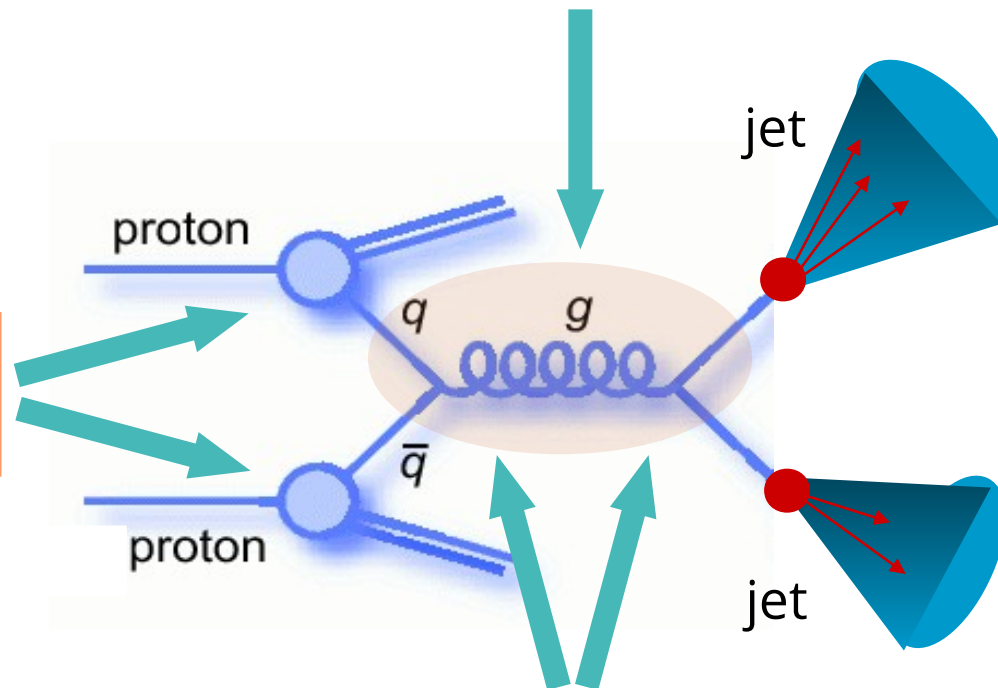


## Matrix Elements

Standard Model or New Physics?

## Parton distribution functions

Values? Evolution?  
Universality?



## Strong coupling $\alpha_s$

Value? Evolution? Universality?



# Ratios of Multi-Jet Cross Sections



3-jet / 2-jet ratios

$$R = \frac{\text{3-jet process diagram}}{\text{2-jet process diagram}} \longleftrightarrow \alpha_s$$

The diagram shows two Feynman-like diagrams representing particle interactions. The top diagram shows a proton and an antiproton interacting via a quark-antiquark pair ( $q\bar{q}$ ) and a gluon ( $g$ ), resulting in three jets. The bottom diagram shows a proton and an antiproton interacting via a quark-antiquark pair ( $q\bar{q}$ ) and a gluon ( $g$ ), resulting in two jets. A large blue 'R' is on the left, followed by an equals sign, then the fraction of diagrams, then a double-headed arrow, and finally the strong coupling constant  $\alpha_s$ .

- sensitive to  $\alpha_s$  (3-jets:  $\alpha_s^3$  | 2-jets:  $\alpha_s^2$ )
- less sensitive to PDFs & exp. uncertainties (cancellations)

# Transverse Energy-Energy Correlations



ATLAS Collab. Eur.Phys.J. C77 (2017) 12, 872

Transverse energy-energy correlations (TEEC)  
Associated asymmetry (ATEEC)

Energy-Energy Correlations = Energy-weighted angular correlations

Event shape  $\rightarrow$  independent of thrust axis or sphericity tensor

Transverse version  $\rightarrow$  use at hadron colliders

Calculated to NLO pQCD

TEEC:

$$\frac{1}{\sigma} \frac{d\Sigma}{d(\cos \phi)} = \frac{1}{\sigma} \sum_{ij} \int \frac{d\sigma}{dx_{Ti} dx_{Tj} d(\cos \phi)} x_{Ti} x_{Tj} dx_{Ti} dx_{Tj} \equiv \frac{1}{N \Delta \cos \phi} \sum_{A=1}^N \sum_{ij} \frac{E_{Ti}^A E_{Tj}^A}{\left(\sum_k E_{Tk}^A\right)^2} \delta(\cos \phi - \cos \phi_{ij})$$

Sum: over all pairs of jets  $i, j$

$\Phi_{ij}$  : azimuthal angle between  $i, j$

$$x_{Ti} = E_{Ti}/E_T \quad E_T = \sum_i E_{Ti}$$

ATEEC:

$$\frac{1}{\sigma'} \frac{d\Sigma'^{\text{asym}}}{d\phi} \equiv \frac{1}{\sigma'} \frac{d\Sigma'}{d\phi} \Big|_{\phi} - \frac{1}{\sigma'} \frac{d\Sigma'}{d\phi} \Big|_{\pi-\phi}$$

# TEEC / ATEEC Measurement



## Data set

ATLAS data at  $\sqrt{s} = 8 \text{ TeV}$  with  $L = 20.2 \text{ fb}^{-1}$   
Single-jet trigger  $E_T > 360 \text{ GeV}$

## Phase space

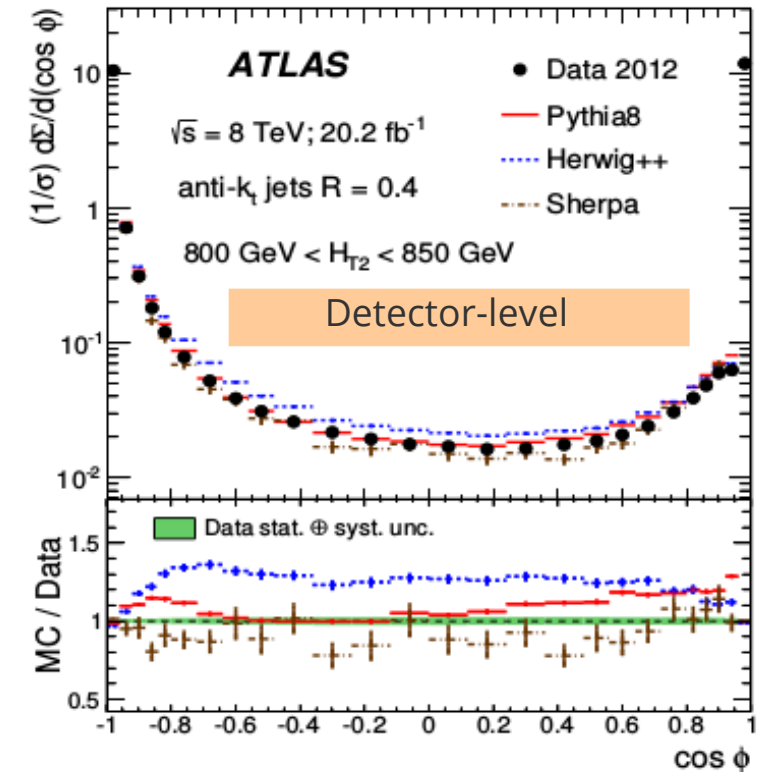
Jets with  $p_T > 100 \text{ GeV}$ ,  $|\eta| < 2.5$

$H_{T2} = (p_{T1} + p_{T2}) > 800 \text{ GeV}$

## Measurement

Normalized distribution in  $\cos(\phi)$  and  $H_{T2}$

Distributions unfolded to particle level



## Event weights

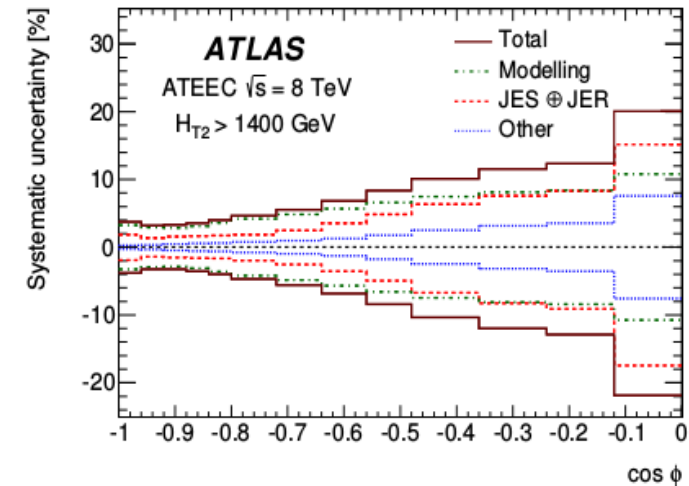
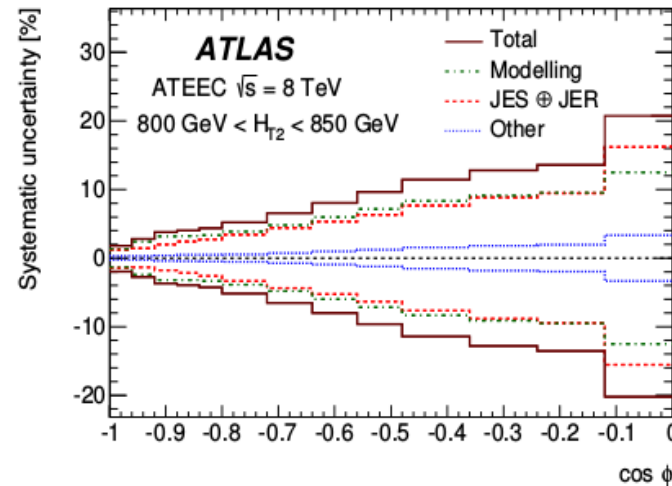
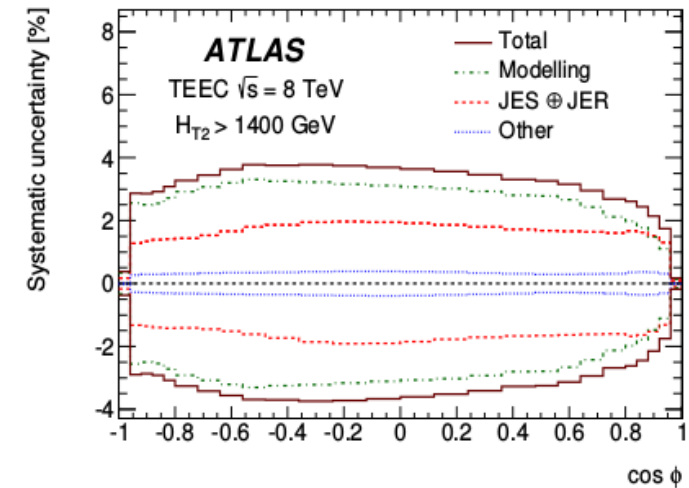
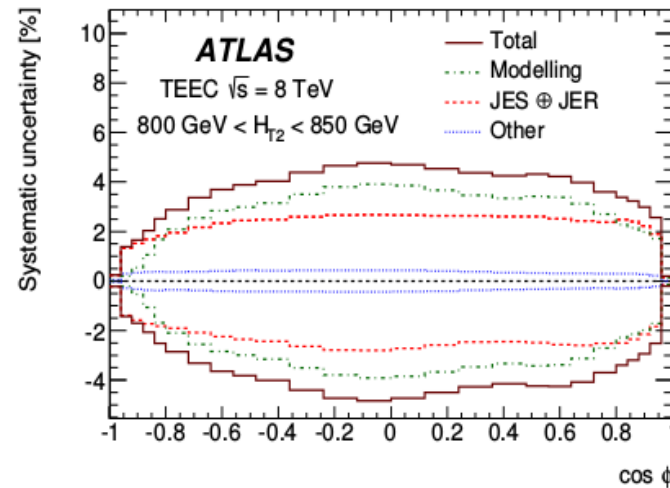
$$w_{ij} = x_{Ti} x_{Tj} = \frac{E_{Ti} E_{Tj}}{(\sum_k E_{Tk})^2}$$

# TEEC / ATEEC Syst. Uncertainties



TEEC (top)  
ATEEC (bottom)

Lowest  $H_{T2}$  (L)  
Highest  $H_{T2}$  (R)



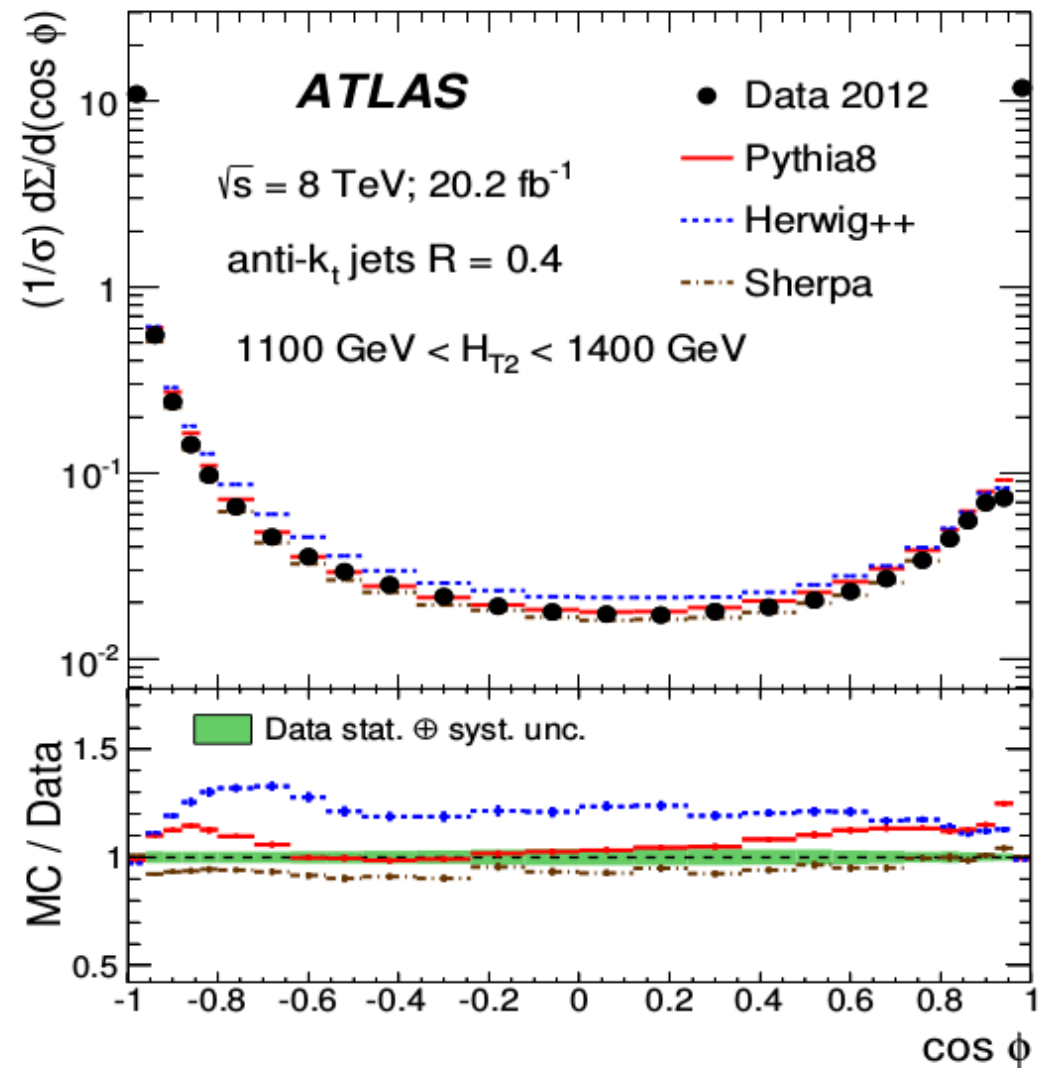
Systematic uncertainties for TEEC are always below 5%  
→ Jet energy calibration uncertainties cancel partially in ratio

# Measurement Results TEEC



Data vs. Monte Carlo

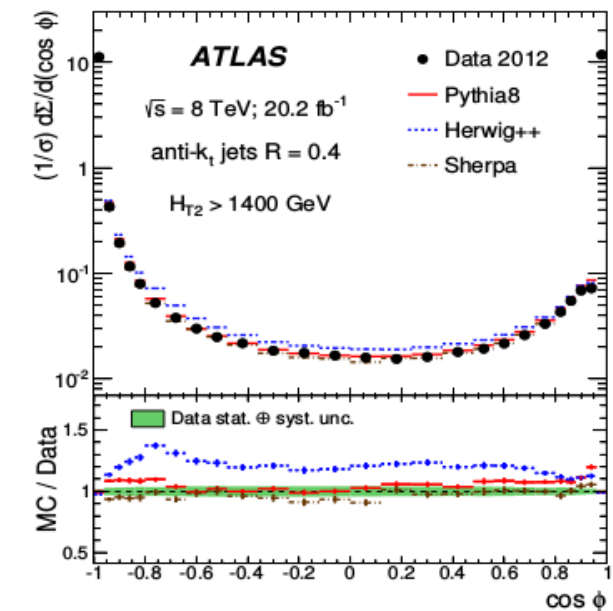
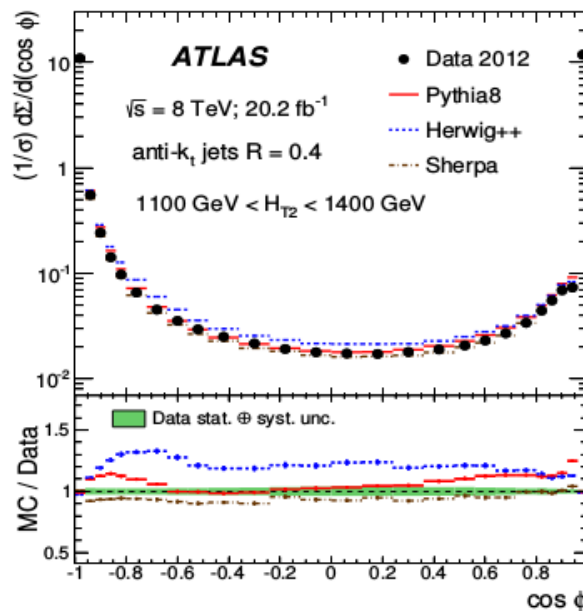
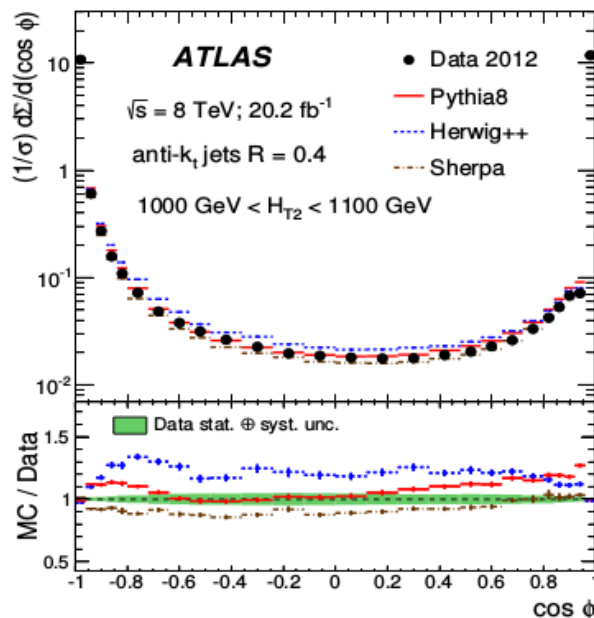
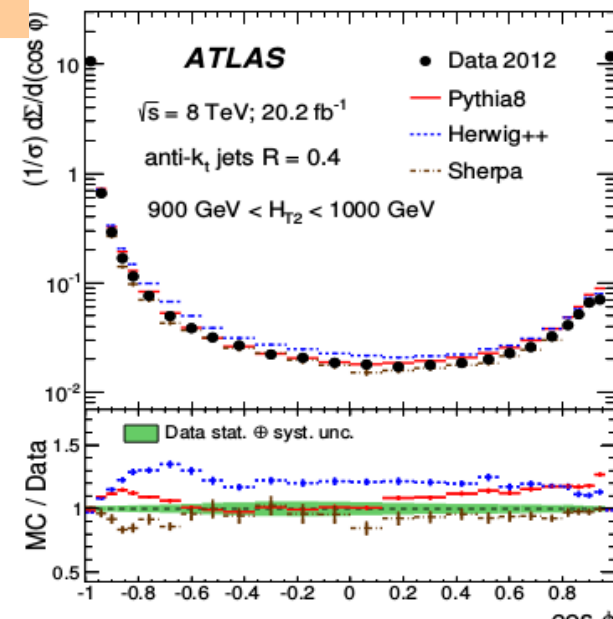
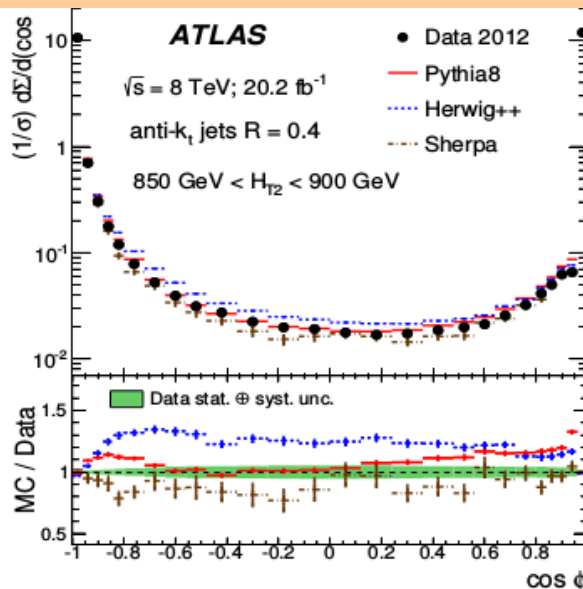
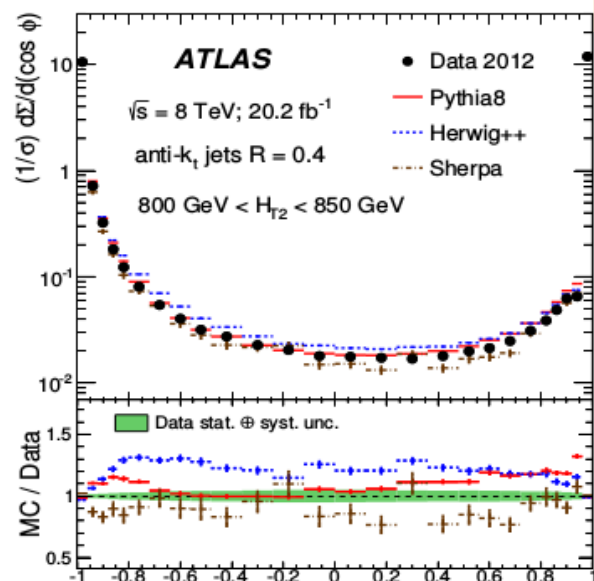
Well described by PYTHIA8



# Measurement Results TEEC



## Data vs. Monte Carlo

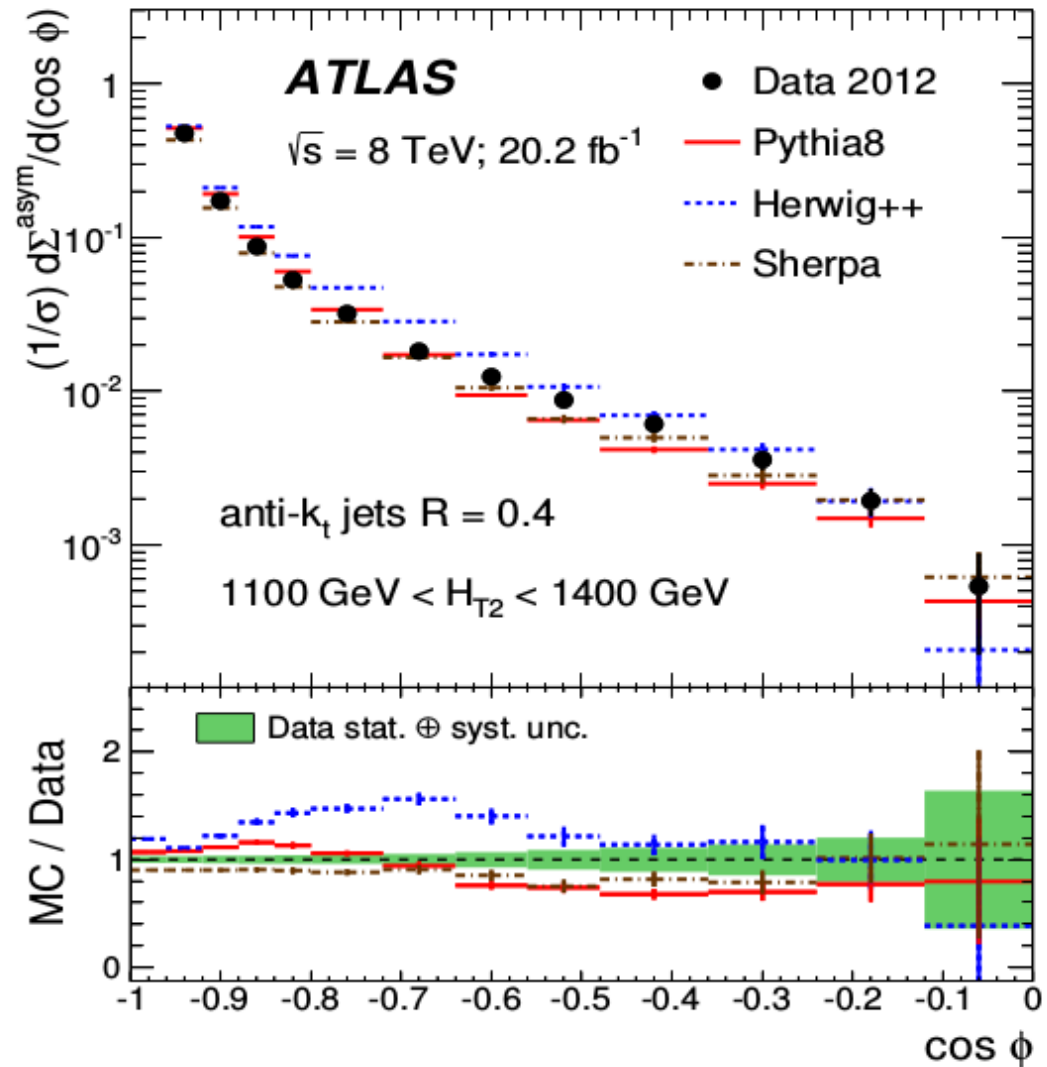


# Measurement Results ATEEC



Data vs. Monte Carlo

Well described by PYTHIA8

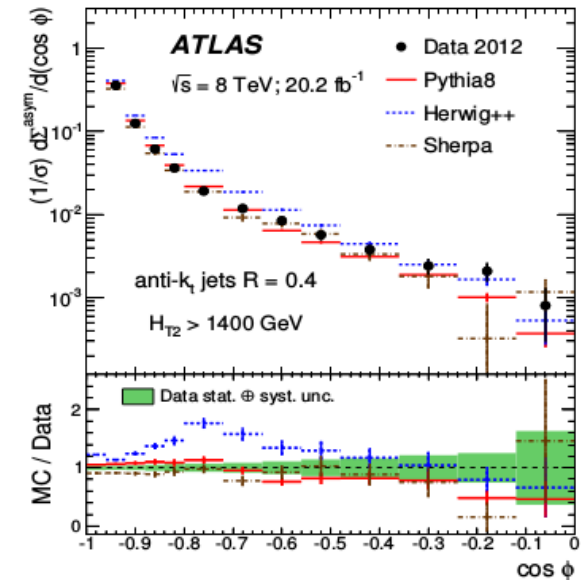
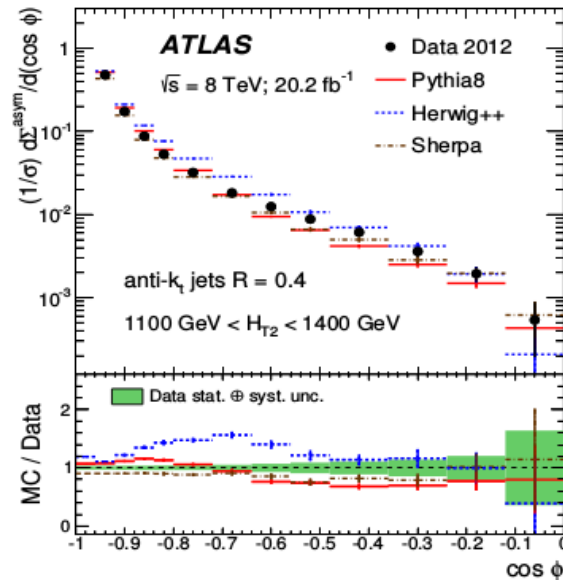
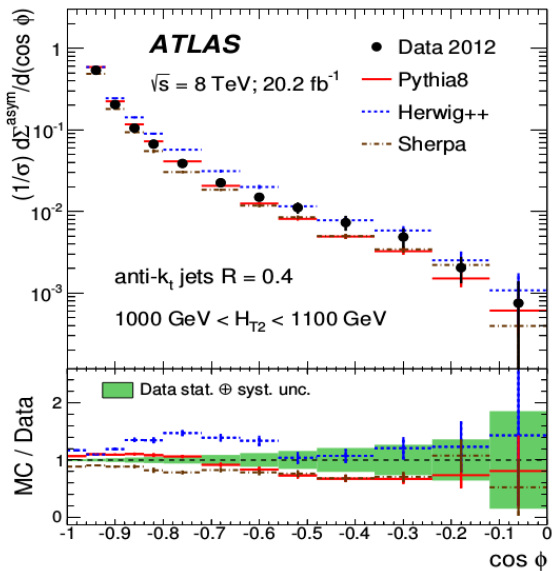
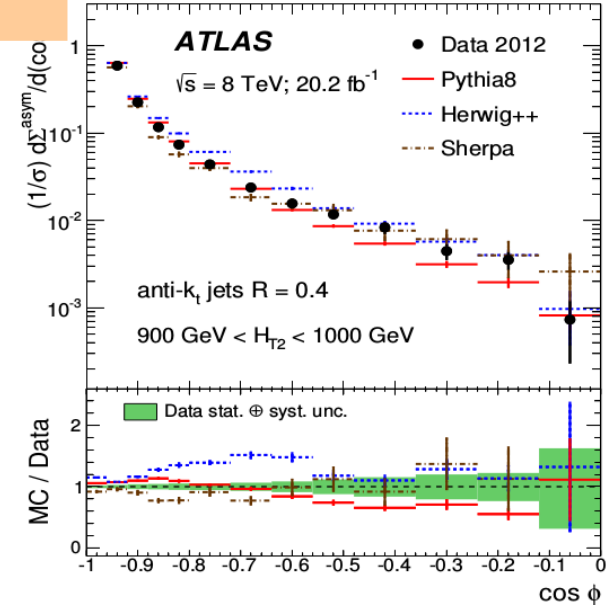
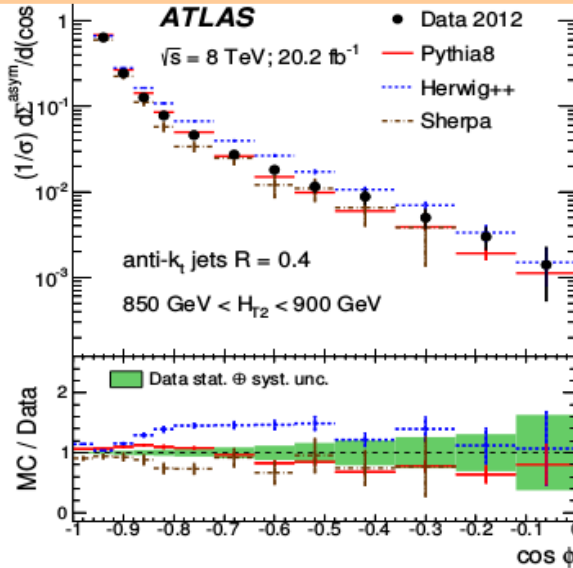
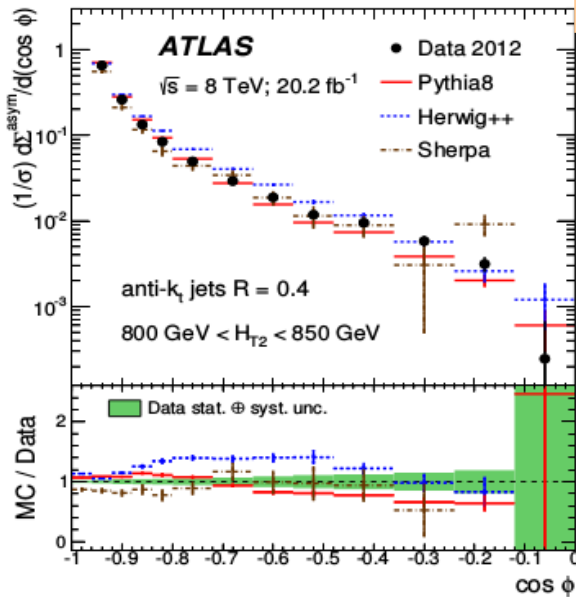




# Measurement Results ATEEC



## Data vs. Monte Carlo





# Theory Predictions



## NLO pQCD

NLOjet++ (massless quarks,  $n_f = 5$ )

renormalization scale:  $H_{T2} / 2$  factorization scale:  $H_{T2} / 4$

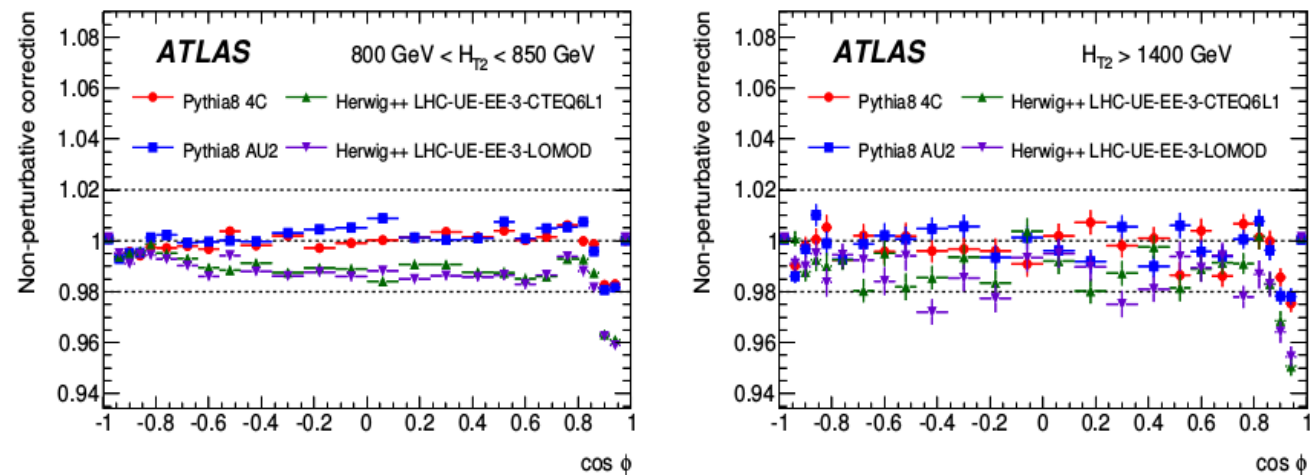
PDFs: MMHT2014, CT14, NNPDF3.0, HERAPDF2.0

## Non-perturbative corrections

PYTHIA8 tunes: **AU2** (nominal), 4C

HERWIG++ tunes: LHC-UE-EE-3-CTEQ6L1, LHC-UE-EE-3-LOMOD

Non-pert corrections  
for TEEC  $< 2\%$



# Data / pQCD Theory Comparison




TEEC


**ATLAS**

$\sqrt{s} = 8 \text{ TeV}; 20.2 \text{ fb}^{-1}$

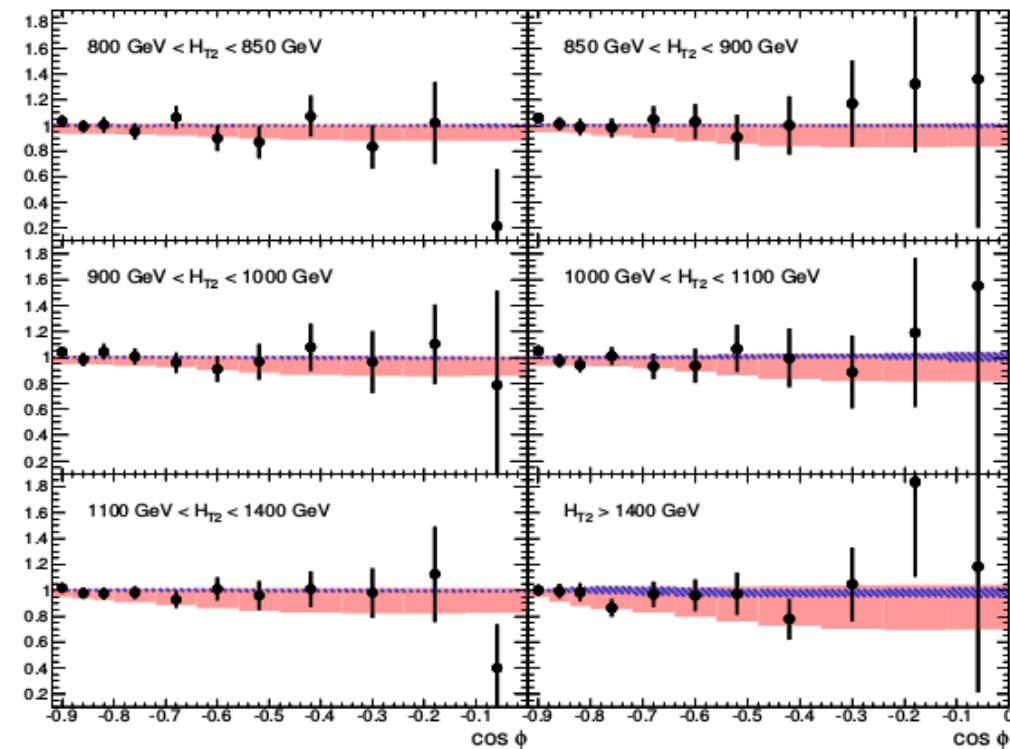
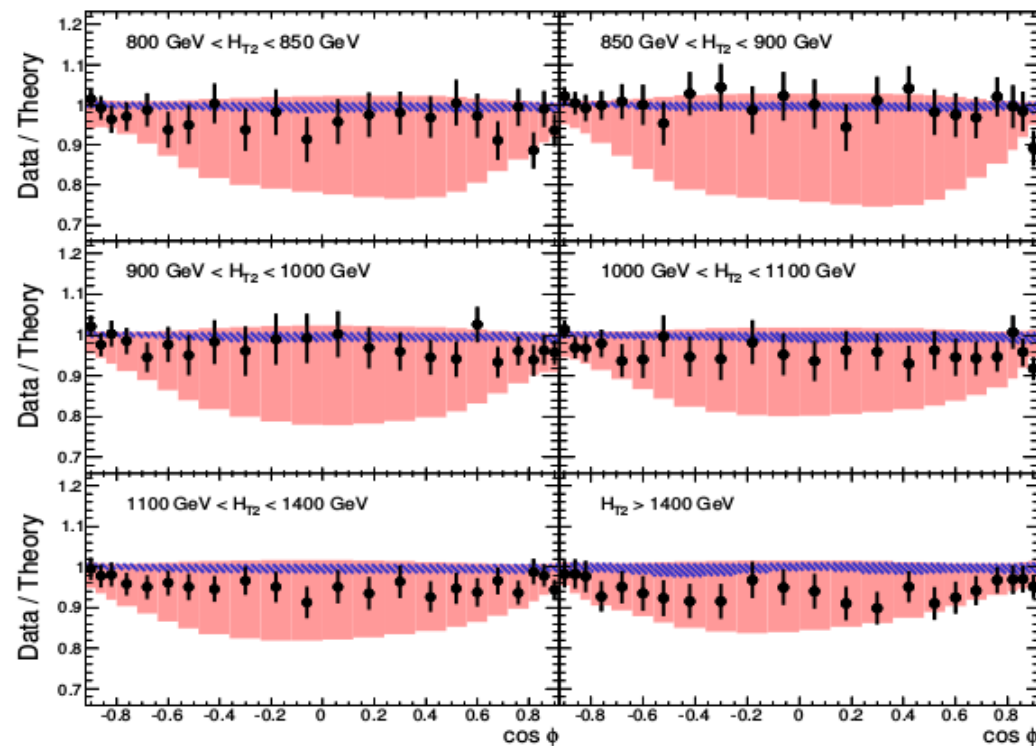
NNPDF 3.0 (NNLO)

— Exp. uncertainty

 Non-scale unc.

 Theo. uncertainty

ATEEC



Good agreement within theoretical uncertainty from scale dependence  
→ <10% for  $|\cos \phi| > 0.7$       → up to 20% for  $|\cos \phi| < 0.3$

# Determination of $\alpha_s$



Minimize  $\chi^2$  function

$$\chi^2(\alpha_s, \vec{\lambda}) = \sum_{\text{bins}} \frac{(x_i - F_i(\alpha_s, \vec{\lambda}))^2}{\Delta x_i^2 + \Delta \xi_i^2} + \sum_k \lambda_k^2,$$

Hessian approach

$$F_i(\alpha_s, \vec{\lambda}) = \psi_i(\alpha_s) \left( 1 + \sum_k \lambda_k \sigma_k^{(i)} \right)$$

Combine data within each HT2 range  $\rightarrow$  6 sets  $\rightarrow$  6  $\alpha_s$  results

TEEC

$\langle Q \rangle$ (GeV)	$\alpha_s(Q^2)$ value (NNPDF 3.0)
412	$0.0966 \pm 0.0014$ (exp.) $^{+0.0054}_{-0.0015}$ (scale) $\pm 0.0009$ (PDF) $\pm 0.0001$ (NP)
437	$0.0964 \pm 0.0012$ (exp.) $^{+0.0048}_{-0.0011}$ (scale) $\pm 0.0009$ (PDF) $\pm 0.0002$ (NP)
472	$0.0955 \pm 0.0011$ (exp.) $^{+0.0051}_{-0.0015}$ (scale) $\pm 0.0009$ (PDF) $\pm 0.0001$ (NP)
522	$0.0936 \pm 0.0011$ (exp.) $^{+0.0043}_{-0.0010}$ (scale) $\pm 0.0010$ (PDF) $\pm 0.0001$ (NP)
604	$0.0933 \pm 0.0011$ (exp.) $^{+0.0050}_{-0.0014}$ (scale) $\pm 0.0011$ (PDF) $\pm 0.0003$ (NP)
810	$0.0907 \pm 0.0013$ (exp.) $^{+0.0049}_{-0.0020}$ (scale) $\pm 0.0011$ (PDF) $\pm 0.0002$ (NP)

$\langle Q \rangle$ (GeV)	$\alpha_s(m_Z)$ value (NNPDF 3.0)	$\chi^2/N_{\text{dof}}$
412	$0.1171 \pm 0.0021$ (exp.) $^{+0.0081}_{-0.0022}$ (scale) $\pm 0.0013$ (PDF) $\pm 0.0001$ (NP)	24.3 / 21
437	$0.1178 \pm 0.0017$ (exp.) $^{+0.0073}_{-0.0017}$ (scale) $\pm 0.0014$ (PDF) $\pm 0.0002$ (NP)	28.3 / 21
472	$0.1177 \pm 0.0017$ (exp.) $^{+0.0079}_{-0.0023}$ (scale) $\pm 0.0015$ (PDF) $\pm 0.0001$ (NP)	27.7 / 21
522	$0.1163 \pm 0.0017$ (exp.) $^{+0.0067}_{-0.0016}$ (scale) $\pm 0.0016$ (PDF) $\pm 0.0001$ (NP)	22.8 / 21
604	$0.1181 \pm 0.0017$ (exp.) $^{+0.0082}_{-0.0022}$ (scale) $\pm 0.0017$ (PDF) $\pm 0.0005$ (NP)	24.3 / 21
810	$0.1186 \pm 0.0023$ (exp.) $^{+0.0085}_{-0.0035}$ (scale) $\pm 0.0020$ (PDF) $\pm 0.0004$ (NP)	23.7 / 21

ATEEC

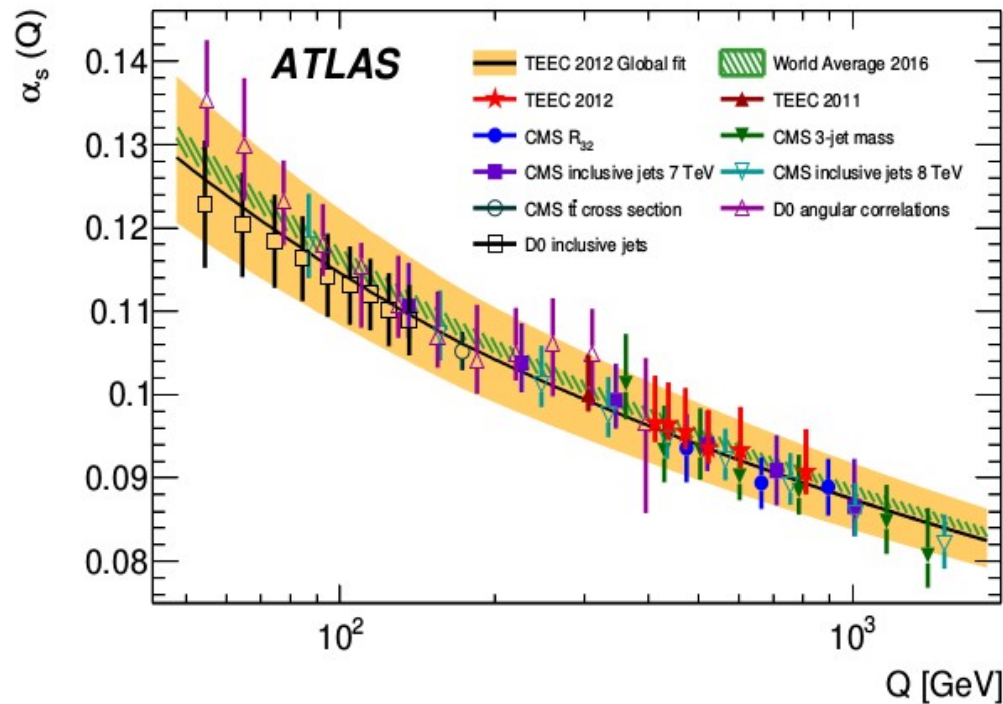
$\langle Q \rangle$ (GeV)	$\alpha_s(Q^2)$ value (NNPDF 3.0)
412	$0.0992 \pm 0.0024$ (exp.) $^{+0.0056}_{-0.0020}$ (scale) $\pm 0.0009$ (PDF) $\pm 0.0002$ (NP)
437	$0.0986 \pm 0.0017$ (exp.) $^{+0.0041}_{-0.0009}$ (scale) $\pm 0.0010$ (PDF) $\pm 0.0007$ (NP)
472	$0.0973 \pm 0.0018$ (exp.) $^{+0.0038}_{-0.0008}$ (scale) $\pm 0.0010$ (PDF) $\pm 0.0001$ (NP)
522	$0.0957 \pm 0.0016$ (exp.) $^{+0.0034}_{-0.0006}$ (scale) $\pm 0.0011$ (PDF) $\pm 0.0003$ (NP)
604	$0.0930 \pm 0.0019$ (exp.) $^{+0.0035}_{-0.0005}$ (scale) $\pm 0.0012$ (PDF) $\pm 0.0003$ (NP)
810	$0.0899 \pm 0.0021$ (exp.) $^{+0.0031}_{-0.0005}$ (scale) $\pm 0.0013$ (PDF) $\pm 0.0001$ (NP)

$\langle Q \rangle$ (GeV)	$\alpha_s(m_Z)$ value (NNPDF 3.0)	$\chi^2/N_{\text{dof}}$
412	$0.1209 \pm 0.0036$ (exp.) $^{+0.0085}_{-0.0031}$ (scale) $\pm 0.0013$ (PDF) $\pm 0.0004$ (NP)	10.6 / 10
437	$0.1211 \pm 0.0026$ (exp.) $^{+0.0064}_{-0.0014}$ (scale) $\pm 0.0015$ (PDF) $\pm 0.0010$ (NP)	6.8 / 10
472	$0.1203 \pm 0.0028$ (exp.) $^{+0.0054}_{-0.0013}$ (scale) $\pm 0.0016$ (PDF) $\pm 0.0002$ (NP)	8.8 / 10
522	$0.1196 \pm 0.0025$ (exp.) $^{+0.0054}_{-0.0010}$ (scale) $\pm 0.0017$ (PDF) $\pm 0.0004$ (NP)	10.9 / 10
604	$0.1176 \pm 0.0031$ (exp.) $^{+0.0058}_{-0.0008}$ (scale) $\pm 0.0020$ (PDF) $\pm 0.0005$ (NP)	6.4 / 10
810	$0.1172 \pm 0.0037$ (exp.) $^{+0.0053}_{-0.0009}$ (scale) $\pm 0.0022$ (PDF) $\pm 0.0001$ (NP)	9.8 / 10

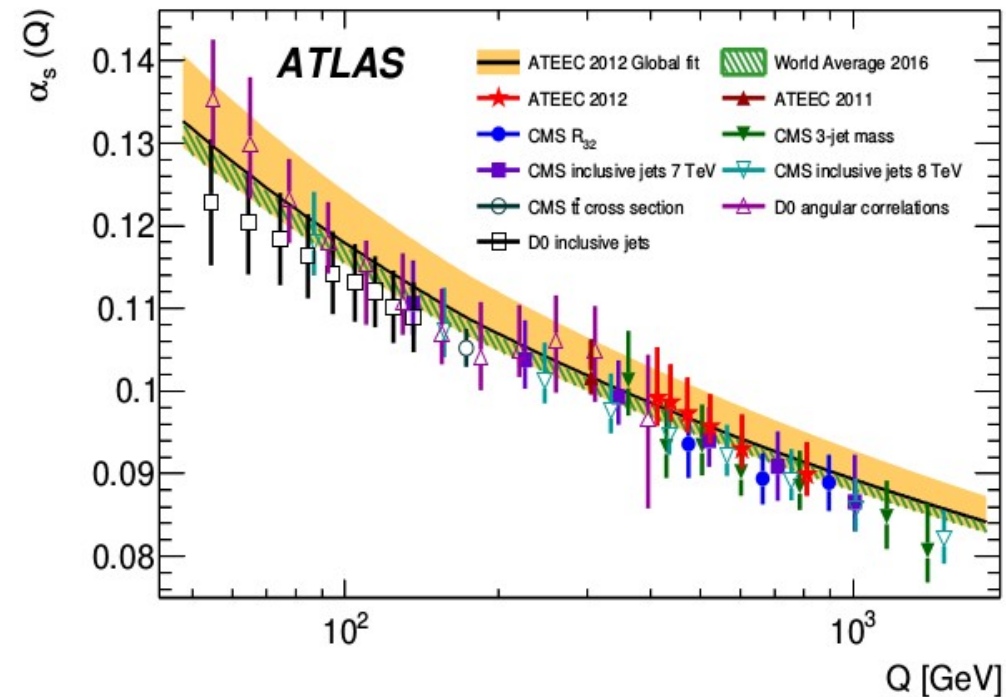
# Determination of $\alpha_s(Q)$



TEEC



ATEEC



Consistency with RGE predictions  
& with results from other experiments

# Determination of $\alpha_s(m_Z)$



## TEEC

PDF	$\alpha_s(m_Z)$ value	$\chi^2/N_{\text{dof}}$
MMHT 2014	$0.1151 \pm 0.0008$ (exp.) $^{+0.0064}_{-0.0047}$ (scale) $\pm 0.0012$ (PDF) $\pm 0.0002$ (NP)	173 / 131
CT14	$0.1165 \pm 0.0010$ (exp.) $^{+0.0067}_{-0.0061}$ (scale) $\pm 0.0016$ (PDF) $\pm 0.0003$ (NP)	161 / 131
NNPDF 3.0	$0.1162 \pm 0.0011$ (exp.) $^{+0.0076}_{-0.0061}$ (scale) $\pm 0.0018$ (PDF) $\pm 0.0003$ (NP)	174 / 131
HERAPDF 2.0	$0.1177 \pm 0.0008$ (exp.) $^{+0.0064}_{-0.0040}$ (scale) $\pm 0.0005$ (PDF) $\pm 0.0002$ (NP) $^{+0.0008}_{-0.0007}$ (mod)	169 / 131

$$\alpha_s(m_Z) = 0.1162 \pm 0.0011 \text{ (exp.) } ^{+0.0076}_{-0.0061} \text{ (scale)} \pm 0.0018 \text{ (PDF)} \pm 0.0003 \text{ (NP)}.$$

PDF	$\alpha_s(m_Z)$ value	$\chi^2/N_{\text{dof}}$
MMHT 2014	$0.1185 \pm 0.0012$ (exp.) $^{+0.0047}_{-0.0010}$ (scale) $\pm 0.0010$ (PDF) $\pm 0.0004$ (NP)	57.0 / 65
CT14	$0.1203 \pm 0.0013$ (exp.) $^{+0.0053}_{-0.0014}$ (scale) $\pm 0.0015$ (PDF) $\pm 0.0004$ (NP)	55.4 / 65
NNPDF 3.0	$0.1196 \pm 0.0013$ (exp.) $^{+0.0061}_{-0.0013}$ (scale) $\pm 0.0017$ (PDF) $\pm 0.0004$ (NP)	60.3 / 65
HERAPDF 2.0	$0.1206 \pm 0.0012$ (exp.) $^{+0.0050}_{-0.0014}$ (scale) $\pm 0.0005$ (PDF) $\pm 0.0002$ (NP) $\pm 0.0007$ (mod)	54.2 / 65

## ATEEC

$$\alpha_s(m_Z) = 0.1196 \pm 0.0013 \text{ (exp.) } ^{+0.0061}_{-0.0013} \text{ (scale)} \pm 0.0017 \text{ (PDF)} \pm 0.0004 \text{ (NP)}$$

Consistent with each other & with world average (0.1181  $\pm$  0.0011)



## Measurement of transverse energy-energy correlations & asymmetry

- 2012 ATLAS data,  $\sqrt{s} = 8 \text{ TeV}$ ,  $L = 20.2 \text{ fb}^{-1}$
- Small experimental uncertainties for TEEC
- Reasonably well described by different MCs & NLO pQCD + non-pert.
- Determinations of  $\alpha_s(Q)$  and  $\alpha_s(m_Z)$
- Fits, combining all different  $H_{T2}$  regions:  
$$\alpha_s(m_Z) = 0.1162 \pm 0.0011 \text{ (exp.) } {}^{+0.0076}_{-0.0061} \text{ (scale)} \pm 0.0018 \text{ (PDF)} \pm 0.0003 \text{ (NP)},$$
$$\alpha_s(m_Z) = 0.1196 \pm 0.0013 \text{ (exp.) } {}^{+0.0061}_{-0.0013} \text{ (scale)} \pm 0.0017 \text{ (PDF)} \pm 0.0004 \text{ (NP)},$$

Good agreement with previous results, world average and RGE predictions