

# Impact of low-x resummation on QCD analysis of HERA data



S. Glazov (DESY), DIS-2018, Kobe 19/04/2018

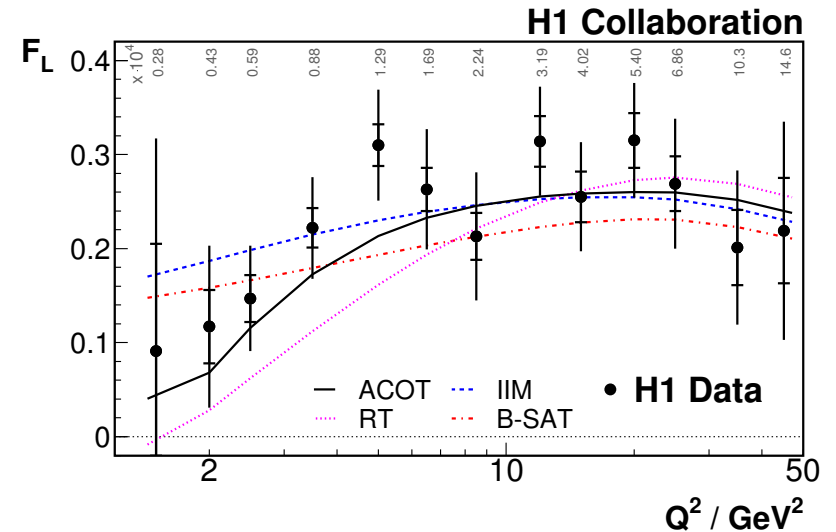
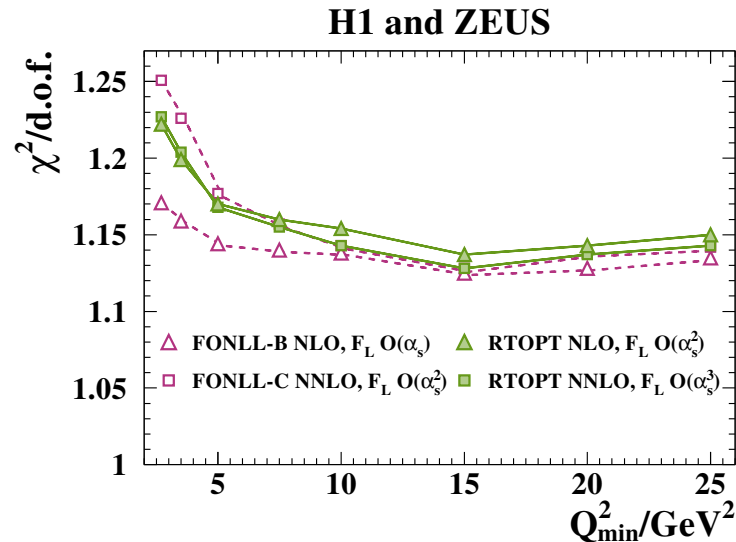
## xFitter project

- **xFitter** is an open source QCD analysis tool.
- Last release, **2.0.0 “Frozen Frog”**, used in many analyses by experimental and phenomenological groups.
- **xFitter** provides interface to many data samples, with complex correlation model, fast  $\chi^2$  computation, fast evolution using QCDNUM, build-in computation of DIS cross sections and interfaces to APPLGRID and FastNLO, and other features such as different PDF parameterisations and regularisation methods.
- **xFitter** has interfaces to a number of external packages, for this talk the most important are evolution package APFEL ([CPC 185, 1647 \(2014\)](#)) and  $\ln 1/x$  resummation package HELL ([EPJ C76\(11\), 597 \(2016\)](#), [JHEP 12, 117 \(2017\)](#).) which is interfaced via APFEL.

→ see talk of Fred Olness for more details on the **xFitter** project.

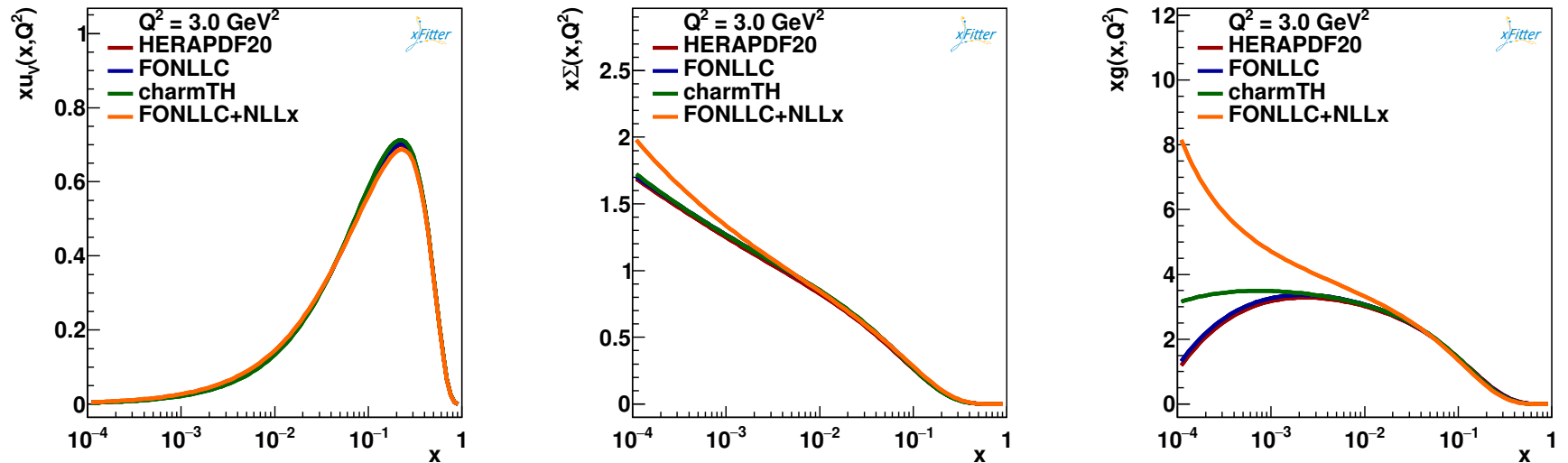
This talk is focused on the studies described in [1802.00064](#).

# Low $x$ analysis motivations



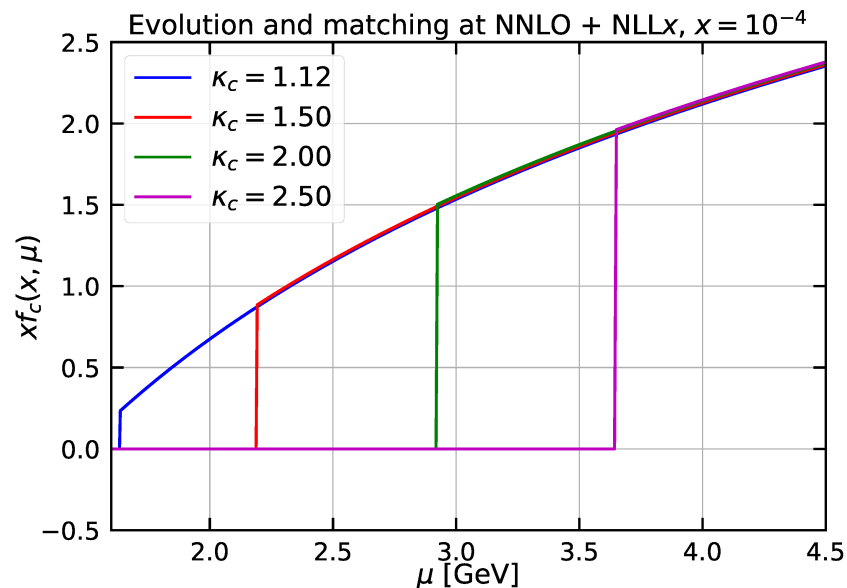
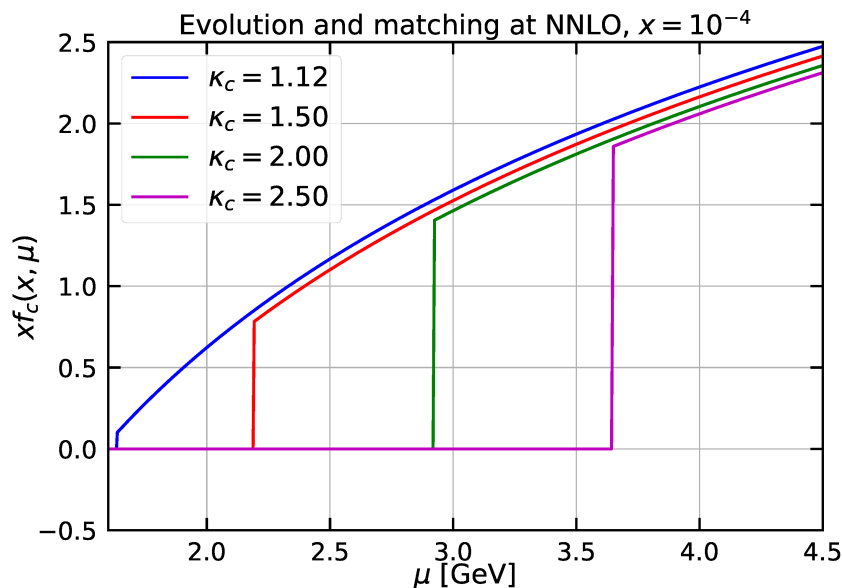
- Several indications that NNLO DGLAP fits have difficulty with to describe low  $Q^2$  HERA data, NLO being better vs NNLO, depending on order of  $F_L$  ([EPJC75 \(2015\) 12, 580](#)).
- Alternative models, such as dipole, provide good description of the data ([EPJC71\(2011\) 1579](#)).
- Recent study from NNPDF collaboration, showing that  $\ln 1/x$  resummation improves NNLO fits [arXiv:1710.05935](#).

# From HERAPDF-like NNLO to NNLO+NLLx



- Start with HERAPDF20-like settings, using RT scheme. Input data: HERA2.0 inclusive and combined charm.
- Move to FONLL-C: no change in PDFs.
- Raise the charm matching point from  $\mu_C = m_C = 1.43 \text{ GeV}$  to  $\mu_C = 1.12 m_C = 1.6 \text{ GeV}$  (needed for HELL). Notable change in the gluon distribution.
- Include  $\ln 1/x$  resummation: large change in the gluon,  $\chi^2$  drops by 73 units (for 1131 degrees of freedom).

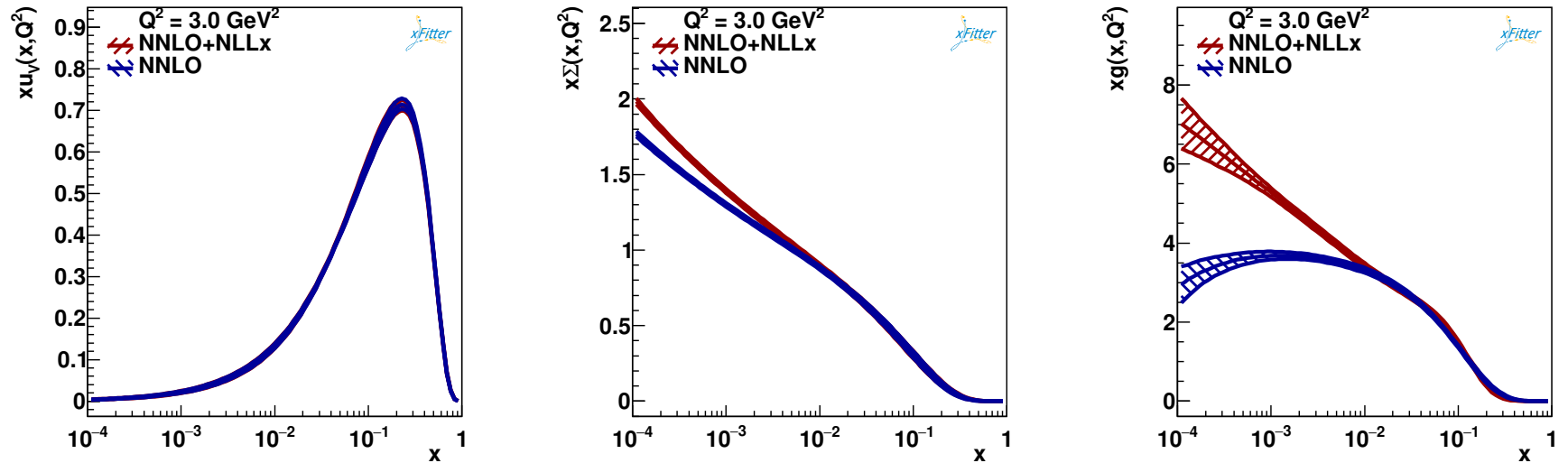
# Matching at NNLO vs NNLO+NLLx



- Vary charm matching point  $\mu_c$  between  $1.12m_c$  and  $2.5m_c$ , study low  $x = 10^{-4}$ .
- For NNLO, steps observed at the matching point; to compensate for smaller charm PDF the gluon distribution is increased.
- Much smoother behavior when  $\ln 1/x$  resummation is included.

(see also talk by Fred Olness on the heavy flavor matching point studies)

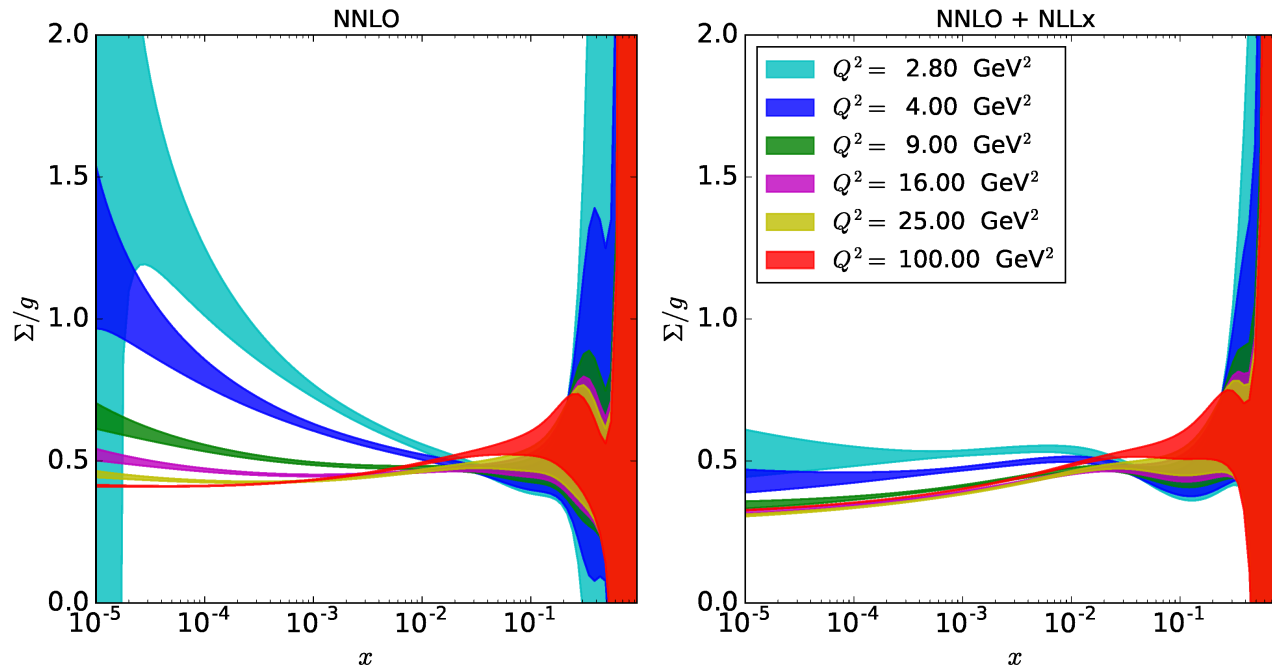
# PDFs at NNLO and NNLO+NLLx



- Optimize settings for the NNLO and NNLO+NLLx fits: charm/bottom-quark mass scan, parametersiation scan.
- Evaluate experimental uncertainties.
- Valence shape is unchanged by including  $\ln 1/x$  resummation, singlet is affected slightly while gluon is affected the most.

→ The rise of the gluon and the singlet towards low  $x$  seems to have the same power after resummation is included.

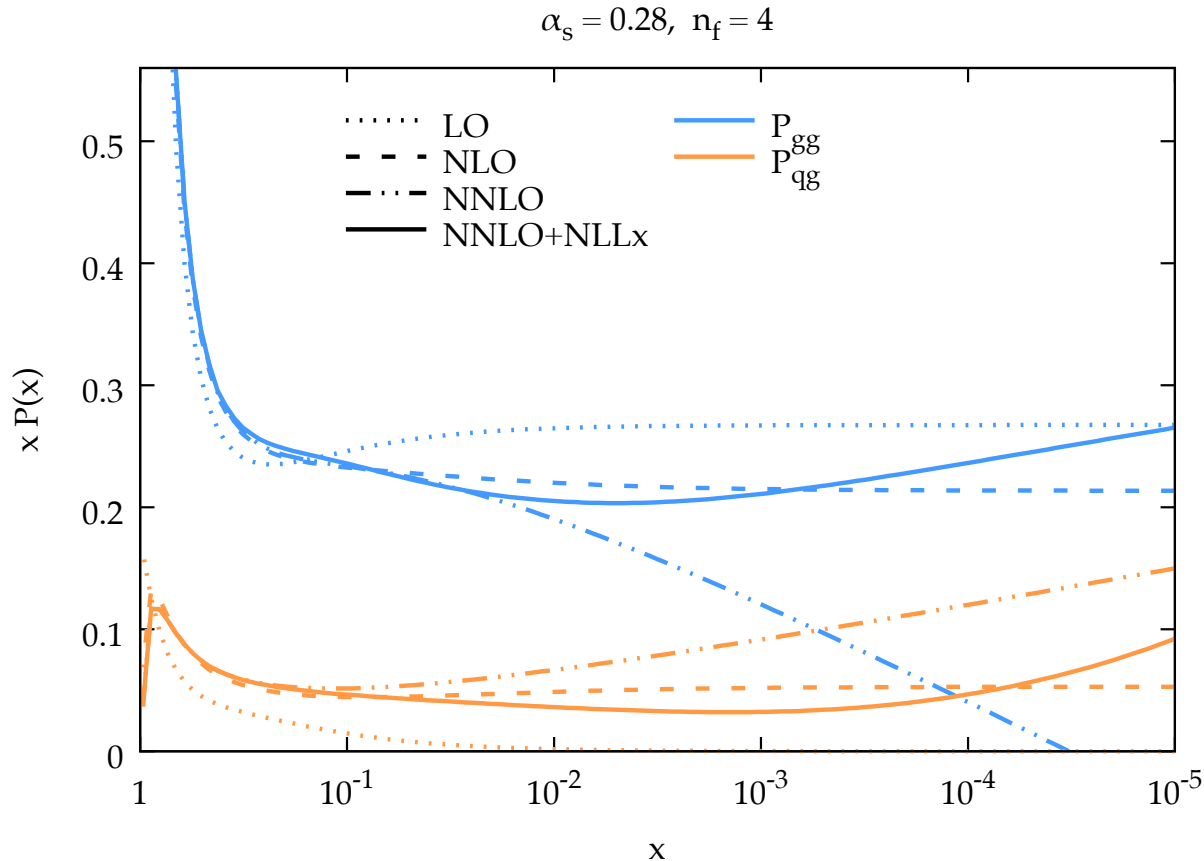
# Ratio $\Sigma/g$



- Quantify the power of the rise of  $xg$  and  $x\Sigma$  by examining evolution of their ratio.
- Large evolution at NNLO, with the ratio exceeding unity at low scales.
- Ratio is  $\leq 0.5$  when  $\ln 1/x$  resummation is included.

→ more inline with “dynamic” picture of PDFs in which the sea is generated from the gluon perturbatively like in GRV fits.

# Splitting functions $P_{qg}$ and $P_{gg}$



Splitting functions  $P_{gg}$  and  $P_{qg}$  show un-physical behavior at NNLO:  $P_{qg} > P_{gg}$  at  $x \sim 10^{-3}$  for  $Q \sim 2 \text{ GeV}$ . This leads to the fast rise of the singlet vs gluon at low scales. Resummed splitting functions show behavior inline with the expectations.



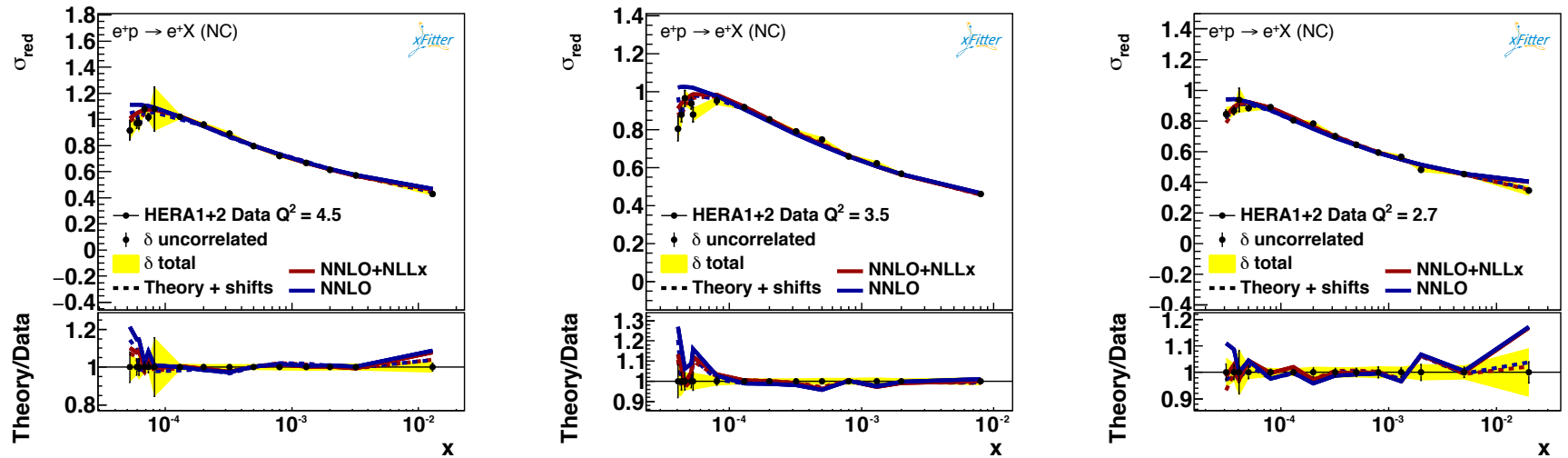
## Data vs theory

|   | NNLO fit  | NNLO+NLL <sub>x</sub> fit |
|---|-----------|---------------------------|
| Total $\chi^2/\text{d.o.f}$                 | 1446/1178 | 1373/1178                 |
| subset NC 920 $\tilde{\chi}^2/\text{n.d.p}$ | 446/377   | 413/377                   |
| subset NC 820 $\tilde{\chi}^2/\text{n.d.p}$ | 70/70     | 65/70                     |
| subset charm $\tilde{\chi}^2/\text{n.d.p}$  | 48/47     | 49/47                     |
| correlated shifts inclusive                 | 102       | 77                        |
| correlated shifts charm                     | 15        | 11                        |
| log term inclusive                          | 20        | -3                        |
| log term charm                              | -2        | -1                        |

$$\chi^2 = \sum_i \frac{[D_i - T_i(1 - \sum_j \gamma_j^i b_j)]^2}{\delta_{i,\text{unc}}^2 T_i^2 + \delta_{i,\text{stat}}^2 D_i T_i} + \sum_j b_j^2 + \sum_i \ln \frac{\delta_{i,\text{unc}}^2 T_i^2 + \delta_{i,\text{stat}}^2 D_i T_i}{\delta_{i,\text{unc}}^2 D_i^2 + \delta_{i,\text{stat}}^2 D_i^2},$$

→ largest improvements in the  $\chi^2$  are observed for the precise  $E_p = 920$  GeV set as well as for correlated systematic uncertainties and log-penalty term.

# Data vs Theory



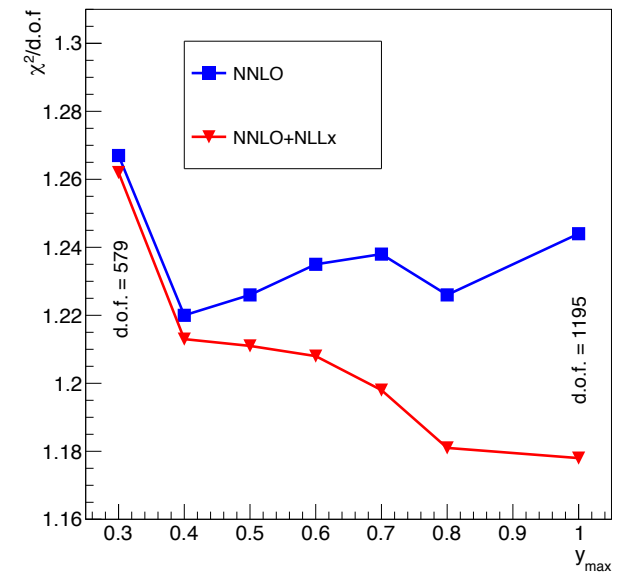
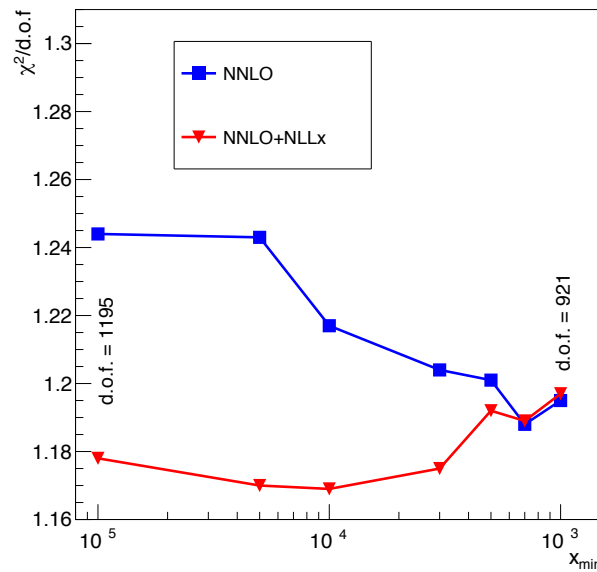
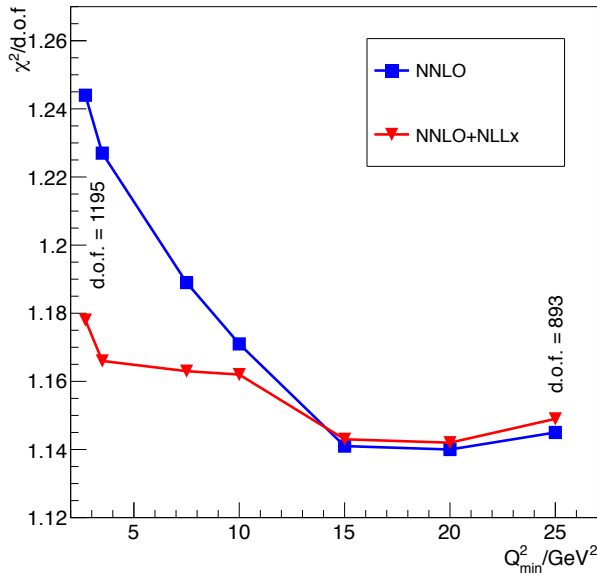
At low  $Q^2$ ,

$$\sigma_{\text{red}} = F_2 - \frac{y^2}{1 + (1 - y)^2} F_L.$$

where inelasticity  $y = \frac{Q^2}{sx}$ .

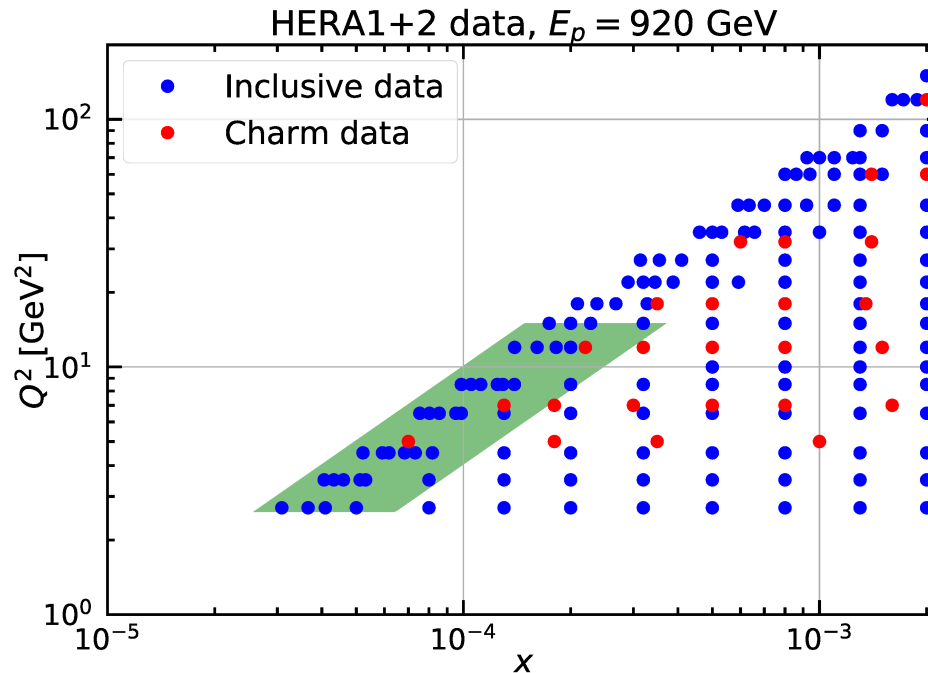
- Turn-over of the cross section at low  $x$  corresponds to large  $y$  and increased influence of  $F_L$ .
- The turn-over is better described when  $\ln 1/x$  resummation is included.
- Even  $Q^2 = 2.7 \text{ GeV}^2$  bin looks acceptable, however  $\chi^2$  for this bin remains poor for both fits.

# Isolating the impact of NLLx



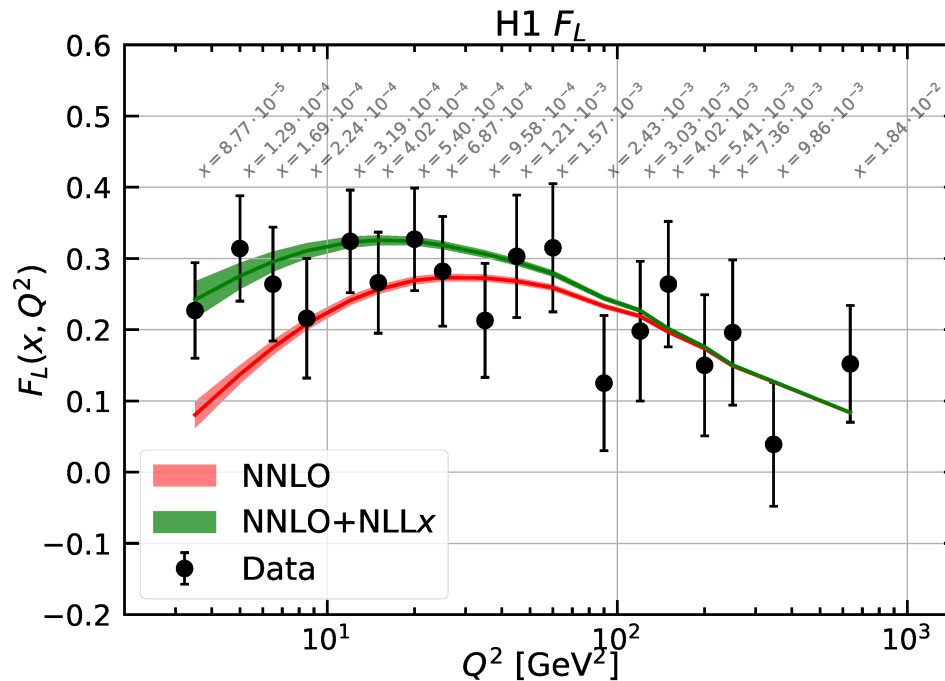
- Repeat fits with various kinematic cuts on the data.
- Include  $Q^2 = 2.7 \text{ GeV}^2$  bin in this study.
- Scan in  $Q_{\min}^2$ ,  $x_{\min}$  and additionally in  $y_{\max}$ .
- Improvements when  $\ln 1/x$  resummation is included for low  $Q^2$ , low  $x$  and high  $y$ .
- Quality of the description by both NNLO and NNLO+NLLx fits becomes similar when these regions are excluded.

# Region of maximal impact



- 1D scans define the regions where  $\ln 1/x$  resummation has largest impact:  $Q^2 < 15$  GeV,  $x < 5 \cdot 10^{-4}$ , and  $y > 0.4$  (assuming  $E_p = 920$  GeV).
- This defines the “green region” in  $x$ ,  $Q^2$  kinematic plane.
- When this region is excluded, the difference in  $\chi^2$  between NNLO and NNLO+NLLx fits is only 15 units compared to 73 units when it is included.

# The structure function $F_L$



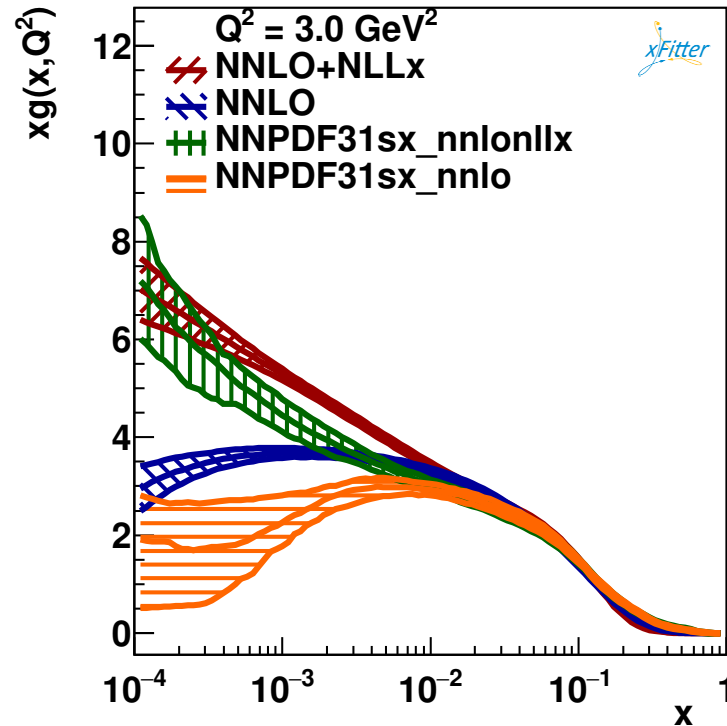
- The fit with  $\ln 1/x$  resummation included gives better description of the SF  $F_L$  measured by H1 (EPJ C74, (2014) 2814).
- However, given uncertainties, more important is the accurate measurement at high  $y$  using large  $E_p = 920 \text{ GeV}$  sample (“indirect  $F_L$ ”).

## Summary

- NNLO fits with and without  $\ln 1/x$  resummation are performed to the HERA data.
- Significant improvement in the  $\chi^2$  is observed when  $\ln 1/x$  resummation is included, concentrated in the region at low  $x$ , low  $Q^2$  and high  $y$  where the contribution of the structure function  $F_L$  is sizable.
- NNLO+NLLx fits have increased gluon distribution at low  $x$  and low  $Q^2$ . The rise of the singlet and gluon distribution towards low  $x$  becomes similar, in contrast to suppressed gluon for pure NNLO fits, suggesting more simple relation between them.



## Comparison to NNPDF3.1sx PDF sets



- Similar trend that NNLO+NLLx gluon is larger at low  $x$  vs NNLO.
- Many differences in the fits to compare them directly: fitted vs perturbative charm, charm threshold, methods for uncertainty estimate.