



# Top quark Physics at the Electron-Proton colliders

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26<sup>th</sup> International WS on Deep Inelastic Scattering & Related Topics

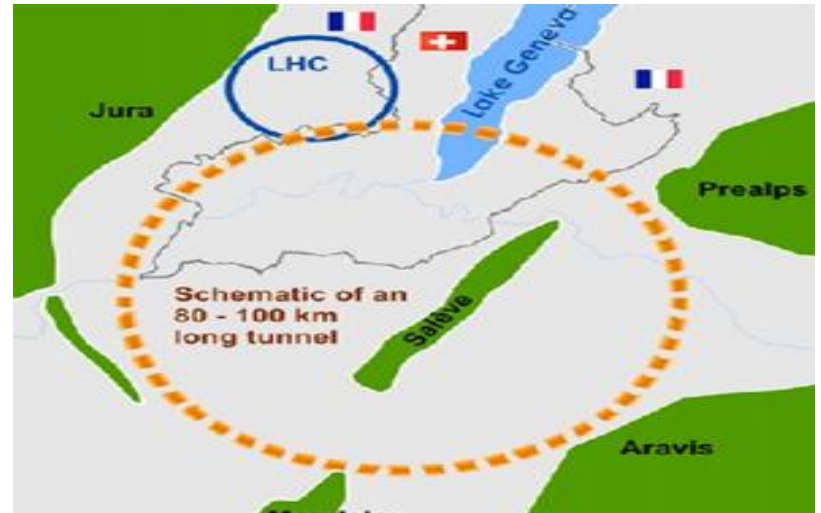
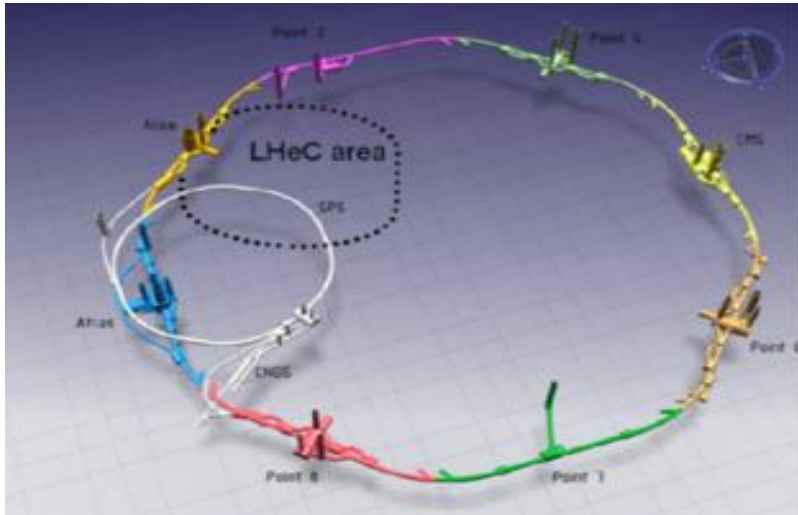
# Outline



- ep colliders and top production
- selected topics in top sector
- selected progress in top sector
  - FCNC  $tqH$
  - CKM element  $V_{tx}$
- summary

# Future projects of ep colliders: LHeC & FCC-eh

Both plan to create new electron facilities



## LHeC

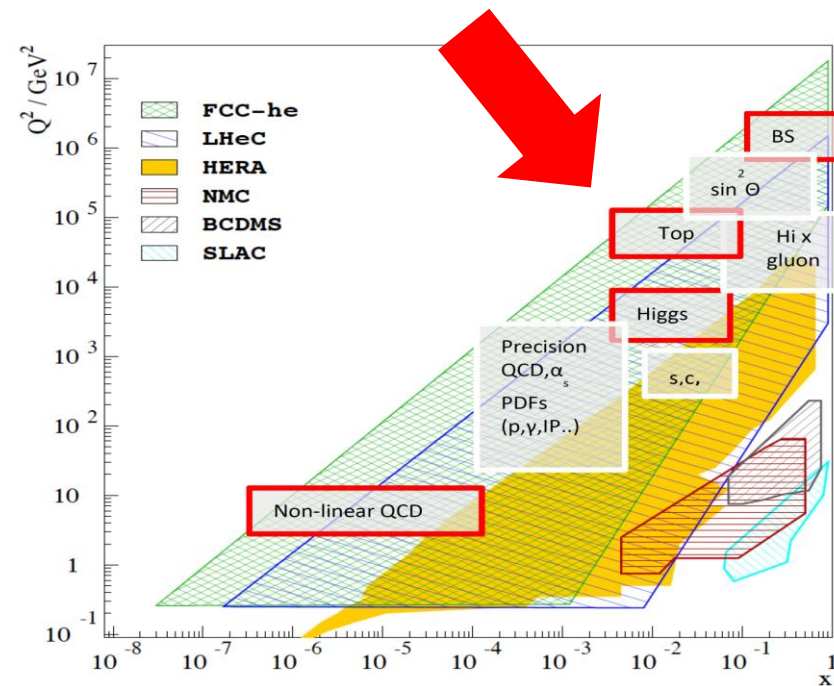
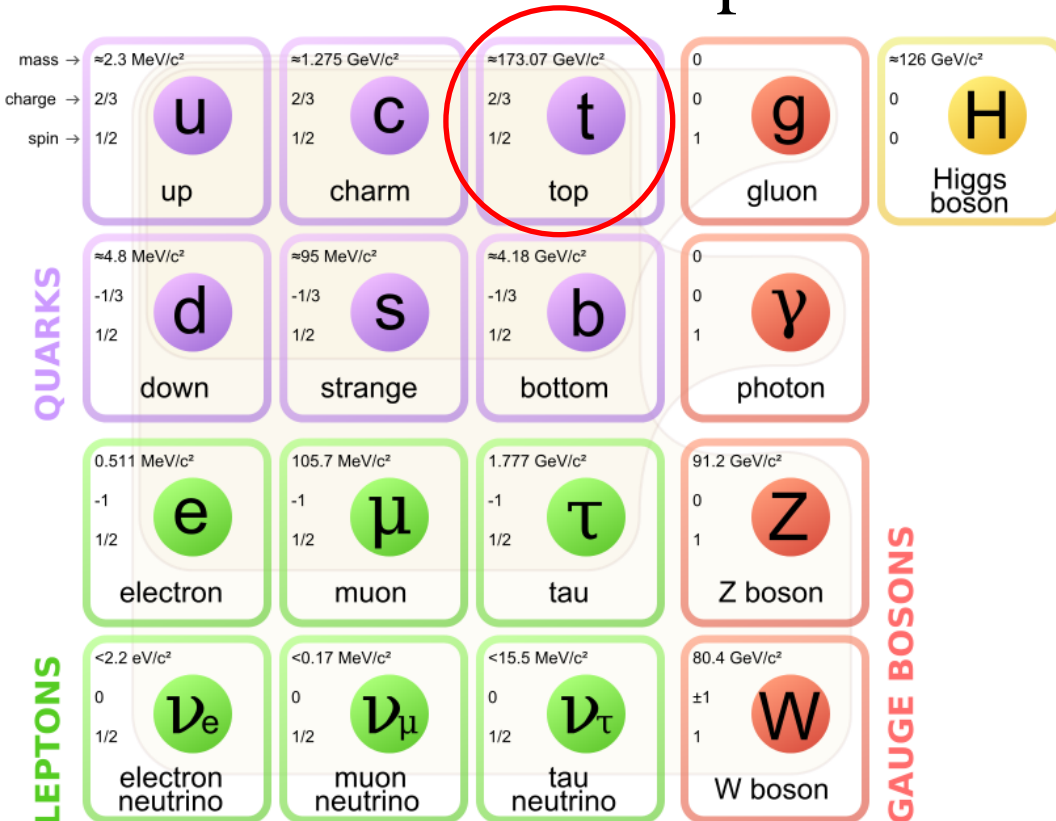
7 TeV proton of LHC  
and 60 GeV electron  
( $\sqrt{s} \sim 1.3$  TeV)

## FCC-eh

50 TeV proton of FCC  
and 60 GeV electron  
( $\sqrt{s} \sim 3.5$  TeV)

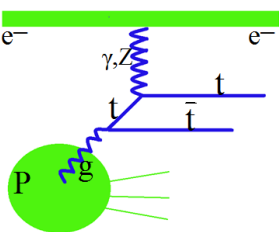
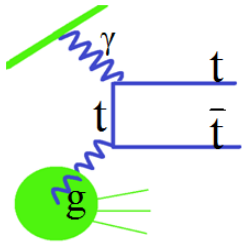
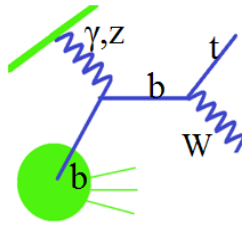
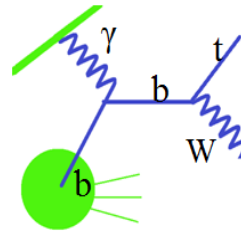
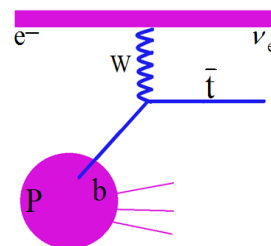
# Top quark Physics at ep colliders

is expected to be sensitive to BSM physics



Ep collider offers nice prospects to study the top quark, especially to study the EW interactions of the top quarks

# Top quark production at the ep colliders

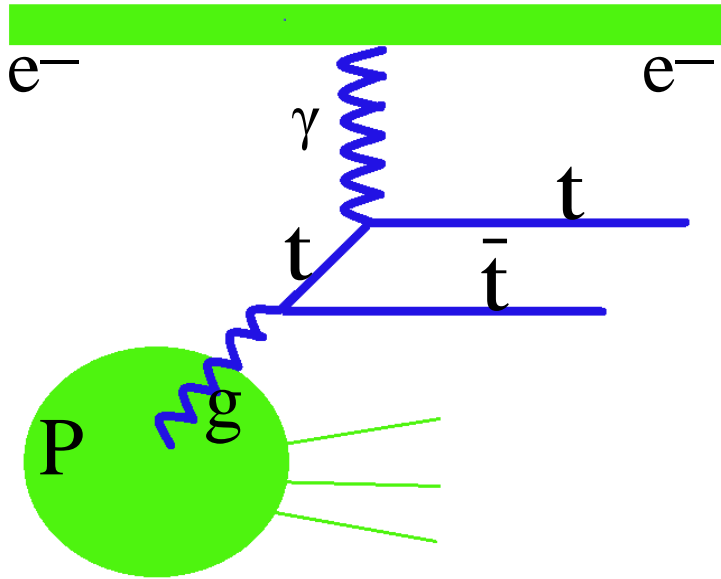
		top pair			single top		
		NC		CC	NC		CC
		DIS	rp	w-exch.	DIS	rp	w-exch.
				-			
30GeV	7TeV	0.003pb	0.009pb		0.003pb	0.013pb	0.74pb
40GeV	7TeV	0.006pb	0.020pb		0.006pb	0.025pb	1.15pb
50GeV	7TeV	0.012pb	0.035pb		0.010pb	0.040pb	1.58pb
60GeV	7TeV	0.017pb	0.053pb		0.014pb	0.056pb	2.02pb
60GeV	50TeV	0.476pb	1.171pb		0.280pb	0.968pb	16.3pb

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# Top Structure Function

NC

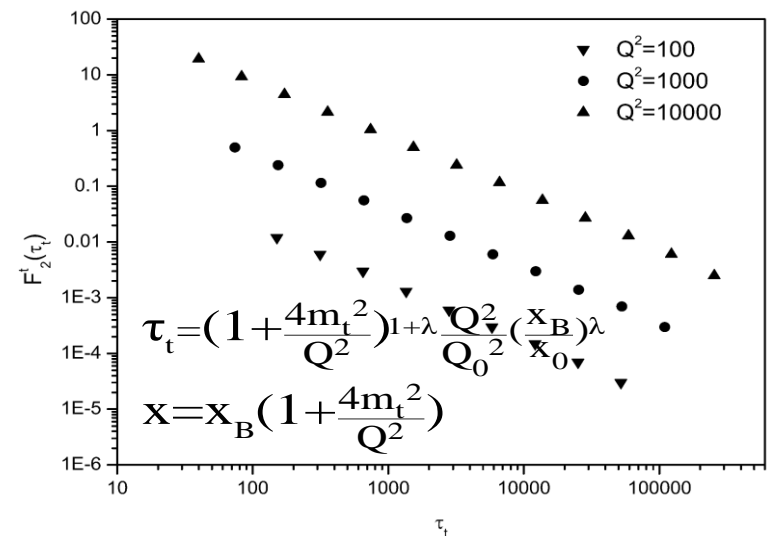
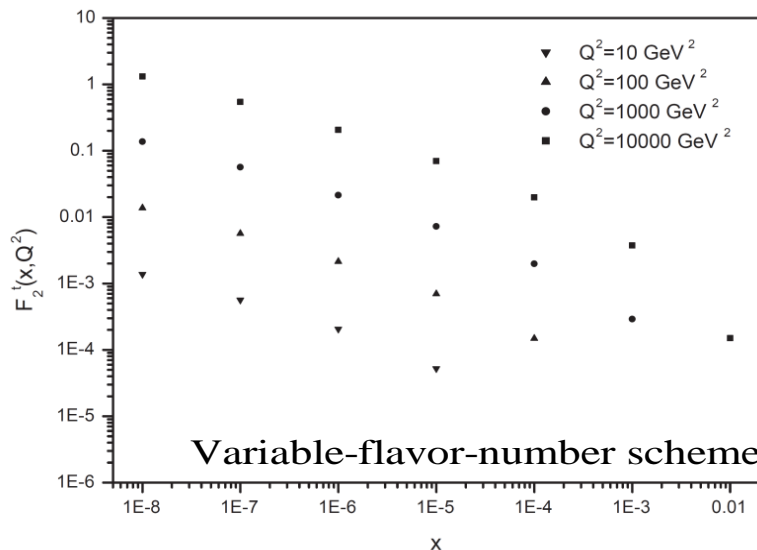


As is known, the DIS  $ff$  production is found sensitive to the gluon density in the proton.

Similarly, but using DIS  $t\bar{t}$  production in, for example, photon-gluon fusion mode, it is useful to

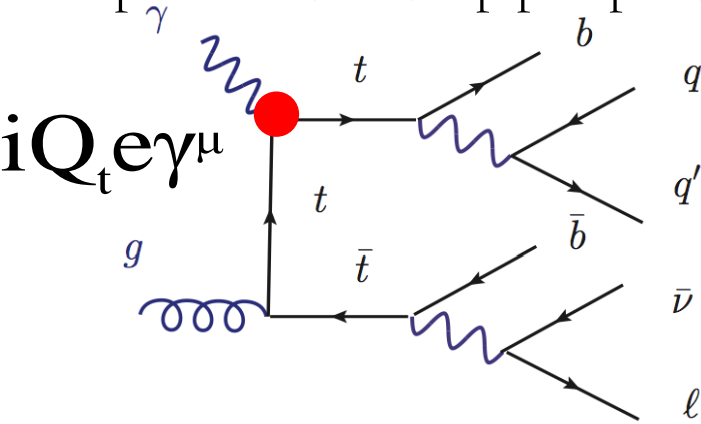


study  $F_2^t(x, Q^2)$ : the top component of the structure function in the ep projects

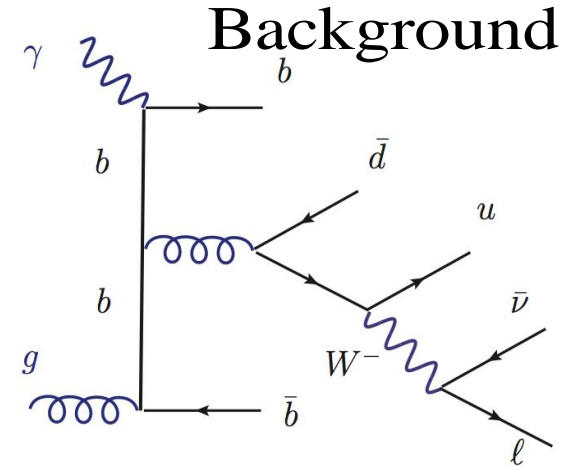


# $t\bar{t}\gamma$ vertex and top electric charge

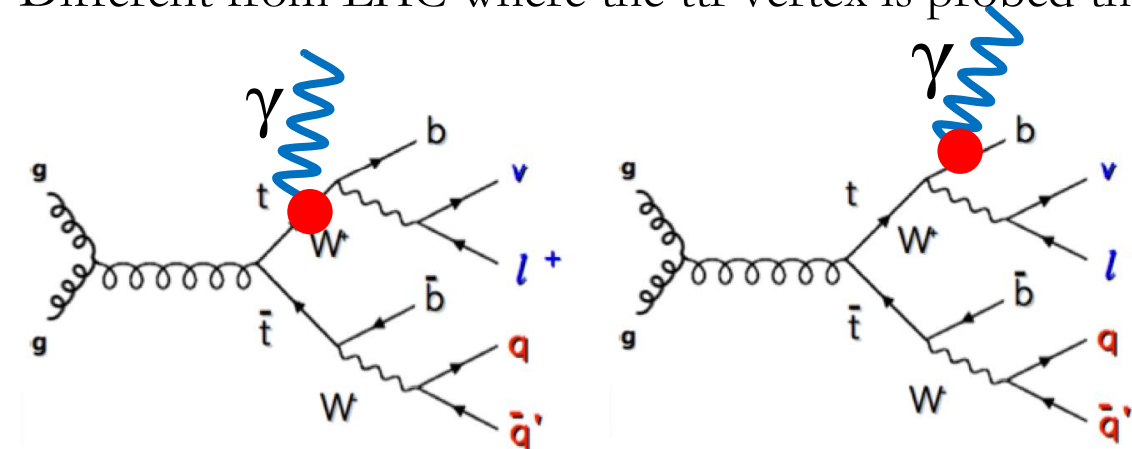
The photo-induced top pair production



measure top quark electric charge



Different from LHC where the  $t\bar{t}\gamma$  vertex is probed through  $t\bar{t}\gamma$  productions.



The out going photon could come from other charge sources like the top decay products

thus make such measurement challenge at the LHC

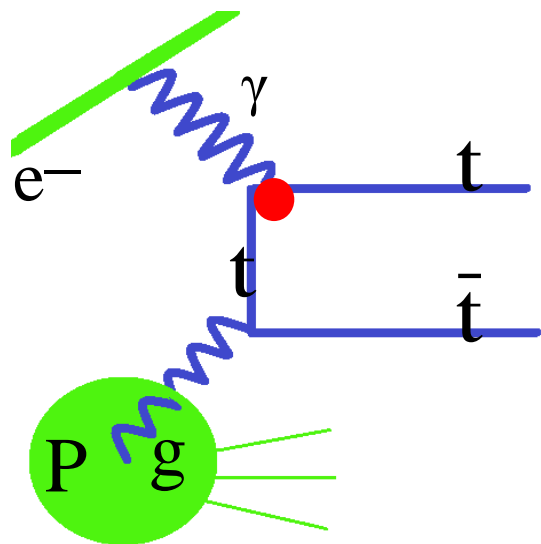


# Anomalous $t\bar{t}\gamma$ couplings

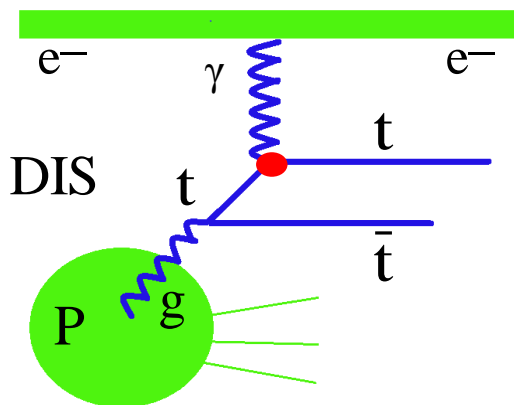
NC

Follow the same idea

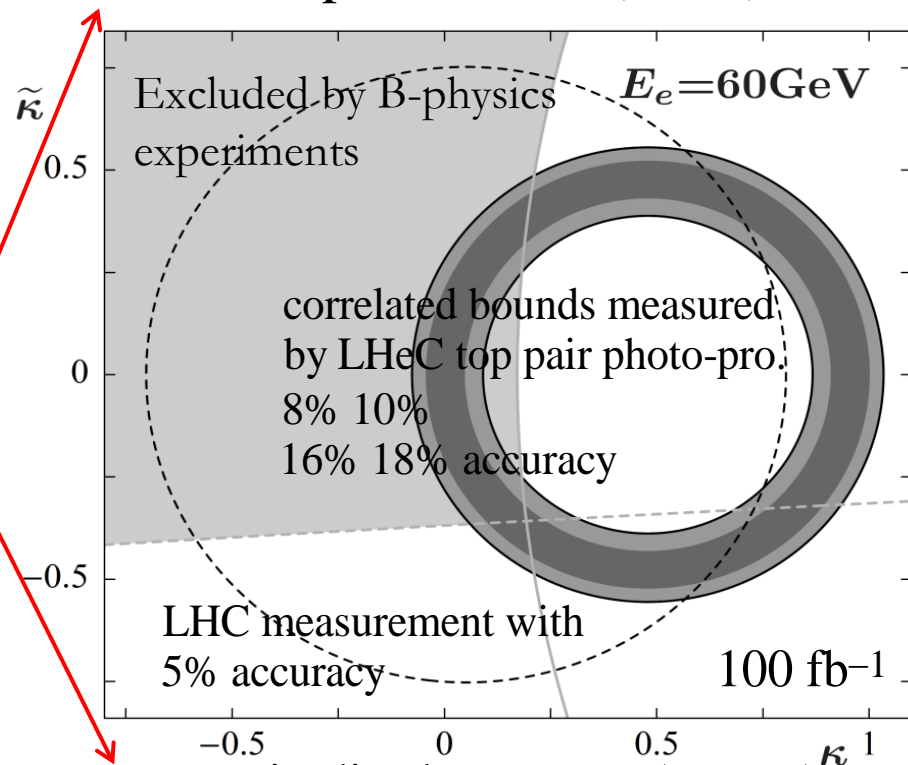
$$\mathcal{L}_{t\bar{t}\gamma} = e\bar{t} \left[ Q_t \gamma^\mu A_\mu + \frac{1}{4m_t} \sigma^{\mu\nu} F_{\mu\nu} (\kappa + i\tilde{\kappa}\gamma_5) \right] t$$



Or can be used to set constraints

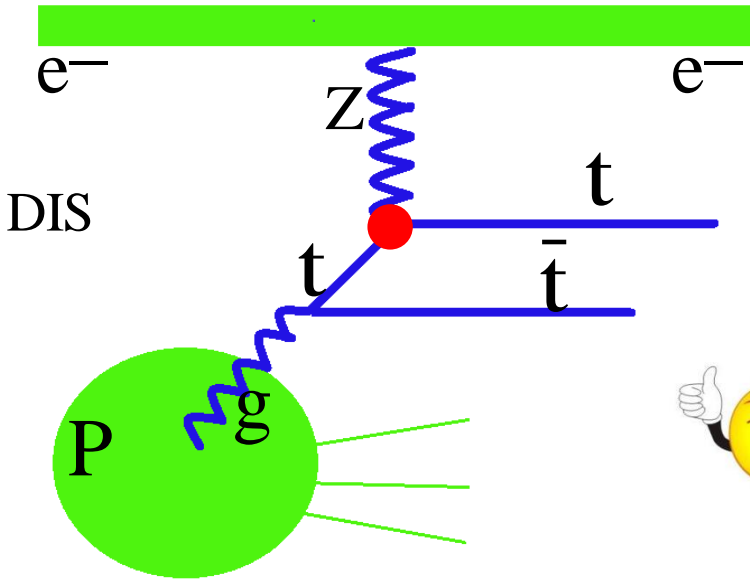


electric dipole moment(EDM):  $\tilde{\kappa}$



magnetic dipole moment(MDM):  $\kappa$

# Anomalous $t\bar{t}Z$ couplings



Similarly, but through DIS top pair production from gluon-Z fusion, one can study ...

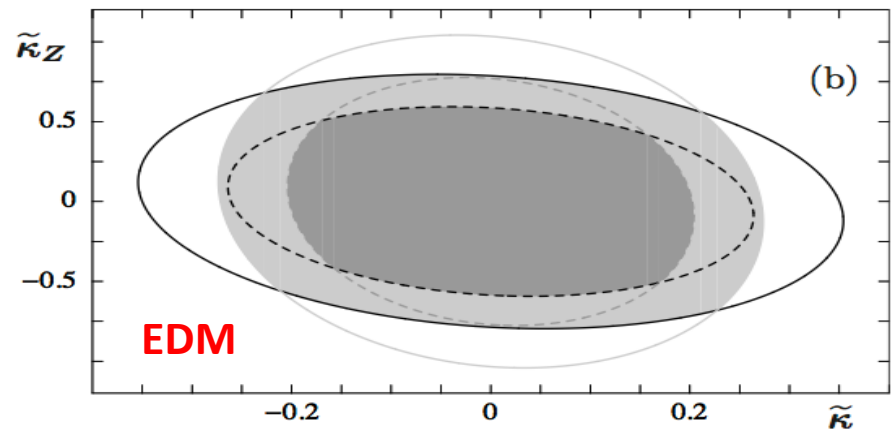
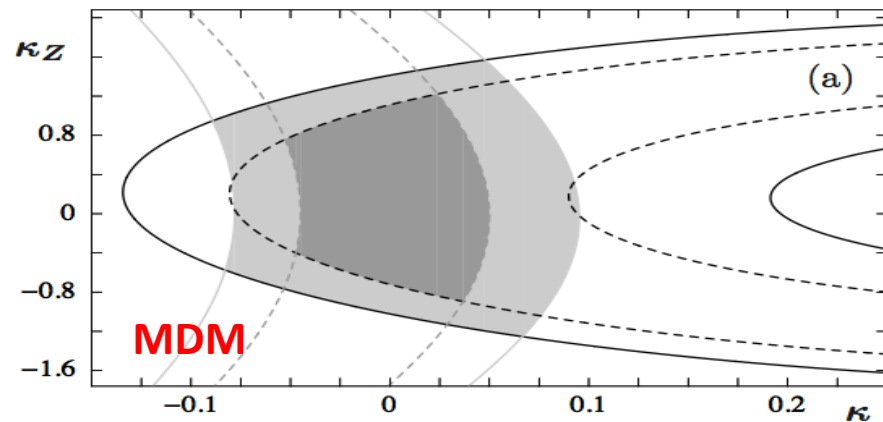
$$\mathcal{L}_{t\bar{t}Z} = \frac{g}{2c_w} \bar{t} \left( \frac{1}{4m_t} \sigma^{\mu\nu} Z_{\mu\nu} (\kappa_Z + i\tilde{\kappa}_Z \gamma_5) \right) t$$



Finally, the parameter bounds can be found:

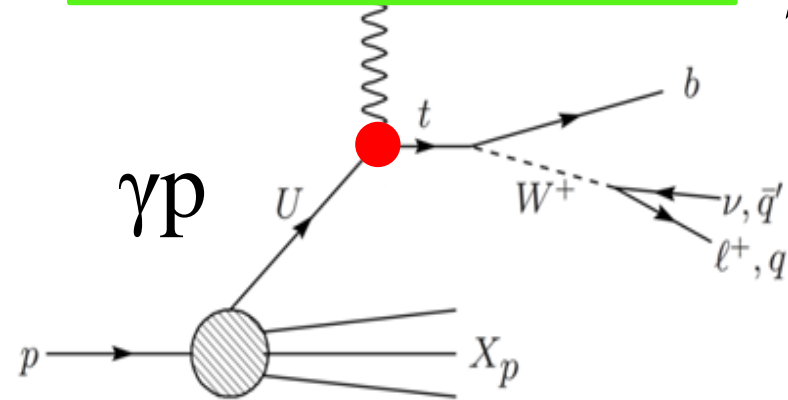
property	precision
EDM: $\tilde{\kappa}/\tilde{\kappa}_Z$	<b>0.20-0.28/0.6-0.8</b>
MDM: $\kappa/\kappa_Z$	<b>0.05-0.09/0.9-1.3</b>

10%-18%  
accuracy



# Anomalous FCNC $tq\gamma$ couplings

NC



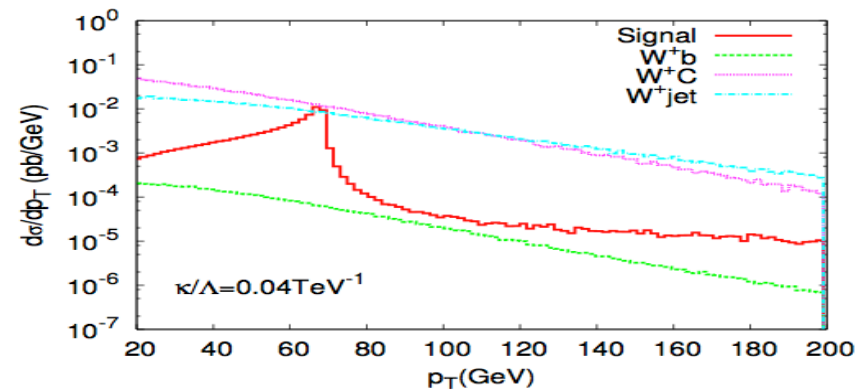
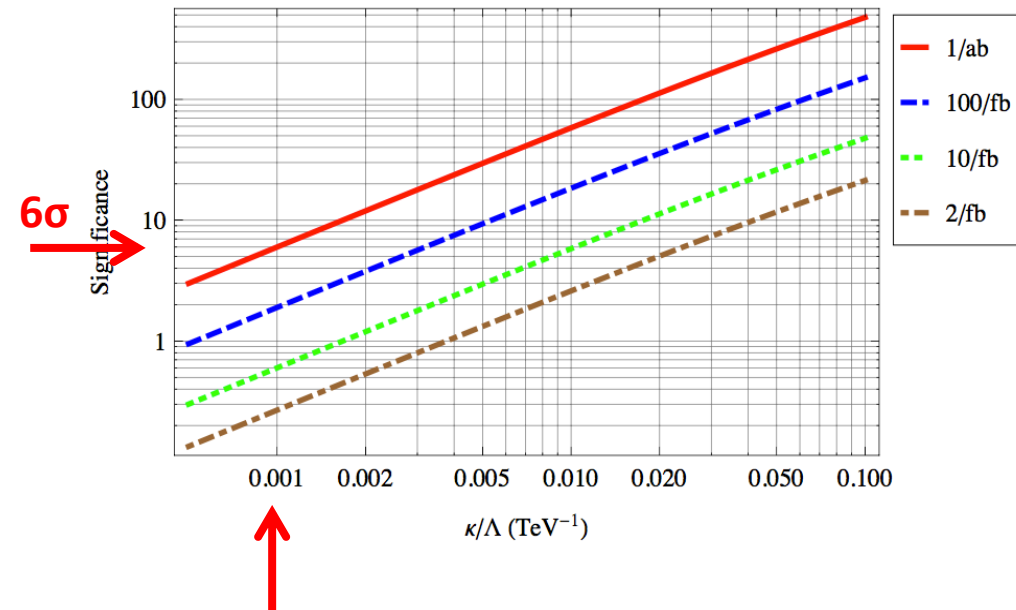
The effective L involving ano.  $tqr$  interaction is given:

$$\mathcal{L}_{tq\gamma} = -g_e \sum_{q=u,c} Q_q \frac{\kappa_q}{\Lambda} \bar{t} \sigma^{\mu\nu} (f_q + h_q \gamma_5) q A_{\mu\nu} + \text{h.c.}$$

It was found that ep based rp collider can provide a nice prospect to probe it:



With 1 ab<sup>-1</sup>, the  $tqr$  coupling can be probed down to order of 10<sup>-3</sup> at the LHeC

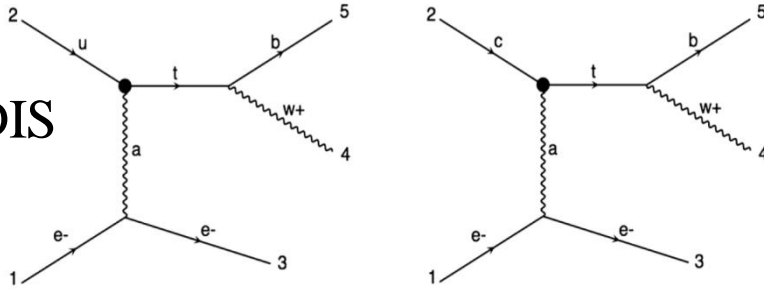


LHeC TDR J.Phys.G39,075001(2012)

Al.T.Cakir, O.Cakir, S.Sultansoy, Phys.Lett.B685:170-173,(2010)

# Anomalous FCNC tq $\gamma$ and tqZ couplings

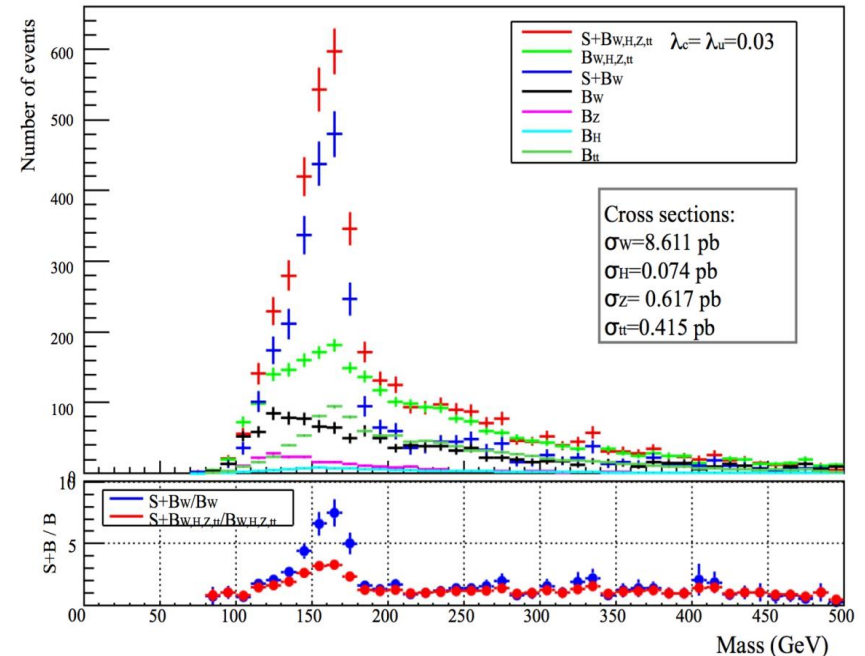
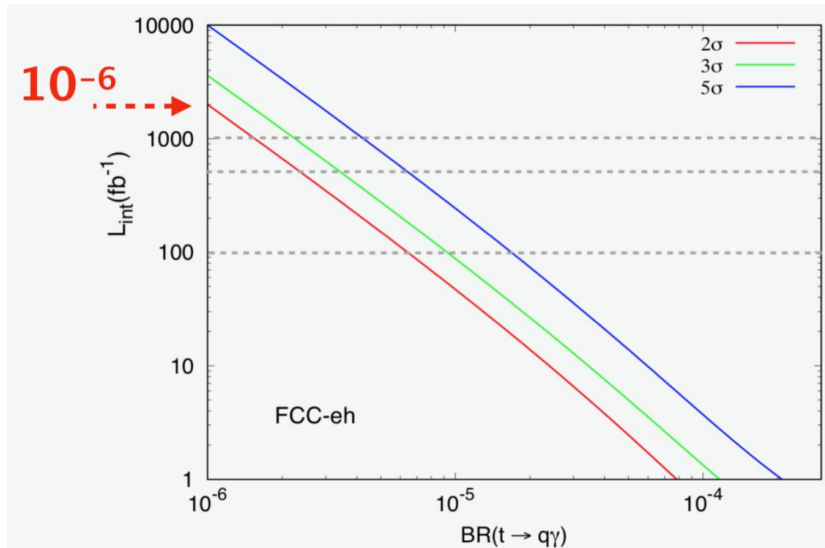
DIS



Through the DIS production, one can set constraints to both the tq $\gamma$  and tqZ couplings

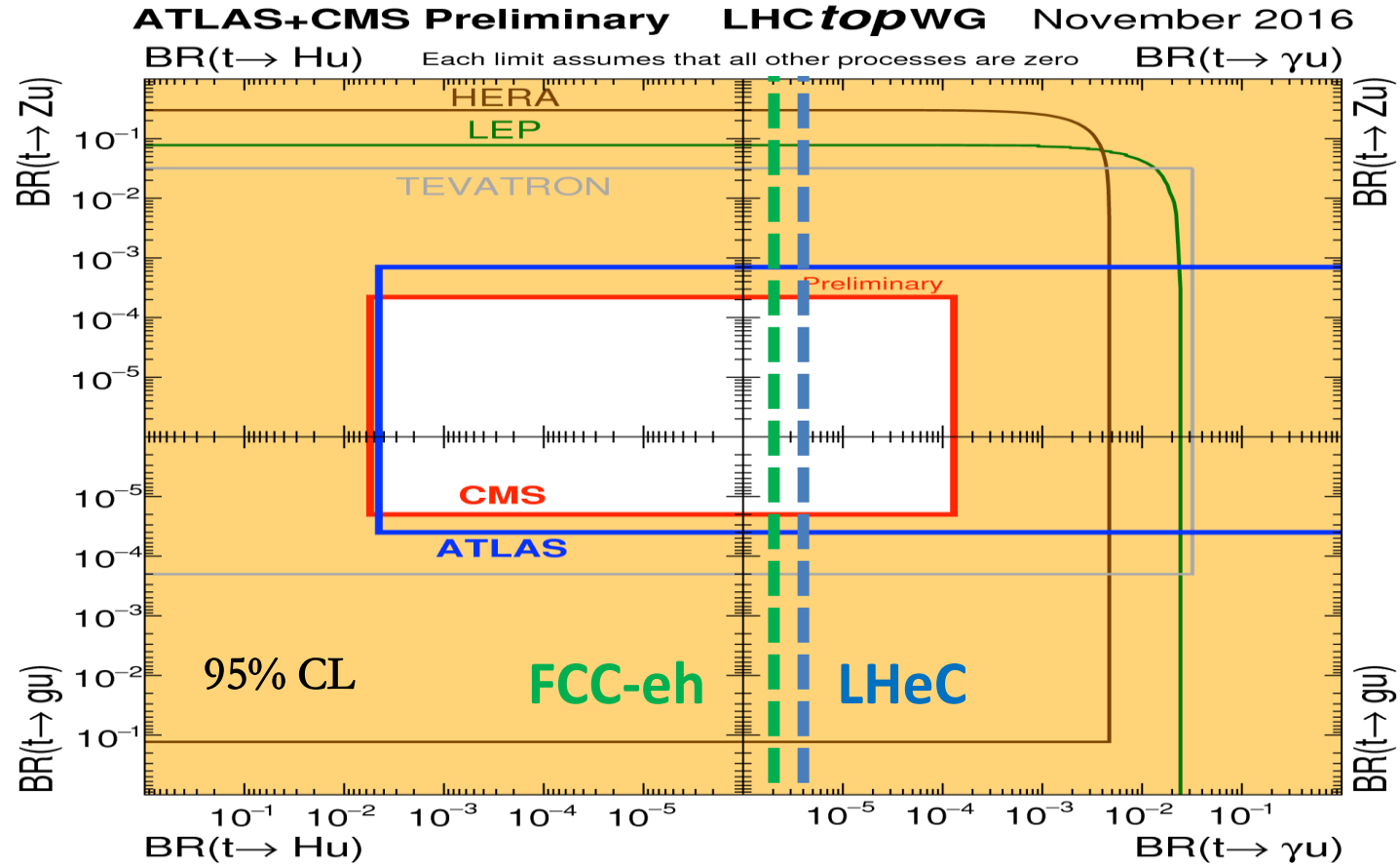
Cuts	Definitions
Cut-0	Preselection cuts with number of jets $\geq 3$ and one electron with $p_T^e > 20$ GeV
Cut-1	One jet with $b$ -tagging
Cut-2	$p_T^b > 40$ GeV and $p_T^{j_2, j_3} > 30$ GeV,
Cut-3	$-5 < \eta^{b, j_2, j_3} < 0$ and $-2.5 < \eta^e < 2.5$
Cut-4	$60 \text{ GeV} < M_{\text{inv}}^{\text{rec}}(j_2, j_3) < 90 \text{ GeV}$
Cut-5	$130 \text{ GeV} < M_{\text{inv}}^{\text{rec}}(j_b, j_2, j_3) < 200 \text{ GeV}$

at the same level at the FCC-eh after the detector effects are considered.



# Anomalous FCNC $tq\gamma$ couplings

NC

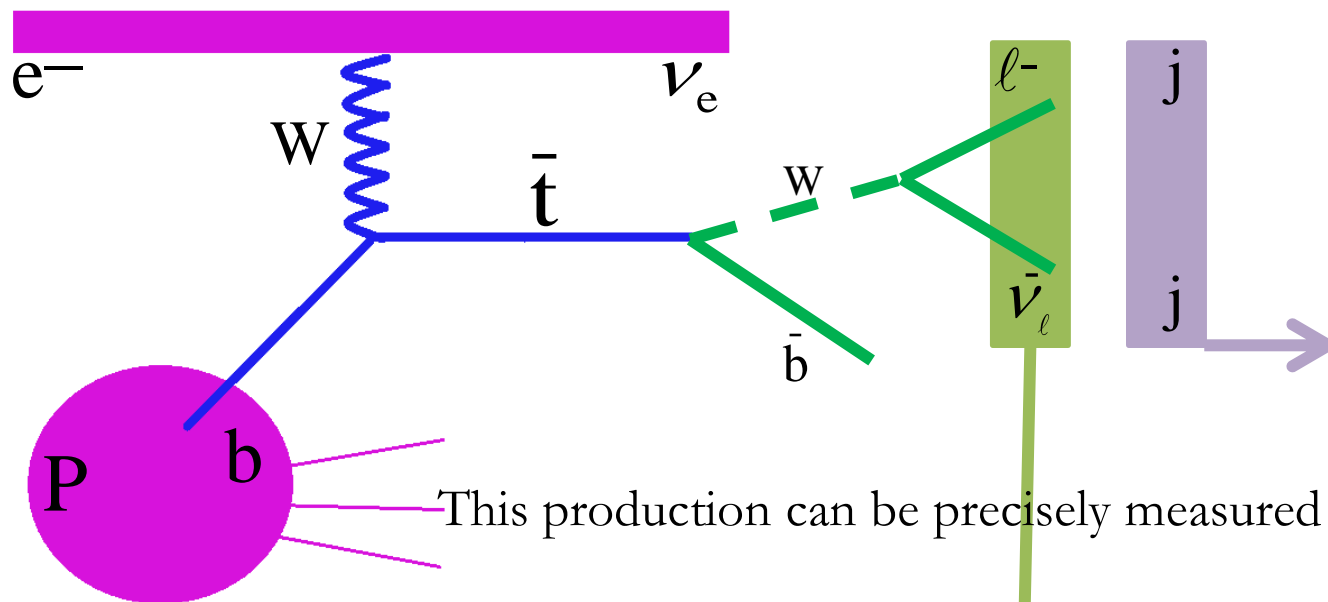


Detector Level study  
 $E_e = 60 \text{ GeV}$   $2ab^{-1}$

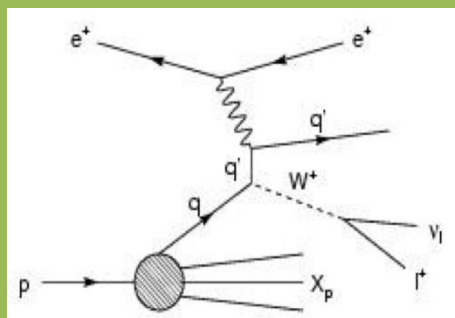


It was found that by performing the detector level study, the branching ratio of  $t \rightarrow q\gamma$  and  $t \rightarrow qZ$  can be measured down to order of  $\sim 10^{-6}$  at the FCC-eh with  $2ab^{-1}$ .

# Charged Current Top quark Production

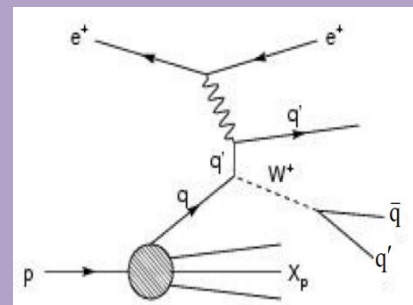


$$\begin{aligned}
 E_T &\geq 25 \text{ GeV} \\
 \Delta\Phi_{E,j} &\geq 0.4 \\
 \Delta\Phi_{E,b} &\geq 0.4 \\
 \Delta\Phi_{E,\ell} &\geq 0.4 \\
 p_{T,j,b,\ell} &\geq 20 \text{ GeV} \\
 |\eta_j| &\leq 5, |\eta_{b,\ell}| \leq 2.5, \\
 \Delta R_{\ell,b/j} &\geq 0.4
 \end{aligned}$$



$$\begin{aligned}
 Nt &= 11000, \\
 S/B &= 11
 \end{aligned}$$

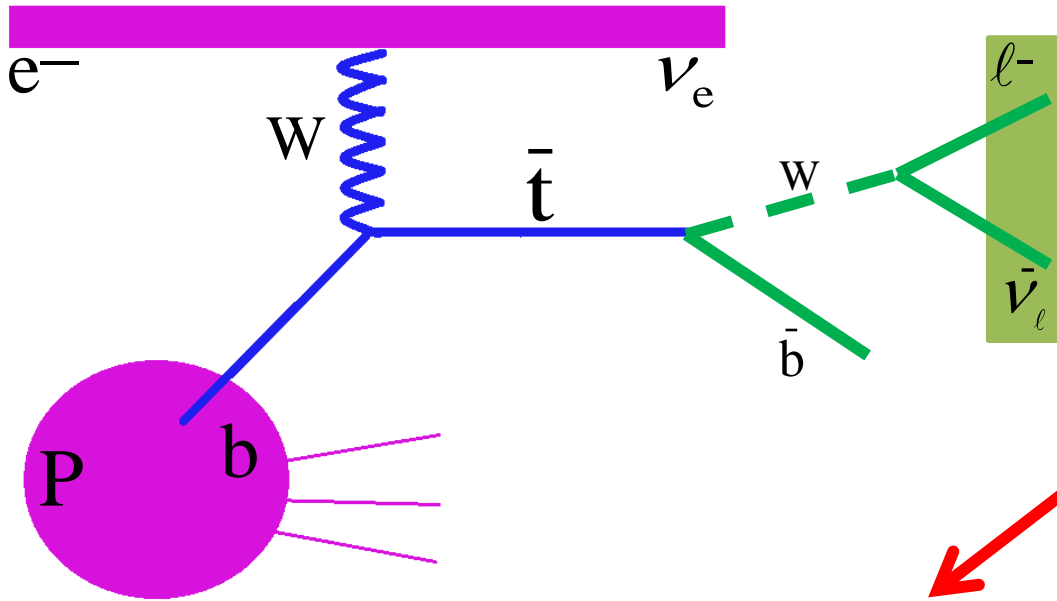
Now let's see some CC top productions through W-boson exc in both decay modes...



$$\begin{aligned}
 E_T &\geq 25 \text{ GeV} \\
 \Delta\Phi_{E,j} &\geq 0.4 \\
 \Delta\Phi_{E,b} &\geq 0.4 \\
 |m_{j,j_2} - m_w| &\leq 22 \text{ GeV} \\
 p_{T,j,b} &\geq 20 \text{ GeV} \\
 |\eta_j| &\leq 5, |\eta_b| \leq 2.5, \\
 \Delta R_{j,b/j} &\geq 0.4
 \end{aligned}$$

$$\begin{aligned}
 Nt &= 22000, \\
 S/B &= 1.2
 \end{aligned}$$

# top quark spin polarisation



Such prediction can be used, for example, to measure the top quark spin polarization.

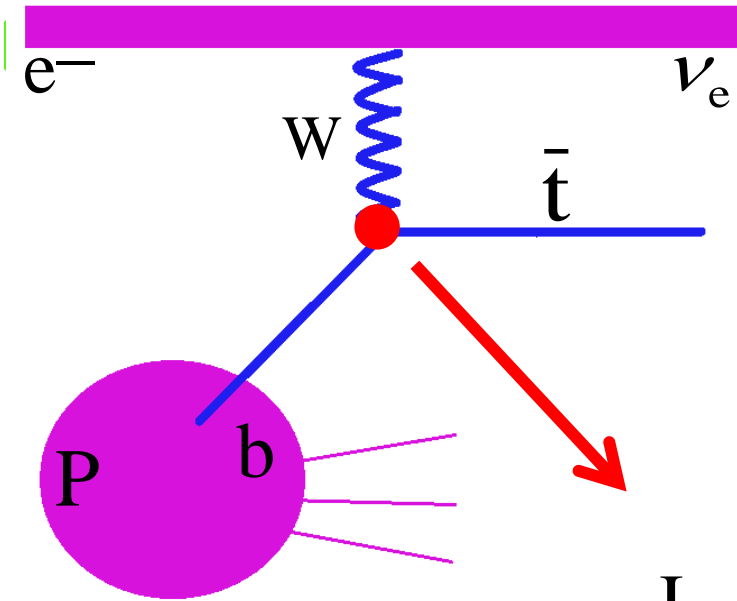
$$\frac{1}{\Gamma_t} \frac{d\Gamma}{d\cos\theta} = \frac{1}{2} (1 + A_{\uparrow\downarrow} \cos\theta)$$

Here,  $\theta$  is angle between the charged lepton and the spin quantisation axis in the top rest frame

$$A_{\uparrow\downarrow} = \frac{N_{\uparrow} - N_{\downarrow}}{N_{\uparrow} + N_{\downarrow}}$$

spin asymmetry

# Anomalous Wtb couplings



The CC single top production is also a good way to test the anomalous tbW couplings.

The Lagrangian is given by this formula

$$\mathcal{L}_{Wtb} = \frac{g}{\sqrt{2}} \left[ -\frac{1}{2m_W} W_{\mu\nu} \bar{t} \sigma^{\mu\nu} (f_{\text{V}}^{\text{L}} P_{\text{L}} + f_{\text{V}}^{\text{R}} P_{\text{R}}) b \right] + \text{h.c.}$$

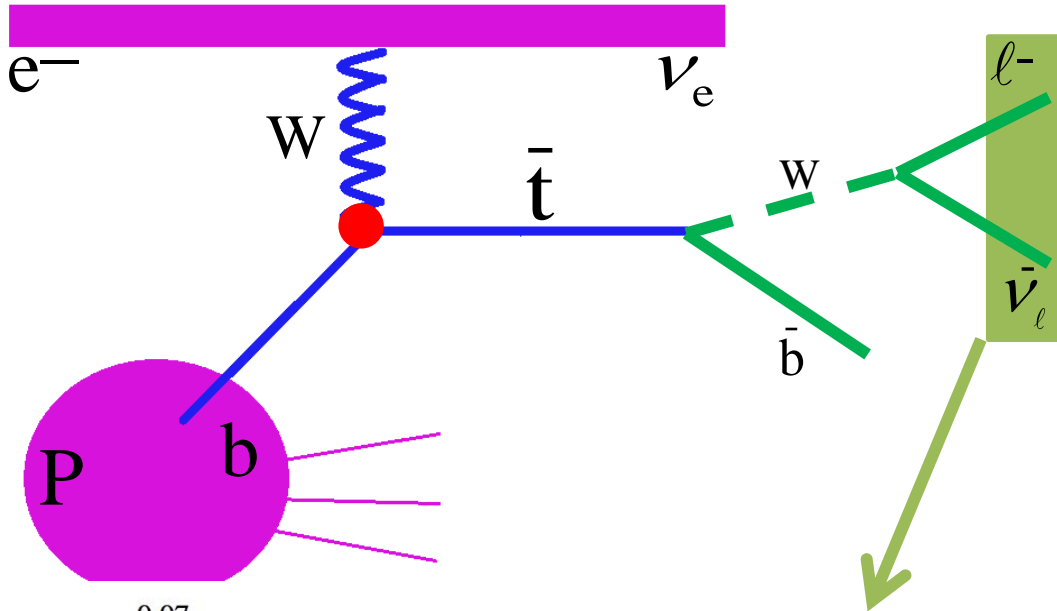
The fact that the left-handed vector current is one to a good approximation, and the vanishing of the other parameters correspond to the SM case as within the SM the tbW vertex is purely left-handed.

$$|V_{\text{tb}}| f_{\text{V}}^{\text{L}} \simeq 1, f_{\text{V}}^{\text{R}}, f_{\text{T}}^{\text{L}}, f_{\text{T}}^{\text{R}} = 0$$



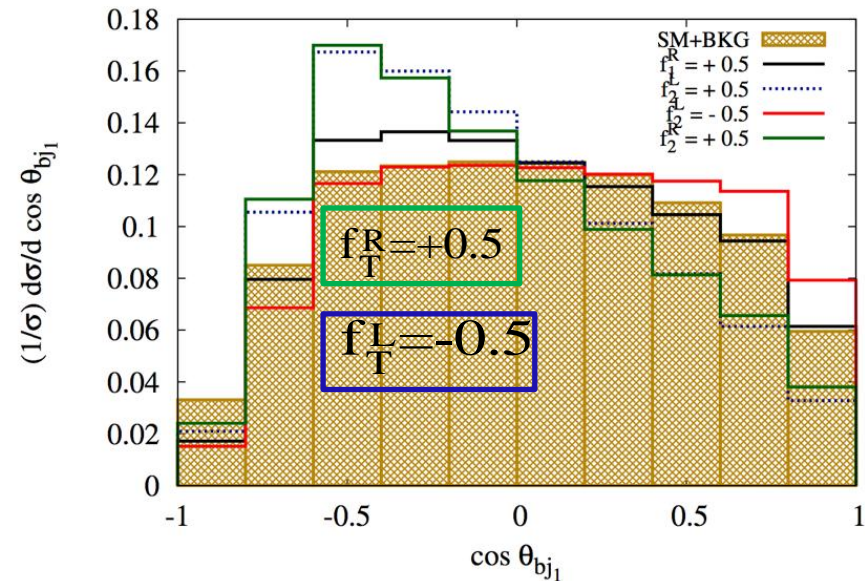
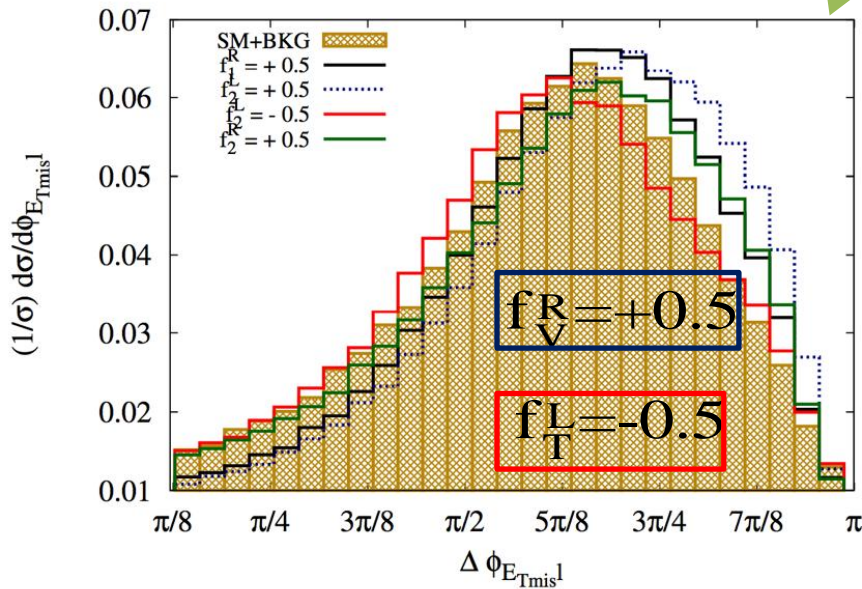
# Anomalous $Wtb$ couplings

CC



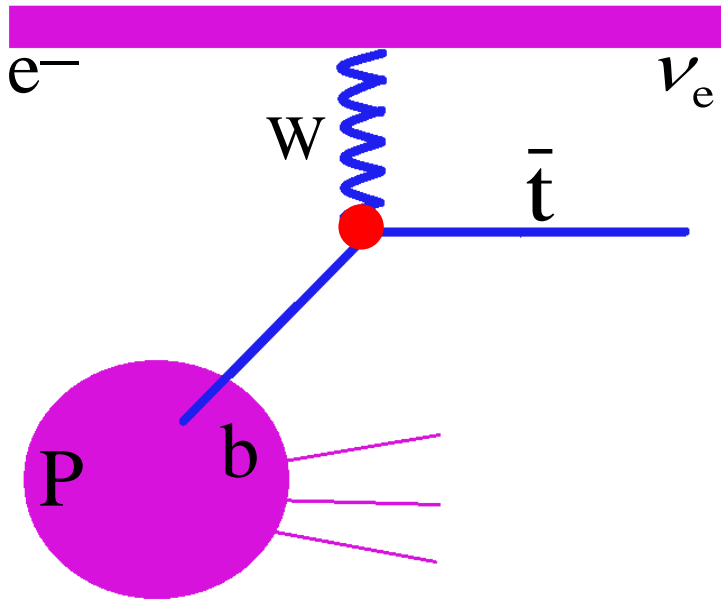
Studies were performed in both the leptonic and hadronic decay modes.

$$L_{Wtb} = \frac{g}{\sqrt{2}} \left[ \frac{W_\mu \bar{t} \gamma^\mu (V_{tb} f_V^L P_L + f_V^R P_R) b}{2m_W} - \frac{1}{2m_W} W_{\mu\nu} \bar{t} \sigma^{\mu\nu} (f_T^L P_L + f_T^R P_R) b \right] + \text{h.c.}$$



# Anomalous $Wtb$ couplings

CC

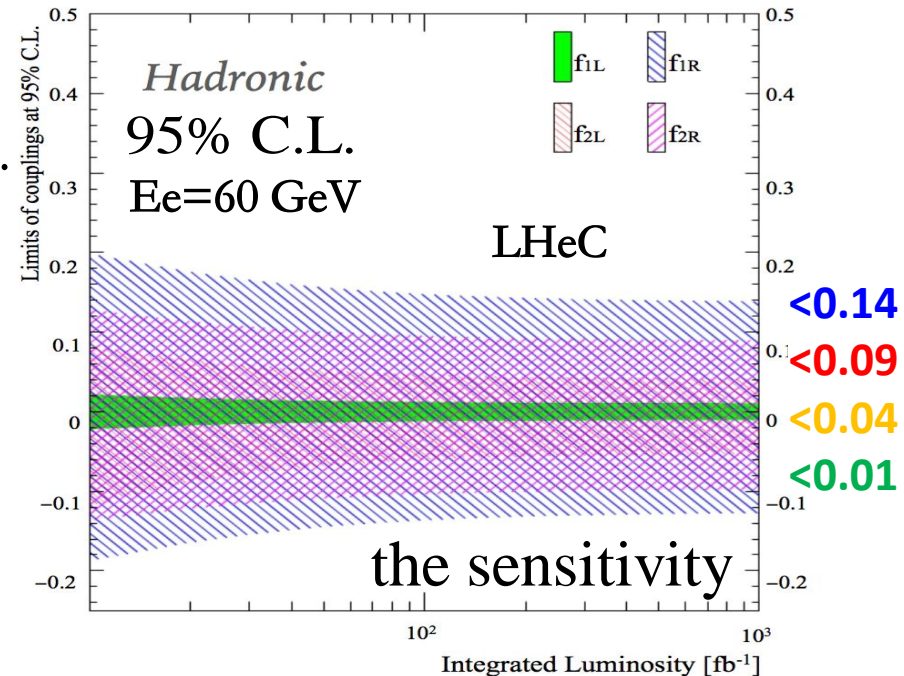
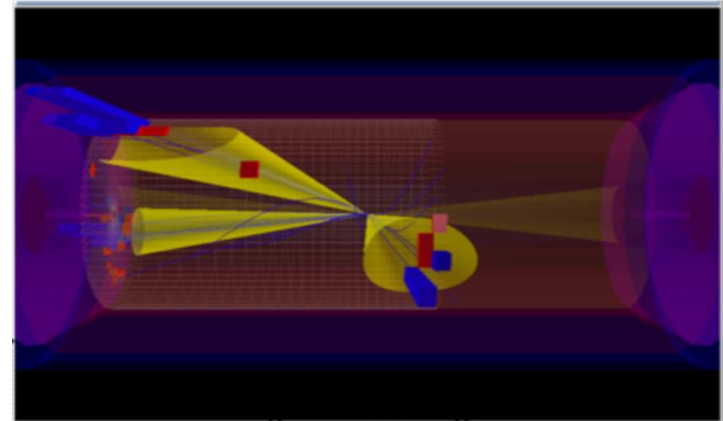


$$L_{Wtb} = \frac{g}{\sqrt{2}} \left[ -\frac{1}{2m_W} W_{\mu\nu} \bar{t} \sigma^{\mu\nu} (f_T^L P_L + f_T^R P_R) b \right] + \text{h.c.}$$



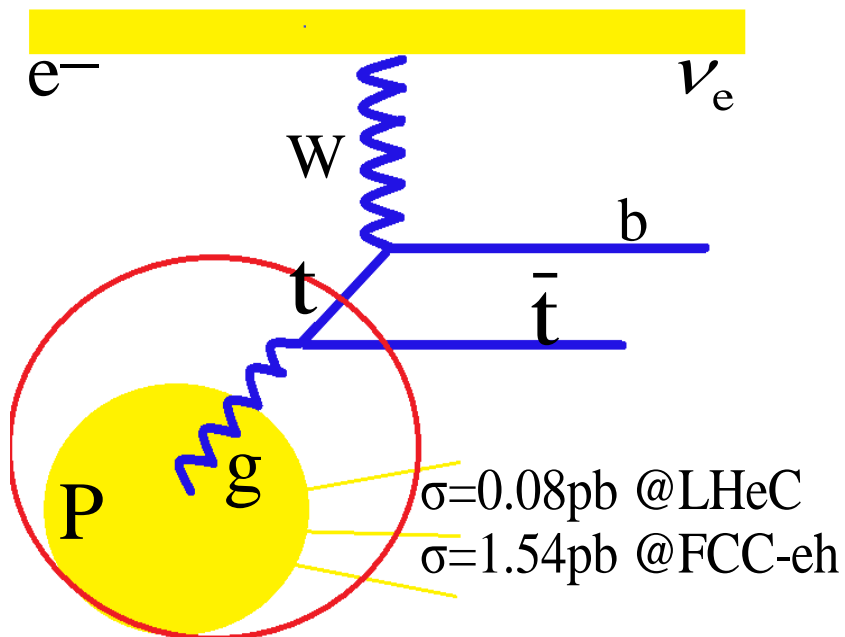
The analysis show that the  $tbW$  vertex can be probed at the LHeC, already to a very high accuracy, compare to the existing limits from the LHC.

By including the detector level simulation, the parameter sensitivity are obtained.



# Charged Current Top quark Production

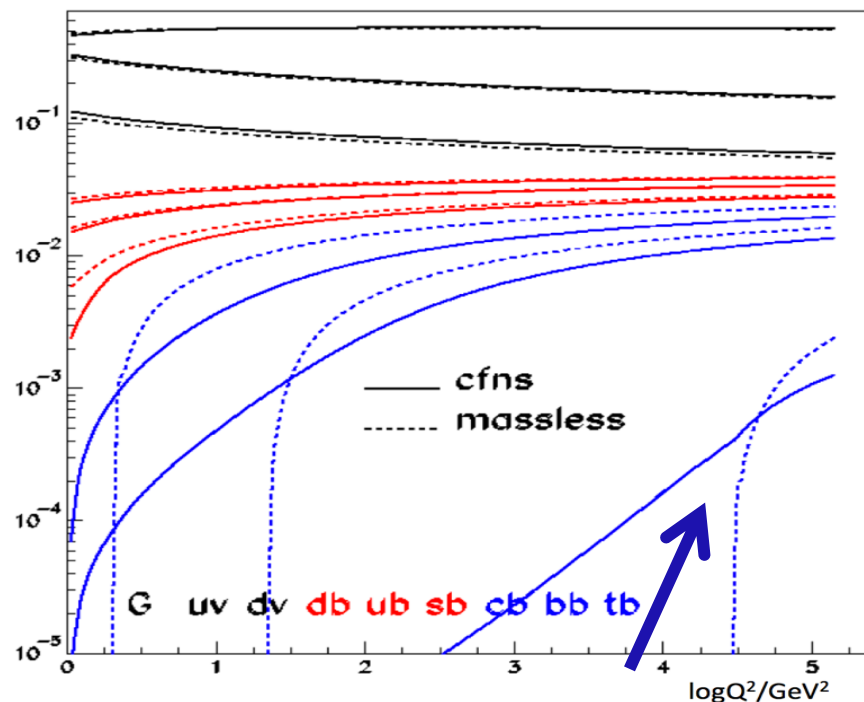
CC



since at very high scale, the top quark may be considered 'light'



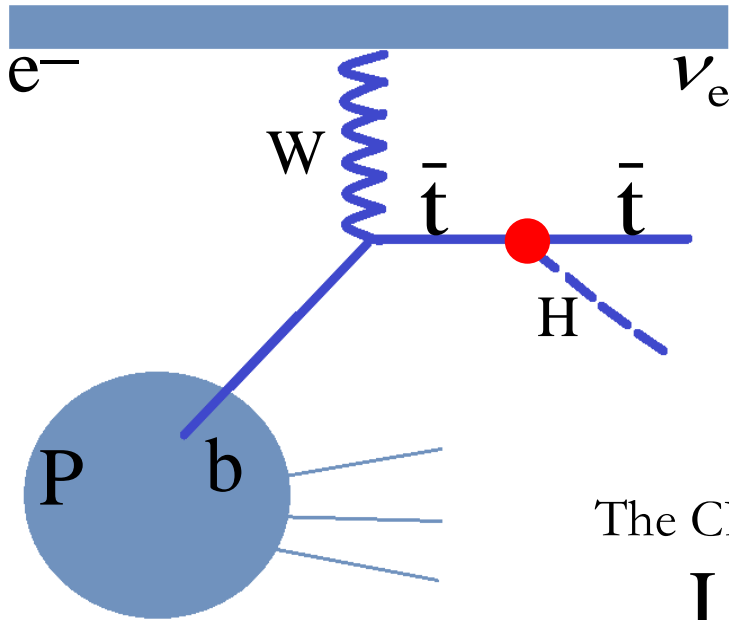
Another charged current top production makes it possible to consider quark density for the top.



Here a six-flavor-variable-number scheme for top quark can be proposed.

Thus the ep projects offers new field of research for the top quark parton distribution functions.

# CP nature of top-Higgs couplings



Considering the top and Higgs associated production, we can study the CP nature of the  $t\bar{t}H$  coupling.

The CP-phase dependent lagrangian can be written here:

$$\mathcal{L}_{t\bar{t}H} = -i \frac{m_t}{v} \bar{t} \left[ \kappa \cos \zeta_t + i \gamma_5 \sin \zeta_t \right] t H$$

$\zeta_t = 0, \kappa = 1 \rightarrow$  SM case

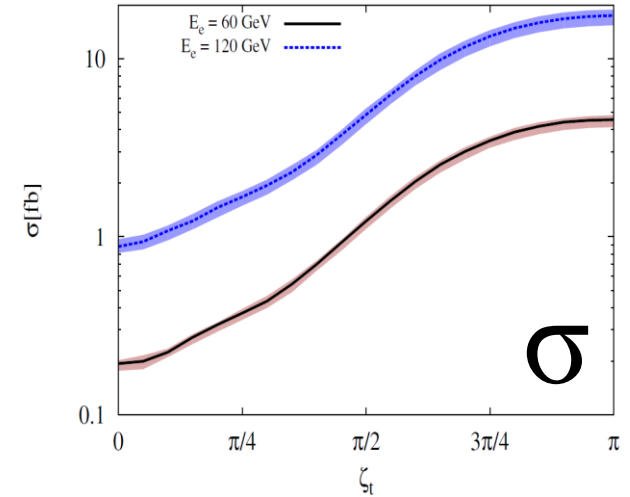
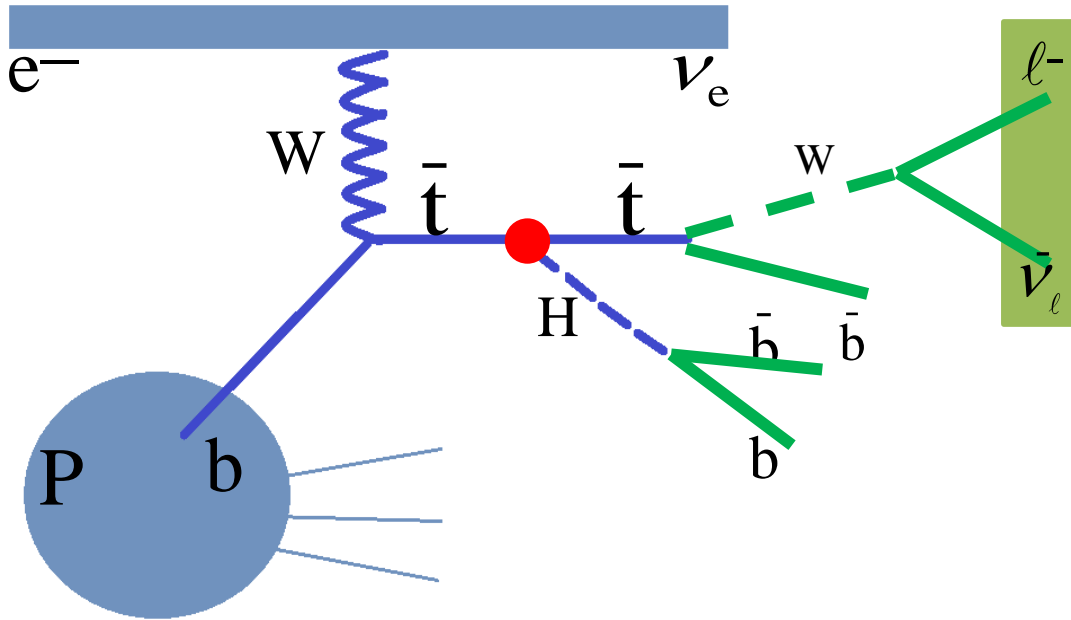
$\zeta_t = 0$  or  $\zeta_t = \pi \rightarrow$  pure scalar state

$\zeta_t = \pi/2 \rightarrow$  pure pseudo scalar state

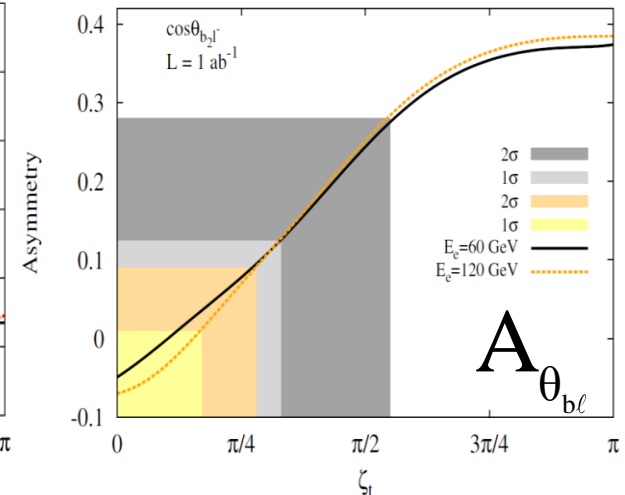
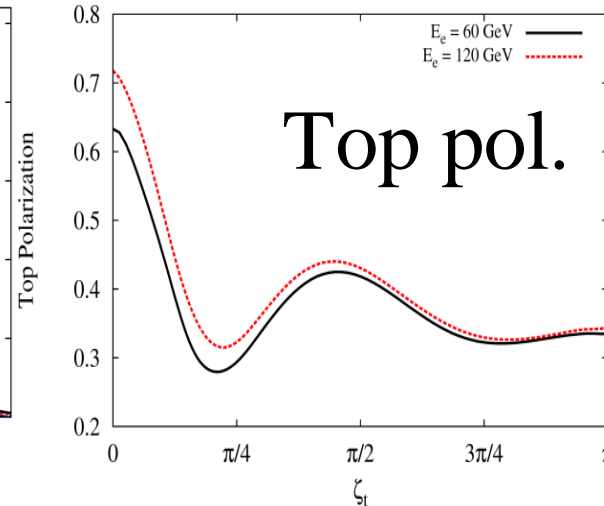
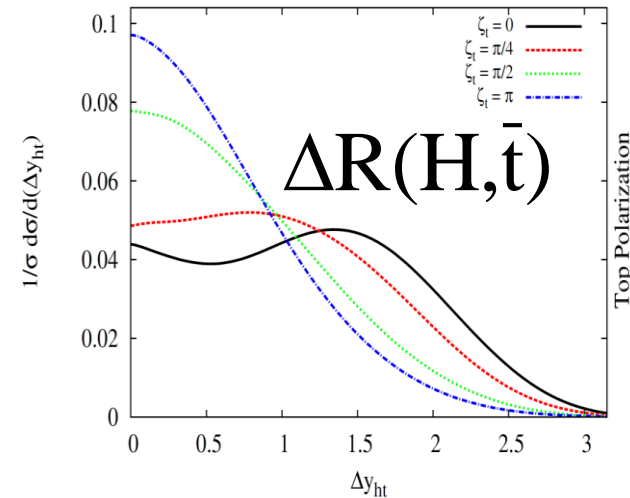
$0 < \zeta_t < \pi/2$  or  $\pi/2 < \zeta_t < \pi \rightarrow$  mixture CP-states

# CP nature of top-Higgs couplings

CC

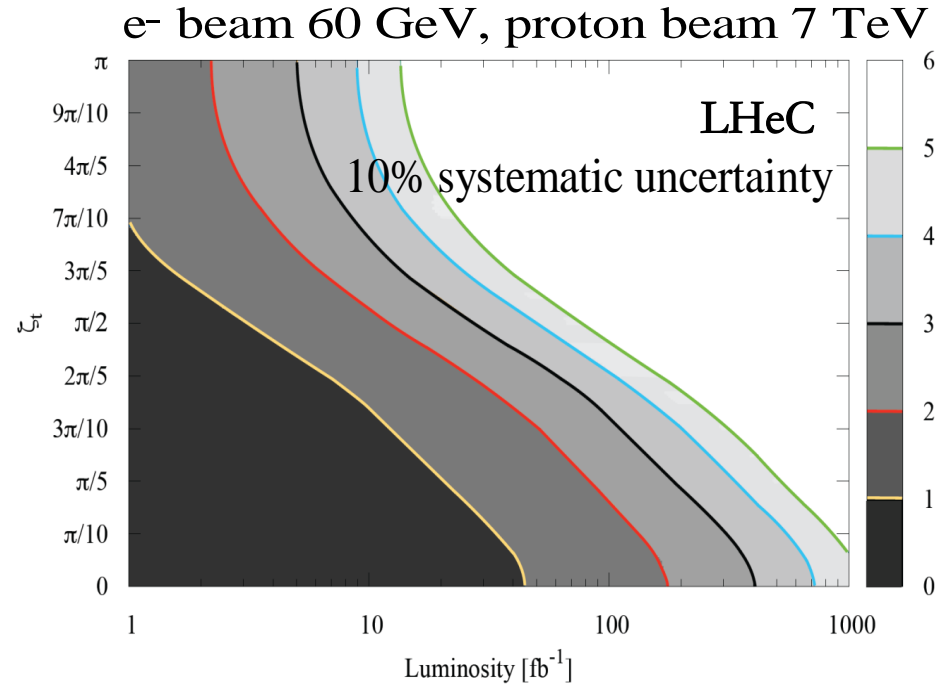
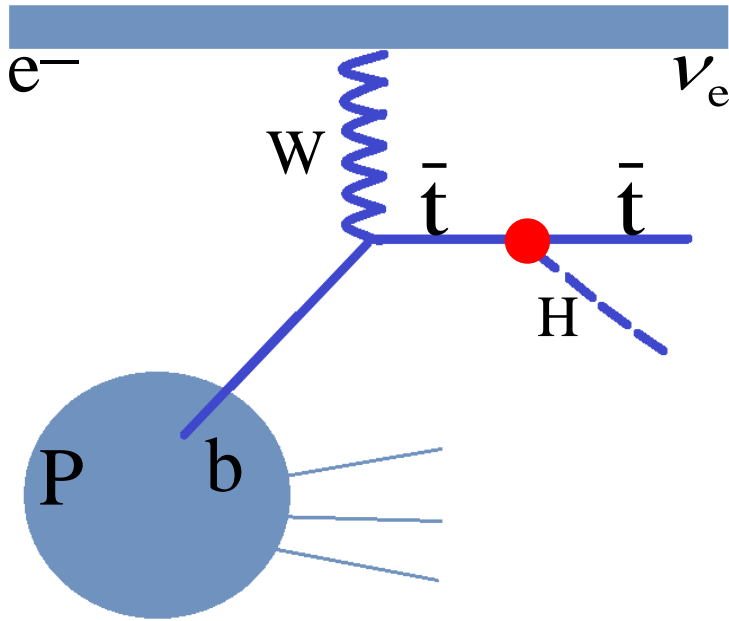


The study was performed by considering  $h \rightarrow b\bar{b}$  and top leptonic decay.



# CP nature of top-Higgs couplings

CC




It was found that a non-zero phase can be observed/excluded better than 4 sigma confidence level.

100 fb<sup>-1</sup>:  $\pi/5 < \zeta_t < \pi$  (2σ) and  $3\pi/10 < \zeta_t < \pi$  (3σ) Exc.  
 400 fb<sup>-1</sup>:  $\pi/6 < \zeta_t < \pi$  (4σ) and  $\pi/4 < \zeta_t < \pi$  (5σ) Exc.  
 HL-LHC 3ab<sup>-1</sup> probe up to  $\zeta_t = \pi/6$

The work is preparing to be update at the FCC-eh.



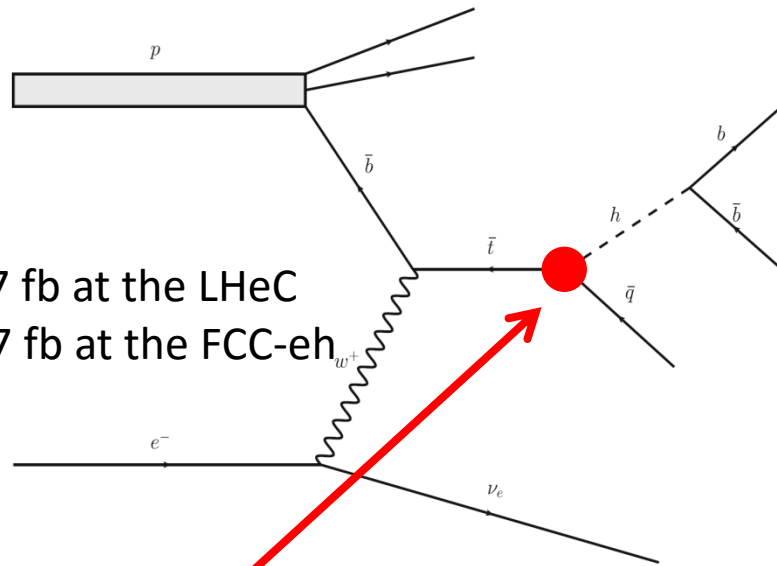
We can conclude that the ep colliders provide a better environment to test the CP nature of the ttH couplings.

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# Anomalous FCNC tqH couplings

signal.I:  $ep \rightarrow \nu_e \bar{t} \rightarrow \nu_e h \bar{q} \rightarrow \nu_e b \bar{b} \bar{q}$



7.97 fb at the LHeC

64.27 fb at the FCC-eh

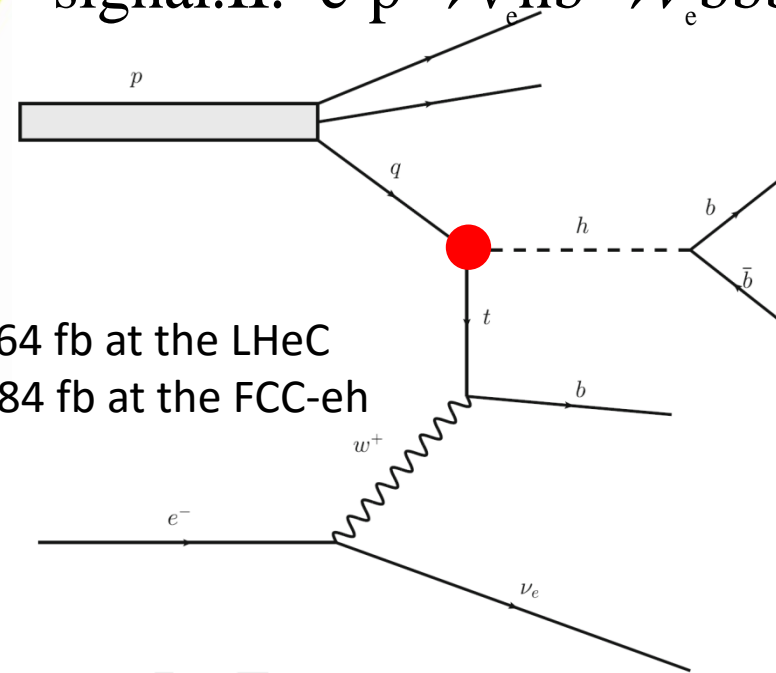
$$\mathcal{L}_{tqH} = \kappa_{\bar{t}uH} \bar{t}uH + \kappa_{\bar{t}cH} \bar{t}cH + \text{h.c.}$$

$$\kappa_{\bar{t}uH} = 0.1$$

$$p_T^{k_0} \geq 20 \text{ GeV}, \quad |\eta^{k_0}| < 10, \quad k_0 = j, b, \ell$$

$$\Delta R(k_1, k_2) > 0.01, \quad k_1 k_2 = jj, j\ell, jb, bb, b\ell$$

signal.II:  $e-p \rightarrow \nu_e h b \rightarrow \nu_e b \bar{b} b$



0.64 fb at the LHeC

3.084 fb at the FCC-eh

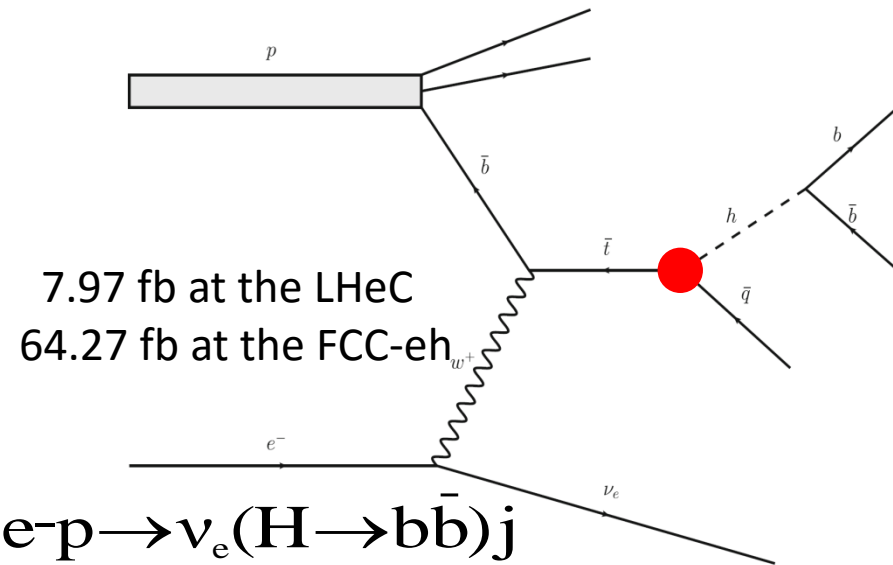
W.Liu, H.Sun, etc, Phys.Rev.D92(2015)7,074015

H.Sun, etc, Eur.Phys.J.C(2018)4,281



# Anomalous FCNC tqH couplings

signal.I:  $e p \rightarrow \nu_e \bar{t} \rightarrow \nu_e h \bar{q} \rightarrow \nu_e b \bar{b} \bar{q}$



$e p \rightarrow \nu_e (H \rightarrow b \bar{b}) j$

$e p \rightarrow \nu_e (Z \rightarrow b \bar{b}) j$

$e p \rightarrow \nu_e (g \rightarrow b \bar{b}) j$

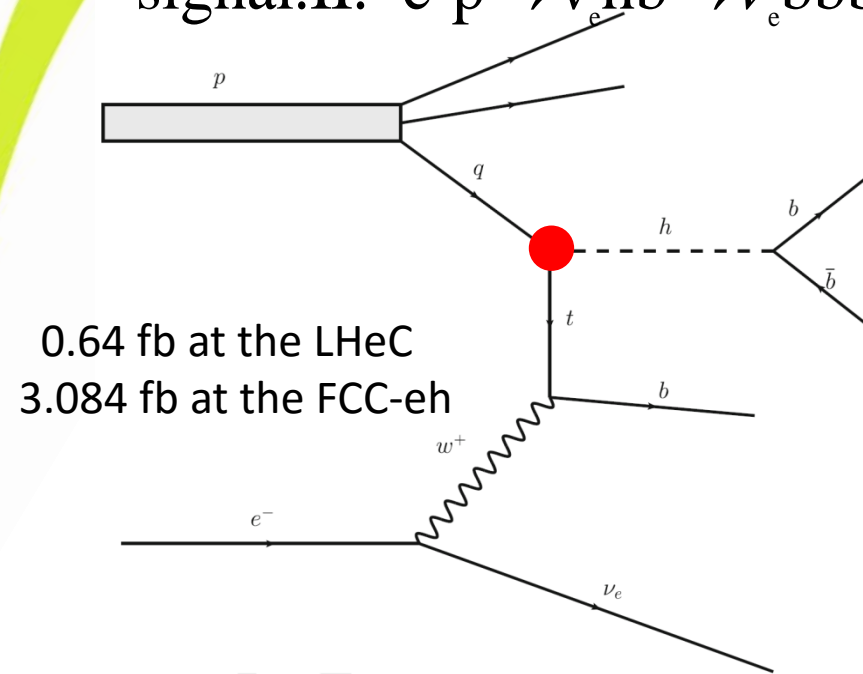
$e p \rightarrow \nu_e j j j$

$e p \rightarrow \nu_e j j b / \bar{b}$

$e p \rightarrow \nu_e \bar{t}$

$e p \rightarrow e^- (g \rightarrow b \bar{b}) j$

signal.II:  $e p \rightarrow \nu_e h b \rightarrow \nu_e b \bar{b} b$



Detector level study

W.Liu, H.Sun, etc, Phys.Rev.D92(2015)7,074015

H.Sun, etc, Eur.Phys.J.C(2018)4,281

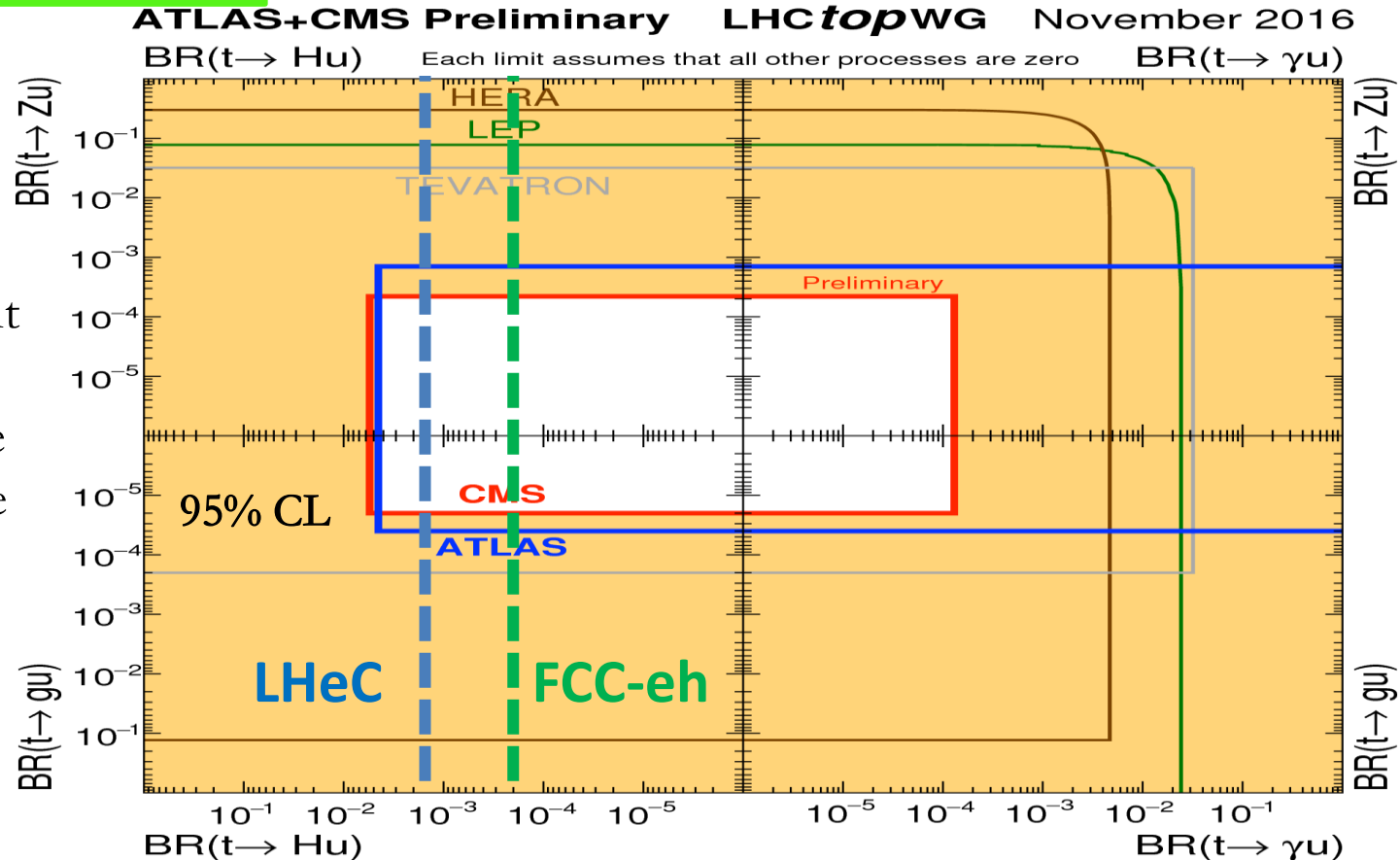
# Anomalous FCNC tqH couplings

$$\text{BR}(t \rightarrow uh)$$

$$\text{LHeC (1ab-1)} \quad 0.15 \times 10^{-2}$$

$$\text{FCC-eh (1ab-1)} \quad 0.22 \times 10^{-3}$$


Finally we found that the 2sigma upper limit on the Br of  $t \rightarrow hu$  is order of  $10^{-3}$  at the LHeC and  $10^{-4}$  at the FCC-eh.  
(all with  $L = 1\text{ab-1}$ )



Therefore we conclude that the potential to probe the FCNC tqH couplings can be much improved than the LHC experiments and even better than some theoretical sensitivities That obtained at the HL-LHC.

W.Liu, H.Sun, etc, Phys.Rev.D92(2015)7,074015

H.Sun, etc, Eur.Phys.J.C(2018)4,281

- 
- ep colliders and top production
  - selected topics in top sector
  - selected progress in top sector
    - FCNC  $tqH$
    - CKM element  $V_{tx}$
  - summary

# Current progress in $V_{td}/V_{ts}$ measurement

The conventional labeling for the flavor mixing matrix is

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

The standard model itself does not predict the elements of  $V$ , thus they should be evaluated experimentally.

Currently, the first two rows of  $V$  are already being probed with improving precision.

On the other hand, few direct measurement exist on the third row of  $V$

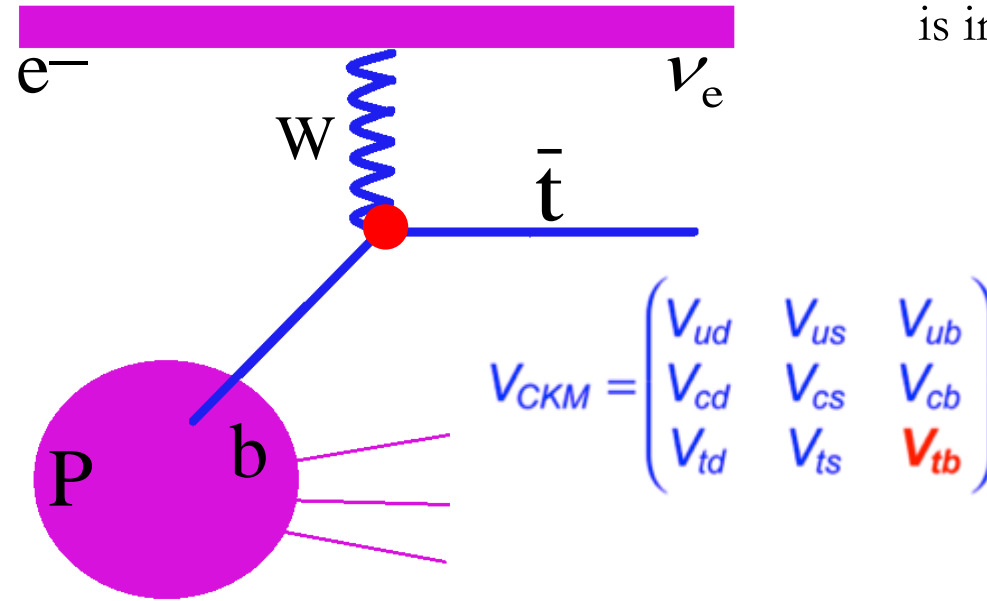
A global CKM fit

$$|V_{tb}| = 1 - 8.81_{-0.24}^{+0.12} \times 10^{-3}$$

$$|V_{ts}| = 41.08_{-5.7}^{+3.0} \times 10^{-3},$$

$$|V_{td}| = 8.575_{-0.098}^{+0.076} \times 10^{-3}.$$

# $V_{tb}$ measurement

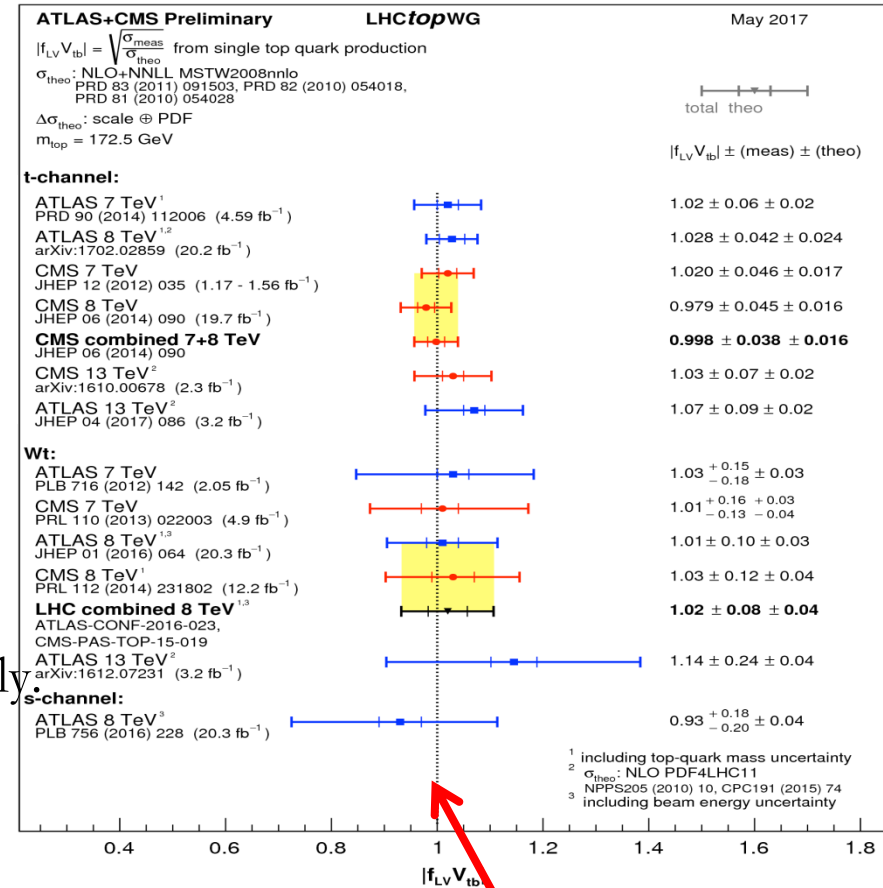


While at the ep projects, the CC single top production can be used to measure  $V_{tb}$  precisely



It was found that at the LHeC, with Luminosity of 100 fb<sup>-1</sup>, the CKM  $V_{tb}$  element can be measured with a precision of 1%.

The current way to precisely measure  $V_{tb}$  is in single top productions at the LHC.



LHeC, 100 fb<sup>-1</sup>  
1.000  $\pm$  0.01  
(expected)

# Current progress in $V_{td}/V_{ts}$ measurement

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

The remaining third row  
Element  $V_{td}$  and  $V_{ts}$  are  
very small.

At the LHC, difficult to measure  
 $t$  to  $d$  and  $t$  to  $s$  transitions.

At the ep colliders, the situation is much better:

1. the suppression of the top-pair background
2. the dominant CC single top signal production

We suggest to extract  $V_{td}$  and  $V_{ts}$  elements through single top  
related production at the ep colliders

# Current progress in $V_{td}/V_{ts}$ measurement

Lagrangian



FeynRules



MadGraph



Pythia



Delphes



ROOT-analysis

Here is our simulation chain.

For LHeC and FCC-he

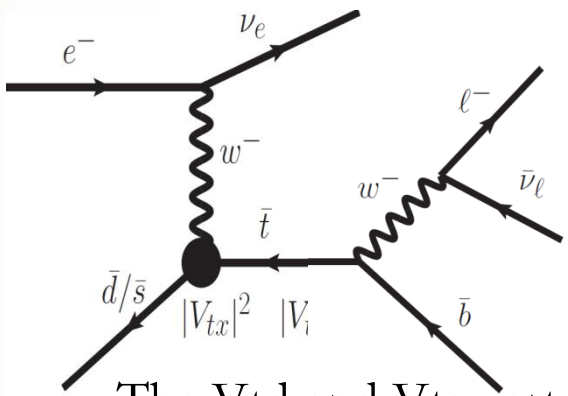


# Current progress in $V_{td}/V_{ts}$ measurement

We study the CKM vertex in four channels.

Signal.I:

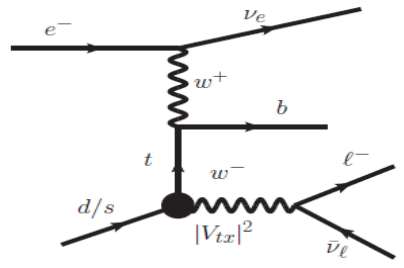
$$pe^- \rightarrow \nu_e \bar{t} \rightarrow \nu_e W^- \bar{b} \rightarrow \nu_e \ell^- \bar{\nu}_\ell \bar{b}$$



The  $V_{td}$  and  $V_{ts}$  vertex is induced here.

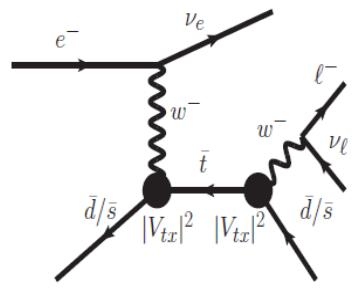
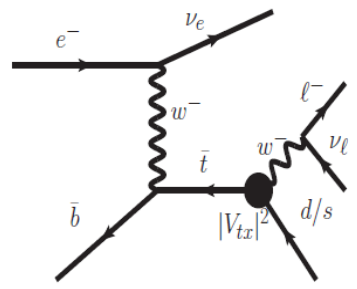
Signal.II:

$$pe^- \rightarrow \nu_e W^- \bar{b} \rightarrow \nu_e \ell^- \bar{\nu}_\ell \bar{b}$$



Signal.III:

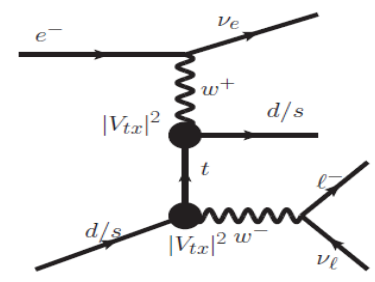
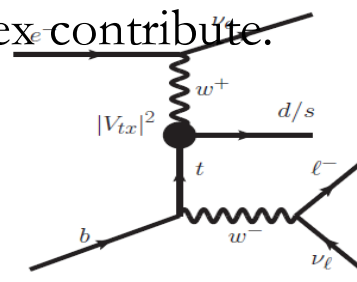
$$pe^- \rightarrow \nu_e \bar{t} \rightarrow \nu_e W^- j \rightarrow \nu_e \ell^- \bar{\nu}_\ell j$$



In this case we have two  $V_{tx}$  vertex contribute.

Signal.IV:

$$pe^- \rightarrow \nu_e W^- j \rightarrow \nu_e \ell^- \bar{\nu}_\ell j$$





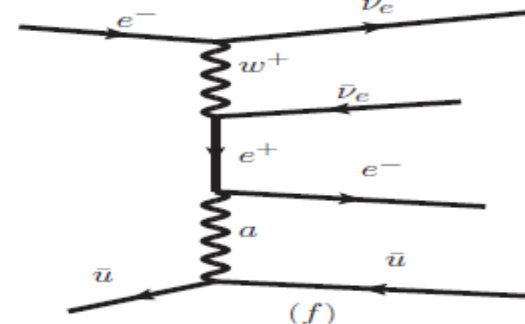
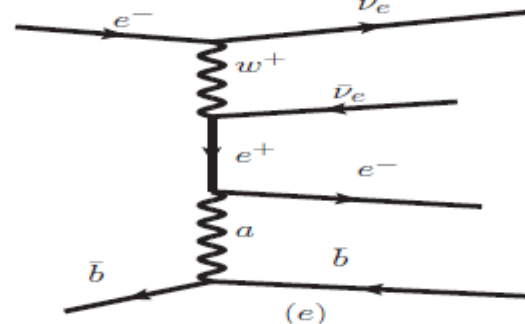
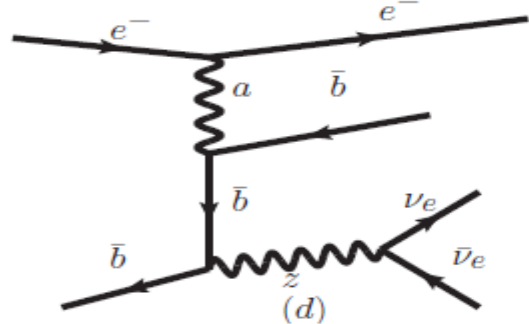
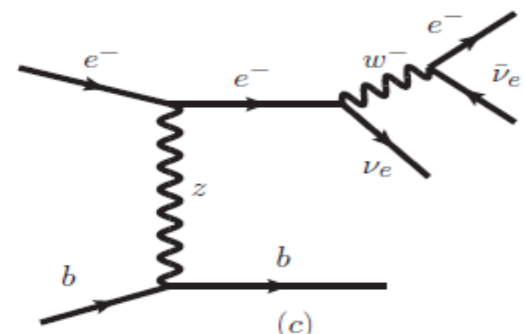
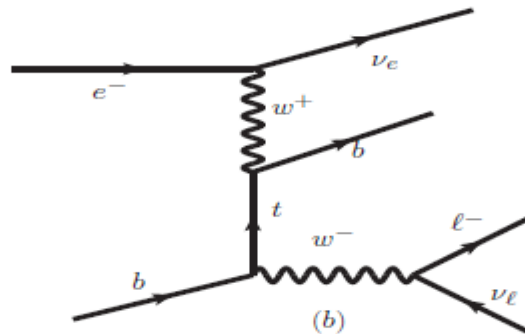
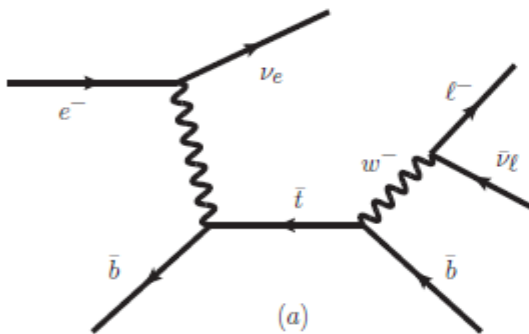
# Current progress in $V_{td}/V_{ts}$ measurement

B1:  $pe^- \rightarrow \nu_e \bar{t} \rightarrow \nu_e W^- \bar{b} \rightarrow \nu_e \ell^- \bar{\nu}_\ell \bar{b}$

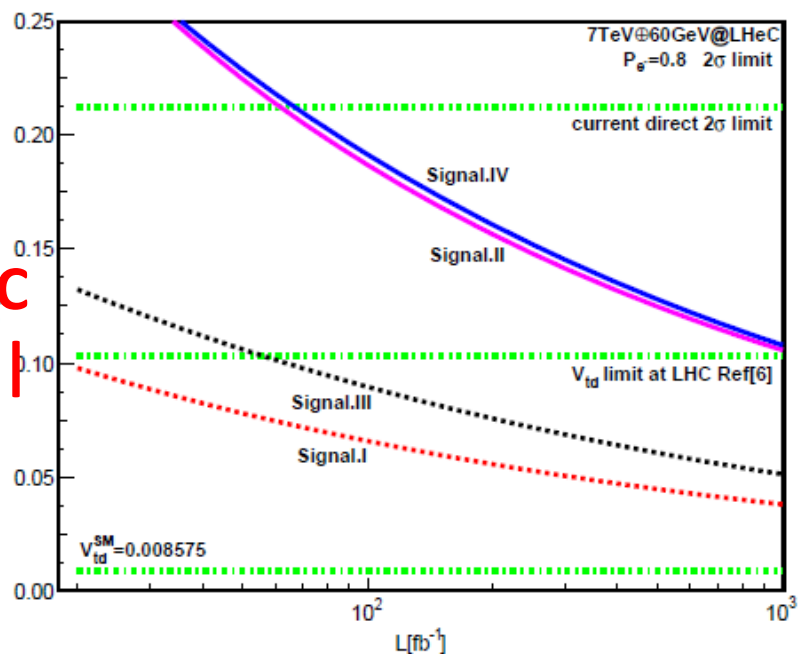
B2:  $pe^- \rightarrow \ell^- E_{T}^{\text{miss}} b/\bar{b}$

B3:  $pe^- \rightarrow \ell^- E_{T}^{\text{miss}} j$

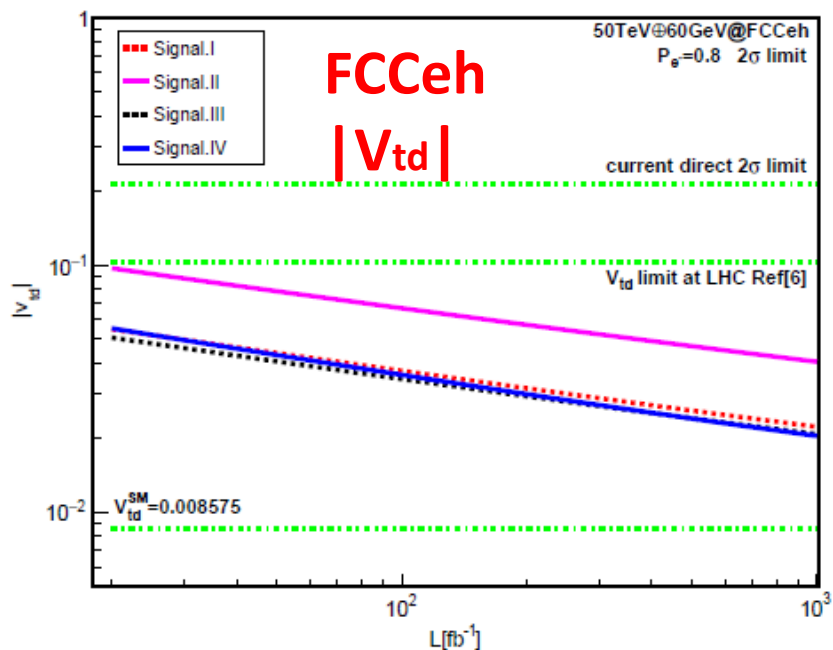
See last talk this morning.



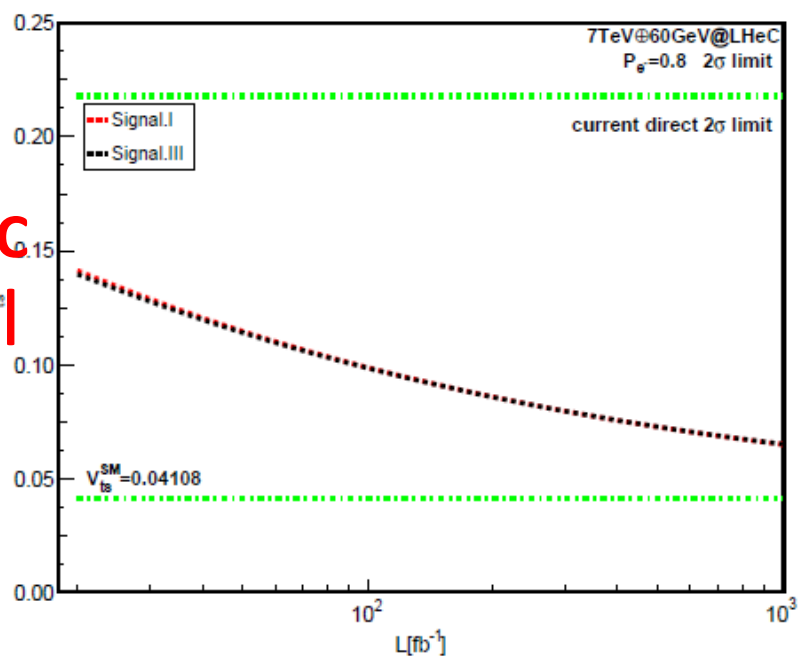
LHeC  
|V<sub>td</sub>|



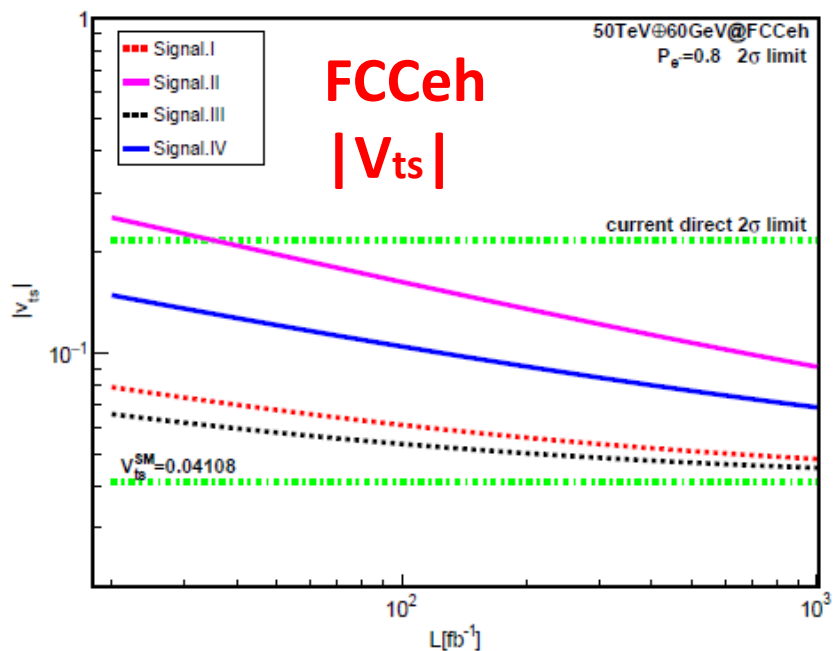
FCCeh  
|V<sub>td</sub>|



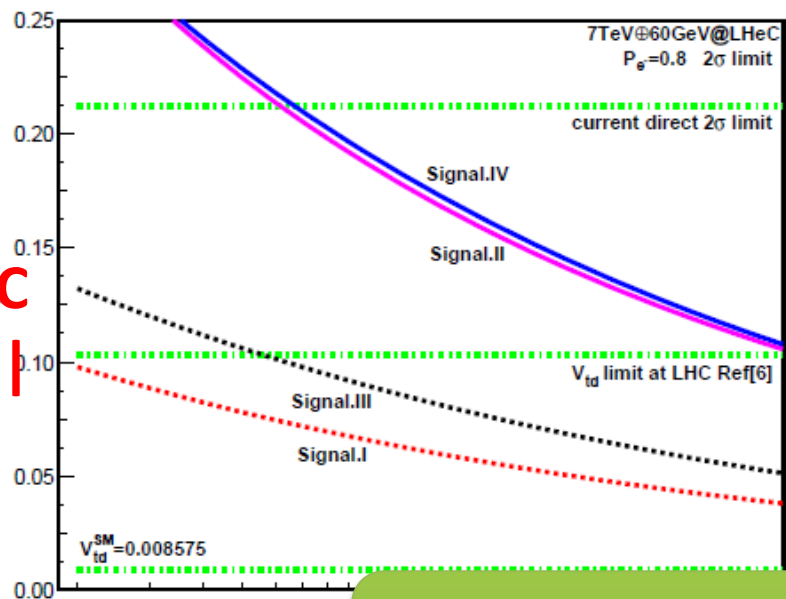
LHeC  
|V<sub>ts</sub>|



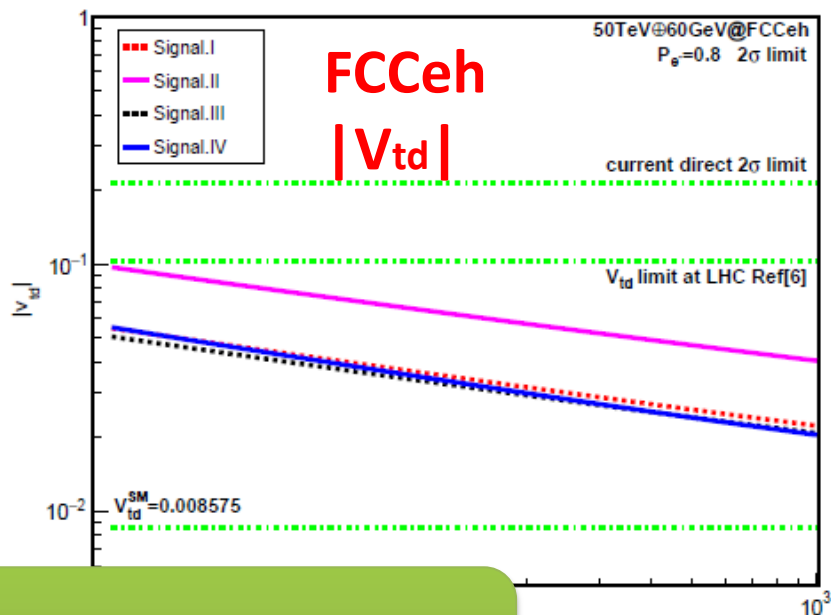
FCCeh  
|V<sub>ts</sub>|



LHeC  
 $|V_{td}|$

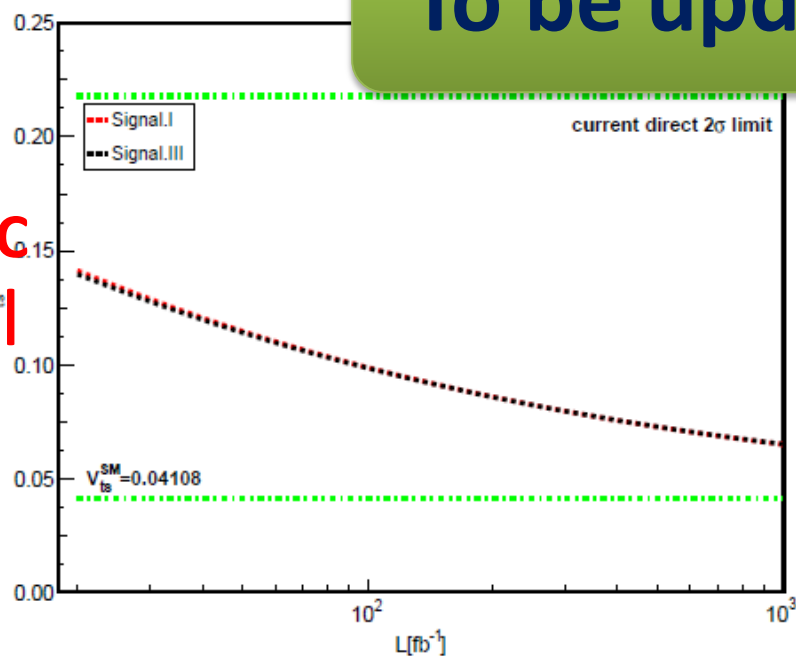


FCCeh  
 $|V_{td}|$

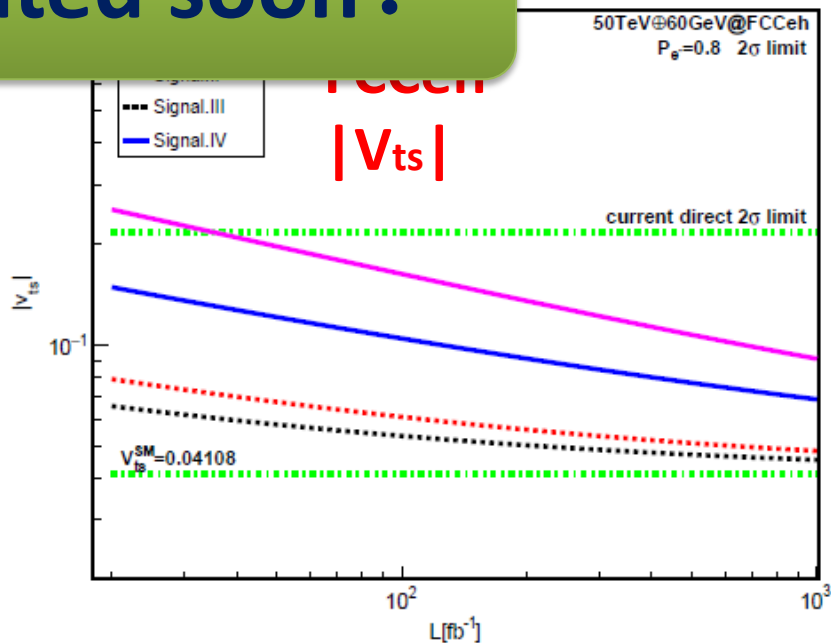


To be updated soon !

LHeC  
 $|V_{ts}|$



FCCeh  
 $|V_{ts}|$



# Summary



1. In this talk we present a short overview of the top physics at the ep collider.
2. Selected topics include, but not limited to:
  - top structure function
  - top PDFs, top spin polarization
  - $|V_{tb}|$ ,  $|V_{ts}|$ ,  $|V_{td}|$ , electric charge  $Q_t$  measurement
  - anomalous  $tt\gamma$ ,  $ttZ$ ,  $tbW$  couplings
  - FCNC  $tq\gamma$ ,  $tqZ$ ,  $tqH$  couplings
  - CP nature of  $ttH$  couplings
3. More studies in top sector are welcomed.

A stylized illustration of a bare tree on a hill with mountains in the background. The tree is dark and stands prominently on a small, rounded hill. The background features soft, hazy mountains and a sky with light, wispy clouds. The overall color palette is muted, with soft pinks, greys, and whites.

Thanks!