

# Study of Quarkonium and Quarkonium-like States at Belle

*Sen Jia*

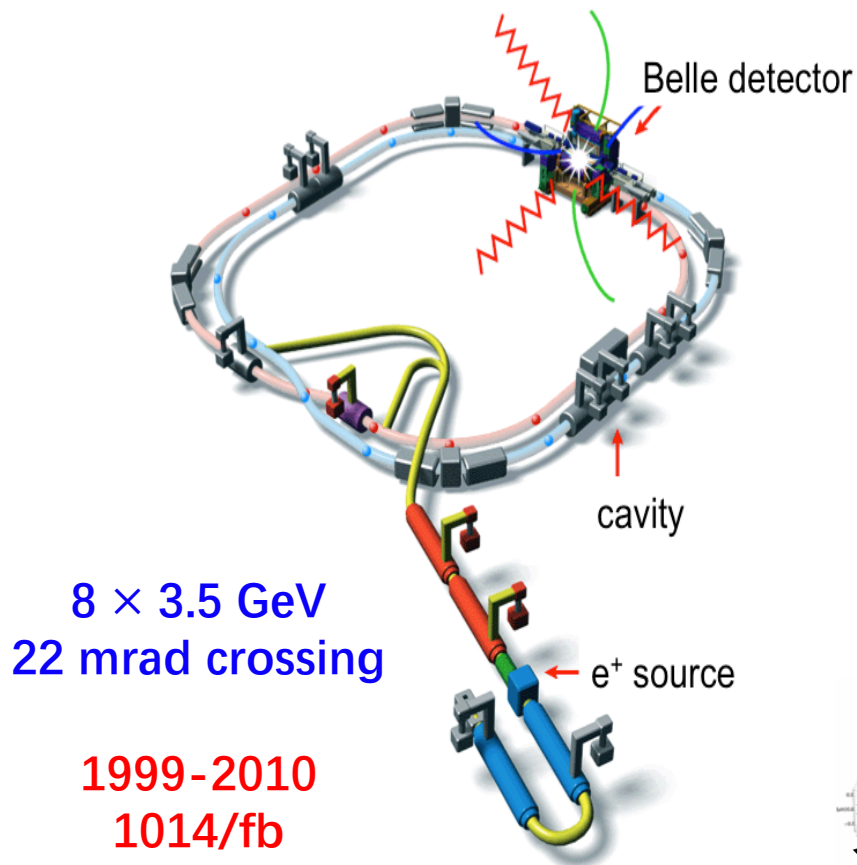
Beihang University  
(on behalf of the Belle Collaboration)

*DIS2018*  
*16-20 April 2018, Kobe, Japan*



# KEKB and Belle Detector

*KEK, Tsukuba, Japan*

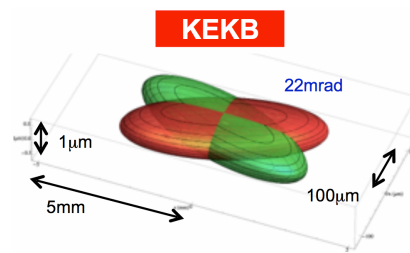
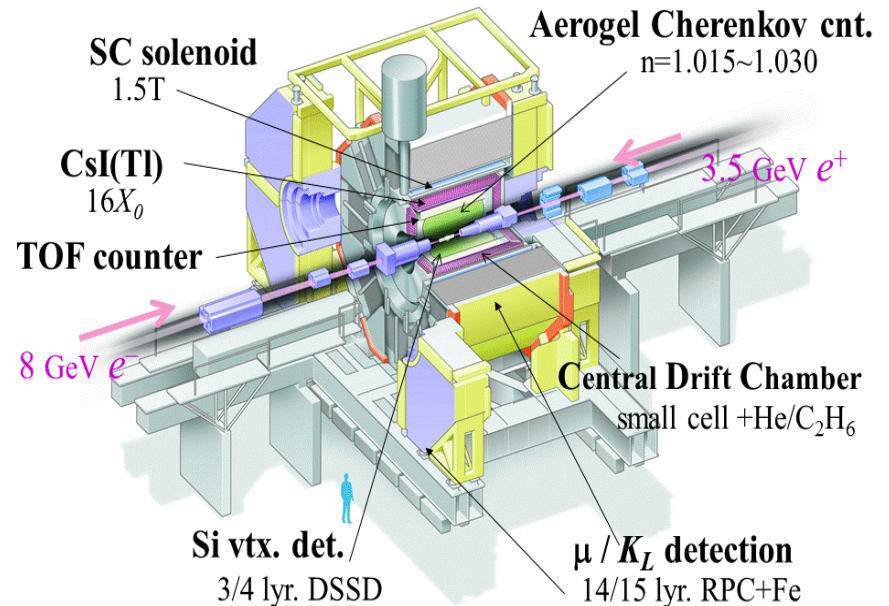


$8 \times 3.5 \text{ GeV}$   
22 mrad crossing

1999-2010  
1014/fb

The KEKB Collider

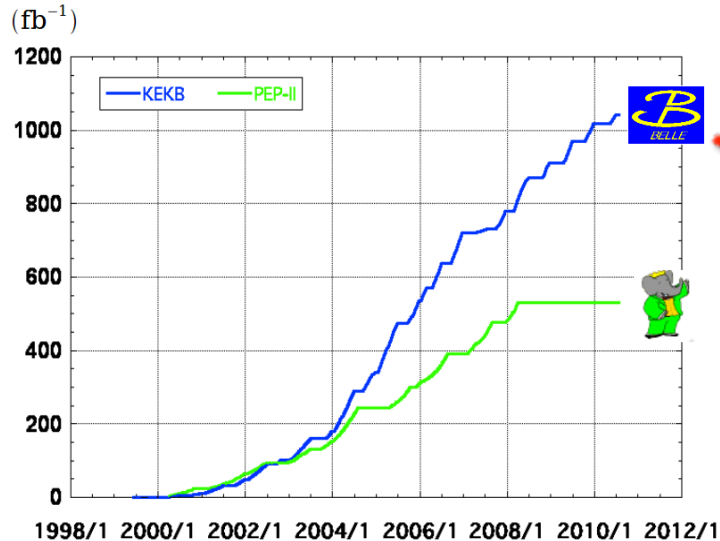
Belle Detector



World record:  
 $L=2.1 \times 10^{34} / \text{cm}^2 / \text{sec}$

# Data set at B-factories

## Integrated luminosity of B factories



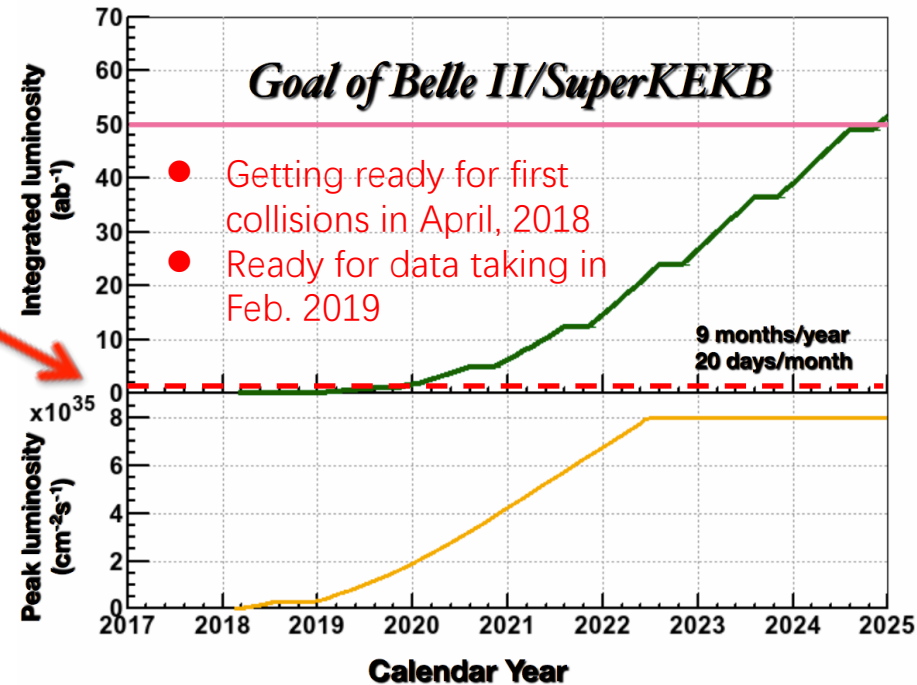
Expected data sample @ full luminosity

Channel	Belle	BaBar	Belle II (per year)
$B\bar{B}$	$7.7 \times 10^8$	$4.8 \times 10^8$	$1.1 \times 10^{10}$
$B_s^{(*)} \bar{B}_s^{(*)}$	$7.0 \times 10^6$	—	$6.0 \times 10^8$
$\Upsilon(1S)$	$1.0 \times 10^8$		$1.8 \times 10^{11}$
$\Upsilon(2S)$	$1.7 \times 10^8$	$0.9 \times 10^7$	$7.0 \times 10^{10}$
$\Upsilon(3S)$	$1.0 \times 10^7$	$1.0 \times 10^8$	$3.7 \times 10^{10}$
$\Upsilon(5S)$	$3.6 \times 10^7$	—	$3.0 \times 10^9$
$\tau\tau$	$1.0 \times 10^9$	$0.6 \times 10^9$	$1.0 \times 10^{10}$

\* assuming 100% running at each energy

**> 1  $\text{ab}^{-1}$**   
**On resonance:**  
 $\Upsilon(5S)$ : 121  $\text{fb}^{-1}$   
 $\Upsilon(4S)$ : 711  $\text{fb}^{-1}$   
 $\Upsilon(3S)$ : 3  $\text{fb}^{-1}$   
 $\Upsilon(2S)$ : 25  $\text{fb}^{-1}$   
 $\Upsilon(1S)$ : 6  $\text{fb}^{-1}$   
**Off reson./scan:**  
 $\sim 100 \text{ fb}^{-1}$

**$\sim 550 \text{ fb}^{-1}$**   
**On resonance:**  
 $\Upsilon(4S)$ : 433  $\text{fb}^{-1}$   
 $\Upsilon(3S)$ : 30  $\text{fb}^{-1}$   
 $\Upsilon(2S)$ : 14  $\text{fb}^{-1}$   
**Off resonance:**  
 $\sim 54 \text{ fb}^{-1}$



- Bottomonia below  $B\bar{B}$  threshold
- Bottomonium-like states above  $B\bar{B}$  threshold
- Initial State Radiation
- Two Photon Collisions
- Double Charmonium Production

# Content:

## *Study of Quarkonium at Belle*

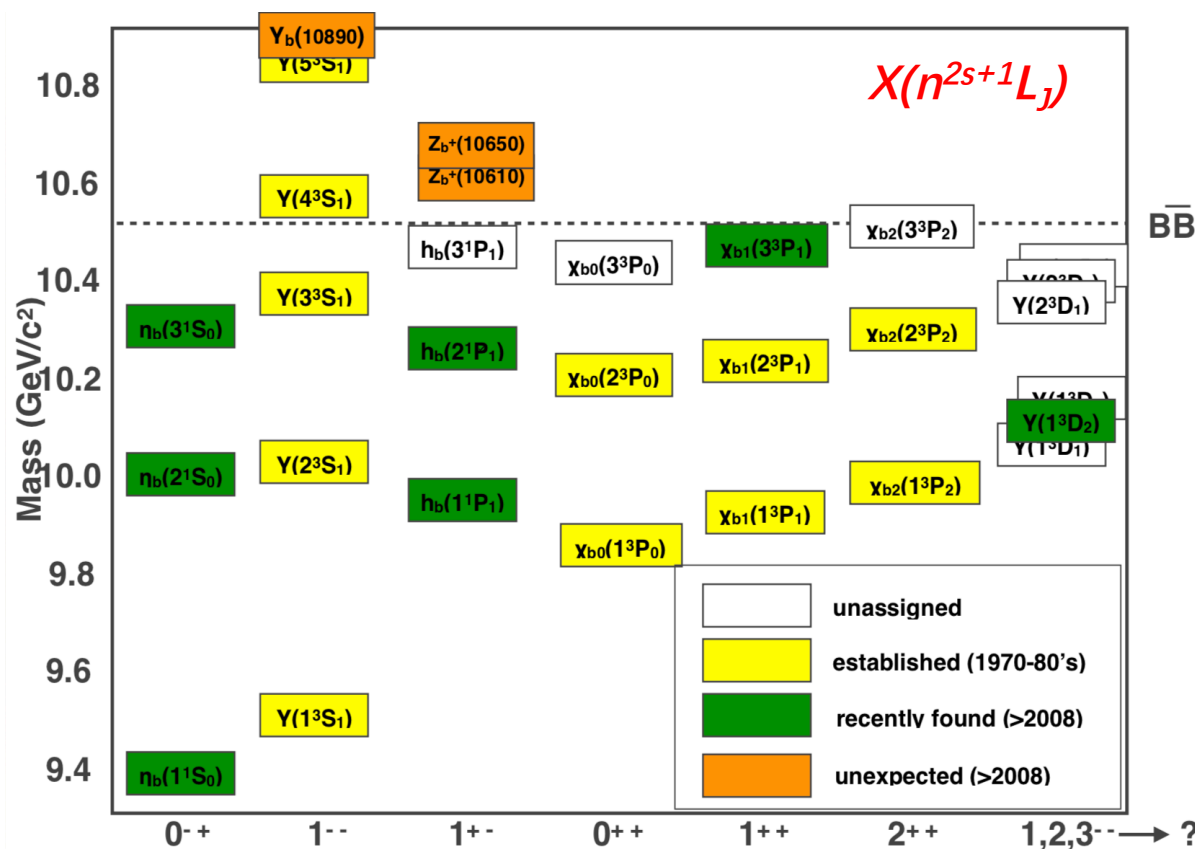
- Hadronic transitions in bottomonium
- A alternative  $\chi_{cJ}(nP)$  candidates in the  $D\bar{D}$  system
- Bottomonium inclusive decays

## *Study of Quarkonium-like states at Belle*

- Measurements of  $B^+ \rightarrow X_{c\bar{c}} K^+$
- Search for  $Y(4660)$  and its spin partner in  $B^+ \rightarrow K^+ \Lambda_c^+ \bar{\Lambda}_c^-$
- Double  $Z_c$  states production

# Bottomonium spectroscopy and Hadronic transitions

- Bottomonium spectroscopy was gradually developed in the past few decades.
- Important information on bottomonium is given by the study of transitions between its states.



Expectations:

- suppression of spin-flipping transitions  
(i.e.  $mS \rightarrow \eta \ nS$  wrt  $mS \rightarrow \pi^+\pi^- nS$ , and  $mS \rightarrow \pi^+\pi^- nP$  wrt  $mS \rightarrow \pi^+\pi^- nS$ )
- Further suppression of isospin-violating transitions  
(i.e.  $mS \rightarrow \pi^0 \ nS$  wrt others)

Experiment:

*PRD 78, 112002 (2008)*

$$\frac{\mathcal{B}(Y(4S) \rightarrow \eta Y(1S))}{\mathcal{B}(Y(4S) \rightarrow \pi^+\pi^- Y(1S))} = 2.41 \pm 0.40_{\text{stat}} \pm 0.12_{\text{syst}}$$

$$\frac{\mathcal{B}(Y(3S) \rightarrow \pi^0 h_b(1P))}{\mathcal{B}(Y(3S) \rightarrow \eta Y(1S))} > 8.6$$

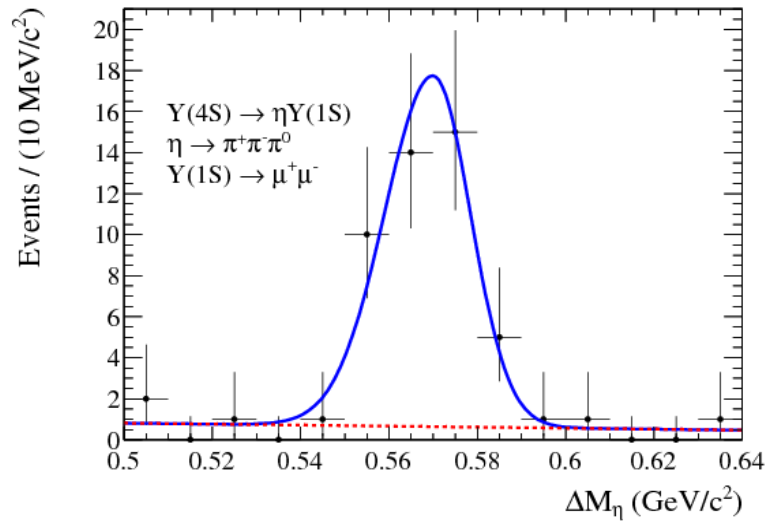
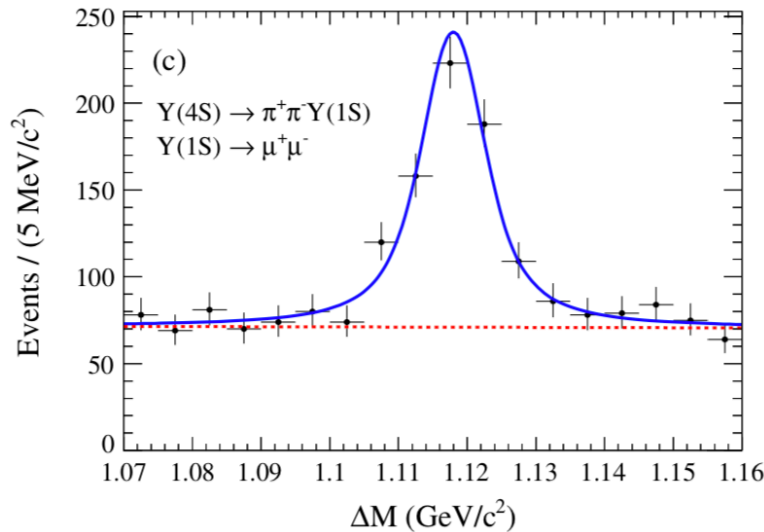
*PRD 84, 091101 (2011)*

# $\eta$ and dipion transitions in $\Upsilon(4S)$ decays

- $\eta \rightarrow \pi^+\pi^-\pi^0, \pi^0 \rightarrow \gamma\gamma, \Upsilon(1S) \rightarrow \mu^+\mu^-$

PRD 96, 052005 (2017)

- Fit to  $\Delta M = M(\pi\pi\mu\mu) - M(\mu\mu)$  and  $\Delta M_\eta = M(\pi\pi\gamma\gamma\mu\mu) - M(\mu\mu) - M(\pi\pi\gamma\gamma)$



Results

PRD 78, 112002 (2008)

BABAR

Belle

$$\mathcal{B}(\Upsilon(4S) \rightarrow \eta\Upsilon(1S))$$

$$1.90 \pm 0.26 \pm 0.09$$

$$1.70 \pm 0.23 \pm 0.08$$

$$\mathcal{R} = \frac{\mathcal{B}(\Upsilon(4S) \rightarrow \eta\Upsilon(1S))}{\mathcal{B}(\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(1S))}$$

$$2.41 \pm 0.40 \pm 0.12$$

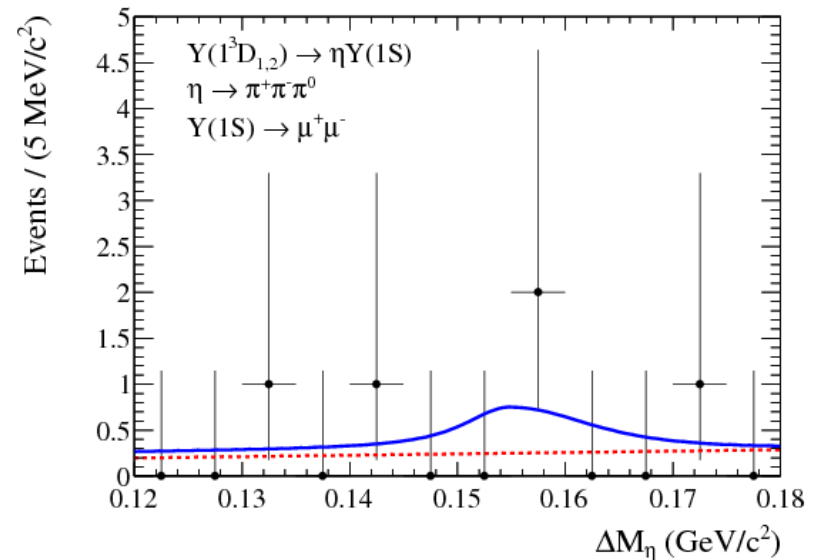
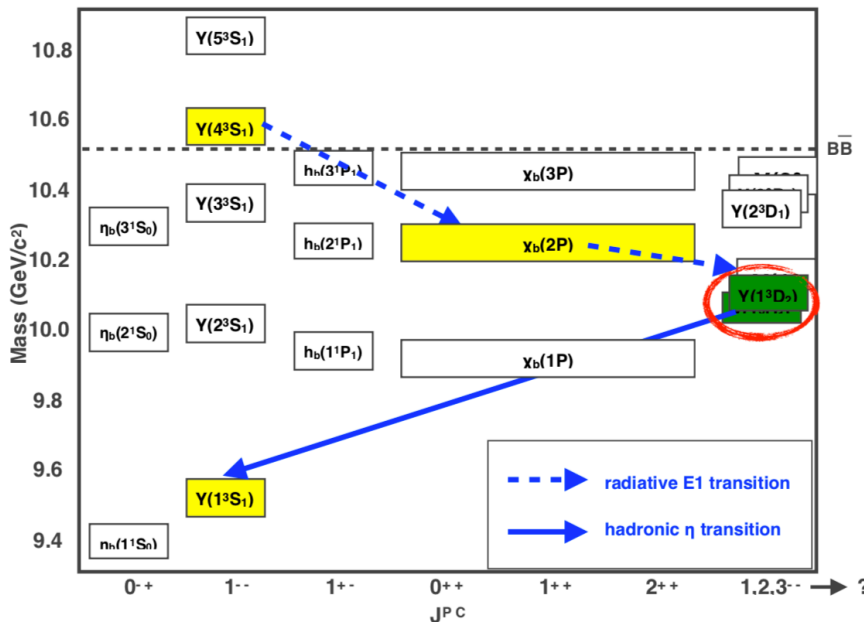
$$2.07 \pm 0.30 \pm 0.11$$

- Confirmation of the enhancement with respect to dipion transition

$$Y(1^3D_{1,2}) \rightarrow \eta Y(1S)$$

- With the same analysis method and similar event selections.
- Predicted to be enhanced with respect to the transition  $Y(1D) \rightarrow \pi\pi Y(1S)$  by the axial anomaly in QCD

*PLB 562, 68 (2003)*



- $Y(1D)$  possibly produced via double-radiative transitions from  $Y(4S)$  through  $\chi_{bJ}(2P)$  states

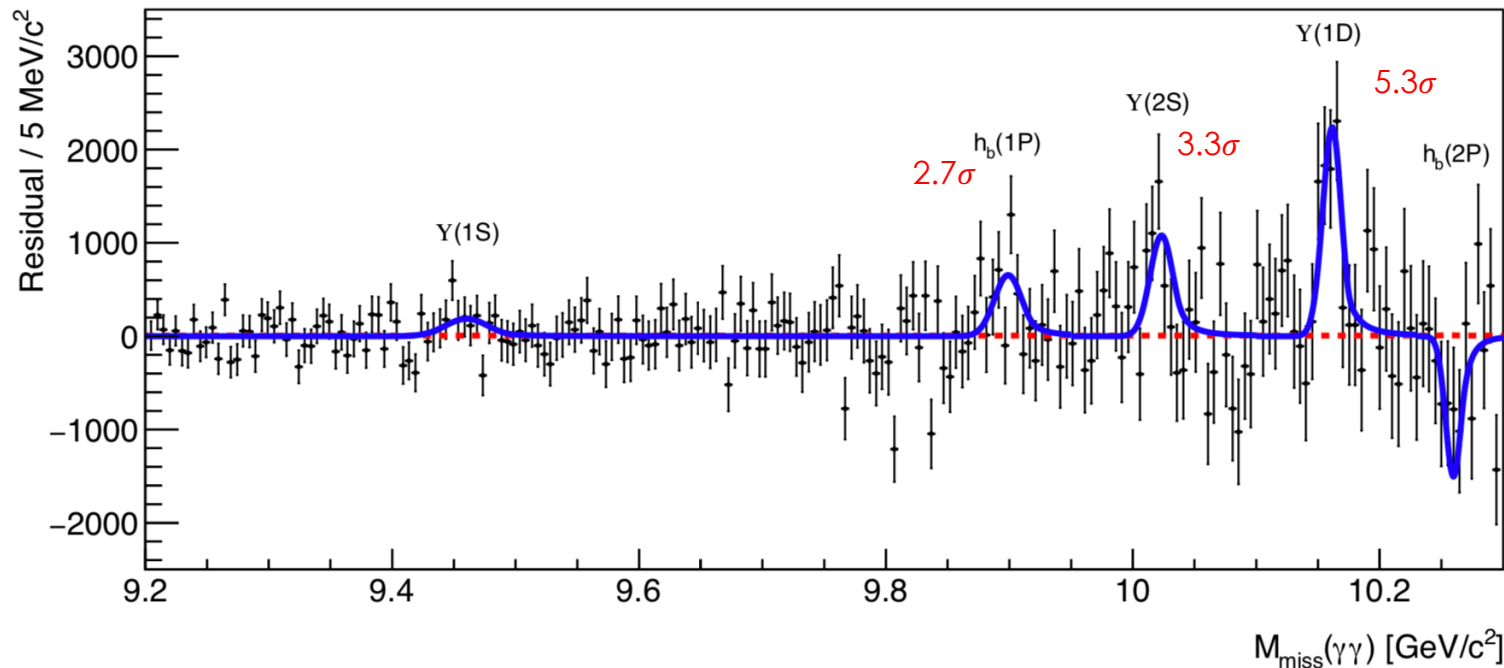
$$\mathcal{B}^{UL} \left( Y(4S) \rightarrow \gamma\gamma Y(1^3D_{1,2}) \right) \times \mathcal{B}^{UL} \left( Y(1^3D_{1,2}) \rightarrow \gamma Y(1S) \right) < 2.3 \times 10^{-5} \text{ at 90\% C. L.}$$



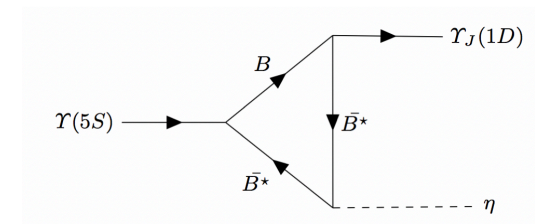
# $\eta$ transitions from $\Upsilon(5S)$

arXiv:1803.03225, submitted to EPJC

- After combinatorial background subtraction, the missing mass spectrum



- In particular,  $\mathcal{B}(\Upsilon(5S) \rightarrow \eta \Upsilon(1D))$  is compatible with the prediction (via hadronic loop mechanism) *PRD 94, 094039 (2016)*
- Observation of  $\Upsilon(5S) \rightarrow \eta \Upsilon_J(1D)$   
 $\sigma_v(\Upsilon(5S) \rightarrow \eta \Upsilon_J(1D)) = (1.14 \pm 0.22 \pm 0.15) \text{ [pb]}$   
 $\sigma_B(\Upsilon(5S) \rightarrow \eta \Upsilon_J(1D)) = (1.64 \pm 0.31 \pm 0.21) \text{ [pb]}$
- Not resolving the  $\Upsilon(1D)$  triplet (resolution  $\sim$  mass splitting)



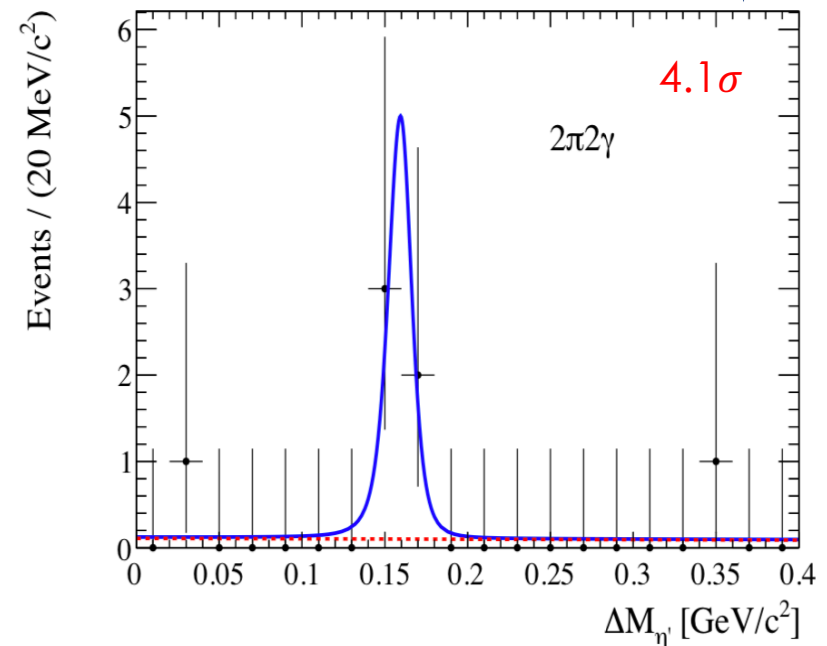
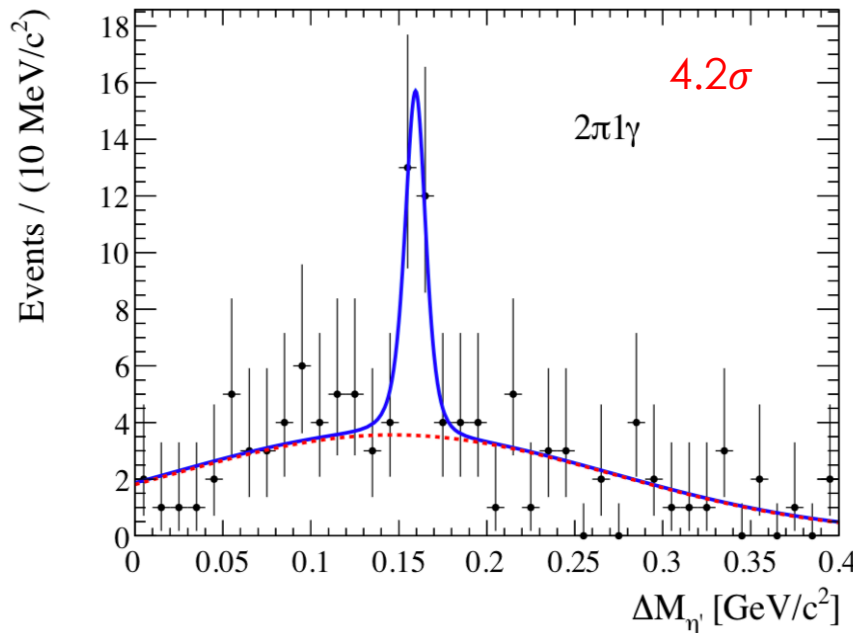


# First observation of $\Upsilon(4S) \rightarrow \eta' \Upsilon(1S)$

*arXiv:1803.10303, submitted to PRL*

- $\eta' \rightarrow \rho^0 \gamma$  ( $2\pi 1\gamma$ ),  $\eta' \rightarrow \pi\pi\eta$  ( $2\pi 2\gamma$ ),  $\Upsilon(1S) \rightarrow \mu^+ \mu^-$  *500th Belle paper*
- Fit to  $\Delta M_{\eta'} = M(\Upsilon(4S)) - M(\Upsilon(1S)) - M(\eta')$ , where  $M(\Upsilon(4S)) = M(\mu\mu\pi\pi\gamma)[M(\mu\mu\pi\pi\gamma\gamma)]$ ,  $M(\eta') = M(\pi\pi\gamma)[M(\pi\pi\gamma\gamma)]$  in the  $2\pi 1\gamma[2\pi 2\gamma]$ .

**New!**



- The statistical significance of combined measurement is  $5.8\sigma$

**BR**

**result**

$$\mathcal{B}(\Upsilon(4S) \rightarrow \eta' \Upsilon(1S)) / \mathcal{B}(\Upsilon(4S) \rightarrow \eta \Upsilon(1S)) = 0.20 \pm 0.06$$

$$\mathcal{B}(\Upsilon(4S) \rightarrow \eta' \Upsilon(1S)) / \mathcal{B}(\Upsilon(4S) \rightarrow \pi^+ \pi^- \Upsilon(1S)) = 0.42 \pm 0.11$$

Agree with the case of four-quark admixture in transitions

*MPLA 26, 773 (2011)*

# The history of $\chi_{c0}(2P)$ [ $\chi_{c2}(2P)$ ]

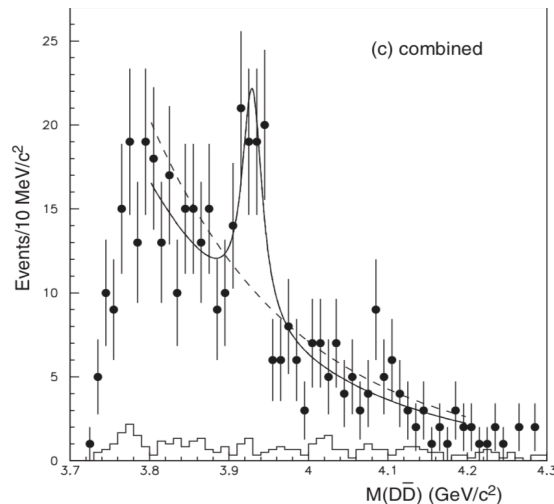
The  $\chi_{c0}(2P)$  [ $\chi_{c2}(2P)$ ] is expected to decay strongly to  $D\bar{D}$  in an S-wave.

A large width of  $\mathcal{T} \geq 100\text{MeV}$

*PRL 94, 182002 (2005)*

- The charmoniumlike state X(3915) was observed in  $B \rightarrow J/\psi \omega K$  decays
  - **But** this process ( $X(3915) \rightarrow J/\psi \omega$ ) belongs to Okubo-Zweig-Iizuka (OZI) suppression process
  - $\mathcal{T}$  of X(3915) ( $\sim 20\text{MeV}$ ) seems too small
  - X(3915) is no longer identified as the  $\chi_{c0}(2P)$  candidate in PDG 2016
- Possible  $\chi_{c2}(2P)$  candidates was observed in  $\gamma\gamma \rightarrow D\bar{D}$ . This charmonium state with  $M = (3838 \pm 12\text{MeV})$ ,  $\mathcal{T} = (211 \pm 19)\text{MeV}$

*PRL 96, 082003 (2006)*



In Ref.[*PRD 86, 091501(2012)*], the authors show that there is an indication of the  $\chi_{c0}(2P)$  with a mass around 3840 MeV and width of about 200 MeV.

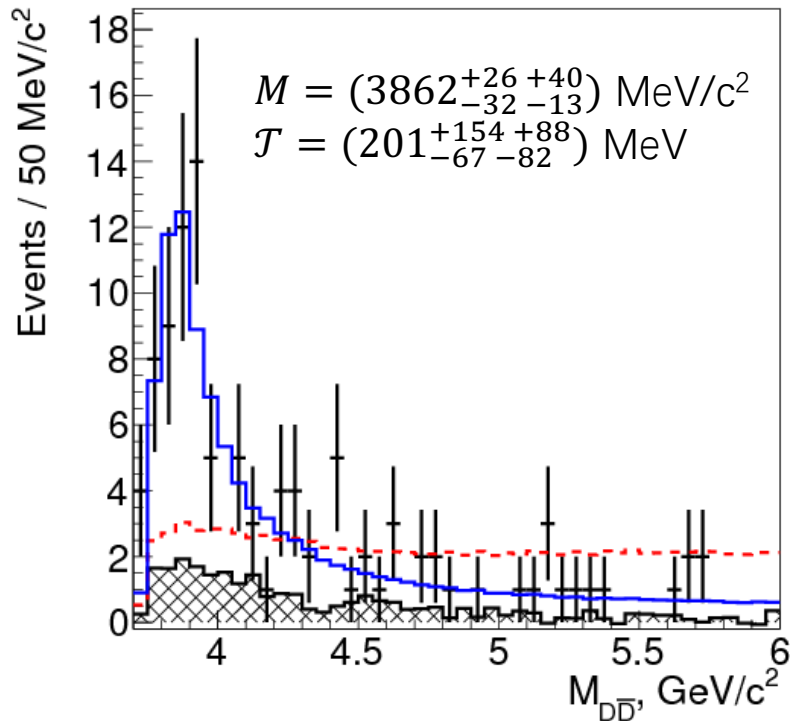
# An updated analysis of $e^+e^- \rightarrow J/\psi D\bar{D}$

PRD 95, 112003 (2017)

Compared to previous analysis of  $e^+e^- \rightarrow J/\psi D\bar{D}$  [*PRL* 100, 202001 (2008)]:

1. the integrated luminosity is **1.4 times** greater than before
2. apply **multivariate method** improve the discrimination of signal and background
3. **amplitude analysis** study the  $J^{PC}$  quantum numbers of the  $D\bar{D}$  system

*A alternative  $\chi_{c0}(2P)$  candidate*



- ◆ Points with error bars represent data
- ◆ The blue solid line is the fit results with **new resonance ( $J^{PC}=0^{++}$ )**
- ◆ The red dashed line is the fit with **nonresonant amplitude**
- ◆ The hatched histogram are the background

*A two-dimensional ( $M_{J/\psi}, M_{D\bar{D}}$ ) sideband as background*

Energy, GeV	$\sigma_{e^+e^- \rightarrow J/\psi X^*(3860)(\rightarrow D\bar{D})}^{(Born)}, \text{ (fb)}$
10.58	$21.7_{-4.3}^{+3.9} +_{-2.1}^{+2.9}$
10.87	$17.9_{-7.3}^{+7.2} +_{-1.8}^{+2.4}$

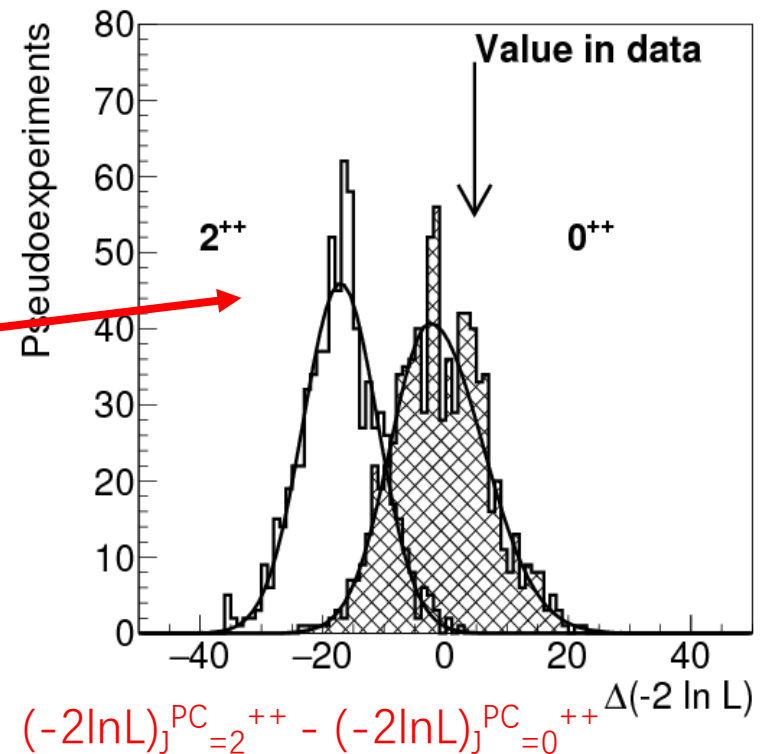
# Comparison of $J^{PC}$ hypotheses

- The X(3860) quantum-number hypotheses  $J^{PC}=0^{++}$  and  $2^{++}$  are compared using MC simulation.

PRD 95, 112003 (2017)

Default mode: a new resonance X(3860) in the  $D\bar{D}$  system with  $J^{PC}=0^{++}$  or  $2^{++}$  + nonresonant amplitude

Model	$2^{++}$ exclusion	$0^{++}$ C.L.
Default (constant nonresonant)	$3.8\sigma$	77%
NRQCD nonresonant	$3.4\sigma$	73%
$M_{D\bar{D}}^{-4}$ nonresonant	$3.6\sigma$	70%
Background mass calculation	$3.8\sigma$	75%
Optimization ( $a = 4$ )	$3.3\sigma$	69%
Optimization ( $a = 6$ )	$3.4\sigma$	64%
Free $r$	$2.5\sigma$	74%



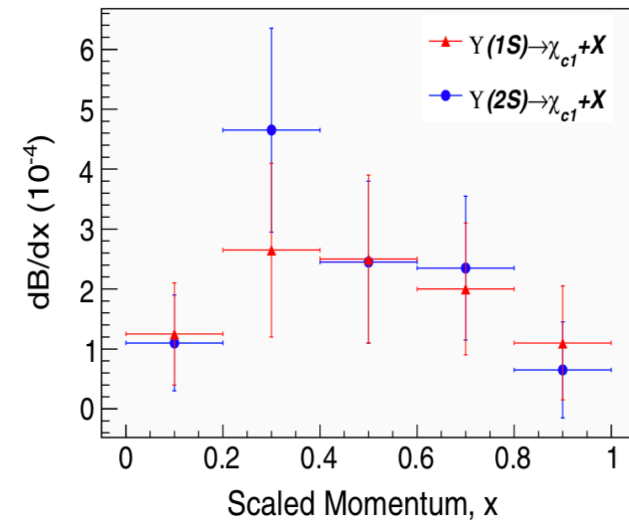
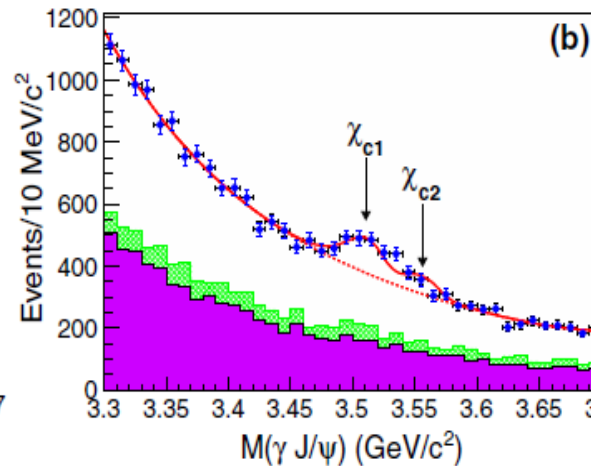
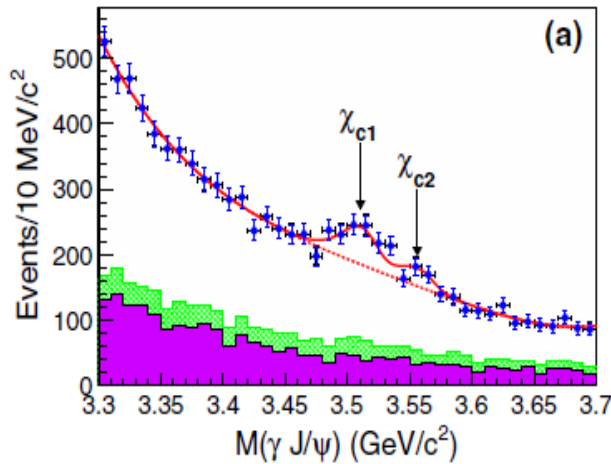
# $\chi_{c1}(1P)$ in $\Upsilon(1S, 2S)$ inclusive decays

PRD 95, 012001 (2017)

- Original aim: search for  $0^{--}$  glueballs in  $\Upsilon(1S, 2S) \rightarrow \chi_{c1} + G_{0^{--}}$
- Partition the data samples according to the scaled momentum to correct the efficiency

$$x = \frac{p_{\chi_{c1}}^*}{\frac{1}{2\sqrt{s}} \times (s - m_{\chi_{c1}}^2)}$$

The differential BR



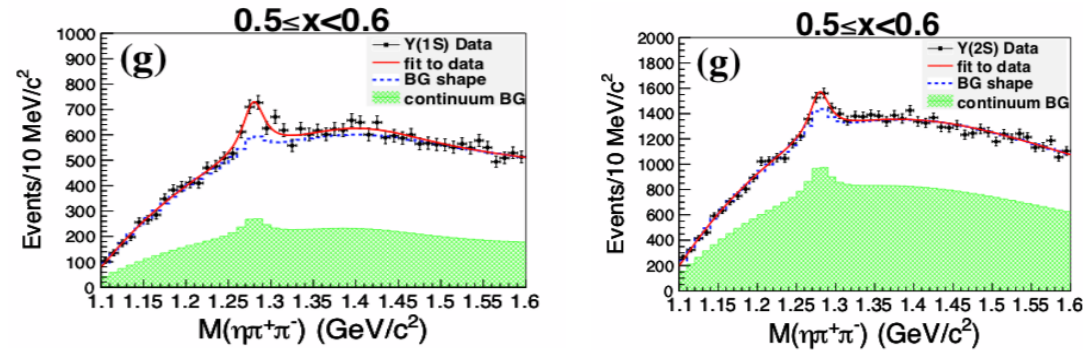
Mode	$BR(\times 10^{-4})$	Comments
$\Upsilon(1S) \rightarrow \chi_{c1} + \text{anything}$	$1.90 \pm 0.43 \pm 0.14$	<i>with an improved precision</i>
$\Upsilon(2S) \rightarrow \chi_{c1} + \text{anything}$	$2.24 \pm 0.44 \pm 0.20$	<i>for the first time</i>

# $\Upsilon(1S, 2S) \rightarrow f_1(1285) + X$ and $\chi_{bJ} \rightarrow J/\psi + X$

- Original aim: search for light tetraquarks in  $\Upsilon(1S, 2S) \rightarrow f_1(1285) + X_{\text{tetra}}$  and  $\chi_{bJ} \rightarrow J/\psi + X_{\text{tetra}}$

PRD 96, 112002 (2017)

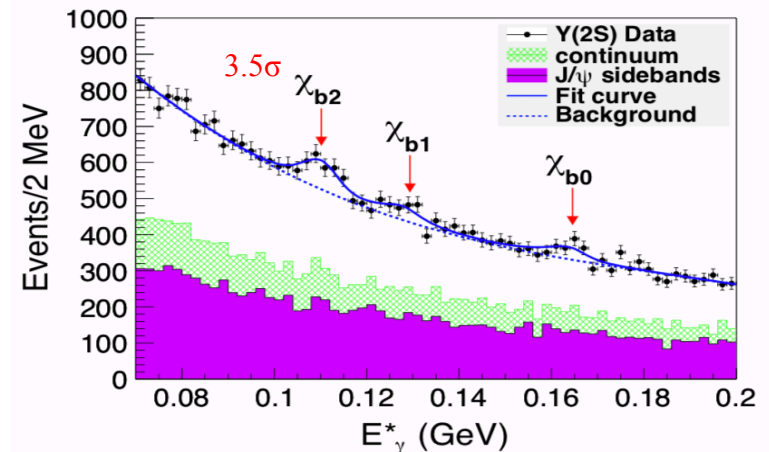
- Clear  $f_1(1285)$  signal in  $\Upsilon(1S, 2S)$  inclusive decays
- Partition the data samples according to the scaled momentum



Mode	$BR(\times 10^{-4})$
$\Upsilon(1S) \rightarrow f_1(1285) + \text{anything}$	$46 \pm 28 \pm 13$
$\Upsilon(2S) \rightarrow f_1(1285) + \text{anything}$	$22 \pm 15 \pm 6.3$

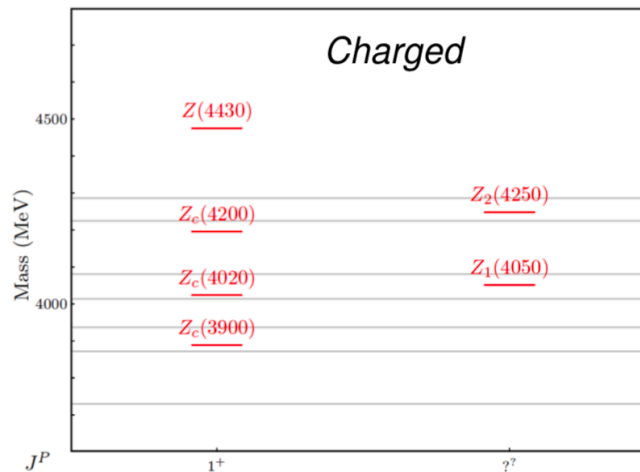
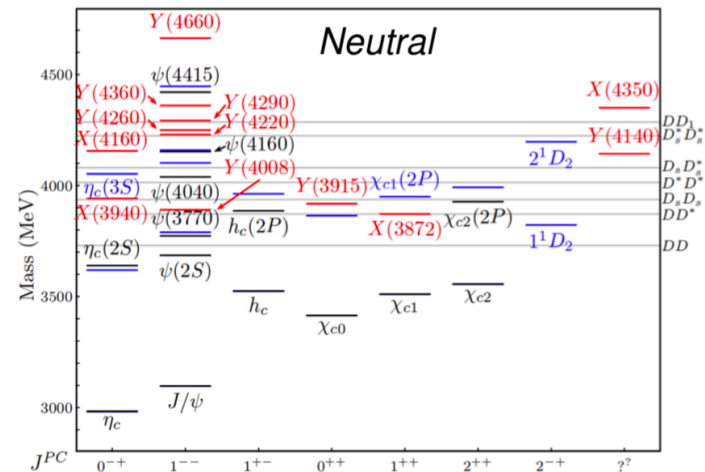
- $J/\psi$  production in  $\chi_{bJ}$  ( $J = 0, 1, 2$ ) decays

Mode	$BR(\times 10^{-3})$
$\chi_{b2} \rightarrow J/\psi + \text{anything}$	$1.5 \pm 0.34 \pm 0.22$
$\chi_{b1} \rightarrow J/\psi + \text{anything}$	1.1 at 90% C.L.
$\chi_{b0} \rightarrow J/\psi + \text{anything}$	2.3 at 90% C.L.



# Discovery of Charmonium-like and Bottomonium-like states

*In the last 10 years we saw an explosion of new states populating the quarkonium spectrum...*

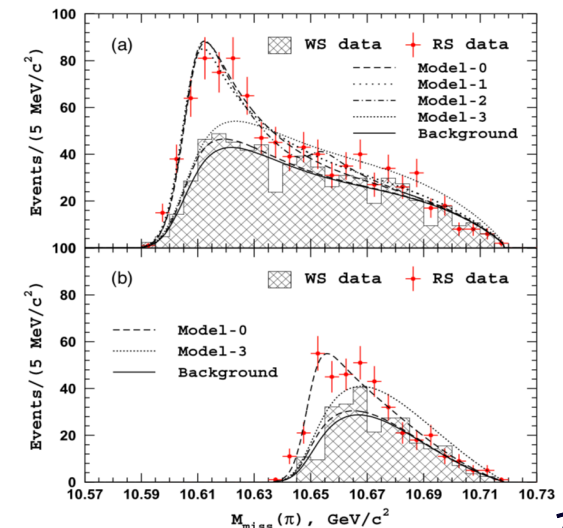


Many explanations

- Molecules
- Tetraquarks
- CUSP effect
- Rescattering
- Hybrids
- Hadroquarkonia

Bottomonium-like:  $Z_b$  states

State	Mode	Reference
$Z_b^\pm(10610)$	$\Upsilon(5S) \rightarrow h_b(mP) \pi^+ \pi^-$	PRL 108, 122001 (2012)
$Z_b^\pm(10650)$	$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^-$	PRL 116, 212001 (2016)
	$e^+ e^- \rightarrow \pi B^{(*)} \bar{B}^*$	
$Z_b^0(10610)$	$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^0 \pi^0$	PRD 88, 052016 (2013)





# Measurements of $B^+ \rightarrow X_{c\bar{c}} K^+$

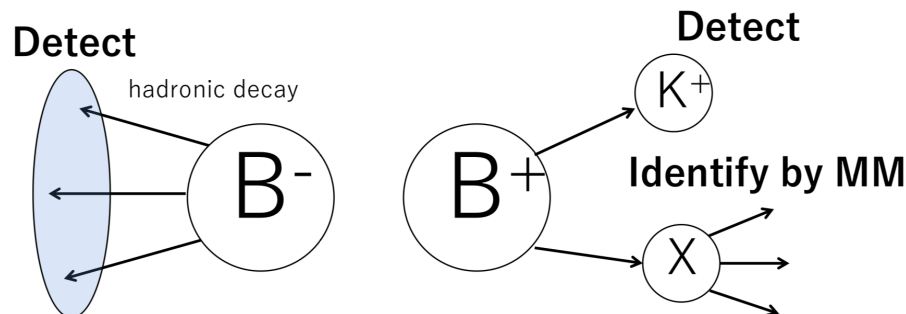
PRD 97, 012005 (2018)

- To determine absolute branching fraction  $\mathcal{B}(B^+ \rightarrow X(3872)K^+)$
- Simultaneously measure the  $\mathcal{B}(B^+ \rightarrow X_{c\bar{c}} K^+)$ , where  $X_{c\bar{c}}$  is  $\eta_c$ ,  $J/\psi$ ,  $\chi_{c0}$ ,  $\chi_{c1}$ ,  $\eta_c(2S)$ ,  $\psi(2S)$ ,  $\psi(3770)$

## Analysis method:

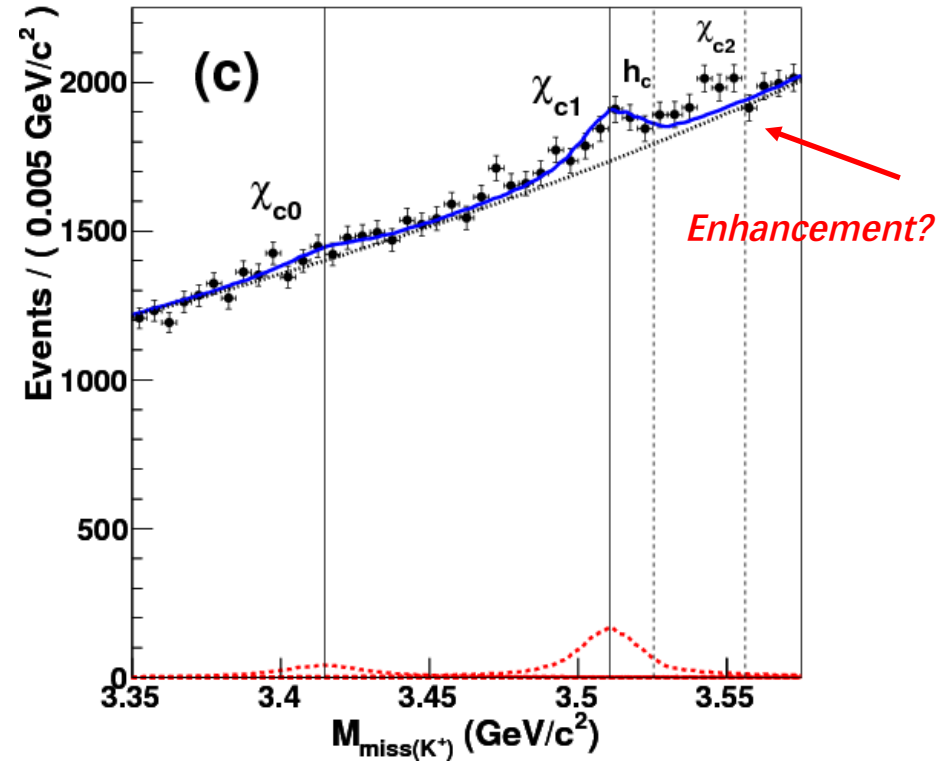
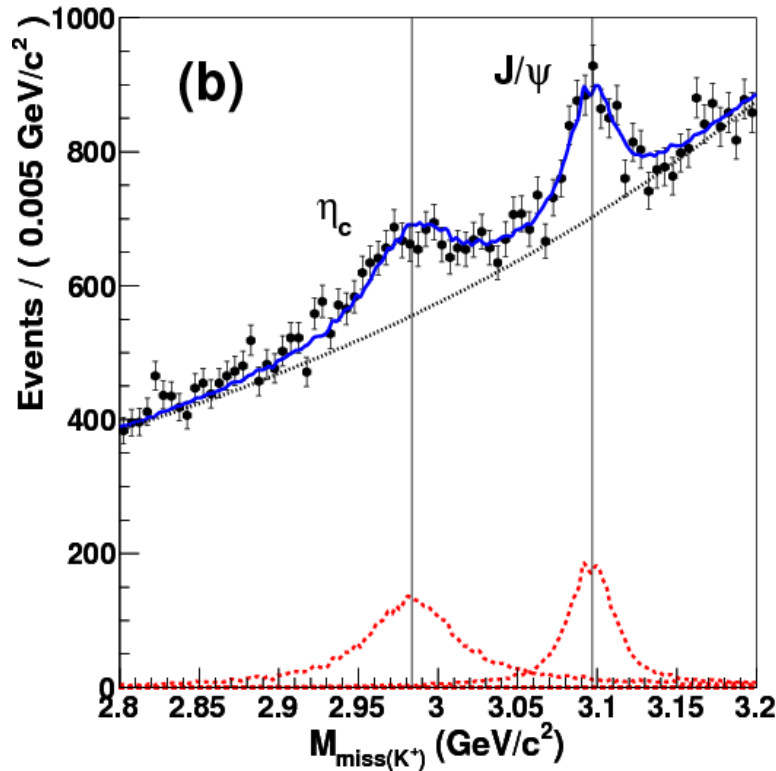
- Fully reconstruct one of the two charged B mesons ( $B_{\text{tag}}$ )
- NeuroBayes neural-network used to suppress continuum events
- Identify the signal as a peak at the nominal  $X_{c\bar{c}}$  mass in

$$M_{\text{miss}}(K^+) = \sqrt{(p_{e^+e^-}^* - p_{\text{tag}}^* - p_h^*)^2 / c}$$



# Measurements of $B^+ \rightarrow X_{c\bar{c}} K^+$

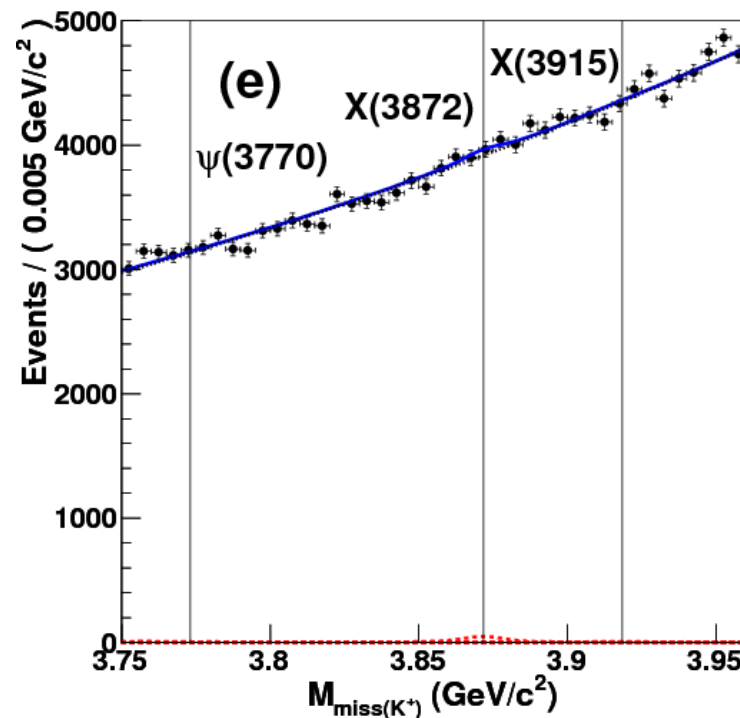
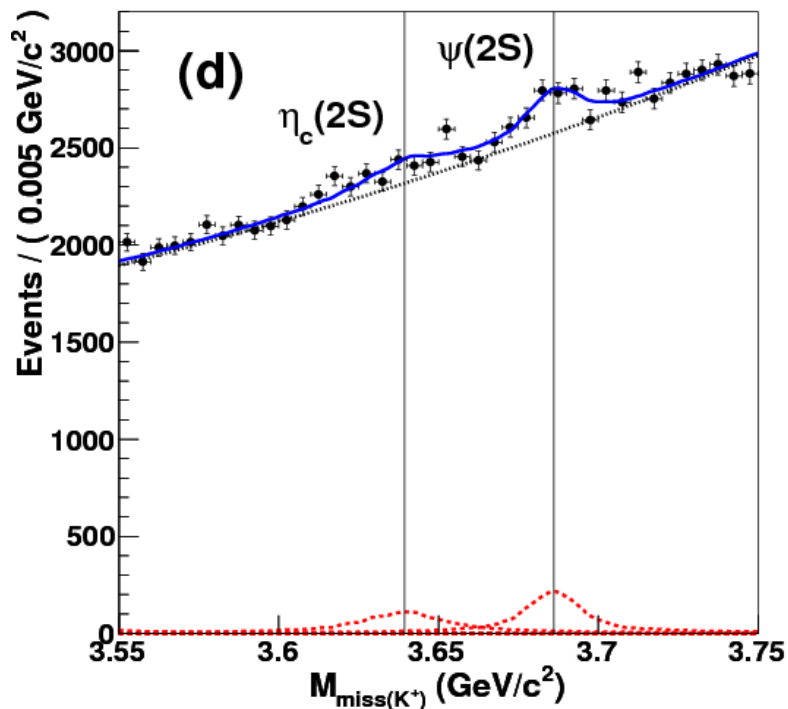
PRD 97, 012005 (2018)



Mode	Significance ( $\sigma$ )	$\mathcal{B}$ ( $10^{-4}$ )	PDG results for $\mathcal{B}$ ( $10^{-4}$ )	Comments
$\eta_c$	14.2	$12.3 \pm 0.8 \pm 0.7$	$9.6 \pm 1.1$	more precise
$J/\psi$	13.7	$9.1 \pm 0.7 \pm 0.5$	$10.26 \pm 0.031$	-
$\chi_{c0}$	2.2	$2.1 \pm 0.9 \pm 0.1$ ( $< 3.4$ )	$1.50^{+0.15}_{-0.14}$	
$\chi_{c1}$	6.8	$6.0 \pm 0.9 \pm 0.5$	$4.79 \pm 0.23$	

# Measurements of $B^+ \rightarrow X_{c\bar{c}} K^+$

PRD 97, 012005 (2018)

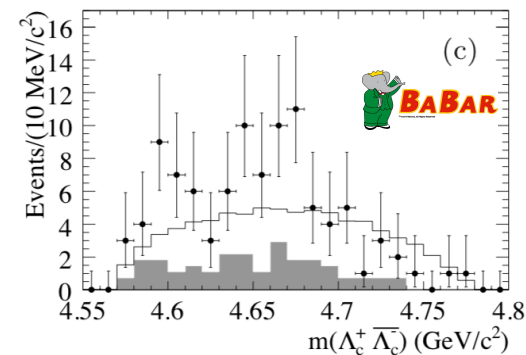
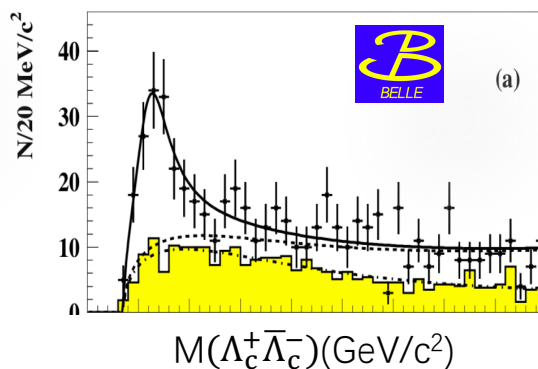
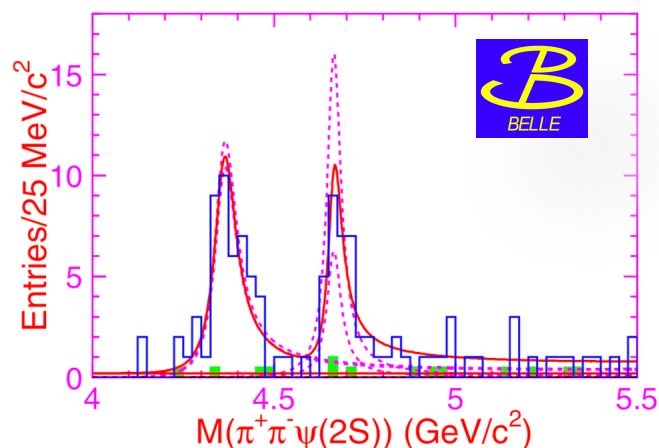


Mode	Significance ( $\sigma$ )	$\mathcal{B}$ ( $10^{-4}$ )	PDG results for $\mathcal{B}$ ( $10^{-4}$ )	Comments
$\eta_c(2S)$	4.1	$4.9 \pm 1.1 \pm 0.3$	$3.4 \pm 1.8$	First significant measurement
$\psi(2S)$	6.6	$6.6 \pm 1.0 \pm 0.4$	$6.26 \pm 0.24$	-
$\psi(3770)$	-	$-0.2 \pm 1.4 \pm 0.0$ ( $< 2.4$ )	$4.9 \pm 1.3$	
$X(3872)$	1.1	$1.2 \pm 1.1 \pm 0.1$ ( $< 2.7$ )	( $< 3.2$ )	From BABAR: $\sim 0.4\sigma$
$X(3915)$	0.3	$0.4 \pm 1.6 \pm 0.0$ ( $< 2.9$ )	-	Measurement for the first time

# Search for $Y(4660)$ and its spin partner in $B^+ \rightarrow K^+ \Lambda_c^+ \bar{\Lambda}_c^-$

EPJC 78, 252 (2018)

- Belle reported a structure, called  $X(4630)$ , in the  $\Lambda_c^+ \bar{\Lambda}_c^-$  invariant mass distribution in  $e^+e^- \rightarrow \gamma_{\text{ISR}} \Lambda_c^+ \bar{\Lambda}_c^-$  *PRL 101, 172001 (2008)*
- $Y(4660)$  is observed in the invariant-mass distribution of  $\pi^+ \pi^- \psi(2S)$  by Belle. *PRL 99, 142002 (2007)*
- BarBar once studied  $B^+ \rightarrow K^+ \Lambda_c^+ \bar{\Lambda}_c^-$  and found two small peaks in  $M_{\Lambda_c^+ \bar{\Lambda}_c^-}$  spectrum. Larger data is needed to verify them. *PRD 101, 172001 (2008)*
- Some theory explained that  $Y(4660)$  has a large partial decay width to  $\Lambda_c^+ \bar{\Lambda}_c^-$  and its isospin partner  $Y_\eta$  is also predicted. *PRD 82, 094008 (2010), PRL 102, 242004 (2009)*

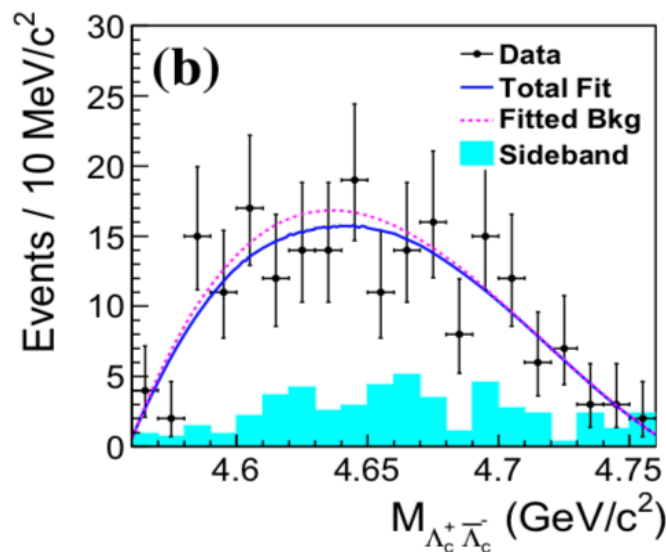
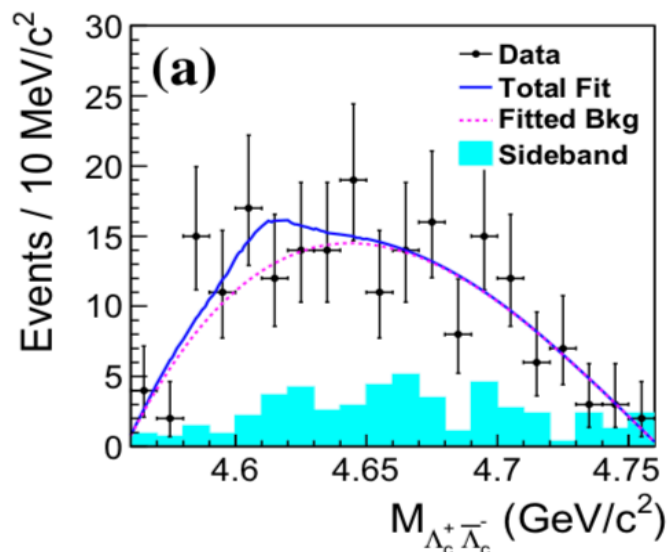


# Search for $Y(4660)$ and its spin partner in $B^+ \rightarrow K^+ \Lambda_c^+ \bar{\Lambda}_c^-$

- $\Lambda_c^+ \rightarrow pK^-\pi^+, pK_S^0, \Lambda\pi^+, pK_S^0\pi^+\pi^-, \Lambda\pi^+\pi^+\pi^-$  *EPJC 78, 252 (2018)*
- At least a  $\Lambda_c^+(\bar{\Lambda}_c^-)$  candidate that decays to  $pK^-\pi^+(\bar{p}K^+\pi^-)$  in combination of  $\Lambda_c^+\bar{\Lambda}_c^-$
- One B signal candidate with minimum  $\chi_{vertex}^2$  in an event

Fit with  $Y_\eta$  signal included

Fit with  $Y(4660)$  signal included



Mode	Upper limits of product $BR$ at 90% C.L.
$B^+ \rightarrow K^+ Y(4660) \rightarrow K^+ \Lambda_c^+ \bar{\Lambda}_c^-$	$1.2 \times 10^{-4}$
$B^+ \rightarrow K^+ Y_\eta \rightarrow K^+ \Lambda_c^+ \bar{\Lambda}_c^-$	$2.0 \times 10^{-4}$

# Search for $\Upsilon(1S, 2S) \rightarrow Z_c^+ Z_c^{(\prime)-}$ and $e^+ e^- \rightarrow Z_c^+ Z_c^{(\prime)-}$ at $\sqrt{s} = 10.52, 10.58$ , and $10.867$ GeV

- The interpretations for  $Z_c$  states are ambiguous, including tetraquarks, molecules, hybrids, or hadrocharmonia, etc.

For  $e^+ e^- \rightarrow Z_c^+ Z_c^-$

*PLB 764, 174 (2017)*  
*PRD 91, 114025(2015)*

$$F_{Z_c^+ Z_c^-} \sim \frac{1}{s^3}$$

tetraquark structure

$$F_{Z_c^+ Z_c^-} \sim \frac{1}{s}$$

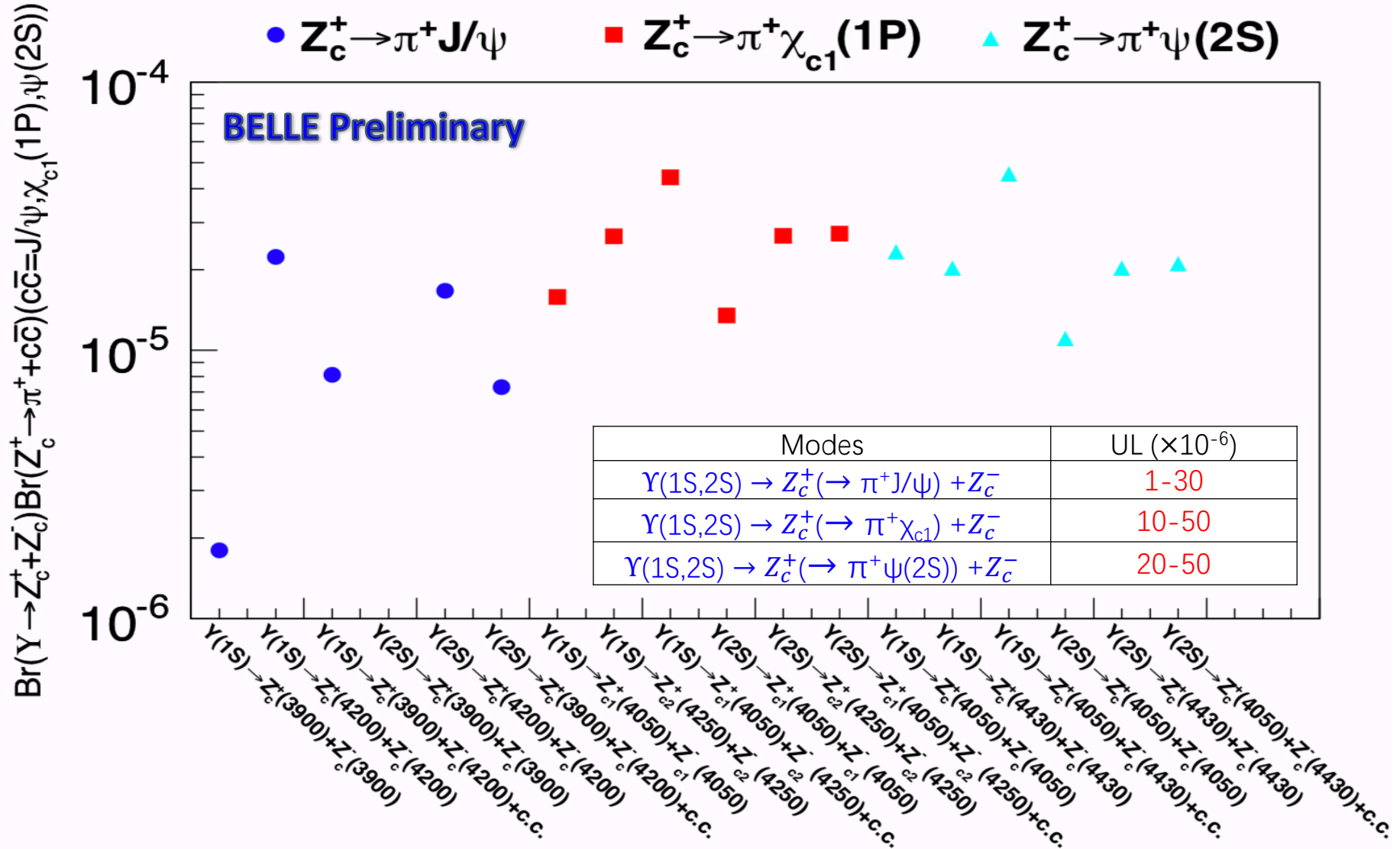
two tightly bound diquarks

- In this analysis, the below modes are included

States	Studied channels
$Z_c(3900)/Z_c(4200) \rightarrow \pi^+ J/\psi$	$\Upsilon(1S, 2S) / e^+ e^- \rightarrow Z_c(3900) + Z_c(3900), Z_c(4200)/Z_c(4200), Z_c(3900)/Z_c(4200)$
$Z_{c1}(4050)/Z_{c2}(4250) \rightarrow \pi^+ \chi_{c1}$	$\Upsilon(1S, 2S) / e^+ e^- \rightarrow Z_{c1}(4050) + Z_{c2}(4250), Z_{c1}(4250) + Z_{c2}(4250), Z_{c1}(4050) + Z_{c2}(4250)$
$Z_c(4050)/Z_c(4430) \rightarrow \pi^+ \psi(2S)$	$\Upsilon(1S, 2S) / e^+ e^- \rightarrow Z_c(4050) + Z_c(4430), Z_c(4050) + Z_c(4430), Z_c(4050) + Z_c(4430)$

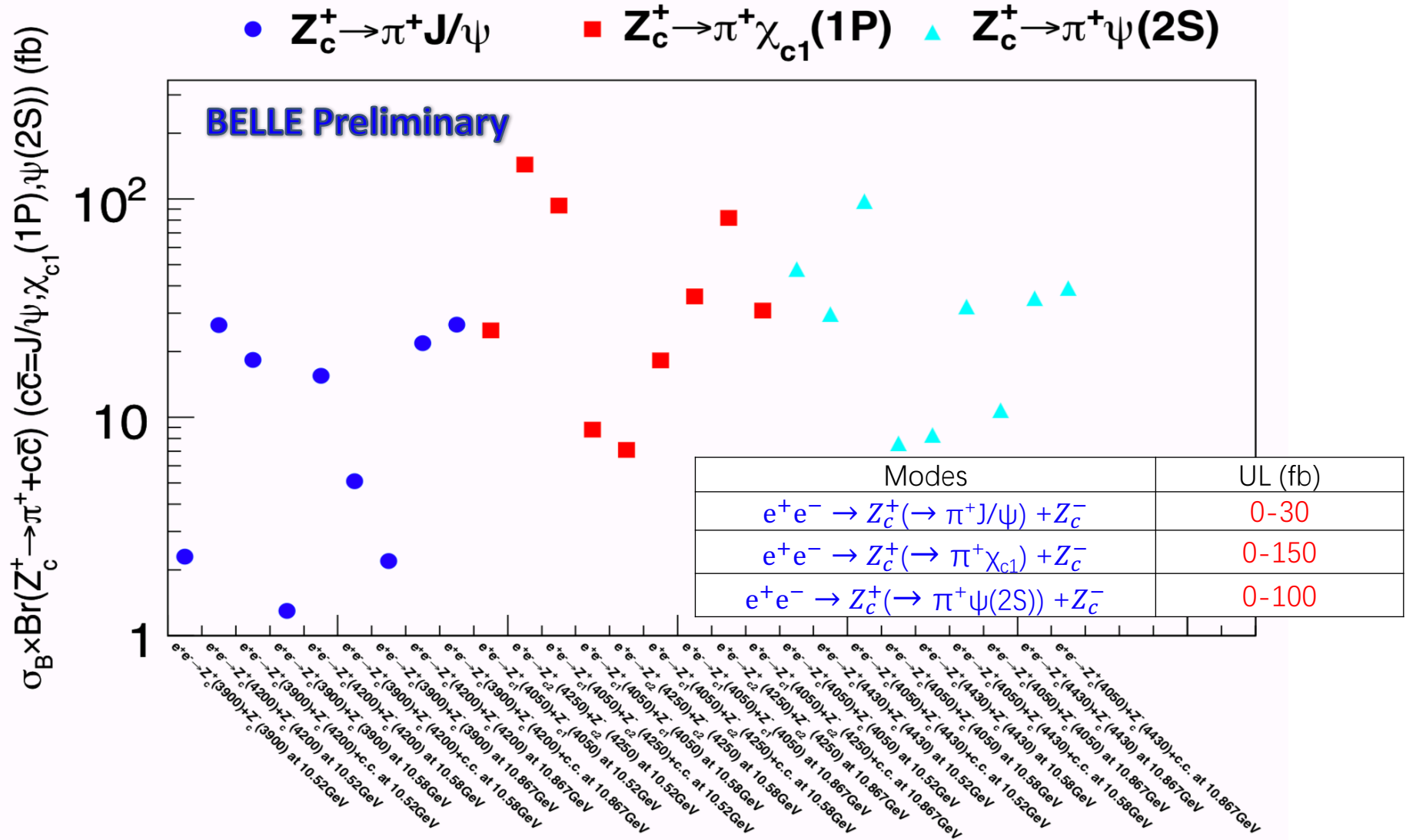
- For the  $Z_c$  pair in one event, one  $Z_c$  decays into  $\pi^+ J/\psi$ ,  $\pi^+ \chi_{c1}$ ,  $\pi^+ \psi(2S)$ , the other is the inclusive decays.
- No clear signals are observed and 90% C.L. upper limits are obtained.

$$\Upsilon(1S,2S) \rightarrow Z_c^+ Z_c^{(')-}$$





# $e^+e^- \rightarrow Z_c^+ Z_c^{(')-}$ at $\sqrt{s} = 10.52, 10.58, \text{ and } 10.867 \text{ GeV}$



# Summary

- Belle data taking is over, but still actively publishing results. Many interesting results are from the studies of Quarkonium and Quarkonium-like States.
  - ✓ Confirmation of the enhancement of  $\Upsilon(4S) \rightarrow \eta \Upsilon(1S)$  with respect to  $\Upsilon(4S) \rightarrow \pi^+ \pi^- \Upsilon(1S)$
  - ✓ First observation of  $\Upsilon(4S) \rightarrow \eta' \Upsilon(1S)$  and  $\Upsilon(5S) \rightarrow \eta \Upsilon_J(1D)$
  - ✓ Update the measurement for  $\mathcal{B}(B^+ \rightarrow X(3872)K^+)$
  - ✓ Search for  $\Upsilon(4660)$  and  $Y_\eta$  in  $B^+ \rightarrow K^+ \Lambda_c^+ \bar{\Lambda}_c^-$
  - ✓ Measurement of double  $Z_c$  production in  $e^+e^-$  reactions
- More promising results are expected at Belle II, where 50 times more statistics than Belle.
  - ✓ Investigate bottomonium spectroscopy, understand exotic states, and more...



More opportunities



*Backup*

# Investigations on the $\Upsilon(1D)$ triplet

*arXiv:1803.03225, submitted to EPJC*

$$\mathcal{F}_{1D} = \frac{N_{1D}}{1 + f_1 + f_2} \cdot [C_2(m_2) + f_1 C_1(m_1) + f_3 C_3(m_3)], \quad (2)$$

with

$$f_1 = \frac{\mathcal{B}[\Upsilon(5S) \rightarrow \eta \Upsilon(1D_1)]}{\mathcal{B}[\Upsilon(5S) \rightarrow \eta \Upsilon(1D_2)]} (= 0.68)_{theory} \quad (3)$$

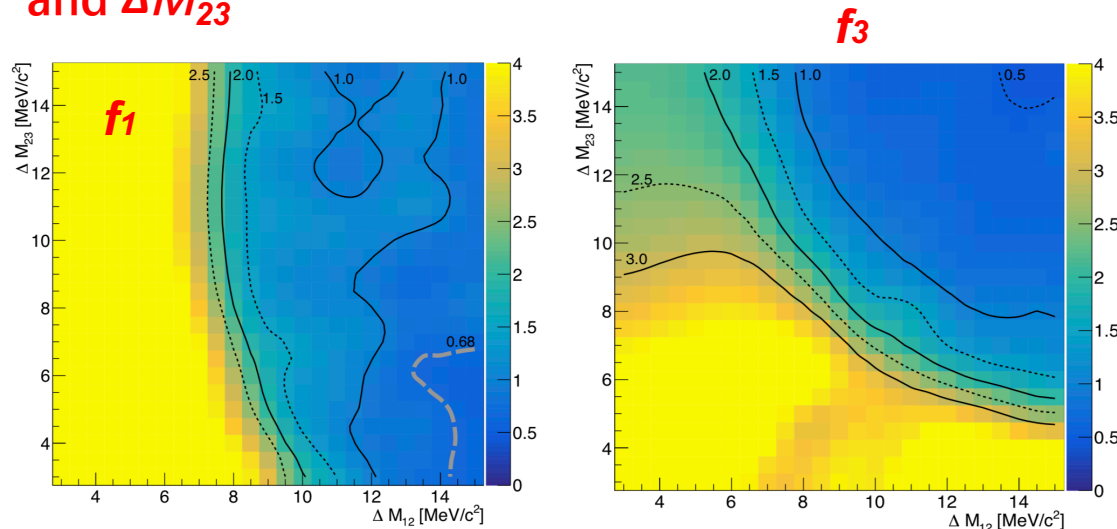
$$f_3 = \frac{\mathcal{B}[\Upsilon(5S) \rightarrow \eta \Upsilon(1D_3)]}{\mathcal{B}[\Upsilon(5S) \rightarrow \eta \Upsilon(1D_2)]} (= 0.13)_{theory} \quad (4)$$

Signal in  $M_{miss}^2(\gamma\gamma)$ : 3 Crystal Ball functions, with free miss relative fractions  $f_1, f_3$  that are precisely predicted in Ref. [[PRD94, 094039\(2016\)](#)]

$m_2$  fixed to world average,  $\Delta M_{ij}$  fixed to different values between 3 and 15  $\text{MeV}/c^2$  (reasonable according to calculations and observations)

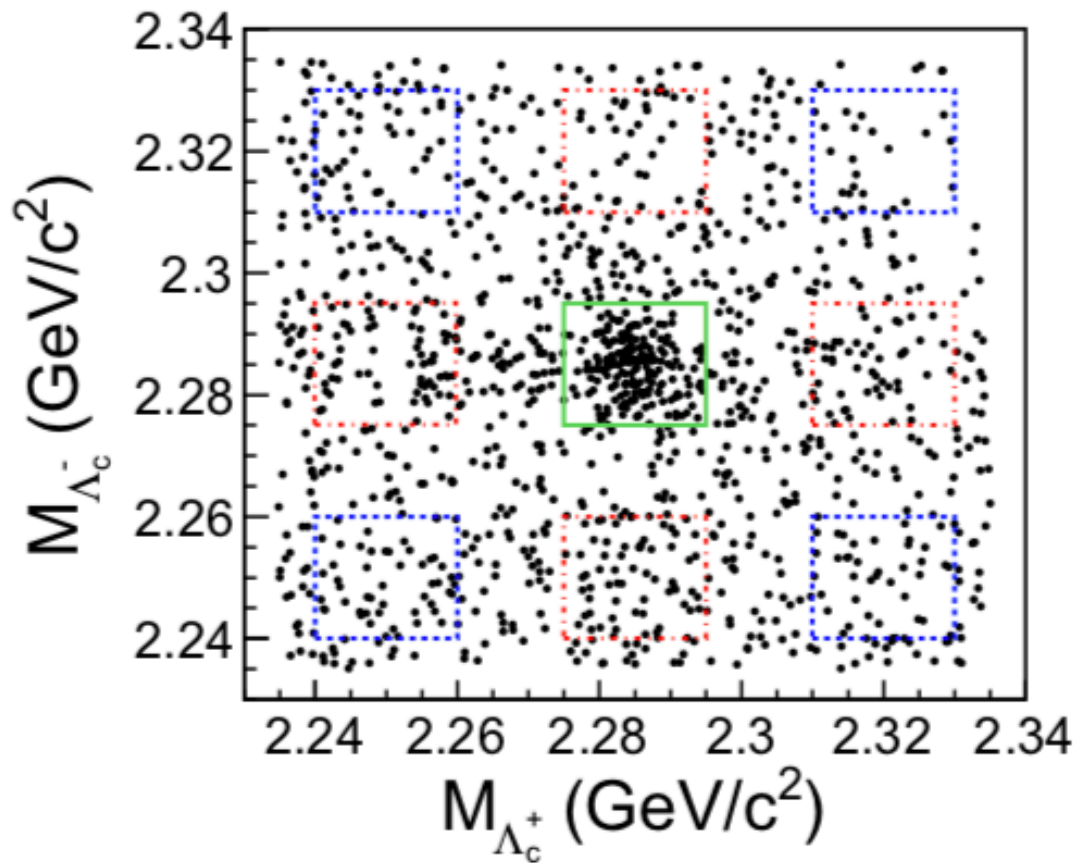
$\Delta M_{12} = m_2 - m_1$ ,  $\Delta M_{23} = m_3 - m_2$

90% CL ULs on  $f_1, f_3$  as a function of  $\Delta M_{12}$  and  $\Delta M_{23}$



# Sideband determination

*EPJC 78, 252 (2018)*

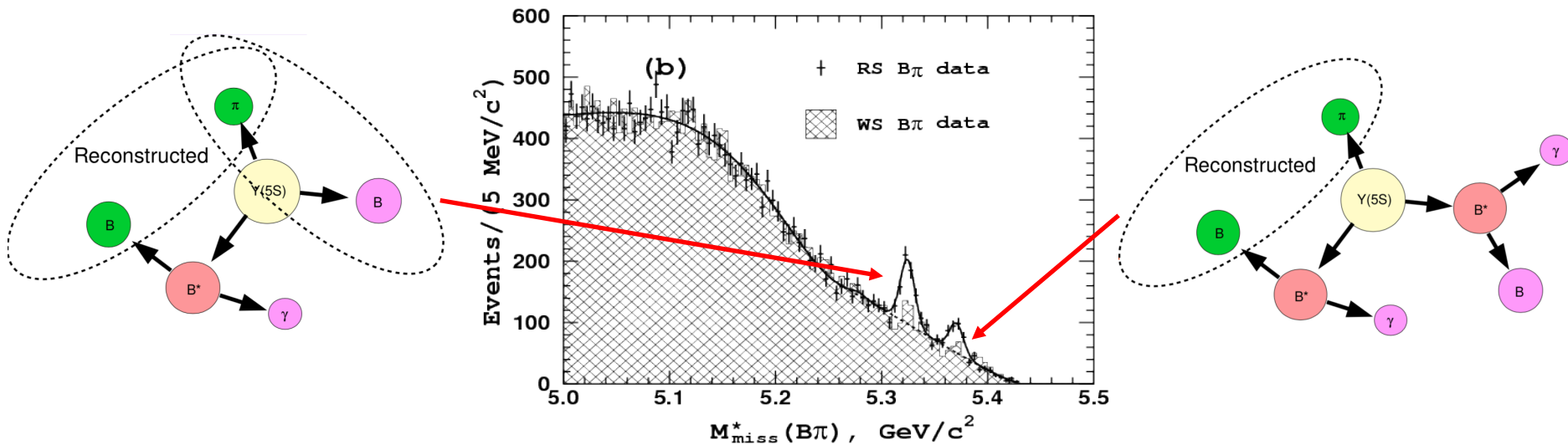


$\frac{1}{2}$  red sidebands -  
 $\frac{1}{4}$  blue sidebands

# Analysis method for $Z_b$ in $B^{(*)}\bar{B}^*$ systems

PRL 116, 212001 (2016)

- We expect the  $Z_b$  states to decay to final states with  $B^{(*)}$  mesons at substantial rates.
- Three-body  $e^+e^- \rightarrow B^+\bar{B}^0\pi^-, B^+\bar{B}^{*0}\pi^-,$  and  $B^{*+}\bar{B}^{*0}\pi^-$  processes near  $\Upsilon(10860)$  peak.
- B mesons are reconstructed in the following decay channel:  $B^+ \rightarrow J/\psi K^{(*)+}, B^+ \rightarrow \bar{D}^{(*)0}\pi^+, B^0 \rightarrow J/\psi K^{(*)0}, B^0 \rightarrow D^{(*)-}\pi^+$



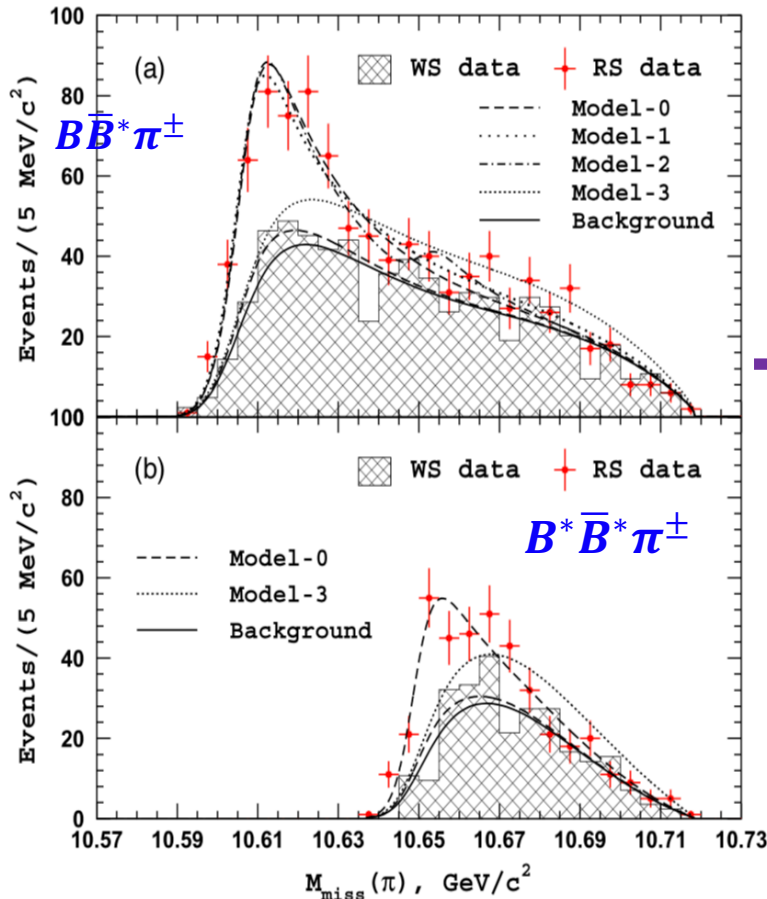
RS(right-sign):  $B^+$  or  $\bar{B}^0$  combined with  $\pi^-$   
 WS(wrong-sign): combinations with  $\pi^+$

The statistical significance of the observed  $BB^*\pi$  and  $B^*B^*\pi$  is  $9.3\sigma$  and  $8.1\sigma$ .

# $Z_b(10610)$ and $Z_b(10650)$ in $B\bar{B}^*$ and $B^*\bar{B}^*$ systems

PRL 116, 212001 (2016)

**Model-0** only  $Z_b(10610)[Z_b(10650)]$  amplitude **Model-1** add a nonresonant component  
**Model-2** add combination of two  $Z_b$  amplitudes **Model-3** a pure nonresonant amplitude



Significance in Mode-0

$Z_b(10610)$	$8.0 \sigma$
$Z_b(10650)$	$6.8 \sigma$

$Z_b$  parameters with **mode-0**

Sample	State	Mass(MeV/c <sup>2</sup> )	Width(MeV/c)
$B\bar{B}^*\pi^\pm$	$Z_b(10610)$	$10605 \pm 6$	$25 \pm 7$
$B^*\bar{B}^*\pi^\pm$	$Z_b(10650)$	$10648 \pm 13$	$23 \pm 8$

$$\frac{\mathcal{B}[Z_b^+(10610) \rightarrow \bar{B}^0 B^{*+} + B^+ \bar{B}^{*0}]}{\mathcal{B}[Z_b^+(10610) \rightarrow \text{bottomonium}]} = 5.93^{+0.99+1.01}_{-0.69-0.73}$$

$$\frac{\mathcal{B}[Z_b^+(10650) \rightarrow B^{*+} \bar{B}^{*0}]}{\mathcal{B}[Z_b^+(10650) \rightarrow \text{bottomonium}]} = 2.80^{+0.69+0.54}_{-0.40-0.36}$$

Channel	Fraction, %	
	$Z_b(10610)$	$Z_b(10650)$
$\Upsilon(1S)\pi^+$	$0.54^{+0.16+0.11}_{-0.13-0.08}$	$0.17^{+0.07+0.03}_{-0.06-0.02}$
$\Upsilon(2S)\pi^+$	$3.62^{+0.76+0.79}_{-0.59-0.53}$	$1.39^{+0.48+0.34}_{-0.38-0.23}$
$\Upsilon(3S)\pi^+$	$2.15^{+0.55+0.60}_{-0.42-0.43}$	$1.63^{+0.53+0.39}_{-0.42-0.28}$
$h_b(1P)\pi^+$	$3.45^{+0.87+0.86}_{-0.71-0.63}$	$8.41^{+2.43+1.49}_{-2.12-1.06}$
$h_b(2P)\pi^+$	$4.6^{+1.24+1.18}_{-1.00-0.89}$	$14.7^{+3.2+2.8}_{-2.8-2.3}$
$B^+ \bar{B}^{*0} + \bar{B}^0 B^{*+}$	$85.6^{+1.5+1.5}_{-2.0-2.1}$	...
$B^{*+} \bar{B}^{*0}$	...	$73.7^{+3.4+2.7}_{-4.4-3.5}$