



# Measurement of $\eta_c(1S)$ , $\eta_c(2S)$ and non-resonant $\eta'\pi\pi$ production in two-photon collisions at Belle

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On behalf of the Belle collaboration

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# Motivation for $\eta_c(1S)$ , $\eta_c(2S)$

- ▶ Playing an **important** role in **QCD** test [1]
  - ✓ Precise **two-photon decay widths** of  $\eta_c(1S)$  and  $\eta_c(2S)$  give sensitive **tests** for **QCD** models [2].
  - ✓ As lowest heavy-quarkonium state,  $\eta_c(1S)$ , as well as  $J/\psi$ ,  $\eta_b(1S)$  and  $\Upsilon(1S)$ , provide a benchmark for fine tuning of **input parameters** in **QCD** calculations.
- ▶ **Poor knowledge** available even for  $\eta_c(2S)$  hadronic decays, such as  $\eta'\pi\pi$ .
- ▶  $\eta_c(1S)$  and  $\eta_c(2S)$  were measured by BESIII in  $\Psi(2S)$  radiative decay, by BELLE and CLEO in B decay and two-photon production.
- ▶ First measurement of **two-photon decay width** of  $\eta_c(2S)$  via  $K^0_S K^+ \pi^-$  is given and an upper limit for  $\eta_c(2S) \rightarrow \eta' \pi^+ \pi^-$  signal is set by CLEO [3].
- ▶ X(1835) is observed by BESII [4] and confirmed by BESIII [5] with  $\eta' \pi^+ \pi^-$  final states. And is seen in two-photon collision by Belle [6].

[1] N. Brambilla et al., Eur. Phys. C 71, 1534 (2011).

[2] J. P. Lansberg and T. N. Pham, Phys. Rev. D 74, 034001 (2006).

[3] D.M. Asner, et al.,(CLEO Collaboration) , Phys. Rev. Lett. 92, 142001 (2004).

[4] M. Ablikim, et al., (BESII Collaboration) , Phys. Rev. Lett. 95, 262001 (2005).

[5] M. Ablikim, et al., (BESIII Collaboration) , Phys. Rev. Lett. 106, 072002 (2011).

[6] C.C. Zhang et al. Belle Collaboratin, Phys. Rev D 86, 052002 (2012).

# Motivation for cross section

- ▶ Test QCD calculations
  - Cross sections for two-photon production of **pseudo-scalar meson** pairs were measured by **Belle** [1].
    - Charged-meson pairs :  $\pi^+\pi^-$ ,  $K^+K^-$
    - Neutral-meson pairs:  $K_S^0 K_S^0$ ,  $\pi^0\pi^0$ ,  $\eta\pi^0$ ,  $\eta\eta$
  - **Leading term QCD** [2] predicts  $1/(W^6 \sin^4\theta)$  dependence for charged-meson pair and  $1/W^{10}$  and model-dependent angular distribution for neutral-meson pair.
  - **Handbag model** [3] gives transition amplitude for energy dependence and predicts  $1/\sin^4\theta$  dependence both for charged- and neutral-meson pairs.
  - **Improved study** both in experiment and QCD prediction at **higher W mass** would provide sensitive test in QCD calculations.
- ▶ Cross section measurements for productions of **pseudo-scalar tensor** pair  $\eta' f_2(1270)$  and three-body final state  $\eta' \pi\pi$  would provide new data for the QCD test.

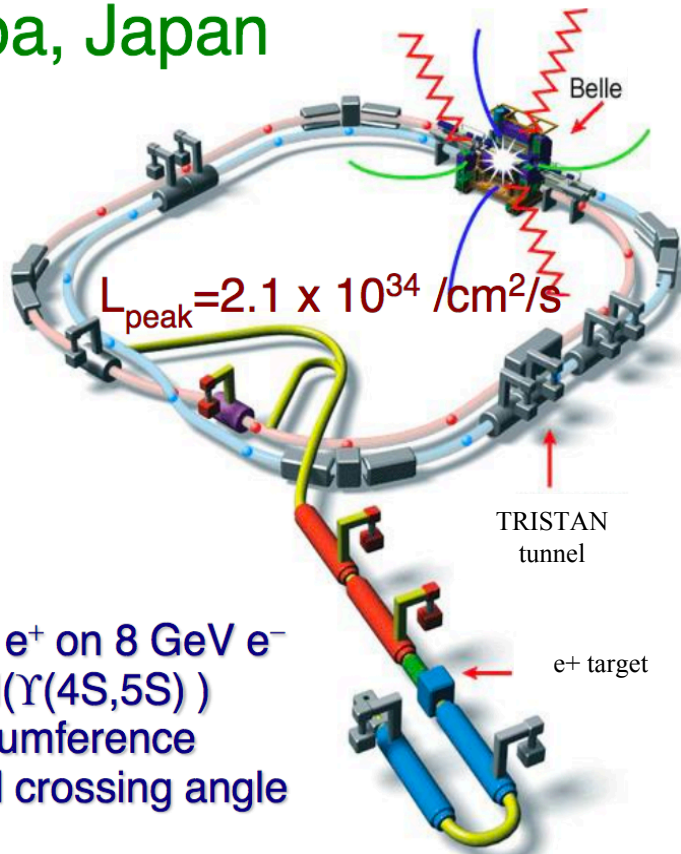
[1] Ed. A.J. Bevan, B. Golob, Th. Mannel, S. Prell, and B.D. Yabsley, Euro.Phys.Jour.C (2014) 74:3026.

[2] M. Benayoun and V. L. Chernyak., *Nucl.Phys.* B329, 285 (1990).

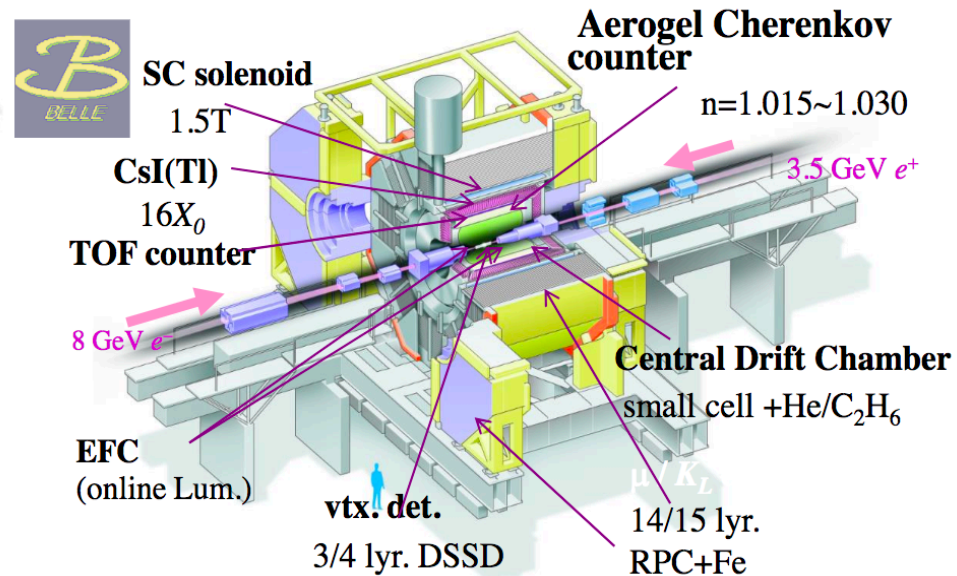
[3] M. Diehl, P. Kroll, and C. Vogt., *Phys. Lett.* B532, 99–110 (2002).

# KEKB and Belle Detector

Tsukuba, Japan



3.5 GeV  $e^+$  on 8 GeV  $e^-$   
 $W_{\text{CM}} = M(\Upsilon(4S, 5S))$   
 3km circumference  
 ~11mrad crossing angle

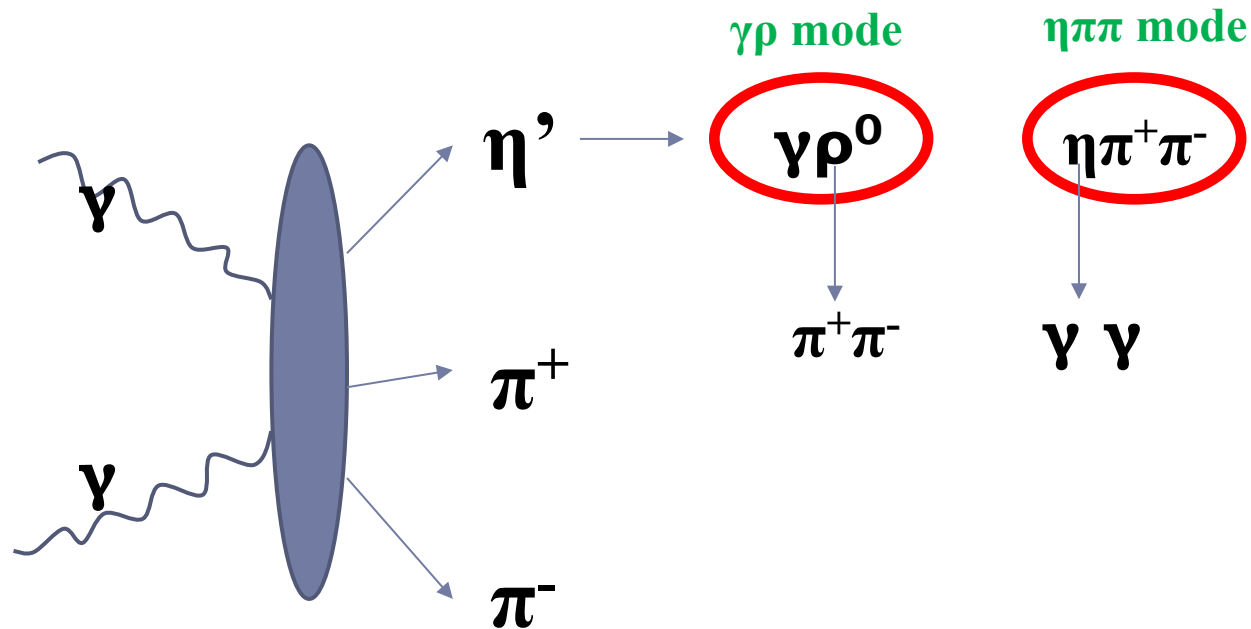


# Belle $\gamma\gamma \rightarrow \eta' \pi\pi$ analysis

Data sample:

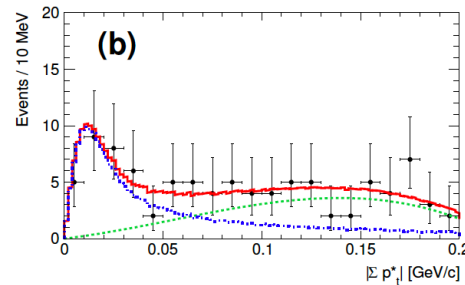
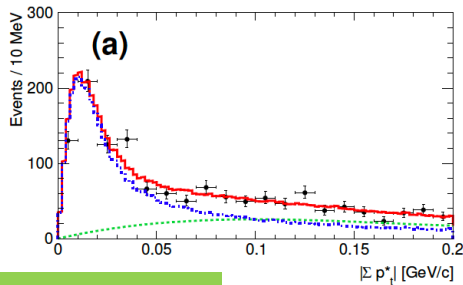
792 fb<sup>-1</sup> at  $\sqrt{s}=10.58$  GeV ( $\Upsilon(4S)$ ) and 60 MeV below it.

149 fb<sup>-1</sup> at  $\sqrt{s}=10.88$  GeV ( $\Upsilon(5S)$ ) and scan data around this energy point.

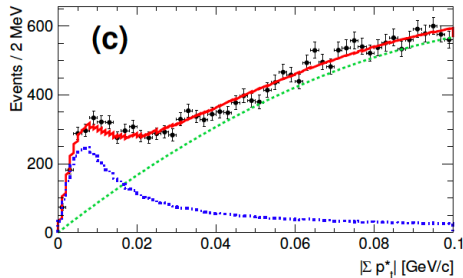


# $|\Sigma P^* t|$ and $M(\eta' \pi \pi)$ distributions

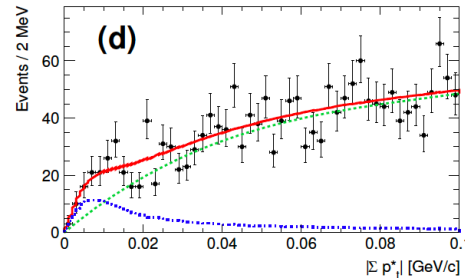
$\eta\pi\pi$  mode



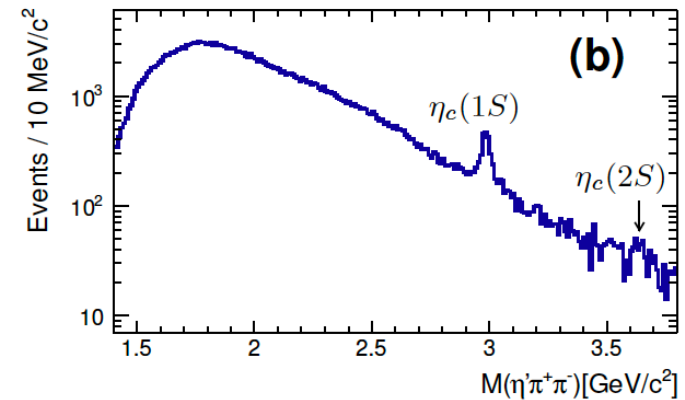
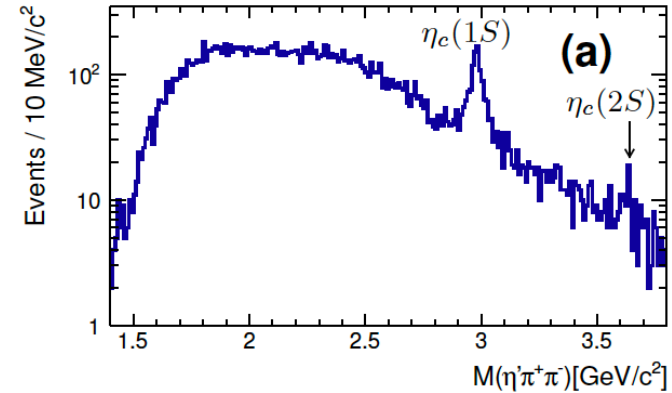
$\gamma\pi$  mode



in  $\eta_c(1S)$  signal region



in  $\eta_c(2S)$  signal region



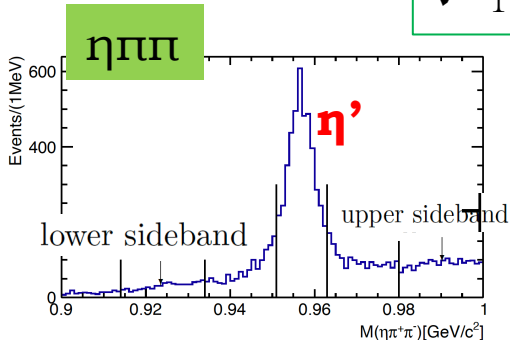
- Untagged two-photon process tend to carry small transverse momentum.
- A  $|\Sigma P^* t|$  requirement allows significant background reduction.

- Clear  $\eta_c(1S)$  signal in the two decay modes.
- A heavy combinational background by the low energy photons for  $\gamma\pi$  mode.

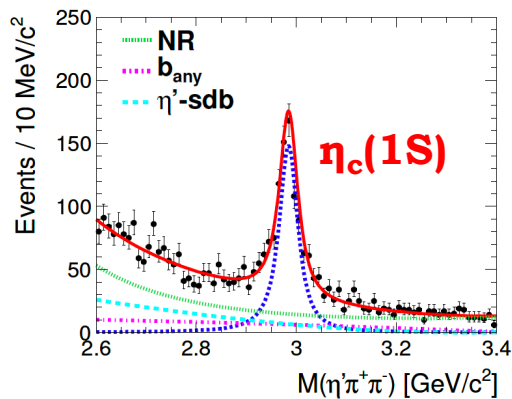
# Background in fit to $\eta'\pi\pi$ mass spectrum

Background for  $M(\eta'\pi\pi)$  spectrum dominant by :

- ✓ Background in  $\eta'$  signal region( $\eta'$ -sdb).
- ✓  $\eta'\pi\pi$ +any ( $b_{any}$ ).
- ✓ Non resonance (NR):  $e^+e^- \rightarrow e^+e^- \eta'\pi^+\pi^-$ .



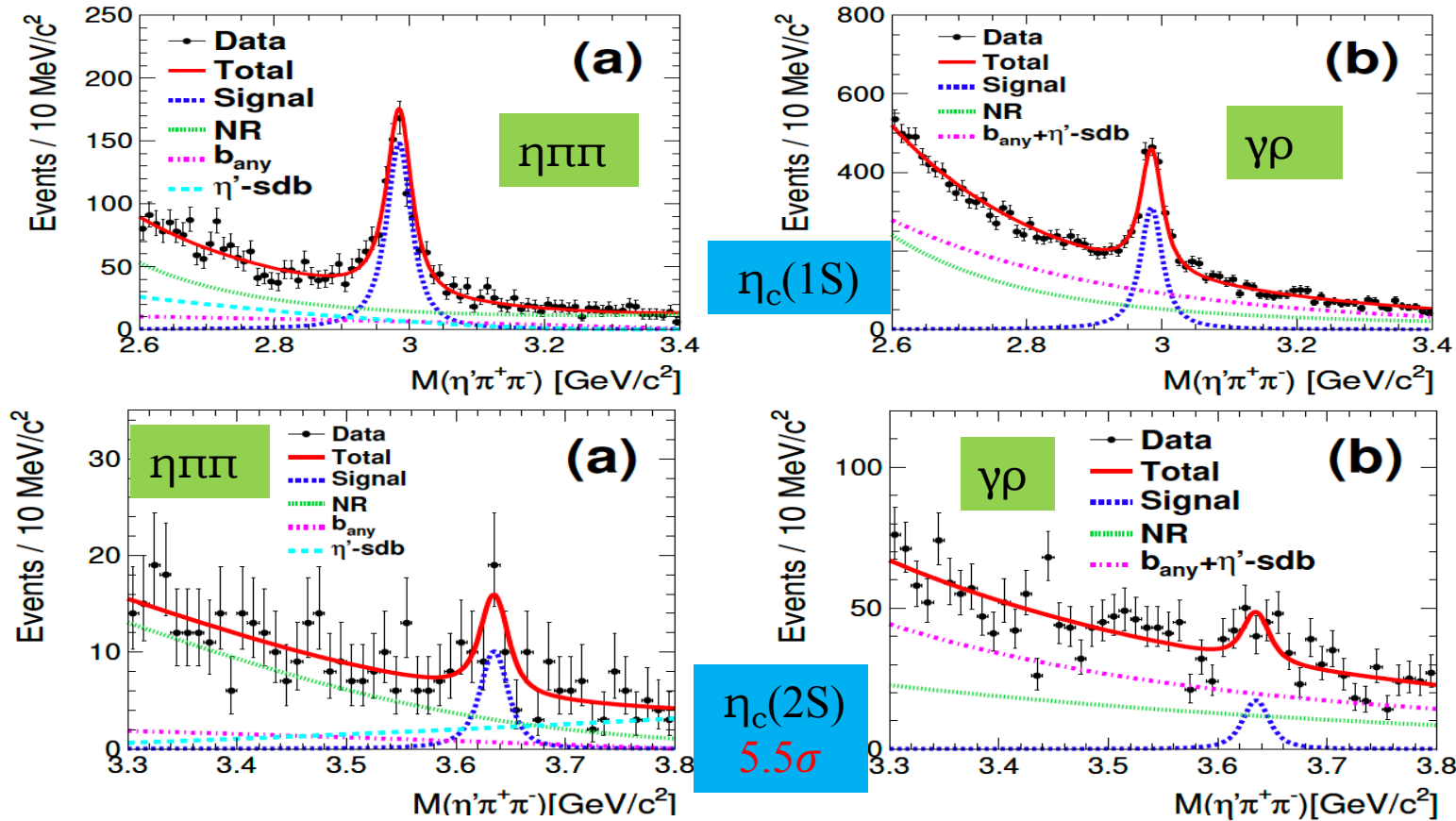
- ✓ Low smooth background.
- ✓  $\eta'$ -sdb determined by events in the  $\eta'$  sideband region
- ✓  $b_{any}$  described by events in region of  $0.17 < |\Sigma P_t^*| < 0.2 \text{ GeV}$ .



- ✓ Heavy background (including a peaking component due to  $\eta'$  mass constraint fit.).
- ✓  $\eta'$ -sdb +  $b_{any}$  determined by events in a region  $0.15 < |\Sigma P_t^*| < 0.2 \text{ GeV}$ .

- ✓ NR described by a 3<sup>rd</sup> exponential polynomial in fit for  $\gamma\rho$  and  $\eta\pi\pi$ .

# Simultaneous Fit for $\eta_c(1S)$ and $\eta_c(2S)$



	$\eta_c(1S)$		$\eta_c(2S)$	
	$\gamma\rho$	$\eta\pi^+\pi^-$	$\gamma\rho$	$\eta\pi^+\pi^-$
$n_s$	$1728^{+69}_{-68}$	$945^{+38}_{-37}$	$65^{+14}_{-13}$	$41^{+9}_{-8}$
$M$ ( $\text{MeV}/c^2$ )	$2984.6 \pm 0.7 \pm 2.2$		$3635.1 \pm 3.7 \pm 2.9$	
$\Gamma$ (MeV)	$30.8^{+2.3}_{-2.2} \pm 2.5$		11.3[fixed]	
$\Gamma_{\gamma\gamma}\mathcal{B}$ (eV)	$65.4 \pm 2.6 \pm 6.9$		$5.6^{+1.2}_{-1.1} \pm 1.1$	



# Discussion on $\Gamma_{\gamma\gamma}$ of $\eta_c(2S)$

- ◆ Defining the ratio  $R = \frac{\Gamma_{\gamma\gamma}(\eta_c(2S))B(\eta_c(2S))}{\Gamma_{\gamma\gamma}(\eta_c(1S))B(\eta_c(1S))}$ , which is directly measured,

	Belle ( $\eta'\pi\pi$ )	BaBar( $K\bar{K}\pi$ )[1]	CLEO ( $K_S K\pi$ )[2]
R	$(8.6 \pm 2.6) \cdot 10^{-2}$	$(10.6 \pm 2.0) \cdot 10^{-2}$	$(18 \pm 5 \pm 2) \cdot 10^{-2}$

Consistent

so, we have  $R_B = \frac{B(\eta_c(2S) \rightarrow \eta'\pi\pi)}{B(\eta_c(1S) \rightarrow \eta'\pi\pi)} \cong \frac{B(\eta_c(2S) \rightarrow K\bar{K}\pi)}{B(\eta_c(1S) \rightarrow K\bar{K}\pi)}$  within error.

- ◆ Assuming  $R_B \cong 1$  and

using the world average value  $\Gamma_{\gamma\gamma}(\eta_c(1S)) = 5.1 \pm 0.4$  keV,  
we obtain  $\Gamma_{\gamma\gamma}(\eta_c(2S)) = 0.44 \pm 0.13$  keV for Belle ( $\eta'\pi\pi$ ) and  
 $0.54 \pm 0.11$  keV for BaBar( $K\bar{K}\pi$ ) [1].

Both  $\Gamma_{\gamma\gamma}(\eta_c(2S))$  values by Belle are lower than

$0.92 \pm 0.28$  keV for CLEO( $K_S K\pi$ ) [2].

Discrepancy between data and QCD values

- ◆ QCD predictions for two-photon decay width of  $\eta_c(2S)$  are ranged from 1.4 to 5.7 [3,4].

- ◆ It is essential to have **precise measurement** of either  $B(\eta_c(2S) \rightarrow K_S K\pi)$  or  $B(B \rightarrow K\eta_c(2S))$

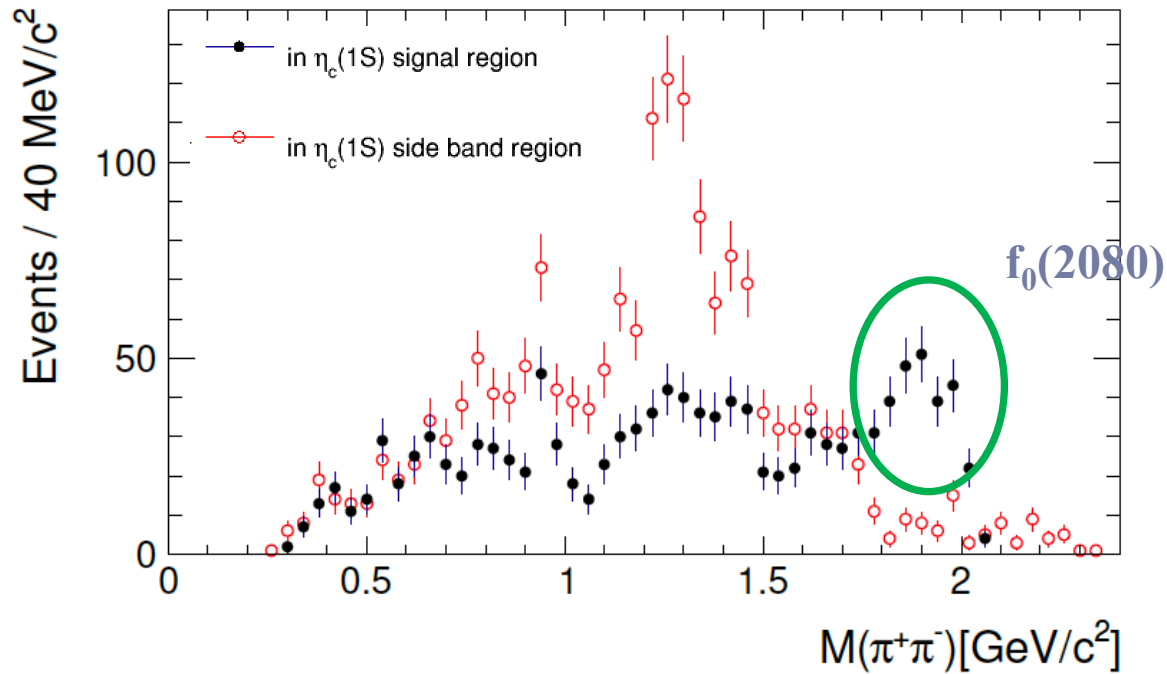
[1] del Amo Sanchez. P. et al. (BaBar Collaboration) Phys.Rev. D84 (2011) 012004.

[2] D. M. Asner *et al.* CLEO Collaboration, Phys. Rev.Lett. **92** (2004) 142001.

[3] T. Barnes, T. E. Browder, and S. F. Tuan, Phys. Lett. B **385**, 391 (1996).

[4] J.P. Lansberg, T.N. Pham, AIP Conf. Proc. 1038 (2008) 259.

# Study of $\eta_c(1S) \rightarrow \eta' f_0(2080)$ decay with $f_0(2080) \rightarrow \pi^+ \pi^-$



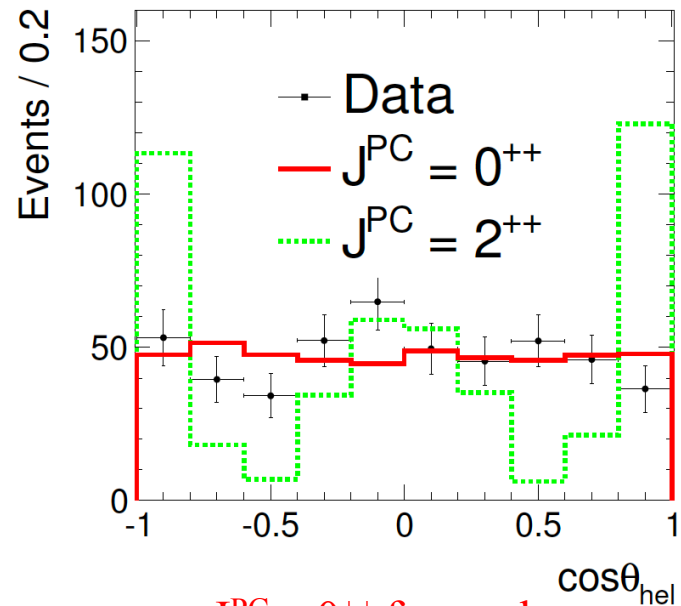
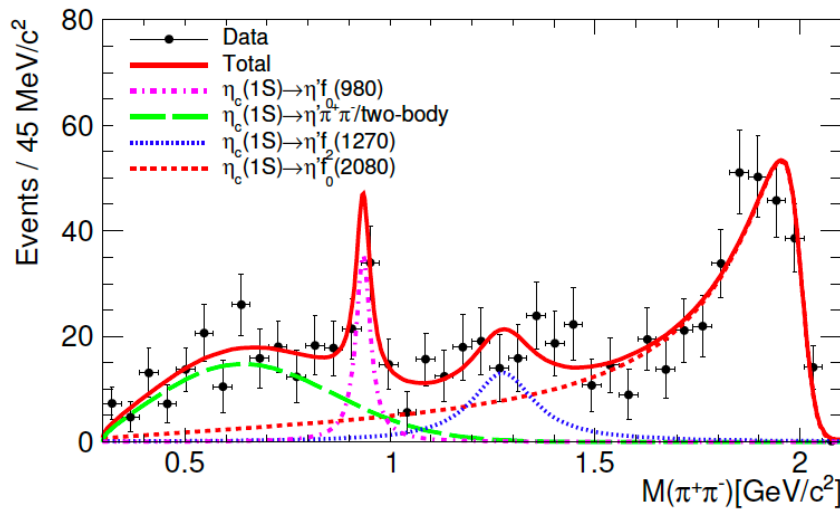
**Black dots** and **red circles** for events selected in  $\eta_c(1S)$  **signal** and **sideband** regions.

# Fitting $f_0(2080) \rightarrow \pi^+\pi^-$ with sample in $\eta_c(1S)$ signal region

Blatt-Weisskopf Breit-Wigner function for the signal:

$$f_s(m) = n_s (f_{BW}(m; M, \Gamma) p(m) \epsilon(m) \int_{m_d}^{m_u} q(m, m_{\eta_c}) f_{BW}(m_{\eta_c}) \frac{dL_{\gamma^*\gamma^*}}{dm_{\eta_c}} dm_{\eta_c}) \otimes g_{res}(m)$$

- ✓  $\epsilon(m)$  : detection efficiency.
- ✓  $p(m)$  :  $\pi$  momentum in  $f_0(2080)$  rest frame.
- ✓  $q(m, m_{\eta_c})$  :  $f_0(2080)$  momentum in  $\gamma\gamma$  rest frame.
- ✓  $\frac{dL_{\gamma\gamma}}{dm_{\eta_c}}$  : two-photon luminosity function.
- ✓  $g_{res}(m)$  : resolution of mass  $m$ .
- ✓  $(m_d, m_u) = (2.9, 3.06)\text{GeV}$  if  $m < 2.9 - 0.958$  ( $\eta'$  mass)
- ✓  $(m_d, m_u) = (m + 0.958, 3.06)\text{GeV}$  if  $m > 2.9 - 0.958$



$$M = 2083_{-66}^{+63} \pm 32 \text{ MeV}, \quad \Gamma = 178_{-178}^{+60} \pm 55 \text{ MeV}$$

$J^{PC} = 0^{++}$  favored

## Cross section for $\gamma\gamma \rightarrow \eta' \pi \pi$ , $\eta' f_2(1270)$

- The **differential cross section** in a  $W$  and  $|\cos\theta^*|$  two-dimensional bin is estimated by :

$$\frac{d\sigma_{\gamma\gamma \rightarrow \eta' \pi^+ \pi^-}(W_{\gamma\gamma}, \cos\theta^*)}{d|\cos\theta^*|} = \frac{\Delta N(W_{\gamma\gamma}, \cos\theta^*) / \epsilon(W_{\gamma\gamma}, \cos\theta^*)}{L_{int} \cdot \frac{dL_{\gamma\gamma}(W_{\gamma\gamma})}{dW_{\gamma\gamma}} \cdot \Delta W_{\gamma\gamma} \cdot \Delta|\cos\theta^*|} \quad (1)$$

- The  **$W$ -dependent cross section** of  $\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$  obtained by a summation over  $\Delta|\cos\theta^*|$  bins:

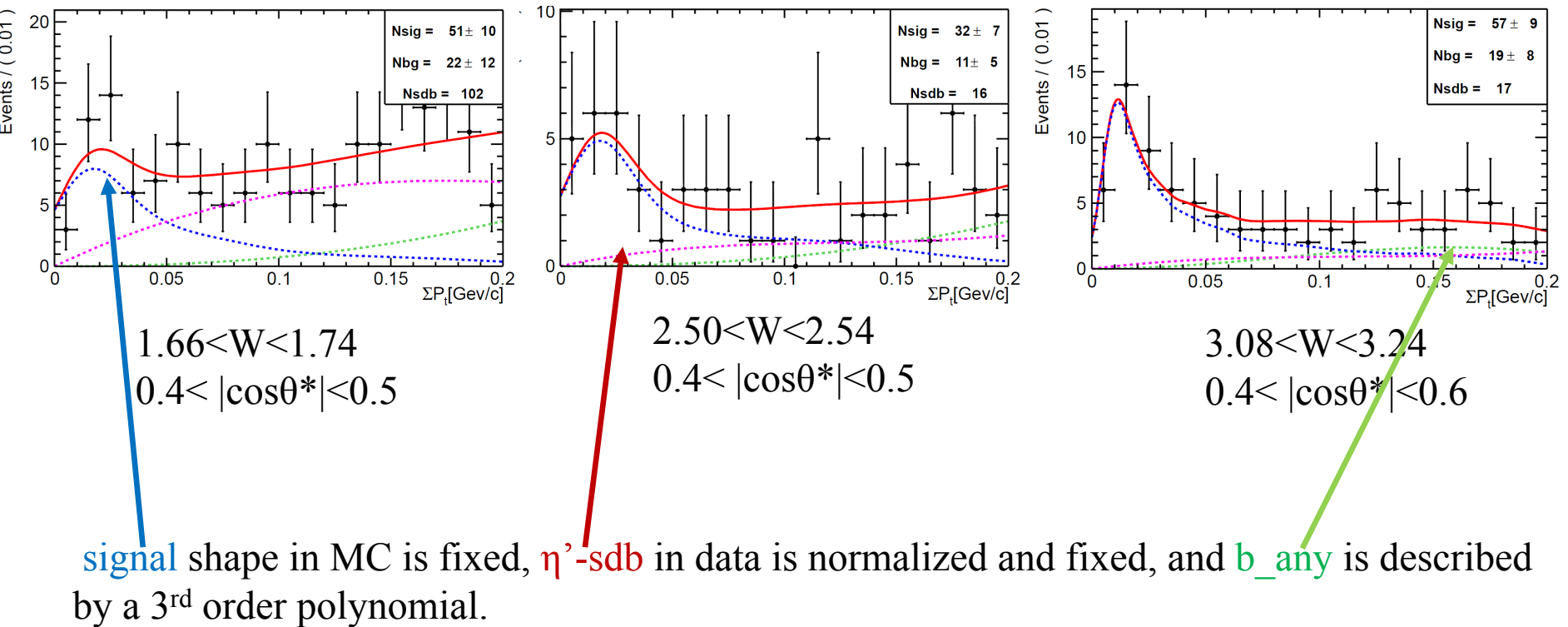
$$\sigma_{\gamma\gamma \rightarrow \eta' \pi^+ \pi^-}(W_{\gamma\gamma}) = \sum_{\Delta_i|\cos\theta^*|} \frac{d\sigma_{\gamma\gamma \rightarrow \eta' \pi^+ \pi^-}(W_{\gamma\gamma}, \cos\theta^*)}{d|\cos\theta^*|} \Delta_i|\cos\theta^*| \quad (2)$$

- The **differential cross section in  $|\cos\theta^*|$**  averaged over  $W$  bins within a certain  $W$  region:

$$\sigma_{\gamma\gamma \rightarrow \eta' \pi^+ \pi^-}(\cos\theta^*) = \frac{\sum \left( \frac{d\sigma_{\gamma\gamma \rightarrow \eta' \pi^+ \pi^-}(W_{\gamma\gamma}, \cos\theta^*)}{d|\cos\theta^*|} \Delta W_{\gamma\gamma} \right)}{\sum \Delta W_{\gamma\gamma}} \quad (3)$$

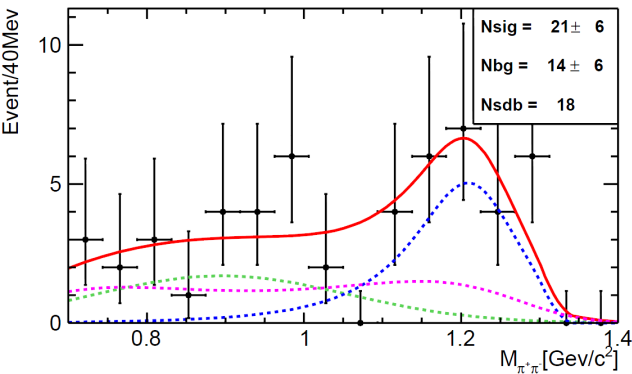
# $\sigma(\gamma\gamma \rightarrow \eta' \pi\pi) : \text{fitting } |\Sigma P^* t|$

Two-photon signal yield is extracted by fitting  $|\Sigma P^* t|$  distribution in data for each 2-dimension bin.

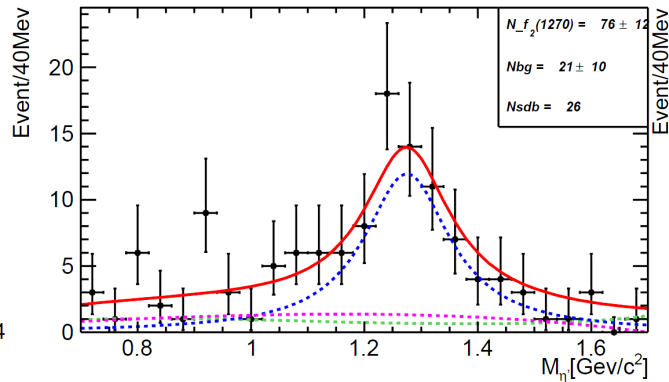


# $\sigma(\gamma\gamma \rightarrow \eta' f_2(1270)) : \text{fitting } M(\pi\pi)$

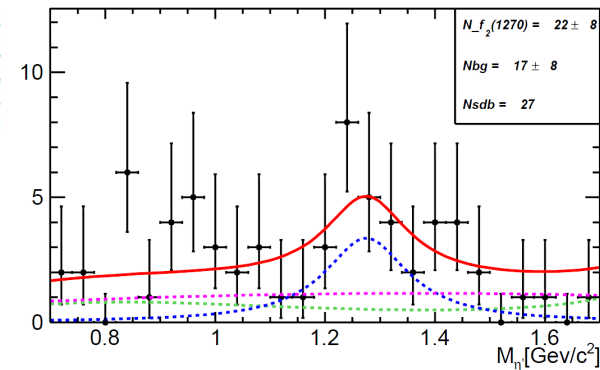
$f_2(1270)$  yield is extracted from fitting  $M(\pi^+\pi^-)$  distribution in data for each 2-dimensional bin.



$2.26 < W < 2.30$   
 $0.4 < |\cos\theta^*| < 0.5$



$2.62 < W < 2.66$   
 $0.4 < |\cos\theta^*| < 0.6$

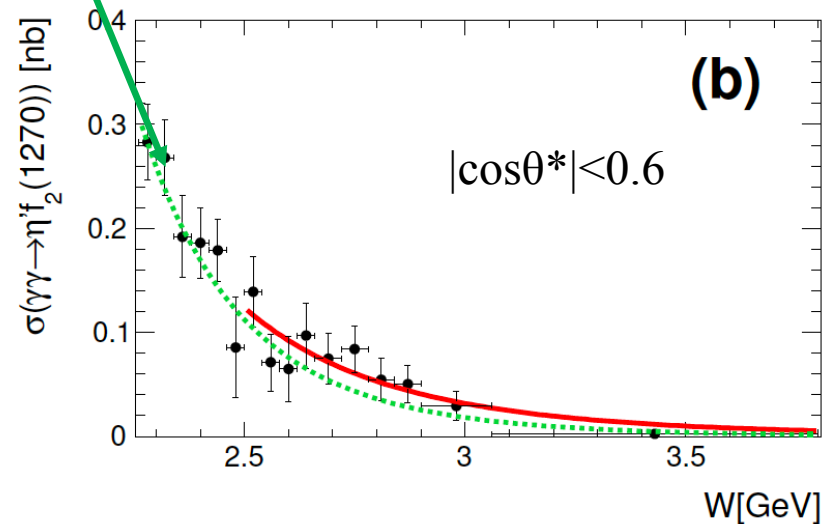
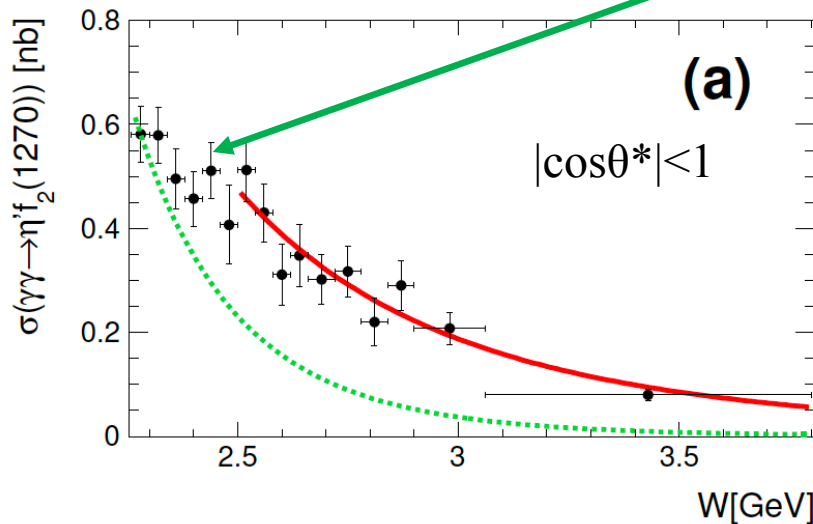


$2.72 < W < 2.78$   
 $0.4 < |\cos\theta^*| < 0.6$

- **Signal shape** is described by a Breit-Wigner with  $\Gamma$  and  $M$  fixed.
- Normalized  **$\eta'$ -sdb** in data is fixed.
- **b\_any** is described by a 4<sup>th</sup> order exponential polynomial.

# Result of $\sigma(\gamma\gamma \rightarrow \eta' f_2(1270))$

Solid points are the measured cross section in data

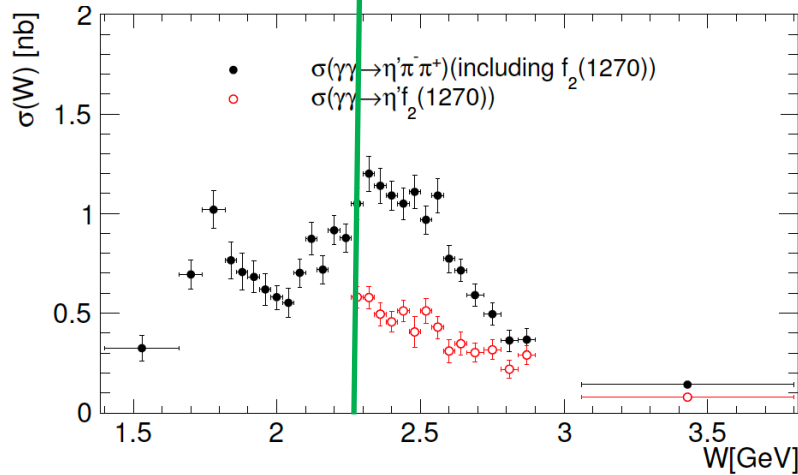


- **Green dashed** is the leading term QCD predictions for neutral meson pairs  $\sim 1/W^{10}$  [1].
- No prediction for  $\gamma\gamma \rightarrow \eta' f_2(1270)$ .
- Assuming  $\sigma \sim 1/w^n$ .
- We get the fitted value of  $n = 5.1 \pm 1.0$  for  $|\cos\theta^*| < 1$  and  $n = 7.5 \pm 2.0$  for  $|\cos\theta^*| < 0.6$ .

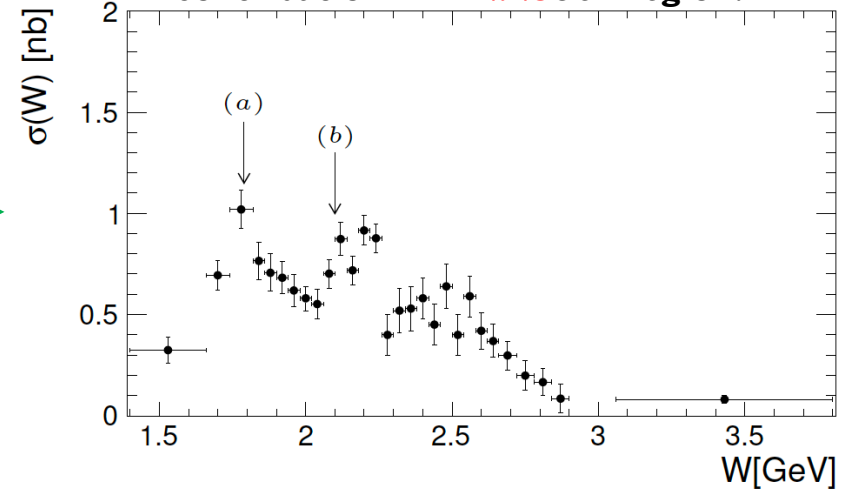
[1] Ed. A.J. Bevan, B. Golob, Th. Mannel, S. Prell, and B.D. Yabsley, Euro.Phys.Jour.C (2014) 74:3026.

# Result of $\sigma(\gamma\gamma \rightarrow \eta' \pi\pi)$

$\eta' f_2(1270)$  threshold



$\sigma(\gamma\gamma \rightarrow \eta' \pi\pi)$  after subtraction  $\eta' f_2(1270)$   
 contribution in  $W > 2.26$  GeV region.



(a). Structure near 1.8 GeV/c<sup>2</sup> is contributed from X(1835) or  $\eta(1760)$  [1].

(b) Enhancement at 2.1 GeV/c<sup>2</sup> is possible contribution from  $\gamma\gamma \rightarrow I(2100) \rightarrow \eta' f_0(980)$ .

[1] C.C. Zhang et al. Belle Collaboration, Phys. Rev D86, 052002 (2012).

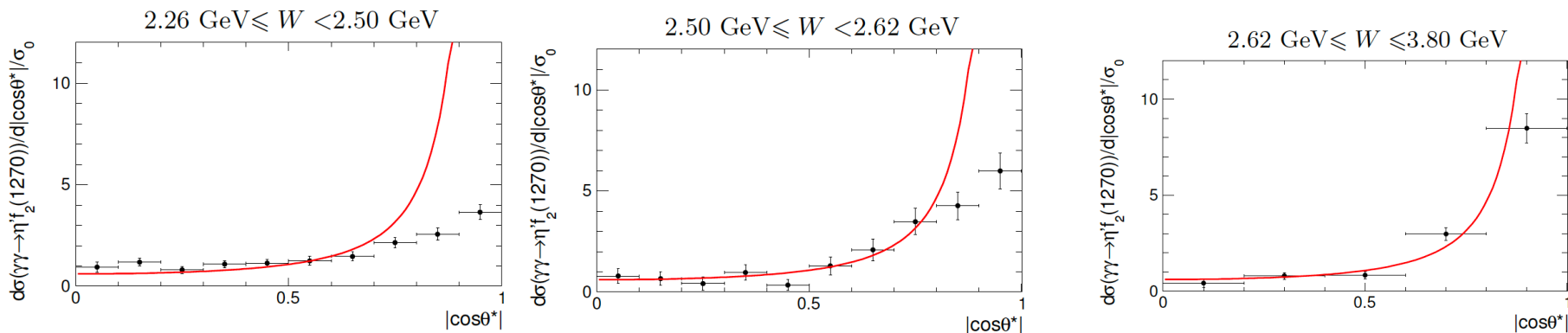


# Cross Section in $|\cos\theta^*|$

- Black dots with error bar are the  $|\cos\theta^*|$  dependent cross sections in data

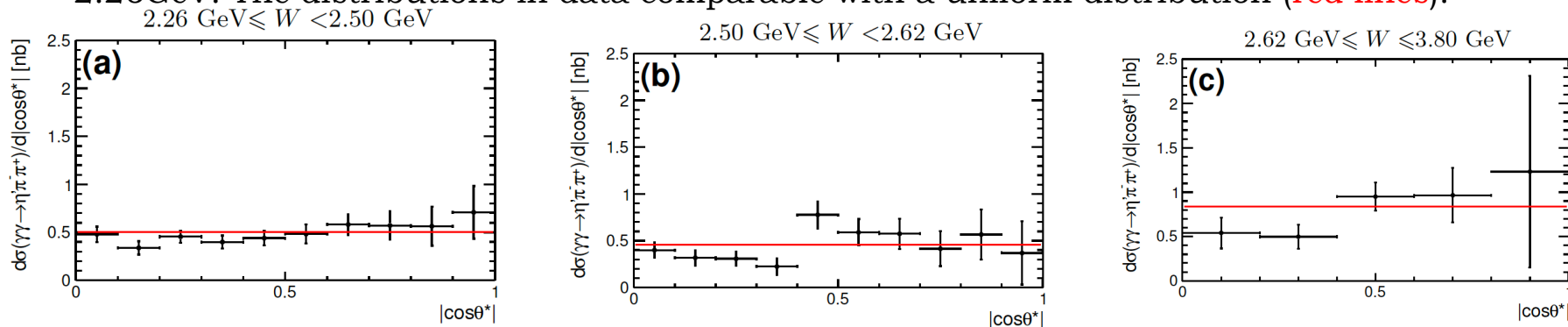
$$\gamma\gamma \rightarrow \eta' f_2(1270)$$

Red line is QCD predictions for neutral meson pairs  $\sim 1/\sin^4\theta$



$$\gamma\gamma \rightarrow \eta' \pi\pi$$

Measured cross section **after subtracting** the  $\gamma\gamma \rightarrow \eta' f_2(1270)$  contribution in W region above 2.26 GeV. The distributions in data comparable with a uniform distribution (**red lines**).



# Summary

- Results on the  $\gamma\gamma\rightarrow\eta'\pi\pi$  process for both  $\eta'\rightarrow\eta\pi\pi$  &  $\gamma\rho$  decays using 941 fb<sup>-1</sup> Belle data are presented.
- First observation of  $\eta_c(2S)\rightarrow\eta'\pi\pi$  with a significance **5.5 $\sigma$**  including systematic error.
  - Consistent ratio  $R = \frac{\Gamma_{\gamma\gamma}(\eta_c(2S))B(\eta_c(2S))}{\Gamma_{\gamma\gamma}(\eta_c(1S))B(\eta_c(1S))}$  between  $K\bar{K}\pi$  (BaBar) and  $\eta'\pi\pi$  (Belle) decays, is interesting in QCD test.
- First observation of  $\eta_c(1S)\rightarrow\eta'f_0(2080)$  decay with  $f_0(2080)\rightarrow\pi^+\pi^-$  with a significance 20 $\sigma$ , and its mass and width is determined to be
$$M = 2083_{-66}^{+63} \pm 32 \text{ MeV}/c^2,$$
$$\Gamma = 178_{-178}^{+60} \pm 55 \text{ MeV}.$$
- Measurements of pseudo-scalar tensor pair  $\eta'f_2(1270)$  production, as well as that of  $\eta'\pi\pi$ , are made for the first time.

Thanks for your attention!

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# Backup

# Selection criteria

## $\gamma p$ mode

Variable	cut value
$P_{sum}$	$< 5.5 \text{ GeV}/c$
$E_{sum}$	$< 4.5 \text{ GeV}$
$N_{\pi^+}, N_{\pi^-}$	2,2
$N_{charge}$	4
$N_{k^+} + N_{k^-}$	$< 1$
$N_{p^+} + N_{p^-}$	$< 1$
$N_{e^+} + N_{e^-}$	$< 1$
$k_s$ -veto	$\notin (0.508, 0.488)[\text{GeV}/c^2]$
$M(\eta')$	$(0.942, 0.974)[\text{GeV}/c^2]$
$\pi^0, \eta$ -veto	$\notin (0.115, 0.155), (0.524, 0.572)[\text{GeV}/c^2]$
$E_\gamma$	$> 100 \text{ MeV}$
$\Sigma p_t$	$< 0.1 \text{ GeV}/c$

## $\eta\pi\pi$ mode

Variable	cut value
$P_{sum}$	$< 5.5 \text{ GeV}/c$
$E_{sum}$	$< 4.5 \text{ GeV}$
$N_{\pi^+}, N_{\pi^-}$	2,2
$N_{charge}$	4
$N_{k^+} + N_{k^-}$	$< 1$
$N_{p^+} + N_{p^-}$	$< 1$
$N_{e^+} + N_{e^-}$	$< 1$
$k_s$ - veto	$\notin (0.488, 0.508)[\text{GeV}/c^2]$
$E(\gamma)$	$> 100 \text{ MeV}$
$M(\eta)$	$(0.524, 0.572)[\text{GeV}/c^2]$
$M(\eta')$	$(0.951, 0.963)[\text{GeV}/c^2]$
$\pi^0$ - veto	$\notin (0.115, 0.155)[\text{GeV}/c^2]$
$\Sigma p_t$	$< 0.15 \text{ GeV}/c$

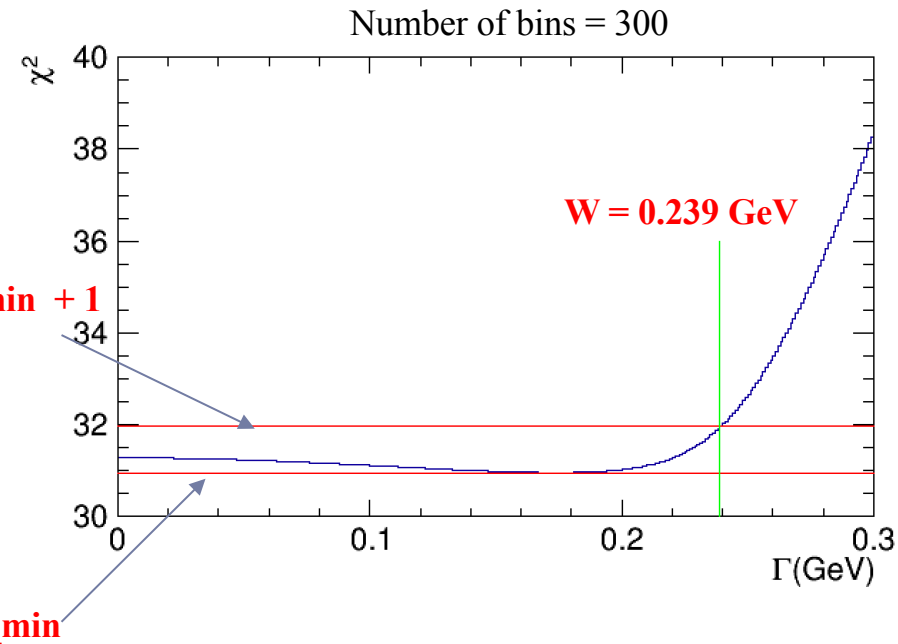
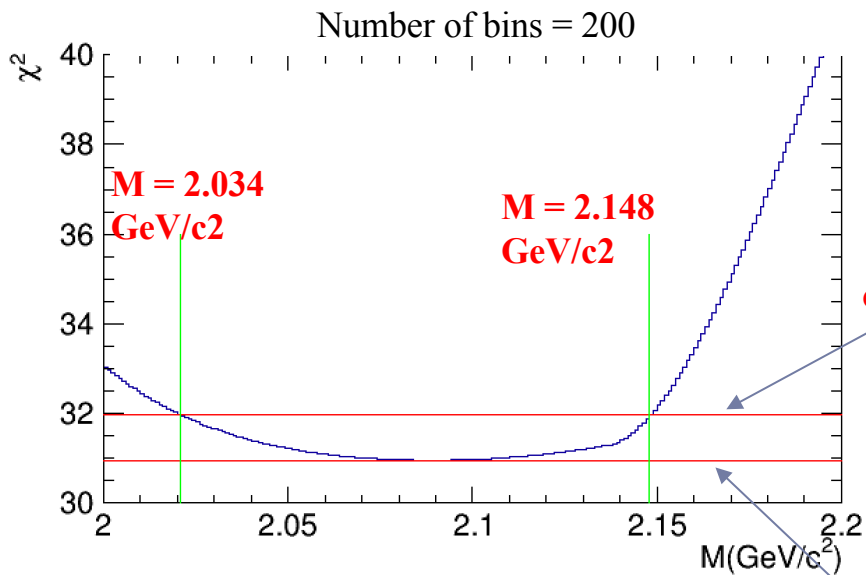
$|\Sigma \mathbf{P}^* \mathbf{t}|$  is optimized with the best  $s/\sqrt{s+b}$  in  $\eta_c(1s)$  and  $\eta_c(2s)$  signal region.

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From PDG 2017

	Branching fraction
$\eta_c(1S) \rightarrow K \bar{K} \pi$	$(7.3 \pm 0.5)\%$
$\eta_c(2S) \rightarrow K \bar{K} \pi$	$(1.9 \pm 1.2)\%$
$B \rightarrow K(\eta_c(1S) \rightarrow K_s K \pi)$	$(2.7 \pm 0.6) \times 10^{-5}$
$B \rightarrow K(\eta_c(2S) \rightarrow K_s K \pi)$	$(3.4^{+2.3}_{-1.6}) \times 10^{-6}$

# $\chi^2$ scan for $f_0(2080)$ mass and width



From the  $\chi^2$  scan we get:

$M = 2088 +60 -54 \text{ MeV}/c^2$

$W = 177 +62 -177 \text{ MeV}$

Which are comparable with the results from MINOS fit.

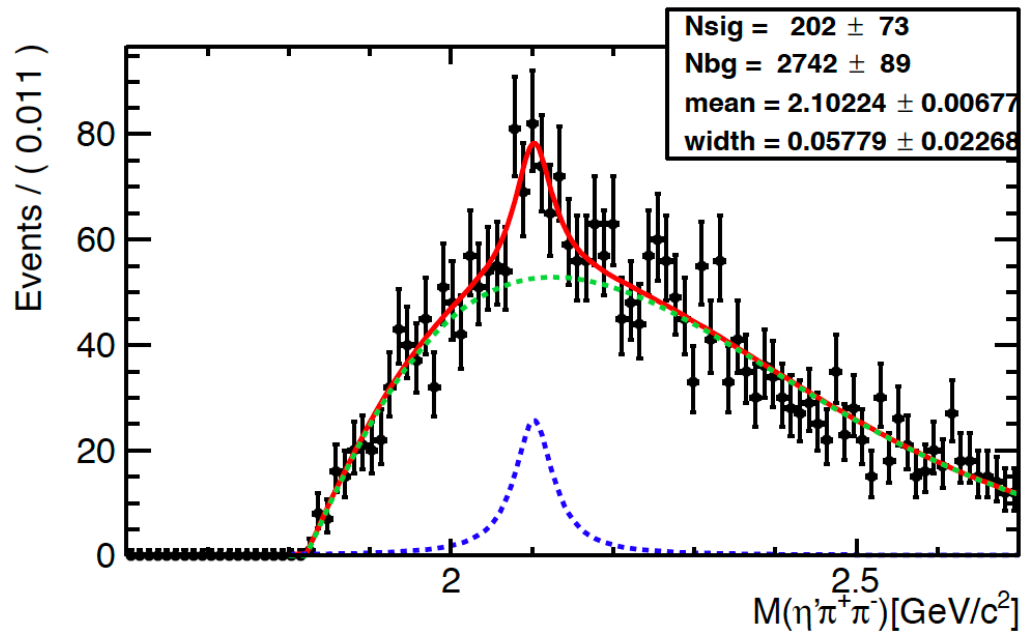
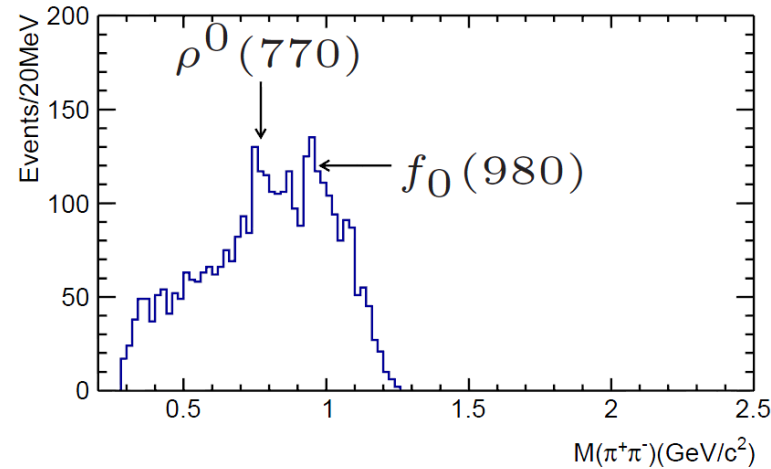
From MINOS fit:

$M = 2083 +63 -67 \text{ MeV}/c^2$

$W = 178 +60 -178 \text{ MeV}$

Possible intermediate from  $\gamma\gamma \rightarrow I(2100) \rightarrow \eta' f_0(980)$

$$2.0 < W < 2.2 \text{ GeV}/c^2$$



- In  $f_0(980)$  signal region  $0.86 < M(\pi\pi) < 1.10 \text{ GeV}/c^2$ .
- $I(2100)$  with statistic significance  $3.5\sigma$ .