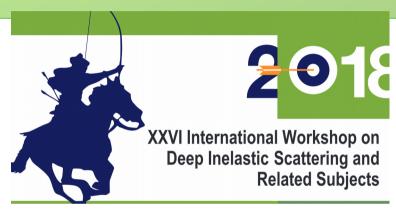
## Recent QCD-related studies with the BaBar detector



16-20 April 2018, Port Island, Kobe



Laura Zani
INFN and University of Pisa



on behalf of the BaBar Collaboration



### Outline

- The BaBar experiment
- Measurement of the D\*+(2010) D+ mass difference BABAR, PRL 119.202003 (2017), arXiv: 1707.09328
- Measurement of the spectral function for the  $\tau \to K\text{-}K_s\nu_\tau$
- Search for the B-meson decay to four baryons  $B \rightarrow p p p p$  Submitted to PRD! arXiv:1803.10378

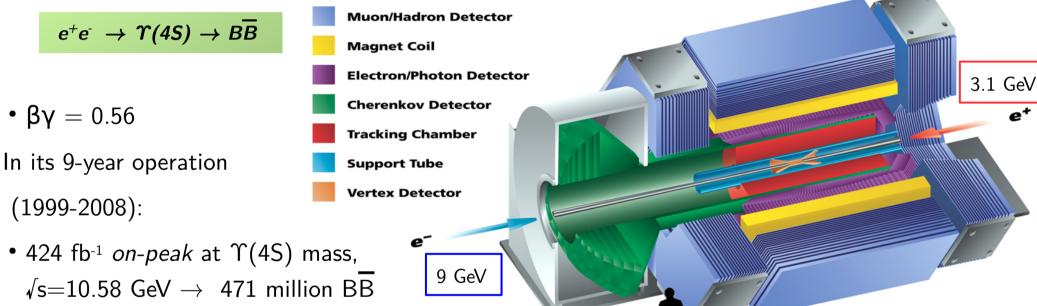






## The BaBar Experiment

**B-factories**: dedicated experiments at  $e^+e^-$  asymmetric-energy colliders for the production of quantum coherent BB pairs  $\rightarrow$  CP-Violation (CPV) studies and New Phisics (NP) indirect searches.



- $\sqrt{s}$ =10.58 GeV  $\rightarrow$  471 million  $\overline{BB}$ pairs.
- 44 fb-1 off-peak, in the continuum hadronization region, √s = 10.54 GeV

Clean environment allows **outstanding tracking** and **vertex** reconstruction; dE/dx,  $cos\theta_c$  measurements provide **excellent PID** performance  $\rightarrow$  high efficiency with pion mislD below 1% at any momentum.







## Measurement of the $(D^{*+}(2010) - D^{+})$ mass difference

#### Motivation for measuring $\Delta m_{+} \equiv m(D^{*+}(2010)) - m(D^{+})$

- Extract  $\Delta m_D \equiv m(D^+)-m(D^0) = \Delta m_0 \Delta m_+$ , by combining with the measurement of  $\Delta m_0 \equiv m(D^{*+}(2010)) m(D^0)$
- Constrain the symmetry breaking due to u-d quark mass difference in chiral perturbation theory & lattice QCD

#### **Previously:**

- Most accurate  $\Delta m_D$  measurement from LHCb,  $\Delta m_D =$  (4.76  $\pm$  0.12  $\pm$  0.07) MeV JHEP 06, 065 (2013)
- CLEO reported the measurement  $\Delta m_+=$  (140.64  $\pm$  0.08  $\pm$  0.06) MeV based on the decay chain D\*+  $\to$  D+  $\pi^0$  with D+  $\to$  K-  $\pi^+$   $\pi^+$  PRL 69, 2046 (1992)
- BaBar measurement of  $\Delta m_0$  using the decay chain  $D^{*+} \to D^0 \pi^+$  with  $D^0 \to K^- \pi^+$  and also  $D^0 \to K^- \pi^+ \pi^- \pi^+$  PRL 111, 111801 (2013)







## **Analysis Strategy**

Reconstruct the decay chain:

$$D^{*+} \to D^+ \pi^0, D^+ \to K^- \pi^+ \pi^+$$

- Extract  $\Delta m_+$  by fitting the distribution of the mass difference between the reconstructed D\*+ and D+
- Define the PDF: MC resolution function (signal)+ threshold function (background contamination)
- Combine with the BaBar measurement of  $\Delta m_0$
- Obtain **∆**m<sub>D</sub>





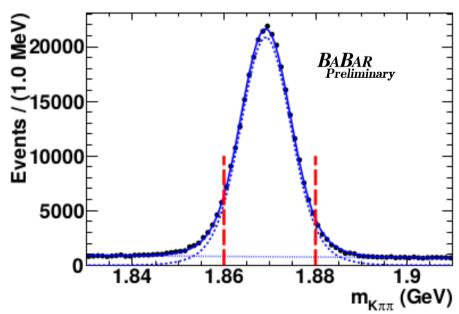


## **Event Reconstruction and Selection**

$$D^{*+} \to D^+ \pi^0, D^+ \to K^- \pi^+ \pi^+$$

- "Slow"  $\pi^0$  (p<sub> $\pi$ </sub> <300 MeV):
  - resolution on pion momentum improved ( $\sim$ 3%) by the kinematic fit to the photon pair invariant mass  $\rightarrow$  constrained to the nominal invariant mass of  $\pi^0$ .
  - MC-Data correction for the energy loss in the EMC is also applied
- $D^{*+}$  (p cM >3 GeV)
  - reject background contamination from D\*+  $\rightarrow$  D0  $\pi$ + : m(K-  $\pi$ +  $\pi$ 0) m(K-  $\pi$ + $\pi$ 0) < 160 MeV
  - geometric and kinematic constraint on the D\*+ production vertex and on D+ decay vertex ( $\text{Prob}(\chi^2) > 0.1\%$ )

- **D**+ (momentum resolution  $\sim 0.5\%$ ):
  - pion/kaon particle identification and a selection on the distribution of polar angle of the reconstructed tracks + invariant mass selection
  - selection based on a likelihood variable
     (Decay vertex, Dalitz-plot position)



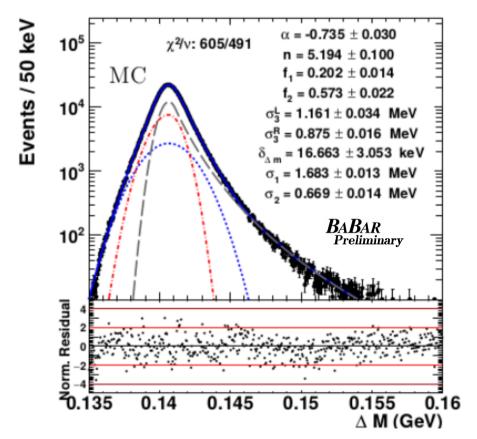




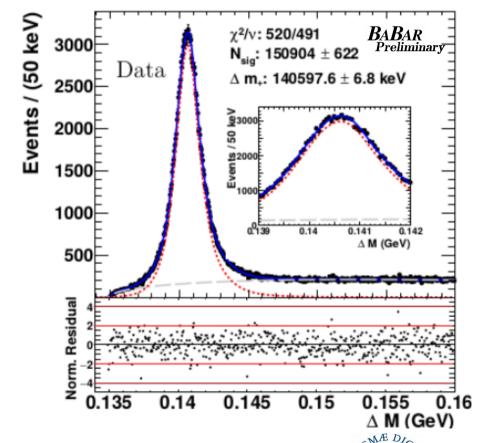


## Fitting Procedure

1. Model the signal component in the  $\Delta m_+$  distribution on simulation and extract the shape parameters (*resolution function* based on Gaussian-like PDFs).



2. Apply an unbinned maximum likelihood fit to the data using as PDF resolution function (signal) + threshold function (combinatorial background) and extract  $\Delta m$ .







## Results & Summary (I)

- From the fitted signal events (150 904  $\pm$  622 ), we measure  $\Delta m_+ =$  (140 597.6  $\pm$  6.8 $_{\rm stat}$ ) keV
- The extracted mass difference is corrected for the **bias** of **3.4 keV** produced by peaking background not considered in the fit (pseudoexperiments)
- The main sources of systematic uncertainty are:
  - detector effects not accounted for in the simulation;
  - MC-data differences in the EMC calibration (photon energies).
- Total systematic uncertainty = 12.9 keV

Summarizing, after adding the fit bias

$$\Delta m_{_+} = (140\ 601.0 \pm 6.8 [stat] \pm 12.9 [syst]) \ keV$$

• Combine with the measurement of  $\Delta m_0 = (145~425.9 \pm 0.5 [stat] \pm 1.8 [syst])$  keV based on the same data set and obtain:

$$\Delta m_D = (4\ 824.9 \pm 6.8[stat] \pm 12.9[syst]) \text{ keV}$$

→ 5 times more accurate than world average







## Measurement of the spectral function for the $\tau^- \rightarrow K^- K_{\varsigma} \nu_{\tau}$

#### Motivation

- T decays are an optimal laboratory for NP searches (Lepton Flavor Violation, Hadron Vacuum Polarization contribution to g-2, Standard Model test of CPV)
- the measurement of the *invariant mass spectrum of the*  $K^-K_S$  *system* allows to measure the spectral function

$$V(q) = \frac{m_{\tau}^{8}}{12\pi C(q)|V_{\rm ud}|^{2}} \frac{\mathcal{B}(\tau^{-} \to K^{-}K_{\rm S}\nu_{\tau})}{\mathcal{B}(\tau^{-} \to e^{-}\bar{\nu_{e}}\nu_{\tau})} \frac{1}{N} \frac{dN}{dq}$$

and provide information on isovector part (Isospin=1) of the  $e^+e^- o KK$  cross section:

$$\sigma_{e^+e^- \to K\bar{K}}^{I=1}(q) = \frac{4\pi^2 \alpha^2}{q^2} V(q)$$

#### Previously

- BaBar: measurement of the e<sup>+</sup> e  $^ \rightarrow$  K $\overline{\text{K}}$  PRD 88, 3, 032013 (2013).
- CLEO: K-  $K_s$  mass spectrum measurement on  $2.7 \times 10^6$   $\tau$  pairs PRD 53, 6037 (1996)
  - ightarrow significantly improving on this measurement by using the full BaBar data sample of  $10^9~ au$  pairs

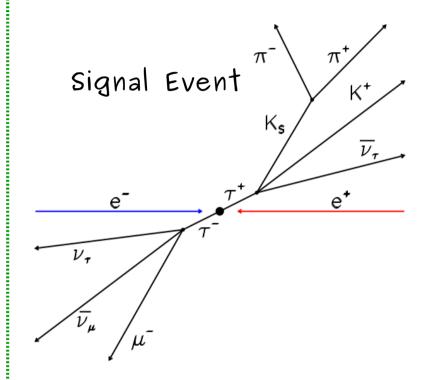






## **Analysis Strategy**

- Exploit the event topology to reconstruct the signal signature
- Apply a signal-like selection for rejecting the background
- Subtract the remaining background contaminating the  $K^-K_S$  invariant mass spectrum
- Correct for detection efficiency and extract:
  - The mass spectrum of the K- K<sub>S</sub> system
  - The branching fraction BF(  $\tau \to K^{\mbox{\tiny -}} \, K_{\mbox{\tiny S}} \, \nu_{\tau})$

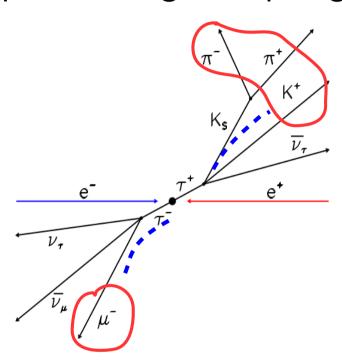


 $\rightarrow$  Compute the spectral function V(q) from the measured mass spectrum

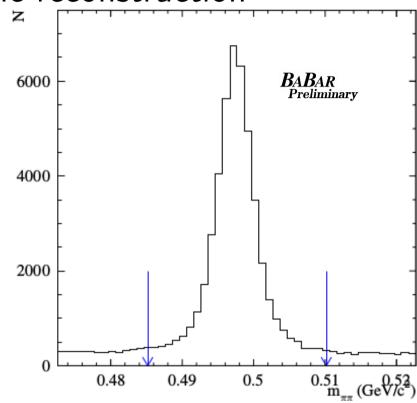


### **Event Reconstruction and Selection**

Exploit the signal topology for the reconstruction



- 4 charged tracks with total charge = 0
- 2 oppositely charged tracks coming
   from the interaction point (PID applied,
   one lepton + one kaon)



- Selection on angular distribution and measured momenta of the reconstructed tracks
- Constrain the reconstructed invariant mass of two charged pions to lie within 25 MeV/ $c^2$  of nominal  $K_s$  mass.

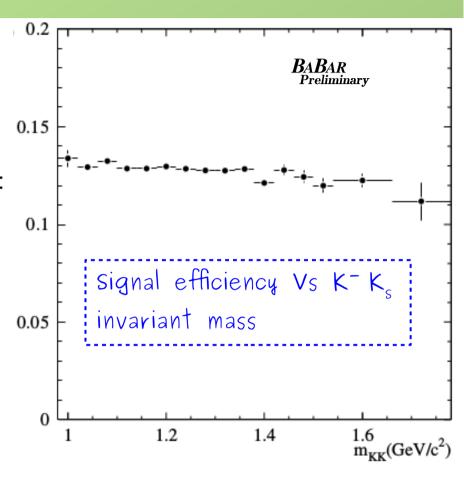
## **Event Selection (II)**

- The applied event selection corresponds to an average signal efficiency (computed on MC simulation) of 13%.
- The background mainly come from two sources:
  - $\rightarrow$  **T background**, T<sup>+</sup>T<sup>-</sup> events

Reduced by a factor of 3.5

ightarrow qq background,  $e^+e^ightarrow qq$  events

Reduced by a factor of 5.5



ightarrow The remaining background is subtracted, using both the data (sideband) or computing the expected amount of background events by exploiting previous measurements and MC simulations.







## **Background Subtraction**

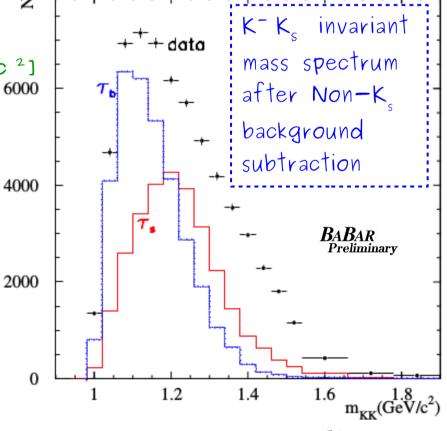
- 1) Non-K<sub>s</sub> background (combinatorial background) is subtracted using data and the MC simulation.
- $-N(N_{sb})$  = total number of events measured in data (in the sideband region only)
- $N_{KS}(N_b)$  = number of true (fake)  $K_s$  candidates of which a fraction  $\beta(\alpha)$  is estimated to be in the sideband region

$$N=N_{\rm K_S}+N_{\rm b},\ N_{\rm sb}=\varpi\ N_{\rm b}+\beta\ N_{\rm K_S}$$
 Signal region: [nominal K  $_{\rm s}$  mass ± 0.0125 GeV/c  $^2$  ]  $^{6000}$  Sideband region: otherwise

- 2) τ -background can be:
- without a π<sup>0</sup>

$$( au^- o \pi^- \, \mathsf{K}_{\mathsf{S}} \, \, \mathsf{v}_{\mathsf{\tau}} \, \, \mathsf{and} \, \, \mathsf{\tau}^+ o \pi^+ \, \, \bar{\mathsf{v}}_{\mathsf{\tau}})$$
:

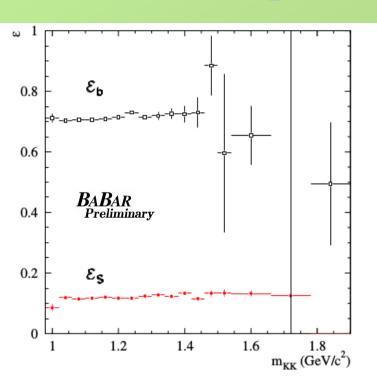
• their branching fractions are measured with precision better than  $2\% \to \text{contamination}$  computed from MC simulation and subtracted

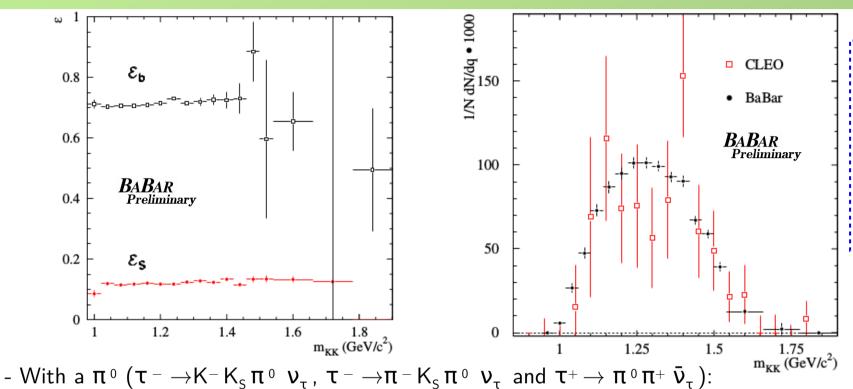






## τ-background Subtraction (II)





K- K invariant mass spectrum after t background subtraction

- generally measured with lower accuracy ( $\sim$ 5%)  $\rightarrow$  subtracted using *data* 
  - A  $\pi^{\,0}$  candidate is defined as a pair of photon whose invariant mass belongs to the range [100-160]  $MeV/c^2$
  - $N_s(N_b)$ ,  $\varepsilon_s(\varepsilon_b)$  = number of signal (background) events with at least one  $\pi^{\,0}$  candidate detected, and the corresponding detection efficiency evaluated on MC simualtion.

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$$N_{0\pi^0} = (1 - \epsilon_s) N_s + (1 - \epsilon_b) N_b$$
  

$$N_{1\pi^0} = \epsilon_s N_s + \epsilon_b N_b,$$





## Results & Summary (II)

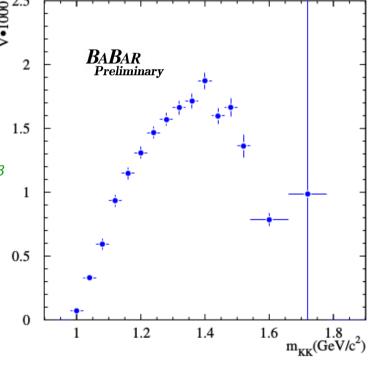
- Systematic uncertainties in the BF( $\tau \to K^- K_S \nu_\tau$ ) are estimated by:
  - varying the selection requirements
  - comparing MC-Data distributions (background subtraction contribution)
- The preliminary BF for the decay  $\tau \to K^-K_S \, \nu_\tau$  is in good agreement with the world average and of comparable accuracy. 
  0.70 
  0.9 
  nb

$$BF = N_{sig}/(arepsilon \ L \ BF_{lep} \sigma_{ au au}) = (0.740 \pm 0.011 \pm 0.021) imes 10^{-3}$$

• The *spectral function* 

$$V(q) = \frac{m_\tau^8}{12\pi C(q)|V_{\rm ud}|^2} \frac{\mathcal{B}(\tau^- \to K^- K_{\rm S} \nu_\tau)}{\mathcal{B}(\tau^- \to e^- \bar{\nu_e} \nu_\tau)} \frac{1}{N} \frac{dN}{dq}$$
 is computed from the measured K- K<sub>S</sub> invariant mass spectrum.











## Search for the B-meson decay to four baryons

#### Motivation

- B-mesons have large mass and they are able to decay to final states with baryons
  - → optimal tool for better understanding the mechanism of *hadronization into*baryons (theoretical models poorly understood) [\*\*]
- **Baryon puzzle**: inclusive BF  $(\sim7\%)$  ≠ Σ exclusive baryonic channels  $(\sim1\%)$
- Experimental features: **threshold enhancement** and **branching fraction hierarchy**

#### Previous measurement at BaBar:

• Upper limit on BF(  $\overline B{}^0\!\!\to\Lambda_{_c}^{^+}$  p  $\overline p$   $\overline p$  )  $< 2.8 \times 10^{\text{-6}}$  at 0.90 CL

(BABAR, Phys. Rev. D 89, 071102 (2014)

#### Estimate of the BF(B $^0\rightarrow p p p p$ ):

- ullet Cabibbo suppression, bightarrow u
- Phase space contribution, using the Q-values of the 2 reactions

#### **Working hypothesis:**

$$(B^0 \to pp\bar{p}\bar{p}) \approx BF^{UL}(\bar{B^0} \to \Lambda_c^+ \bar{p}p\bar{p}) \cdot \frac{|V_{ub}|^2}{|V_{cb}|^2} \cdot \frac{Q_{pp\bar{p}\bar{p}}}{Q_{\Lambda_c^+ p\bar{p}\bar{p}}} \sim 10^{-7}$$

First decay mode into four-baryon final state, no PDG limit yet!



[\*\*] V.L. Chernyak and I.R. Zhitnitsky, Nuclear Physics B, Vol. 345, 1 pp. 137-172 (1990); He Xiao-Gang, Li Tong, Li Xue-Qian and Wang Yu-Ming, Phys. Rev. D, 75, id. 034011 (2007).



### **Event Reconstruction**

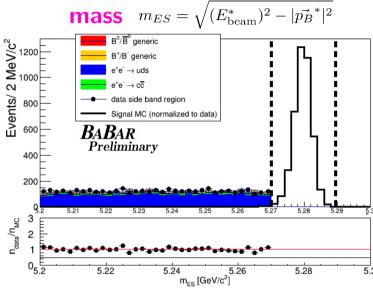
- Performed as <code>blind analysis</code>  $\to$  without looking at the <code>signal region</code> in data (5.27 <  $m_{ES}$  < 5.29  $\,$  GeV/c² )
- Sideband region data ( $\rm m_{ES} < 5.27~GeV/c^2)$  used to validate studies on background Monte Carlo samples

(*EvtGen* for generic B decays from  $\Upsilon(4S)$ , *JetSet* for continuum events)

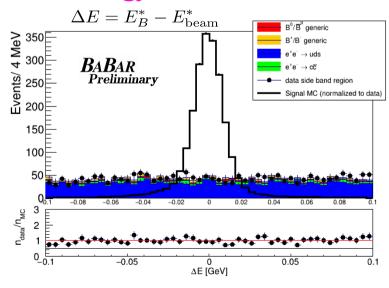
- Four oppositely charged tracks, coming from the Interaction Point, identified as two **protons** and two antiprotons
- Kinematic fit to the common vertex with a  $Prob(\chi^2) > 0.1\%$
- Loose cuts on kinematic variables



Beam energy substituted



#### Energy difference

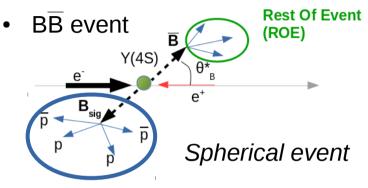


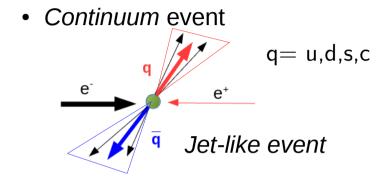




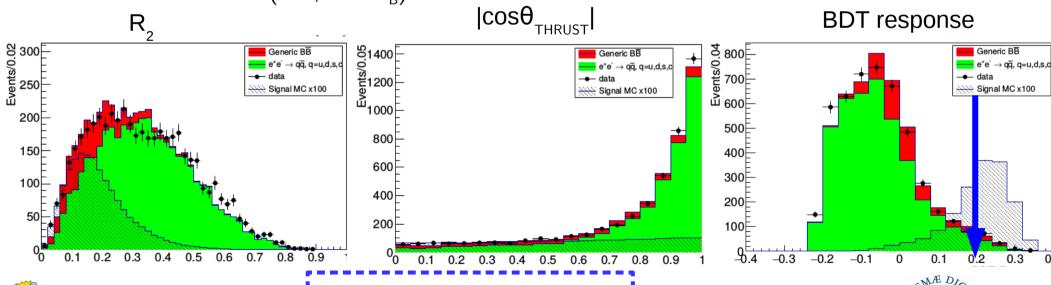
### **Event Selection**

 ${f P}$  Mainly  ${f combinatorial\ background\ }$  due to real protons from  ${\it continuum\ events}\ {f e^+e^-}
ightarrow {f qq}$ 





• Further rejection achieved by applying a signal-like selection on the output of a multivariate Boosted Decision Tree (BDT) algorithm, trained on **event shape variables** ( $R_2$ ,  $|\cos\theta_{THRUST}|$ ), on angular and kinematic variables ( $\Delta E$ ,  $\cos\theta_{B}^*$ ).





Signal efficiency  $\epsilon=21\%$ 

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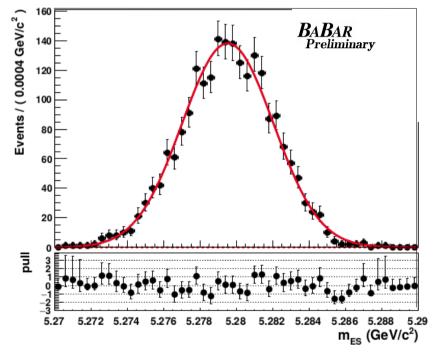
## Fitting Procedure

• The signal yield is extracted from an *unbinned* extended maximum likelihood fit to the data  $m_{ES}$  distribution, in the range  $5.2 < m_{ES} < 5.3 \text{ GeV/c}^2$ , after the BDT selection is applied.

$$\log L(N_{\text{sig}}, N_{\text{bkg}}; x) = -(N_{\text{sig}} + N_{\text{bkg}}) + \sum_{i=1}^{n} \log(N_{\text{sig}} \cdot f_{\text{sig}}(x_i) + N_{\text{bkg}} \cdot f_{\text{bkg}}(x_i))$$

- Signal PDF  $(f_{\scriptscriptstyle sig}) o {\sf Gaussian}$  function
- Background PDF  $(f_{bkg}) \rightarrow$  empirical ARGUS function, depending on 2 parameters: the *cutoff* (fixed to the endpoint 5.28 GeV/c<sup>2</sup> of the m<sub>ES</sub> distribution) and the **shape parameter**.
- The shape parameter, the background and signal yields  $(N_{bkg}, N_{sig})$  are extracted from the fit to the data.

#### Gaussian function fit to Signal MC









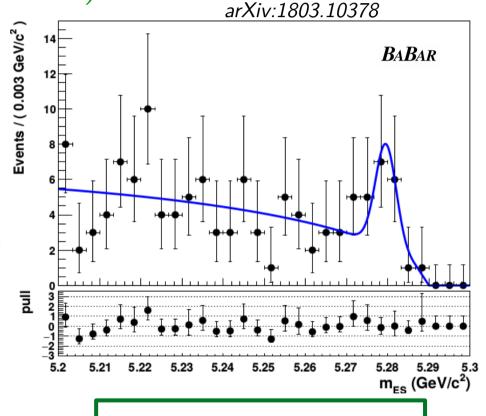
## Signal Yield Extraction and BF Estimate

The fit to the m $_{\rm ES}$  distribution gives  ${\sf N}_{\sf sig}=(11.1\pm4.6)$  , with a  $2.9\sigma$  significance

$$\rightarrow$$
 BF =  $(1.14 \pm 0.47 \pm 0.17) \times 10^{-7}$ 

- $\rightarrow$  The statistical uncertainty on  $N_{\text{sig}}$  is the main source of uncertainty on the BF.
- $\rightarrow$  Systematic uncertainties contribute as a further 15% relative uncertainty in the BF.

Variable	Source	Relative systematic
		uncertainty $(\%)$
$N_{B\overline{B}}$	B counting	0.6
$N_{ m sig}$	ARGUS cutoff	0.9
$\epsilon$	MC statistics	0.2
$\epsilon$	PID efficiency	0.9
$\epsilon$	Track finding efficiency	0.9
$\epsilon$	BDT selection	2.2
$\epsilon$	Decay model	14
Total		15



Bayesian upper limit at 90% CL:  $2 \times 10^{-7}$ 





## Summary (III)

SUBMITTED to PRD arXiv:1803.10378

- The analysis for the search of the BF(  $B^0 \rightarrow p p p$ ) has been performed on 471 million BB pairs at BaBar
  - → The first upper limit on this channel is set!

- 11 decay events with a significance of 2.9 standard deviations
- BF $^{UL} = 2 \times 10^{-7}$  at 90% CL







# Thanks for your attention.







## Backup: Measurement of the (D\*+(2010) – D+) mass difference







## Fitting Procedure Details

The total PDF corresponds to the sum of the signal and background PDFs :

$$S(\Delta m) = f_1 G(\Delta m; \Delta m_+ + \delta_{\Delta m_+}, \sigma_1)$$

$$+ (1 - f_1) \left[ f_2 CB(\Delta m; \Delta m_+ + \delta_{\Delta m_+}, \sigma_2, \alpha, n) + (1 - f_2) BfG(\Delta m; \Delta m_+ + \delta_{\Delta m_+}, \sigma_3^L, \sigma_3^R) \right],$$

$$T(\Delta m; \kappa) = \Delta m \sqrt{u} \exp(\kappa \cdot u)$$

o The fixed parameters in the fit to the data are the fraction  $f_1$ ,  $f_2$ , the CB tails parameters and the bias  $\delta_{\Delta m}$ 







### Results

• Sources of systematic uncertainty:

Detector effects not accounted for in the simulation

Rescaling technique for evaluating MC-Data differences

Source	$\Delta m_+$ systematic [keV]
Fit bias	1.7
$D^{*+}$ $p_{\text{lab}}$ dependence	5.0
$D^{*+}\cos\theta$ dependence	6.9
$D^{*+}$ $\phi$ dependence	0.0
$m(D_{\rm reco}^+)$ dependence	0.0
Diphoton opening angle dependence	6.1
Run period dependence	0.0
Signal model parametrization	2.1
EMC calibration	7.0
$MC \pi^0$ momentum rescaling	0.5
Total	12.9







## Backup: Measurement of the spectral function for the $\tau \to K_s K^- \nu_{\tau}$



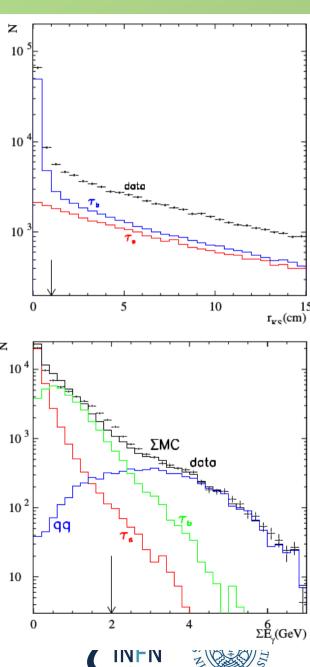




### The Event Selection

- Lepton candidate momentum (lab frame) > 1.2 GeV/c, (c.m. frame) < 4.5 GeV/c.
- $\text{Cos}\theta_{\text{l}} < 0.9$  , where  $\theta_{\text{l}}$  is the lepton polar angle is measured in the lab frame.
- $\bullet$  Charged kaon candidate momentum 0.4 < p  $_{\rm K}$  < 5 GeV/c.
- $-0.7374 < \cos \theta_{\kappa} < 0.9005$ , with  $\theta_{\kappa}$  the polar angle.
- K  $_S$  flight length  $r_{KS}$  , measured as a distance between the  $\pi^+\pi^-$  vertex and the K-  $K_S$  vertex, must be larger than 1 cm.
- $\Sigma E_{\gamma} <$  2 GeV, where  $\Sigma E_{\gamma}$  is the total energy of all photons with  $E_{\nu} >$  10 MeV found in the event.
- The thrust value is required to be T > 0.875.
- $\theta_{lh} > 110^{\circ}$ , where  $\theta_{lh}$  is the angle between the lepton and the K- K<sub>S</sub> system.





## Results

• Systematic uncertainties in the BF( $\tau \to K^- K_S \nu_{\tau}$ ):

Luminosity Requirement on the $K_s$ decay length Estimated by varying the selection	1.0
	0.4
	0.4
Requirement on the charged kaon momentum	0.9
Requirement on the lepton momentum  Criteria	0.5
Requirement on the lepton $\cos \theta$	0.6
Requirement on $\Sigma E_{\gamma}$ energy Dependent on the K-K <sub>s</sub>	1.0
Tracking efficiency	1.0
PID invariant mass	0.5
non- $K_{\rm S}$ background subtraction	0.4
$\tau^+\tau^-$ background without $\pi^0$ Evaluated as the observed difference in the	0.2
$\tau^+\tau^-$ background with $\pi^0$	1.6
$q\bar{q}$ background mass spectra between data and MC	0.5
total	2.8

 $\bullet$  Systematic uncertainties in the  $K^{\scriptscriptstyle -}\,K_{\scriptscriptstyle S}$  invariant mass spectrum:

$m_{K^-K_S}(GeV)$	$N_s/N_{tot} \times 10^3$	$V \times 10^3$
0.98 - 1.02	$5.6 \pm 1.4$	$0.071 \pm 0.018 \pm 0.007$
1.02 - 1.06	$26.0 \pm 2.7$	$0.331 \pm 0.034 \pm 0.030$
1.06 - 1.10	$46.0 \pm 3.2$	$0.593 \pm 0.042 \pm 0.052$
1.10 - 1.14	$70.8 \pm 3.5$	$0.934 \pm 0.046 \pm 0.065$
1.14 - 1.18	$84.4 \pm 3.4$	$1.148 \pm 0.047 \pm 0.069$
1.18 - 1.22	$92.3 \pm 3.3$	$1.309 \pm 0.046 \pm 0.065$
1.22 - 1.26	$98.2 \pm 3.2$	$1.468 \pm 0.048 \pm 0.059$
1.26 - 1.30	$98.4 \pm 3.2$	$1.569 \pm 0.050 \pm 0.063$
1.30 - 1.34	$96.3 \pm 3.0$	$1.663 \pm 0.052 \pm 0.050$
1.34 - 1.38	$90.2 \pm 2.9$	$1.715 \pm 0.052 \pm 0.052$
1.38 - 1.42	$87.8 \pm 3.1$	$1.873 \pm 0.066 \pm 0.056$
1.42 - 1.46	$65.1 \pm 2.6$	$1.597 \pm 0.064 \pm 0.043$
1.46 - 1.50	$57.3 \pm 2.5$	$1.6665 \pm 0.073 \pm 0.042$
1.50 - 1.54	$38.1 \pm 2.5$	$1.361 \pm 0.090 \pm 0.032$
1.54 - 1.66	$3 \times (12.3 \pm 0.8)$	$0.785 \pm 0.049 \pm 0.016$
1.66 - 1.78	$3 \times (2.2 \pm 3.4)$	$0.986 \pm 1.52 \pm 0.020$



## Backup: Search for the B-meson decay to four baryons



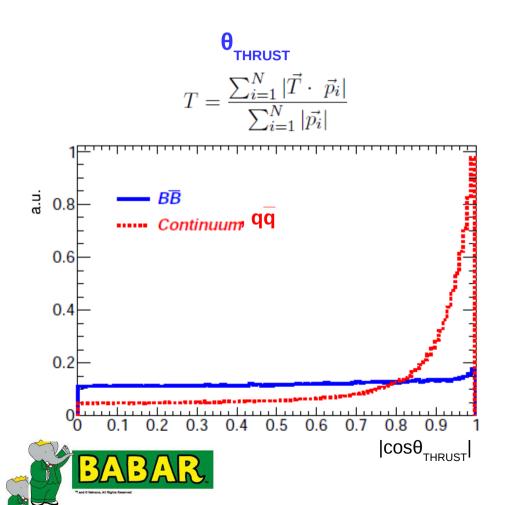


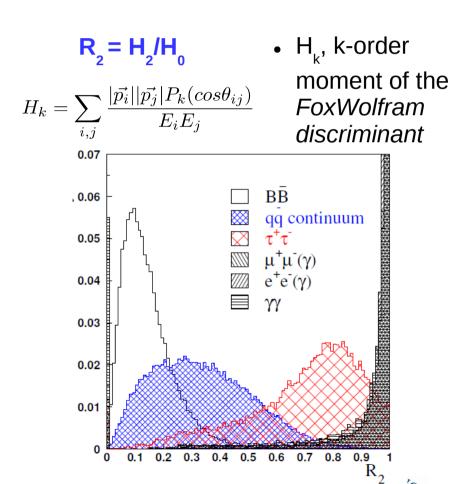


## Event shape variables

### **Shape variables:** $\boldsymbol{\theta}_{\text{THRUST}}$ , $R_2$

- $\theta_{\text{THRUST}}$ , angle between the *thrust axis* of the  $B_{\text{sig}}$  and that of ROE.
- R<sub>2</sub> provides information about particle direction correlations.





## Systematic uncertainties



- BB pairs: calculated from the B counting method
- Systematic uncertainty  $\sim 1\%$  ( mainly due to the hadronic event selection efficiency)



- Signal pdf choice
- Shape parameter estimates

ightarrow Evaluated by letting them vary in their uncertainty ranges.



- The MC-data differences are the major source of systematic uncertainty on signal selection efficiency, coming from:
  - 1) Tracking (1%)
  - 2) PID (**0.86%**)

Weighting technique

- 3) BDT (**2.2%**)
- 4) Decay model implemented in the Signal MC generation (14%)



## BDT uncertainty study

#### Weighting technique

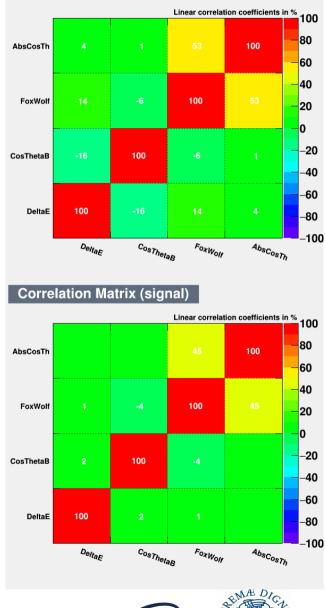
for each input variable distribution, BEFORE THE BDT, define bin by bin weights comparing background MC-data samples:

$$w_i = \frac{n_i^{data}}{n_i^{\text{bkgMC}}} \cdot C$$

- ^ Apply the weights to the Signal MC distribution for the given variable AFTER THE BDT  $\rightarrow$  recalculate efficiency  $\rightarrow$  take as uncertainty the difference between un-weighted and weighted efficiency.
- Uncertainty contributions from all the 4 input variables are summed in quadrature, taking into account the correlation coefficients.

BDT relative uncertainty on  $\varepsilon = 2.2\%$ 





Correlation Matrix (background)





## Decay model uncertainty study

- There are no specific four-body baryonic decay models currently known
- DEFAULT implemented in simulated signal MC: **Phase space model**, meaning proton momentum probability is flat in the phase space.
- NO PROTON RELATED VARIABLES (momentum, energy, angular distributions) directly
  exploited in the analysis might relax the selection efficinecy dependence on the decay model
- However, systematic studies show the expected contribution from the decay model to the relative uncertainty on BF is 14%

Implemented with the **re-weighting technique**: based on the comparison between the resulting proton momentum spectra from *2 different decay models*:

- Default (phase space)
- Assuming a different decay model (e.g., intermediate resonances:  $B \to XX(\to pp)$ )

Weights: bin by bin, normalized ratio of the new spectrum to the default one.

Weights are applied to the signal MC sample after the BDT cut  $\rightarrow$  the difference in the efficiencies with/without weights is assumed as systematic uncertainty.







## Signal MC: proton momentum distributions

