

# Towards universal fit of parton distributions and fragmentation functions

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# Motivations

- SIDIS data from JLab 12 brings new challenges to understand the microscopic nature of  $e + P$  reactions
  - + It demands to know the limits in  $x$  and  $Q^2$  where factorization theorems are applicable  $\rightarrow$  opens up the possibility to extend, modify existing approximations
  - + Tests on universality of non perturbative objects associated with nucleon structure and hadronization
- To study the data one needs to have self consistent tools
  - + A framework that analyzes the data with the same theoretical assumptions  $\rightarrow$  simultaneous extraction of all non perturbative functions
  - + A framework that integrates collinear physics and TMDs is needed to reliably understand SIDIS
- As a first step we explore a combined unpolarized PDF and fragmentation function analysis

# Setup

## ■ Data sets

- + All inclusive DIS with  $Q^2 > m_c^2$  and  $W^2 > 10\text{GeV}^2$
- +  $pp$  and  $pd$  DY data from E866
- + SIDIS  $\pi^\pm$  and  $K^\pm$  multiplicities
- + All inclusive SIA ( $e^+e^- \rightarrow h + X$ ) data + HQ tagged data

## ■ Theory assumptions

- + All observables computed at NLO in pQCD
- + We work in Mellin space with truncated DGLAP evolution and numerically solved  $\alpha_S$
- + DIS structure functions computed at leading twist
- + Nuclear smearing for deuterium DIS
- + We use ZMVF
- + To describe SIA tagged data we fit HQ FFs

## ■ Likelihood analysis

- + For the results presented here we use maximum likelihood and resampling
- + Final analysis will be done using Nested Sampling

# Setup

- Parametrization  $\rightarrow$  generic template functions

$$T(\xi; \mathbf{a}) = N \frac{\xi^a (1 - \xi)^b (1 + c\sqrt{\xi} + d\xi)}{B(2 + a, b + 1) + cB(5/2 + a, b + 1) + dB(3 + a, b + 1)}$$

- For PDFs 13 parameters

- +  $g, u_v, d_v, \bar{u}, \bar{d}, s = \bar{s}$

- + momentum sum rules and quark number sum rule

- For FFs  $\pi^+$  16 parameters

- +  $g, u(\text{fav.}), d(\text{ufav.}), c, b$

- +  $u = \bar{d}, d = \bar{u} = s = \bar{s}$

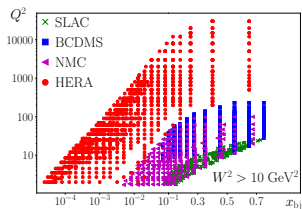
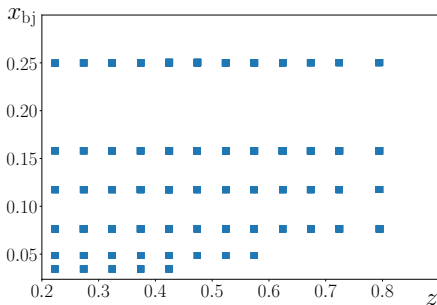
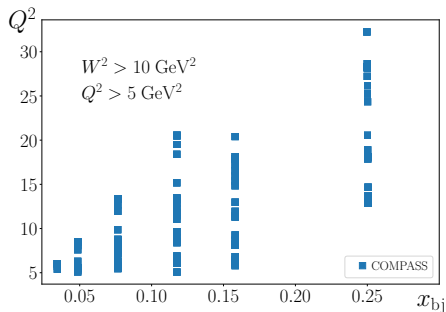
- For FFs  $K^+$  15 parameters

- +  $g, u(\text{fav.}), d(\text{unf.}), \bar{s}(\text{fav.}), c, b$

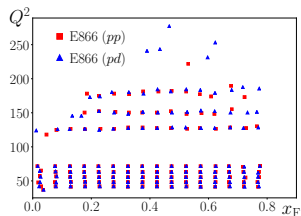
- +  $d = \bar{d} = \bar{u} = s$

# Data Kinematics

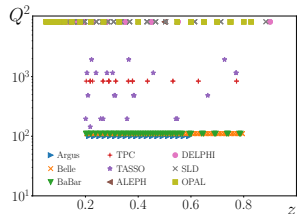
SIDIS (COMPASS)



DIS

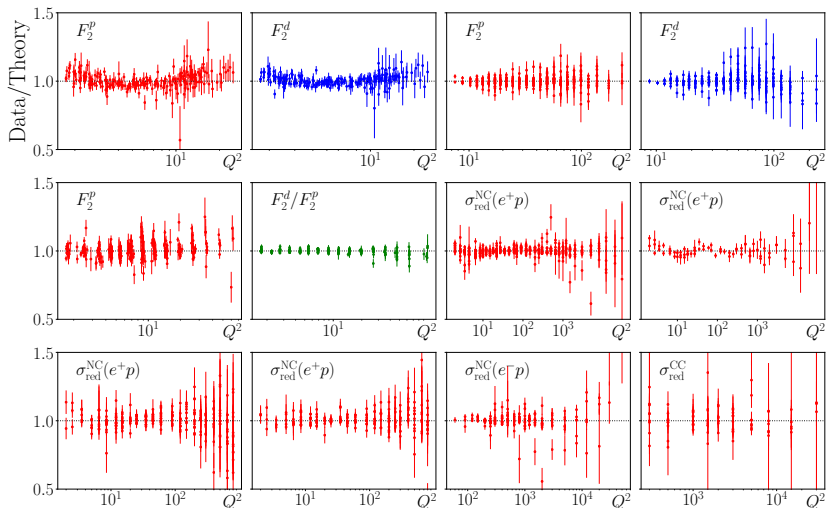


DY



SIA

# Inclusive DIS: $l + (p, d) \rightarrow l' + X$

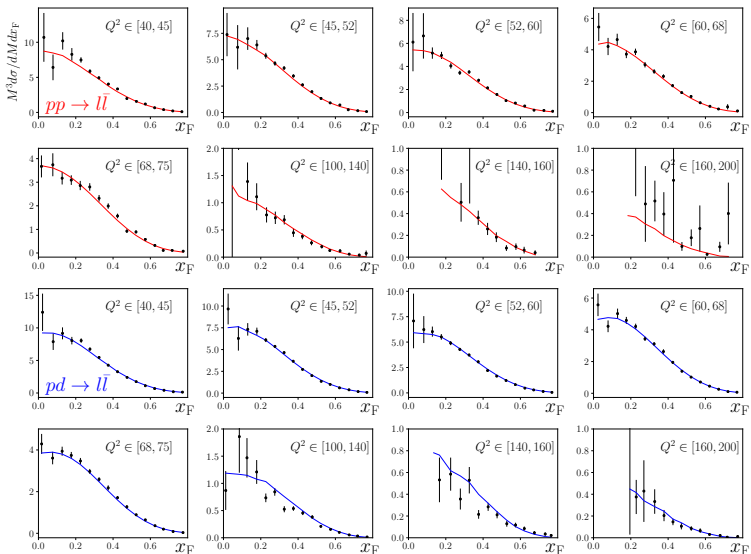


tar	col	npts	$\chi^2$	$\chi^2/\text{npts}$	$\chi^2\text{-npts}$
$p$	BCDMS	348	375	1.1	27
$d$	BCDMS	254	280	1.1	26
$p$	NMC	273	499	1.8	226
$d/p$	NMC	174	172	1.0	-2
$p$	SLAC	218	300	1.4	82
$d$	SLAC	228	231	1.0	3

tar	col	npts	$\chi^2$	$\chi^2/\text{npts}$	$\chi^2\text{-npts}$
$p$	HERA	402	627	1.6	225
$p$	HERA	75	93	1.2	18
$p$	HERA	259	265	1.0	6
$p$	HERA	209	231	1.1	22
$p$	HERA	159	261	1.6	102

tar	col	npts	$\chi^2$	$\chi^2/\text{npts}$	$\chi^2\text{-npts}$
$p$	HERA	39	44	1.1	5
$p$	HERA	42	48	1.1	6

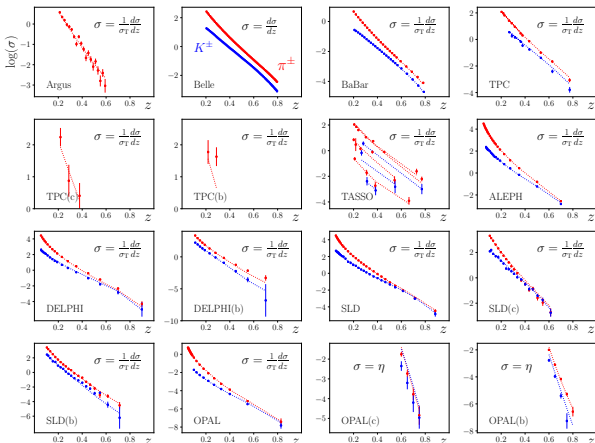
# Lepton pair production: $p + (p, d) \rightarrow \bar{l}l + X$



tar	col	npts	chi2	chi/npts	chi2-npts
pp	E866	121	169	1.4	48.07
pd	E866	129	169	1.3	40.07

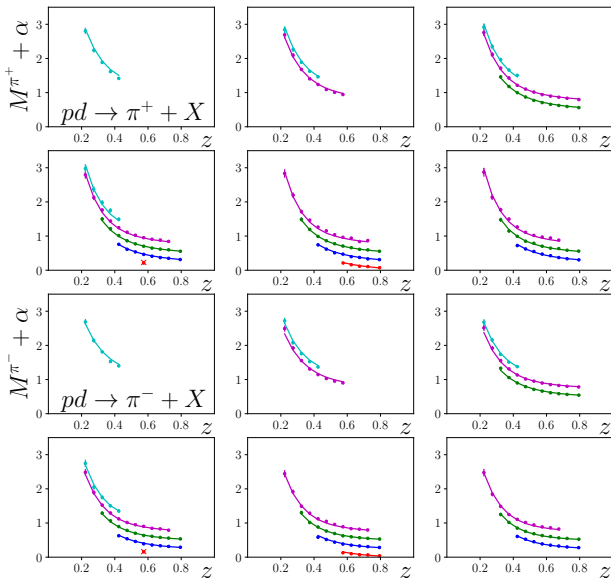
# SIA: $e^+e^- \rightarrow (\pi^\pm, K^\pm) + X$

rs	col	had	npts	$\chi^2$	$\chi^2/npts$	$\chi^2-npts$
12	TASSO	pion	1	0.8	0.8	-0.2
14	TASSO	pion	4	12.3	3.1	8.3
22	TASSO	pion	4	2.9	0.7	-1.1
34	TASSO	pion	5	7.6	1.5	2.6
44	TASSO	pion	3	5.4	1.8	2.4
29	TPC	pion	3	0.9	0.3	-2.1
29	TPC	pion	9	4.8	0.5	-4.2
29	TPC(c)	pion	3	1.5	0.5	-1.5
29	TPC(b)	pion	2	4.8	2.4	2.8
58	TOPAZ	pion	1	0.1	0.1	-0.9
91	SLD	pion	29	31.2	1.1	2.2
91	SLD(c)	pion	19	63.8	3.4	44.8
91	SLD(b)	pion	20	19.8	1.0	-0.3
91	ALEPH	pion	22	40.6	1.8	18.6
91	OPAL	pion	22	46.5	2.1	24.5
91	OPAL(c)	pion	4	15.3	3.8	11.3
91	OPAL(b)	pion	5	11.0	2.2	6.0
91	DELPHI	pion	17	25.9	1.5	8.9
91	DELPHI(b)	pion	11	15.4	1.4	4.4
11	BABAR	pion	25	20.1	0.8	-5.0
11	BELLE	pion	60	25.9	0.4	-34.1
10	ARGUS	pion	20	37.3	1.9	17.3
14	TASSO	kaon	2	4.1	2.1	2.1
22	TASSO	kaon	2	0.2	0.1	-1.9
34	TASSO	kaon	2	0.1	0.1	-1.9
29	TPC	kaon	2	7.3	3.7	5.3
29	TPC	kaon	7	13.9	2.0	6.9
58	TOPAZ	kaon	1	0.2	0.2	-0.8
91	SLD	kaon	29	20.1	0.7	-8.9
91	SLD(c)	kaon	19	46.1	2.4	27.1
91	SLD(b)	kaon	20	54.8	2.7	34.8
91	ALEPH	kaon	18	7.7	0.4	-10.3
91	OPAL	kaon	10	6.0	0.6	-4.0
91	OPAL(c)	kaon	4	55.3	13.8	51.3
91	OPAL(b)	kaon	5	39.8	8.0	34.8
91	DELPHI	kaon	17	20.6	1.2	3.6
91	DELPHI(b)	kaon	11	4.4	0.4	-6.6
11	BABAR	kaon	26	10.7	0.4	-15.3
11	BELLE	kaon	60	14.9	0.3	-45.2





# SIDIS: $l + d \rightarrow l' + \pi^\pm + X$

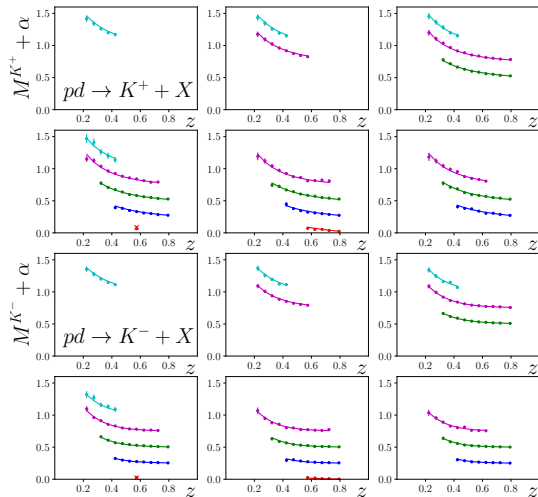


tar	had	col	npts	$\chi^2$	$\chi^2$ -npts	$\chi^2$ /npts
d	$\pi^-$	COMPASS	142	175	33	1.23
d	$\pi^+$	COMPASS	142	158	16	1.11
d	$K^-$	COMPASS	141	67	-74	0.48
d	$K^+$	COMPASS	141	70	-71	0.5

- $\alpha$  is use to offset the data
- Difficulty in fitting all the low  $Q^2$  data. Only  $Q^2 > 5\text{GeV}^2$  included

—  $y \in [0.10, 0.15], \alpha = 0.00$       —  $y \in [0.20, 0.30], \alpha = 0.50$   
—  $y \in [0.15, 0.20], \alpha = 0.25$       —  $y \in [0.30, 0.50], \alpha = 0.75$

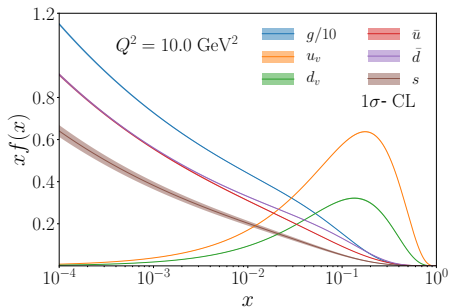
# SIDIS: $l + d \rightarrow l' + K^\pm + X$



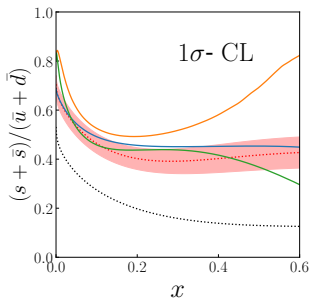
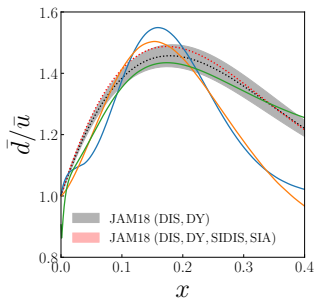
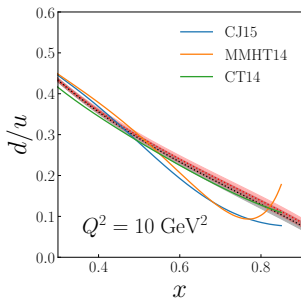
—  $y \in [0.10, 0.15], \alpha = 0.00$      —  $y \in [0.20, 0.30], \alpha = 0.50$   
—  $y \in [0.15, 0.20], \alpha = 0.25$      —  $y \in [0.30, 0.50], \alpha = 0.75$

tar	had	col	npts	$\chi^2$	$\chi^2$ -npts	$\chi^2$ /npts
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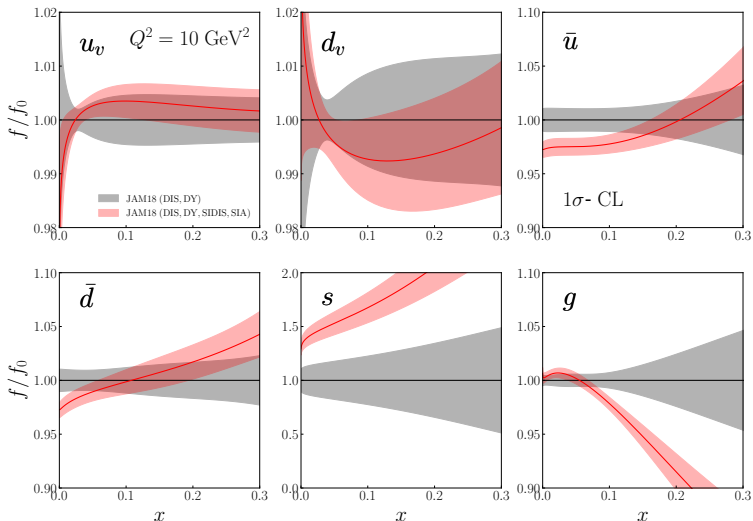
# PDFs (preliminary)



- + consistent with previous analyses  $\bar{d} - \bar{u}$  except at large  $x$  JAM18 predicts large asymmetry at large  $x$  to be tested by SeaQuest data
- + SIDIS data supports the strange suppression

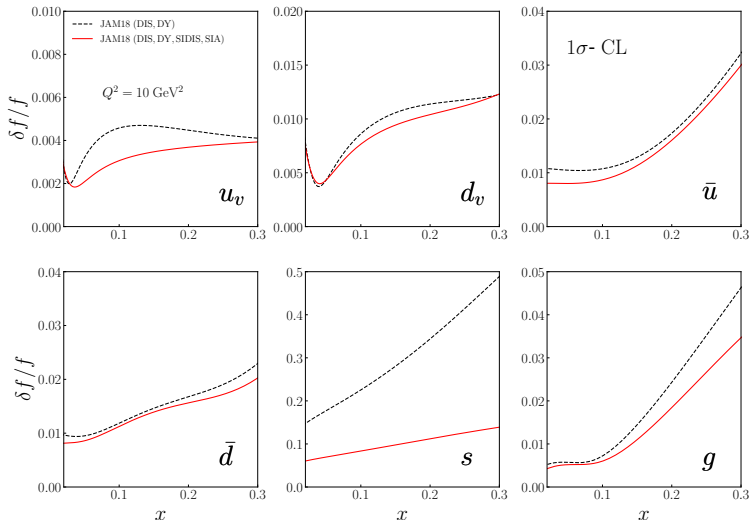


# PDFs: impact of SIDIS (preliminary) $f_0$ : central JAM18 DIS+DY PDFs



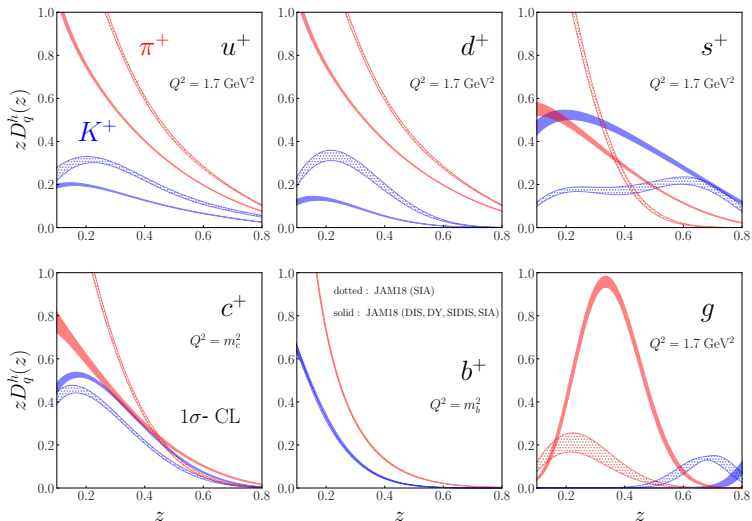
- + The gluon distribution seems to change significantly with the inclusion of SIDIS

# PDFs: uncertainties after SIDIS (preliminary)



- + As expected, inclusion of  $K$  data decreases significantly uncertainties on the strange distribution

# FFs: impact of SIDIS (preliminary)



+ Flavor decomposition of FFs changes significantly if SIDIS data is included

# Summary and outlook

- Preliminary analysis of combined DIS, SIDIS and SIA
  - + It is possible to fit simultaneously PDFs and FFs using DIS, SIDIS and SIA
  - + SIDIS Kaon data provides significant constraints on the strange distribution → It support the strange suppression for PDFs
  - + Flavor decomposition of FFs is significantly affected by SIDIS data in comparison with SIA only analysis
  - + Difficulties in incorporating low  $Q^2 < 5\text{GeV}^2$  data → it suggests that power corrections in SIDIS shows up at higher  $Q^2$  values than in DIS
- To do list:
  - + Inclusion of HQ treatment especially for low  $Q^2$  and low  $x$  HERA data
  - + Release the  $s = \bar{s}$  constraint since SIDIS  $K$  can discriminate  $s$  from  $\bar{s}$  → needs to be done using MC approach
  - + Inclusion of polarized DIS and SIDIS and extract  $\Delta$ PDFs in addition to PDFs and FFs → unpolarized SIDIS can affect polarized SIDIS asymmetries