# CLIC DR design using variable bends and high-field wigglers

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#### **Outline**

- Optimization of the arc TME cell
  - -Longitudinally variable bends
  - -Parametrization with the drift space lengths and with the phase advances
- Optimization of the wiggler FODO cell
  - -A high field wiggler
- Design parameters of the main CLIC DRs
- Magnet design based on the characteristics of the variable bends for the CLIC DR dipoles

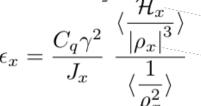
The longitudinal variable bends can give lower emittances than a uniform dipole of the same bending angle [1].

Longitudinally variable bends bends than the second bends 
$$\epsilon_x = \frac{C_q \gamma^2}{J_x} \sqrt{\frac{\frac{\mathcal{H}_x}{|\rho_x|^3}\rangle}{\frac{1}{\langle \frac{1}{\rho_x^2}\rangle}}}$$
 Dispersion invariant parameters and Bending radius

■ Dispersion invariant, determined by the Twiss parameters and the dispersion function

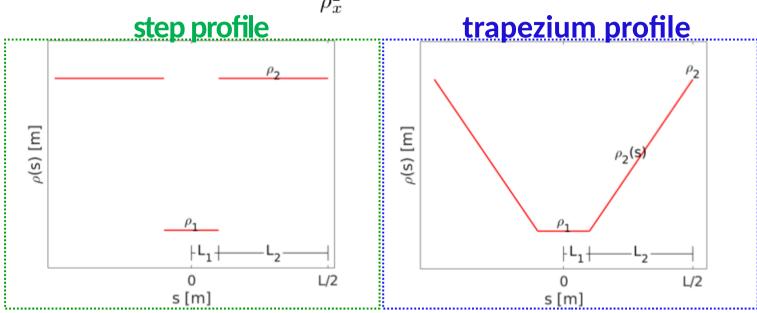
Longitudinally variable bends

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Dispersion invariant, determined by the Twiss parameters and the dispersion function

►Bending radius



# Longitudinally variable bends

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■ Dispersion invariant, determined by the Twiss parameters and the dispersion function

L/2

► Bending radius

step profile trapezium profile

#### Bending radii ratio

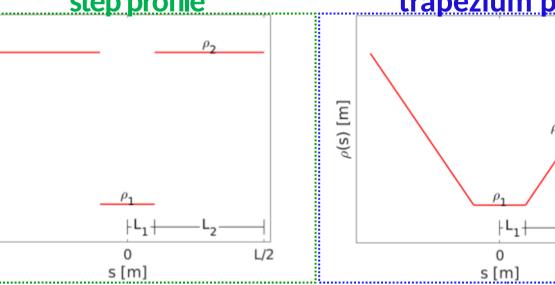
$$\rho = \frac{\rho_1}{\rho_2}$$

#### Lengths ratio

$$\lambda = \frac{L_1}{L_2}$$

#### **Emittance** reduction factor

$$F_{TME} = \frac{\epsilon_{TME_{uni}}}{\epsilon_{TME_{var}}}$$
$$F_{TME} > 1$$



# Longitudinally variable bends pends $\frac{\mathcal{H}_x}{\mathcal{H}_x}$ Dispersion invariants

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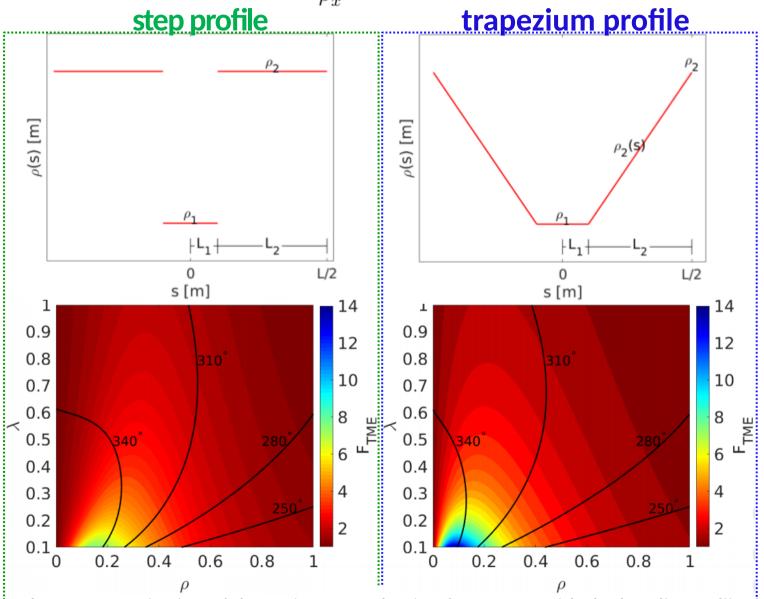
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# Emittance reduction factor

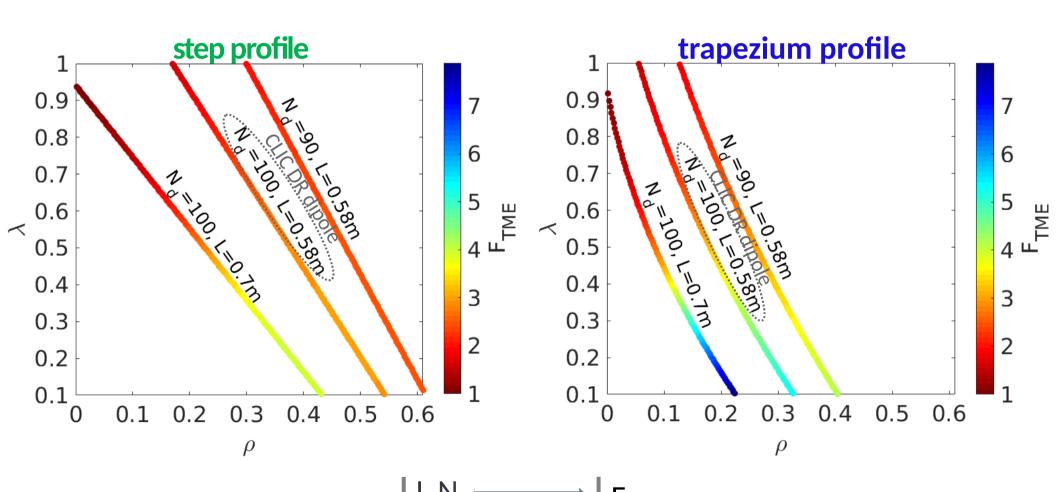
$$F_{TME} = \frac{\epsilon_{TME_{uni}}}{\epsilon_{TME_{var}}}$$
$$F_{TME} > 1$$

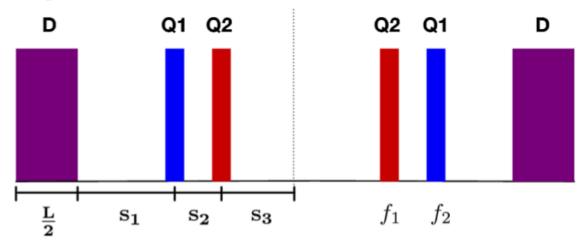


The parameterization of the emittance reduction factor FTME with the bending radii ratio  $\rho$  and the lengths ratio  $\lambda$ , for  $\lambda>0.1$ .

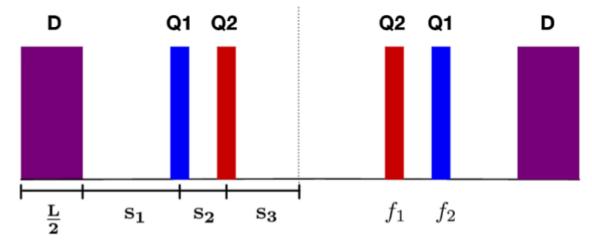
# Fixing the dipole's characteristics (bending angle, length and minimum bending radius)

$$\theta_{step} = \underbrace{\frac{L(\lambda + \rho)}{\rho_1(1 + \lambda)}}_{\rho_1(1 + \lambda)} + \lambda(\rho) \text{ or } \rho(\lambda) \xrightarrow{\mathsf{Ftme}(\rho, \lambda)}_{\rho_1(-1 + \rho)(1 + \lambda)} + \lambda(\rho) \text{ or } \rho(\lambda) \xrightarrow{\mathsf{Ftme}(\rho, \lambda)}_{\rho_1(-1 + \rho)(1 + \lambda)}$$



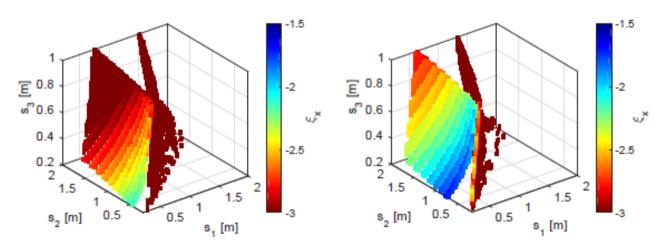


Fix the dipoles' characteristics in order to get a large  $F_{TME}$ 

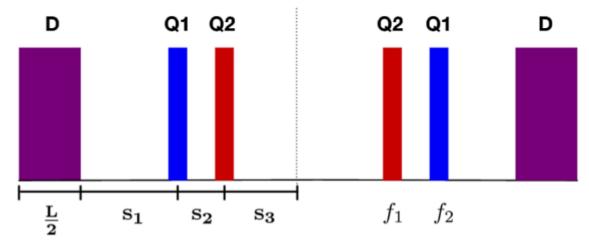


Fix the dipoles' characteristics in order to get a large  $F_{\text{TME}}$ 

Find the lengths of the elements and of the drifts that result in a compact cell



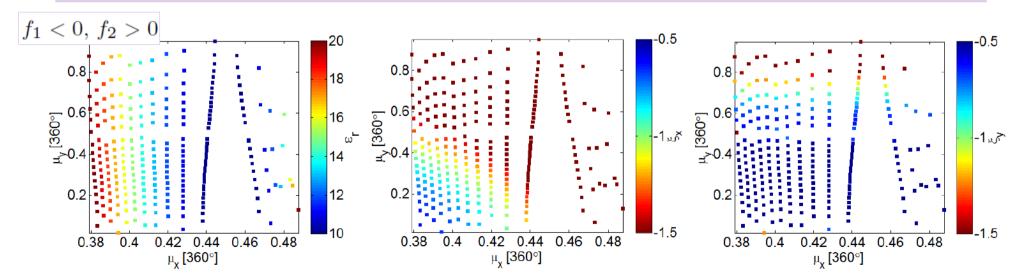
The horizontal chromaticity  $\xi_x$  is parameterized with the drift lengths  $s_1$ ,  $s_2$ ,  $s_3$  for the TME, for the step (left) and the trapezium (right) profile



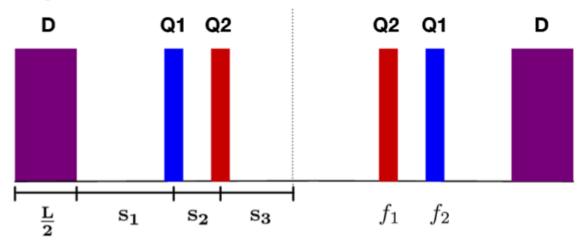
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Find the lengths of the elements and of the drifts that result in a compact cell

Find the optimal phase advances that give the required emittance, chromaticities, quadrupole strengths



The parameterization of the detuning factor  $\varepsilon_r$  ( $\varepsilon_r = \varepsilon_x/\varepsilon_{TME}$ ) and of the horizontal and vertical chromaticities ( $\xi_x$  and  $\xi_y$ ) with the horizontal and vertical phase advances  $\mu_x$  and  $\mu_y$ , only for the trapezium profile.



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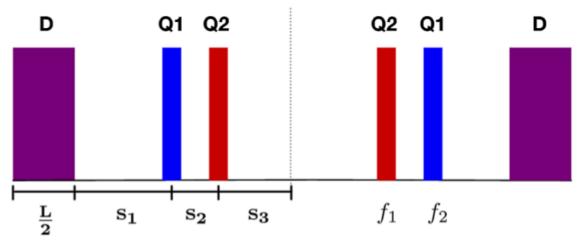
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Find the optimal phase advances that give the required emittance, chromaticities, quadrupole strengths

$$\frac{\epsilon_{var}}{\epsilon_{uni}} < 1$$

$$\frac{\epsilon_{var}}{\epsilon_{uni}} = \frac{\epsilon_{r_{var}} \epsilon_{TME_{var}}}{\epsilon_{r_{uni}} \epsilon_{TME_{uni}}} = \frac{\epsilon_{r_{var}}}{\epsilon_{r_{uni}}} \frac{1}{F_{TME}}$$

$$\frac{\epsilon_{r_{var}}}{\epsilon_{r_{uni}}} < F_{TME}$$



Fix the dipoles' characteristics in order to get a large  $F_{TMF}$ 

Find the lengths of the elements and of the drifts that result in a compact cell

Find the optimal phase advances that give the required emittance, chromaticities, quadrupole strengths

$$\frac{\epsilon_{var}}{\epsilon_{uni}} < 1$$

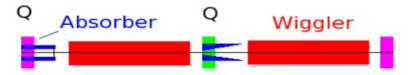
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$$\frac{\epsilon_{r_{var}}}{\epsilon_{r_{uni}}} < F_{TME}$$

For optimized variable bends characteristics, lower emittances than the ones of the current design are reached. This gives us the flexibility to reduce the existing TME cells of the arcs, till the point we get the required output parameters.

The optimal solutions are found to be  $N_d$ =96 for the step and  $N_d$ =90 for the trapezium profile, instead of the existing arc's cell that are  $N_d$ =100.

### Optimization of the wiggler FODO cell



Results obtained after the optimization of the arc TME cell.



When increasing the wigglers' peak field  $B_w$  up to a certain point, the emittance and the IBS effect are lowered [2].

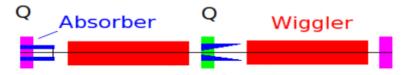


Based on the technological restrictions, a new working point for the damp. wiggler is proposed to be at 3.5T (prev. 2.5T), with 49mm period length [3].



Removing some FODO cells from the existing straight section (N<sub>FODO</sub>=13 per section) is possible.

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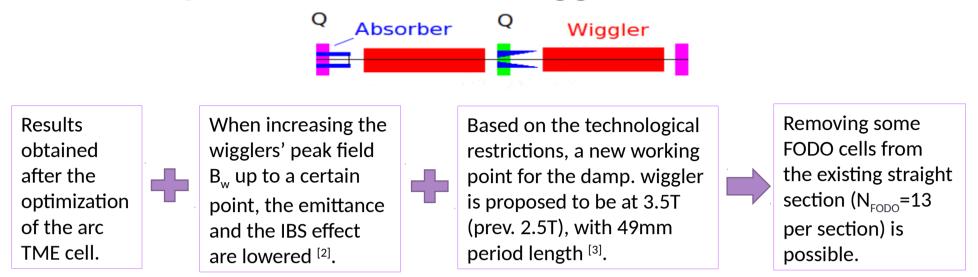
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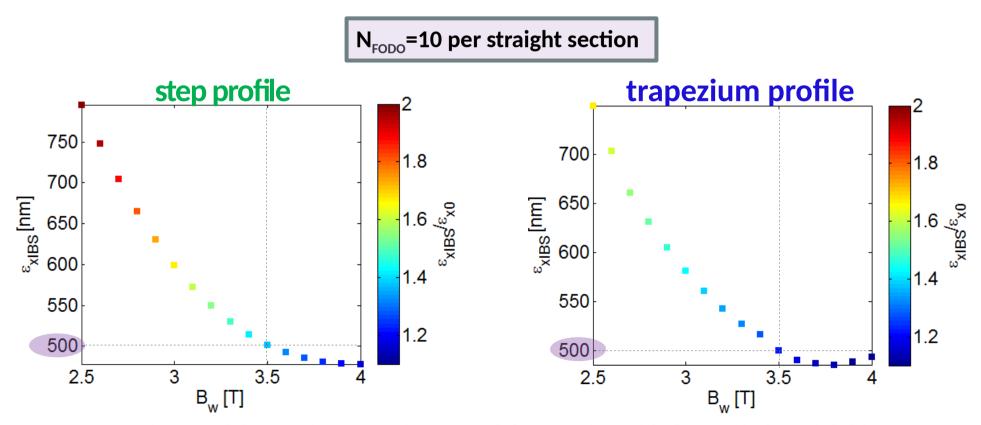


Removing some FODO cells from the existing straight section (N<sub>FODO</sub>=13 per section) is possible.

N<sub>FODO</sub>=10 per straight section

### Optimization of the wiggler FODO cell





Parametrization of the steady state emittance and the IBS effect with the wiggler's peak field  $B_{\rm w}$ 

## Design parameters for the main DRs, E=2.86 GeV, 2GHz

Nb=4.07e+09

Nb=5.7e+09

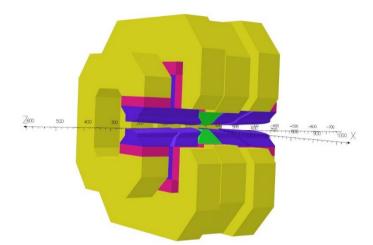
Parameters, Symbol [Unit]	uniform	step	trapezium	trapezium
Number of arc TME cells/wigglers	100/52	96/40	90/40	90/40
Dipole field (max/min), B [T]	0.97/0.97	1.77/1.01	1.77/0.73	1.77/0.73
horiz. /vert. chromaticities $\xi_x/\xi_y$	-113/-82	-135/-76	-126/-72	-134/-41
Wiggler peak field $B_w$ [T] for length $L_w$ =2m	2.5	3.5	3.5	3.5
Wiggler period, $\lambda_{_{w}}$ [cm]	5.0	4.9	4.9	4.9
Mom. compaction, $\alpha_{_{c}}$ [10 <sup>-4</sup> ]	1.3	1.3	1.2	1.2
Energy loss/turn, U [MeV/turn]	4	5.7	5.7	5.8
Energy spread (rms), $\sigma_{\delta}$ [%]	0.12	0.13	0.13	0.13
Bunch length (rms), $\sigma_{_{\! s}}$ [mm]	1.8	1.6	1.6	1.3
Long. emittance , $\epsilon_{\rm l}$ [keV m]	5.9	6.1	6.0	5.0
Damp. times, $(\tau_x, \tau_y, \tau_l)$ [ms]	(2.0, 2.0, 1.0)	(1.2, 1.3, 0.6)	(1.2, 1.2, 0.6)	(1.2, 1.2, 0.6)
IBS factors hor./ver./long.	2.2/1.5/1.2	1.4/1.5/1.1	1.4/1.5/1.1	1.4/2.0/1.1
Norm. horizontal emittance (with IBS), $\gamma \varepsilon_{_{\mathrm{x}}}$ [nm]	681	502	500	579
Norm. vertical emittance (with IBS), $\gamma \epsilon_{_{y}}$ [nm]	5	5	5	6.7
Circumference, C [m]	427.5	374.1 (-14%)	359.4 (-19%)	359.4 (-19%)

<sup>-</sup> S. Papadopoulou, F. Antoniou and Y. Papaphilippou, Alternative optics design of the CLIC Damping Rings with variable dipole bends and high-field wigglers, IPAC'15

<sup>-</sup>H. Ghasem et al., Nonlinear Optimization of CLIC DRS New Design with Variable Bends and High Field Wigglers, IPAC'16

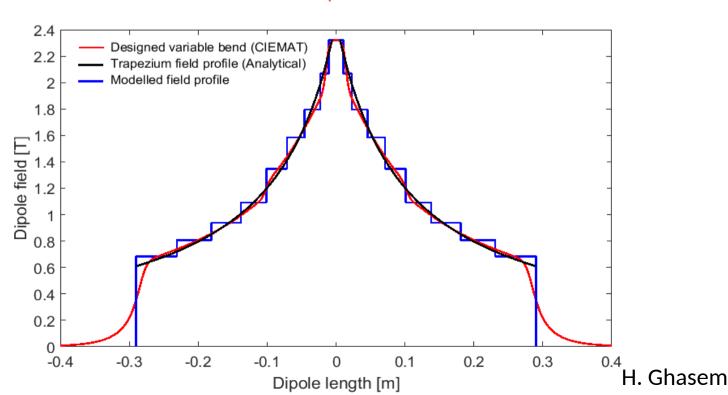
# Magnet design based on the characteristics of the variable bends for the CLIC DRs

- -Based on the trapezium profile, the designed dipole has a total length of 56 cm and bends the beam by 4 degrees.
- A maximum field of 2.3 T is reached. The  $\lambda$  and  $\rho$  values achieved are 0.04 and 0.29 respectively, corresponding to a  $F_{TME}$ =7.





M. A. Domínguez, F. Toral (CIEMAT, Spain) see "Design of a Variable bend prototype", CLIC workshop 2018 https://indico.cern.ch/event/656356/contributions/2838073/

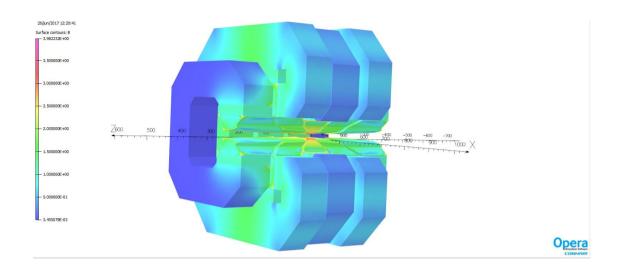


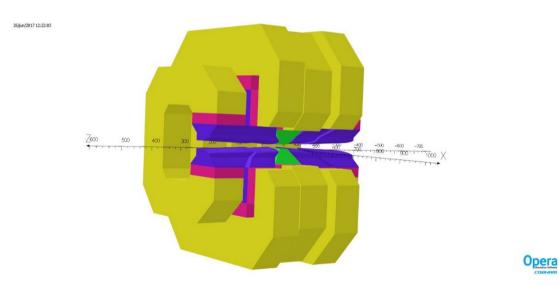
#### References

- [1] -J. Guo and T. Raubenheimer, proc. of EPAC 2002, Paris (2002).
  - -Y. Papaphilippou, P. Elleaume, PAC 2005, Knoxville (2005).
  - -R. Nagaoka, A.F. Wrulich, Nucl. Instrum. Methods Phys. Res., Sect. A 575, 292 (2007).
  - -C.-x Wang, PRST-AB 12, 061001 (2009).
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  - -S. Papadopoulou, F. Antoniou and Y. Papaphilippou, Alternative optics design of the CLIC Damping Rings with variable dipole bends and high-field wigglers, proc. of IPAC'15
- [2] -F. Antoniou, PhD thesis, NTUA, (2013)
  - -D. Schoerling et al, PRST-AB 15, 042401 (2012).
- [3] L. Garcia Fajardo, "Nb3Sn prototype progress", CLIC Workshop, CERN, Geneva (2015).

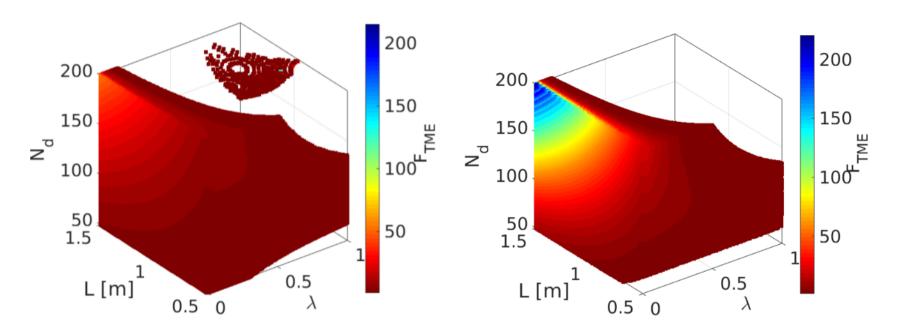
Thank you!

# Magnet design based on the characteristics of the variable bends for the CLIC DRs

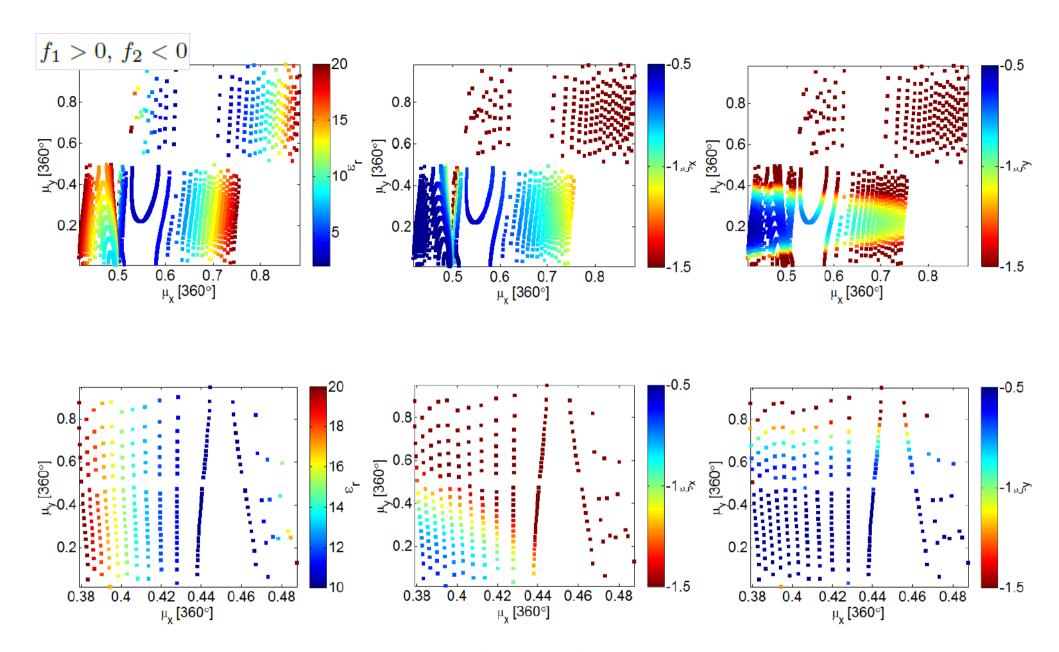




- -Armco (pure iron) for the yokes, low and medium field poles
- -Iron-cobalt in the high field pole
- -SmCo in the low field permanent magnet
- -NdFeBo in the medium and high field permanent magnets



The parameterization of the emittance reduction factor FTME with the lengths ratio  $\lambda$ , the dipole length L and the number of dipoles used N<sub>d</sub> for the step (left) and the trapezium (right) profile.



The parameterization of the detuning factor  $\varepsilon_r$  ( $\varepsilon_r = \varepsilon_x/\varepsilon_{\text{TME}}$ ) and of the horizontal and vertical chromaticities  $\xi_x$  and  $\xi_y$  with the horizontal and vertical phase advances  $\mu_x$  and  $\mu_y$ , only for the trapezium profile.