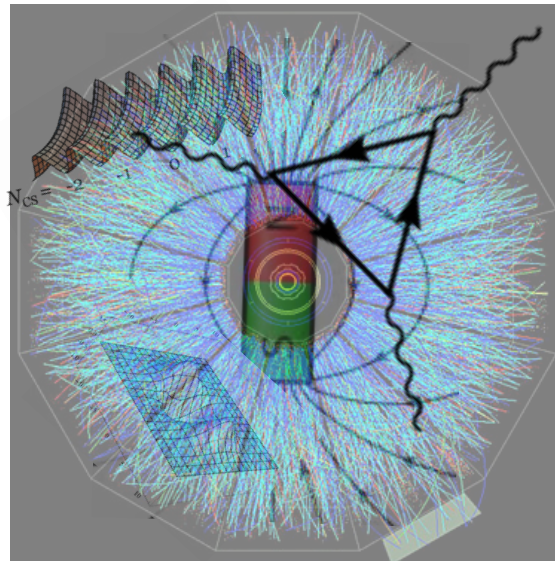


Chiral Magnetic Effect in Isobaric Collisions from Anomalous-Viscous Fluid Dynamics (AVFD)



Jinfeng Liao

Indiana University, Physics Dept. & CEEM

**Research Supported by U.S. NSF & DOE
and by the IAS of Indiana University**



BEST
COLLABORATION

arXiv:1611.04586

Quantifying the chiral magnetic effect from anomalous-viscous fluid dynamics^{*}

Yin Jiang(姜寅)¹ Shuzhe Shi(施舒哲)² Yi Yin(尹伊)³ Jinfeng Liao(廖劲峰)^{2,4;1}

¹ School of Physics and Nuclear Energy Engineering, Beihang University, Beijing 100191, China

² Physics Department and Center for Exploration of Energy and Matter, Indiana University, 2401 N Milo B. Sampson Lane, Bloomington, IN 47408, USA

³ Center for Theoretical Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

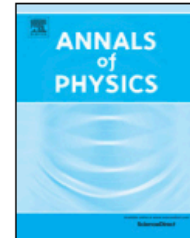
⁴ Institute of Particle Physics and Key Laboratory of Quark & Lepton Physics (MOE), Central China Normal University, Wuhan 430079, China

Annals of Physics 394 (2018) 50–72

Contents lists available at ScienceDirect

Annals of Physics

journal homepage: www.elsevier.com/locate/aop



Anomalous chiral transport in heavy ion collisions from Anomalous-Viscous Fluid Dynamics

Shuzhe Shi^{a,*}, Yin Jiang^{b,c}, Elias Lilleskov^{d,a}, Jinfeng Liao^{a,e,*}



Shuzhe Shi
(PhD @ IUB)

Other collaborators:
Yin Jiang (Beihang),
Yi Yin (MIT),
Elias Lilleskov (REU);

Hui Zhang, Defu Hou
(CCNU).

arXiv:1711.02496

Exciting Progress: See Recent Reviews

Progress in Particle and Nuclear Physics 88 (2016) 1–28



Contents lists available at ScienceDirect

Progress in Particle and Nuclear Physics

journal homepage: www.elsevier.com/locate/ppnp



Review

Chiral magnetic and vortical effects in high-energy nuclear collisions—A status report



D.E. Kharzeev^{a,b}, J. Liao^{c,d,*}, S.A. Voloshin^e, G. Wang^f

^a Department of Physics and Astronomy, Stony Brook University, Stony Brook, NY 11794-3800, USA

^b Department of Physics and RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, NY 11973-5000, USA

^c Physics Department and Center for Exploration of Energy and Matter, Indiana University, 727 E Third Street, Bloomington, IN 47405, USA

^d RIKEN BNL Research Center, Bldg. 510A, Brookhaven National Laboratory, Upton, NY 11973, USA

^e Department of Physics and Astronomy, Wayne State University, 666 W. Hancock, Detroit, MI 48201, USA

^f Department of Physics and Astronomy, University of California, Los Angeles, CA 90095, USA

Prog. Part. Nucl. Phys. 88, 1 (2016)[arXiv:1511.04050 [hep-ph]].

J. Liao, Pramana 84, no. 5, 901 (2015) [arXiv:1401.2500 [hep-ph]].

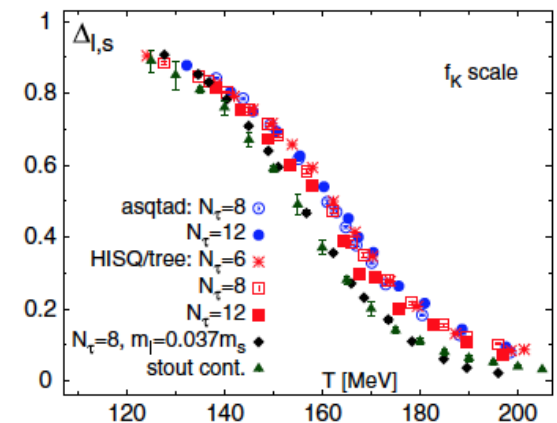
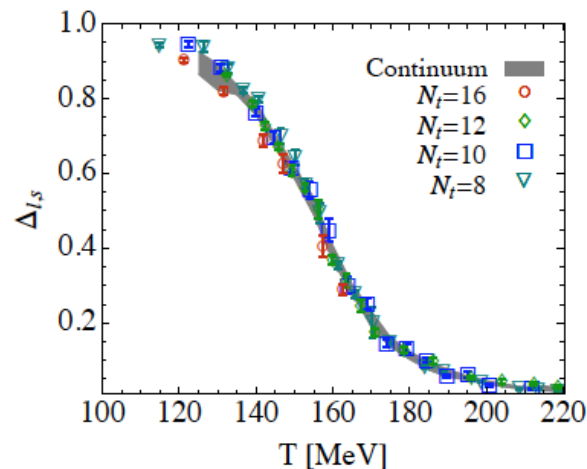
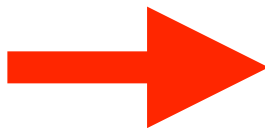
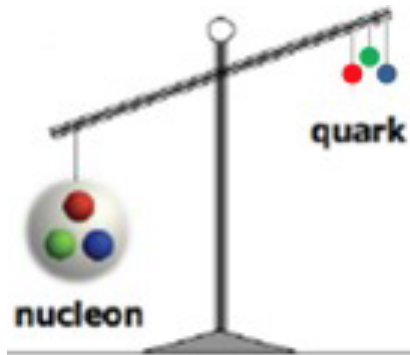
Outline

- Introductory Discussions
- The AVFD Framework
- AVFD Results for AuAu Collisions
- Searching for CME in Isobaric Collisions
- Summary

Introductory Discussions

QCD & Chiral Symmetry

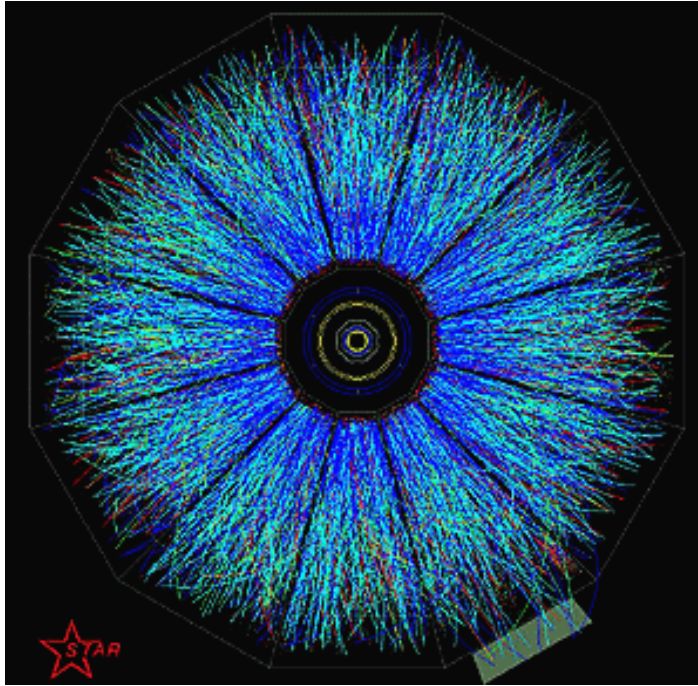
** Spontaneously broken chiral symmetry in the vacuum is a fundamental property of QCD.*



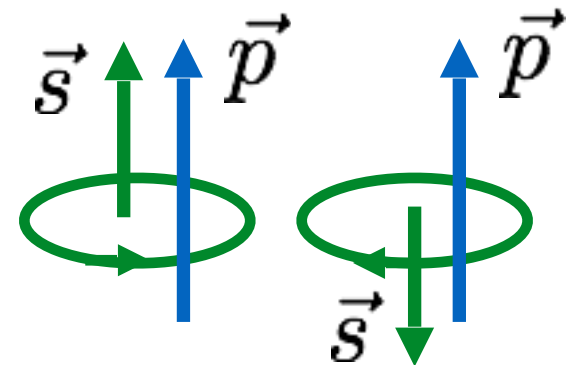
** A chirally symmetric quark-gluon plasma at high temperature is an equally fundamental property of QCD!*

Could we see direct experimental evidence for that?

“Little Bang” in High Energy Nuclear Collision



- * Quark-gluon plasma (QGP) is created in such collisions.*
- * It is PRIMORDIALLY HOT ~ trillion degrees ~ early universe.*
- * Is chiral symmetry restored?*



Chiral Anomaly

Chiral anomaly is a fundamental aspect of QFT with chiral fermions.

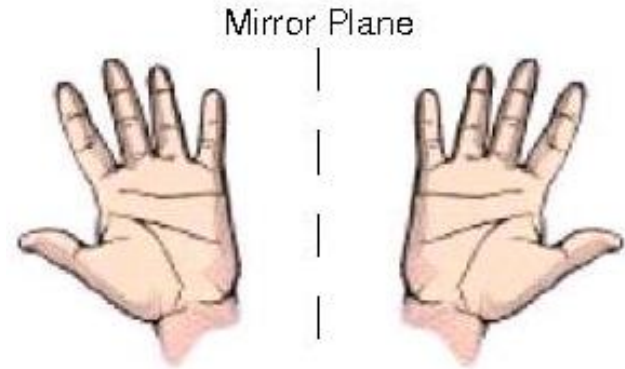
Classical symmetry:

$$\mathcal{L} = i\bar{\Psi}\gamma^\mu\partial_\mu\Psi$$

$$\mathcal{L} \rightarrow i\bar{\Psi}_L\gamma^\mu\partial_\mu\Psi_L + i\bar{\Psi}_R\gamma^\mu\partial_\mu\Psi_R$$

$$\Lambda_A : \Psi \rightarrow e^{i\gamma_5\theta}\Psi$$

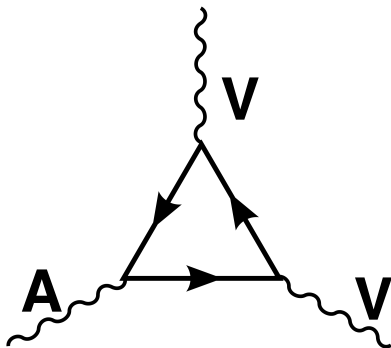
$$\partial_\mu J_5^\mu = 0$$



Broken at QM level:

$$\partial_\mu J_5^\mu = C_A \vec{E} \cdot \vec{B}$$

$$dQ_5/dt = \int_{\vec{x}} C_A \vec{E} \cdot \vec{B}$$



[e.g. $\pi^0 \rightarrow 2 \gamma$]

* C_A is universal anomaly coefficient

* Anomaly is intrinsically QUANTUM effect

The Chiral Magnetic Effect (CME)

Chirality & Anomaly & Topology

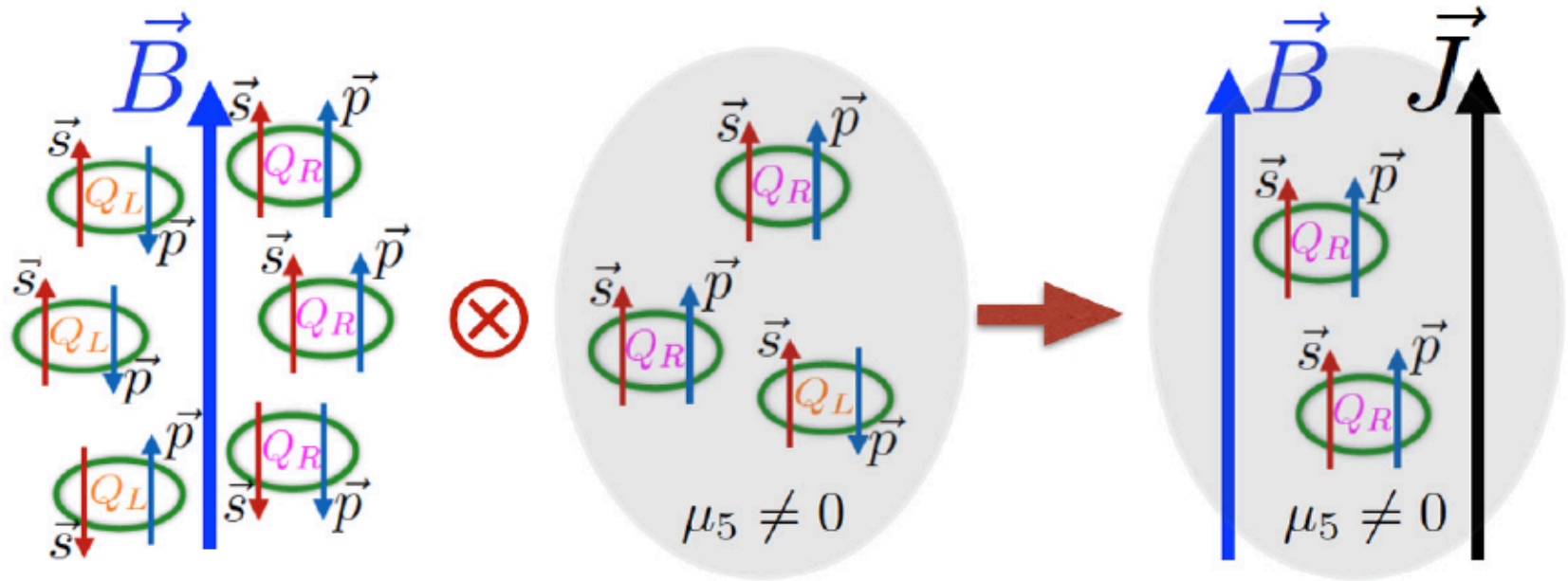
$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$

Electric
Current

Magnetic
Field

Q.M. Transport

Intuitive Picture of CME



Intuitive understanding of CME:

Magnetic polarization \rightarrow
correlation between micro.
SPIN & EXTERNAL FORCE



Chiral imbalance \rightarrow
correlation between directions of
SPIN & MOMENTUM

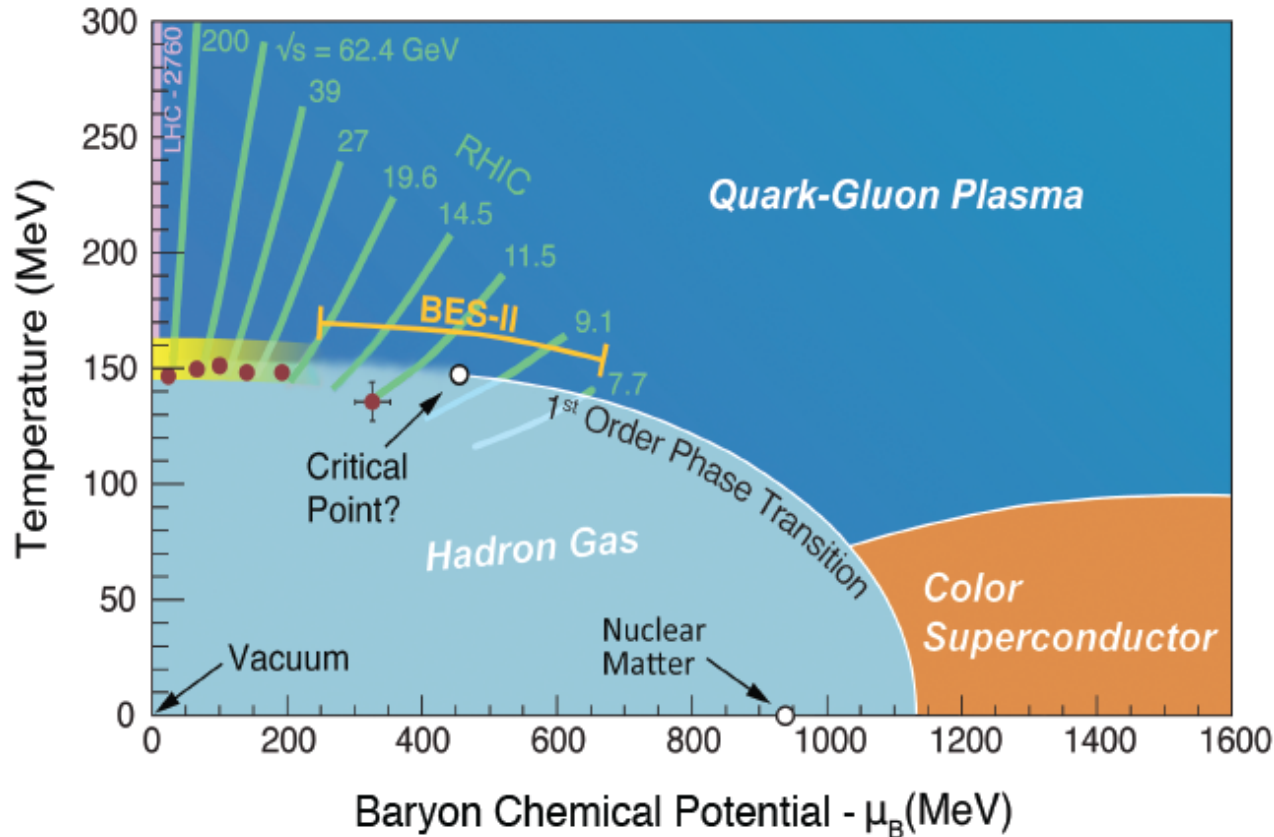


Transport current along magnetic field

$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$

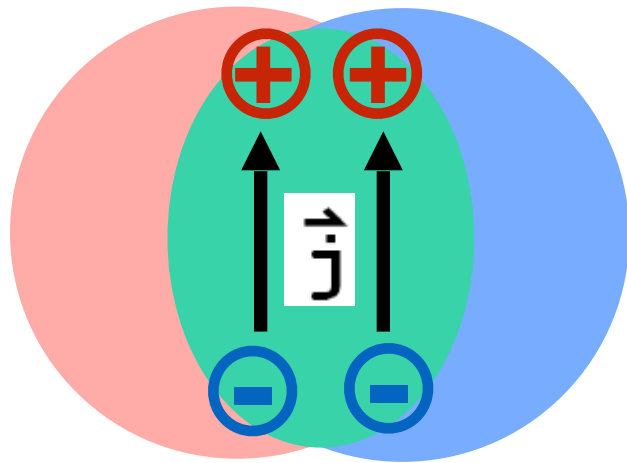
CME and Beam Energy Scan

$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$



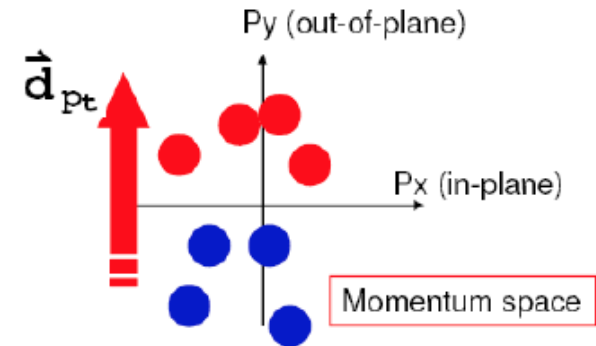
- * *We'd like to see a chiral QGP above certain threshold energy via CME*
- * *We'd like to see its turning off at low enough energy*

From CME Current to Charge Separation



$$\vec{J} = \sigma_5 \mu_5 \vec{B}$$

*strong radial blast:
position \rightarrow momentum*



Charge Separation or
Electric Dipole in Pt Space
(along out-of-plane)

[Kharzeev 2004; Kharzeev, McLerran, Warringa, 2008; ...]

$$\frac{dN_{\pm}}{d\phi} \propto \dots + a_{\pm} \sin(\phi - \Psi_{RP})$$

$$\langle a_{\pm} \rangle \sim \pm \langle \mu_5 \rangle B$$

Very difficult measurement:

- * *Zero average, only nonzero variance;*
- * *Correlation measurement with significant backgrounds;*
- * *Signal likely very small*

Experimental Observable

charge separation \Rightarrow charge dept. two-particle correlation

Voloshin, 2004

$$\gamma = \langle \cos(\Delta\phi_i + \Delta\phi_j) \rangle = \langle \cos\Delta\phi_i \cos\Delta\phi_j \rangle - \langle \sin\Delta\phi_i \sin\Delta\phi_j \rangle$$

$$\delta = \langle \cos(\Delta\phi_i - \Delta\phi_j) \rangle = \langle \cos\Delta\phi_i \cos\Delta\phi_j \rangle + \langle \sin\Delta\phi_i \sin\Delta\phi_j \rangle$$

$$\gamma = \kappa v_2 \text{ F} - \text{H}$$

F: Bulk Background

$$\delta = \text{F} + \text{H}$$

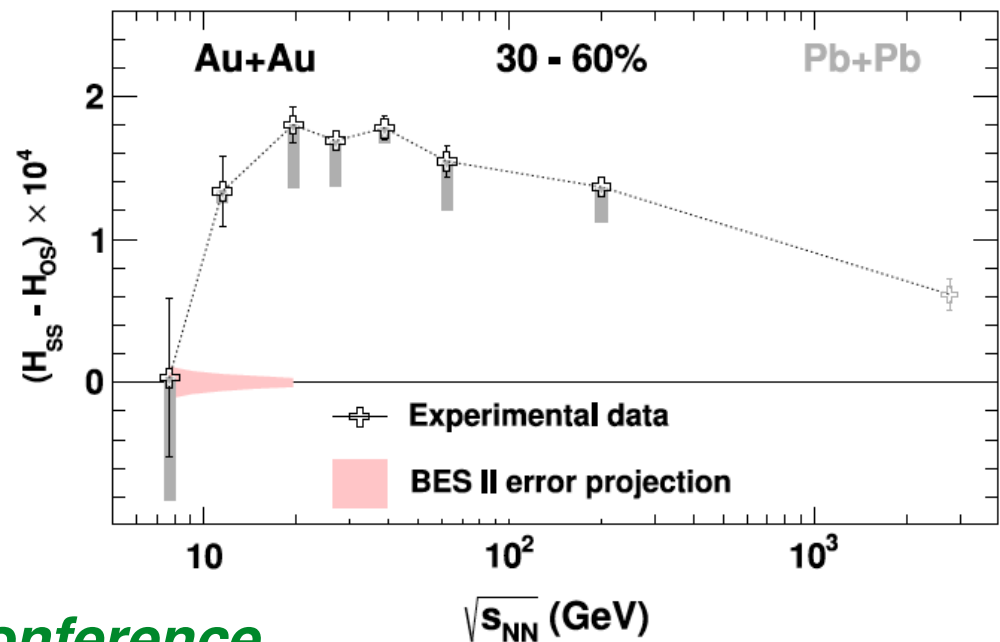
H: Possible Pure CME Signal = $(a_{1,\text{CME}})^2$

Bzdak, Koch, JL, 2012

$$H_{\text{SS}} - H_{\text{OS}} \leftrightarrow 2(a_1)^2$$

*Many interesting proposals
of new observables!*

See many other talks at this conference.



Summarizing Exp. Search Status

Main challenge: flow-driven background v.s. CME signal

Vary v_2 for fixed B:

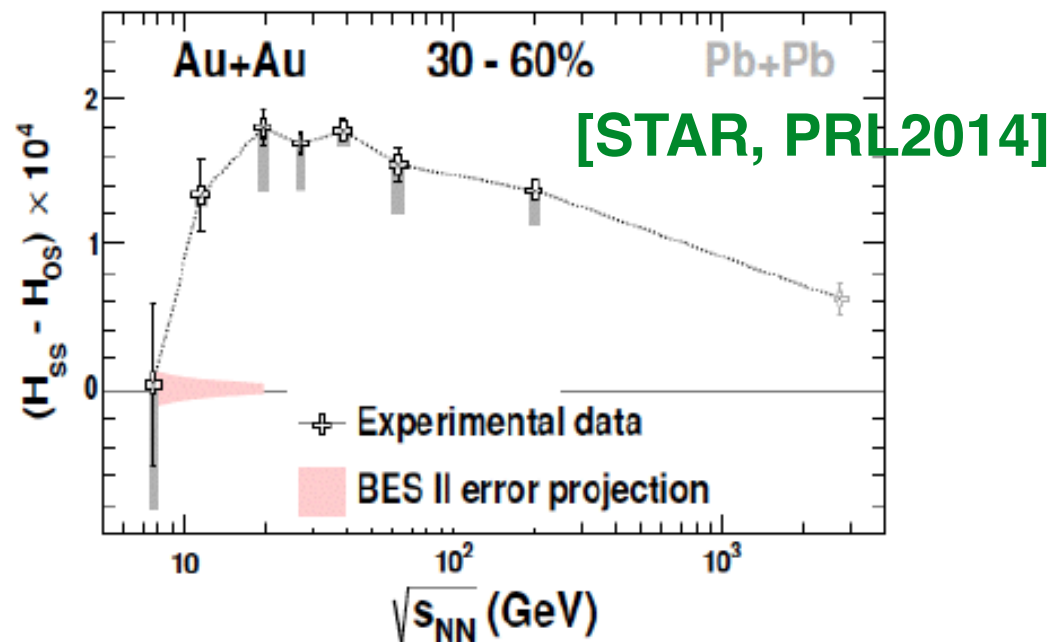
AuAu v.s. UU;

*Varying event-shape;
2-component subtraction.*

Vary B for fixed v_2 :

*Isobaric collisions with
RuRu v.s. ZrZr*

Our best guess for now:



*Encouraging experimental evidence for CME in QGP
— can we quantitatively compute CME signal?*

AVFD Framework

Fluid Dynamics That Knows Left & Right

conservation
law:

$$\partial_\mu J^\mu = 0 \longrightarrow \partial_\mu J^\mu = C E^\mu B_\mu$$

constituent
relation:

$$J^\mu = n u^\mu + \nu^\mu$$

$$\partial_\mu s^\mu \geq 0 \quad \nu^\mu = -\sigma T P^{\mu\nu} \partial_\nu \left(\frac{\mu}{T} \right) + \sigma E^\mu + \xi \omega^\mu + \xi_B B^\mu$$

[Son, Surowka, 2009;...]

CVE

CME

**Microscopic quantum anomaly emerges as
macroscopic anomalous hydrodynamic currents!**

*It would be remarkable to actually “see” this new
hydrodynamics at work in real world materials!*

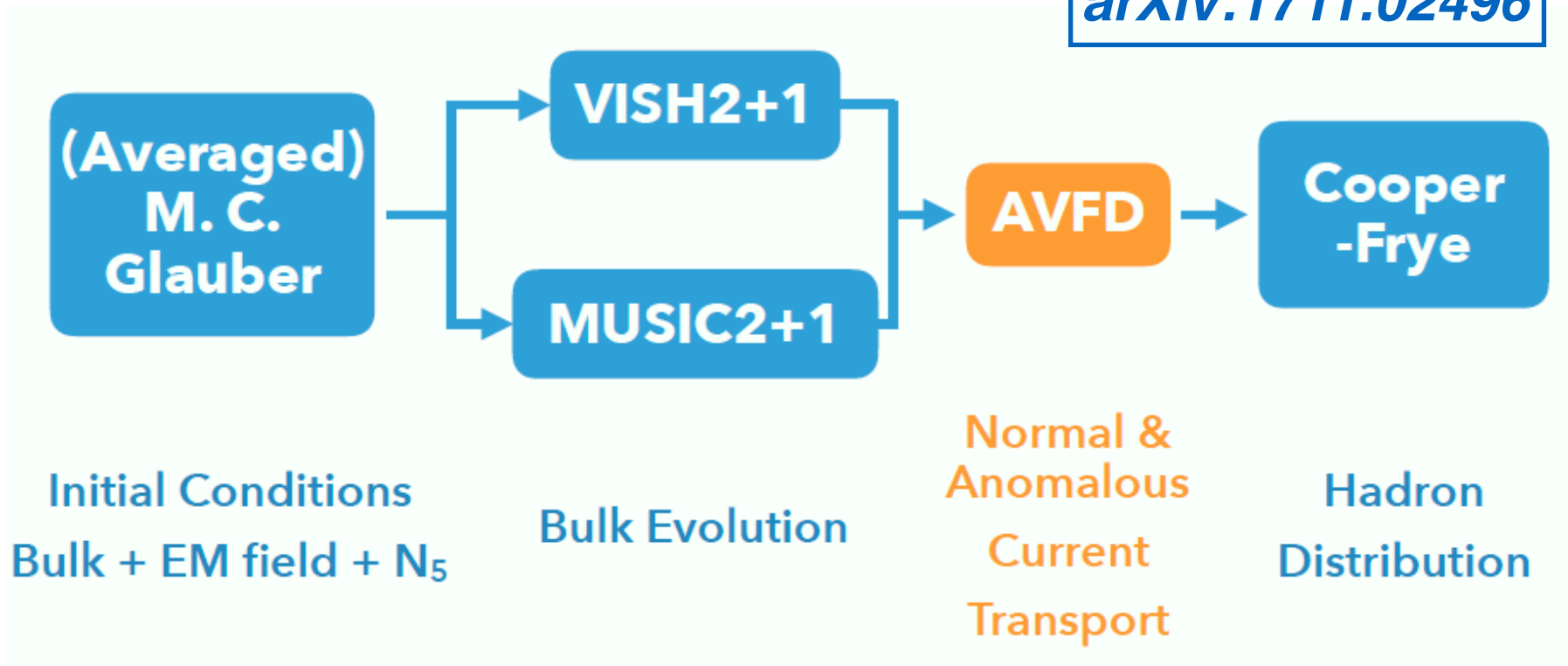
The AVFD Framework



The AVFD Framework

[arXiv:1611.04586](https://arxiv.org/abs/1611.04586)

[arXiv:1711.02496](https://arxiv.org/abs/1711.02496)



AVFD:
Anomalous-Viscous Fluid Dynamics

The AVFD Framework

Anomalous-Viscous Fluid Dynamics

$$D_\mu J_R^\mu = + \frac{N_c q^2}{4\pi^2} E_\mu B^\mu \quad D_\mu J_L^\mu = - \frac{N_c q^2}{4\pi^2} E_\mu B^\mu$$

$$J_R^\mu = n_R u^\mu + v_R^\mu + \frac{N_c q}{4\pi^2} \mu_R B^\mu$$

$$J_L^\mu = n_L u^\mu + v_L^\mu - \frac{N_c q}{4\pi^2} \mu_L B^\mu$$

CME

Viscous Effect

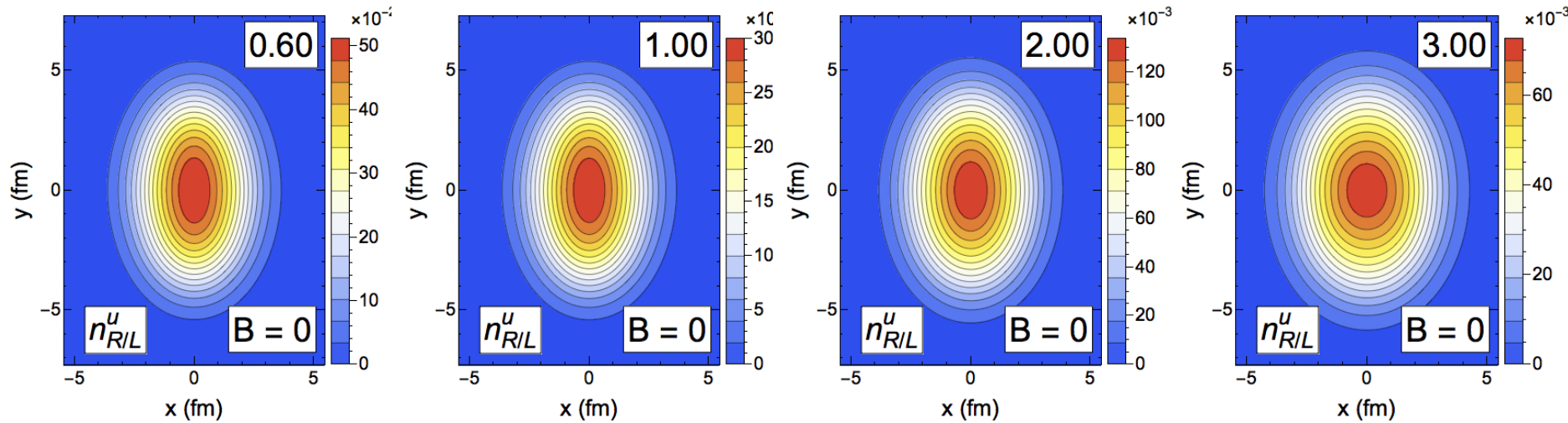
$$\Delta^\mu_\nu d v_{R,L}^\nu = - \frac{1}{\tau_{\text{rlx}}} (v_{R,L}^\mu - v_{\text{NS}}^\mu)$$

$$v_{\text{NS}}^\mu = \frac{\sigma}{2} T \Delta^{\mu\nu} \partial_\nu \frac{\mu}{T} + \frac{\sigma}{2} q E^\mu$$

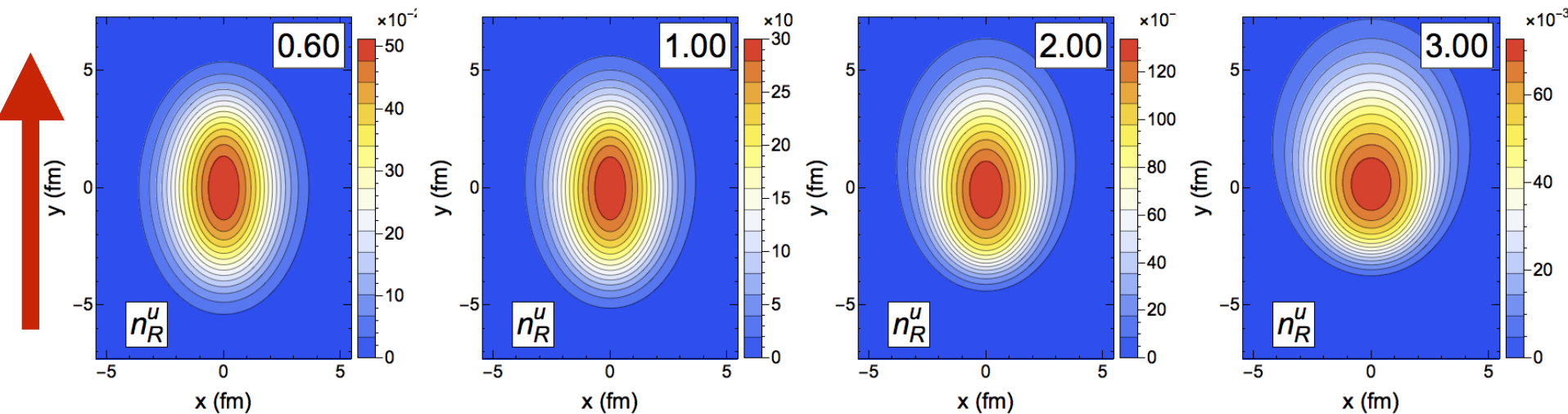
on top of VISH2+1D -- OSU Group

[We now also have MUSIC-AVFD!]

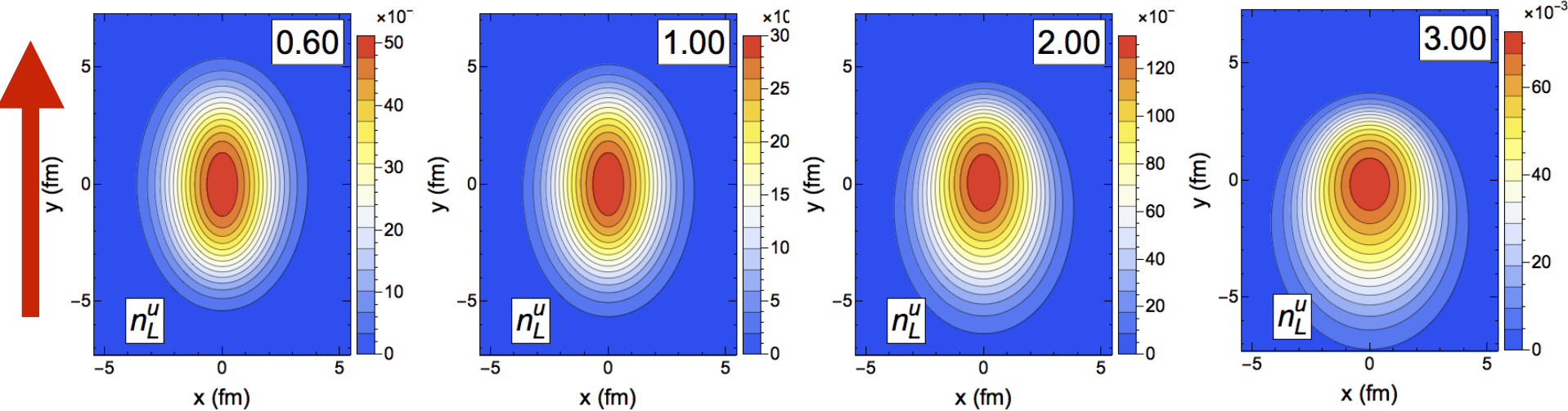
Demonstrating the AVFD



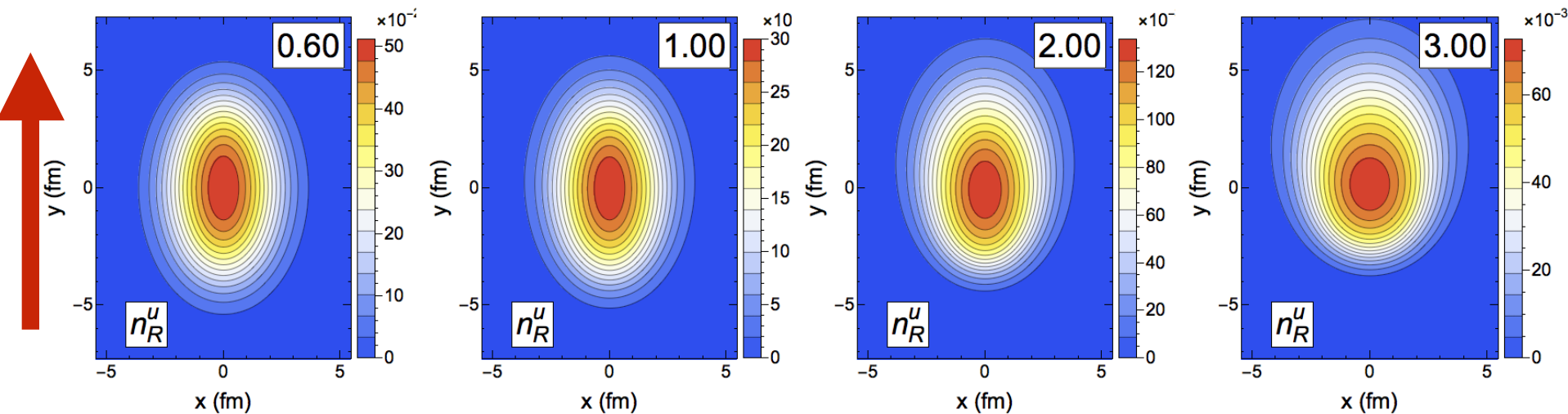
Upper: NO magnetic field
Lower: with B field (along y+ direction)



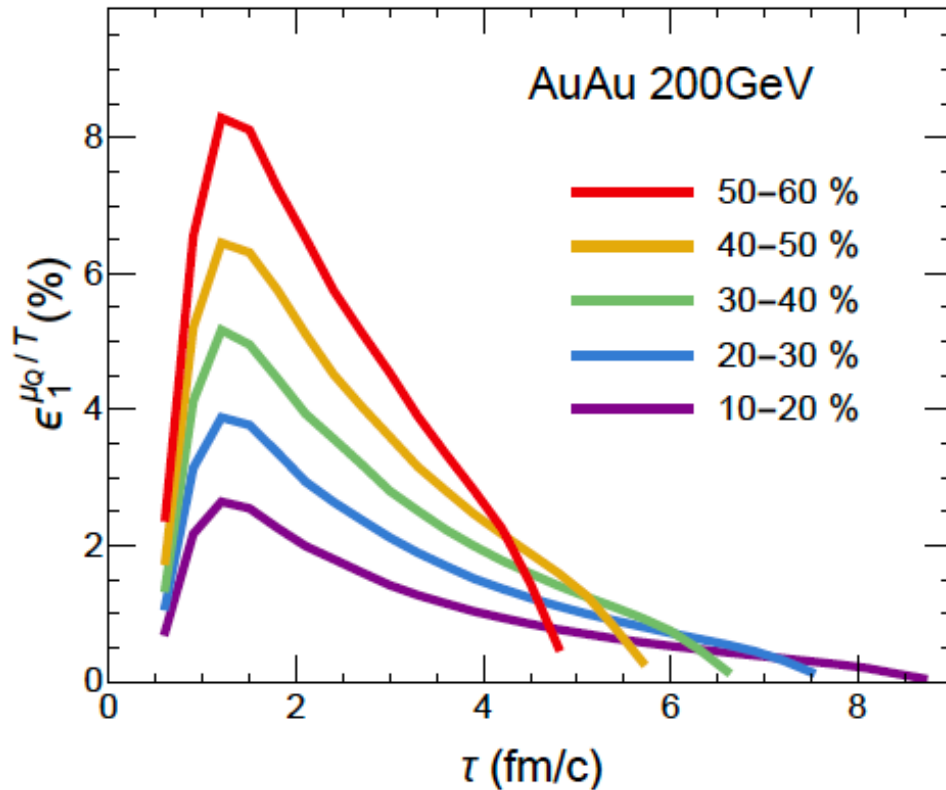
Demonstrating the AVFD



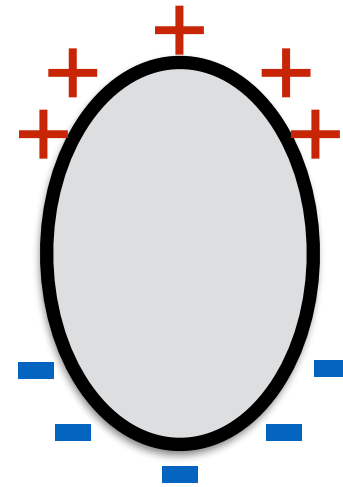
Upper: Left-Handed (LH), with B field (along y + direction)
Lower: Right-Handed (RH), with B field (along y + direction)



The Charge Separation from AVFD



$$E \frac{dN}{d^3p}(x^\mu, p^\mu) = \frac{g}{(2\pi)^3} \int_{\Sigma_{fo}} p^\mu d^3\sigma_\mu f(x, p)$$



B field $\otimes \mu_5 \Rightarrow$ current \Rightarrow dipole (charge separation)

$$dN_{\pm}/d\phi \propto 1 + 2 \mathbf{a}_{1\pm} \sin(\phi - \psi_{RP}) + \dots$$

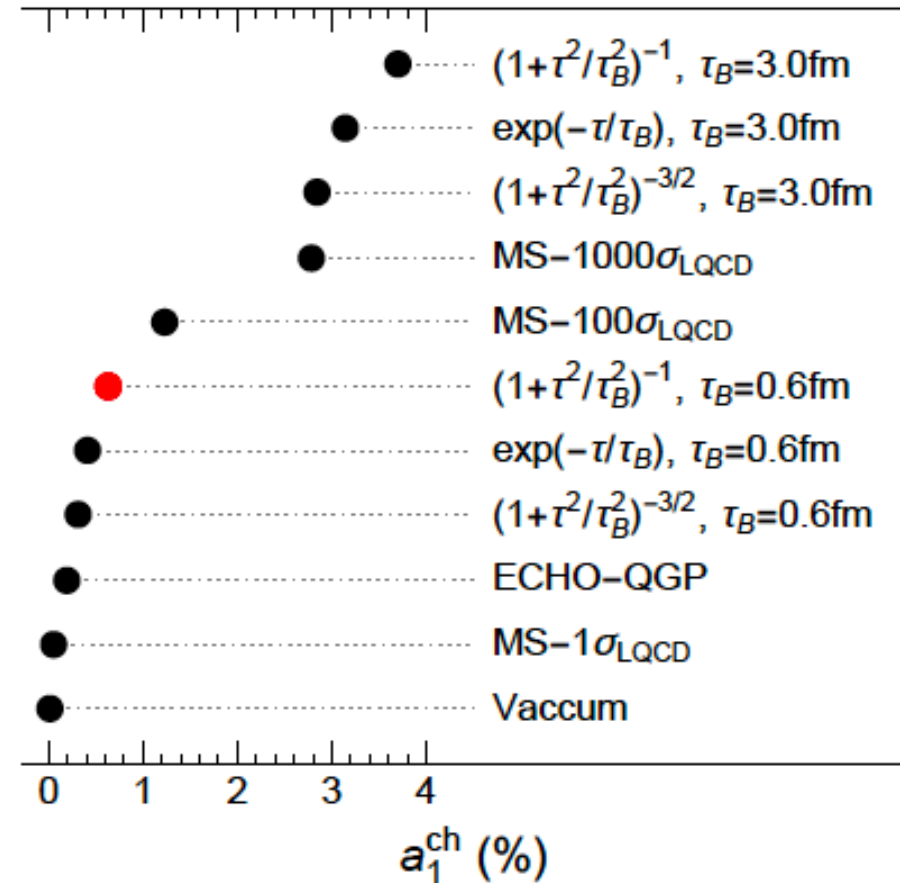
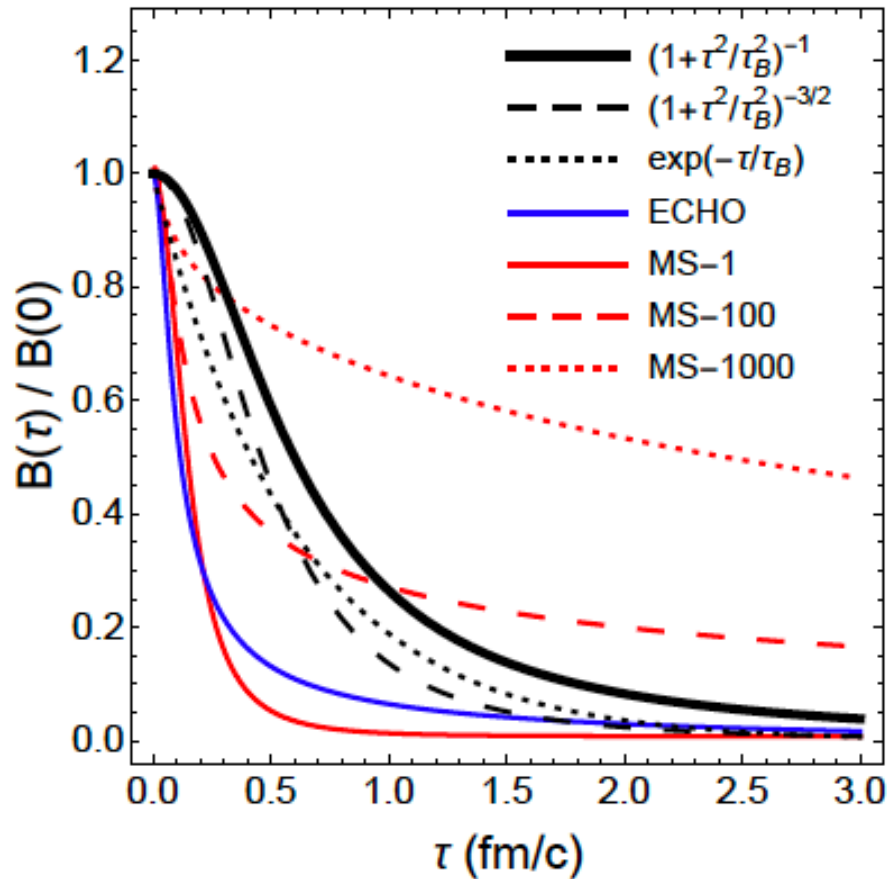
$$H_{SS} - H_{OS} \leftrightarrow 2(a_1)^2$$

AVFD Results for AuAu Collisions

arXiv:1611.04586

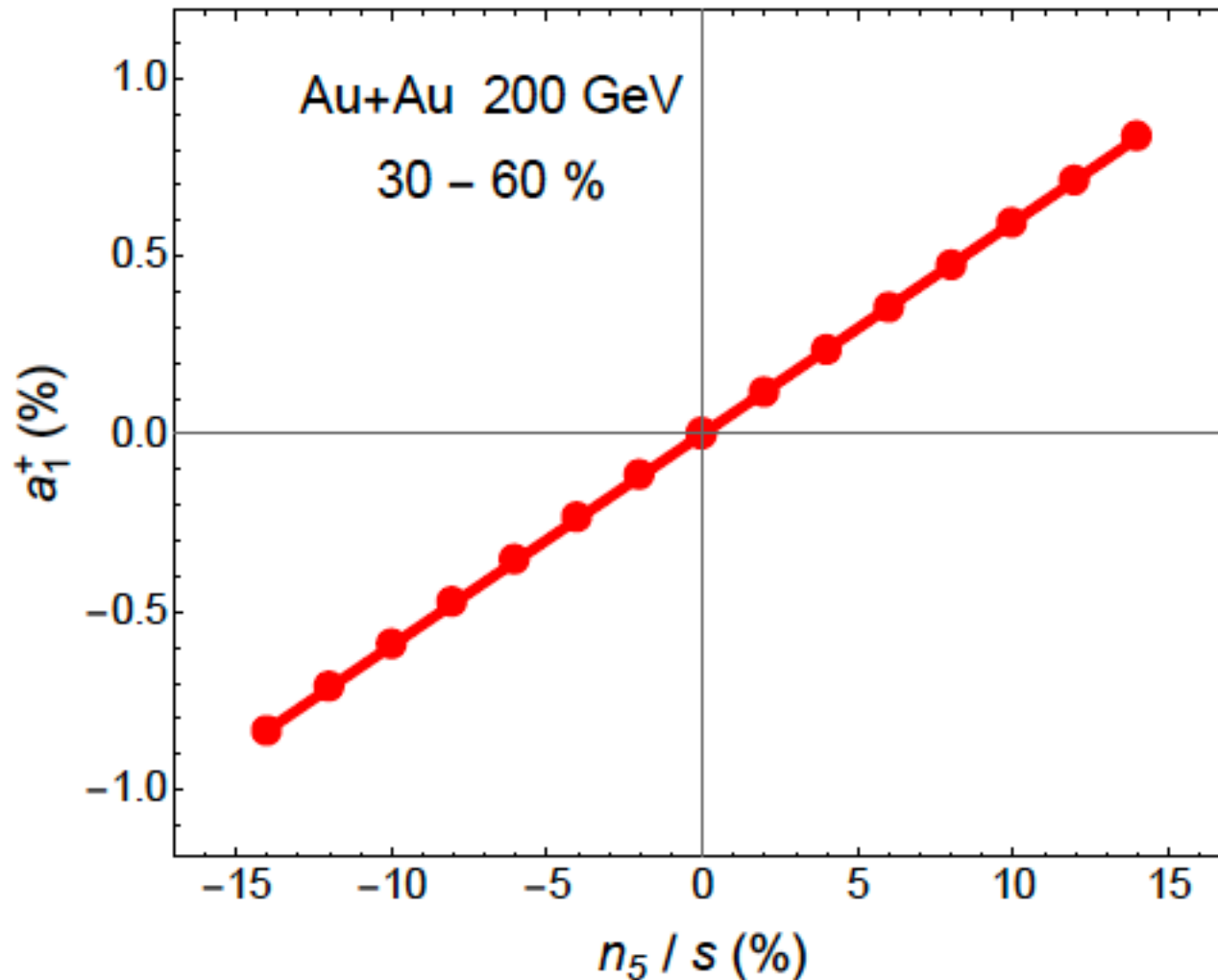
arXiv:1711.02496

The Influence of the Magnetic Field



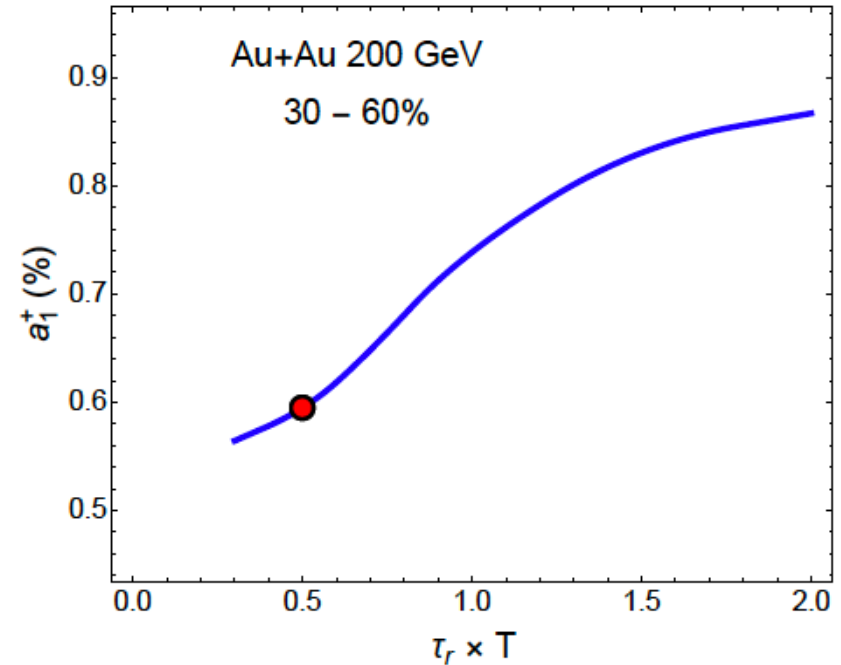
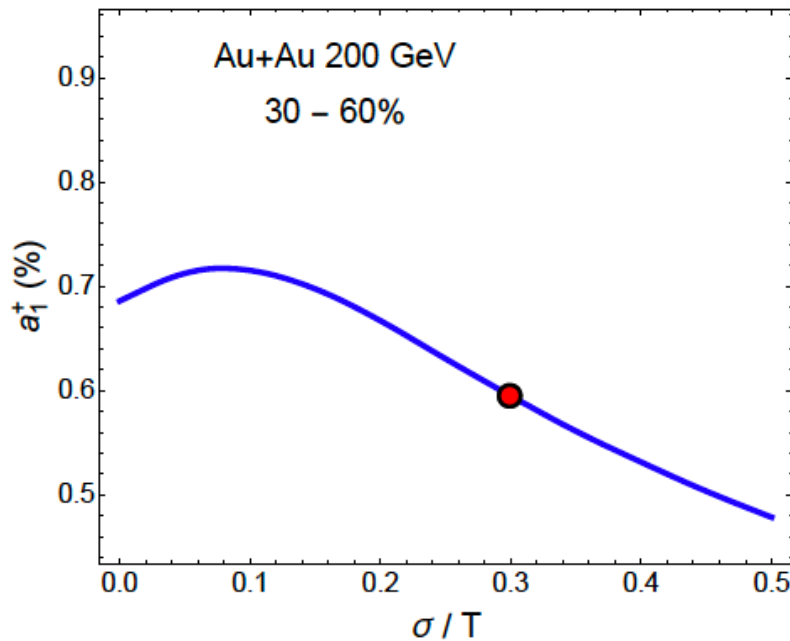
**Strong influence by B field evolution;
Significant theoretical uncertainty!**

The Axial Charge Initial Condition



**Very sensitive to initial axial charge;
Significant theoretical uncertainty!**

The Influence of the Viscous Transport

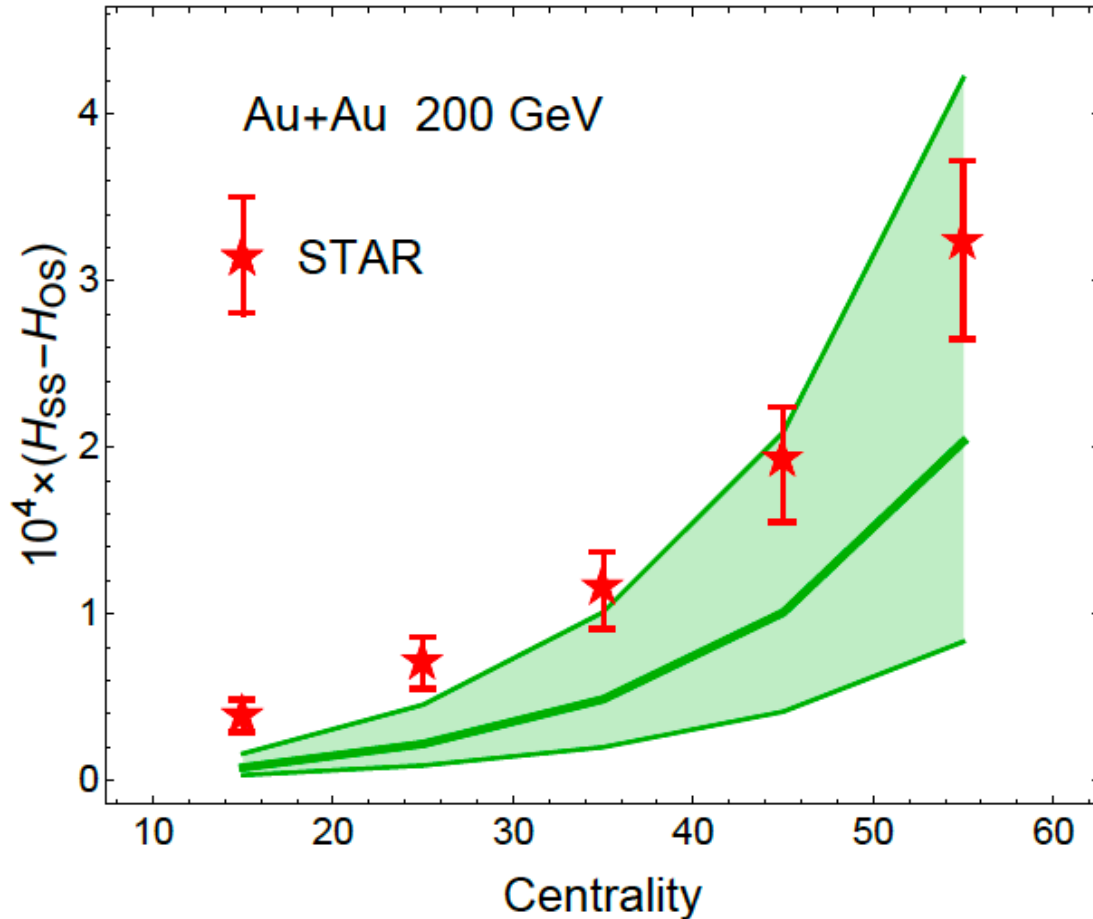


$$\Delta_{\nu}^{\mu} \mathbf{d} \nu_{R,L}^{\nu} = -\frac{1}{\tau_{rlx}} (\nu_{R,L}^{\mu} - \nu_{NS}^{\mu})$$

$$\nu_{NS}^{\mu} = \frac{\sigma}{2} T \Delta^{\mu\nu} \partial_{\nu} \frac{\mu}{T} + \frac{\sigma}{2} q E^{\mu}$$

First calibration for the influence of the viscous transport on charge separation signal!

AVFD Predictions v.s Experimental Data



$$B(\tau) = \frac{B_0}{1 + (\tau/\tau_B)^2}$$

$$\tau_B = 0.6 \text{ fm}/c$$

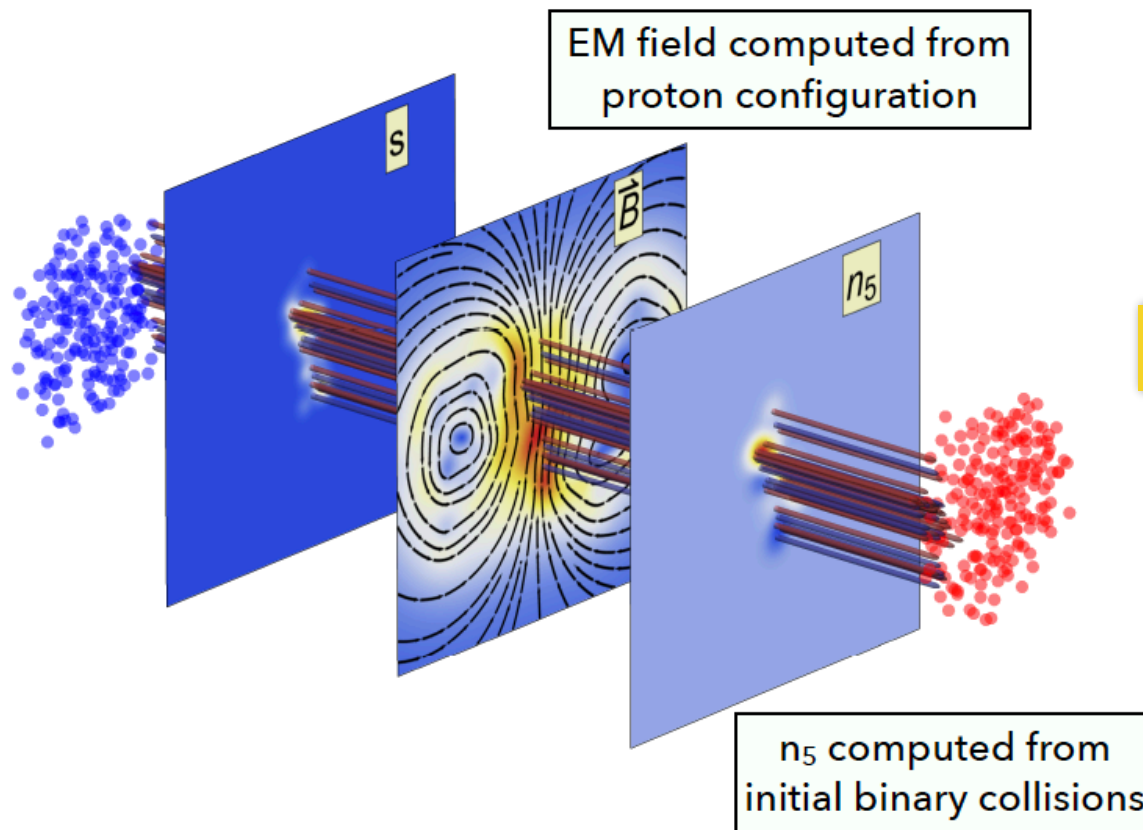
$$\sqrt{\langle n_5^2 \rangle} \simeq \frac{Q_s^4 (\pi \rho_{tube}^2 \tau_0) \sqrt{N_{coll.}}}{16\pi^2 A_{overlap}}$$

*Nice agreement;
But read them in
perspective!*

centrality bin	10-20%	20-30%	30-40%	40-50%	50-60%
$eB_0(m_\pi^2)$	2.34	3.10	3.62	4.01	4.19
n_5/s	0.065	0.078	0.095	0.119	0.155

Table 1. Centrality dependence of magnetic field peak strength and the initial chirality imbalance. The n_5/s shown here is obtained with a saturation scale $Q_s^2 = 1.25 \text{ GeV}^2$.

Event-By-Event AVFD



Include EBE fluctuations:

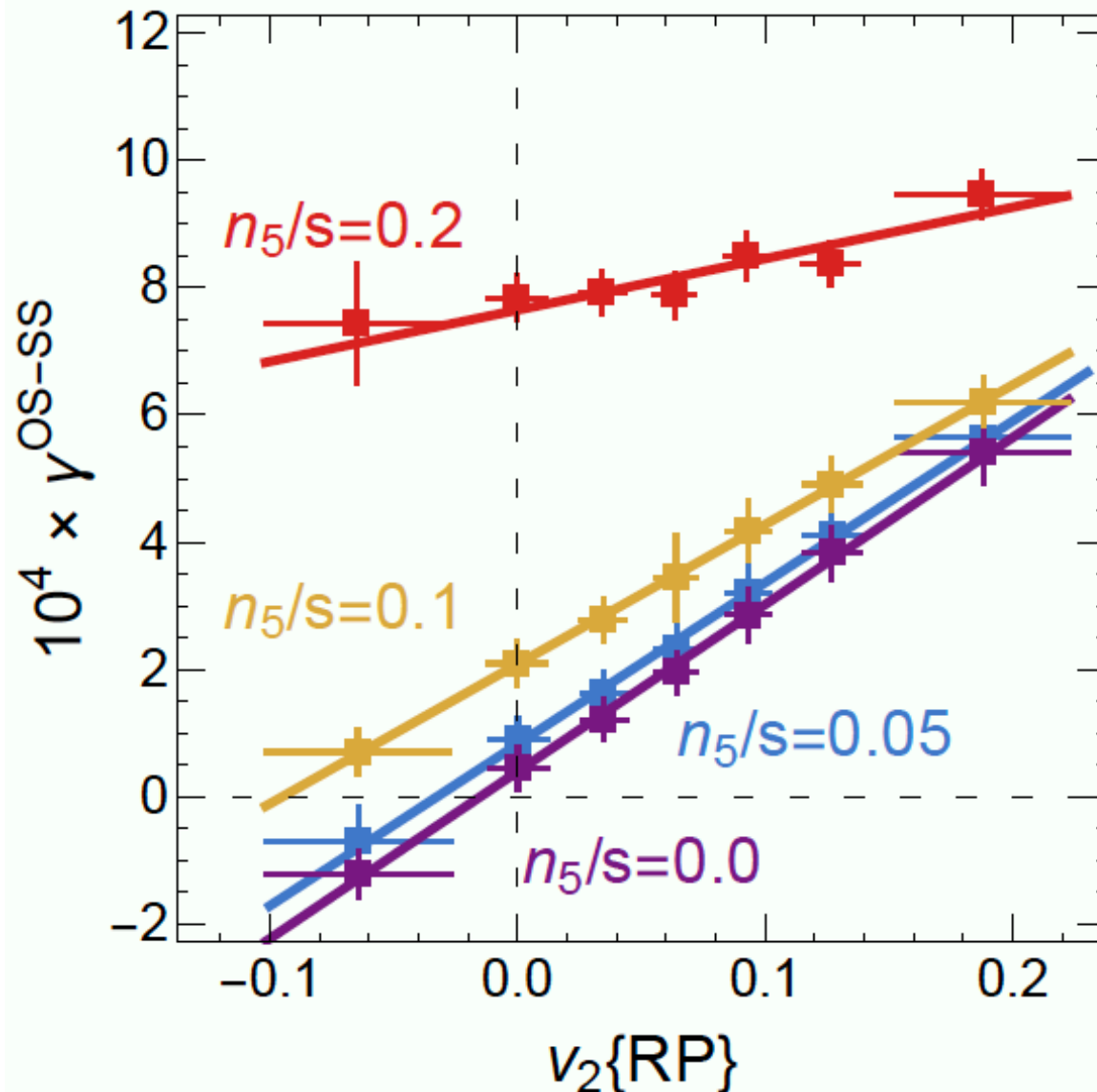
- ▶ Initial Conditions
- ▶ Statistic @ Freeze-out
- ▶ Hadron Cascade

Important for better understanding:

- * *Interplay between signal and BKG;*
- * *Experimental analysis methods*

EBE-AVFD for Event-Shape Engineering

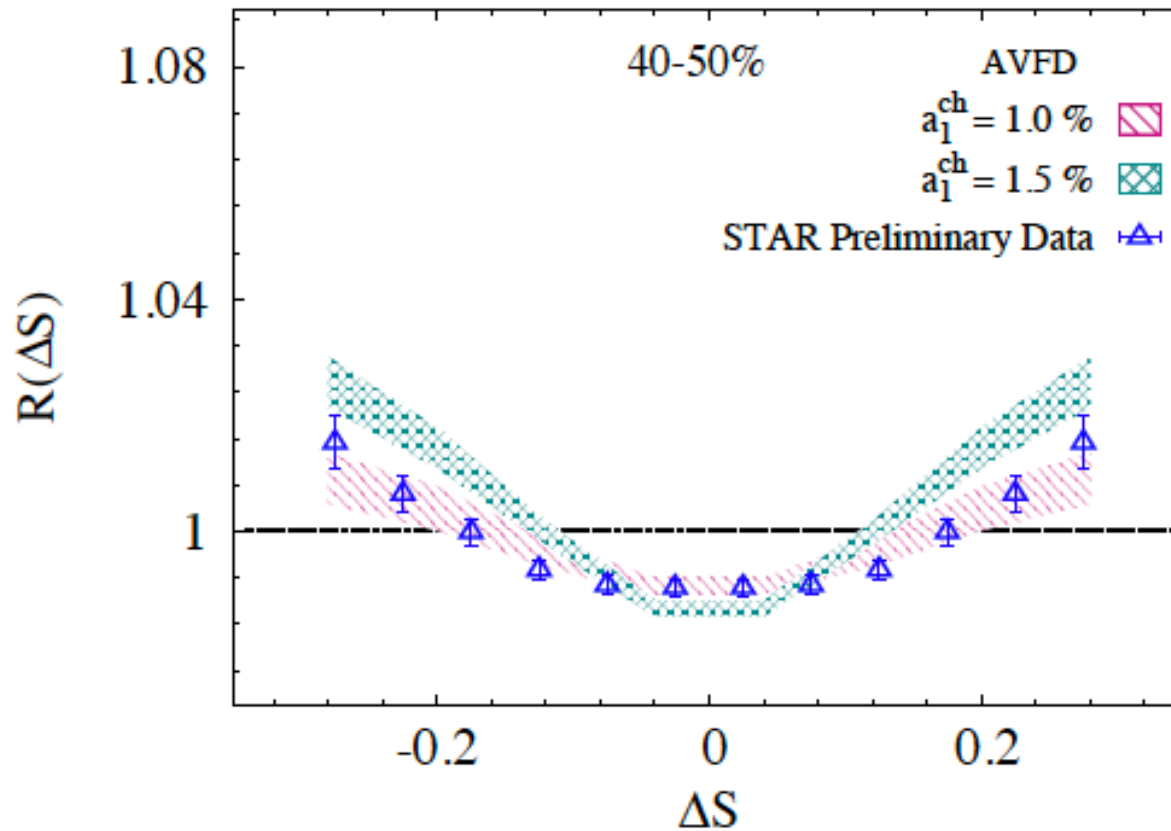
Au-Au @ 200GeV 50-60%



The intercept is very sensitive to the CME contribution!

Slope depends on CME too: naive subtraction may not be good.

EBE-AVFD for R-Correlator

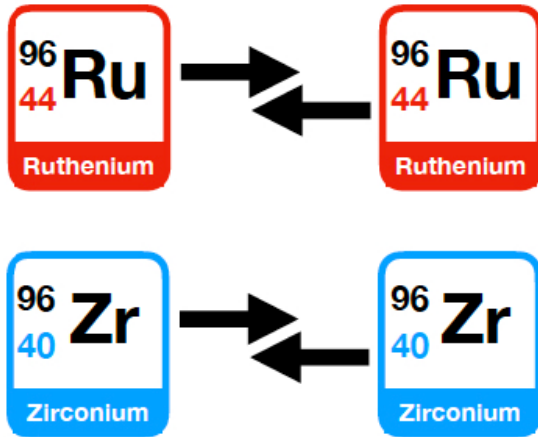


*Magdy, Lacey, et al,
arXiv:1710.01717;
arXiv:1803.02416*

R-correlator sensitively responds to CME contribution.

Searching for CME in Isobaric Collisions (Newest results!)

Using Isobaric Collisions for CME Search



*Key idea: contrasting
two systems with
identical bulk,
varied magnetic fields.*

***Charge Asymmetry
Correlation Measurement***

Background

Signal

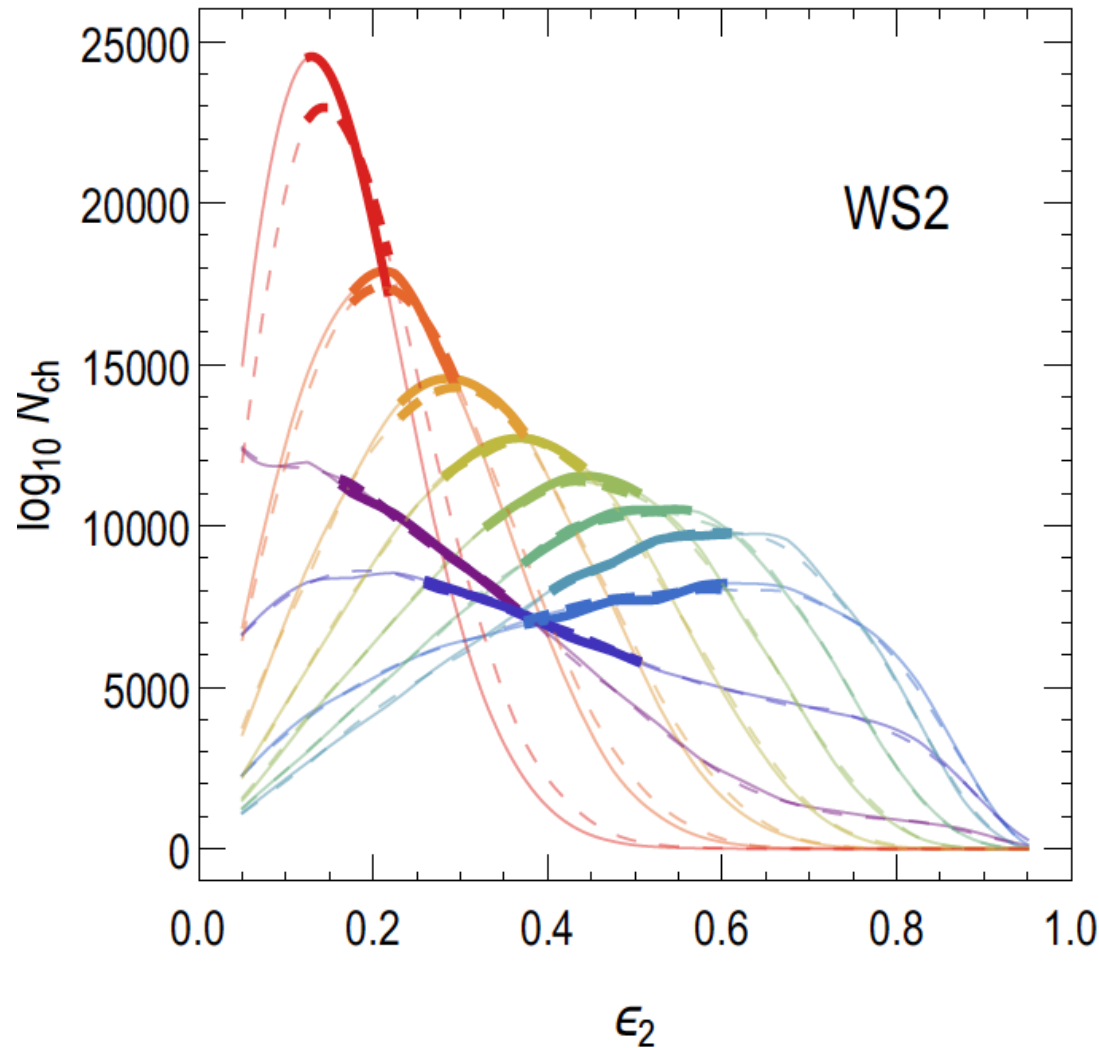
RuRu

Background

Signal

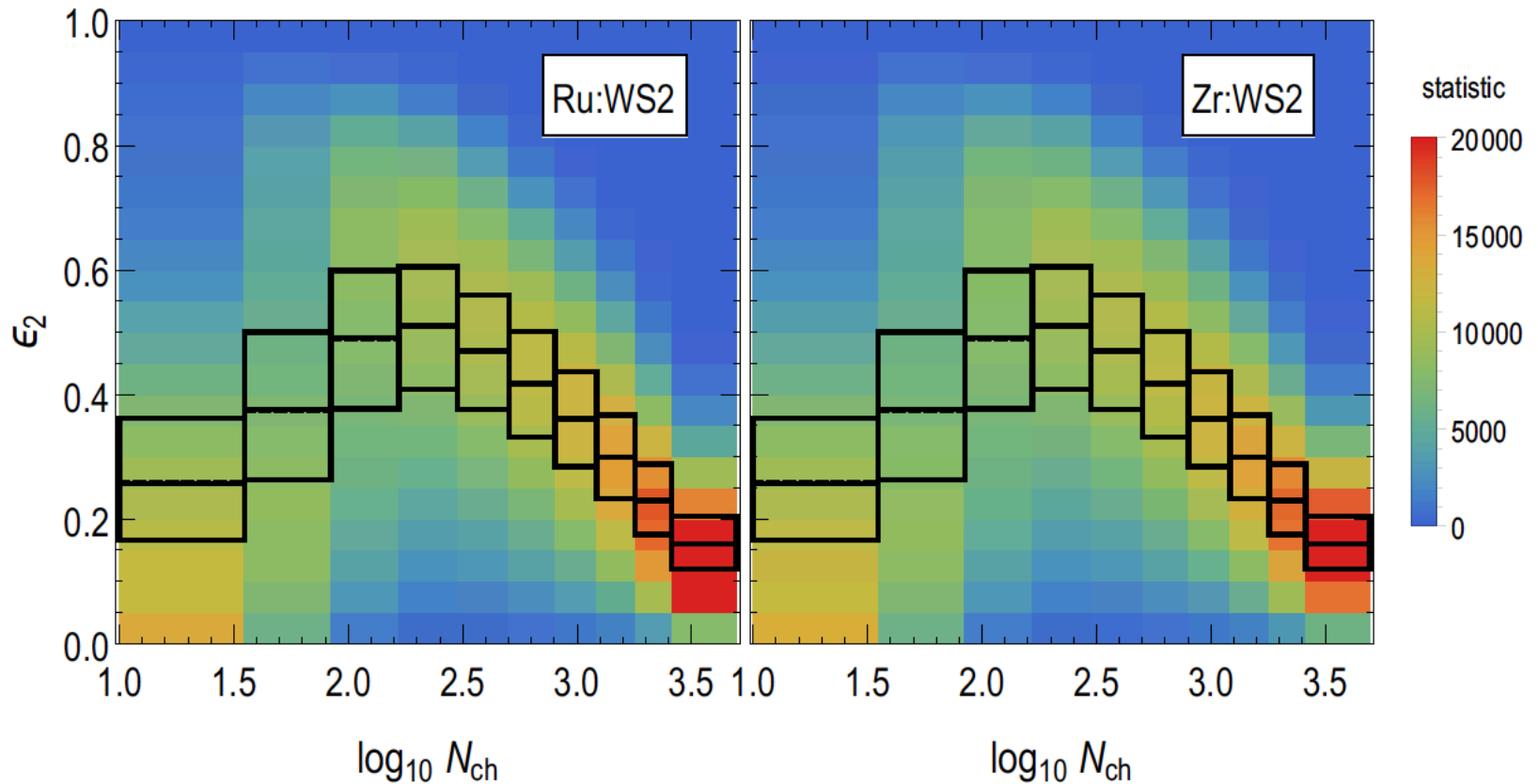
ZrZr

How to Choose Identical Systems?



***Insight from initial conditions:
joint cut on Multiplicity-Eccentricity***

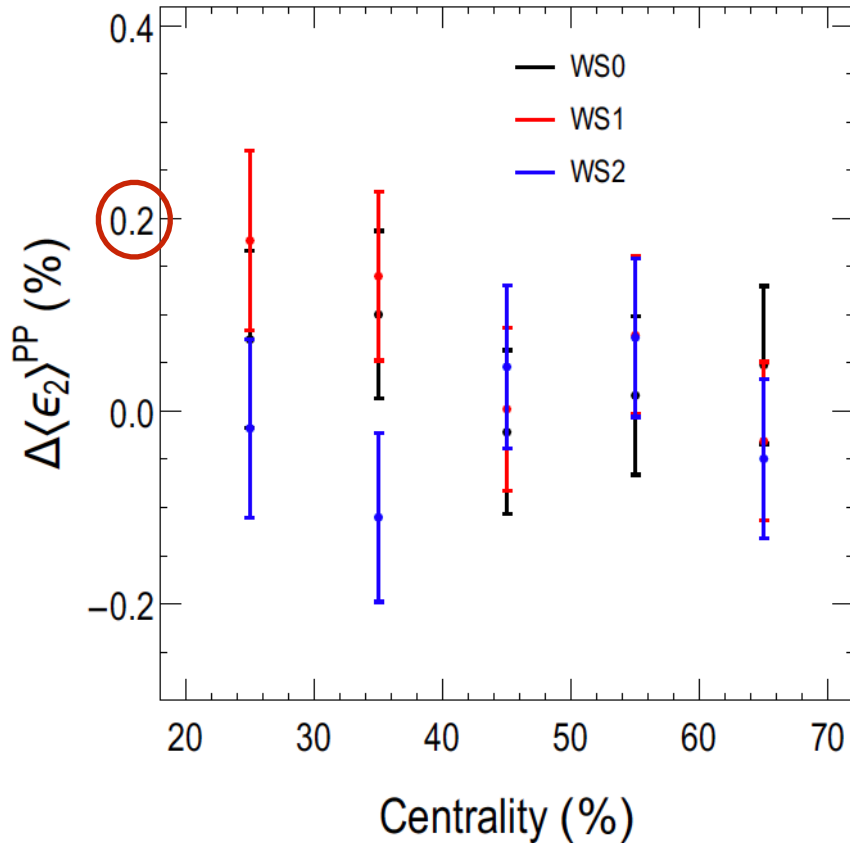
How to Choose Identical Systems?



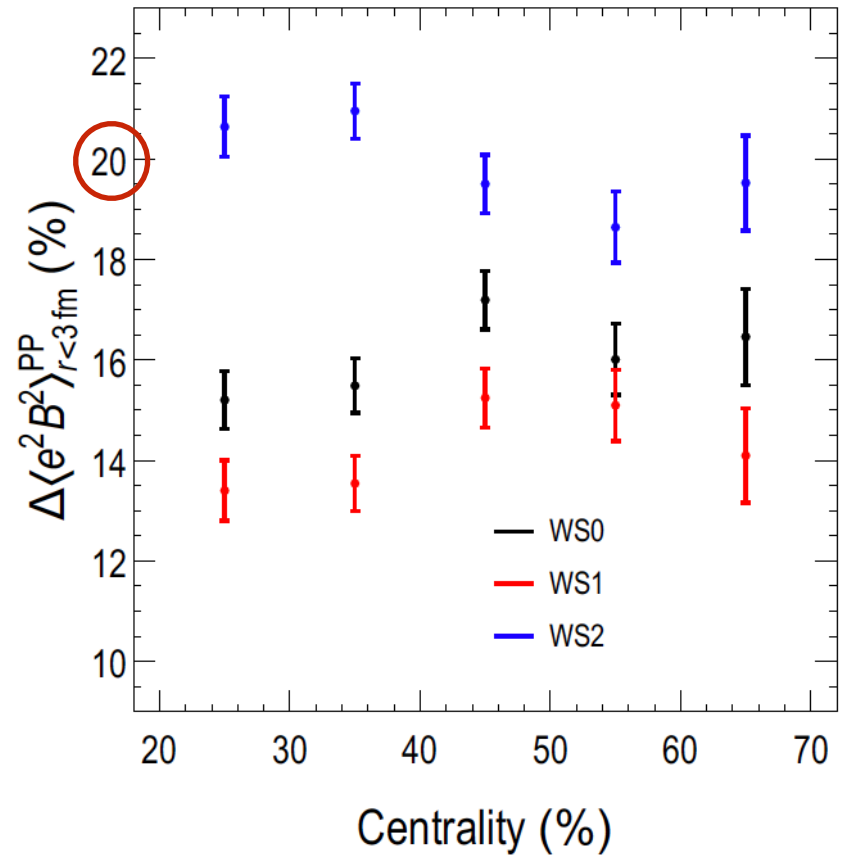
*Insight from initial conditions:
joint cut on Multiplicity-Eccentricity*

How to Choose Identical Systems?

Eccentricity is guaranteed the same!

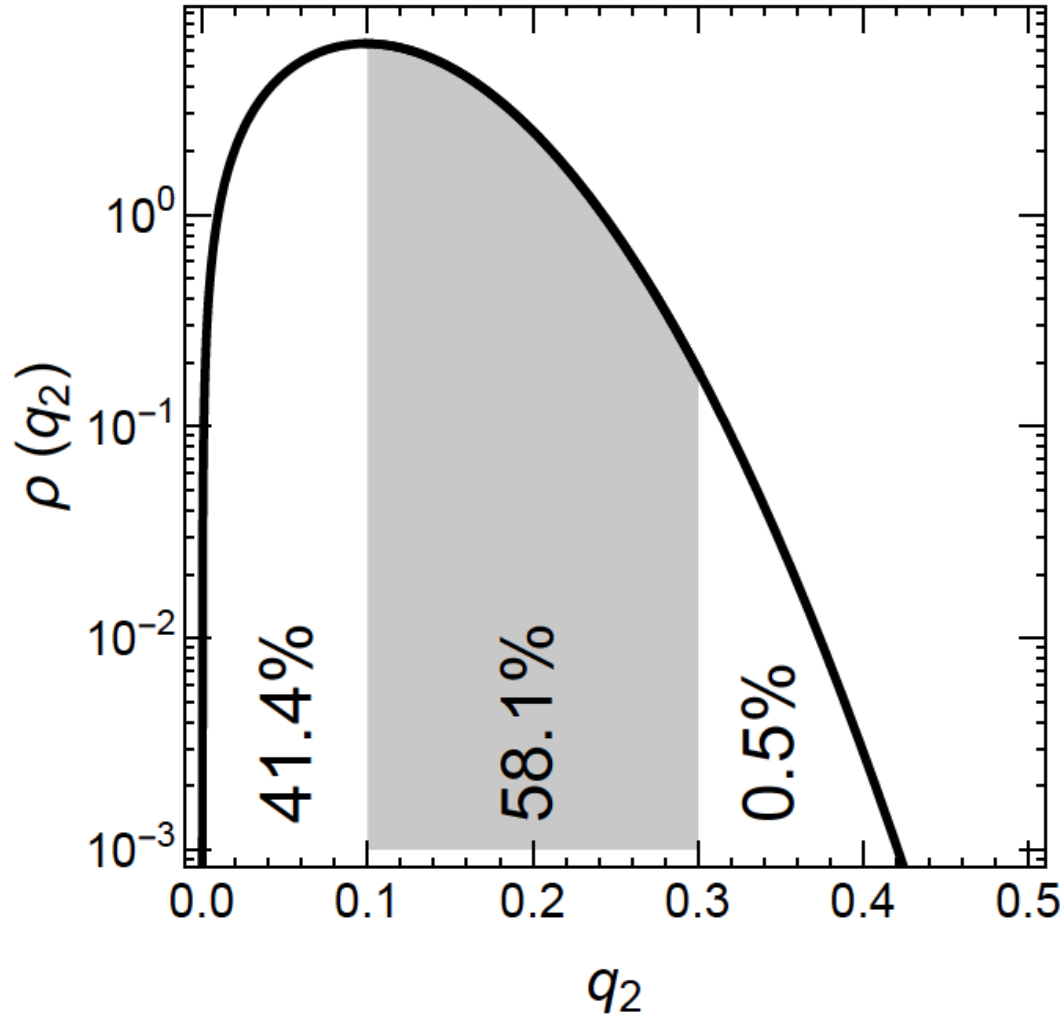


B field differs by 12~20% !



After joint-cut:
Vanishing difference in eccentricity,
Sizable difference in magnetic fields!!!

Analyzing actual EBE-AVFD for Isobars

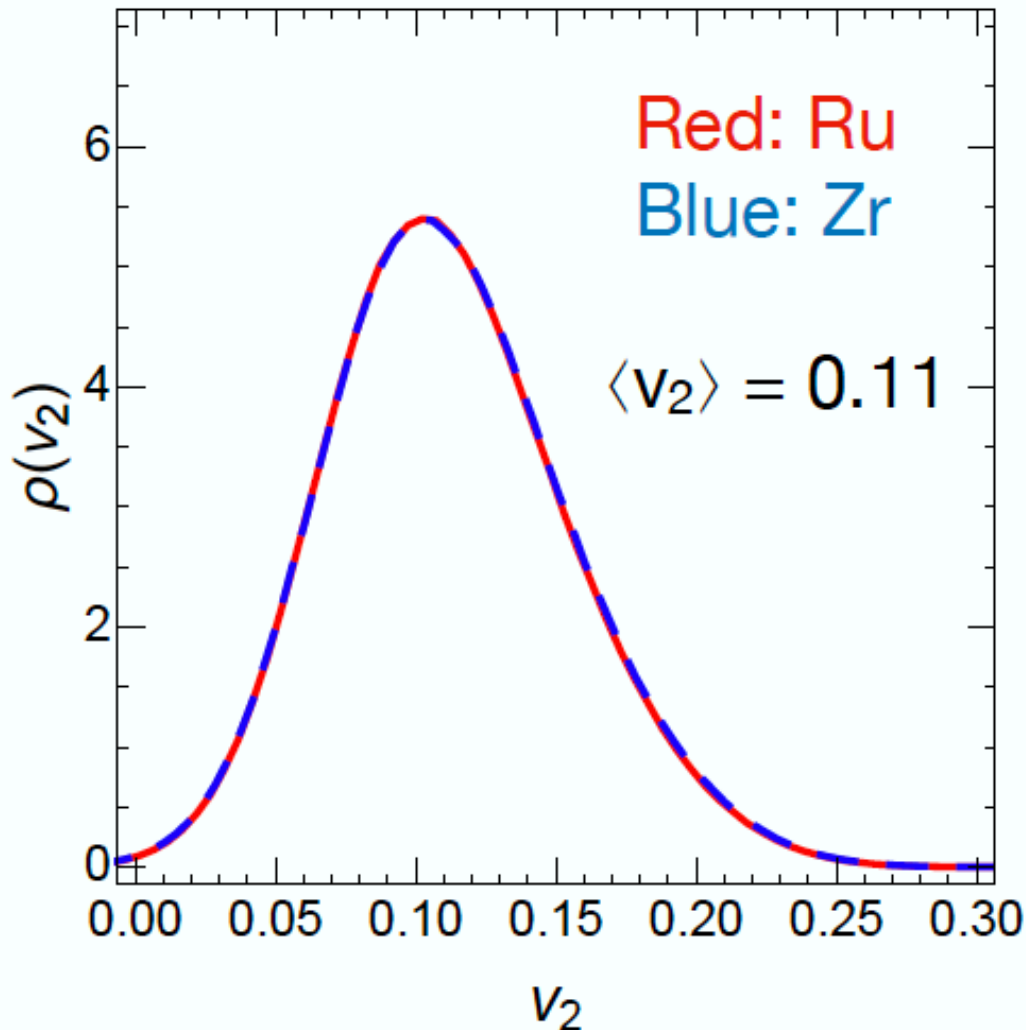


**100M EBE-AVFD events:
Subject to joint-cut**

$32 < N_{\text{ch}, |y| < 0.5} < 48$

$0.1 < q_2 < 0.3$

Analyzing actual EBE-AVFD for Isobars

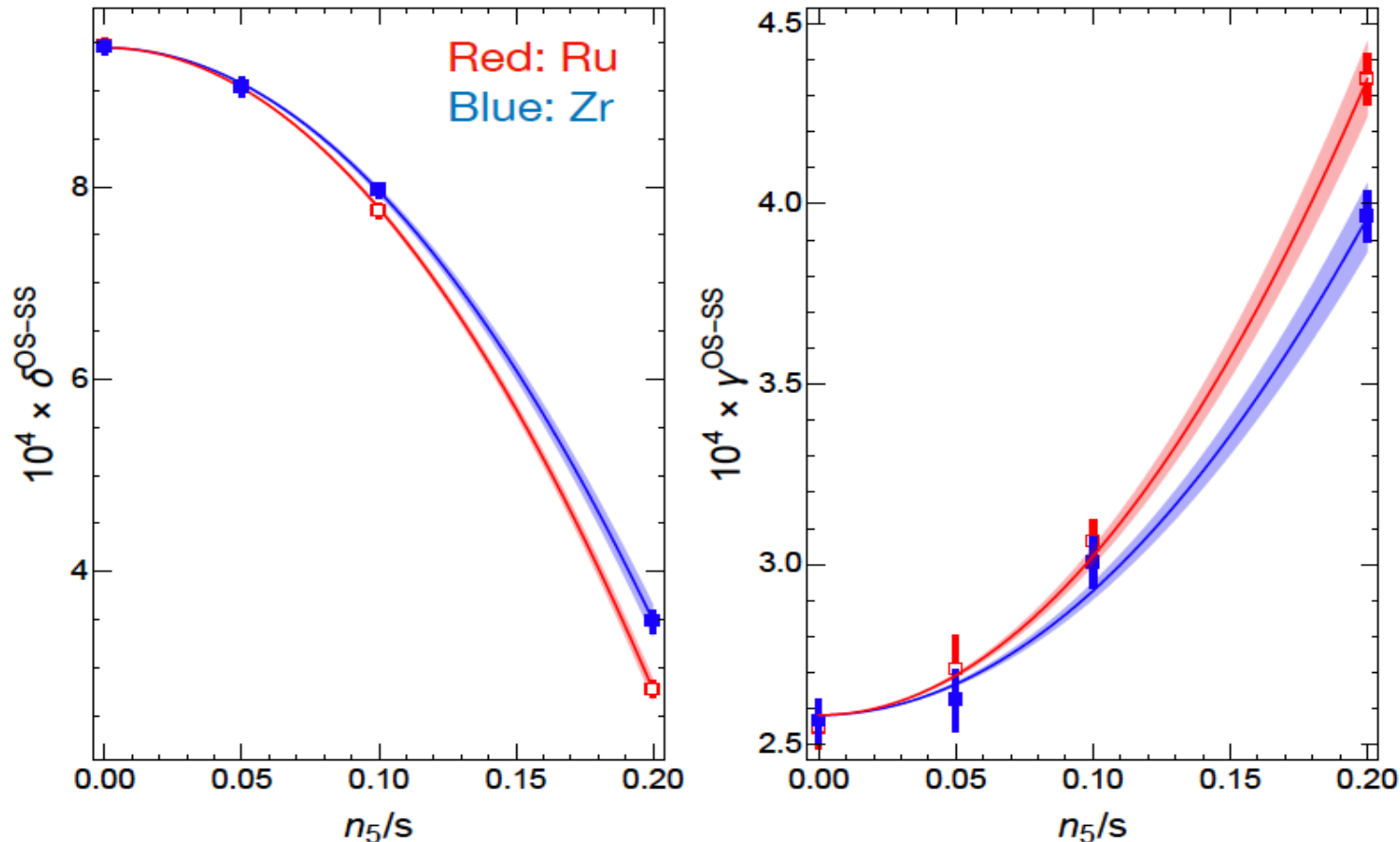


**Post-selection
double-check:
Identical v_2 !**

*Getting two identical
sample of isobar
events for contrast*

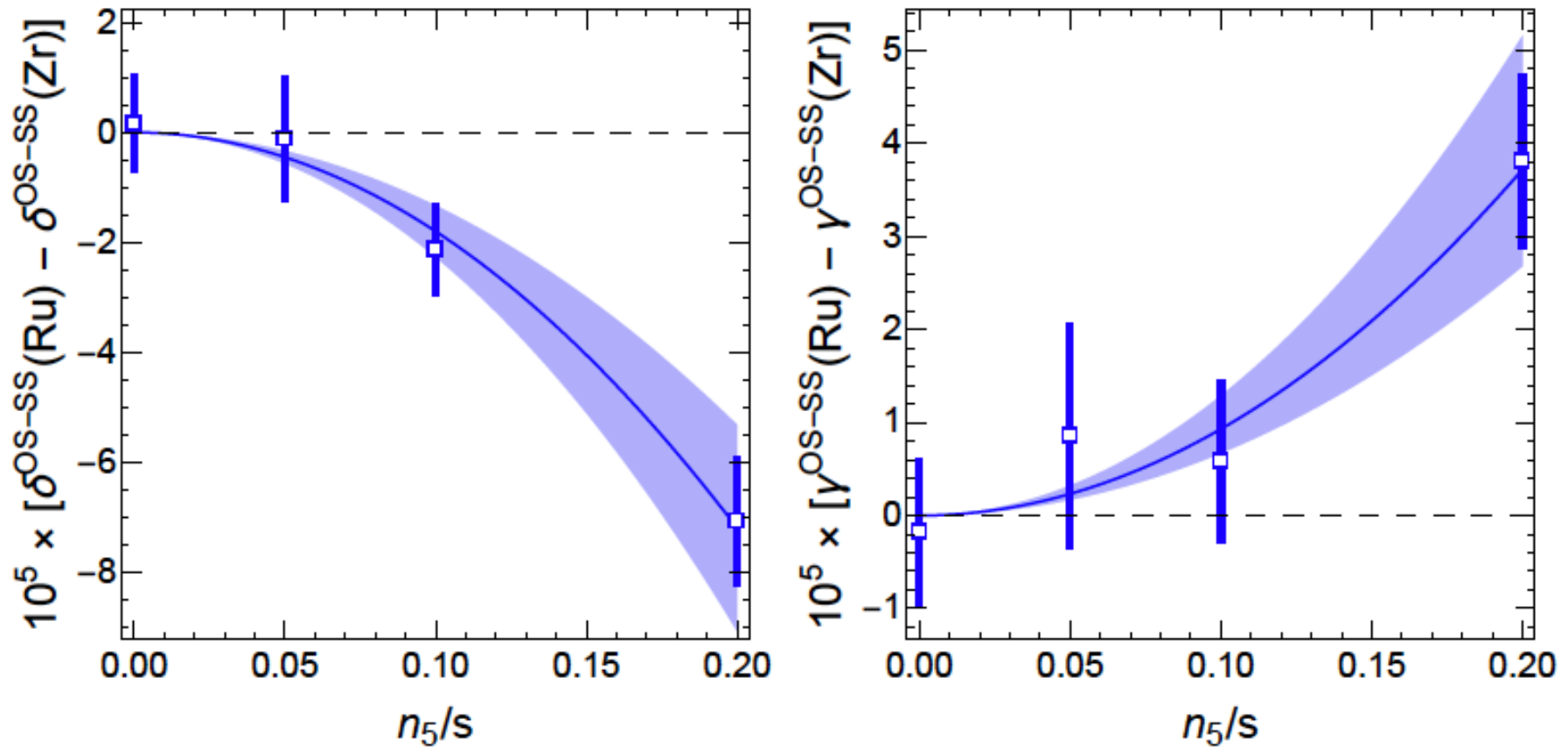
Correlations of Isobars

Points: EBE-AVFD simulation events after cut (~6M events each);
Curve: quadratic fitting, $a + b * (n_5)^2$ (as expected from CME)



Clear difference in correlations!
Very sensitive to CME contribution!

Absolute Difference between Isobars



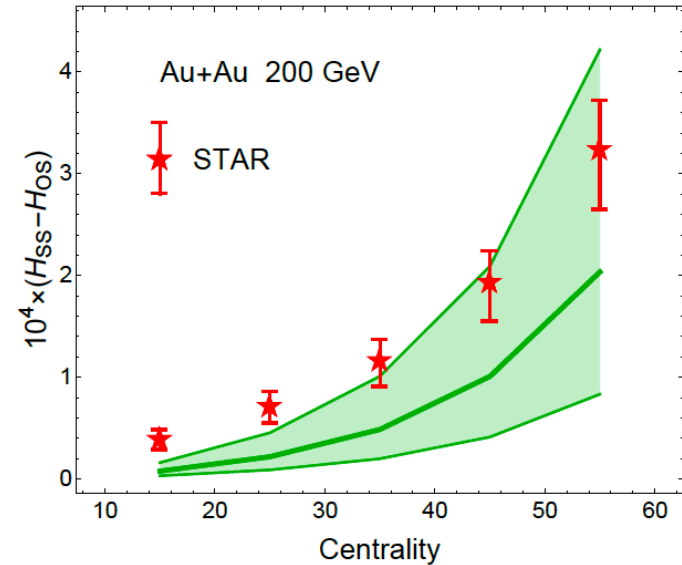
The absolute difference between isobars, after identical multiplicity+elliptic flow cuts, will provide the most sensitive and clean probe of CME signal.

Summary & Outlook

Summary

AVFD:

A versatile tool for an era of quantitative study of CME signals in heavy ion collisions !



EBE-AVFD for the Isobars:

- 1) Event selection for truly identical bulk;
- 2) Absolute difference in correlations very sensitive to CME!

