



Pion-kaon femtoscopy in Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV

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(for the ALICE collaboration)

Introduction

- It is impossible to measure dimensions of fireball directly due to its very small size
- Femtoscopy (or HBT technique) provides a direct tool to measure the source size

Two particle correlation function

$$C_2 = \frac{P_2(p_a, p_b)}{P_1(p_a)P_1(p_b)}$$

Koonin-Pratt Equation,

PLB70 (1977) 43, S. Pratt et al., PRC42 (1990) 2646

$$C(q) = \int d\mathbf{r} |\psi(q, \mathbf{r})|^2 S(\mathbf{r})$$

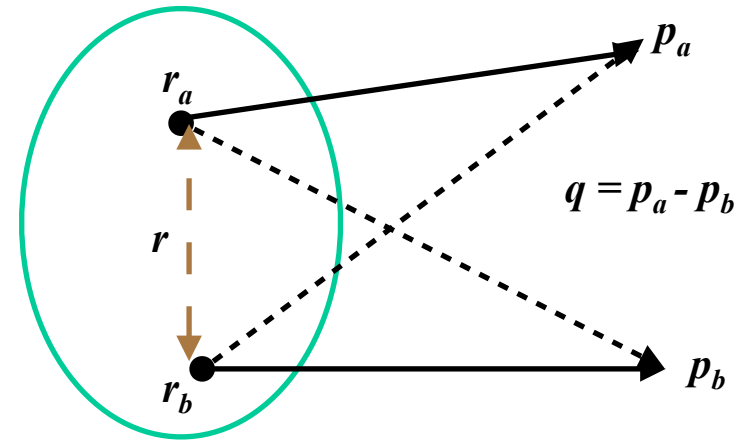
Experimental correlation function

Pair wave function

Source function

→ $P_2(p_a, p_b)$ – probability of detection of particles with momenta p_a and p_b

→ $P_1(p_i)$ – probability of detection of particle with momentum p_i



Relevant coordinate system

Longitudinal co-moving system (LCMS):

A rest frame moving along the beam direction such that $P_z = 0$

$$V_{long} = (P_0 V_z - P_z V_0) / M_T$$

$$V_{side} = (P_x V_y - P_y V_x) / P_T$$

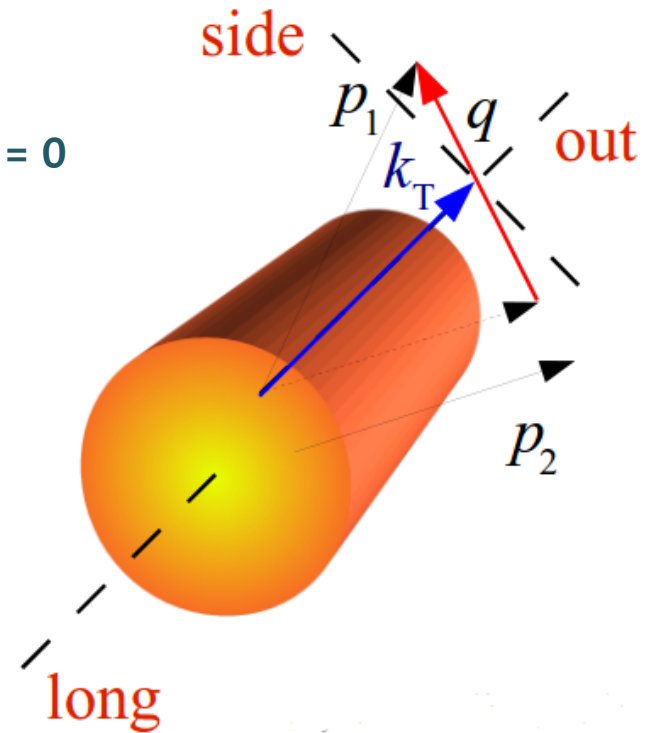
$$V_{out} = (P_x V_x + P_y V_y) / P_T$$

Pair rest frame (PRF):

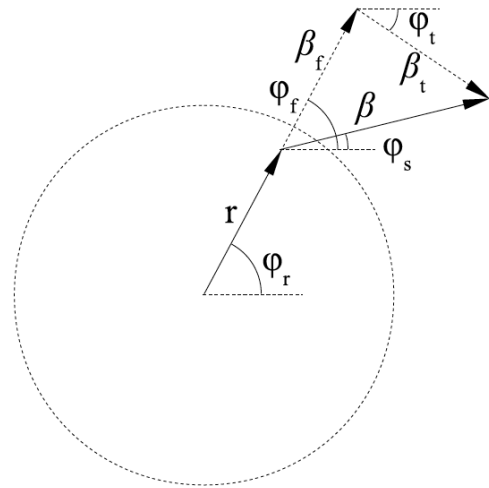
$$V'_{out} = \frac{M_{inv}}{M_T} \frac{(P_x V_x + P_y V_y)}{P_T} - \frac{P_T}{M_T M_{inv}} P \cdot V$$

Where $M_T^2 = P_0^2 - P_z^2$, $P_T^2 = P_x^2 + P_y^2$ and $M_{inv}^2 = P^2$

Pion-kaon femtoscopy analysis has been performed in PRF



Why non-identical particles ?



Adam Kisiel, *Phy.Rev.C* **81**, 064906 (2010)

$$\beta_{particle} = \beta_f + \beta_t$$

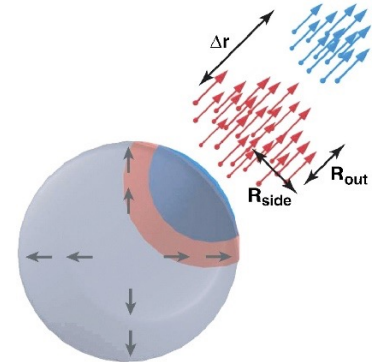
component of mean emission point of a single particle parallel to the velocity

$$\langle x_{out} \rangle = \frac{\langle r \beta_f \rangle}{\langle \sqrt{\beta_t^2 + \beta_f^2} \rangle} = \frac{r_0 \beta_0 \beta}{\beta_0^2 + T/m_t}$$

assume a Gaussian density profile with radius r_0 and linear transverse velocity profile $\beta_f = \beta_0 r/r_0$

emission asymmetry

$$\mu_{out}^{light,heavy} = \langle r_{out}^{light,heavy} \rangle = \langle x_{out}^{light} - x_{out}^{heavy} \rangle$$



- Emission asymmetry only arises in a system where both random (thermal) and correlated (flow) velocities exist and are comparable in magnitude
- Identical particle femtoscopy - source size
- Non-identical particle femtoscopy - source size plus emission asymmetry

Experimental Correlation function

$$C(\mathbf{k}^*) = \frac{N(\mathbf{k}^*)}{D(\mathbf{k}^*)}$$

distribution of k^* of pairs from same events

distribution of k^* of pairs from mixed events

where k^* : momentum of the first particle (pions) in PRF

Method 1. Cartesian representation (CC)

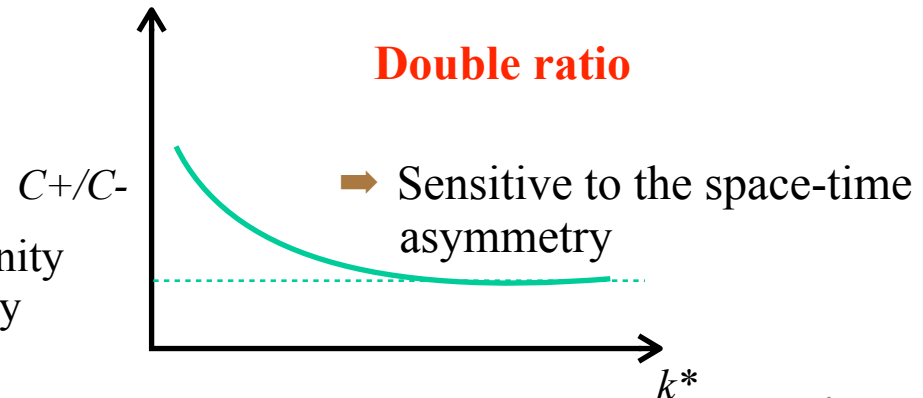
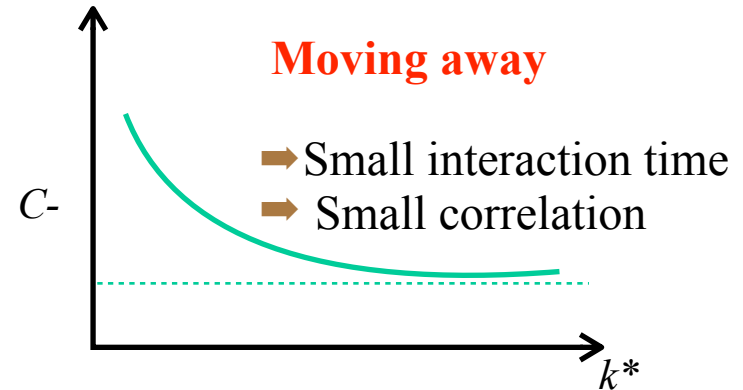
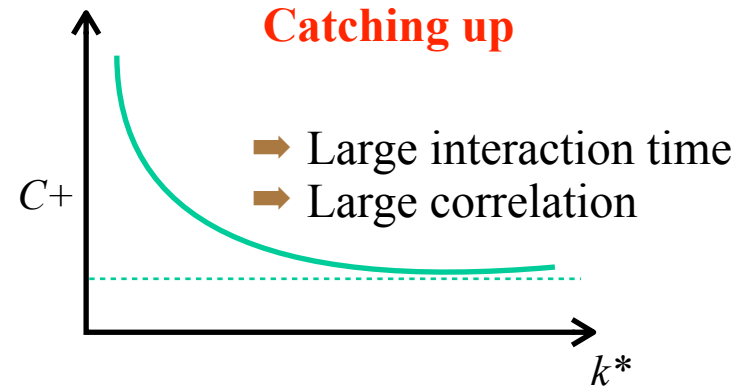
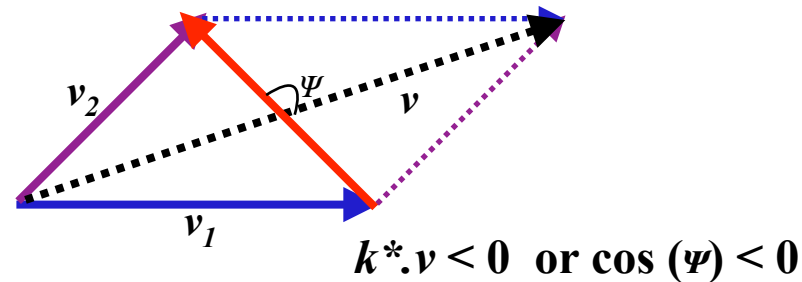
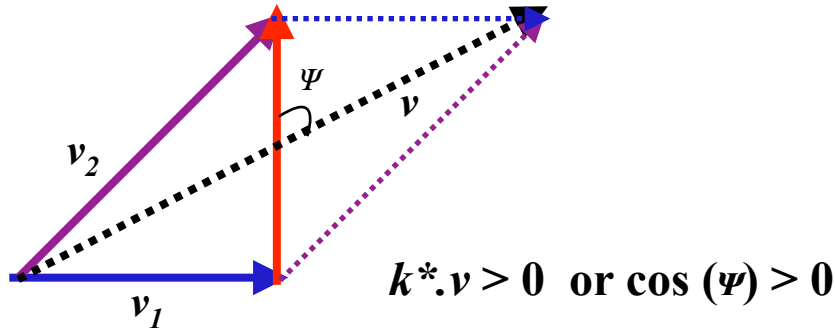
Measured Correlation functions can be divided into two groups:

- C+ : \mathbf{k}^* and \mathbf{v} aligned ($\mathbf{k}^* \cdot \mathbf{v} > 0$) i.e. pions are faster
- C- : \mathbf{k}^* and \mathbf{v} anti-aligned ($\mathbf{k}^* \cdot \mathbf{v} < 0$) i.e. kaons are faster.
- Double ratio C+/C- : sensitive to emission asymmetry (if unity - no asymmetry)

Method 2. Spherical Harmonics representation (SH)

- 3D correlation function converted into infinite set of 1D functions in terms of spherical harmonics (Y_l^m).
 - ➔ C_0^0 - reflects the growth of the overall system size;
 - ➔ $\text{Real}(C_l^l)$ - sensitive to emission asymmetry (if zero - no asymmetry)
 - ➔ Other terms vanish because of symmetry

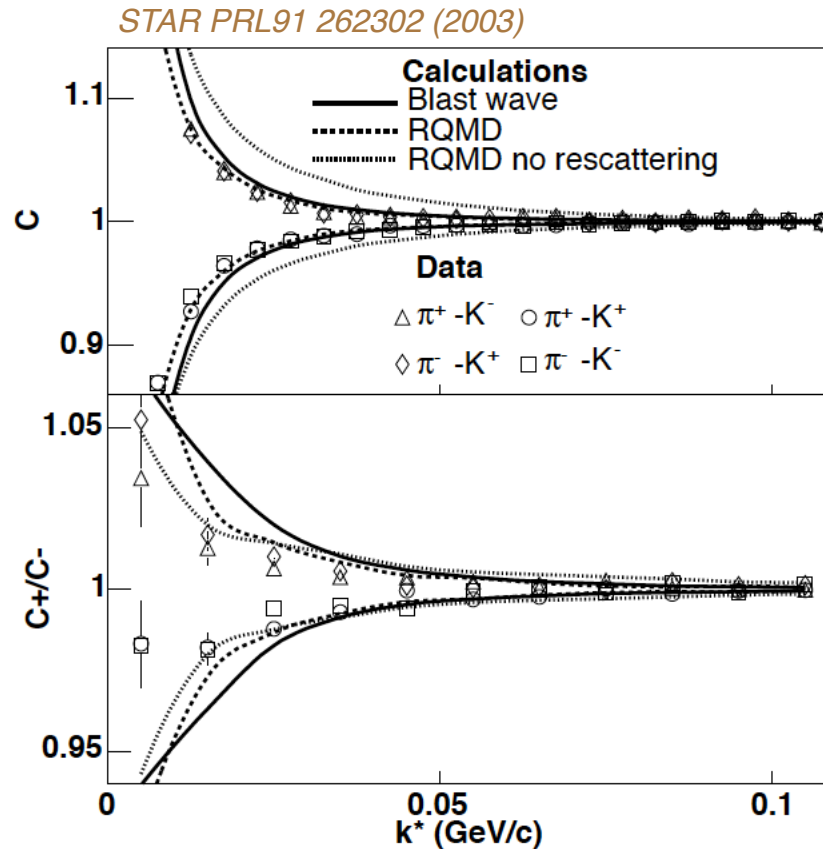
Probing space-time asymmetry



- C_+/C_- and $\text{Real}(C_I^I)$ (unlike-sign pairs) : above unity
- C_+/C_- and $\text{Real}(C_I^I)$ (like-sign pairs) : below unity

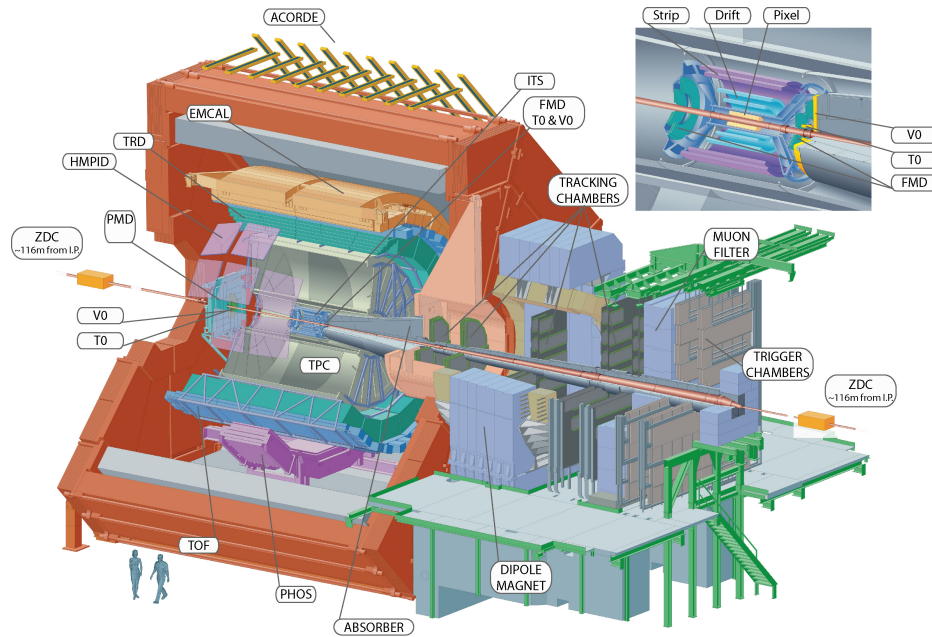
Previous measurement : STAR Au-Au @ 130 GeV

- Emission asymmetry observed between kaons and pions
- On average, pions are emitted closer to the centre/later than kaons



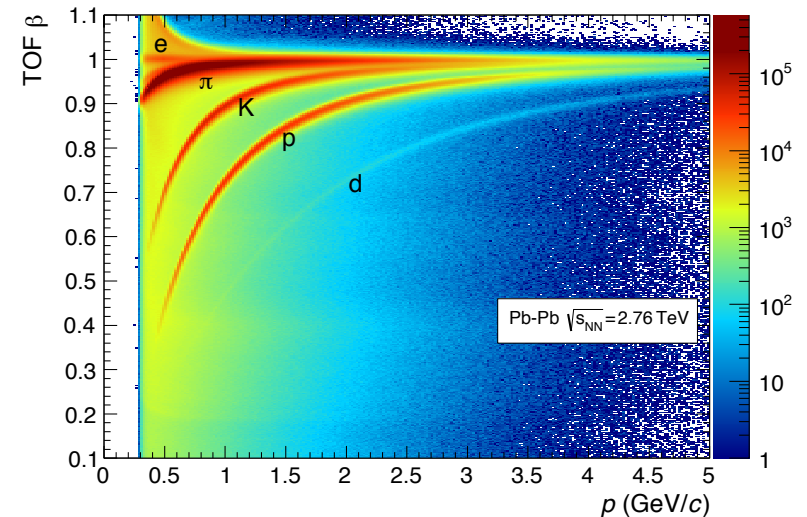
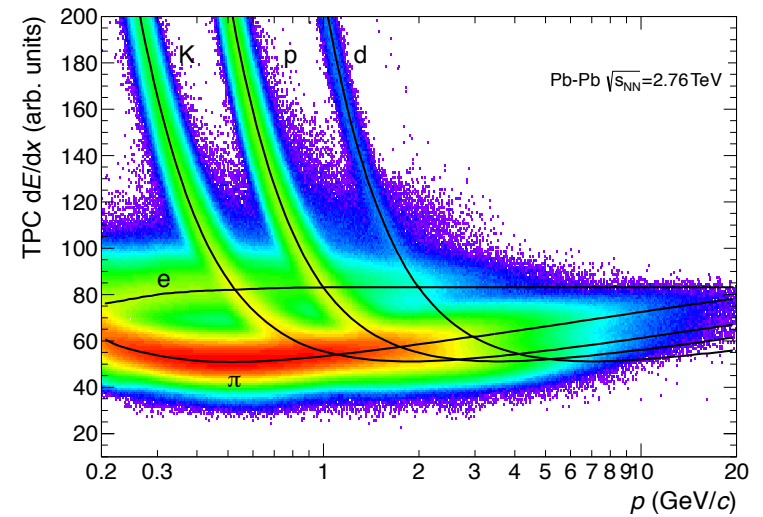
New STAR results : talk by Sebastian Siejka

ALICE detector

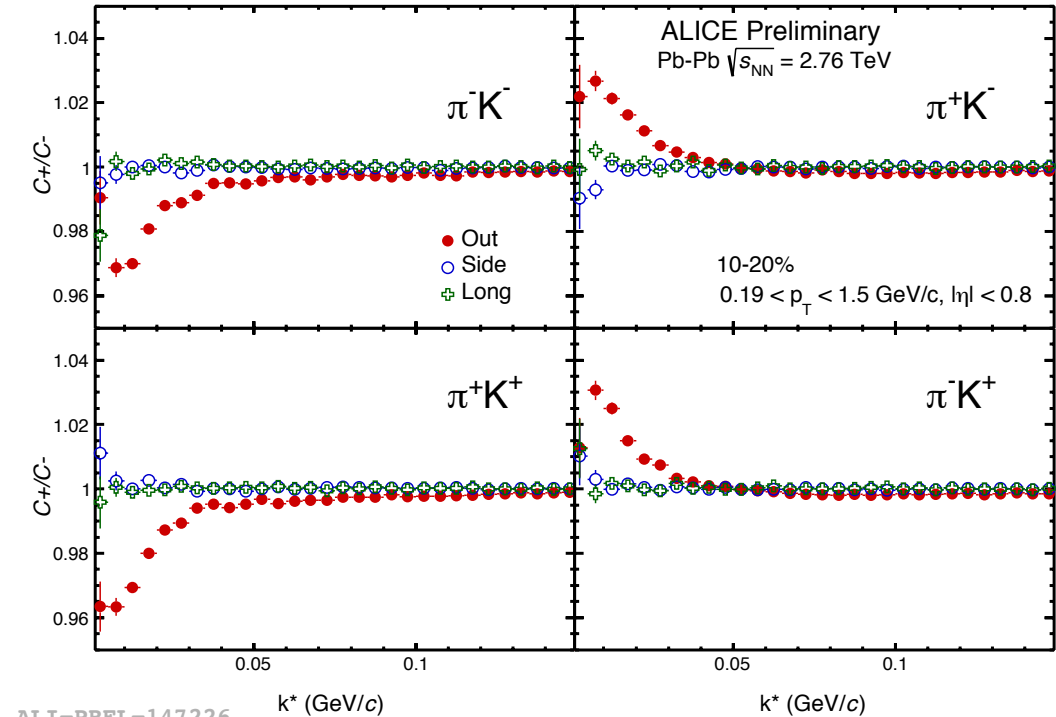
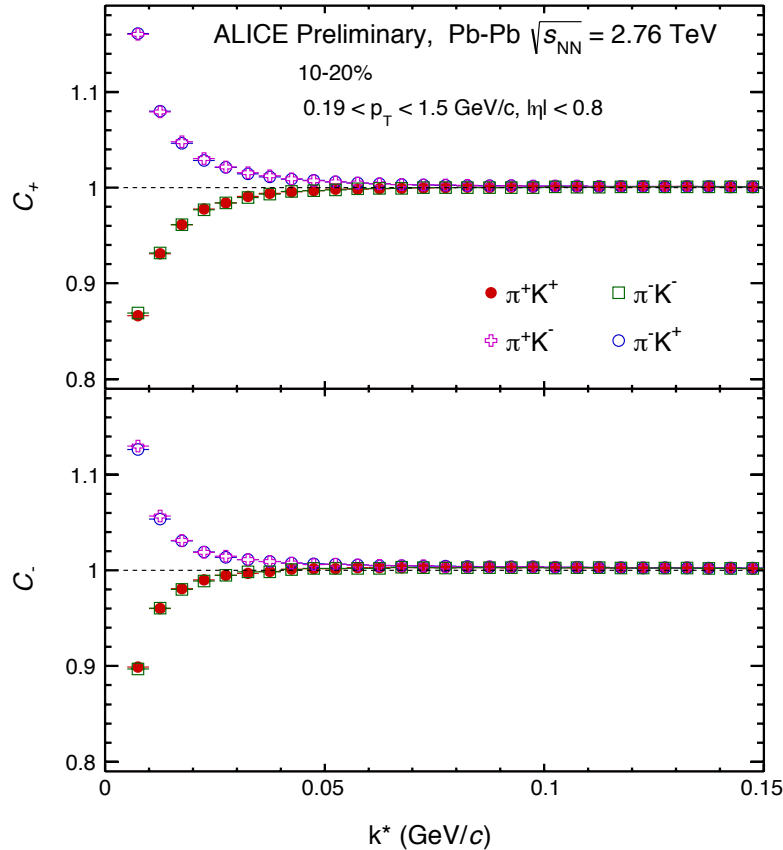


p_T range: 0.19-1.5 GeV/c, $|\eta| < 0.8$

- Excellent tracking by ALICE detector enables us to analyse correlations of particles with low momentum
- TPC was used for track reconstruction
- TPC and TOF are used for particle identification



Correlation Functions (Cartesian representation)



ALI-PREL-147226

- Double ratio (C_+/C_-) in “out” direction deviates significantly from unity
- On average, pions are emitted closer to the centre/later than kaons
- Double ratio (C_+/C_-) in “side” and “long” directions is consistent with unity

Correlation Functions (Spherical Harmonics)

attractive correlation
for unlike-sign pairs &
repulsive for like-sign pairs

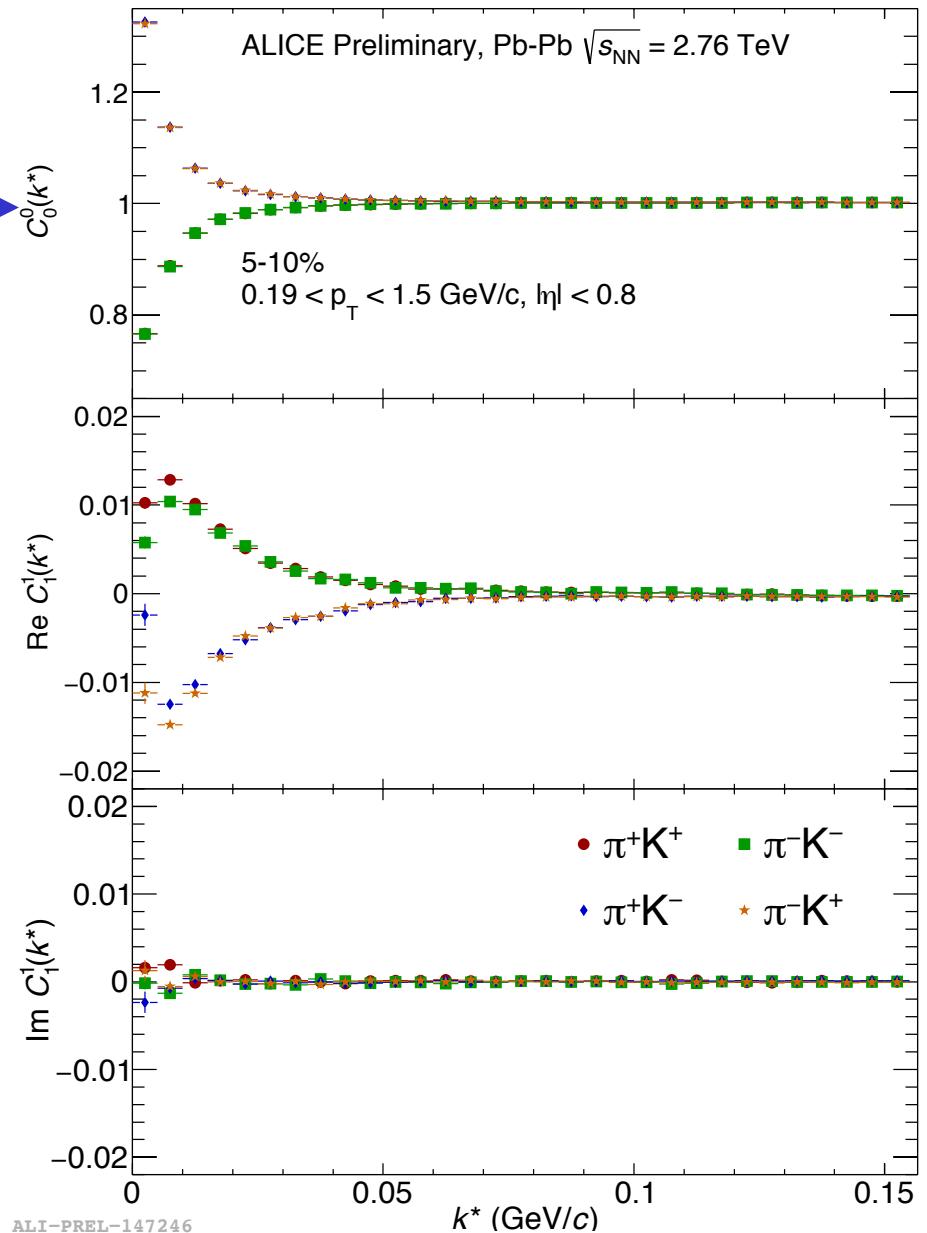
$C_0^0(k^*)$

Significantly deviates from
unity - asymmetry exists

$\text{Re } C_1^1(k^*)$

Required to vanish due
to symmetries

$\text{Im } C_1^1(k^*)$



Non-femtoscopic background

Correlation function contains femtoscopic correlation as well as contributions from:

- elliptic flow v_2
- global energy and momentum conservation
- resonance decay correlations
- residual correlations (remnants of the femtoscopic correlations from weakly decaying particles)

Background correction :

$$C_{exp}^{ij} = B^{ij} + |\psi^{ij}|^2 \quad \text{where } i,j \text{ are } +,- \text{ (pion-kaon)}$$

Experimental correlation function

Non-femtoscopic background

real femtoscopic correlation

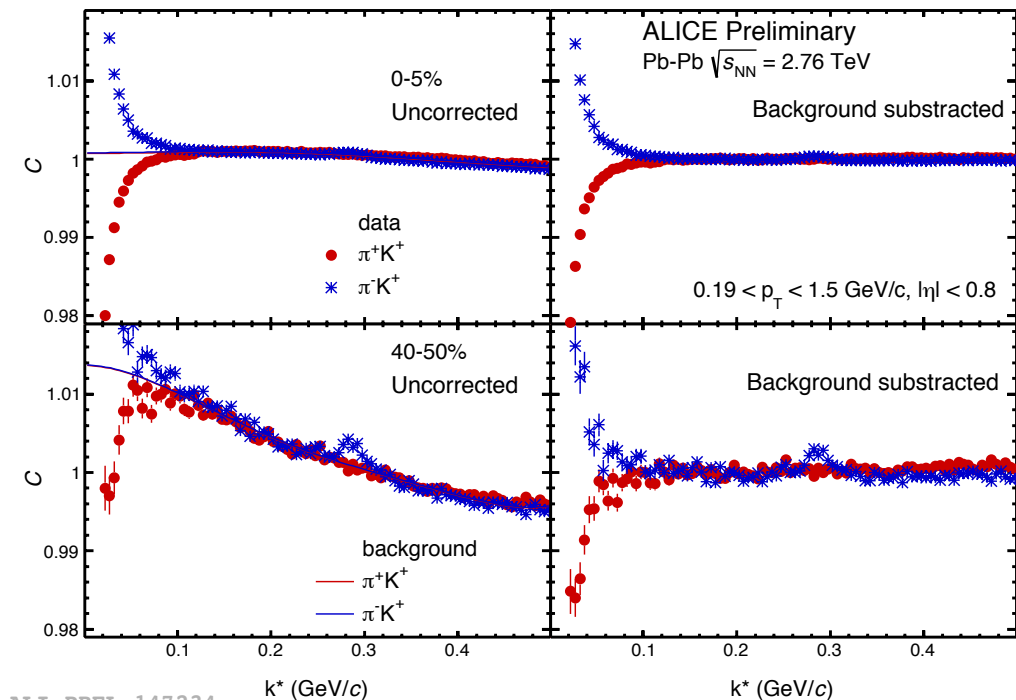
$$B^{ij} = a_0^{ij} + \sum_{l=1}^5 a_l x^{(l+1)}$$

*Adam Kisiel, ACTA PHYSICA POLONICA B,
Vol. 48 (2017)*

$$C_{real}^{ij} = C_{exp}^{ij} - B^{ij}$$

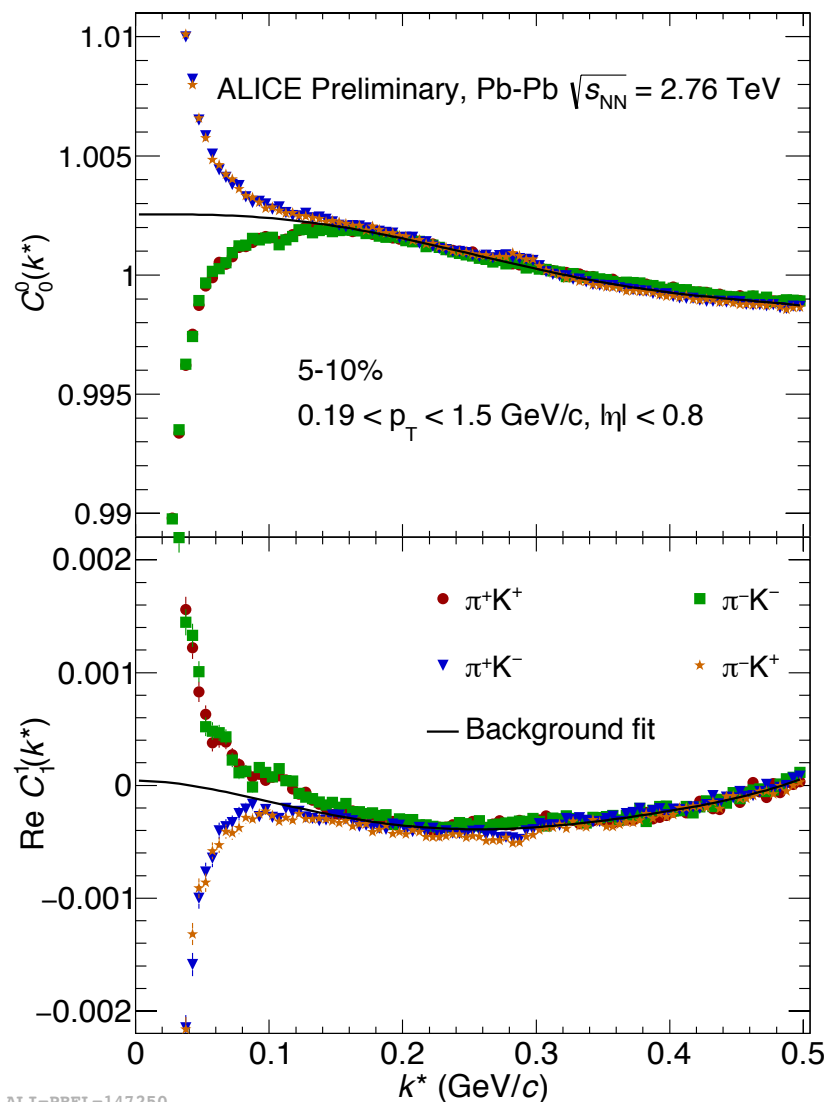
Non-femtoscopic background contribution in the data

Cartesian representation



- Non-femtoscopic background function shape changes from central to peripheral collisions

Spherical Harmonics



Extracting the source size and emission asymmetry

$$C(k^*) = \int d\mathbf{r}' |\psi(k^*, \mathbf{r}')|^2 S(\mathbf{r}')$$

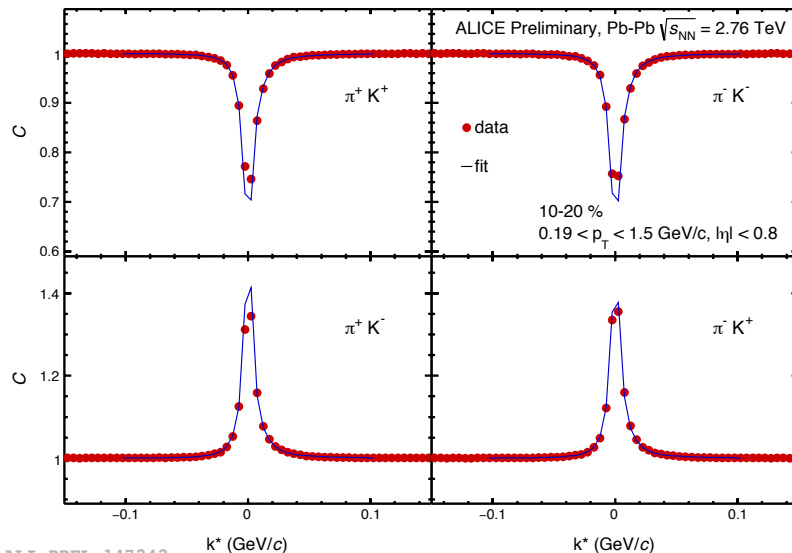
known

unknown

$$S(\mathbf{r}) = \exp \left(-\frac{(r_{out} - \mu_{out})^2}{R_{out}^2} - \frac{r_{side}^2}{R_{side}^2} - \frac{r_{long}^2}{R_{long}^2} \right)$$

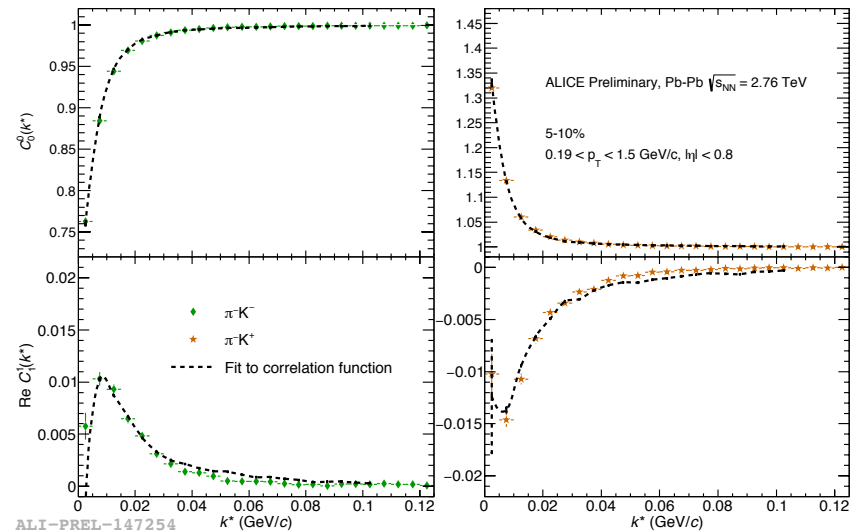
- ★ $R_{side} = \alpha R_{out}$, $R_{long} = \gamma R_{out}$, α is fixed to 1, γ is fixed to 1.3 based on identical pion femtoscopic measurements
- ★ Can't measure R_{out} , R_{side} , R_{long} and μ_{out} together (too many free parameters), need more statistics to measure C_{0^0} , C_{1^1} , C_{0^2} and C_{2^2} components for it

Cartesian representation



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Spherical Harmonics



ALI-PREL-147254

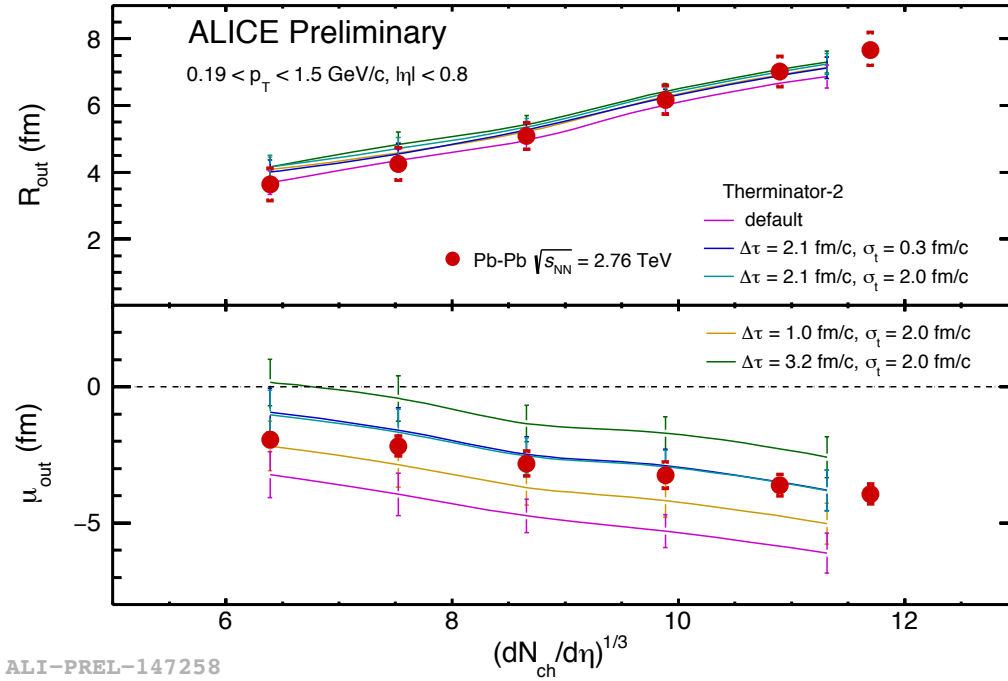
Extraction using CorrFit package (Adam Kisiel, NUKLEONIKA 2004;49(Supplement 2):S81–S83)

Quark Matter (14-19 May 2018)

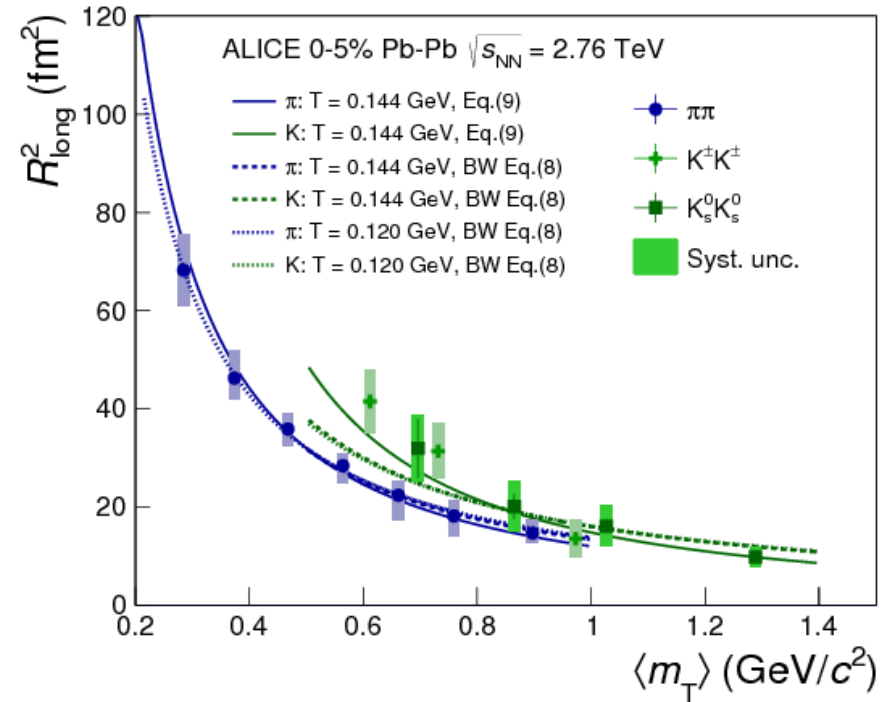
Ashutosh Kumar Pandey (IIT BOMBAY)

Results: source size and emission asymmetry

[10.1103/PhysRevC.96.064613](https://arxiv.org/abs/10.1103/PhysRevC.96.064613)



ALI-PREL-147258



- Significant pion-kaon emission asymmetry is observed which increases with centrality.
- Source size increases from peripheral to central collisions
- Blast-wave fits of ALICE identical pion and kaon data show 2.1 fm/c delay between pion and kaon average emission time.
- The pion-kaon data is consistent with such delay. It is independent and possibly more precise measurement of such delay

Therminator-2 results : Adam Kisiel, [arXiv:1804.06781](https://arxiv.org/abs/1804.06781)

Summary

- First measurement of emission asymmetry at the LHC in Pb-Pb collisions at 2.76 TeV
- Results indicate that “pions emitted closer to the centre/earlier than kaons”
- It is expected in a system with strong collectivity which includes flow of resonances (consistent with model predictions, e.g. Therminator2)
- Source size increases from peripheral to central collisions
- Results may suggest a 2.1 fm/ c delay in emission time which means different particle species freeze-out at different times

THANK YOU