#### HELMHOLTZ SPITZENFORSCHUNG FÜR **GROSSE HERAUSFORDERUNGEN**

HGS-HIRe for FAIR Helmholtz Graduate School for Hadron and Ion Research



# Shear viscosity and resonance lifetimes in the hadron gas

#### Jean-Bernard Rose

with D. Oliinychenko, J. Torres-Rincon, A. Schäfer, J. Hammelmann, H. Petersen

based on Phys Rev C 97.055204 (arXiv:1709.03826) and arXiv:1709.00369

Helmholtz International Center







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## Viscosity in heavy ion collisions

 RHIC and LHC measured large elliptic flow at the high energies corresponding to what is thought to be QGP



http://www.quantumdiaries.org/wp-content/uploads/2011/02/FlowPr.jpg

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- RHIC and LHC measured large elliptic flow at the high energies corresponding to what is thought to be QGP
- Hydrodynamics relatively successful at explaining this with small η/s



Luzum & Romatschke 10.1103/Phys. Rev. C 78.034915

## Viscosity in heavy ion collisions

- RHIC and LHC measured large elliptic flow at the high energies corresponding to what is thought to be QGP
- Hydrodynamics relatively successful at explaining this with small η/s
- Still not clear what the behavior of η/s is at low energies (FAIR, late stage RHIC/LHC)



### Previous HG viscosity calculations



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## Modelling the hadron gas: SMASH

See talk by H. Petersen earlier today at 12:30 in Collective Dynamics session



- SMASH is a new semi-classical transport approach for the hadron gas
- Geometric collision criterion:

$$d_{trans} < d_{int} = \sqrt{\frac{\sigma_{tot}}{\pi}}$$

• Spectral functions of resonances are described by relativistic Breit-Wigner functions, with resonance lifetime

$$\tau_{\rm res} = \frac{1}{\Gamma(m)}$$

- Elastic scatterings parameterized for NN; all other elastic scatterings assumed to go through resonances
- Inelastic scatterings, currently include
  - $NN \leftrightarrow NR, NN \leftrightarrow \Delta R$
  - $KN \leftrightarrow KN, KN \leftrightarrow \pi H$
  - +antiparticles
- Strings (turned off for detailed balance)

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#### **Green-Kubo Formalism**





## Equilibrium in SMASH

- Box calculations simulating infinite matter to apply the Green-Kubo procedure
- MUST have thermal & chemical equilibrium
- Baryon/antibaryon annihilation implemented to conserve detailed balance via an average decay to 5π





## Test case #1: $\pi$ with constant $\sigma$



J. Torres-Rincon, PhD dissertation (2012), Hadronic Transport Coefficients from Effective Field Theories

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### Test case #2: π-ρ gas

 Normal SMASH run does not coincide directly with Chapman-Enskog





## Hadron Gas: Degrees of freedom

Ν	Δ	٨	Σ	Ξ	Ω	Unflavored				Strange
N <sub>938</sub>	Δ <sub>1232</sub>	$\Lambda_{1116}$	Σ <sub>1189</sub>	Ξ <sub>1321</sub>	Ω <sup>-</sup> <sub>1672</sub>	π <sub>138</sub>	f <sub>0 980</sub>	f <sub>2 1275</sub>	π <sub>2 1670</sub>	K <sub>494</sub>
N <sub>1440</sub>	$\Delta_{1620}$	$\Lambda_{1405}$	Σ <sub>1385</sub>	Ξ <sub>1530</sub>	Ω <sup>-</sup> 2250	$\pi_{1300}$	f <sub>0 1370</sub>	f <sub>2 1525</sub>		K* <sub>892</sub>
N <sub>1520</sub>	Δ <sub>1700</sub>	$\Lambda_{1520}$	Σ <sub>1660</sub>	Ξ <sub>1690</sub>		$\pi_{1800}$	f <sub>0 1500</sub>	f <sub>2 1950</sub>	$ ho_{31690}$	К <sub>1 1270</sub>
N <sub>1535</sub>	$\Delta_{1905}$	$\Lambda_{1600}$	Σ <sub>1670</sub>	Ξ <sub>1820</sub>			f <sub>0 1710</sub>	f <sub>2 2010</sub>		K <sub>1 1400</sub>
N <sub>1650</sub>	Δ <sub>1910</sub>	$\Lambda_{1670}$	Σ <sub>1750</sub>	Ξ <sub>1950</sub>		η <sub>548</sub>		f <sub>2 2300</sub>	$\Phi_{31850}$	K* <sub>1410</sub>
N <sub>1675</sub>	Δ <sub>1920</sub>	$\Lambda_{1690}$	Σ <sub>1775</sub>	Ξ <sub>2030</sub>		η' <sub>958</sub>	a <sub>0 980</sub>	f <sub>2 2340</sub>		K <sub>0</sub> * <sub>1430</sub>
N <sub>1680</sub>	Δ <sub>1930</sub>	$\Lambda_{1800}$	Σ <sub>1915</sub>			$\eta_{1295}$	a <sub>0 1450</sub>		a <sub>4 2040</sub>	K <sub>2</sub> * <sub>1430</sub>
N <sub>1700</sub>	Δ <sub>1950</sub>	$\Lambda_{1810}$	Σ <sub>1940</sub>			$\eta_{1405}$		f <sub>1 1285</sub>		K* <sub>1680</sub>
N <sub>1710</sub>		$\Lambda_{1820}$	Σ <sub>2030</sub>			$\eta_{1475}$	$\Phi_{1019}$	f <sub>1 1420</sub>	f <sub>4 2050</sub>	К <sub>2 1770</sub>
N <sub>1720</sub>		$\Lambda_{1830}$	Σ <sub>2250</sub>				$\varphi_{1680}$			K <sub>3</sub> * <sub>1780</sub>
N <sub>1875</sub>		$\Lambda_{1890}$				$\sigma_{800}$		a <sub>2 1320</sub>		К <sub>2 1820</sub>
N <sub>1900</sub>		$\Lambda_{2100}$					h <sub>1 1170</sub>			K <sub>4</sub> * <sub>2045</sub>
N <sub>1990</sub>		$\Lambda_{2110}$				$\rho_{776}$		$\pi_{11400}$		
N <sub>2080</sub>		$\Lambda_{2350}$				$ ho_{1450}$	b <sub>1 1235</sub>	$\pi_{11600}$		
N <sub>2190</sub>		• 5	ospin sv	mmetrv		$ ho_{1700}$				
N <sub>2220</sub>		•Pe	erturbat	ive treat	ment		a <sub>1 1260</sub>	η <sub>2 1645</sub>		
N <sub>2250</sub>		of	non-hac	Ironic pa	articles	ω <sub>783</sub>				
		(pł	notons.	dilepton	s)	$\omega_{1420}$		$\omega_{31670}$		
15/05/2018	3	Jean-Be	ernard Rose		-1	$\omega_{1650}$				14

## Hadron Gas: T and $\mu_{\text{B}}$ dependence



## HG: Viscosity Comparison



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#### High temperature $\eta/s$ : Resonance lifetimes



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### High temperature $\eta/s$ : Resonance lifetimes



#### $\pi$ - $\rho$ : Zero lifetimes vs relaxation time

Large part of the difference explained from eliminating lifetimes



#### Effect of many non-resonant interactions

Introduce a constant elastic cross-section between all particles to add many non-resonant interactions



## Summary & Outlook

- Investigated temperature, cross-section and mass dependence of the shear viscosity in an elastic pion box
  - Very good agreement with Chapman-Enskog approximation (within 10%)
  - Resonance lifetimes need to be considered

#### • Full hadron gas $\eta/s$ calculated at zero and non-zero $\mu_B$

- High T discrepancy explained by looking at microscopic details of resonance modelling; finite lifetime <u>increases</u> viscosity
- Could be used to constrain the treatment of resonances

#### • Outlook:

- Investigation of angular dependent interactions on viscosity
- At temperatures close to the phase transition, inclusion of multi-particle interaction will play a role, and needs to be investigated
- Other transport coefficients (electrical conductivity, bulk viscosity, etc.)



## Backup slides



## Where to stop the fitting?

J. Torres-Rincon, PhD dissertation (2012), Hadronic Transport Coefficients from Effective Field Theories



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## Test case #2: Energy-dependent σ

- Pions in a (20 fm)<sup>3</sup> box simulating infinite matter
- Cross-section uses ρ resonance
- Runs for  $t_{max}$ =200 fm
- Initialized with initial densities consistent with Boltzmann ideal gas



## Hadron Gas

- All particles and resonances initialized to thermal multiplicities (at the pole mass)
- Must wait for equilibration and compute *T*, μ once in equilibrium from most abundant particles
  - T fitted from weighted momentum spectra of π, K & N
  - $\mu_{B} \text{ obtained from} \\ N / \text{ anti-} N \text{ ratio}$



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## What about entropy?

The entropy density can be calculated from the Gibbs formula:

$$s = \frac{e + p - \mu n}{T} = \frac{w - \mu n}{T}$$

where the energy density and pressure can be taken from the average shear-stress tensor according to:

$$T^{\mu\nu} = diag(e, p, p, p)$$

Assuming a nearly ideal gas, one can fit the temperature and chemical potential with momentum distributions:

$$\frac{dN}{dp} = \frac{g}{2\pi^2} V p^2 \exp\left(-\frac{\sqrt{p^2 + m^2} - \mu}{T}\right)$$

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## Hadron Gas: $\eta$ , s and w/T



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## Hadron Gas: Low temperature $\eta/s$

- Low temperature hadron gas is composed almost exclusively of pions
- π-π cross-section is then most relevant
  - At very low energy,
     SMASH much higher than UrQMD/χPT
  - χPT includes angular dependence, UrQMD&SMASH don't; increases viscosity by factor up to 5/3 for ρ resonance

