

Direct flow of heavy mesons as unique probes of the initial Electro-Magnetic fields in Ultra-Relativistic Heavy Ion collisions

G. Coci^{1,2}, S. Plumari^{1,2}, L. Oliva², S. K. Das^{1,3} and V. Greco^{1,2}

¹Department of Physics and Astronomy University of Catania, ²Laboratori Nazionali del Sud INFN-LNS,

³School of Nuclear Science and Technology Lanzhou University



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Introduction

In ultra-relativistic Heavy-Ion Collisions (HICs) very **strong initial Electro-Magnetic (E.M.)** fields are created inducing a vorticity in the reaction plane that is odd under charge exchange, allowing to distinguish it from the large vorticity of the bulk matter due to the initial angular momentum conservation. **Heavy Quarks (HQs)**, mainly charm and bottom, have the right features to probe the impact of this E.M. field. [1]

$M_{c,b} \gg \Lambda_{QCD}$	HQs are produced in hard pQCD processes not coupled with chiral magnetic effects.
$M_{c,b} \gg T_0$	HQ thermal production is negligible (out of equilibrium).
$\tau_f \approx 1/2M_{c,b}$	HQs formation time scale is comparable with time when E.M. field reaches maximum value.
$\tau_{eq} \geq \tau_{QGP} \gg \tau_f$	HQs probe all phase-space evolution of QGP and retain the initial kick from E.M. field.
$M_{c,b} \gg q = gT$	HQ dynamics reduced to Brownian motion, but at $T \approx 0.3$ GeV the strong coupling $g(T) \approx 2$: this condition is challenged for charm, while still good for bottom.

Objectives

In this work we describe the propagation of HQs in the Quark-Gluon Plasma (QGP) within a **relativistic Boltzmann transport approach** where we consider an enhancement of the interaction strength near critical temperature T_c according to Lattice QCD (LQCD) thermodynamics. In this framework we are able to simultaneously describe the nuclear suppression factor $R_{AA}(p_T)$ and the elliptic flow $v_2(p_T)$ of charmed mesons both at RHIC and LHC energies. [2][3]

Our main goal is to include a **time-dependent external E.M. field** based on a realistic model of E.M. charge and current density at initial stage of HICs and study its effect on HQ dynamics. The presence of an E.M. field results in a formation of a finite **direct flow** $v_1 = \langle \cos(\phi_p) \rangle = \langle p_x/p_T \rangle$. [4] Moreover, the favorable conditions presented in this Introduction are responsible of the significant enhancement of v_1 for HQs with respect to the light quark sector that hopefully could be measured as a **splitting** of $D[c\bar{q}]$ and $\bar{D}[\bar{c}q]$ mesons at RHIC and LHC experiments.

Model (I): Electro-Magnetic Field

We follow the scheme in Fig. (1a). [4]

We calculate E.M. field $E^+, B^+ (E^-, B^-)$ generated by a single charge e located at position $\vec{x}_\perp = (x_\perp, \phi)$ in transverse plane and moving towards the $+z(-z)$ direction with speed β (rapidity $\eta = \arctan(\beta)$) solving **Maxwell Equations**. [5]

$$\begin{cases} \nabla \cdot \vec{E} = \delta(z' - \beta t) \delta(\vec{x}'_\perp - \vec{x}_\perp) \\ \nabla \cdot \vec{B} = 0 \\ \nabla \times \vec{E} = -\partial_t \vec{B} \\ \nabla \times \vec{B} = (\partial_t + \sigma_{el}) \vec{E} + e\beta \delta(z' - \beta t) \delta(\vec{x}'_\perp - \vec{x}_\perp) \end{cases}$$

Then we fold these elementary fields with the nuclear transverse density profile ρ_- for spectator protons and we sum forward (η) and backward ($-\eta$) contributions (Eq.(1)) for \vec{B}_s and similar for \vec{E}_s . Results for E.M. as function of evolution time are shown in Fig. (1b).

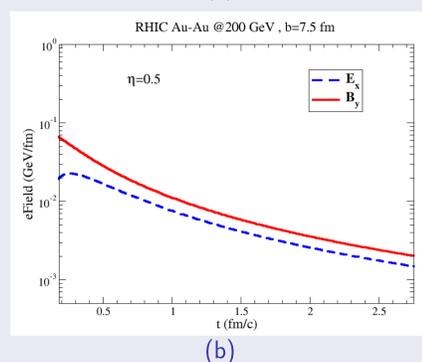
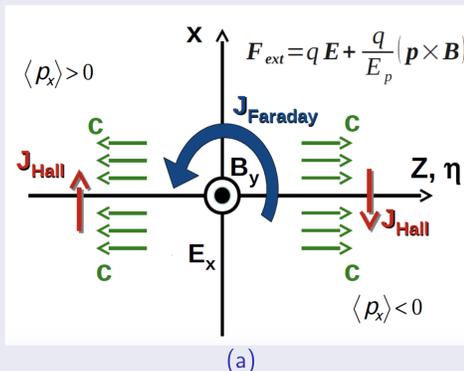


Figure 1: 1(a) Illustration of v_1 formation due to E.M. field in HICs. 1(b) Time variation of \vec{B} and \vec{E} dominant components at fixed η .

$$e\vec{B}_s = -Ze \int d\phi' dx'_\perp x'_\perp \rho_-(x'_\perp, \phi') \left[\vec{B}_s^+(\tau, \eta, x_\perp, \phi) + \vec{B}_s^-(\tau, -\eta, x_\perp, \phi) \right] \quad (1)$$

Time variation of \vec{B} induces an electric field \vec{E} , i.e. a **Faraday current** in the conducting QGP $\vec{J}_{Faraday} = \sigma_{el} \vec{E}$. Meanwhile Lorentz force $q\vec{v} \times \vec{B}$ acts on longitudinal expanding medium and drifts charged particles along the direction orthogonal to \vec{B} and flow velocity akin to the classical **Hall effect** (\vec{J}_{Hall}). The combination of $\vec{J}_{Faraday} + \vec{J}_{Hall}$ leads to a charge and rapidity odd dependent v_1 . We assume also:

- 1) Constant electric conductivity from LQCD ($\sigma_{el} = 0.023 \text{ fm}^{-1}$).
- 2) Neglect bulk modification due to E.M. currents.
- 3) No event-by-event fluctuations.

Model (II): Boltzmann Equation

We describe HQ dynamics in QGP by means of **Relativistic Boltzmann Equation**:

$$\left[p_\mu \partial_x^\mu + qF_{\mu\nu}(x) p^\nu \partial_p^\mu \right] f_{HQ} = C_{22}[f_{HQ}] \quad (2)$$

The single particle phase-space distribution function $f_{HQ}(x, p)$ is sampled using **test-particle method**. The Boltzmann-like collision integral $C_{22}[f_{HQ}]$ is the kernel of elastic scattering between charm and bulk partons and it is solved by means of a **stochastic algorithm**. [2]

$F_{\mu\nu}$ is the Maxwell strength field constructed from \vec{B} and \vec{E} (see: Model (I)).

Main ingredients:

- (a) HQ p_T -spectra from FONLL [Cacciari et al. 2012], while quarks and gluons distributed according to thermal + minijet ($p_T \geq 2-3$ GeV).
- (b) Shadowing is included as a parametrization of EPS09 [Eskola et al. 2009].
- (c) Interaction between charm and bulk partons, in terms of drag coefficient $\gamma(T) = \tau_{eq}^{-1}$, has a nearly constant behavior close to T_c and slightly increases with T : $\gamma \approx 0.15 - 0.3 \text{ fm}^{-1}$. [2]
- (d) Charm **Hadronization** by **coalescence + fragmentation** model. [6]

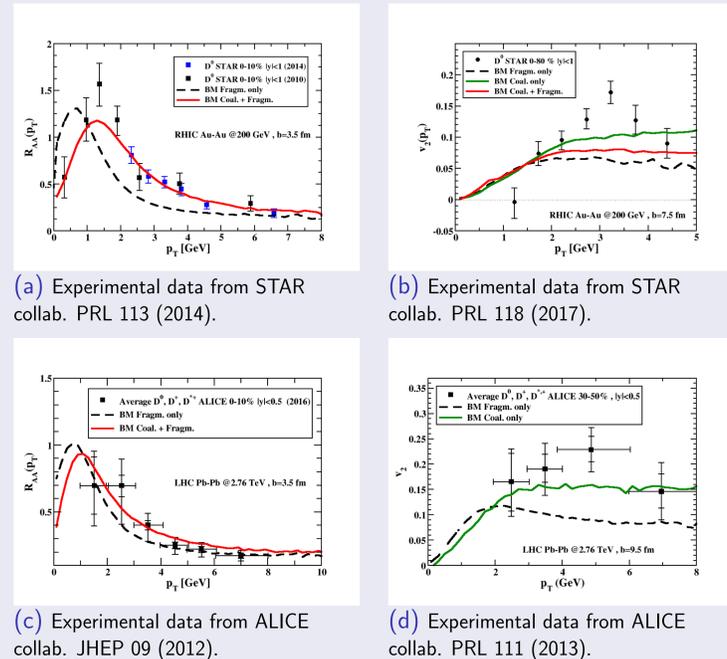


Figure 2: $R_{AA}(p_T)$ and $v_2(p_T)$ of D mesons at RHIC and LHC within Boltzmann transport approach.

Results and Conclusions

In Fig. (3a) we present our predictions for the direct flow v_1 of $D-\bar{D}$ at RHIC energies as function of rapidity. Following charm evolution we have observed that v_1 **saturates** at $t \approx 1-2 \text{ fm}$ which is consistent with the time of persistence of intense E.M. field (see Fig.(1b)). In Fig. (3b) we relate the amount of produced v_1 due to initial E.M. field with thermalization time τ_{eq} of charm quarks. [1]

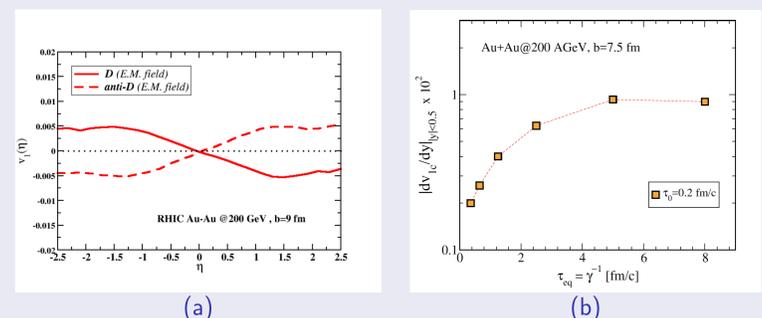


Figure 3: 3(a) Predicted $v_1(\eta)$ for $D-\bar{D}$ at RHIC collisions. 3(b) Slope parameter of charm direct flow $|dv_{1c}/d\eta|$ at mid-rapidity from same conditions at RHIC as function of charm drag coefficient γ .

Our results indicate that v_1 is an excellent probe for investigating the strong E.M. field created at initial stage of HICs.

PRELIMINARY: Within this model we can also introduce an initial vorticity due to angular momentum conservation and study its effects on HQ dynamics coupled to E.M. field looking at possible changes on the production of v_1 . (see Fig.(4)). [7]

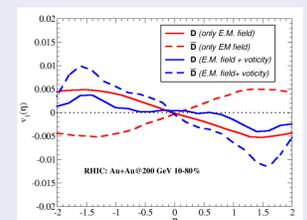


Figure 4: $v_1(\eta)$ for $D-\bar{D}$ mesons in Boltzmann model coupled to initial E.M. field and vorticity.

References

- [1] S. K. Das, S. Plumari, S. Chatterjee, J. Alam, F. Scardina, V. Greco, PLB 768 (2017) 260-264.
- [2] F. Scardina, S. K. Das, V. Minissale, S. Plumari, V. Greco, PRC 96 (2017) no. 4 044905.
- [3] S. K. Das, F. Scardina, S. Plumari, V. Greco, PLB 747 (2015) 260-264.
- [4] U. Gürsoy, D. Kharzeev, K. Rajagopal, PRC 89 (2014) no. 5 054905.
- [5] K. Tuchin, PRC 88 (2013) no. 2 024911.
- [6] S. Plumari, V. Minissale, S. K. Das, G. Coci, V. Greco, Eur. Phys. J. C 78 (2018) no. 4, 348.
- [7] G. Coci, L. Oliva, S. Plumari and V. Greco in preparation.