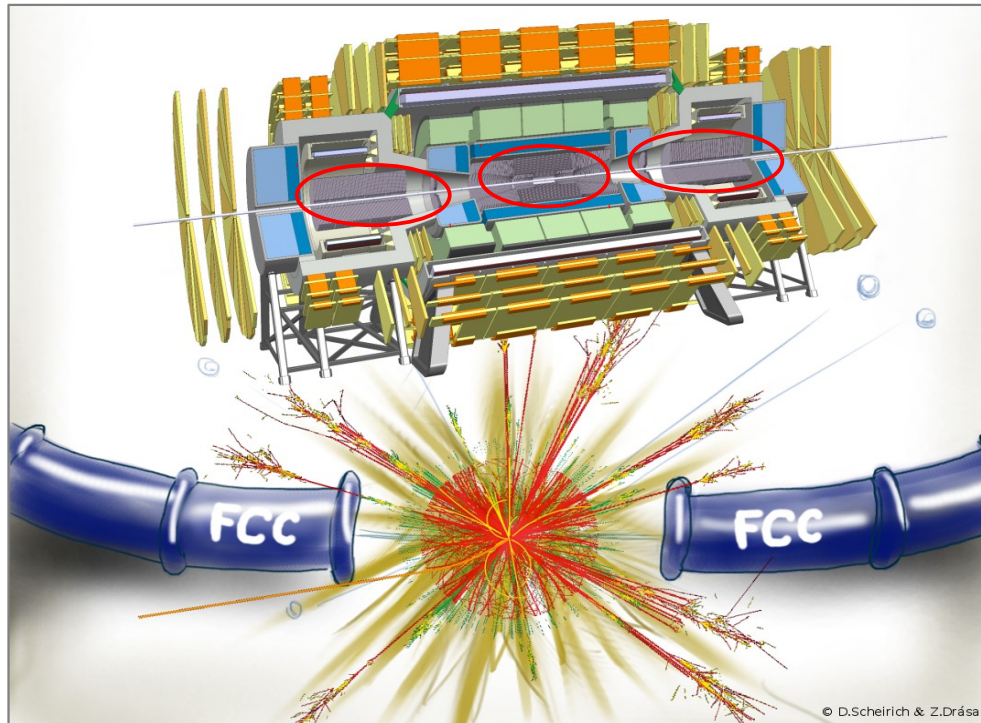


Status and Challenges of Tracker Design for FCC-hh



Zbyněk Drásal

CERN & Charles University Prague

With special thanks to: M.Mannelli, S.Mersi & W.Riegler



Overview

- Tracker/vertex detector design & expected performance
 - Key FCC-hh challenges & design driving principles
 - Mathematical approach & SW tools
 - Reference layout & tracking performance
 - Effects of non-uniform magnetic field: solenoid vs. dipole
 - Implications of high pile-up & high-rate/occupancy environment
 - Pattern recognition capabilities & requirements on granularity in Z, tilted vs. flat layout
 - Primary vertexing in high pile-up & requirements on timing resolution
- Summary & Challenges

FCC-hh & Challenges for Tracker Design

Parameter	FCC-hh		HE-LHC	(HL) LHC
Collision cms energy [TeV]	100		27	14
Dipole field [T]	16		16	8.33
Circumference [km]	97.75		26.7	26.7
# IP	2 main & 2		2 & 2	2 & 2
Beam current [A]	0.5		1.12	(1.12) 0.58
Bunch intensity [10^{11}]	1	1 (0.2)	2.2 (0.44)	(2.2) 1.15
Bunch spacing [ns]	25	25 (5)	25 (5)	25
beta* [m]	1.1	0.3	0.25	(0.20) 0.55
Luminosity/IP [$10^{34} \text{ cm}^{-2}\text{s}^{-1}$]	5	30	25	(5) 1
# Events/bunch crossing	170	<1020 (204)	~800 (160)	(135) 27
Stored energy/beam [GJ]	8.4		1.3	(0.7) 0.36
Synchrotron rad. [W/m/ap.]	28.4		4.6	(0.33) 0.17

14TeV \rightarrow 100 TeV
 $\sigma_{\text{inelastic}}$: 80mb \rightarrow 108mb
 average p_T : 0.6 \rightarrow 0.8 GeV/c
 multiplicity_{charged/unit η} : 5.4 \rightarrow 8

5x increase in pile-up wrt HL-LHC

- The min. bias events @FCC are quite similar to ones @HL-LHC, but ...
 - \rightarrow Pile-up per bunch crossing **O(1000)** is a big challenge

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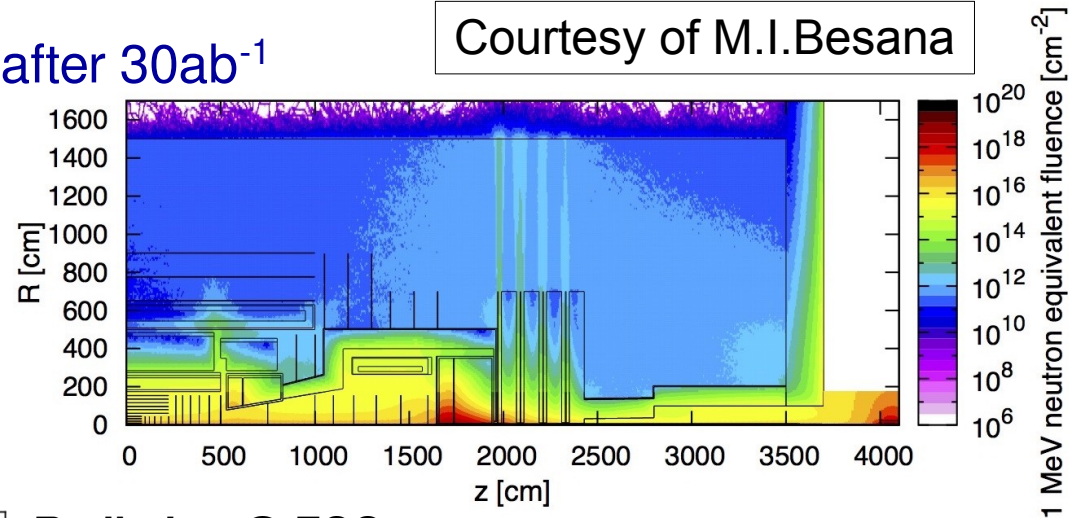
6x increase in luminosity
 wrt HL-LHC

- The min. bias events @FCC are quite similar to ones @HL-LHC, but ...
 - \rightarrow Pile-up per bunch crossing **O(1000)** is a big challenge
 - \rightarrow Huge particle/data rates & significantly higher rad. levels in the inner/fwd detector are expected due to luminosity increase

Tracker: Long-term Damage & Data Rates

- Fluka simulation: 1 MeV neq fluence after 30ab⁻¹

Courtesy of M.I.Besana



Long-term damage for Tracker after 30ab⁻¹

R [mm]	z[m]	Dose [MGy]	1 MeV equivalent Fluence [cm ⁻²]
25	0	320	5.5 10 ¹⁷
60	0	88	1.25 10 ¹⁷
100	0	40	6 10 ¹⁶
150	0	23	3.3 10 ¹⁶
270	0	8.8	1.51 10 ¹⁶
900	0	0.65	3.2 10 ¹⁵
25	5	410	3.7 10 ¹⁷
50	16	250	2 10 ¹⁷

Radiation @ FCC:

→ @R=25mm: ~6x10¹⁷ neq cm⁻², TID~0.4GGy

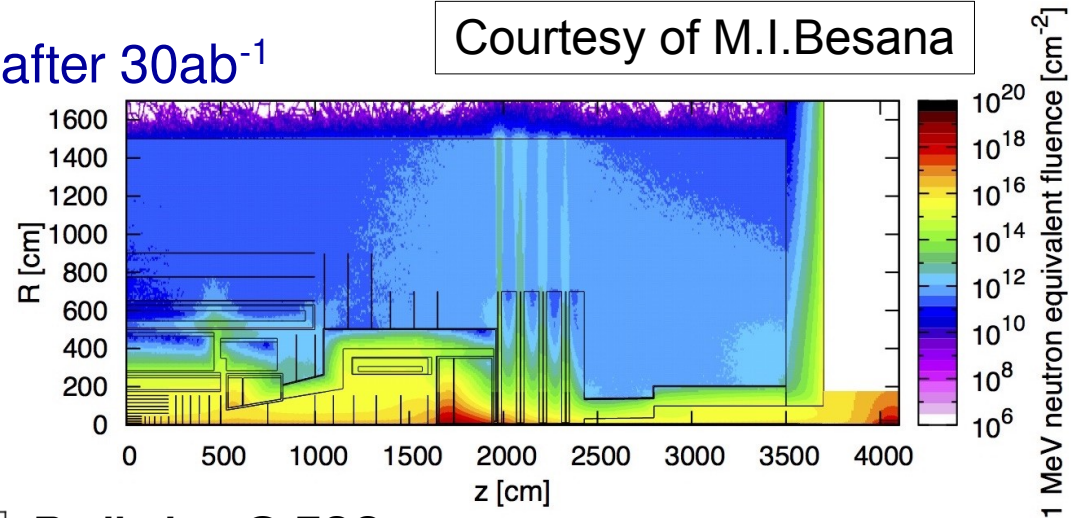
- LHC = 1
- HL-LHC → 20x LHC
- FCC → 600x LHC

→ HL-LHC rad. tolerance limit @R~270mm

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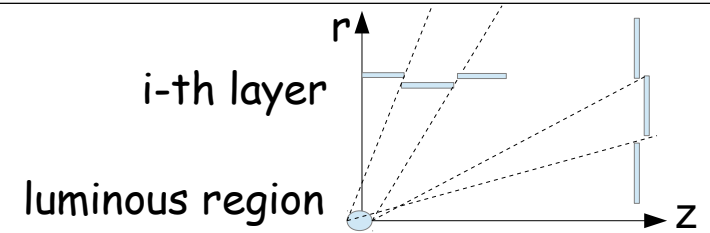
HL-LHC rad. tolerance limit @R~270mm

True challenge for sensor/chip R&D & high fluence rates for data output (trigger)

- data rates: **766 TB/s** (@40MHz), **19 TB/s** (@1MHz)
- data flows in innermost layers: **≥1Gb/s/cm² @1MHz**

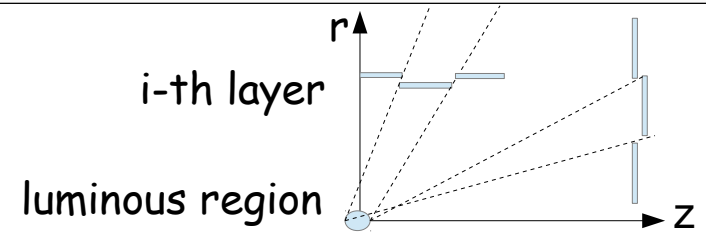
Tracker: Layout & Design Driving Principles

- **Hermetic tracking up-to $|\eta| \sim 4$** (c.f. $|\eta| \sim 2.5$ for LHC exp.)
+ efficient **VBF jet meas. up-to $|\eta| \sim 6$**



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- **Granularity in $R-\Phi$** \rightarrow driven by dp_T/p_T , efficient b,c, τ -tagging (d0) & low occupancy limit ($\sim 1\%$)

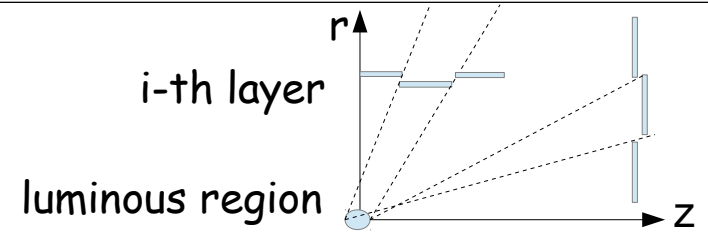
$$\frac{\Delta p_T}{p_T} = \frac{\sigma[\text{m}] p_T[\text{GeV}/c]}{0.3 B[\text{T}] L^2[\text{m}^2]} f(N)$$

L: 1.55m
B: uniform 4T
 $\sigma_{R-\Phi}$: 10(7.5)um

$\sim 20\%$ @ 10TeV/c (cf. LHC: 10% @1TeV)

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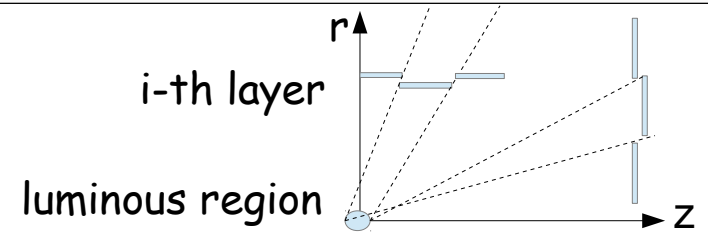
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- Note:** res. improves as $1/\sqrt{N_{\text{layers}}}$, but material budget (MB) increases as N_{layers}
- Low MB important!**
 $N_{\text{layers}} : 12$

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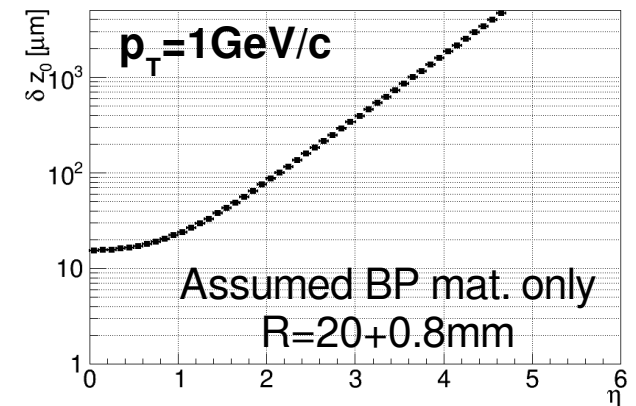
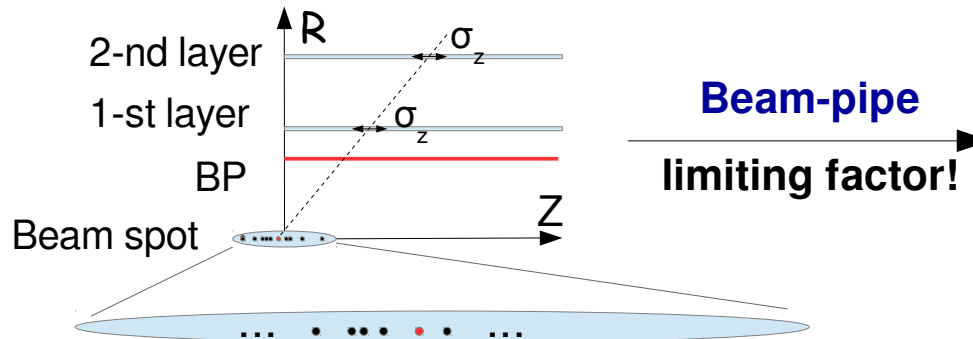


- **Granularity in R- Φ** \rightarrow driven by dp_T/p_T , efficient b,c, τ -tagging (d0) & low occupancy limit ($\sim 1\%$)

$$\left. \begin{array}{l} \frac{\Delta p_T}{p_T} = \frac{\sigma[\text{m}] p_T[\text{GeV}/c]}{0.3 B[\text{T}] L^2[\text{m}^2]} f(N) \\ L: 1.55\text{m} \\ B: \text{uniform } 4\text{T} \\ \sigma_{R-\Phi}: 10(7.5)\mu\text{m} \end{array} \right\} \sim \mathbf{20\% @ 10\text{TeV}/c} \text{ (cf. LHC: } 10\% \text{ @ } 1\text{TeV)}$$

- **Number of layers N** \rightarrow driven by dp_T/p_T (sensitivity to low p_T tracks) & pattern recognition } **Low MB important!**
Note: res. improves as $1/\sqrt{N_{\text{layers}}}$, but material budget (MB) increases as N_{layers} } **$N_{\text{layers}}: 12$**

- **Granularity in Z** \rightarrow driven by pattern recognition, low occupancy limit ($\sim 1\%$) & primary vertexing in expected pile-up **$O(1000)$**

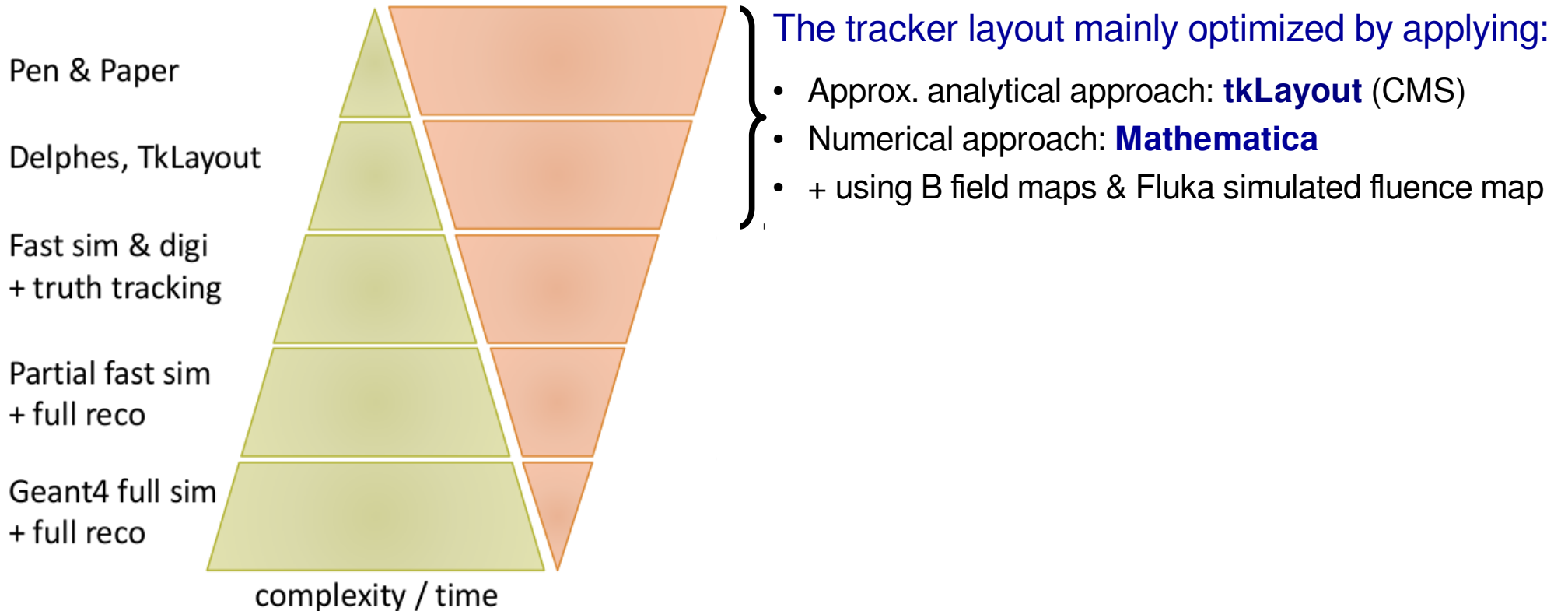


Mathematical Techniques & SW Tools

- **Extremely important to choose the right tools given the tight schedule for CDR...**

Picture by A.Salzburger

detector layouts

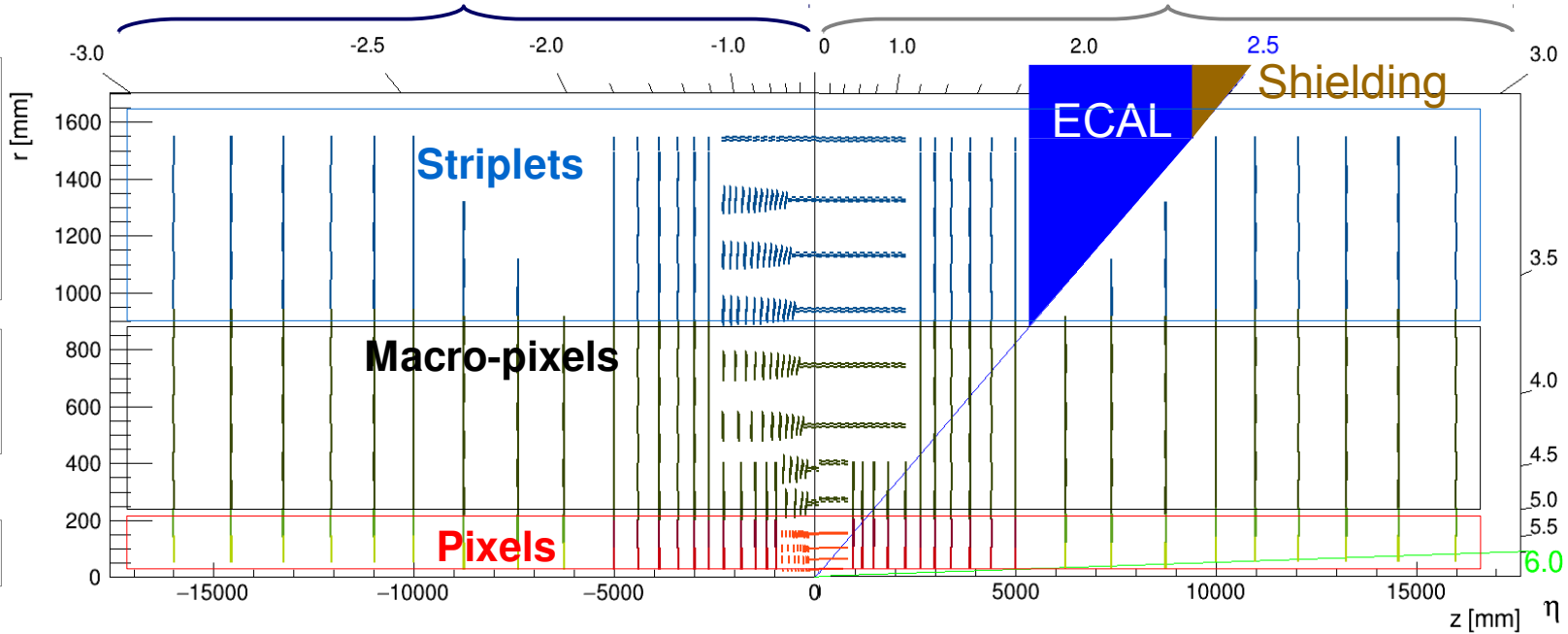


Ref. Tracker Layout: Tilted v4.01 vs. Flat v3.03

Surface: ~ 430 (391) m^2
#Channels: **489.4M**
9964.4M
5460.9M

(Macro)-pixel $R \nearrow 0.9$ m
due to occupancy

4 (seed) BRL layers

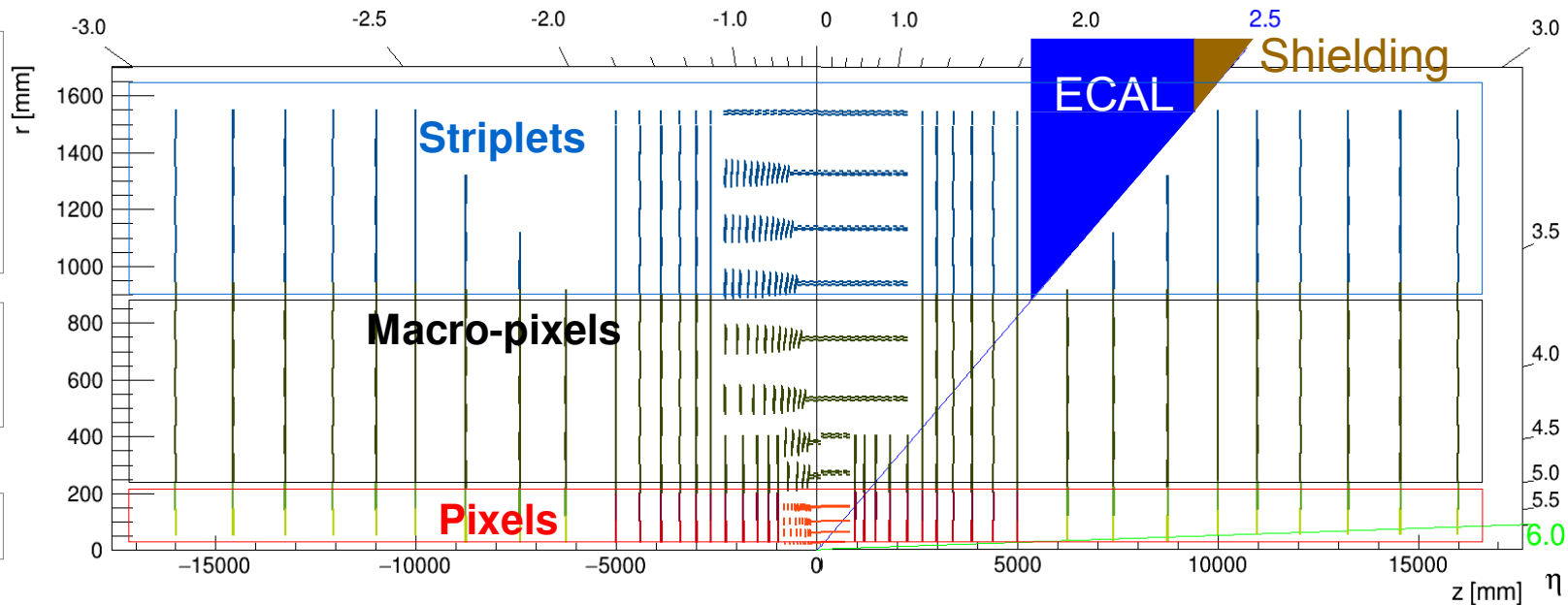


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(Macro)-pixel R ↗ 0.9 m
 due to occupancy

4 (seed) BRL layers



Granularity of flat design:

Pixels : 25x50um² (1-4th BRL layers, EC R1),
 100/3x100um² (R2),
 100/3x400um² (R3,R4)

Macro-pixels: 100/3x400um²

Strips : 100/3umx50mm (BRL),
 100/3umx10mm (EC)

→ Assumed binary R/O → res. ~ pitch/√12

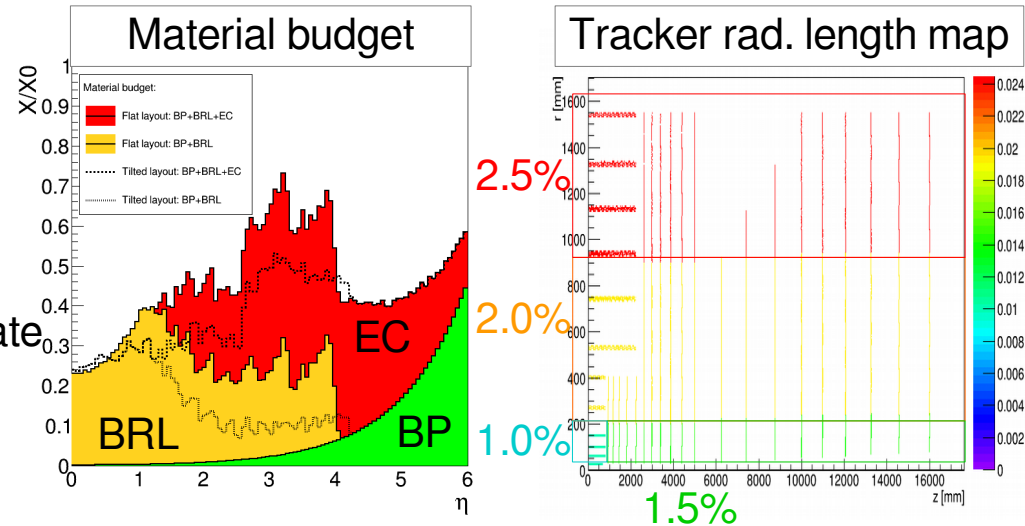
Huge increase in #pixel channels wrt LHC exp.
 due to:

- requirements on tracking up to $\eta=6$
- resilience to **high rad. levels** generated by FCC-hh

For details see <http://fcc-tklayout.web.cern.ch>

Material Budget & Tracking Resolution

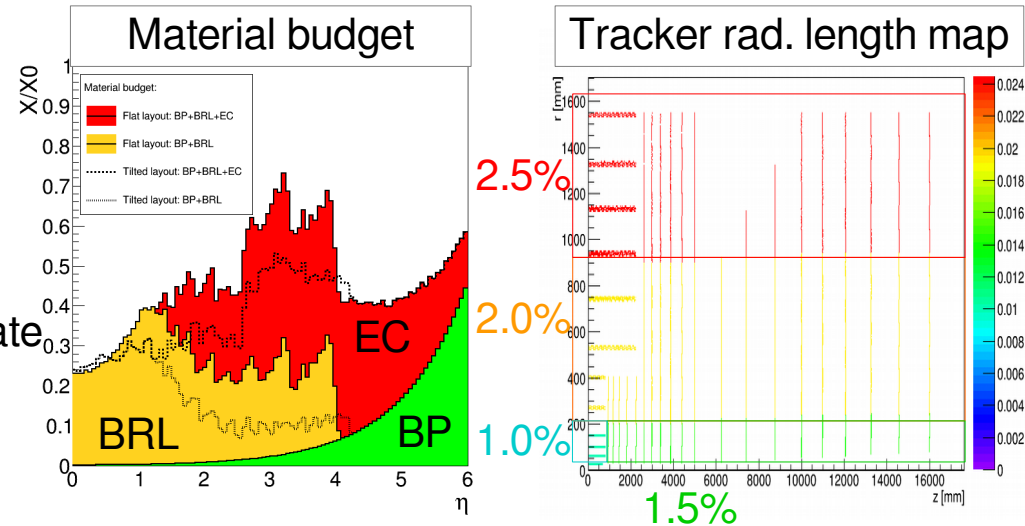
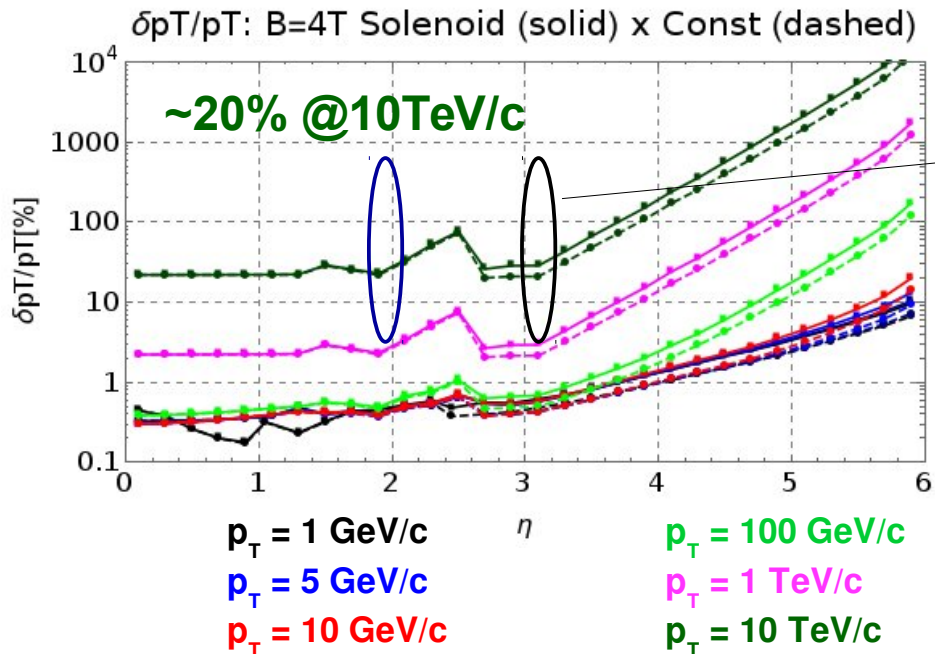
- A simplified model for MB assumed:
 - $x/x_0 \sim 1-2.5\%$ per layer (services accumul. effect)
(20% Si, 42% C, 2% Cu, 6% Al, 30% Plastic)
- **technology input needed** for more real. estimate



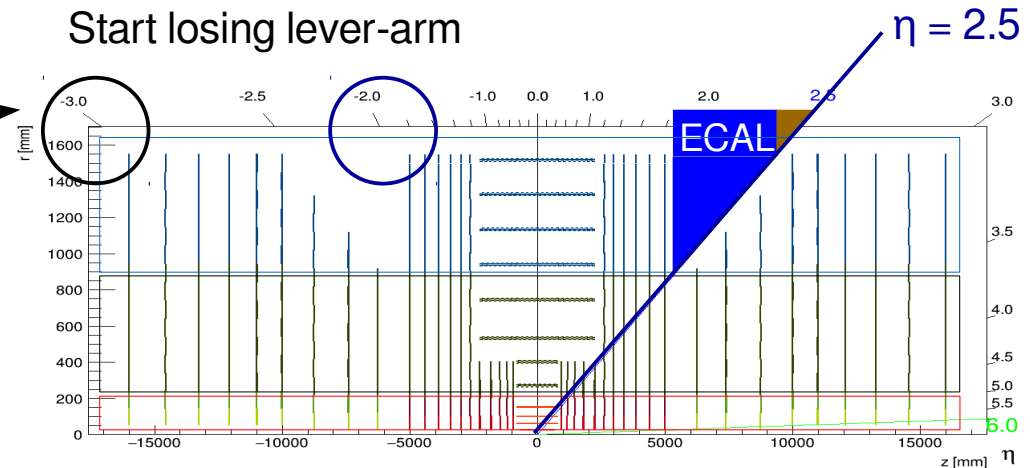
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- **Tracking resolution:**



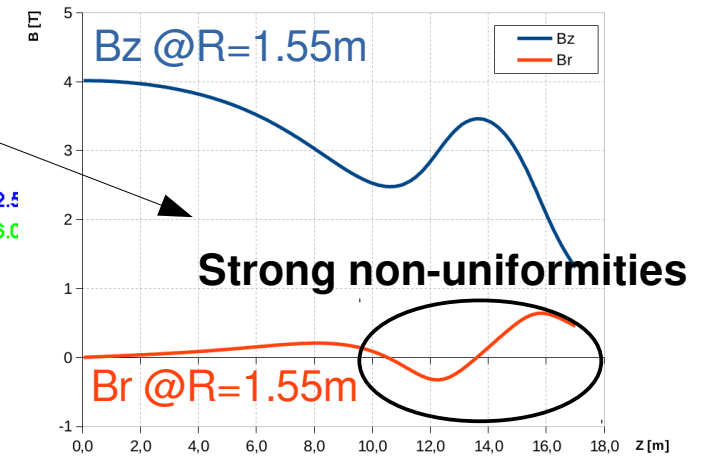
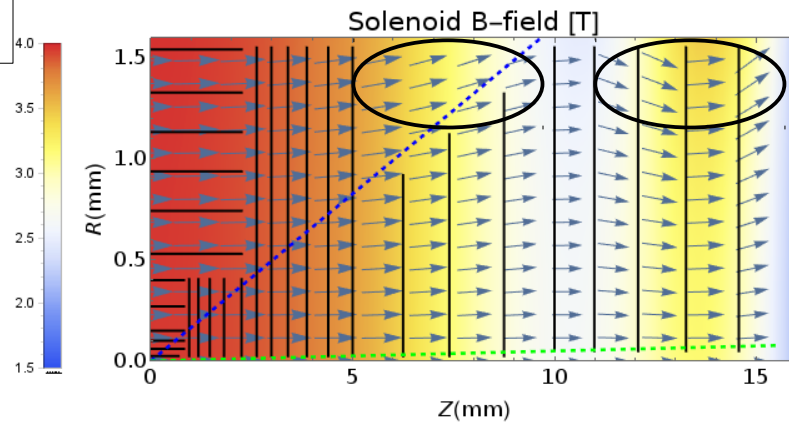
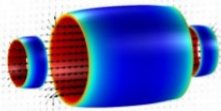
Start losing lever-arm



Solenoid Scenario & dp_T/p_T Resolution

- Full solenoid B field map \rightarrow effect on dp_T/p_T ?

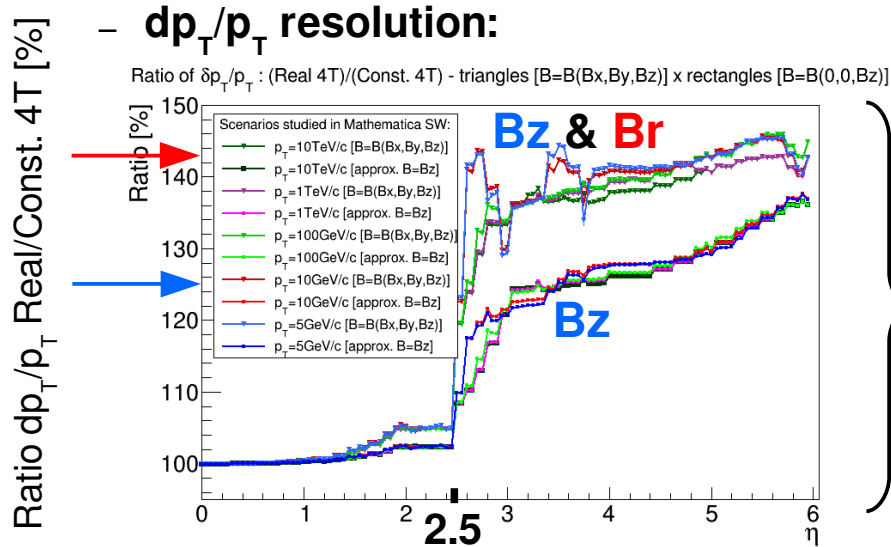
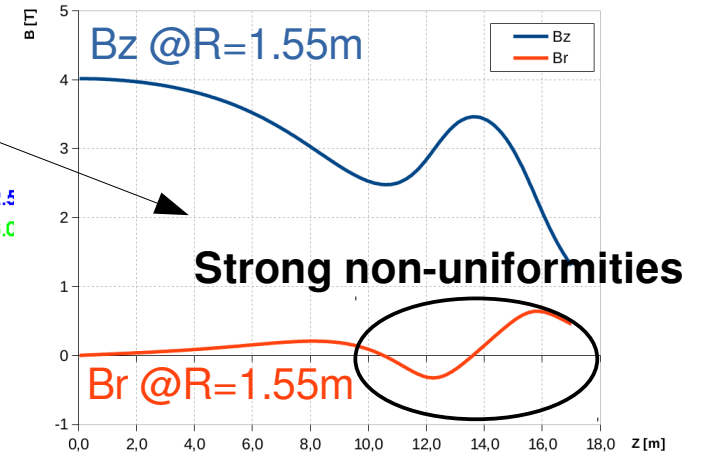
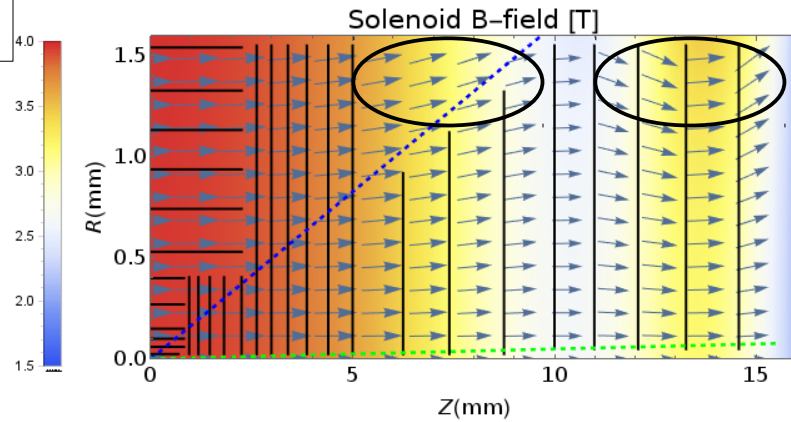
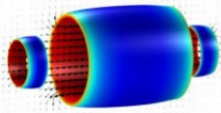
Courtesy of E. Bielert



Solenoid Scenario & dp_T/p_T Resolution

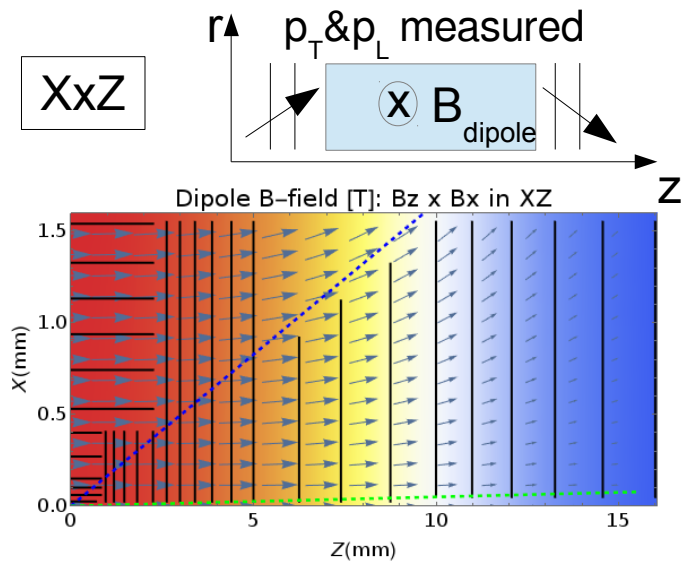
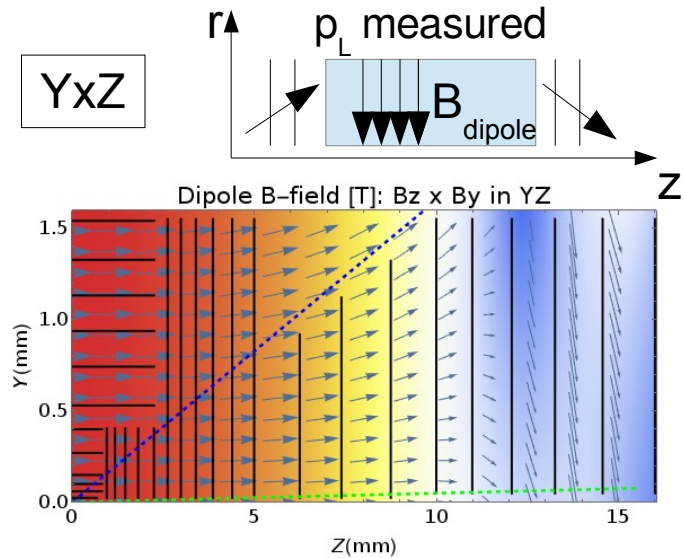
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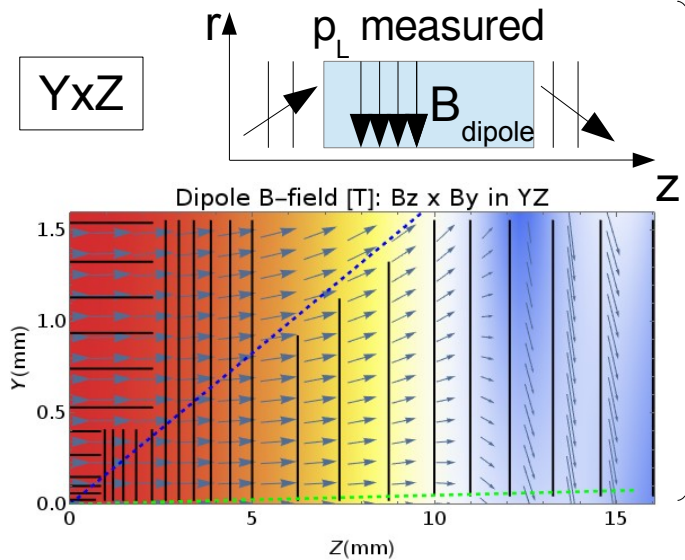


Total deterioration in $\delta p_T/p_T$ due to non-uniformity of solenoid B field $\sim 35\text{-}45\%$ @ $\eta=2.5$ or higher

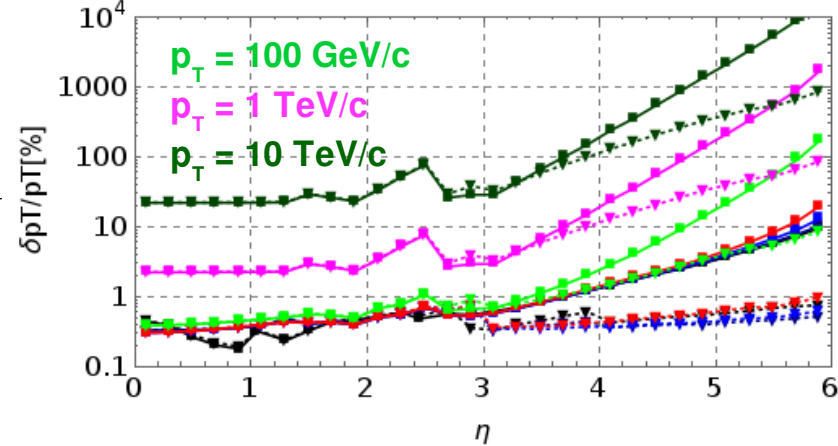
Dipole Alternative & dp_T/p_T Resolution



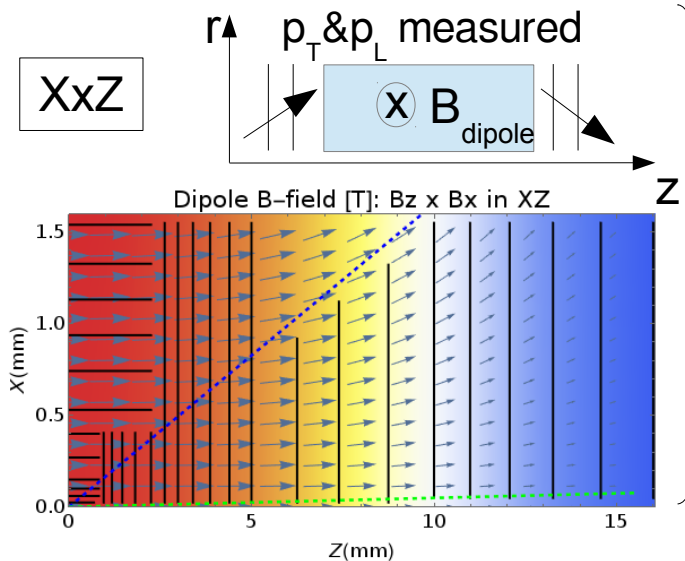
Dipole Alternative & $\delta p_T/p_T$ Resolution



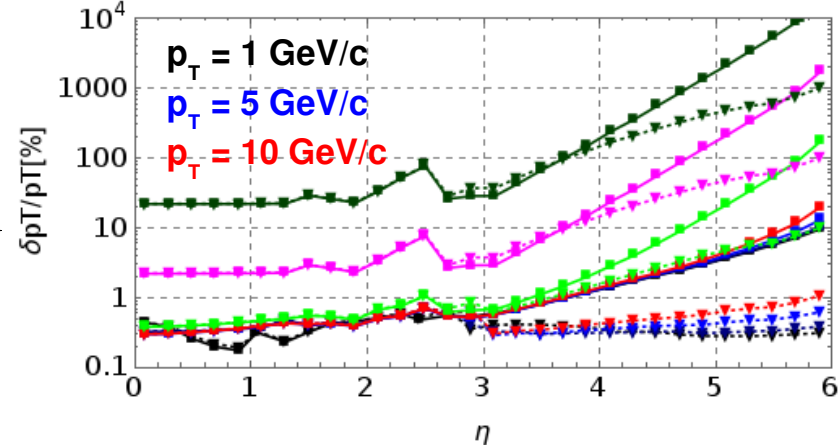
$\delta p_T/p_T$: FWD solenoid (solid) x dipole (dotted) \rightarrow Y-axis



$\delta p_T/p_T$ affected only by granularity in R- Φ



$\delta p_T/p_T$: FWD solenoid (solid) x dipole (dotted) \rightarrow X-axis



$\delta p_T/p_T$ affected by both granularity in R&R- Φ , must be comparable!

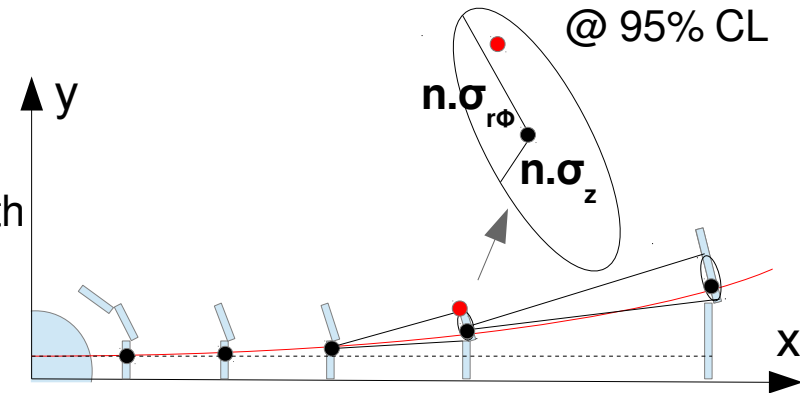
\rightarrow Dipole: $\delta p_T/p_T$ improves by: **x2.5, x5.0, x13.0** @ $\eta=4.0, 5.0, 6.0$

Pattern Recognition (PR) Capabilities

- PR limit given by Multiple Scattering (MS) (low p_T tracks affected most) → use **track propagator** & analyze **layout “weak” spots**:

- assume **perfect seeding** (nontrivial)
- propagate $\sigma_{r\phi}$, σ_z to i^{th} layer (in → out)
- calculate probability that a **signal hit** is not mismatched with a **bkg hit** anywhere on the track @95% CL **in PU=1000**

$$\epsilon \sim \prod_{i=4}^N (1 - p_{\text{bkg}95\%}^i)$$

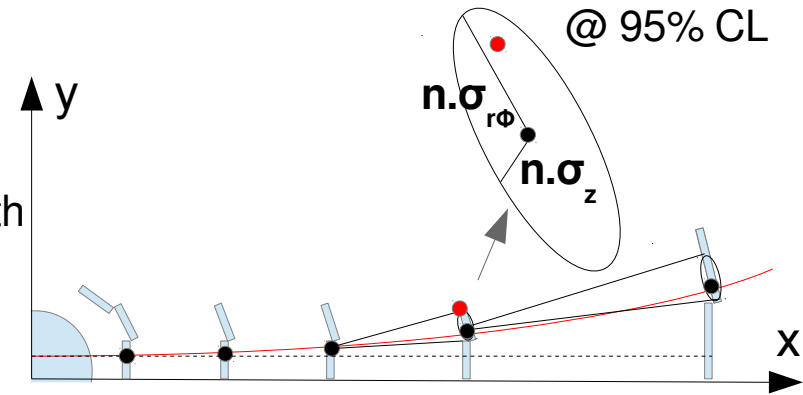


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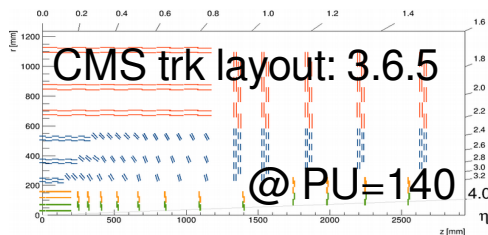
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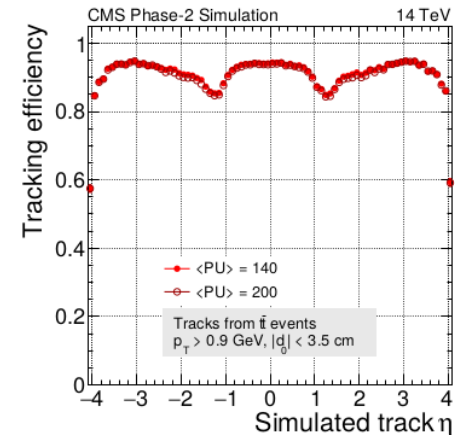
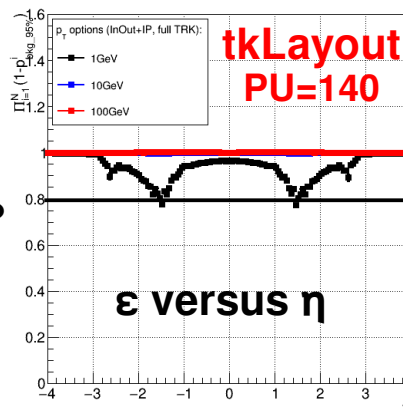
$$\epsilon \sim \prod_{i=4}^N (1 - p_{\text{bkg}}^i_{95\%})$$



- How to interpret & “calibrate” a limit value on $\epsilon \sim$ **efficiency**?



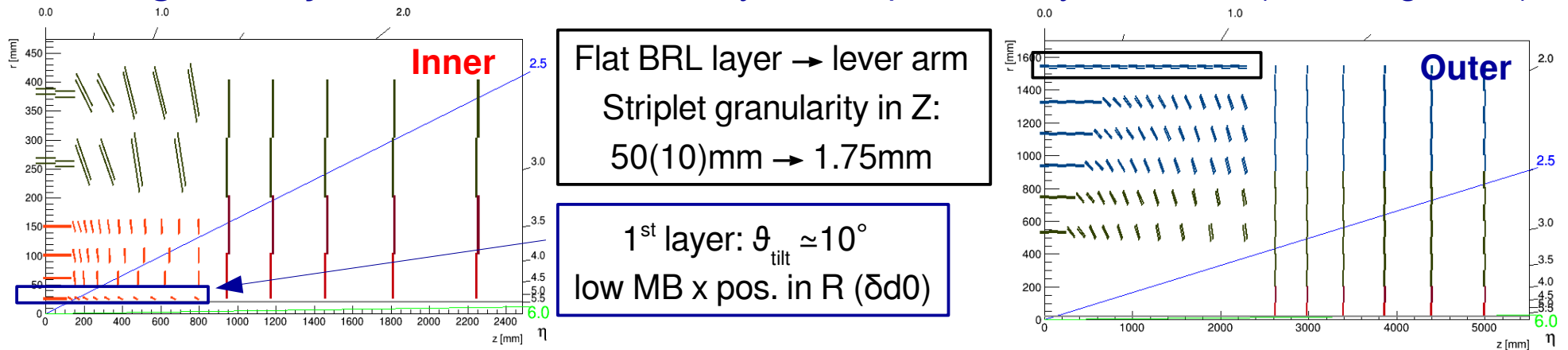
$\epsilon \sim 80\%$



The Ph.2 Upgrade of the CMS Tracker
<http://cds.cern.ch/record/2272264>

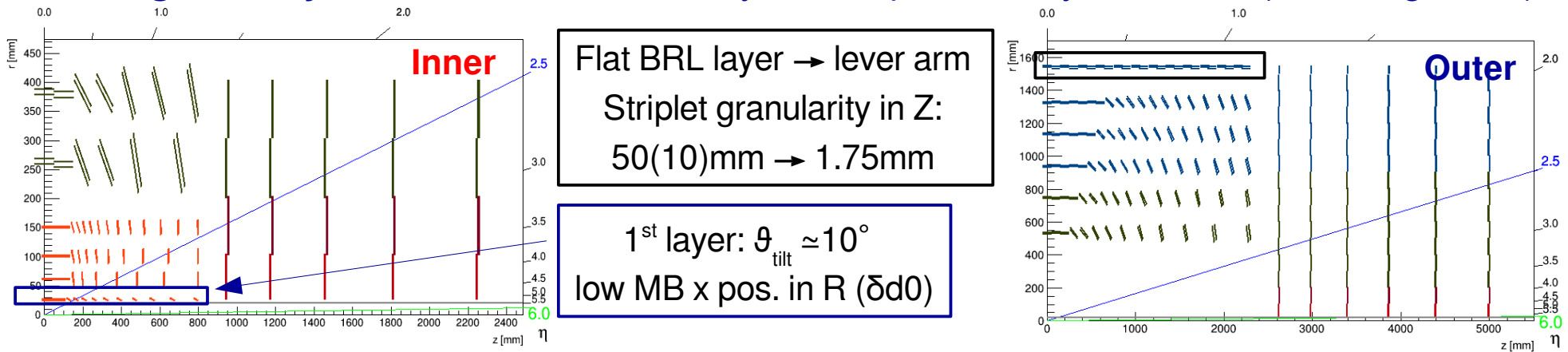
Tilted Layout 4.01 & PR Performance

- **Tilted geometry** minimizes MS → final layout as optimized by PR & δz_0 (vertexing in PU):



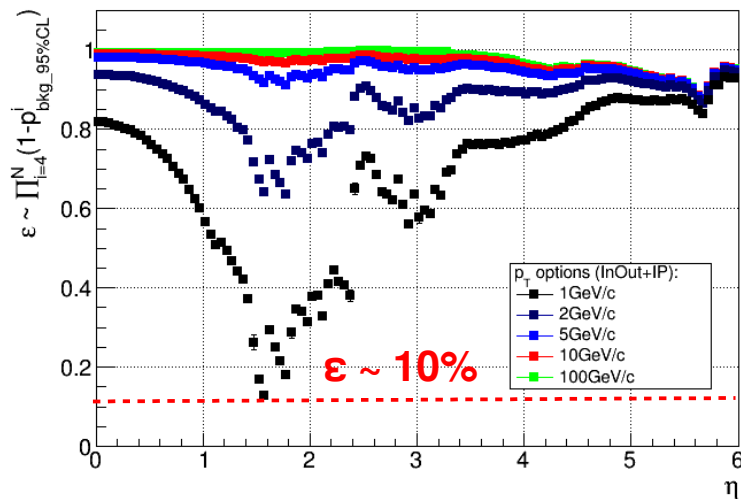
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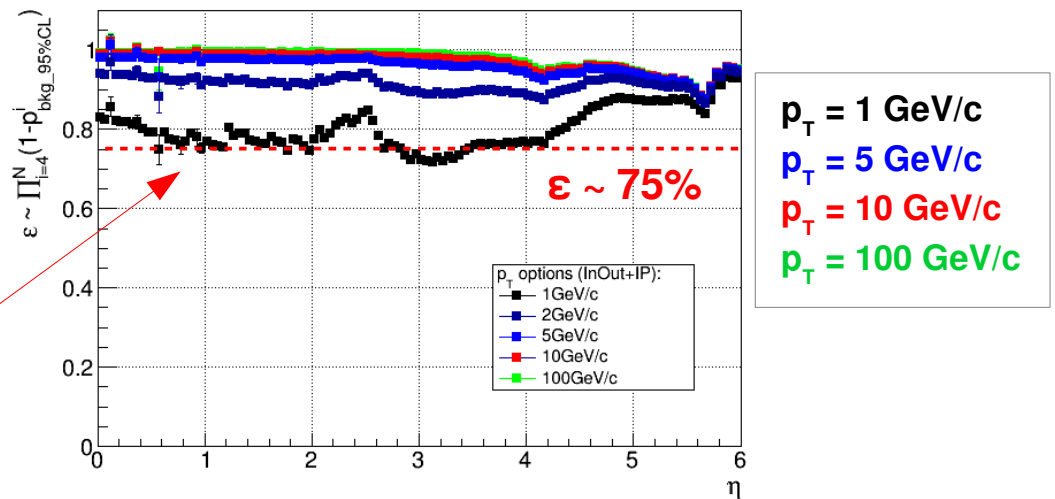
PR for flat layout v3.03:

In-Out PR: Accumulated probability of no backg. contamination across N layers @ 95%CL



PR for tilted layout v4.01:

In-Out PR: Accumulated probability of no backg. contamination across N layers @ 95%CL

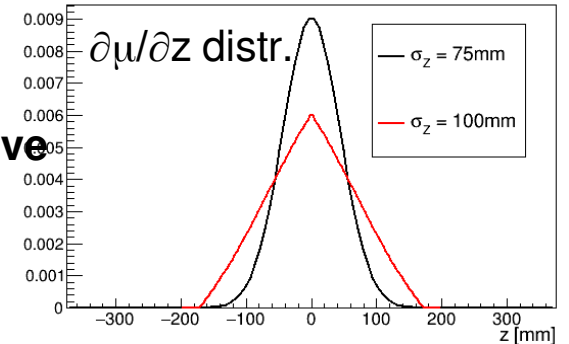


Vertexing @ PU=1000 & Timing Information

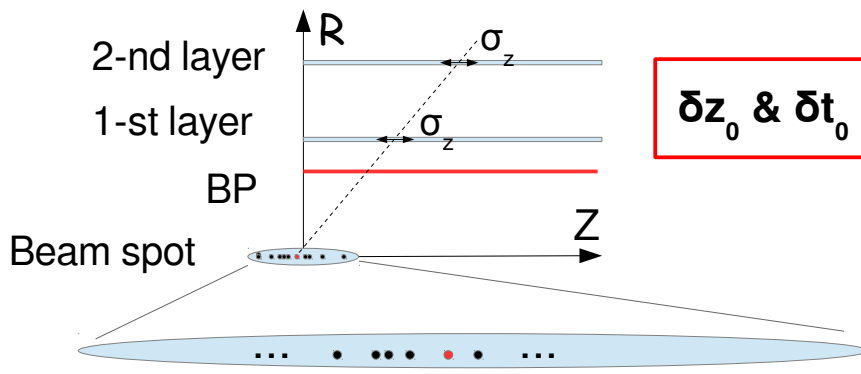
- Primary vertexing in huge pile-up (PU)~1000:

→ Study how many PU vertices are effectively contained within 95% CL interval of the primary track wrt primary vertex (LV) → **estimate effective PU** (LV assumed to be “precisely” found from e.g. high p_T tracks)

Line PU distr.: gaussian versus rectangular shaped bunches



Piwinsky angle $\Phi \sim 0.67$
Time Piw. angle $\Psi \sim 0.40$



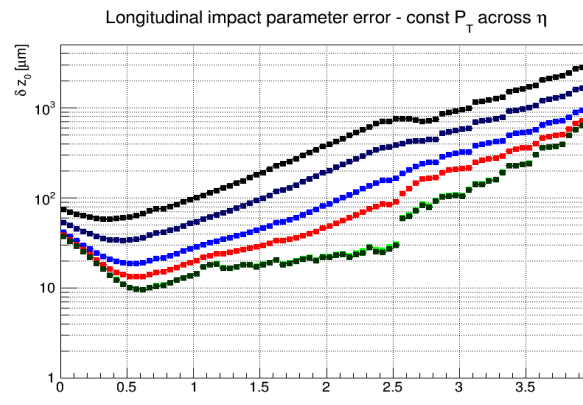
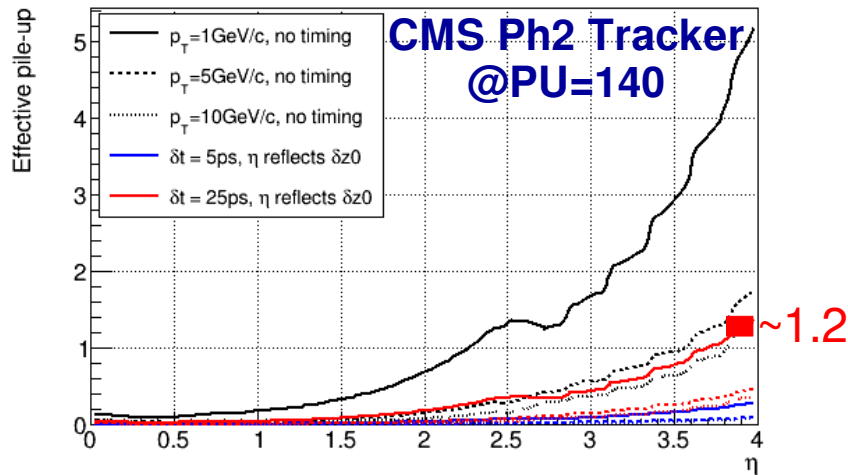
δz_0 & δt_0 interplay crucial!

$\sigma_z^{\text{lum.region}} \sim 44\text{mm}$ & $\sigma_t^{\text{lum.region}} \sim 165\text{ps}$

Effective Pile-up Rate & Timing Information

→ Compare **FCC-hh** to **HL-LHC** conditions (**PU~140**), applied to e.g. CMS Ph2 upgrade layout

Effective pile-up confusing prim. vertexing @95% CL: $\sigma_z^{\text{Gauss}}=75\text{mm}$, $\langle\mu_{\text{tot}}\rangle=140$

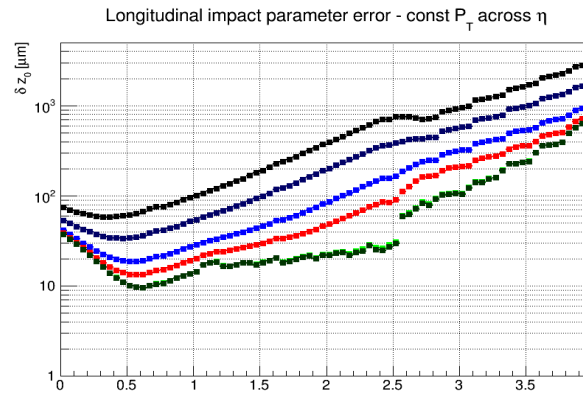
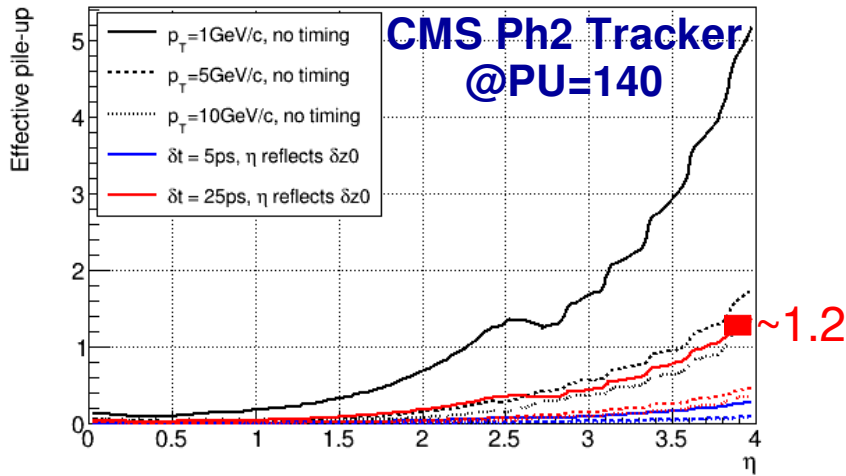


Decrease in δz_0 needs to be “compensated” by extra timing info (in FWD)

Effective Pile-up Rate & Timing Information

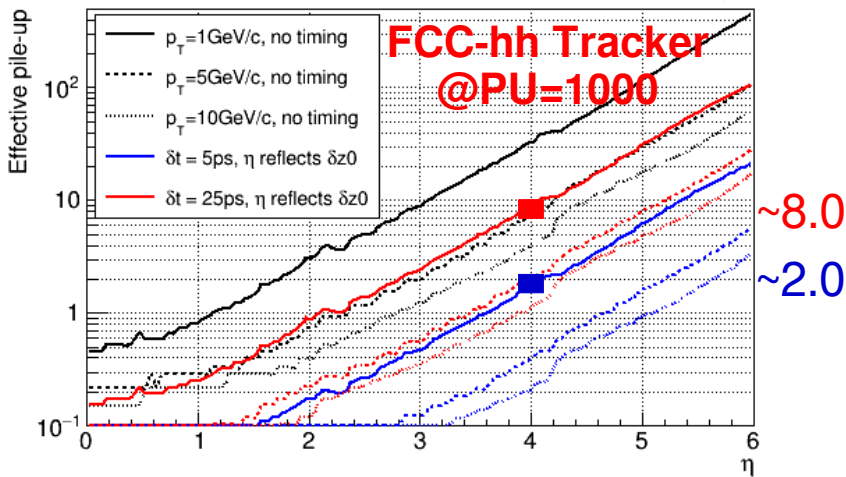
→ Compare **FCC-hh** to **HL-LHC** conditions (**PU~140**), applied to e.g. CMS Ph2 upgrade layout

Effective pile-up confusing prim. vertexing @95% CL: $\sigma_z^{\text{Gauss}}=75\text{mm}$, $\langle\mu_{\text{tot}}\rangle=140$



Decrease in δz_0 needs to be “compensated” by extra timing info (in FWD)

Effective pile-up confusing prim. vertexing @95% CL: $\sigma_z^{\text{Gauss}}=75\text{mm}$, $\langle\mu_{\text{tot}}\rangle=1000$



FCC-hh: 2D vertexing (time & z) essential, namely in the FWD region! But..., may not be sufficient to mitigate the PU effect for tracks @ $\eta > 4.0$

Summary & Challenges

- **The key tracker/vertex detector parameters understood:**

- Layout with extended coverage up-to $\eta=6$ designed: $\sim 430\text{m}^2$ (391m^2 in tilted layout) of Si

- Granularity in $R-\Phi$ mostly driven by dp_T/p_T @ $p_T=10\text{TeV}/c$ → **achieved $dp_T/p_T \sim 20\%$**

- Effect of dipole on dp_T/p_T in the FWD region assessed → **x13** improvement @ $\eta=6.0$ vs. solenoid

- Granularity in Z driven by prim. vertexing & pattern recognition @ **PU=1000**:

- To minimize the effect of MS (mat. budget), **tracker design in tilted layout suggested**

- To mitigate the pile-up effect, **tracking with precise timing information required ($\delta t \sim 5-10\text{ps}$ per track) → the limiting factor for low p_T tracks remains still the beam-pipe material**

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- **The key technology challenges:**

- Huge data rates: 766 TB/s (untrig. @40MHz) & extreme data flows (densities) at low radii $\gtrsim 1\text{Gb/s/cm}^2$ @ **1MHz** implicate need for **new read-out technologies** & dedicated trigger design!
- Fluences $\sim 6 \times 10^{17} n_{eq}/\text{cm}^2$ @ innermost tracker radii represent **a new challenge for the R&D**
- Tracker technology providing **simultaneously position & timing information along the track** would open a new & powerful direction in the future track/vertex reconstruction

Back-up Slides

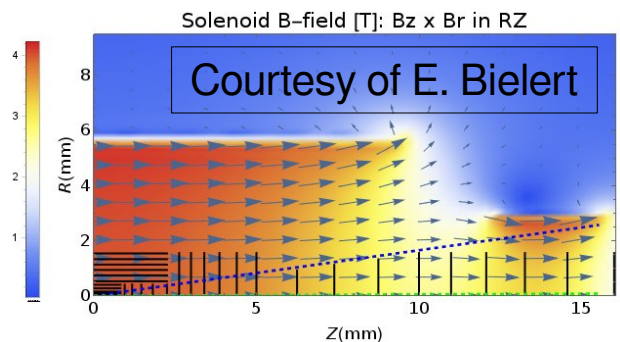
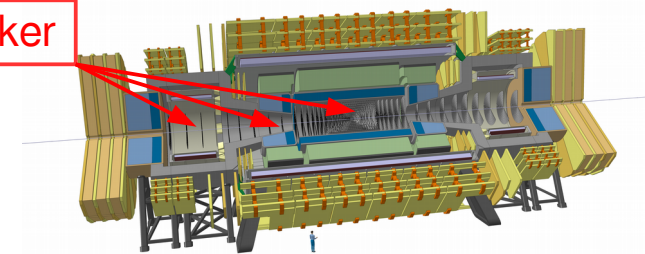
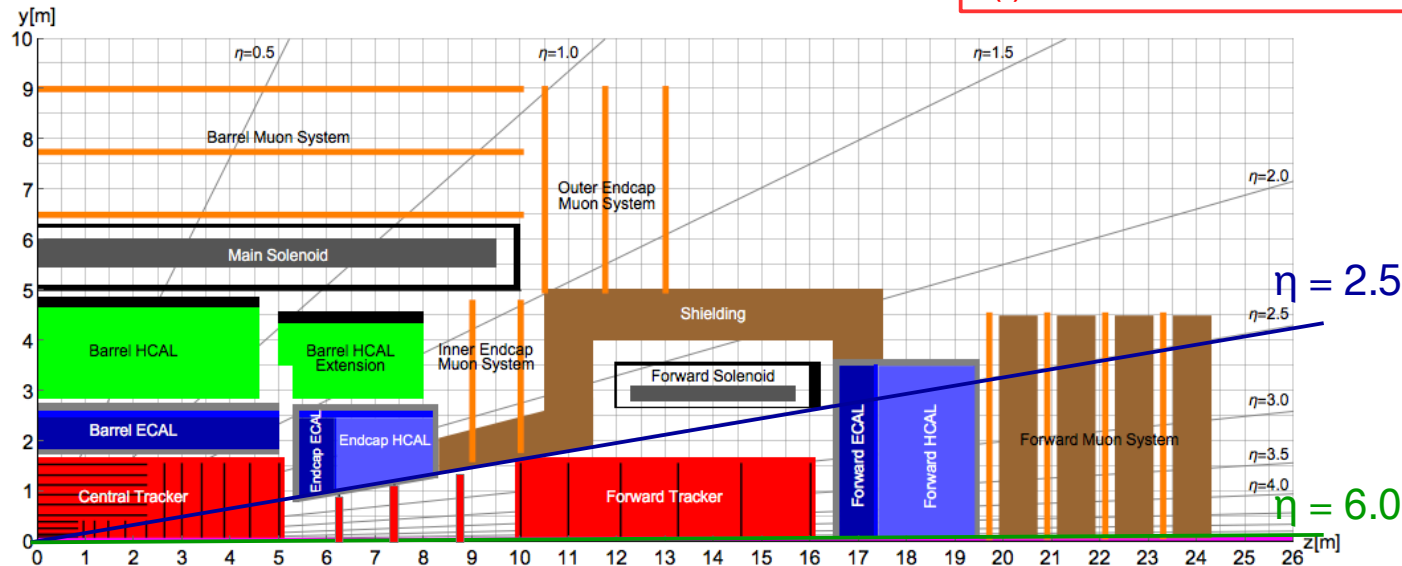
Back-up Slides:

Reference Design & Tracker Requirements

Reference Design & Tracker Requirements

- **FCC opens us a new kinematic & dynamical regime + physics @100TeV highly boosted → challenging requirements on tracker/vertex detector design:**
 - **Extended tracking up-to $|\eta| \sim 4$** (c.f. $|\eta| \sim 2.5$ for LHC exp.) + efficient **VBF jet meas. up-to $|\eta| \sim 6$**
 - **High p_T res. $\sim 10\text{-}20\%$ @ 10TeV** (cf. LHC: 10% @1TeV) & still **keep sensitivity to low p_T tracks**
 - **Provide efficient b,c, τ -tagging despite huge PU & high energies**
 - **High tracker granularity essential** to resolve jet-substructure (collimated objects), reject bkg,...

(i) Fwd + Central Tracker



Tracker Granularity: Tilted vs. Flat Layout

Pixels (inner)	Macro-pixels (middle)	Triplets/Macro-pixels (outer)
$25 \times 50 \mu\text{m}^2$ (1–4th BRL, 1st EC ring)	$33.3 \times 400 \mu\text{m}^2$	$33.3 \mu\text{m} \times 50 \text{mm}$ (BRL)
$33.3 \times 100 \mu\text{m}^2$ (2nd EC ring)		$33.3 \mu\text{m} \times 10 \text{mm}$ (EC)
$33.3 \times 400 \mu\text{m}^2$ (3–4th EC ring)		

Table 1: Flat layout: The summary of assumed in-detector resolutions for different categories of sensors.

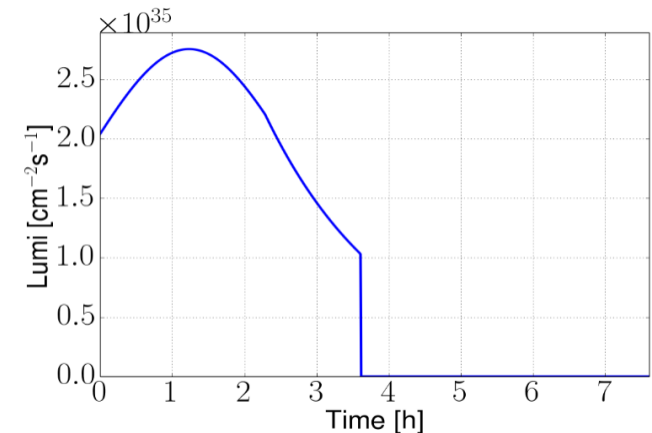
Pixels (inner)	Macro-pixels (middle)	Triplets/Macro-pixels (outer)
$25 \times 50 \mu\text{m}^2$ (1–4th BRL, 1st EC ring)	$33.3 \times 400 \mu\text{m}^2$	$33.3 \mu\text{m} \times 1.75 \text{mm}$ (BRL & EC)
$33.3 \times 100 \mu\text{m}^2$ (2nd EC ring)		$33.3 \mu\text{m} \times 50 \text{mm}$ (12th BRL layer)
$33.3 \times 400 \mu\text{m}^2$ (3–4th EC ring)		

Table 2: Tilted layout: The summary of assumed in-detector resolutions for different categories of sensors.

Pile-up Numbers: Estimation for FCC-hh

- How to estimate pile-up limits for FCC-hh?

→ numbers extrapolated (plot from D.Schulte's talk at [FCC Week](#))



$$\langle \mu \rangle = \frac{\sigma_{inel} \cdot L}{n_B \cdot f_r}$$

- $\sigma_{inel} \sim 108\text{mb}$ @ 100TeV FCC-hh
- **Tunnel length** = 97.500 km
- n_B (HL-LHC) = 2748
(Bunches fill-up factor $f_{up} = 2748/3554 \sim 77.3\%$)
→ n_B (FCC-hh) = **10050** (using f_{up} factor)
- $f_r = 3.075\text{kHz}$ (revolution frequency assuming FCC tunnel)
- **Ultimate Luminosity** $\sim 30 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- **Levelled luminosity (assuming loss in int. L $\sim 20\%$)** = $15 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$

- **Luminosity variations** between bunches $\pm 8\%$ (see e.g. [ATL-PHYS-PUB-2013-014](#))
- **Pile-up: μ is Poisson distributed** → quantify **limits** by 95% confidence interval ($\sigma \sim 1.96\sqrt{N}$)

→ **FCC-hh Ultimate: $\langle \mu \rangle = [(1048 \pm 84) \pm 66]$ → Max O(1200), Avg \sim O(1000)**

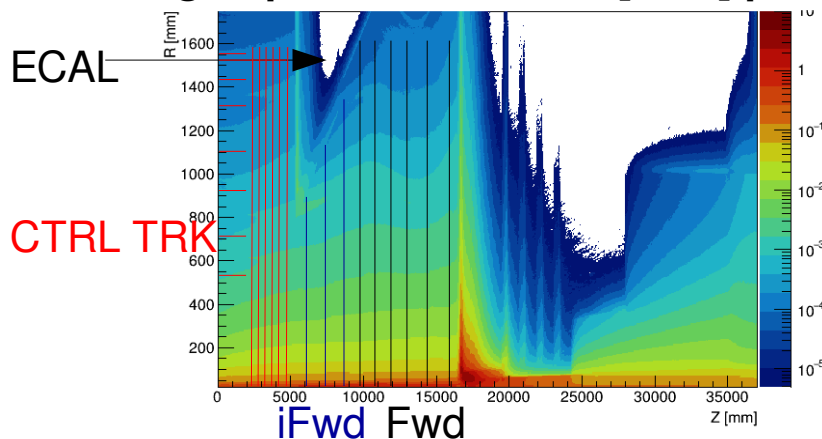
→ **FCC-hh Levelled: $\langle \mu \rangle = [(524 \pm 42) \pm 47]$ → Max O(600)**

Back-up Slides: Hit Occupancy & Expected Data Rates

Occupancy & Expected Data Rates @ PU=1000

- Tracker granularity in a view of hit occupancy ($\sim <1\%$) \rightarrow data rates @ **1000 PU**?
 - \rightarrow Use Fluka simulated charged particles fluence per pp collision [cm^{-2}] scaled by 1000 PUs
 - \rightarrow Calculate occupancy & hit rates for 2 scenarios:
 - Non-triggered data @ $f = 40\text{MHz}$
 - Triggered data @ $f \sim 1\text{MHz}$ (given \sim by hardware limits, e.g. FPGA)
 - \rightarrow Assume sparsified data read-out scheme:
 - address each channel: **nBits** = $\log_2(\text{nRows}) + \log_2(\text{nColumns})$
 - add data block for cluster-width: assuming avg cluster-size $\sim 3 \rightarrow$ **2bits**
 - add data block for pulse-height: **0bits** (binary read-out)

Charged particles fluence [cm^{-2}] per 1 pp collision



Inner Flat: Occupancy & Expected Data Rates

Layer no :	1	2	3	4	5	6	Total [TB/s]
Radius [mm] :	25.0	60.0	100.0	150.0	270.0	400.0	
Module max occupancy (max[sen1,sen2])[%] :	0.45	0.11	0.05	0.02	0.08	0.04	
#Hit-channels per module per BX :	2694	741	333	166	314	150	
Module avg occupancy (max[sen1,sen2])[%] :	0.38	0.09	0.04	0.02	0.08	0.04	
Module bandwidth/(addr+clsWidth=2b[b] :	22	22	22	22	21	21	
Mod. bandwidth(#chnls*(addr+clsWidth)[kb] :	57.88	15.93	7.16	3.57	6.44	3.08	
Mod. bandwidth (matrix*1b/channel) [kb] :	685.00	820.00	820.00	820.00	384.00	384.00	
Data rate per layer - 40MHz,spars [Tb/s] :	603.7	379.9	277.3	202.2	138.7	97.5	212.4
Data rate per layer - 1MHz,spars [Tb/s] :	15.1	9.5	6.9	5.1	3.5	2.4	5.3
Data rate per ladder - 40MHz,spars [Gb/s] :	44159.7	24313.2	10920.7	5449.3	4177.1	1996.5	
Data rate per ladder - 1Mhz,spars [Gb/s] :	1104.0	607.8	273.0	136.2	104.4	49.9	
Data rate per module - 40MHz,spars [Gb/s] :	2207.99	607.83	273.02	136.23	245.71	117.44	
Data rate per module - 1Mhz,spars [Gb/s] :	55.20	15.20	6.83	3.41	6.14	2.94	
Data rate per cm ² - 40MHz,spars [Gb/s/cm ²]:	251.82	57.91	26.01	12.98	4.69	2.24	
Data rate per cm ² - 1Mhz,spars [Gb/s/cm ²]:	6.30	1.45	0.65	0.32	0.12	0.06	

→ Hit occupancy [%] (~ <1%)

→ Layer data rate (40MHz)
→ Layer data rate (1MHz, trigger)

→ Data rate per cm² (40MHz)
→ Data rate per cm² (1MHz, trigger)

Ring no :	1	2	3	4	Total [TB/s]
Average radius [mm] :	64.8	153.0	251.1	353.3	
Module max occupancy (max[sen1,sen2])[%]:	0.46	0.13	0.18	0.08	
Data rate per ringLayer-40MHz,spars [Tb/s]:	194.2	148.2	105.1	74.3	65.2
Data rate per ringLayer- 1MHz,spars [Tb/s]:	4.9	3.7	2.6	1.9	1.6
Data rate per cm ² - 40MHz,spars [Gb/s/cm ²]	64.44	15.67	6.62	3.42	
Data rate per cm ² - 1Mhz,spars [Gb/s/cm ²]:	1.61	0.39	0.17	0.09	

Challenge: 6.3 Gb/s/cm²

Challenge: 1.6 Gb/s/cm²

**Extreme data flows >>10Gb/s/module
(even triggered @ 1MHz)**

Outer & Fwd Flat: Occupancy & Data Rates

→ Expected huge tracker data rates: 766 TB/s (untriggered), 19 TB/s (triggered @ 1MHz)

Layer no :	Outer:	1	2	3	4	5	6	Total [TB/s]										
Radius [mm] :		530.0	742.4	937.2	1132.0	1326.7	1539.5											
Module max occupancy (max[sen1,sen2])[%] :		0.02	0.01	0.75	0.43	0.27	0.21											
Data rate per layer - 40MHz,spars [Tb/s] :		226.0	134.5	63.6	43.9	31.7	28.1	66.0										
Data rate per layer - 1MHz,spars [Tb/s] :		5.6	3.4	1.6	1.1	0.8	0.7	1.6										
Data rate per cm ² - 40MHz,spars [Gb/s/cm ²]:		1.38	0.61	0.23	0.13	0.08	0.06											
Data rate per cm ² - 1Mhz,spars [Gb/s/cm ²]:		0.03	0.02	0.01	0.00	0.00	0.00											
Ring no :		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Total [TB/s]
Average radius [mm] :		64.6	151.5	251.0	352.0	451.6	553.6	651.1	753.6	850.8	953.5	1049.7	1152.6	1247.6	1350.8	1444.7	1522.8	
Module max occupancy (max[sen1,sen2])[%]:		0.58	0.15	0.21	0.10	0.06	0.04	0.02	0.02	0.01	0.23	0.20	0.13	0.12	0.08	0.08	0.05	
Data rate per ringLayer-40MHz,spars [Tb/s]:		263.8	213.3	153.4	109.8	93.2	63.1	63.8	49.9	42.5	28.5	21.9	19.2	15.7	13.8	11.4	4.6	146.0
Data rate per ringLayer- 1MHz,spars [Tb/s]:		6.6	5.3	3.8	2.7	2.3	1.6	1.6	1.2	1.1	0.7	0.5	0.5	0.4	0.3	0.3	0.1	3.6
Data rate per cm ² - 40Mhz,spars [Gb/s/cm ²]:		71.30	18.72	7.98	4.18	2.65	1.54	1.18	0.78	0.62	0.36	0.26	0.21	0.15	0.13	0.10	0.08	
Data rate per cm ² - 1Mhz,spars [Gb/s/cm ²]:		1.78	0.47	0.20	0.10	0.07	0.04	0.03	0.02	0.02	0.01	0.01	0.01	0.00	0.00	0.00	0.00	
Ring no :	iFWD:	1	2	3	4	5	6	7	8	9	10	11	12	13	Total [TB/s]			
Average radius [mm] :		72.8	167.5	266.5	366.3	464.9	564.8	664.6	766.8	866.7	969.0	1068.4	1170.9	1269.8				
Module max occupancy (max[sen1,sen2])[%]:		0.99	0.13	0.20	0.11	0.07	0.04	0.03	0.02	0.02	0.48	0.24	0.12	0.07				
Data rate per ringLayer-40MHz,spars [Tb/s]:		165.8	114.5	81.6	64.9	50.6	39.3	42.3	30.0	43.3	16.8	7.8	2.8	1.9	82.7			
Data rate per ringLayer- 1MHz,spars [Tb/s]:		4.1	2.9	2.0	1.6	1.3	1.0	1.1	0.8	1.1	0.4	0.2	0.1	0.0	2.1			
Data rate per cm ² - 40Mhz,spars [Gb/s/cm ²]:		65.73	18.17	8.18	4.75	2.92	1.87	1.44	0.94	1.18	0.64	0.27	0.18	0.11				
Data rate per cm ² - 1Mhz,spars [Gb/s/cm ²]:		1.64	0.45	0.20	0.12	0.07	0.05	0.04	0.02	0.03	0.02	0.01	0.00	0.00				
Ring no :	FWD:	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Total [TB/s]	
Average radius [mm] :		97.1	190.1	288.9	388.3	487.1	588.6	689.4	791.4	891.9	994.1	1094.4	1196.6	1296.6	1398.8	1498.5		
Module max occupancy (max[sen1,sen2])[%]:		0.28	0.11	0.20	0.12	0.08	0.05	0.04	0.03	0.02	0.46	0.34	0.25	0.16	0.11	0.09		
Data rate per ringLayer-40MHz,spars [Tb/s]:		318.3	244.3	180.2	149.6	121.5	116.4	101.0	77.1	76.7	54.9	35.5	25.6	19.5	15.2	11.0	193.4	
Data rate per ringLayer- 1MHz,spars [Tb/s]:		8.0	6.1	4.5	3.7	3.0	2.9	2.5	1.9	1.9	1.4	0.9	0.6	0.5	0.4	0.3	4.8	
Data rate per cm ² - 40Mhz,spars [Gb/s/cm ²]:		48.67	17.20	8.37	5.17	3.35	2.37	1.71	1.21	1.04	0.66	0.40	0.26	0.19	0.13	0.09		
Data rate per cm ² - 1Mhz,spars [Gb/s/cm ²]:		1.22	0.43	0.21	0.13	0.08	0.06	0.04	0.03	0.03	0.02	0.01	0.01	0.00	0.00	0.00		

Back-up Slides:

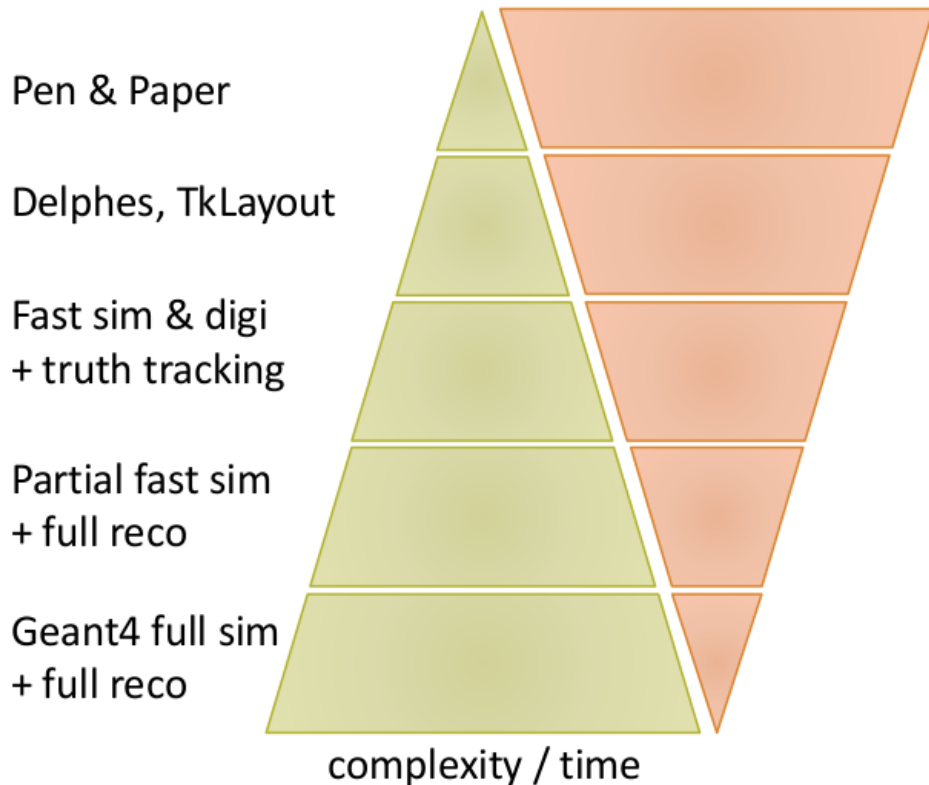
SW Tools & Mathematical Approach to Track Resolution

Mathematical Techniques & SW Tools

- **Extremely important to choose the right tools given the tight schedule for CDR...**

Picture by A.Salzburger

detector layouts



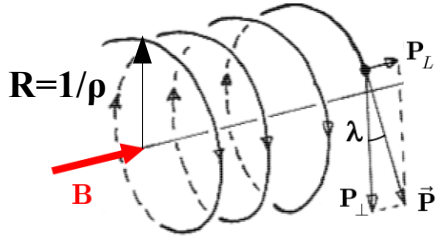
The tracker layout mainly optimized by applying:

- Approx. analytical approach: **tkLayout** (CMS)
- Numerical approach: **Mathematica**
- + using B field maps & Fluka simulated fluence map

Mathematical Approach: Analytical & Numerical

- Estimate 5x5 cov. matrix of track parameters (global χ^2 with MS)

$$\rho, \phi_0, d_0, \cotg(\vartheta), z_0$$



$$\text{cov}(\vartheta_i, \vartheta_j) = (A^T V^{-1} A)^{-1}, A_{ij} = \left. \frac{\partial y_i(\vartheta_j)}{\partial \vartheta_j} \right|_{\vartheta=\hat{\vartheta}}$$

$$V = V_{\text{det}} + V_{\text{MS}}$$

Tracker precision & material

- "Parabolic" approximation (tkLayout SW) vs. full numerical approach (Mathematica):

Approx. analytical approach to $\frac{d^2 \vec{x}(s)}{ds^2} = \frac{0.3}{p} \frac{d\vec{x}(s)}{ds} \times \vec{B}(\vec{x}(s)) \rightarrow$ assume const. B field & separate r- Φ & s-z:

- r- $\Phi \rightarrow$ circle in polar coordinates:

$$0 = \frac{\rho}{2} r_i^2 - \sin(\varphi_i - \varphi_0) (1 + d_0 \rho) r_i + d_0 (1 + d_0 \frac{\rho}{2})$$

$$d_0 \rho \ll 1$$

- s-z: \rightarrow approx. path length $s \sim r$

$$z_i = z_0 + s_i \sin \lambda$$

cyl. symmetry $\rightarrow \phi_0 \equiv 0$

- Note:

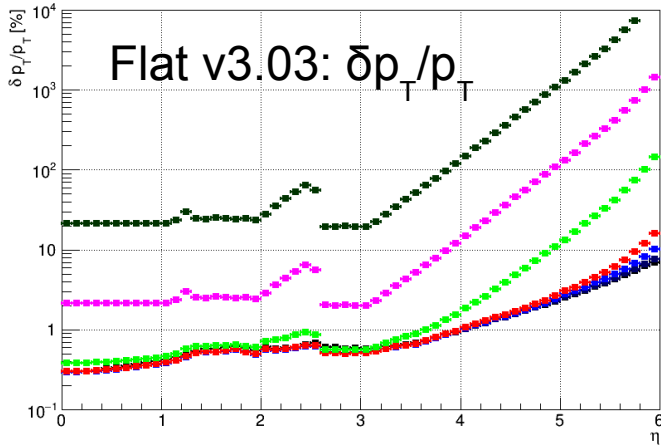
$$V_{ij}^{\text{MS}} = \sum_{k=1}^{\max[i-1, j-1]} (s_i - s_k)(s_j - s_k) f_i^{\text{proj}} f_j^{\text{proj}} \langle \vartheta_k^2 \rangle$$

$$\langle \vartheta_k^2 \rangle = \left(\frac{13.6 \text{ MeV}}{\beta p c} \right)^2 \frac{d_k / X_0}{\sin(\vartheta_k + \alpha_k)} \left(1 + 0.038 \ln \frac{d_k / X_0}{\sin(\vartheta_k + \alpha_k)} \right)^2$$

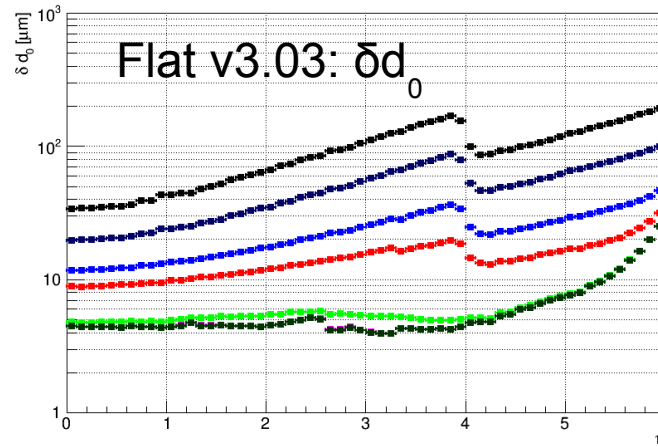
- f_i^{proj} : projection of track \perp error ellipse to meas. plane (module)
- α_k : tilt angle of meas. plane
- d_k / X_0 : module thickness in X_0

Layout v3.03 x v4.01: Track Parameters Res.

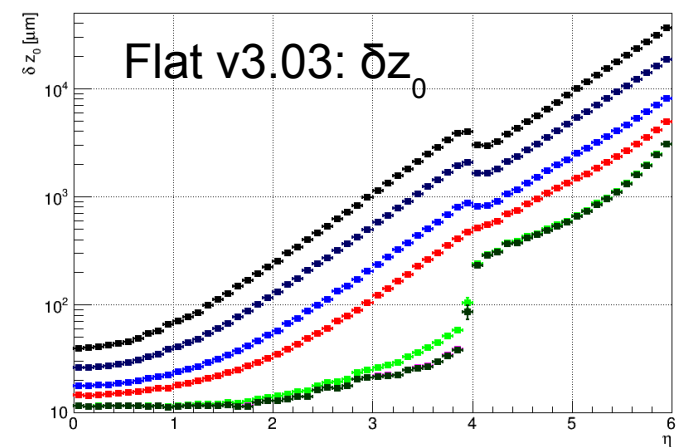
p_T resolution versus η - const p_T across η



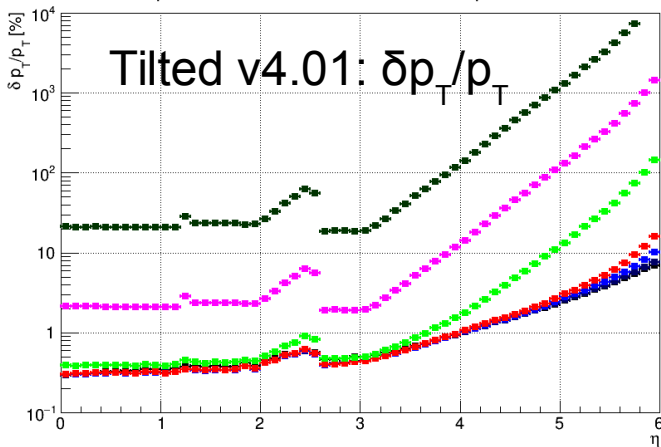
Transverse impact parameter error - const p_T across η



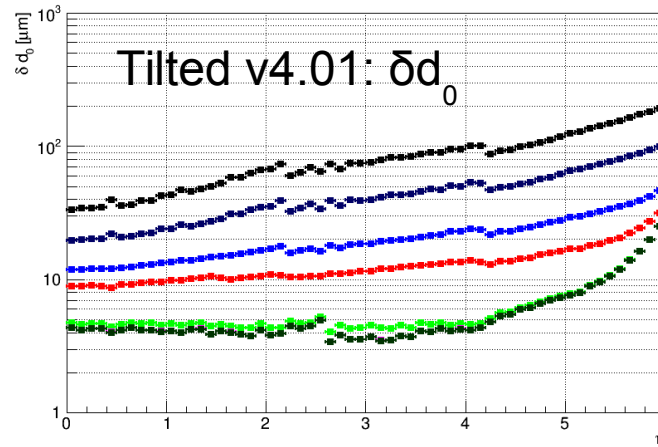
Longitudinal impact parameter error - const p_T across η



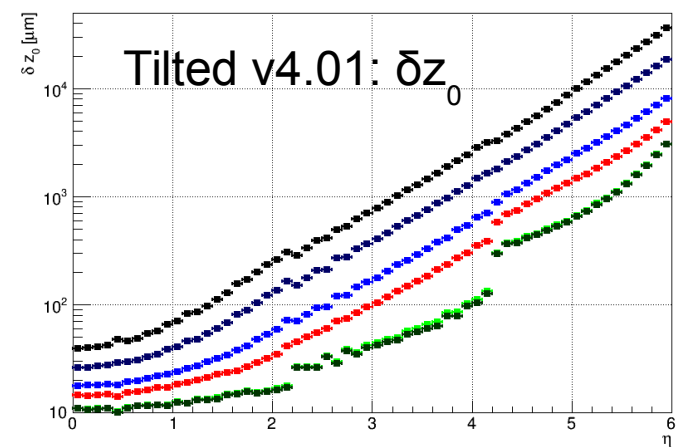
p_T resolution versus η - const p_T across η



Transverse impact parameter error - const p_T across η



Longitudinal impact parameter error - const p_T across η



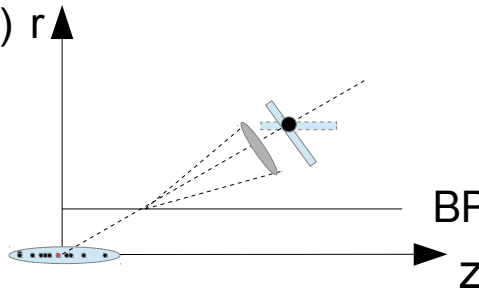
For details see <http://fcc-tklayout.web.cern.ch>

Back-up Slides: Track Propagator & MS Effects

Track Propagator in PR & MS

- 4 key parameters affecting propagation of error ellipse:

- material effect @ ϑ (tilt angle α)
- radial propagation distance (notice dependence on p_T not p)
- projection factor on det. plane



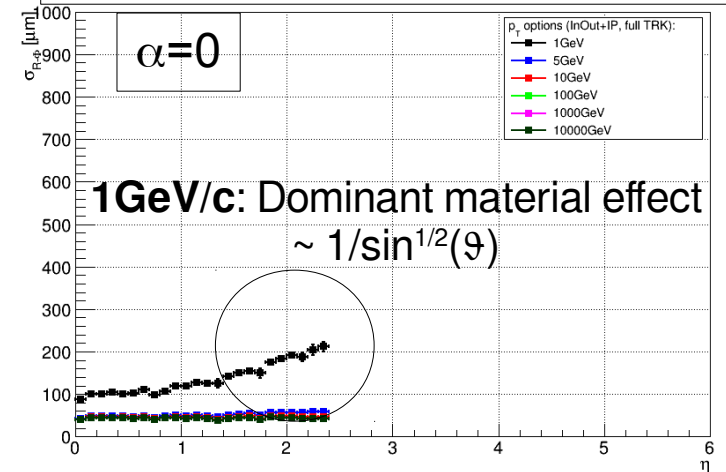
$$\sigma_{MS}^2 \approx \langle \vartheta_{pT}^2 \rangle \frac{d/X_0}{\sin(\vartheta + \alpha)} \Delta r^2 f_{proj}$$

$$\langle \vartheta_{pT}^2 \rangle = \left(\frac{13.6 \text{ MeV}}{\beta p_{TC}} \right)^2 \left(1 + 0.038 \ln \frac{d/X_0}{\sin(\vartheta + \alpha)} \right)^2$$

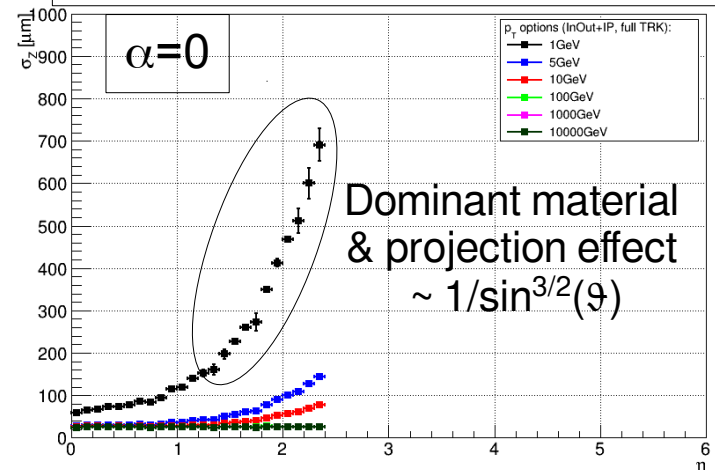
$$f_{proj} = \left(\frac{1}{\sin(\vartheta + \alpha)} \right)^2 \text{ proj. in } Z$$

$$f_{proj} = 1 \text{ proj. in } R-\Phi$$

Propagated $\sigma_{R-\Phi}$ on 4th BRL layer



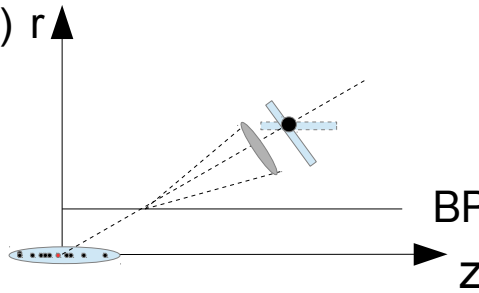
Propagated σ_z on 4th BRL layer



Track Propagator in PR & MS – Ideal Tilting

- 4 key parameters affecting propagation of error ellipse:

- **material effect @ ϑ (tilt angle α)**
- **radial propagation distance**
(notice dependence on p_T not p)
- **projection factor** on det. plane



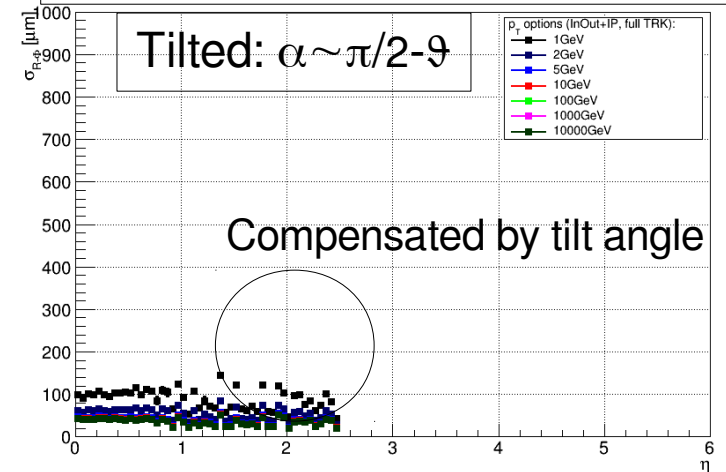
$$\sigma_{MS}^2 \approx \langle \vartheta_{pT}^2 \rangle \frac{d/X_0}{\sin(\vartheta + \alpha)} \Delta r^2 f_{proj}$$

$$\langle \vartheta_{pT}^2 \rangle = \left(\frac{13.6 \text{ MeV}}{\beta p_{TC}} \right)^2 \left(1 + 0.038 \ln \frac{d/X_0}{\sin(\vartheta + \alpha)} \right)^2$$

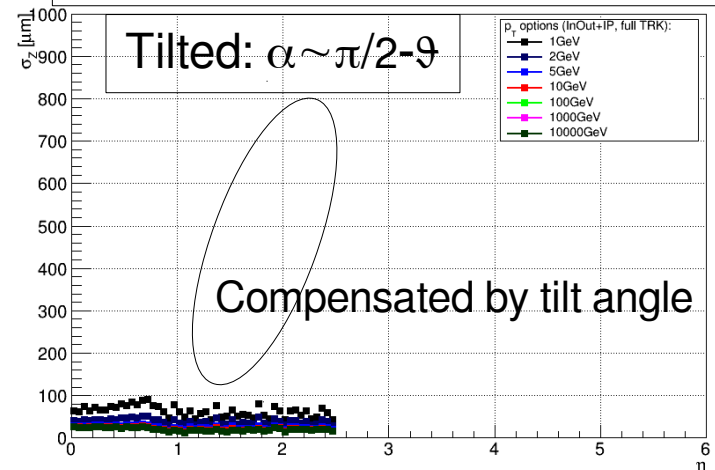
$$f_{proj} = \left(\frac{1}{\sin(\vartheta + \alpha)} \right)^2 \text{ proj. in } Z$$

$$f_{proj} = 1 \text{ proj. in } R-\Phi$$

Propagated $\sigma_{R-\Phi}$ on 4th BRL layer



Propagated σ_z on 4th BRL layer



- To min. mat. effects, tracker in tilted layout advantageous!**

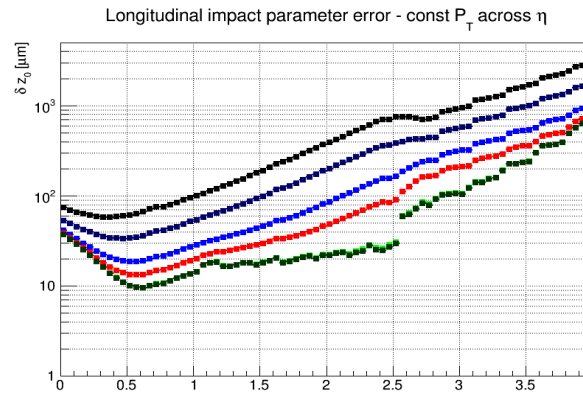
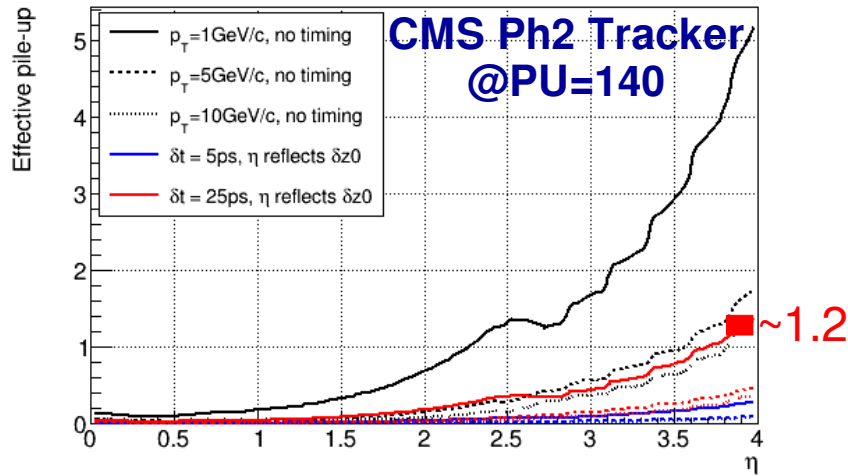
Back-up Slides:

Implications of High Pile-Up on Primary Vertexing

Effective Pile-up Rate

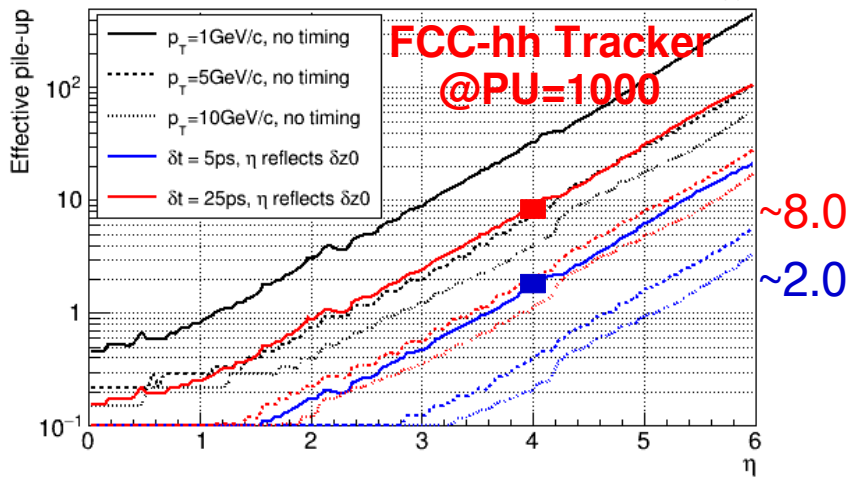
→ Compare **FCC-hh** to **HL-LHC** conditions (**PU~140**), applied to e.g. CMS Ph2 upgrade layout

Effective pile-up confusing prim. vertexing @95% CL: $\sigma_z^{\text{Gauss}}=75\text{mm}$, $\langle\mu_{\text{tot}}\rangle=140$



Decrease in δz_0 needs to be “compensated” by extra timing info (in FWD)

Effective pile-up confusing prim. vertexing @95% CL: $\sigma_z^{\text{Gauss}}=75\text{mm}$, $\langle\mu_{\text{tot}}\rangle=1000$

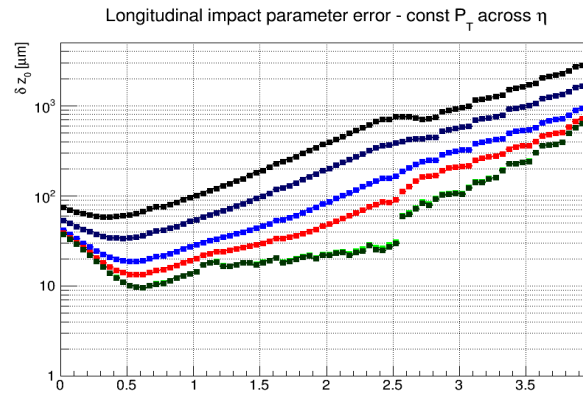
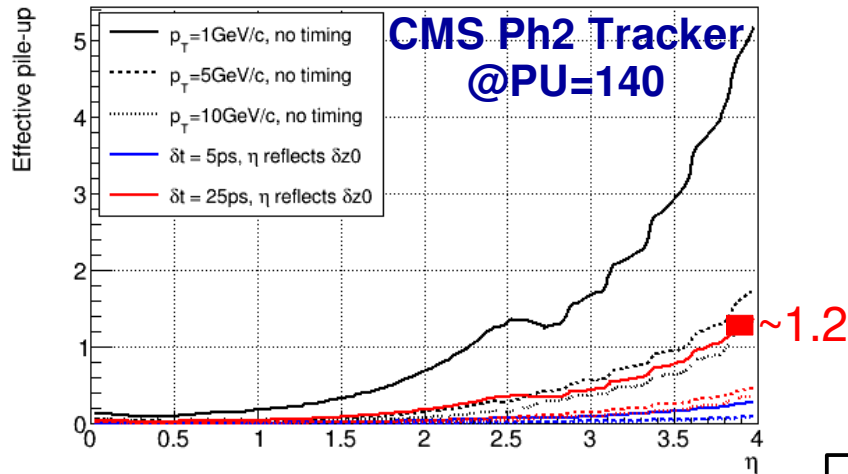


FCC-hh: 2D vertexing (time & z) essential, namely in the FWD region! But..., may not be sufficient to mitigate the PU effect for tracks @ $\eta > 4.0$

Effective Pile-up Rate & Effect of Bunch Size

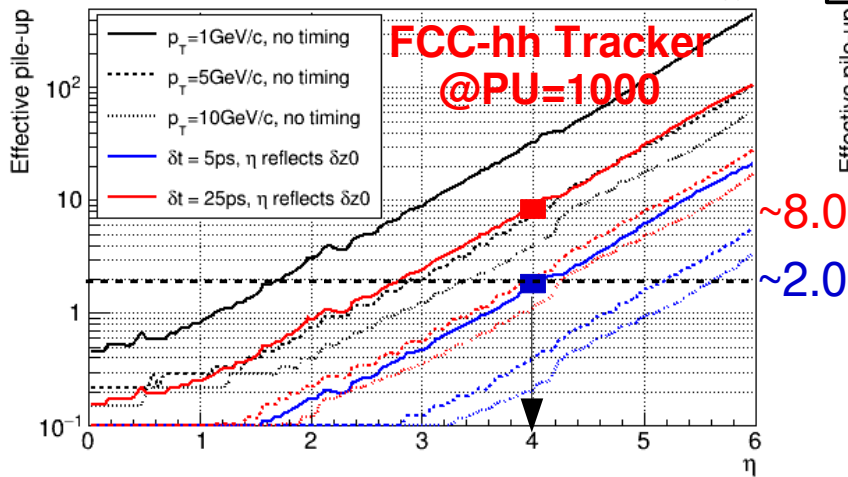
→ Compare **FCC-hh** to **HL-LHC** conditions (**PU~140**), applied to e.g. CMS Ph2 upgrade layout

Effective pile-up confusing prim. vertexing @95% CL: $\sigma_z^{\text{Gauss}}=75\text{mm}$, $\langle\mu_{\text{tot}}\rangle=140$

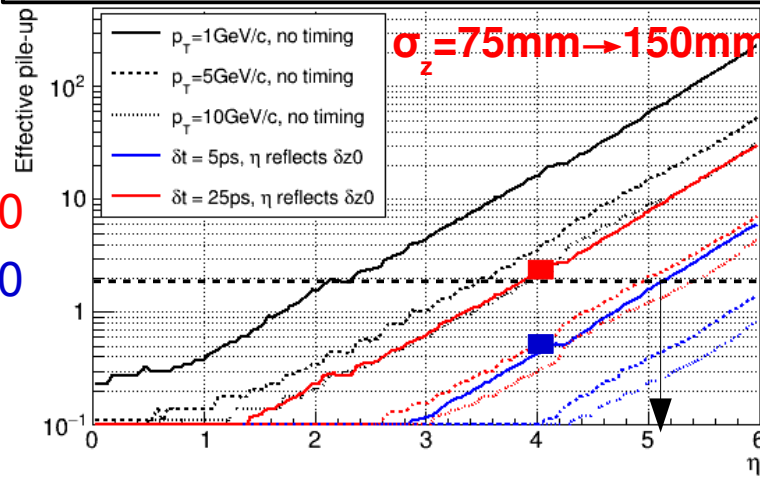


Decrease in δz_0 needs to be “compensated” by extra timing info (in FWD)

Effective pile-up confusing prim. vertexing @95% CL: $\sigma_z^{\text{Gauss}}=75\text{mm}$, $\langle\mu_{\text{tot}}\rangle=1000$



How about increasing bunch size in Z?



Improves quadratically due to 2D VTX