

QCD calculations of heavy baryon form factors

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Why beauty baryon decays?

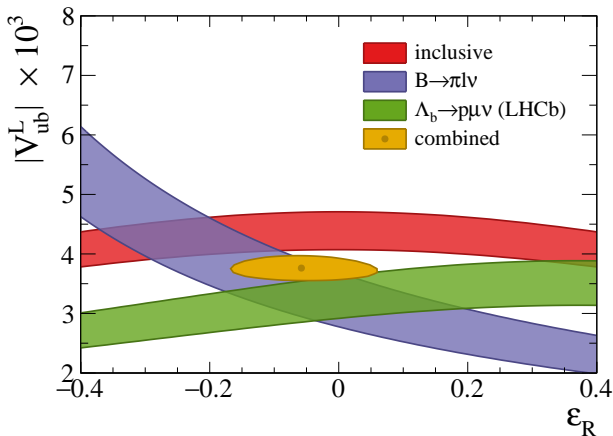
- Systematic studies in QCD not yet available.
 - ▶ Novel factorization properties for heavy baryon form factors.
 - ▶ Renormalization properties for the LCDAs of heavy baryons beyond the leading twist.
 - ▶ Perturbative calculations of short-distance functions more challenging.
- Great efforts on beauty meson decays already, no NP found yet.
 - ▶ Topical anomalies and tensions?
- Beauty baryon decays provide non-trivial tests of the SM.
 - ▶ Allow for the study of spin correlations, extract the helicity structure of \mathcal{H}_{eff} .
 - ▶ $\Lambda_b \rightarrow \Lambda(\rightarrow N\pi)\ell\ell$ offers complementary information on the short-distance physics.
 - ▶ Λ_b baryon is simpler than B meson in the heavy quark limit.
- A lot of progresses on the measurements of beauty baryon decays from CDF and LHCb.
 - ▶ Semileptonic decays: $\Lambda_b \rightarrow p\ell\nu$, $\Lambda_b \rightarrow \Lambda\ell\ell$, $\Lambda_b \rightarrow \Lambda_c\ell\nu$. (→ this talk!)
 - ▶ Hadronic decays: $\Lambda_b \rightarrow p\pi$, $\Lambda_b \rightarrow pK$, $\Lambda_b \rightarrow \Lambda\phi$, $\Lambda_b \rightarrow \Lambda_c\pi$, etc.

Calculational tools for beauty baryon form factors

- Lattice QCD (→ Next talk by Stefan Meinel).
- Light-Cone Sum Rules in QCD/SCET:
 - ▶ QCD factorization for the correlation function in the **appropriate** kinematical region.
 - ▶ Hadronic dispersion relation for the the correlation function.
 - ▶ Matching with the quark-hadron duality and the Borel transformation.
 - ▶ **Constructions of the sum rules with different LCDAs possible.**
- QCD/SCET Factorization:
 - ▶ Less assumptions theoretically, more challenging conceptually/technically.
 - ▶ Parametrically power suppressed corrections numerically dominant.
→ Rapidity divergences in the subleading-power factorization formulae.
- **TMD Factorization:**
 - ▶ Including the Sudakov mechanism, but no definite power counting scheme.
 - ▶ Definitions of TMD parton densities more complicated.

Part I: Semileptonic $\Lambda_b \rightarrow p\ell\nu_l$ decays

- An alternative way to determine $|V_{ub}|$ exclusively [arXiv:1504.01568].



- ▶ Strong interaction dynamics described by the transition form factors.
- ▶ Much more complicated when including QED corrections.

General aspects of $\Lambda_b \rightarrow p$ form factors

- Traditional parameterizations [Manohar and Wise \oplus many others]:

$$\begin{aligned}\langle N(P') | \bar{u} \gamma_\mu b | \Lambda_b(P) \rangle &= \bar{N}(P') \left\{ f_1(q^2) \gamma_\mu + i \frac{f_2(q^2)}{m_{\Lambda_b}} \sigma_{\mu\nu} q^\nu + \frac{f_3(q^2)}{m_{\Lambda_b}} q_\mu \right\} \Lambda_b(P), \\ \langle N(P') | \bar{u} \gamma_\mu \gamma_5 b | \Lambda_b(P) \rangle &= \bar{N}(P') \left\{ g_1(q^2) \gamma_\mu + i \frac{g_2(q^2)}{m_{\Lambda_b}} \sigma_{\mu\nu} q^\nu + \frac{g_3(q^2)}{m_{\Lambda_b}} q_\mu \right\} \gamma_5 \Lambda_b(P).\end{aligned}$$

Axial-vector matrix element does not vanish, different from $B \rightarrow \pi$ transition.

- Helicity-based parameterizations [Feldmann and Yip, 2011]:

$$\begin{aligned}\langle N(P') | \bar{u} \gamma_\mu b | \Lambda_b(P) \rangle &= \bar{N}(P') \left\{ f_+(q^2) \frac{m_{\Lambda_b} + m_N}{s_+} \left(P_\mu + P'_\mu - \frac{q_\mu}{q^2} (m_{\Lambda_b}^2 - m_N^2) \right) \right. \\ &\quad \left. + f_\perp(q^2) \left(\gamma_\mu - \frac{2m_N}{s_+} P_\mu - \frac{2m_{\Lambda_b}}{s_+} P'_\mu \right) + f_0(q^2) (m_{\Lambda_b} - m_N) \frac{q_\mu}{q^2} \right\} \Lambda_b(P).\end{aligned}$$

Simpler expressions for angular distributions and for unitary bounds.

- Symmetry-based parameterizations [Feldmann and Yip, 2011]:

$$\langle N(P') | \bar{u} \Gamma b | \Lambda_b(P) \rangle = \xi_{ij}^{(\pm)}(v \cdot P') \bar{N}(P') \left\{ \Gamma_i \frac{\not{v} \pm \not{P}'_\mp}{4} \Gamma \Gamma_j \right\} \Lambda_b(P).$$

$\xi_{ij}^{(-)}(v \cdot P')$ suppressed in both the HQET and SCET limits.

Symmetry relations of $\Lambda_b \rightarrow p$ form factors

- Form factors in the HQET limit [Manohar and Wise 2000]:

$$\langle N(P') | \bar{u} \Gamma b | \Lambda_b(P) \rangle = \bar{N}(P') [F_1(v \cdot P') + F_2(v \cdot P') \not{v}] \Gamma \Lambda_b(P),$$

implying the relations

$$\begin{aligned} f_1 = g_1 &= F_1 + \frac{m_N}{m_{\Lambda_b}} F_2, & f_2 = f_3 = g_2 = g_3 &= F_2, \\ f_0 = g_+ = g_\perp &= F_1 + F_2, & g_0 = f_+ = f_\perp &= F_1 - F_2. \end{aligned}$$

- ▶ Only two form factors in the HQET limit.

- Form factors in the SCET limit [Mannel and YMW, 2011; Feldmann and Yip, 2011]:

$$\langle N(P') | \bar{u} \Gamma b | \Lambda_b(P) \rangle = F(n_+ \cdot P') \bar{N}(P') \Gamma \Lambda_b(P).$$

- ▶ Only a single (soft) form factor in the large recoil limit.
- ▶ Symmetry relations still hold including the leading-power hard spectator interaction.
- ▶ Symmetry breaking effects induced by the perturbative and power corrections.

SCET factorization for $\Lambda_b \rightarrow p$ form factors

- QCD Factorization at leading power in Λ/m_b [Wei Wang, 2011]:

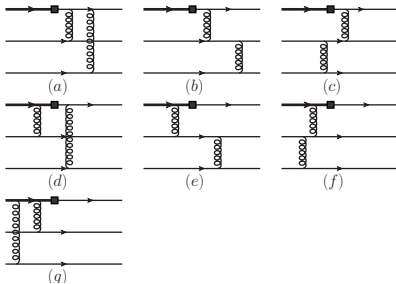
$$F(n_+ \cdot P') = \Phi_{\Lambda_b}(\omega_i) \otimes H(\omega_i, x_i) \otimes \Phi_N(x_i) + \mathcal{O}(\Lambda_{QCD}/E).$$

- ▶ Leading power contribution due to the exchanges of two hard-collinear gluons.
- ▶ Leading power contribution calculable in QCD factorization.
- ▶ The scaling behaviour (different from the soft contribution):

$$F(n_+ \cdot P') \sim \mathcal{O}(\Lambda_{QCD}^2/(n_+ \cdot P')^2).$$

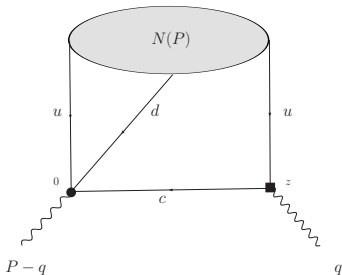
- The LO QCD diagrams:

- ▶ Leading power contributions from the diagrams (a), (b), (f), but (b) + (f) vanishes.
- ▶ For the diagram (a), both two gluons are transverse polarized.
- ▶ Need the light-cone projectors of both the Λ_b -baryon and nucleon for a complete calculation even at tree level [BFWY, 2013; BFMS, 2000].



Light-cone sum rules of $\Lambda_b \rightarrow p$ form factors

- Correlation function [Khodjamirian, Klein, Mannel, YMW, 2011]:



- ▶ Interpolating current of Λ_b baryon is not unique.

$$\Pi_a(P, q) = i \int d^4z e^{iq \cdot z} \times \langle 0 | T \{ \eta(0), j_a(z) \} | N(P) \rangle .$$

Will consider both the axial-vector and pseudoscalar Λ_b currents.

- ▶ Background pollution from the negative-parity baryons in the dispersion relation.

- How to avoid the background pollution?

- ▶ Parity projector matrix $(1 \pm \gamma_5)/2$ for heavy-baryon sum rule [Bagan, Chabab, Dosch, Narison, 1993].
- ▶ Choose the “old-fashioned” correlation function and construct sum rules in the complex q_0 -space [Jido, Kodama, Oka, 1996].
- ▶ Eliminate the contamination by combining sum rules obtained from different kinematical structures [Khodjamirian, Klein, Mannel, YMW, 2011].

Light-cone sum rules of $\Lambda_b \rightarrow p$ form factors

- 27 nucleon LCDAs up to the twist-6 approximation [Braun, Fries, Mahnke, Stein, 2000]:

$$\begin{aligned}
 & 4 \langle 0 | \varepsilon^{ijk} u_\alpha^i(a_1 z) u_\beta^j(a_2 z) d_\gamma^k(a_3 z) | N(P) \rangle \\
 &= \mathcal{S}_1 m_N C_{\alpha\beta} (\gamma_5 u_N)_\gamma + \mathcal{S}_2 m_N^2 C_{\alpha\beta} (\not{z} \gamma_5 u_N)_\gamma + \mathcal{P}_1 m_N (\gamma_5 C)_{\alpha\beta} (u_N)_\gamma \\
 &+ \mathcal{P}_2 m_N^2 (\gamma_5 C)_{\alpha\beta} (\not{z} u_N)_\gamma + \left(\mathcal{V}_1 + \frac{z^2 m_N^2}{4} \mathcal{V}_1^M \right) (PC)_{\alpha\beta} (\gamma_5 u_N)_\gamma \\
 &+ \mathcal{V}_2 m_N (PC)_{\alpha\beta} (\not{z} \gamma_5 u_N)_\gamma + \mathcal{V}_3 m_N (\gamma_\mu C)_{\alpha\beta} (\gamma^\mu u_N)_\gamma \\
 &+ \mathcal{V}_4 m_N^2 (\not{z} C)_{\alpha\beta} (\gamma_5 u_N)_\gamma + \mathcal{V}_5 m_N^2 (\gamma_\mu C)_{\alpha\beta} (i\sigma^{\mu\nu} z_\nu \gamma_5 u_N)_\gamma \\
 &+ \mathcal{V}_6 m_N^3 (\not{z} C)_{\alpha\beta} (\not{z} \gamma_5 u_N)_\gamma + \left(\mathcal{A}_1 + \frac{z^2 m_N^2}{4} \mathcal{A}_1^M \right) (P\gamma_5 C)_{\alpha\beta} (u_N)_\gamma \\
 &+ \mathcal{A}_2 m_N (P\gamma_5 C)_{\alpha\beta} (\not{z} u_N)_\gamma + \mathcal{A}_3 m_N (\gamma_\mu \gamma_5 C)_{\alpha\beta} (\gamma^\mu u_N)_\gamma \\
 &+ \mathcal{A}_4 m_N^2 (\not{z} \gamma_5 C)_{\alpha\beta} (u_N)_\gamma + \mathcal{A}_5 m_N^2 (\gamma_\mu \gamma_5 C)_{\alpha\beta} (i\sigma^{\mu\nu} z_\nu u_N)_\gamma \\
 &+ \mathcal{A}_6 m_N^3 (\not{z} \gamma_5 C)_{\alpha\beta} (\not{z} u_N)_\gamma + \left(\mathcal{T}_1 + \frac{z^2 m_N^2}{4} \mathcal{T}_1^M \right) (P^v i\sigma_{\mu\nu} C)_{\alpha\beta} (\gamma^\mu \gamma_5 u_N)_\gamma \\
 &+ \mathcal{T}_2 m_N (z^\mu P^v i\sigma_{\mu\nu} C)_{\alpha\beta} (\gamma_5 u_N)_\gamma + \mathcal{T}_3 m_N (\sigma_{\mu\nu} C)_{\alpha\beta} (\sigma^{\mu\nu} \gamma_5 u_N)_\gamma \\
 &+ \mathcal{T}_4 m_N (P^v \sigma_{\mu\nu} C)_{\alpha\beta} (\sigma^{\mu\rho} z_\rho \gamma_5 u_N)_\gamma + \mathcal{T}_5 m_N^2 (z^v i\sigma_{\mu\nu} C)_{\alpha\beta} (\gamma^\mu \gamma_5 u_N)_\gamma \\
 &+ \mathcal{T}_6 m_N^2 (z^\mu P^v i\sigma_{\mu\nu} C)_{\alpha\beta} (\not{z} \gamma_5 u_N)_\gamma + \mathcal{T}_7 m_N^2 (\sigma_{\mu\nu} C)_{\alpha\beta} (\sigma^{\mu\nu} \not{z} \gamma_5 u_N)_\gamma \\
 &+ \mathcal{T}_8 m_N^3 (z^v \sigma_{\mu\nu} C)_{\alpha\beta} (\sigma^{\mu\rho} z_\rho \gamma_5 u_N)_\gamma.
 \end{aligned}$$

Light-cone sum rules of $\Lambda_b \rightarrow p$ form factors

- Conformal expansion of the LCDAs:

$$\begin{aligned}V_1(x_i, \mu) &= 120x_1x_2x_3[\phi_3^0(\mu) + \phi_3^+(\mu)(1 - 3x_3)], \\A_1(x_i, \mu) &= 120x_1x_2x_3(x_2 - x_1)\phi_3^-(\mu), \\T_1(x_i, \mu) &= 120x_1x_2x_3[\phi_3^0(\mu) - \frac{1}{2}(\phi_3^+(\mu) - \phi_3^-(\mu))(1 - 3x_3)].\end{aligned}$$

- ▶ All DAs expanded up to the NLO conformal spin.
- ▶ For the d -wave contributions to the twist-3 DAs, see [Lenz et al, 2009].
- ▶ For more recent update, see [Anikin, Braun, Offen, 2013].

- Input parameters [Braun, Fries, Mahnke, Stein, 2000]:

$$\begin{aligned}f_N &= (5.0 \pm 0.5) \times 10^{-3} \text{ GeV}^2, & \lambda_1 &= -(27 \pm 9) \times 10^{-3} \text{ GeV}^2, \\ & & \lambda_2 &= (54 \pm 19) \times 10^{-3} \text{ GeV}^2.\end{aligned}$$

QCDSR estimates already confronted with the lattice calculations [Braun et al, 2014]:

$$\begin{aligned}f_N &= 2.84(1)(33) \times 10^{-3} \text{ GeV}^2, & \lambda_1 &= -4.13(2)(20) \times 10^{-3} \text{ GeV}^2, \\ & & \lambda_2 &= 8.19(5)(39) \times 10^{-3} \text{ GeV}^2.\end{aligned}$$

5 additional parameters taken from [Braun, Lenz, Wittmann, 2006].

Light-cone sum rules of $\Lambda_b \rightarrow p$ form factors

- LCSR predictions $q^2 = 0$ [Khodjamirian, Klein, Mannel, YMW, 2011]:

form factors	$\eta_{\Lambda_b}^{(\mathcal{A})}$	$\eta_{\Lambda_b}^{(\mathcal{P})}$
$f_1(0)$	$0.14^{+0.03}_{-0.03}$	$0.12^{+0.03}_{-0.04}$
$f_2(0)$	$-0.054^{+0.016}_{-0.013}$	$-0.047^{+0.015}_{-0.013}$
$g_1(0)$	$0.14^{+0.03}_{-0.03}$	$0.12^{+0.03}_{-0.03}$
$g_2(0)$	$-0.028^{+0.012}_{-0.009}$	$-0.016^{+0.007}_{-0.005}$

- ▶ The SCET relations $f_1(0) = g_1(0)$ and $f_2(0) = g_2(0) \sim \mathcal{O}(\Lambda/m_b)$ hold numerically.
- ▶ The LCSR predictions insensitive to the choices of the Λ_b current.
- ▶ All twist 3, 4, 5 components of nucleon DAs numerically important.
- ▶ Only Feynman mechanism considered here.

Light-cone sum rules of $\Lambda_b \rightarrow p$ form factors

- Extrapolation toward larger q^2 with the z -series parametrization:

$$z(q^2, t_0) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}, \quad t_+ = (m_B + m_\pi)^2.$$

Conformal mapping of the cut q^2 -plane onto the disk $|z(q^2, t_0)| \leq 1$.

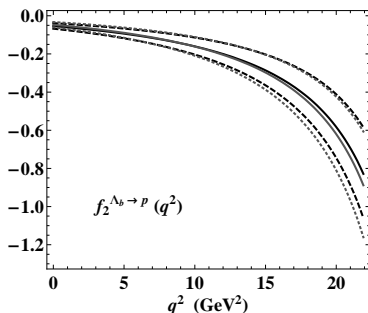
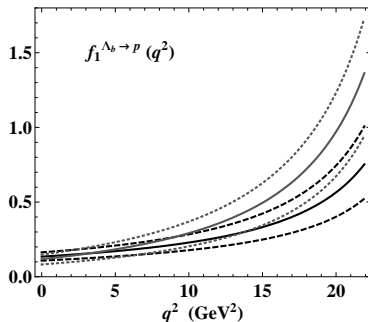
- The BCL parametrization [Bourrely, Caprini, Lellouch, 2009]:

$$f_i(q^2) = \frac{f_i(0)}{1 - q^2/m_{B^*(1^-)}^2} \left\{ 1 + b_i \left(z(q^2, t_0) - z(0, t_0) \right) \right\},$$
$$g_i(q^2) = \frac{g_i(0)}{1 - q^2/m_{B^*(1^+)}^2} \left\{ 1 + \tilde{b}_i \left(z(q^2, t_0) - z(0, t_0) \right) \right\}.$$

- ▶ Alternative parameterizations possible [Boyd, Grinstein, Lebed, 1995].
- ▶ Unitary bounds improvable [Becher, Hill, 2006].

Light-cone sum rules of $\Lambda_b \rightarrow p$ form factors

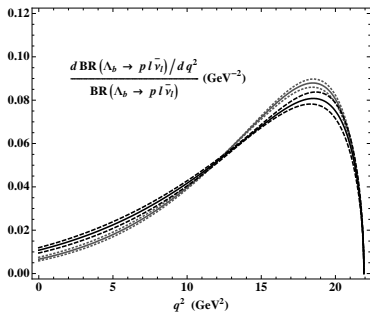
- Theory predictions of $\Lambda_b \rightarrow p$ form factors in the whole q^2 region:



- The q^2 -shape of form factors more sensitive to the choice of the Λ_b current at large q^2 .
- Confronted with the lattice predictions with extrapolation toward small q^2 [Detmold, Lehner, Meinel, 2015]. → A combined LCSR \oplus Lattice fit?

Semileptonic $\Lambda_b \rightarrow p \ell \bar{\nu}_l$ decays

- Differential branching ratio [Khodjamirian, Klein, Mannel, YMW, 2011]:



- Enhancement at large q^2 due to the growing form factors and the S -wave phase space factor.
- Integrated BR:

$$\left(3.3^{+1.5}_{-1.2} \Big|_{\text{th.}} \pm 0.1 \Big|_{\text{exp.}}\right) \times 10^{-4}.$$
 LHCb 2015 data:

$$(4.1 \pm 1.0) \times 10^{-4}.$$
- About 10% uncertainty of $\mathcal{B}(\Lambda_b \rightarrow p \ell \nu)$ at $q^2 > 15 \text{ GeV}^2$ normalized to the Λ_c channel.

- Determination of $|V_{ub}|$:

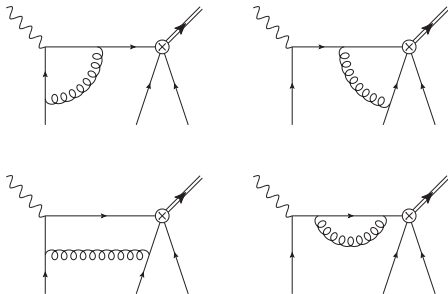
$$\Delta\zeta(0, q_{\text{max}}^2) = \frac{1}{|V_{ub}|^2} \int_0^{q_{\text{max}}^2} dq^2 \frac{d\Gamma}{dq^2}(\Lambda_b \rightarrow p \ell \nu_l),$$

$$\Delta\zeta(0, 11 \text{ GeV}^2) = 5.5^{+2.5}_{-2.0} \text{ ps}^{-1}.$$

- Compare with $B \rightarrow \pi \ell \nu_l$ (NLO LCSR): $\Delta\zeta(0, 12 \text{ GeV}^2) = 4.59^{+1.00}_{-0.85} \text{ ps}^{-1}$.
- Perturbative corrections to $\Lambda_b \rightarrow p$ form factors needed to reduce uncertainties.

The nucleon-LCSR at NLO

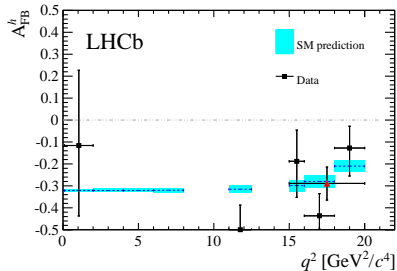
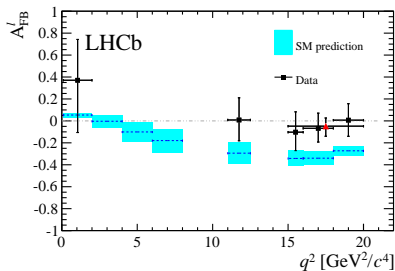
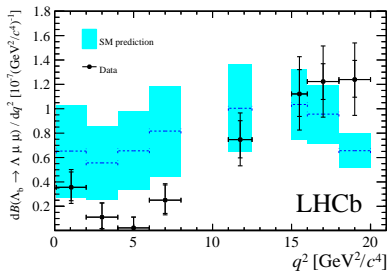
- Technical aspects of the baryonic correlation functions at NLO:
 - ▶ Renormalization (subtraction) scheme in dimensional regularization.
 - ▶ Complicated operator mixing beyond the twist four approximation.
 - ▶ A large number of the nucleon LCDAs.
- An example: nucleon form factors[Passek-Kumerički, Peters, 2011; Anikin, Braun, Offen, 2013]
 - ▶ The Krankl-Manashov scheme without evanescent operators.
 - ▶ Typical NLO diagrams:



- ▶ More complicated for $\Lambda_b \rightarrow p$ form factors due to two hard scales.
→ Hard-collinear factorization for the QCD matrix elements.

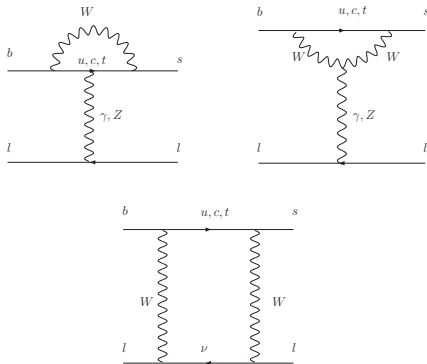
Part II: FCNC $\Lambda_b \rightarrow \Lambda \ell \ell$ decays

- Experimental status [LHCb, 2015]:



FCNC $\Lambda_b \rightarrow \Lambda \ell \ell$ decays

● Partonic $b \rightarrow s \ell^+ \ell^-$ diagrams in the SM:



► Effective Hamiltonian [Buchalla, Buras and Lautenbacher, 1996].

► Semileptonic and magnetic operators:

$$O_{7\gamma} \propto \bar{s} \sigma_{\mu\nu} (m_s L + m_b R) b F^{\mu\nu},$$

$$O_{8g} \propto \bar{s}_i \sigma_{\mu\nu} (1 + \gamma_5) T_{ij}^a b_j G^{a\mu\nu},$$

$$O_{9,10} \propto (\bar{s}b)_{V-A} (\bar{\ell}\ell)_{V,A}.$$

Need C_9 and C_{10} at NNLL, C_7^{eff} and C_8^{eff} at NLL.

● Four-quark operators [Beneke, Feldmann and Seidel, 2001]:

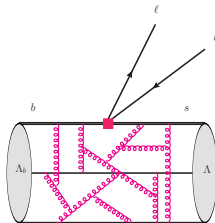
$$O_1 = (\bar{s}p)_{V-A} (\bar{p}b)_{V-A}, \quad O_2 = (\bar{s}^i p^i)_{V-A} (\bar{p}^j b^j)_{V-A} \quad (p = u, c),$$

$$O_{3,5} = (\bar{s}b)_{V-A} \sum_q (\bar{q}q)_{V\mp A}, \quad O_{4,6} = (\bar{s}^i b^j)_{V-A} \sum_q (\bar{q}^j q^i)_{V\mp A}.$$

In practice the **CMM operator basis** used [Chetyrkin, Misiak and Münz, 1996].

Naive factorization

- Heavy-to-light form factors:



$$\begin{aligned} & \langle \Lambda(p', s') \ell^+ \ell^- | (\bar{s}b)_{V-A} (\bar{\ell}\ell)_{V,A} | \Lambda_b(p, s) \rangle \\ &= \underbrace{\langle \Lambda(p', s') | (\bar{s}b)_{V-A} | \Lambda_b(p, s) \rangle}_{\Lambda_b \rightarrow \Lambda \text{ form factors!}} \langle \ell^+ \ell^- | (\bar{\ell}\ell)_{V,A} | 0 \rangle. \end{aligned}$$

Need also tensor form factors!

- Less known Λ -baryon LCDAs [Liu, Cui, Huang, 2014].
→ (Soft) Helicity form factors of $\Lambda_b \rightarrow \Lambda$ computed from the Λ_b -baryon LCSR.
- The Λ_b LCDAs in HQET [Ball, Braun, Gardi, 2008]:

$$\varepsilon^{abc} \langle 0 | \left(u^a(\tau_1 n_-) C \gamma_5 \not{n}_- d^b(\tau_2 n_-) \right) h_v^c(0) | \Lambda_b(v, s) \rangle = f_{\Lambda_b}^{(2)} \tilde{\phi}_2(\tau_1, \tau_2) u_{\Lambda_b}(v, s),$$

$$\varepsilon^{abc} \langle 0 | \left(u^a(\tau_1 n_-) C \gamma_5 \not{n}_+ d^b(\tau_2 n_-) \right) h_v^c(0) | \Lambda_b(v, s) \rangle = f_{\Lambda_b}^{(2)} \tilde{\phi}_4(\tau_1, \tau_2) u_{\Lambda_b}(v, s),$$

$$\varepsilon^{abc} \langle 0 | \left(u^a(\tau_1 n_-) C \gamma_5 d^b(\tau_2 n_-) \right) h_v^c(0) | \Lambda_b(v, s) \rangle = f_{\Lambda_b}^{(1)} \tilde{\phi}_3^s(\tau_1, \tau_2) u_{\Lambda_b}(v, s),$$

$$\varepsilon^{abc} \langle 0 | \left(u^a(\tau_1 n_-) C \gamma_5 i \sigma_{\mu\nu} n_+^\mu n_-^\nu d^b(\tau_2 n_-) \right) h_v^c(0) | \Lambda_b(v, s) \rangle = 2 f_{\Lambda_b}^{(1)} \tilde{\phi}_3^\sigma(\tau_1, \tau_2) u_{\Lambda_b}(v, s).$$

RGE of $\phi_2(\omega_1, \omega_2)$ contains both the [Lange-Neubert](#) and [Brodsky-Lepage](#) kernels.

Light-cone projectors for the Λ_b -baryon

- General three-quark matrix elements [Bell, Feldmann, YMW, Yip, 2013]:

$$\begin{aligned} & \varepsilon^{abc} \langle 0 | \left[(u_\alpha^a(z_1) d_\beta^b(z_2)) h_v^c(0) | \Lambda_b(v, s) \right] \rangle \\ & \equiv \frac{1}{4} \left\{ \underbrace{f_{\Lambda_b}^{(1)} \left[\tilde{M}^{(1)}(v, z_1, z_2) \gamma_5 C^T \right]_{\beta\alpha}}_{\text{chiral odd}} + f_{\Lambda_b}^{(2)} \left[\tilde{M}^{(2)}(v, z_1, z_2) \gamma_5 C^T \right]_{\beta\alpha} \right\} u_{\Lambda_b}(v, s). \end{aligned}$$

- Lorentz-covariant parametrization:

$$\begin{aligned} \tilde{M}^{(2)}(v, z_1, z_2) &= \tilde{\Phi}_2(t_1, t_2, z_1^2, z_2^2, z_1 \cdot z_2) \not{v} + \frac{\tilde{\Phi}_X(t_1, t_2, z_1^2, z_2^2, z_1 \cdot z_2)}{4t_1 t_2} (\not{z}_2 \not{v} \not{z}_1 - \not{z}_1 \not{v} \not{z}_2) \\ &+ \frac{\tilde{\Phi}_{42}^{(i)}(t_1, t_2, z_1^2, z_2^2, z_1 \cdot z_2)}{2t_1} \not{z}_1 + \frac{\tilde{\Phi}_{42}^{(ii)}(t_1, t_2, z_1^2, z_2^2, z_1 \cdot z_2)}{2t_2} \not{z}_2. \end{aligned}$$

Expanding z_i around the light-cone ($n_- z_i \ll z_i^\perp \ll n_+ z_i$) [$\tau_i = n_+ z_i / 2$]:

$$\begin{aligned} \tilde{M}^{(2)}(v, z_1, z_2) &\longrightarrow \frac{\not{n}_+}{2} \tilde{\Phi}_2(\tau_1, \tau_2) + \frac{\not{n}_-}{2} \left(\tilde{\Phi}_2(\tau_1, \tau_2) + \tilde{\Phi}_{42}^{(i)}(\tau_1, \tau_2) + \tilde{\Phi}_{42}^{(ii)}(\tau_1, \tau_2) \right) \\ &+ \frac{\tilde{\Phi}_{42}^{(i)}(\tau_1, \tau_2)}{2\tau_1} \not{z}_1^\perp + \frac{\tilde{\Phi}_{42}^{(ii)}(\tau_1, \tau_2)}{2\tau_2} \not{z}_2^\perp \\ &+ \tilde{\Phi}_X(\tau_1, \tau_2) \left(\frac{\not{z}_1^\perp}{2\tau_1} - \frac{\not{z}_2^\perp}{2\tau_2} \right) \left(\frac{\not{n}_- \not{n}_+}{4} - \frac{\not{n}_+ \not{n}_-}{4} \right) + \mathcal{O}(z_{i\perp}^2, n_- z_i). \end{aligned}$$

Light-cone projectors for the Λ_b -baryon

- Performing the Fourier transformation yields:

$$\begin{aligned} M^{(2)}(\omega_1, \omega_2) &= \frac{\not{h}_+}{2} \phi_2(\omega_1, \omega_2) + \frac{\not{h}_-}{2} \phi_4(\omega_1, \omega_2) \\ &\quad - \frac{1}{2} \gamma_\mu^\perp \int_0^{\omega_1} d\eta_1 \left(\phi_{42}^{(i)}(\eta_1, \omega_2) - \phi_X(\eta_1, \omega_2) \right) \frac{\not{h}_+ \not{h}_-}{4} \frac{\partial}{\partial k_{1\mu}^\perp} \\ &\quad - \frac{1}{2} \gamma_\mu^\perp \int_0^{\omega_1} d\eta_1 \left(\phi_{42}^{(i)}(\eta_1, \omega_2) + \phi_X(\eta_1, \omega_2) \right) \frac{\not{h}_- \not{h}_+}{4} \frac{\partial}{\partial k_{1\mu}^\perp} \\ &\quad - \frac{1}{2} \gamma_\mu^\perp \int_0^{\omega_2} d\eta_2 \left(\phi_{42}^{(ii)}(\omega_1, \eta_2) - \phi_X(\omega_1, \eta_2) \right) \frac{\not{h}_- \not{h}_+}{4} \frac{\partial}{\partial k_{2\mu}^\perp} \\ &\quad - \frac{1}{2} \gamma_\mu^\perp \int_0^{\omega_2} d\eta_2 \left(\phi_{42}^{(ii)}(\omega_1, \eta_2) + \phi_X(\omega_1, \eta_2) \right) \frac{\not{h}_+ \not{h}_-}{4} \frac{\partial}{\partial k_{2\mu}^\perp}. \end{aligned}$$

Four more LCDAs sensitive to **the transverse momenta** of the light quarks.

- Constraints due to the Wandzura-Wilczek ("on-shell") approximation:

$$\begin{aligned} \phi_{42}^{(i)}(\omega_1, \omega_2) - \phi_{42}^{(ii)}(\omega_1, \omega_2) &= \frac{\partial}{\partial \omega_1} (\omega_1 \phi_4(\omega_1, \omega_2)) - \frac{\partial}{\partial \omega_2} (\omega_2 \phi_4(\omega_1, \omega_2)), \\ 2\phi_X(\omega_1, \omega_2) + \phi_4(\omega_1, \omega_2) - \phi_2(\omega_1, \omega_2) &= \frac{\partial}{\partial \omega_1} (\omega_1 \phi_4(\omega_1, \omega_2)) + \frac{\partial}{\partial \omega_2} (\omega_2 \phi_4(\omega_1, \omega_2)). \end{aligned}$$

- **Can construct the light-cone projectors in the momentum space directly.**

$\Lambda_b \rightarrow \Lambda$ form factors from the Λ_b -baryon LCSR

- Starting point: correlation function [Feldmann, Yip, 2011; YMW and Shen, 2015]

$$\begin{aligned}\Pi_{\mu,a}(p,q) &= i \int d^4x e^{iq \cdot x} \langle 0 | T \{ j_\Lambda(x), j_{\mu,a}(0) \} | \Lambda_b(p) \rangle, \\ j_{\mu,a} &= \bar{s} \Gamma_{\mu,a} b, \quad j_\Lambda = \epsilon_{ijk} (u_i^\top C \gamma_5 \not{d}_j) s_k.\end{aligned}$$

Different choices of the Λ -baryon current possible, but **the axial-vector collinear current favored**.

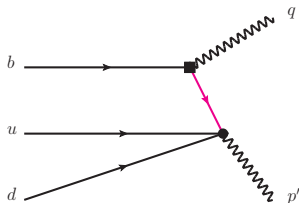
- Hadronic dispersion relations:

$$\begin{aligned}\Pi_{\mu,V}(p,q) &= \frac{f_\Lambda(\mu) (n \cdot p')}{m_\Lambda^2 / n \cdot p' - \bar{n} \cdot p' - i0} \frac{\not{n}}{2} \left[f_{\Lambda_b \rightarrow \Lambda}^T(q^2) \gamma_{\perp\mu} + \frac{f_{\Lambda_b \rightarrow \Lambda}^0(q^2) - f_{\Lambda_b \rightarrow \Lambda}^+(q^2)}{2(1 - n \cdot p' / m_{\Lambda_b})} n_\mu \right. \\ &\quad \left. + \frac{f_{\Lambda_b \rightarrow \Lambda}^0(q^2) + f_{\Lambda_b \rightarrow \Lambda}^+(q^2)}{2} \bar{n}_\mu \right] \Lambda_b(p) \\ &\quad + \int_{\omega_s}^{+\infty} d\omega' \frac{1}{\omega' - \bar{n} \cdot p' - i0} \frac{\not{n}}{2} \left[\rho_{V,\perp}^h(\omega', n \cdot p') \gamma_{\perp\mu} + \rho_{V,n}^h(\omega', n \cdot p') n_\mu \right. \\ &\quad \left. + \rho_{V,\bar{n}}^h(\omega', n \cdot p') \bar{n}_\mu \right] \Lambda_b(p).\end{aligned}$$

The effects from the negative-parity baryons treated naively.

$\Lambda_b \rightarrow \Lambda$ form factors from the Λ_b -baryon LCSR

Factorization at tree level:



$$\begin{aligned} & \Pi_{\mu, V(A)}^{(0)}(p, q) \\ &= f_{\Lambda_b}^{(2)}(\mu) \int_0^{+\infty} d\omega'_1 \int_0^{+\infty} d\omega'_2 \frac{\Psi_4(\omega'_1, \omega'_2)}{\omega'_1 + \omega'_2 - \bar{n} \cdot p' - i0} \\ & \quad \times (1, \gamma_5) \frac{\not{n}}{2} (\gamma_{\perp\mu} + \bar{n}_\mu) \Lambda_b(v) + \mathcal{O}(\alpha_s), \end{aligned}$$

Kinematics:

$$n \cdot p' \sim \mathcal{O}(m_b), \quad |\bar{n} \cdot p'| \sim \mathcal{O}(\Lambda).$$

- The LO LCSR after the continuum subtraction ($\rightarrow \omega_s$) and the Borel transformation ($\rightarrow \omega_M$):

$$\begin{aligned} F_{\Lambda_b \rightarrow \Lambda}^i(q^2) &= \frac{f_{\Lambda_b}^{(2)}(\mu)}{f_\Lambda(\mu) n \cdot p'} \exp\left[\frac{m_\Lambda^2}{n \cdot p' \omega_M}\right] \int_0^{\omega_s} d\omega' e^{-\omega'/\omega_M} \underbrace{\tilde{\Psi}_4(\omega')}_{\equiv \omega' \int_0^1 du \phi_4(u \omega', (1-u) \omega')} + \mathcal{O}(\alpha_s). \\ &\equiv \omega' \int_0^1 du \phi_4(u \omega', (1-u) \omega') \end{aligned}$$

- Power counting scheme:

$$\omega_s \sim \omega_M \sim \frac{\Lambda^2}{n \cdot p'}, \quad \implies \quad F_{\Lambda_b \rightarrow \Lambda}^i(q^2) \sim 1/(n \cdot p')^3.$$

Suppressed by a factor of $\Lambda/n \cdot p'$ compared to the LP contribution.

Factorization of the correlation functions

- Aim: QCD factorization of the correlation functions [YMW and Shen, 2015]

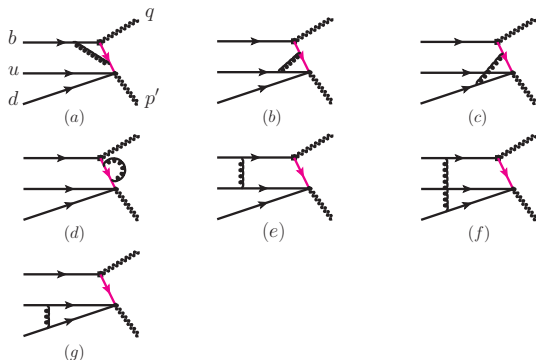
$$\begin{aligned}\Pi_{\mu,V(A)} &= (1, \gamma_5) \frac{\not{n}}{2} \left[\Pi_{\perp,V(A)} \gamma_{\perp\mu} + \Pi_{\bar{n},V(A)} \bar{n}_{\mu} + \Pi_{n,V(A)} n_{\mu} \right] \Lambda_b(v), \\ \Pi_{\perp,V(A)} &= f_{\Lambda_b}^{(2)}(\mu) C_{\perp,V(A)}(n \cdot p', \mu) \int_0^{\infty} d\omega_1 \int_0^{\infty} d\omega_2 \frac{1}{\omega_1 + \omega_2 - \bar{n} \cdot p' - i0} \\ &\quad J\left(\frac{\mu^2}{\bar{n} \cdot p' \omega_i}, \frac{\omega_i}{\bar{n} \cdot p'}\right) \psi_4(\omega_1, \omega_2, \mu).\end{aligned}$$

Similar factorization formulae for the other invariant functions.

- **Hard functions** the same as the matching coefficients of weak currents from QCD onto SCET_I.
 - ▶ Already known at **one loop** [Bauer et al, 2000; Beneke et al, 2004] and at **two loops** [Bonciani et al, 2008; Asatrian et al, 2008; Beneke et al, 2008; Bell, 2008; Bell et al, 2010].
- **Two equivalent strategies for computing the jet function:**
 - ▶ Apply the SCET_I Feynman rules.
 - ▶ Extract the hard-collinear contributions of QCD diagrams with the method of regions. Algebraically simpler [**→ this talk!**].
- **Factorization-scale independence of the correlation functions:**
 - ▶ Explicit RGE of $\phi_4(\omega_1, \omega_2, \mu)$ unknown.
 - ▶ The Λ -baryon current not renormalization invariant.

Factorization of the correlation functions

- QCD diagrams at one loop:



- ▶ Only hard, hard-collinear and soft regions contribute at LP in Λ/m_b .
- ▶ Soft contributions cancelled by the IR subtraction terms.
Automatically in SCET, also verified diagrammatically at one loop.
- ▶ Symmetrical diagrams related to each other simply.

Factorization of the correlation functions

- Hard functions:

$$C_{\perp, V(A)}(n \cdot p', \mu) = 1 - \frac{\alpha_s(\mu) C_F}{4\pi} \left[2 \ln^2 \frac{\mu}{n \cdot p'} + 5 \ln \frac{\mu}{m_b} - 2 \text{Li}_2 \left(1 - \frac{1}{r} \right) - \ln^2 r + \frac{3r-2}{1-r} \ln r + \frac{\pi^2}{12} + 6 \right].$$

- ▶ Similar for the other hard functions, reproduced exactly.
- ▶ All hard functions obey the same RGEs.

- Jet function [YMW and Shen, 2015]:

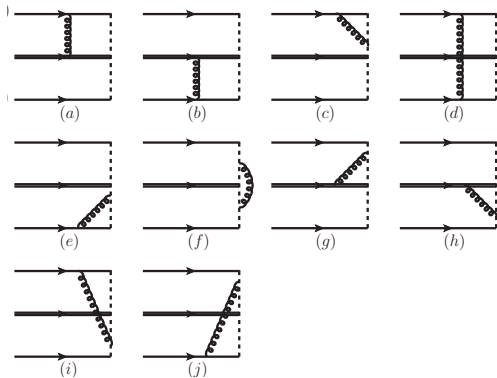
$$J \left(\frac{\mu^2}{\bar{n} \cdot p' \omega_i}, \frac{\omega_i}{\bar{n} \cdot p'} \right) = 1 + \frac{\alpha_s(\mu)}{4\pi} \frac{4}{3} \left\{ \ln^2 \frac{\mu^2}{n \cdot p' (\omega - \bar{n} \cdot p')} - 2 \ln \frac{\omega - \bar{n} \cdot p'}{\omega_2 - \bar{n} \cdot p'} \ln \frac{\mu^2}{n \cdot p' (\omega - \bar{n} \cdot p')} - \frac{1}{2} \ln \frac{\mu^2}{n \cdot p' (\omega - \bar{n} \cdot p')} - \ln^2 \frac{\omega - \bar{n} \cdot p'}{\omega_2 - \bar{n} \cdot p'} + 2 \ln \frac{\omega - \bar{n} \cdot p'}{\omega_2 - \bar{n} \cdot p'} \left[\frac{\omega_2 - \bar{n} \cdot p'}{\omega_1} - \frac{3}{4} \right] - \frac{\pi^2}{6} - \frac{1}{2} \right\}.$$

- ▶ **Universal jet function** for all the form factors.
- ▶ Symmetry property of $\psi_4(\omega_1, \omega_2, \mu)$ used to reduce the expression.

Factorization of the correlation functions

- Factorization-scale dependence:

$$\begin{aligned} \frac{d}{d \ln \mu} \Pi_{\perp, V(A)} &= \frac{\alpha_s(\mu)}{4\pi} \frac{4}{3} \int_0^\infty d\omega_1 \int_0^\infty d\omega_2 \frac{1}{\omega_1 + \omega_2 - \bar{n} \cdot p' - i0} \\ &\times \left[4 \ln \frac{\mu}{\omega - \bar{n} \cdot p'} - 4 \ln \frac{\omega - \bar{n} \cdot p'}{\omega_2 - \bar{n} \cdot p'} - 6 \right] \left[f_{\Lambda_b}^{(2)}(\mu) \psi_4(\omega_1, \omega_2, \mu) \right] \\ &+ \int_0^\infty d\omega_1 \int_0^\infty d\omega_2 \frac{1}{\omega_1 + \omega_2 - \bar{n} \cdot p' - i0} \frac{d}{d \ln \mu} \left[f_{\Lambda_b}^{(2)}(\mu) \psi_4(\omega_1, \omega_2, \mu) \right]. \end{aligned}$$



Renormalization of $\psi_4(\omega_1, \omega_2, \mu)$ yields

$$\begin{aligned} & - \frac{\alpha_s(\mu)}{4\pi} \frac{4}{3} \int_0^\infty d\omega_1 \int_0^\infty d\omega_2 \frac{1}{\omega - \bar{n} \cdot p' - i0} \\ & \times \left[4 \ln \frac{\mu}{\omega - \bar{n} \cdot p'} - 4 \ln \frac{\omega - \bar{n} \cdot p'}{\omega_2 - \bar{n} \cdot p'} - 5 \right] \\ & \times \left[f_{\Lambda_b}^{(2)}(\mu) \psi_4(\omega_1, \omega_2, \mu) \right], \end{aligned}$$

implying

$$\frac{d}{d \ln \mu} \left[\frac{\Pi_{\perp, V(A)}(n \cdot p', \bar{n} \cdot p', \mu)}{f_{\Lambda}(\mu)} \right] = 0.$$

Resummation of large logarithms

- Distinguish the factorization scale (μ) from the renormalization scales for the Λ -baryon current (\mathbf{v}) and for the weak current in QCD (\mathbf{v}'):

$$J\left(\frac{\mu^2}{\bar{n}\cdot p' \omega_i}, \frac{\omega_i}{\bar{n}\cdot p'}, \mathbf{v}\right) = J\left(\frac{\mu^2}{\bar{n}\cdot p' \omega_i}, \frac{\omega_i}{\bar{n}\cdot p'}\right) + \delta J\left(\frac{\mu^2}{\bar{n}\cdot p' \omega_i}, \frac{\omega_i}{\bar{n}\cdot p'}, \mathbf{v}\right),$$
$$C_{T(\bar{T})}^A(n\cdot p', \mu, \mathbf{v}') = C_{T(\bar{T})}^A(n\cdot p', \mu) + \delta C_{T(\bar{T})}^A(n\cdot p', \mu, \mathbf{v}').$$

- Determination of \mathbf{v} and \mathbf{v}' dependence:

$$\frac{d}{d \ln \mathbf{v}} \ln \delta J\left(\frac{\mu^2}{\bar{n}\cdot p' \omega_i}, \frac{\omega_i}{\bar{n}\cdot p'}, \mathbf{v}\right) = -\sum_k \left(\frac{\alpha_s(\mu)}{4\pi}\right)^k \gamma_\Lambda^{(k)},$$
$$\frac{d}{d \ln \mathbf{v}'} \ln \delta C_{T(\bar{T})}^A(n\cdot p', \mu, \mathbf{v}') = -\sum_k \left(\frac{\alpha_s(\mu)}{4\pi}\right)^k \gamma_{T(\bar{T})}^{(k)}.$$

Renormalization conditions:

$$\delta J\left(\frac{\mu^2}{\bar{n}\cdot p' \omega_i}, \frac{\omega_i}{\bar{n}\cdot p'}, \mu\right) = 0, \quad \delta C_{T(\bar{T})}^A(n\cdot p', \mu, \mu) = 0.$$

- NLL resummation for **the hard functions** by solving the evolution equations in μ and \mathbf{v}' .

NLL resummation of $\Lambda_b \rightarrow \Lambda$ form factors

- Resummation improved form factors [YMW and Shen, 2015]:

$$\begin{aligned}
 & f_{\Lambda}(v) (n \cdot p') e^{-m_{\Lambda}^2/(n \cdot p' \omega_M)} \left\{ f_{\Lambda_b \rightarrow \Lambda}^T(q^2), g_{\Lambda_b \rightarrow \Lambda}^T(q^2) \right\} \\
 &= f_{\Lambda_b}^{(2)}(\mu) [U_1(n \cdot p'/2, \mu_h, \mu) C_{\perp, V(A)}(n \cdot p', \mu_h)] \int_0^{\omega_S} d\omega' e^{-\omega'/\omega_M} \psi_{4, \text{eff}}(\omega', \mu, v), \\
 & f_{\Lambda}(v) (n \cdot p') e^{-m_{\Lambda}^2/(n \cdot p' \omega_M)} \left\{ f_{\Lambda_b \rightarrow \Lambda}^0(q^2), g_{\Lambda_b \rightarrow \Lambda}^0(q^2) \right\} \\
 &= f_{\Lambda_b}^{(2)}(\mu) [U_1(n \cdot p'/2, \mu_h, \mu) C_{\bar{n}, V(A)}(n \cdot p', \mu_h)] \int_0^{\omega_S} d\omega' e^{-\omega'/\omega_M} \psi_{4, \text{eff}}(\omega', \mu, v) \\
 & \quad + f_{\Lambda_b}^{(2)}(\mu) \left(1 - \frac{n \cdot p'}{m_{\Lambda_b}} \right) C_{n, V(A)}(n \cdot p', \mu_h) \int_0^{\omega_S} d\omega' e^{-\omega'/\omega_M} \tilde{\psi}_4(\omega', \mu).
 \end{aligned}$$

- NLL resummation for the twist-4 Λ_b -DA not included (unknown 2-loop RGE).

- Only symmetry-breaking effect from the hard-gluon contribution taken into account.
- Including the hard-collinear symmetry breaking effect [Feldmann and Yip, 2011]

$$\begin{aligned}
 f_{\Lambda_b \rightarrow \Lambda}^T(q^2) &= [\dots] + \frac{2m_{\Lambda_b}}{n \cdot p'} \Delta\xi_{\Lambda}(n \cdot p'), & g_{\Lambda_b \rightarrow \Lambda}^T(q^2) &= [\dots] - \frac{2m_{\Lambda_b}}{n \cdot p'} \Delta\xi_{\Lambda}(n \cdot p'), \\
 f_{\Lambda_b \rightarrow \Lambda}^0(q^2) &= [\dots] - \frac{2m_{\Lambda_b}}{n \cdot p'} \Delta\xi_{\Lambda}(n \cdot p'), & g_{\Lambda_b \rightarrow \Lambda}^0(q^2) &= [\dots] + \frac{2m_{\Lambda_b}}{n \cdot p'} \Delta\xi_{\Lambda}(n \cdot p').
 \end{aligned}$$

$\Delta\xi_{\Lambda}$ defined by the **B-type SCET current**, calculable with the **power-suppressed** correction function.

The Λ_b -baryon LCDAs

- Light-cone distribution amplitudes of the Λ_b -baryon [Ball, Braun, Gardi, 2008]:

$$\phi_4^{\text{I}}(\omega, \mu_0) = \frac{1}{\omega_0^2} e^{-\omega/\omega_0},$$

$$\phi_4^{\text{II}}(\omega, \mu_0) = \frac{1}{\omega_0^2} e^{-(\omega/\omega_1)^2}, \quad \omega_1 = \sqrt{2} \omega_0,$$

$$\phi_4^{\text{III}}(\omega, \mu_0) = \frac{1}{\omega_0^2} \left[1 - \sqrt{\left(2 - \frac{\omega}{\omega_2}\right) \frac{\omega}{\omega_2}} \right] \theta(\omega_2 - \omega), \quad \omega_2 = \sqrt{\frac{12}{10 - 3\pi}} \omega_0.$$

$\phi_4^{(\text{II}, \text{III})}(\omega, \mu_0)$ analogy to the mesonic counterparts [De Fazio, Feldmann, Hurth, 2008].

- The shape of $F_{\Lambda_b \rightarrow \Lambda}^i(q^2)$ less model dependent.

Solid, dotted, and dashed curves from Model-I, II and III.

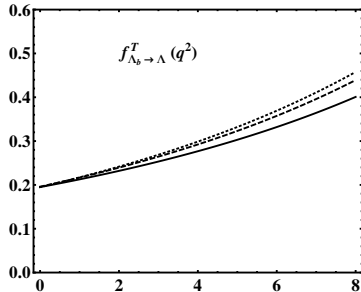
Fitting $f_{\Lambda_b \rightarrow \Lambda}^+(0) = 0.18 \pm 0.04$

\Rightarrow

Model-I: $\omega_0 = 280_{-38}^{+47}$ MeV ,

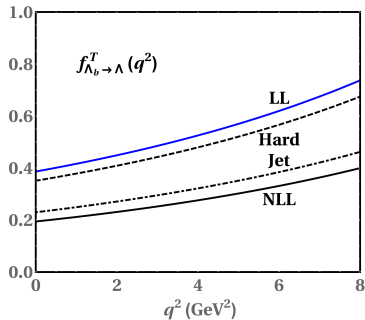
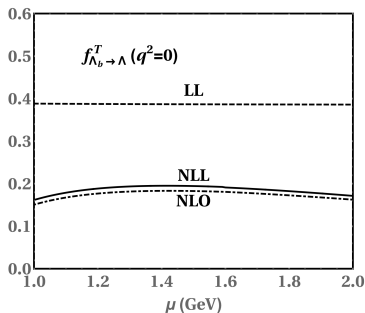
Model-II: $\omega_0 = 386_{-37}^{+45}$ MeV ,

Model-III: $\omega_0 = 273_{-29}^{+38}$ MeV .



$\Lambda_b \rightarrow \Lambda$ form factors from the Λ_b -baryon LCSR

- Factorization scale dependence and radiative correction:



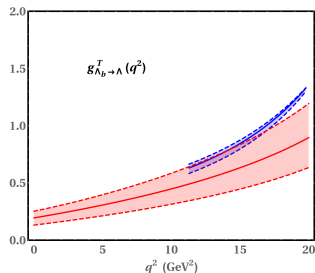
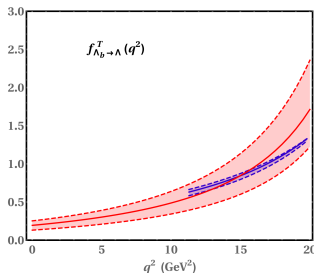
- ▶ Dominant radiative effect from the NLO QCD correction instead of the QCD resummation.
- ▶ NLO correction dominated by the hard-collinear contribution instead of the hard fluctuation.
⇒ **A complete calculation of the NLO jet function important!**
- ▶ Radiative effect can induce 50 % reduction of the form factors.

$\Lambda_b \rightarrow \Lambda$ form factors from the Λ_b -baryon LCSR

- Extrapolation toward larger q^2 with the z -series expansion:

$$z(q^2, t_0) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}, \quad t_+ = (m_{B_s} + m_\pi)^2 < (m_{\Lambda_b} + m_\Lambda)^2.$$

- The predicted form factors [YMW and Shen, 2015]:



- ▶ Pink and blue bands predicted from LCSR and Lattice QCD [Detmold et al, 2012].
- ▶ Reasonable agreement but different shapes, only HQET form factors from Lattice QCD.
- ▶ Agreement with the lattice results from relativistic b quarks [Detmold and Meinel, 2016].

Non-factorizable corrections

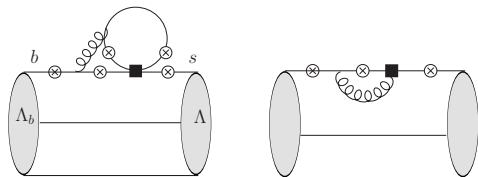
- Hadronic operators enter into the game, when combined with the QED interaction.
- Nonlocal hadronic matrix element:

$$\mathcal{H}_\mu^{(\Lambda_b \rightarrow \Lambda)}(p, q) = i \int d^4x e^{iq \cdot x} \langle \Lambda(p') | T \{ J_\mu^{em}(x), H_{eff}(0) \} | \Lambda_b(p) \rangle.$$

- QED corrections to the hadronic operators \nRightarrow the form factors.
 - (a) Hard spectator interactions \nRightarrow local operators at the m_W scale.
 - (b) Soft gluon radiations generate non-local operators.
 - (c) Strong phases of the matrix elements.
- Focus on the QCD dynamics at large hadronic recoil.

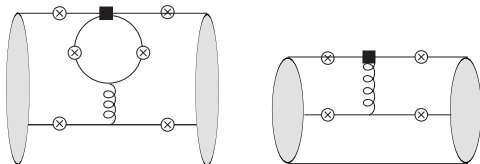
FCNC $\Lambda_b \rightarrow \Lambda ll$ decays

- Hard vertex corrections [Asatyan, Asatrian, Greub and Walker, 2001; Seidel, 2004]:



- ▶ Two-loop matrix elements of penguin operators still missing.
- ▶ Sizeable two-loop hard vertex corrections due to $\ln(q^2/m_b^2)$ enhancement.

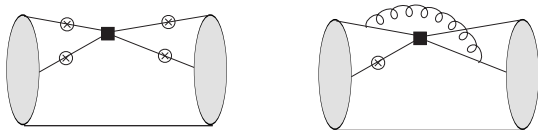
- Hard spectator interactions:



- ▶ Cannot be computed with QCD factorization approach.
- ▶ SCET matrix elements can be computed from the Λ_b -baryon LCSRs.

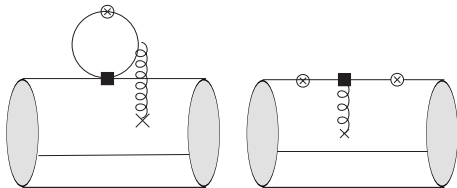
FCNC $\Lambda_b \rightarrow \Lambda$ decays

- Weak annihilations:



- ▶ Either CKM or Wilson-coefficient suppressed.
- ▶ Small correction estimated in the soft-overlap approach [Mannel and Recksiegel, 1997].

- Soft gluon radiations [Khodjamirian, Mannel, Pivovarov, YMW, 2010; KMW, 2012]:

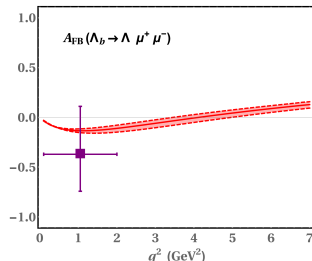
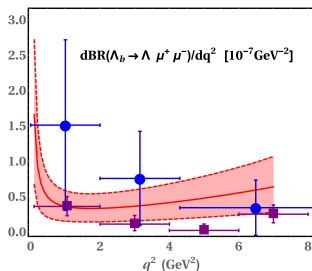


- ▶ Soft gluon radiation power suppressed, but enhanced by the photon pole.
- ▶ Need the still unknown four-particle Λ_b LCDAs in HQET.

Physical observables in $\Lambda_b \rightarrow \Lambda \ell \ell$ decays

- Predictions in the factorization limit:

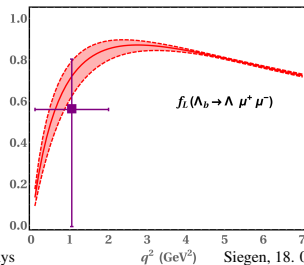
$$\frac{d^2\Gamma(\Lambda_b \rightarrow \Lambda \ell^+ \ell^-)}{dq^2 d\cos\theta} = \frac{3}{8} \left[(1 + \cos^2\theta) H_T(q^2) + 2\cos\theta H_A(q^2) + 2(1 - \cos^2\theta) H_L(q^2) \right].$$



Pink bands predicted by LCSR.

Purple squares from LHCb.

Blue circles from CDF.



Conclusions and Outlook

- Novel factorization properties of beauty baryon decays at large recoil.
- $|V_{ub}|$ determination from the semileptonic $\Lambda_b \rightarrow p\ell\nu_\ell$ decays promising.
 - ▶ Subleading power contribution to the form factors dominant numerically.
 - ▶ NLO corrections to the nucleon-LCSR necessary to extract $|V_{ub}|$.
 - ▶ A direct calculation of the LP contribution at NLO in QCDF possible.
 - ▶ Improvement of nonperturbative input parameters from lattice QCD?
- Interesting FCNC $\Lambda_b \rightarrow \Lambda\ell\ell$ decays:
 - ▶ Sizeable hard-collinear corrections from the Λ_b -baryon LCSR at NLL.
 - ▶ Non-form-factor corrections to $\Lambda_b \rightarrow \Lambda\ell\ell$ still missing.
→ SCET factorization \oplus LCSR for the effective matrix elements.
 - ▶ Renormalization properties of the higher-twist Λ_b LCDAs.
- Hadronic beauty baryon decays in QCD:
 - ▶ Only factorizable contribution at LP in the heavy quark limit?
 - ▶ Asymmetries more challenging due to the competing (N)LP contributions.