

Differential cross sections in collisions of low-energy antiprotons with ions and atoms

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Outline

- 1 Differential cross sections for ionization
- 2 Elastic scattering: the Coulomb glory

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- **Kinematically complete experiments** for ion-impact ionization became feasible within development of the 'reaction microscope' techniques.
- **Fully differential cross sections** (FDCS) are accessible now, and provide the most stringent test of theoretical models.
- Different types of '**Reaction Microscopes**': COLTRIMS, MOTRIMS, advanced MOTRIMS with an alternative optical cooling and trapping scheme.
- For some systems one found **large discrepancies** at differential level between theory and experiment, as well as between different theories.
- Studying ionization process at detailed level to gain insight into the phenomenon of **spontaneous electron-positron pair creation** in heavy-ion collisions.

Key aspects of the developed approach

- **Semiclassical treatment** of the collision.
- **Time-dependent Dirac equation** for a bare ion projectile colliding with a one-active-electron target atom

$$i\frac{\partial\Psi(\mathbf{r}, t)}{\partial t} = [H_T + V_P(t)]\Psi(\mathbf{r}, t).$$

- **Finite-basis-set expansion** of wave function Ψ is used to solve it.

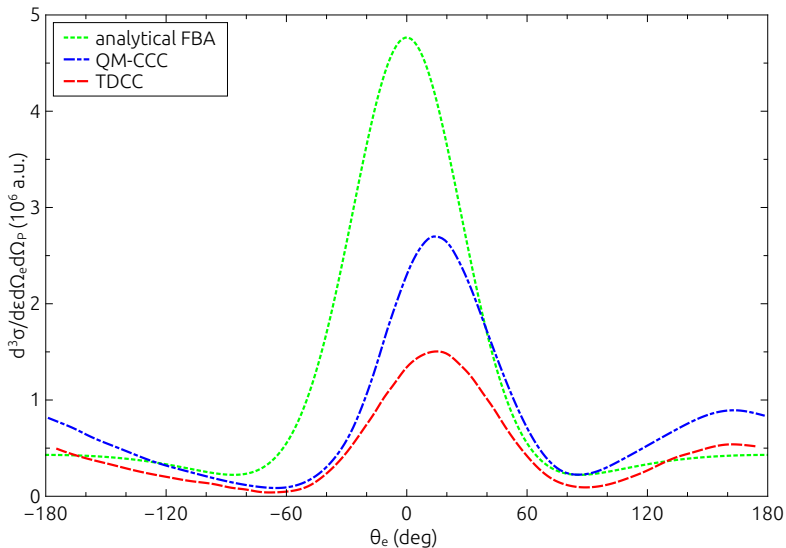
For details: A.I. Bondarev *et al.*, PRA **95**, 052709 (2017).

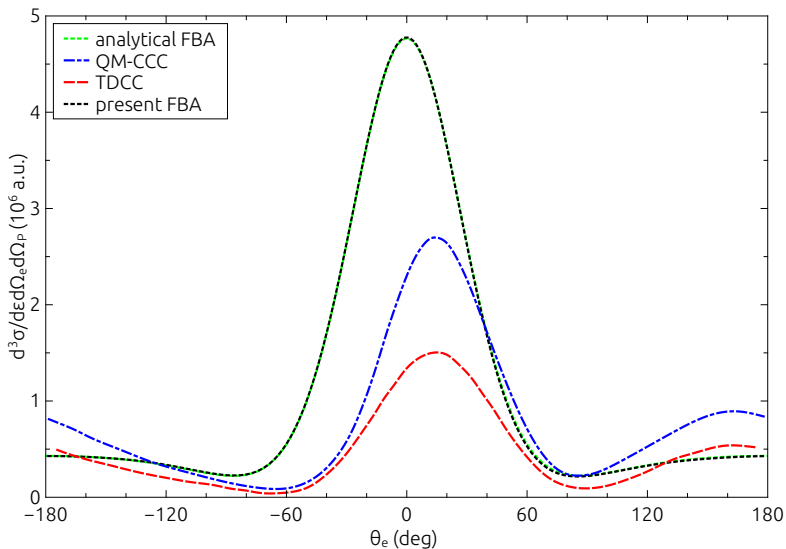
Antiproton-impact ionization of atomic hydrogen

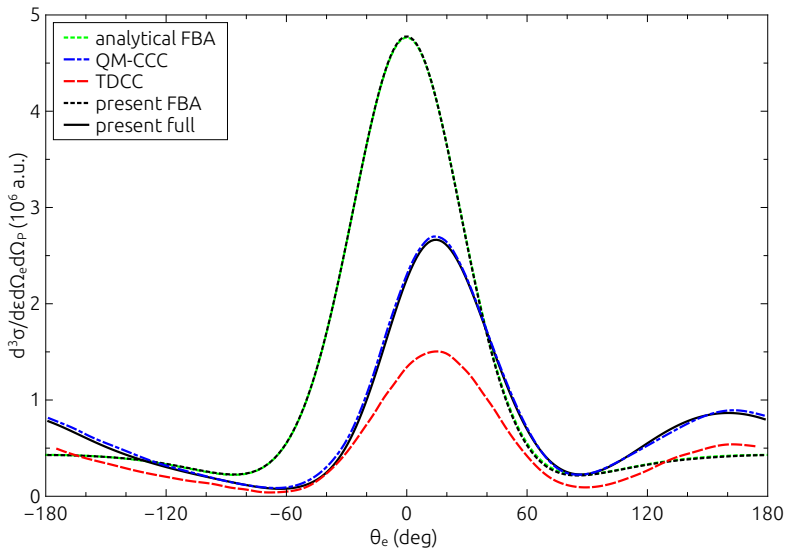
- A pure three-body system
- Absence of charge-transfer processes in contrast to proton-impact
- Absence of correlation effects in contrast to electron-impact
- Discrepancies in the recent predictions of **non-perturbative** approaches:

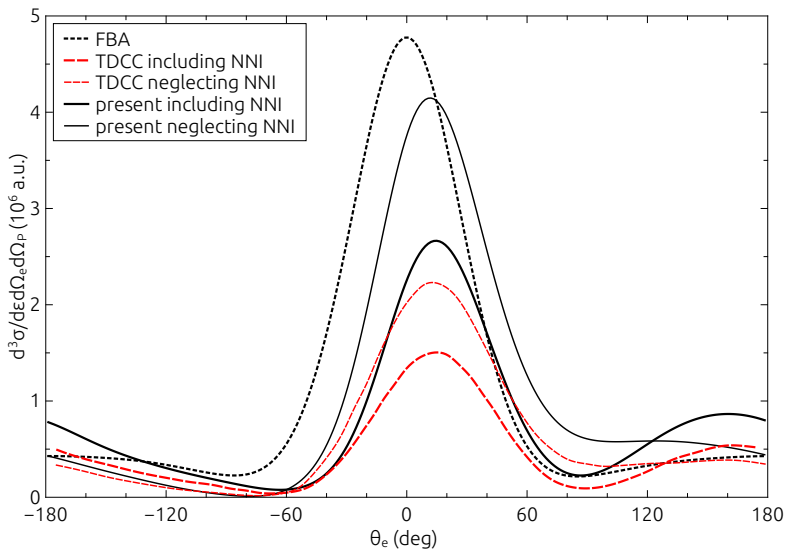
CP	—	M. McGovern <i>et al.</i> , PRA 79 , 042707 (2009),
QM-CCC	—	I.B. Abdurakhmanov <i>et al.</i> , JPB 44 , 165203 (2011),
TDCC	—	M.F. Ciappina <i>et al.</i> , PRA 88 , 042714 (2013),
WP-CCC	—	I.B. Abdurakhmanov <i>et al.</i> , PRA 94 , 022703 (2016).

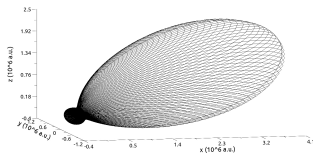
- Experimental data are unavailable at the moment

TDCS @ 200 keV for $\theta_p = 0.2$ mrad and $\varepsilon = 4$ eV

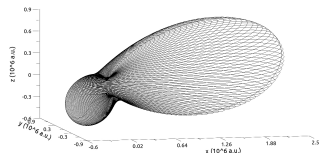
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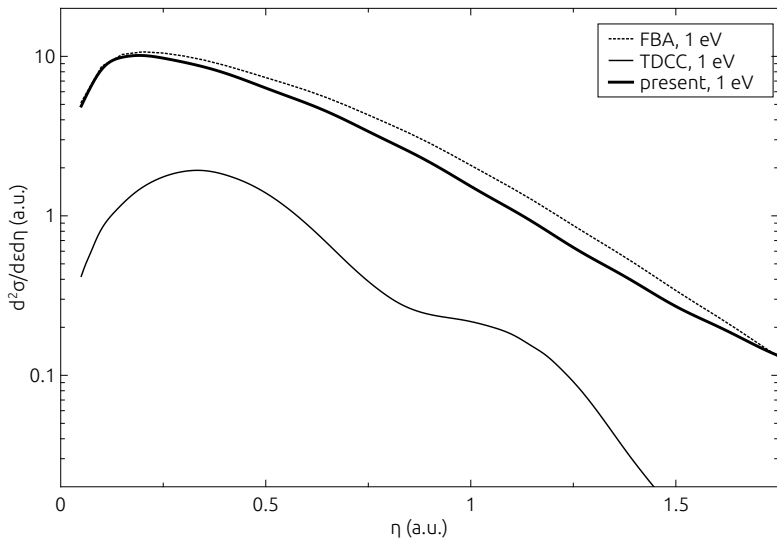
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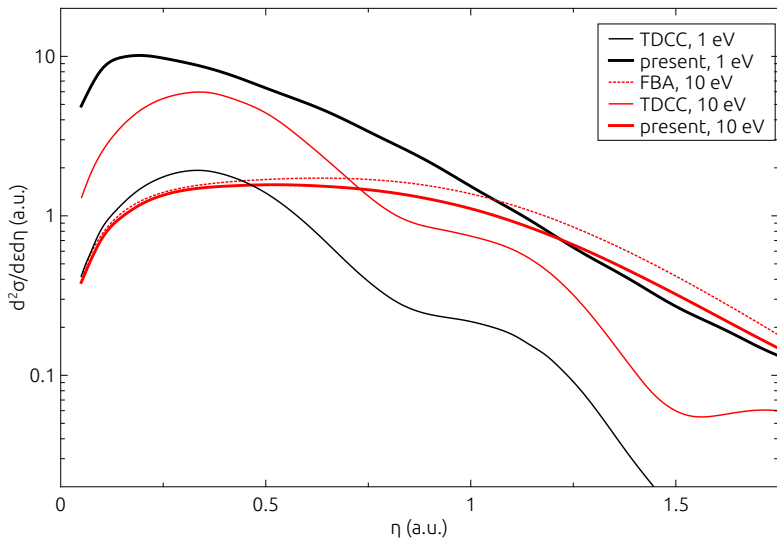
TDCS @ 200 keV for $\theta_p = 0.2$ mrad and $\varepsilon = 5$ eV

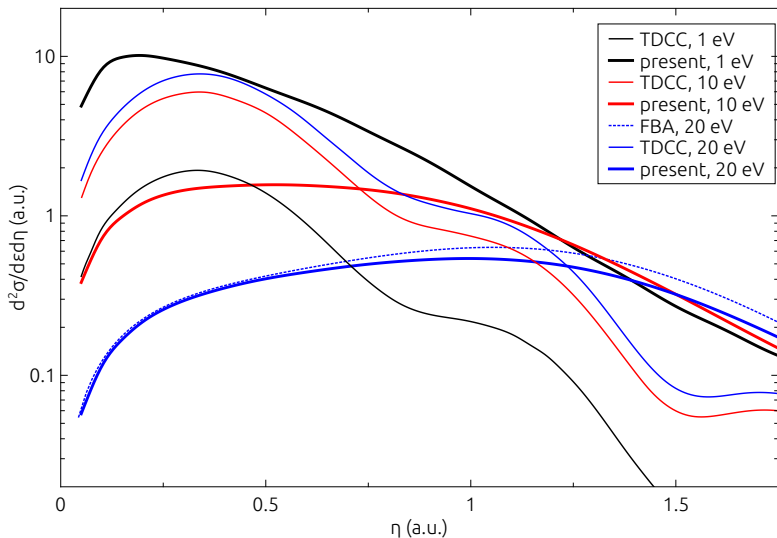
(a) FBA

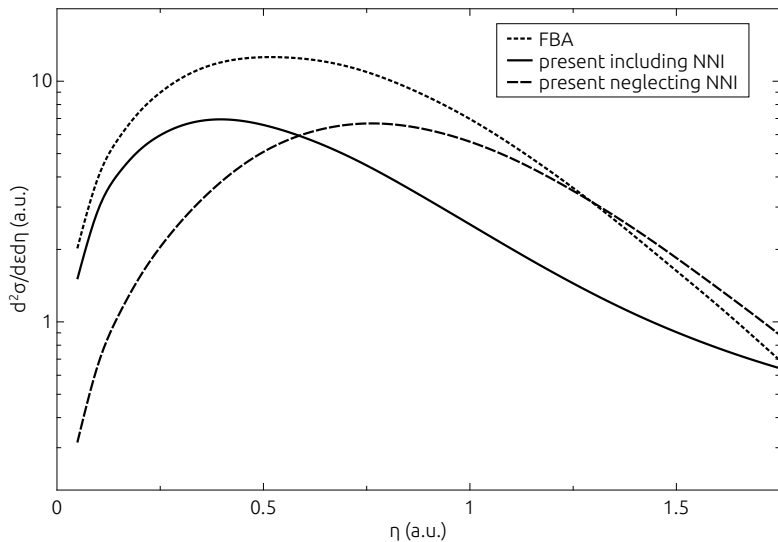


(b) full calculation

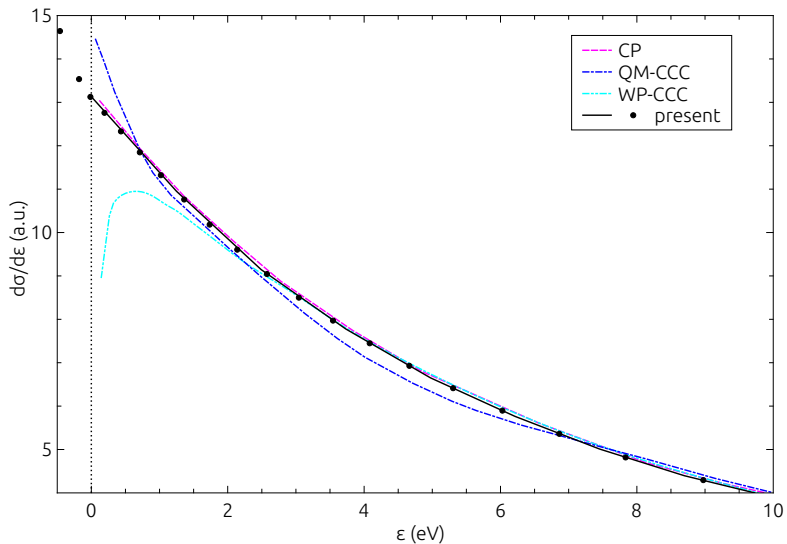
DDCS @ 200 keV for $\varepsilon = 1$ eV

DDCS @ 200 keV for $\varepsilon = 1$ and 10 eV

DDCS @ 200 keV for $\varepsilon = 1, 10$ and 20 eV

DDCS @ 30 keV for $\varepsilon = 5$ eV

SDCS @ 30 keV



Total ionization cross sections

Table 1 : Total ionization cross sections (10^{-16} cm^{-2}).

E_P (keV)	30.00	200.00	500.00
FBA	2.15	0.77	0.36
present (FBA)	2.16	0.77	0.36
QM-CCC	1.35	0.66	0.34
TDCC	1.46	0.65	0.33
present (full)	1.37	0.68	0.35

Conclusion and Outlook

- Differential cross sections for ionization provide much more stringent test for theory than total ones: fine peculiarities can be smeared in the latter.
- Antiprotons at low and medium energies are interesting objects to be used as projectiles in kinematically complete experiments.
- Our recently developed approach can compete with prominent non-perturbative techniques.
- Further improvement and application of the approach to experimentally investigated collisions of heavy ions with atoms.

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Analogy with classical mechanics

- In classical mechanics (the result of the Mie theory for scattering of light is similar) DCS is given by

$$\frac{d\sigma}{d\Omega} = \frac{b}{\sin\theta} \left| \frac{db}{d\theta} \right|$$

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- Two types of singularities: the **rainbow** and **glory**

Solar glory from an airplane



Timeline

- 1984 Yu.N. Demkov and co-workers found special behavior of the DCS for backward scattering in **screened Coulomb attractive potential** and named it the **Coulomb glory**. At some energies of the incident particle there is a prominent **maximum** of the DCS in the **backward direction**;
- 2001 Quasi-classical calculations of the Coulomb glory phenomenon in antiproton-xenon collisions:
Yu.N. Demkov and V.N. Ostrovsky, J. Phys. B **34** L595 (2001).
- 2007 – 2010 **Quantum-mechanical relativistic** calculations of the Coulomb glory in antiproton-uranium collisions:
A.V. Maiorova et al., Phys. Rev. A **76**, 032709 (2007);
A.V. Maiorova et al., J. Phys. B **41**, 245203 (2008);
A.V. Maiorova et al., J. Phys. B **43**, 205006 (2010).

Scaled differential cross section

- For pure Coulomb potential DCS is given by the Rutherford formula

$$\frac{d\sigma_C}{d\Omega} = \left(\frac{Z}{4E}\right)^2 \frac{1}{\sin^4(\theta/2)},$$

and has a **minimum at $\theta = \pi$** .

- To describe the Coulomb glory quantitatively, let us introduce the **scaled** DCS,

$$\frac{d\sigma'}{d\Omega} = \left(\frac{4E}{Z}\right)^2 \frac{d\sigma}{d\Omega},$$

so that

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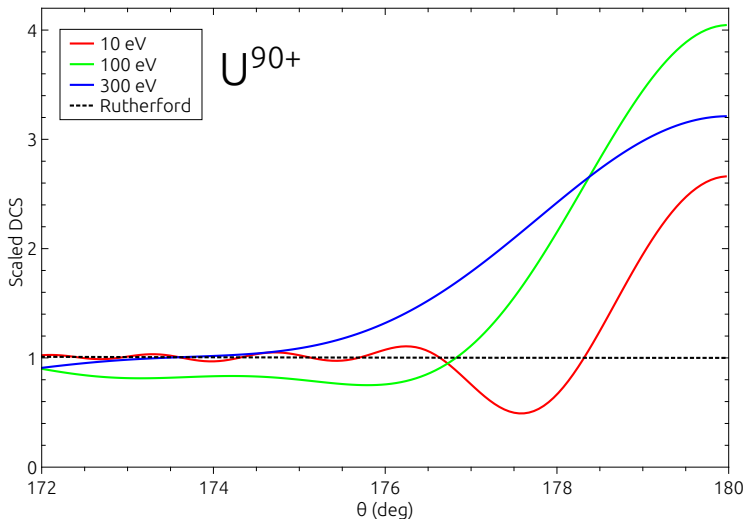
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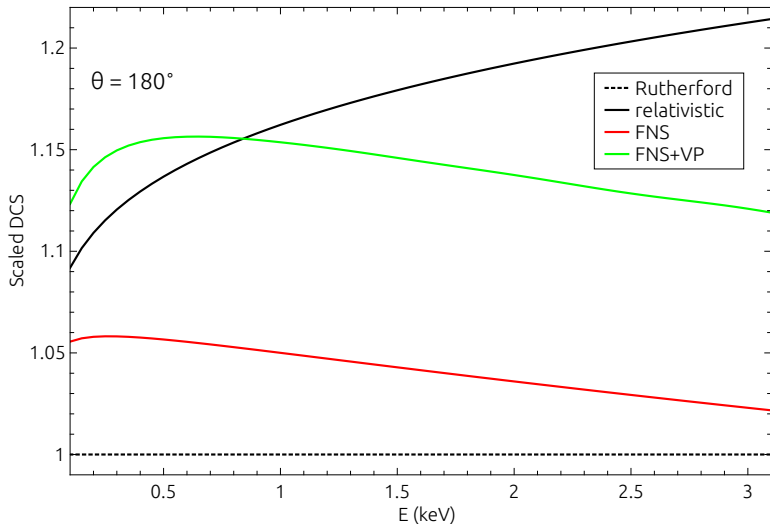
$$\frac{d\sigma'_C}{d\Omega} = \frac{1}{\sin^4(\theta/2)}.$$

Scaled DCS for antiproton scattering on uranium ions

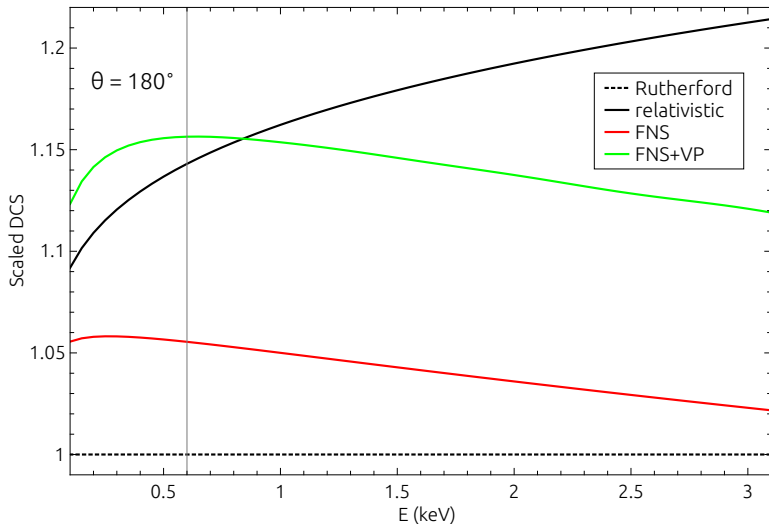


Maximal enhancement is 90 at $E = 300$ eV and 680 at $E = 1.8$ keV for U^{82+} and U^{64+} ions, respectively.

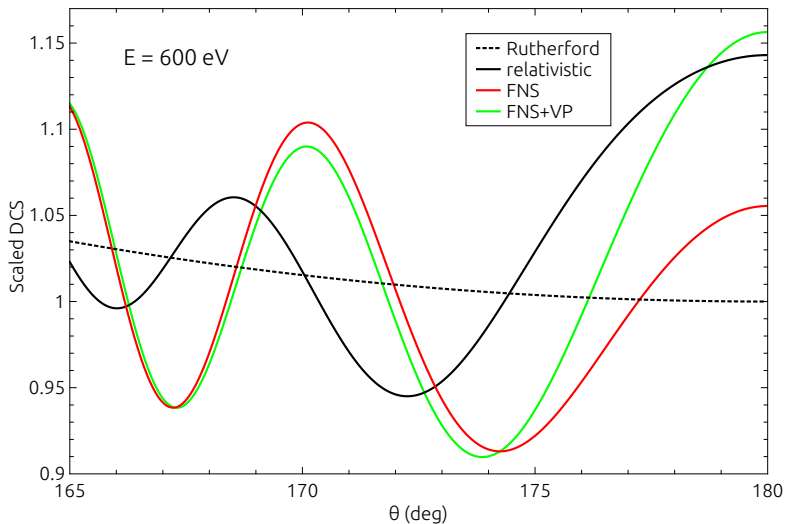
Scaled DCS for antiproton scattering on bare uranium



Scaled DCS for antiproton scattering on bare uranium



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Summary

- The backward scattering of antiprotons by ions is very sensitive to the screening potential. It provides a tool to study screening properties of the vacuum polarization potential in dynamical processes.
- The role of inelastic processes such as radiative recombination and antiproton annihilation has also been estimated. It is found that they should not mask the Coulomb glory phenomenon.

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- The role of inelastic processes such as radiative recombination and antiproton annihilation has also been estimated. It is found that they should not mask the Coulomb glory phenomenon.

Thank you for your attention!