

Karlsruhe Institute of Technology (KIT, Karlsruhe, Germany)

Institute for Beam Physics and Tehcnology,  
KIT, Karlsruhe, Germany



## **Non-linear beam dynamics studies at the Karlsruhe Research Accelerator KARA**

**The XXV European Synchrotron Light Sources Workshop, Dortmund, Germany 20-  
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A.Papash\* for THz and Accelerator team  
KIT, 76344, Karlsruhe, Germany

**[\\* alexander.papash@kit.edu](mailto:alexander.papash@kit.edu)**

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- 
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- **Marcel Schuh**, Markus Schwarz, Nigel J. Smale, **Johannes L. Steinmann**,
- Minjie Yan

\* **outlined** are people involved into Beam dynamics experiments

## Outline



- The IBPT of KIT operates the 2.5 GeV electron storage ring KARA (former ANKA) as an accelerator test research facility and synchrotron radiation source
  - Two high field superconducting wigglers (CLIC=3T and CATACT=2.5 T) are installed in the ring straights. While CLIC is located in the LONG straight section with small vertical beta-function ( $\approx 0.5$  m) the CATACT wiggler is displaced in short straight where vertical beta-function is large ( $\approx 13$  m)
  - The lifetime of the electron beam degraded from  $\sim 15$  hours to  $\sim 12$  h at high level of CATACT wiggler field even though the coherent shift of vertical tune was compensated locally
  - Computer simulations show non-linear nature of the effect --
    - 1) Strengths of chromatic sextupoles are strong in order to operate ring at high positive chromaticity
    - 2) Residual octupole components of wiggler field, even at tolerance level, reduce the dynamic aperture for particles with momentum offset;
    - 3) At high chromaticity the betatron tune for off-momentum particles shifts toward weak octupole resonance. As a consequence, particles from beam halo are lost with higher probability and life time is reduced
    - 4) vertical betatron tune WAS in vicinity of sextupole resonance  $Q_y=8/3$ . Large resonance stop-band and proximity to  $Q_y=2.667\dots$  harmed lifetime, beam stability during injection and ramp
- CURE**
- Working point of ring has been shifted away from suspected high-order resonances and beam lifetime as well as stability at injection, ramp and plateau were essentially improved
- MORE**
- Reduced compaction factor settings at high vertical tune have been implemented and successfully tested

# Model of KARA ring created in OPA\*

CATACT - short straight section      CLIC - long straight section

## RING

E = 2.5 GeV      |      B·R = 8.33 T·m  
 4-fold symmetry      |      L = 110.4 m  
 Long/short straight sections 5.604 / 2.236 m

## Bends (16)

B = 1.5 T      L=2.183 m,  
 Bending angle  $\theta=22.5^\circ$ ,  
 Bending radius  $R=5.559$  m  
 Parallel edges  $\theta_1=\theta_2=11.25^\circ$   
 Gradient  $G=0$  (flat)      |      Vertical gap=40 mm  
 Pole width =160 mm      |      Field index = 0  
 Current = 900 A      |       $N \cdot I = 54 \text{ kA} \times \text{Turns}$   
 Power=23.5 kW

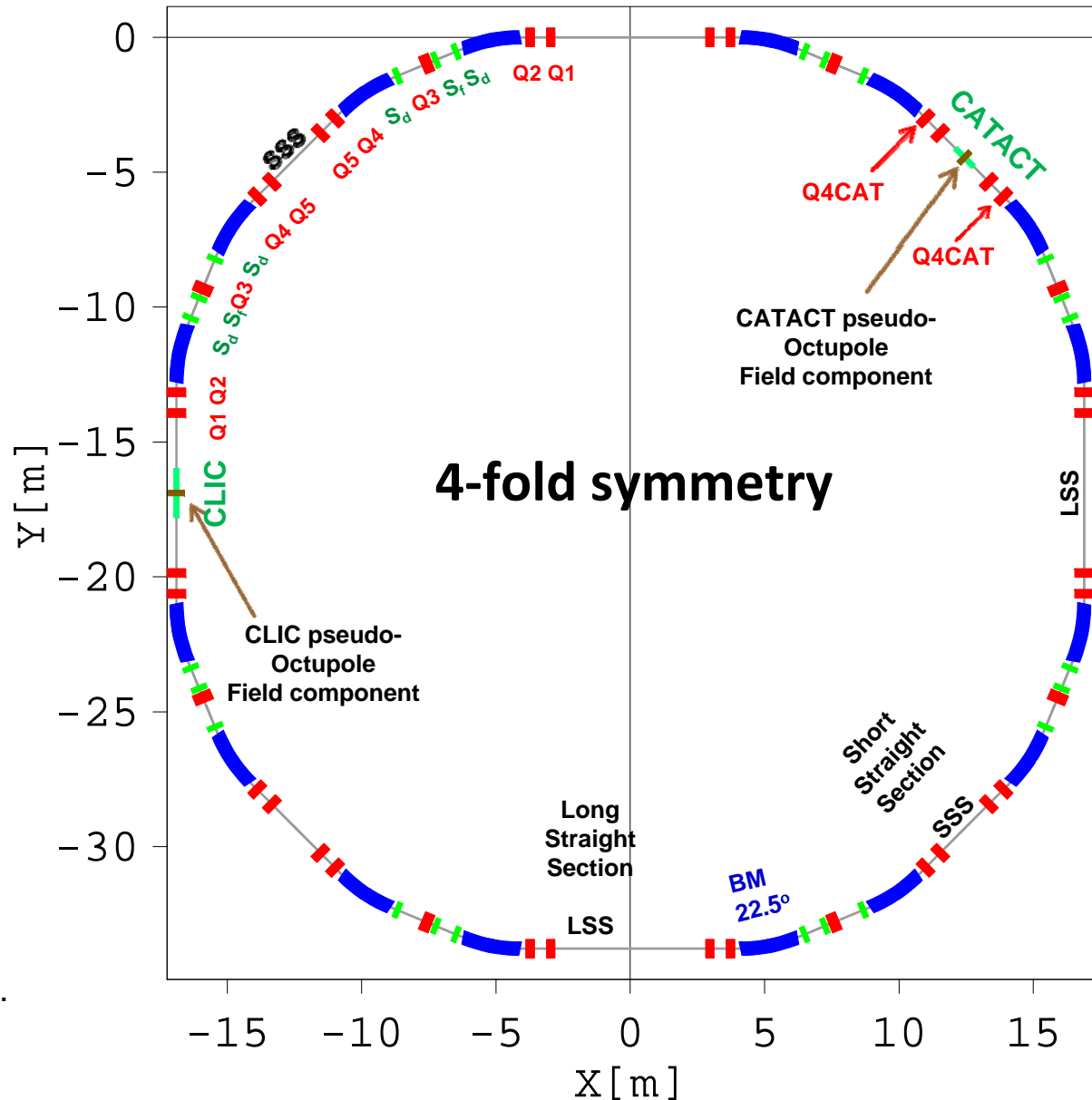
## Quads (32 + 8)

Aperture  $\varnothing = 70$  mm  
 Length LQ1,2,4,5=0.32 / 0.35 m (iron/eff)  
 Length LQ3=0.39 / 0.42 m (iron/eff)  
 Gradient  $\partial B / \partial R \leq 22 \text{ T/m}$   
 Strength  $k = (1/BR) \cdot (\partial B / \partial R) \leq 2.6 \text{ m}^{-2}$

## Sextupoles (16+8)

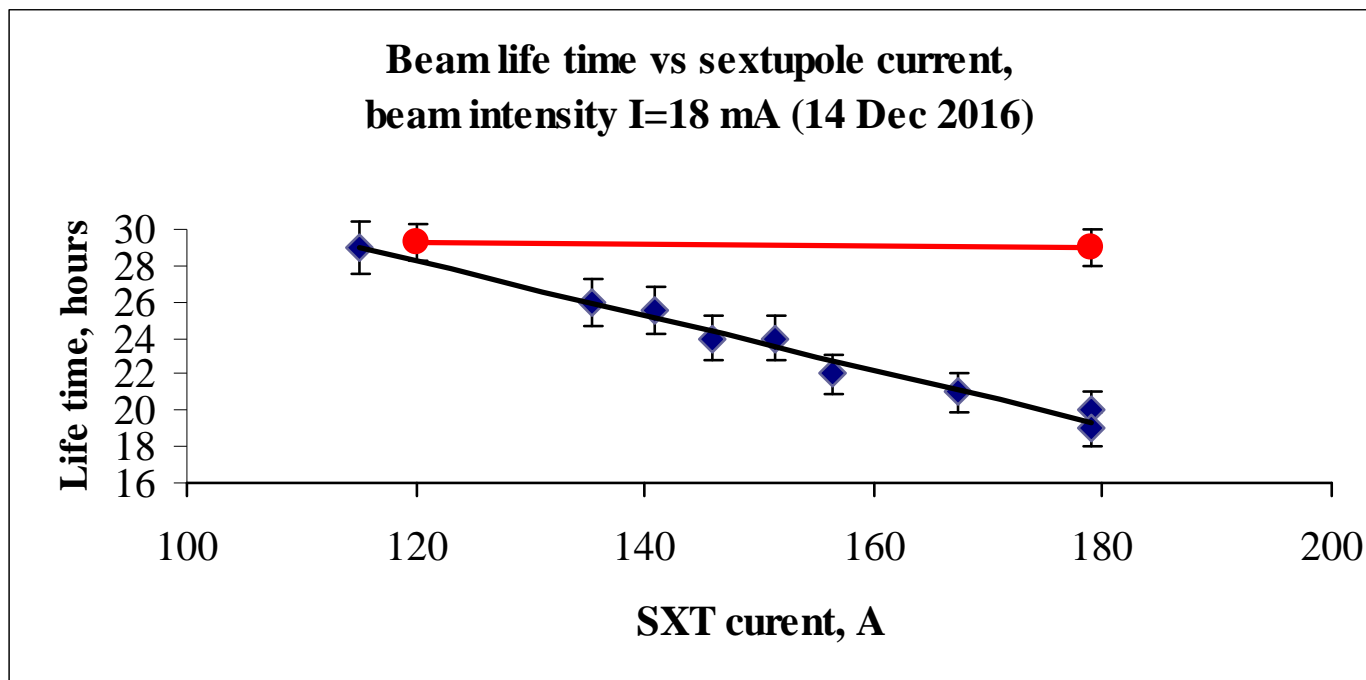
Aperture  $\varnothing = 75$  mm  
 SXT Grad       $G_s = \partial^2 B / \partial R^2 \leq 800 \text{ T/m}^2$   
 SXT Str.       $k_s = (1/BR) \cdot (\partial^2 B / \partial R^2) \leq 90 \text{ m}^{-3}$   
 SXT Length       $L_s = 0.12$  m  
 SXT Integr strength       $k_s \cdot L_s \leq 10 \text{ m}^{-2}$

\* A.Streun. Computer code OPA.  
 Version 3.81. SLS Design note. 2016.



# Life time measurements.

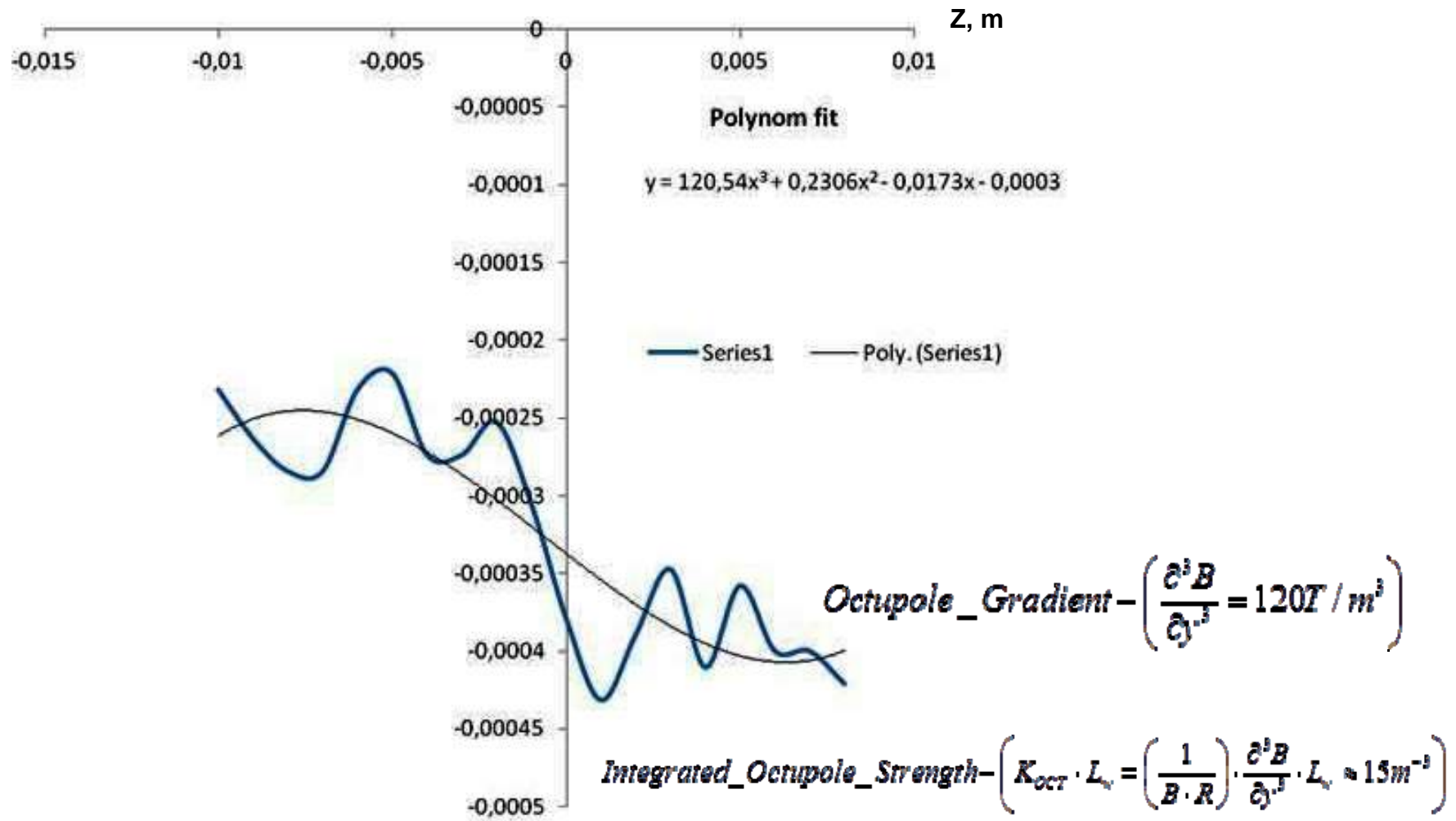
**E=2.5 GeV. Original tune  $Q_y=2.69$**



Life time (hours) as function of current of vertical sextupole.  
**I=18 mA.** ANKA tests 15 Dec 2016

**Red** – CATACT is OFF.  
**Black** – CATACT=2.5 T.

## High order magnetic field components of CATACT (measured)



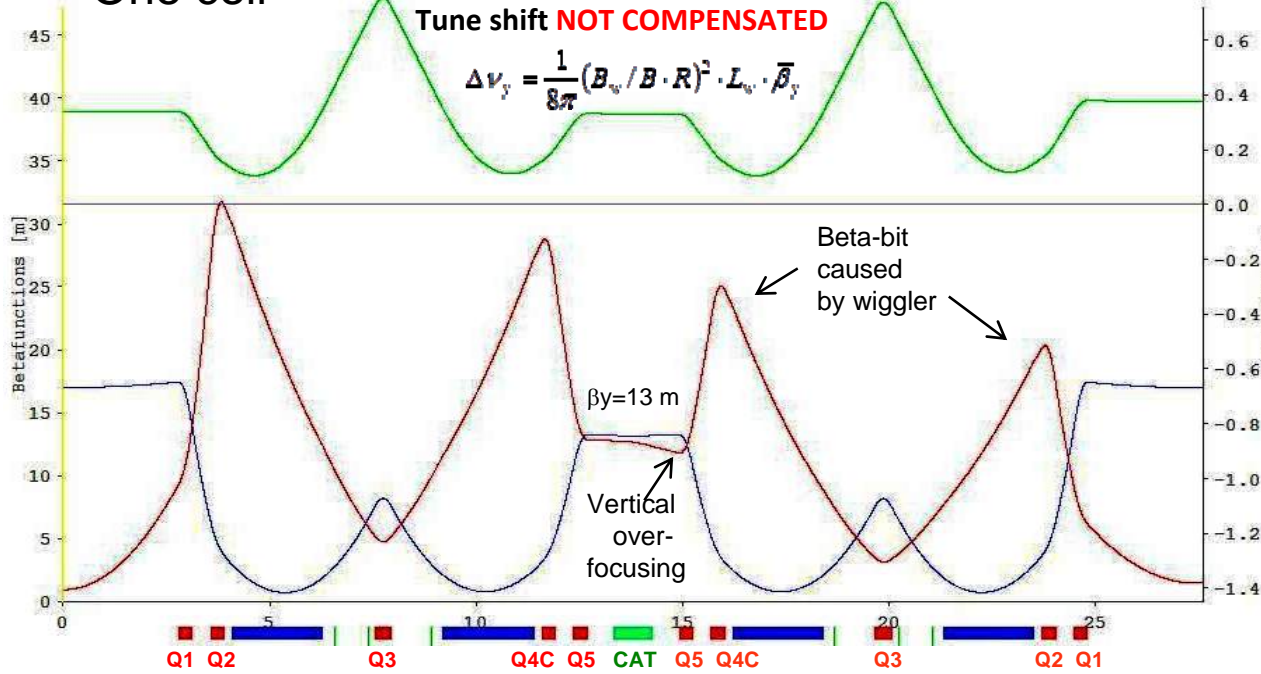
Integrated Octupole gradient of CATACT wiggler measured during BINP on-site tests does not exceed tolerances set by design specifications

$$GR\_OCT \cdot L \approx 100 T/m^2$$

# One cell

CATACT Wiggler field B=2.5 T.  
Tune shift **NOT COMPENSATED**

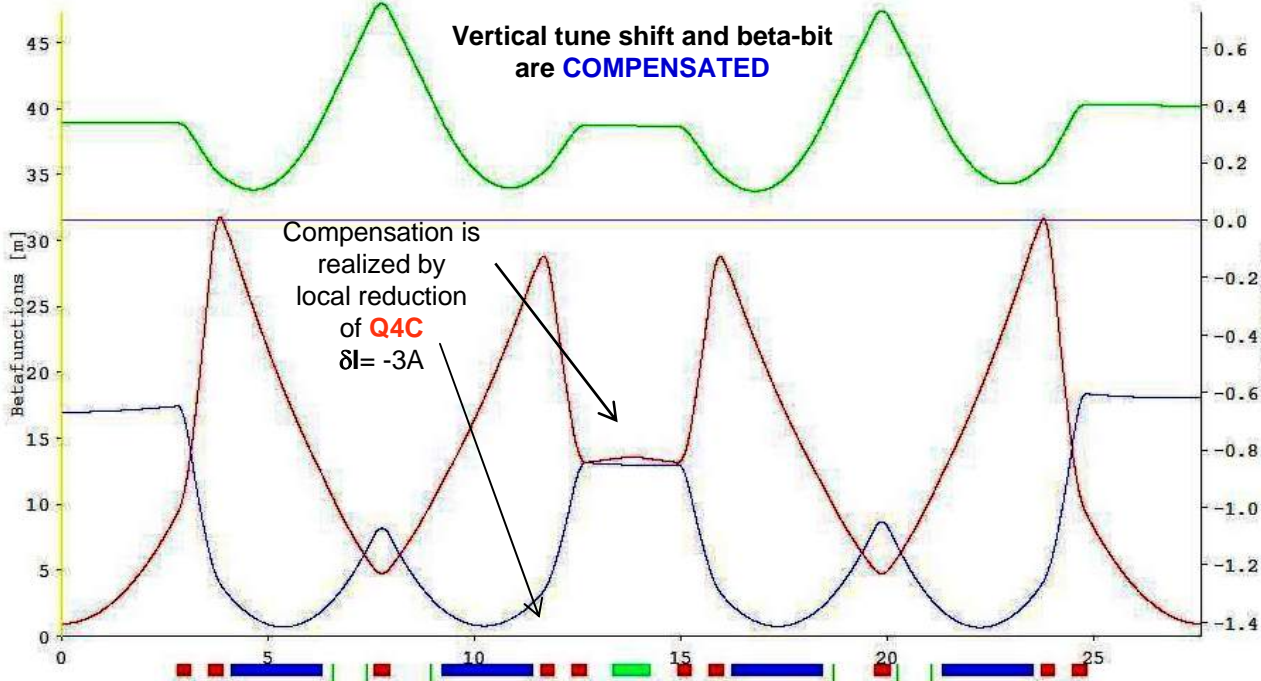
$$\Delta \nu_y = \frac{1}{8\pi} (B_w / B \cdot R)^2 \cdot L_w \cdot \bar{\beta}_y$$



CATACT cell  
STR Q4CAT = -1.82 m<sup>-2</sup>  
**Qy(CAT\_cell) = 0.7177**  
Qx (CAT-cell)=1.6889

Regular cell  
STR Q4 = -1.82 m<sup>-2</sup>  
**Qy(reg\_cell) = 0.6720**  
Qx (reg-cell)=1.6888

Vertical tune shift and beta-bit  
are **COMPENSATED**



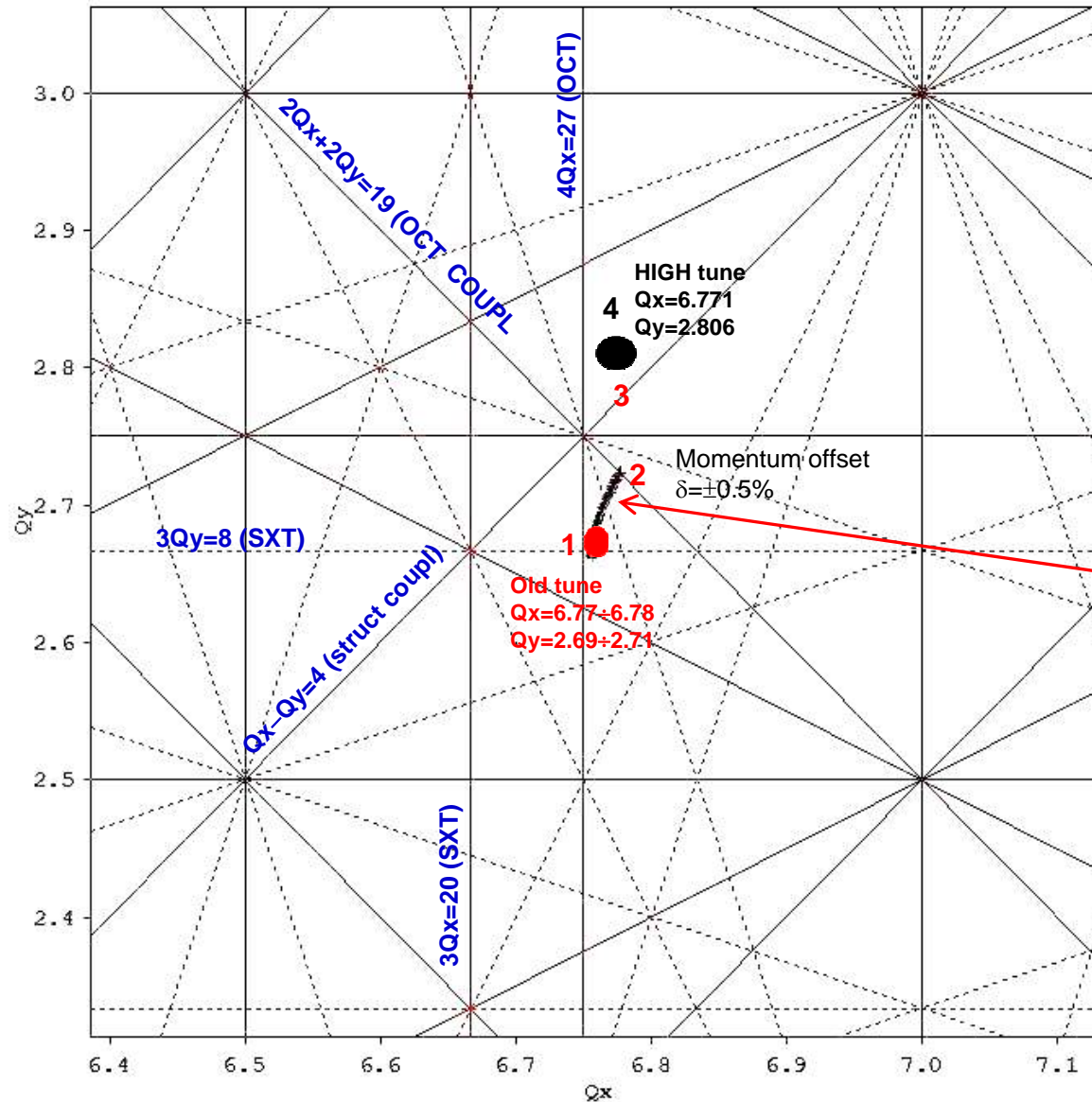
Regular cell  
Q4 STR = -1.82 m<sup>-2</sup>  
**Qy(reg\_cell) = 0.6720**  
Qx (reg-cell)=1.6889

CATACT cell  
Q4CAT STR=-1.79155 m<sup>-2</sup>  
**Qy(CAT\_cell) = 0.6720**  
Qx (CAT-cell)=1.6964

I(Q4) ≈ -196 A    δI = -3 A



# Tune diagram of KARA ring



**RED spot (1)** – original betatron tune

**BLACK spot (4)** – high betatron tune

Ring operation at old tune suffered from proximity to SXT resonance  $Q_y = 8/3$  (2,667) and coupling octupole resonance excited by CATACT wiggler at high field level (2 ÷ 2.5 T).

At the same, the ring operates at **high positive chromaticity** to avoid HEAD-TAIL instability.

**Tune shift at HIGH CHR $x,y = +2/+6$  push OFF-MOMENTUM particles towards high order resonances (2) driven by residual octupole comp. of CATACT field. Particles with momentum offset cross OCT RES (2)**

Ring Operation at reduced chromaticity (+1,+1) AND at High vertical tune ( $Q_y = 2.81$ ) does not affected by sextupole either octupole resonances.

**The life time of beam at high tune (4) was restored to nominal value and even improved**

Tune diagram – up to 4<sup>th</sup> order incl. Skew resonances

**1** – unstable operation close to SXT resonance  
Strong sextupoles create Large stop-band of resonance

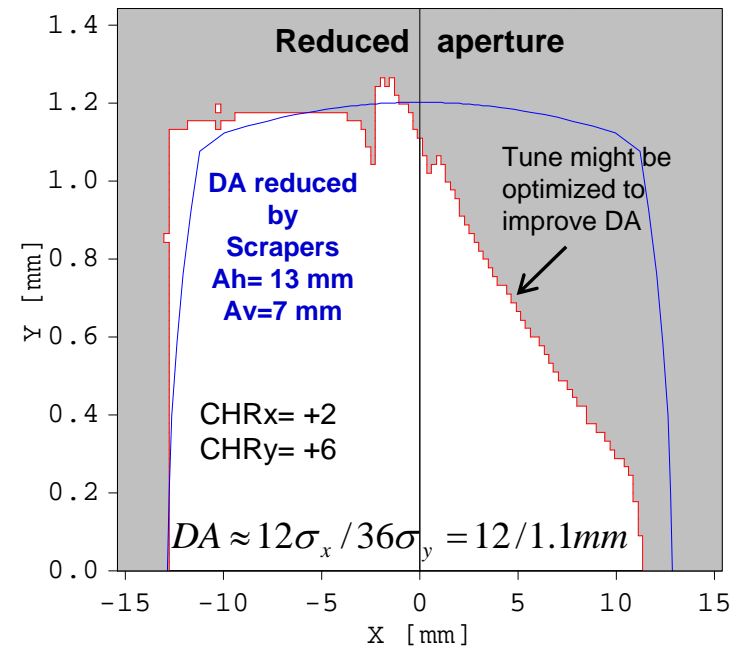
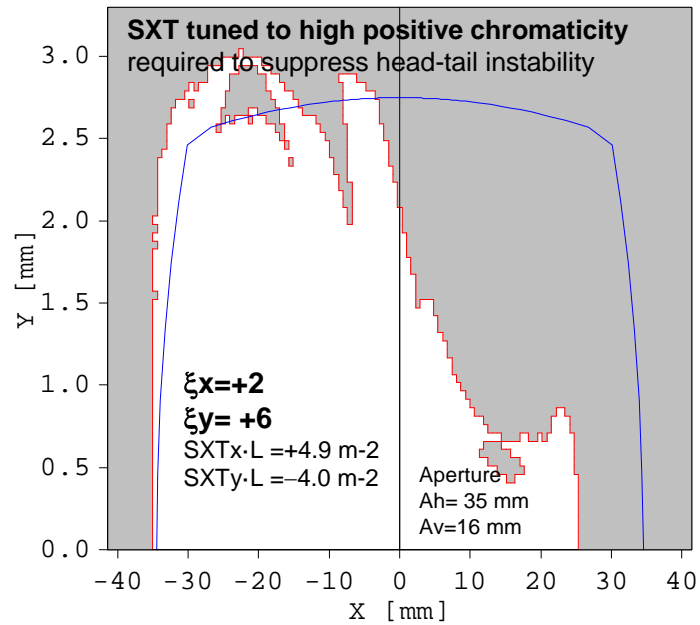
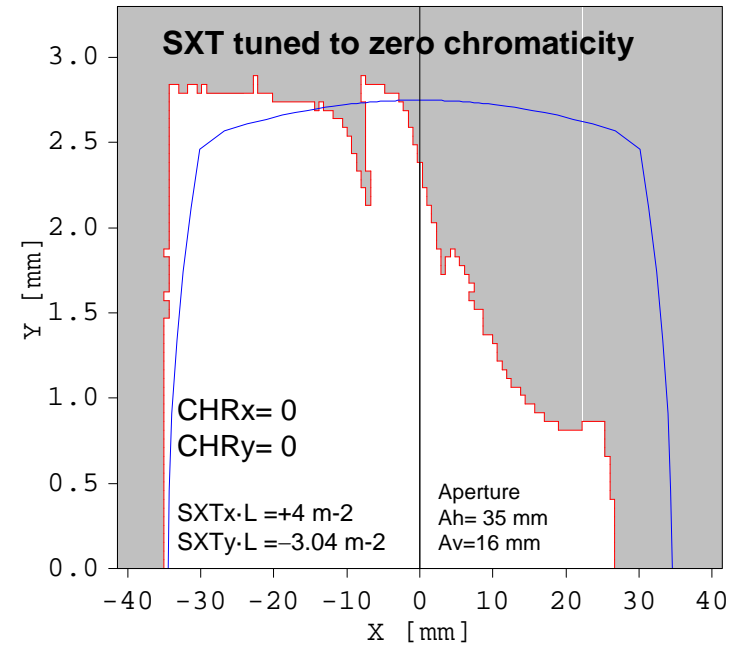
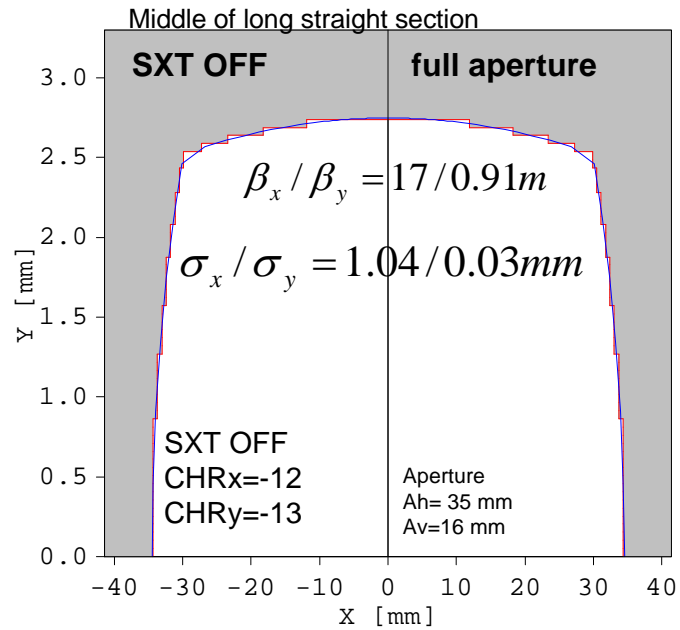
**2** – reduced life time  
Cross coupl Oct Res excited by CATACT at high field level

**3** -- Reduction of life time  
Cross coupl Str res  $Q_x - Q_y = 4$  excited by field Errors & misalignments of quads



**Dynamic Aperture of KARA ring  
and  
effects of high order components  
of  
residual field  
of  
CATACT wiggler**

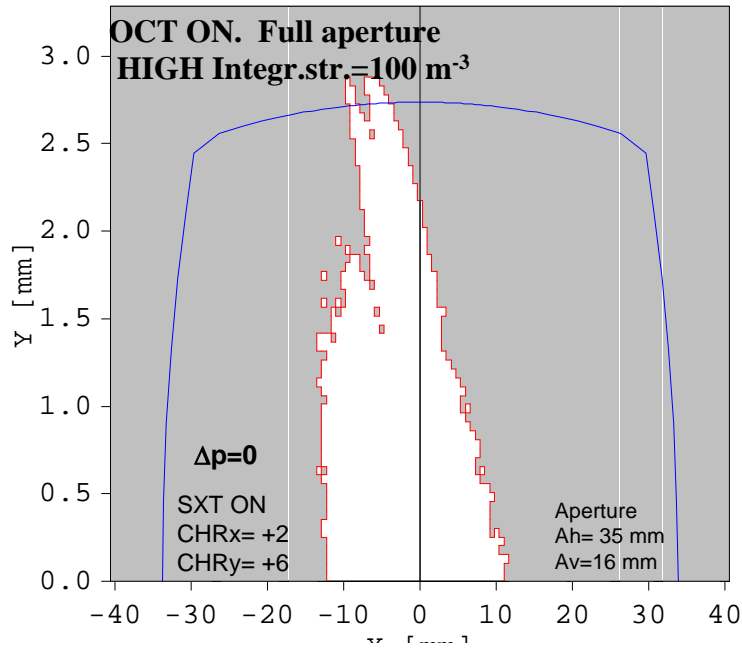
# Dynamic Aperture (DA). Original tune $Q_y=2.69$ . Wigglers OFF



# Dynamic Aperture for ON momentum particles. OLD tune $Q_y=2.69$ . Wiggler $B=2.5$ T

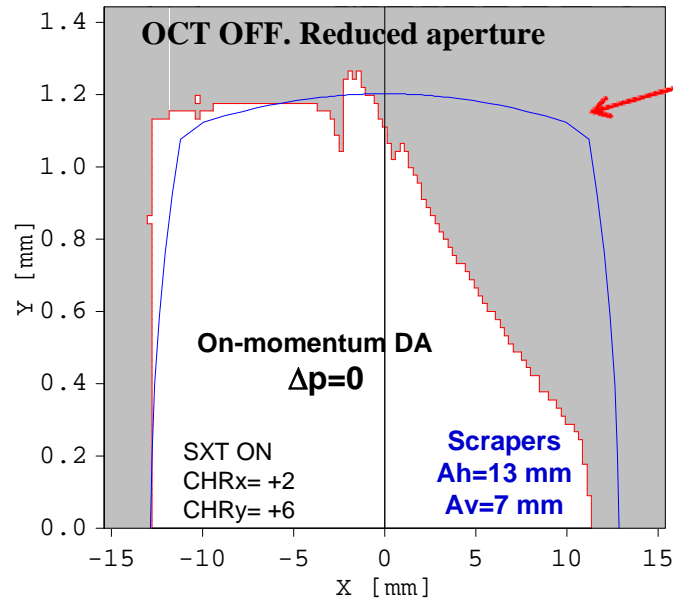
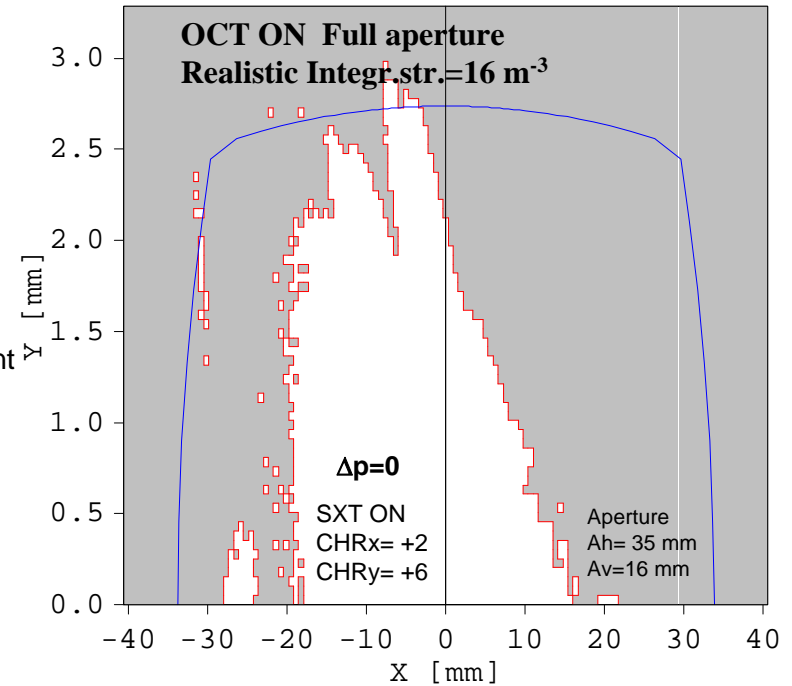
$$\text{Integrated\_Octupole\_Strength} - \left( K_{OCT} \cdot L_w = \left( \frac{1}{B \cdot R} \right) \cdot \frac{\partial^3 B}{\partial y^3} \cdot L_w \approx 15 m^{-3} \right)$$

On-momentum DA  $\Delta p=0$



Octupole field drastically reduces Dynamic Aperture (and life time) due to ADTS if beam is wide ( $\Delta X > 15$  mm) - even at WEAK (RESIDUAL) OCTUPOLE component

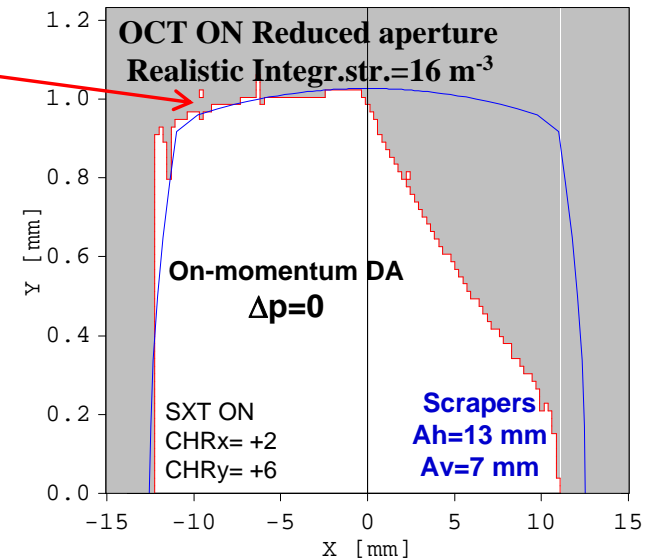
On-momentum DA  $\Delta p=0$



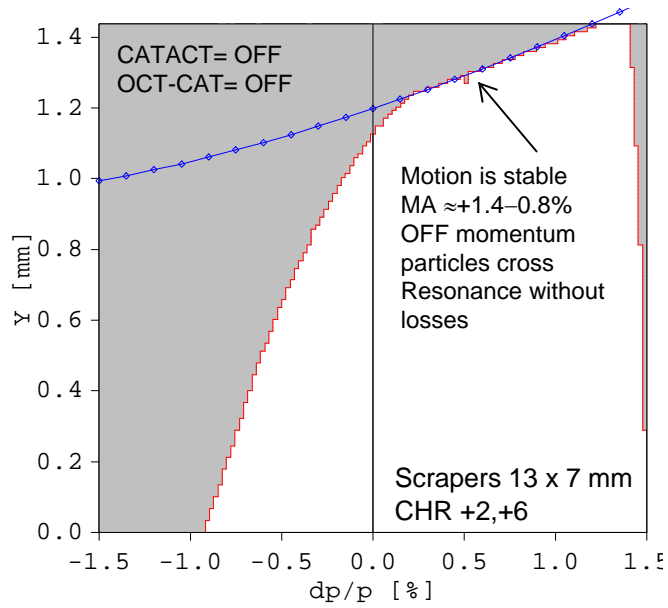
If ring DA is restricted by scrapers

The effect of residual OCTUPOLE component of CATACT field is NOT VISIBLE for ON-momentum particles

**BUT !**

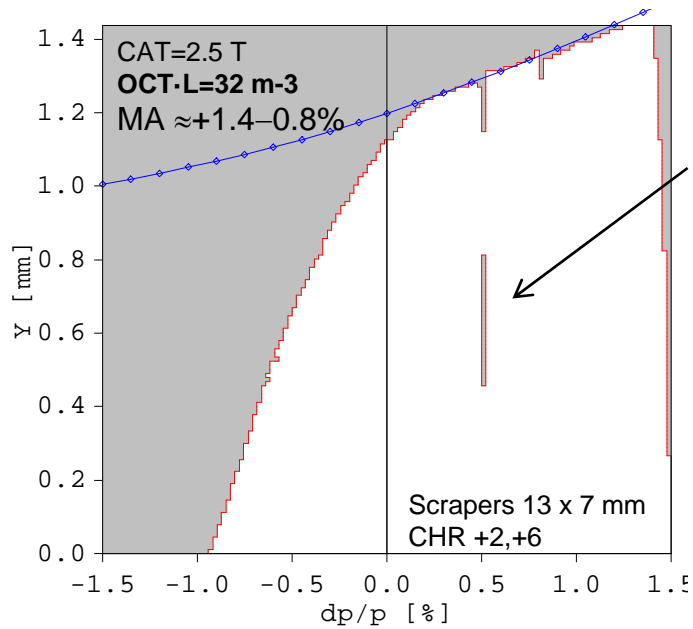
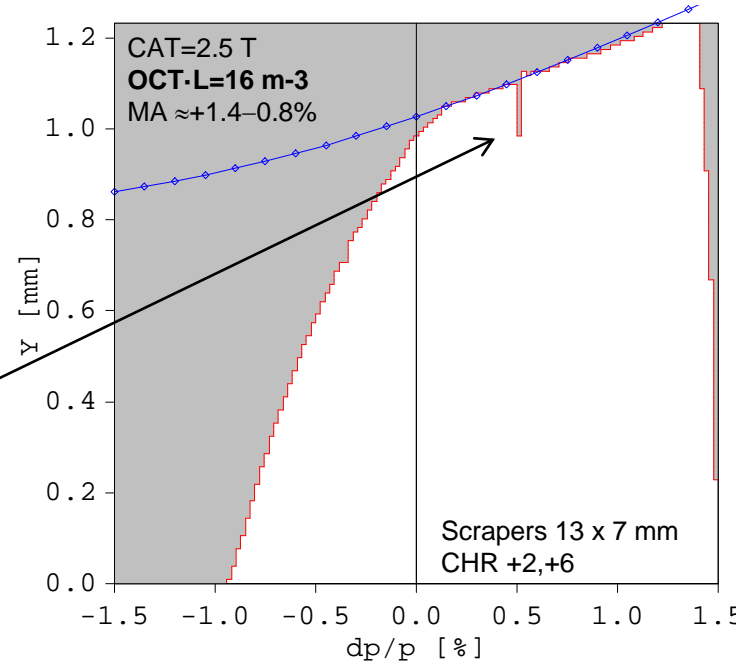


# Momenutm acceptance. Original tune $Q_y=2.69$ Wiggler field $B= 2.5$ T.



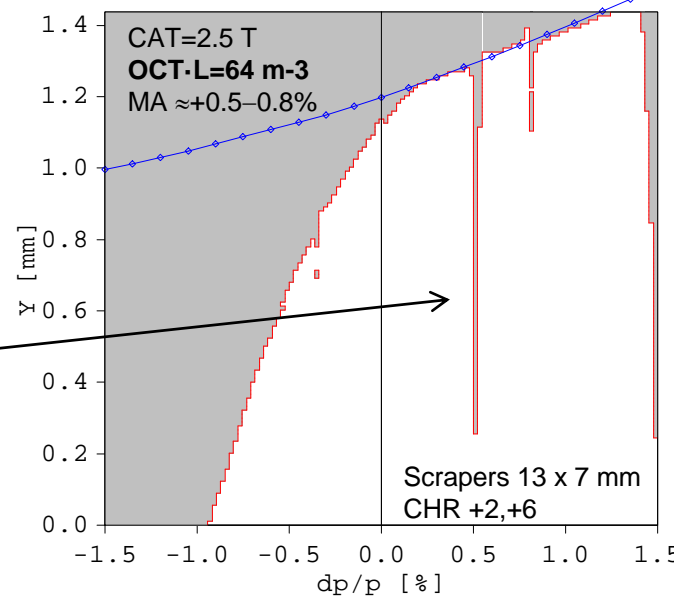
Resonance  
 $2Q_x+2Q_y=19$   
for OFF-Momentum  
particles  $\delta p/p \approx +0.5\%$   
driven by octupole  
appears

Octupole strength  
does not exceed  
tolerance set  
on CATACT wiggler

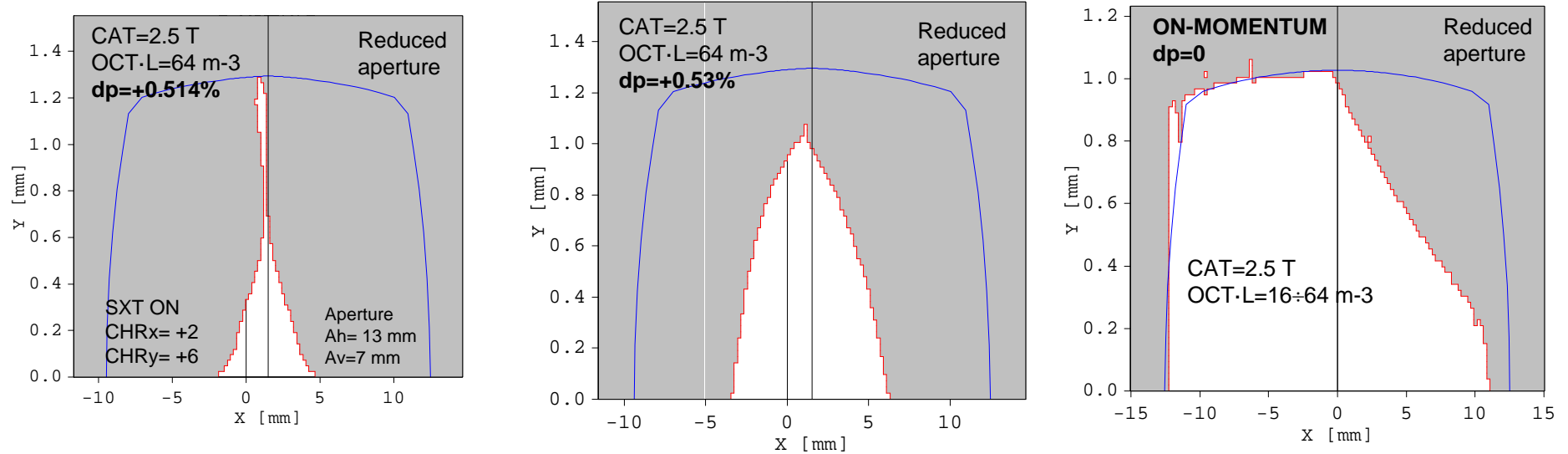


Resonance  
 $2Q_x+2Q_y=19$   
for OFF-Momentum  
particles  $\delta p/p \approx +0.5\%$   
driven by octupole  
grows

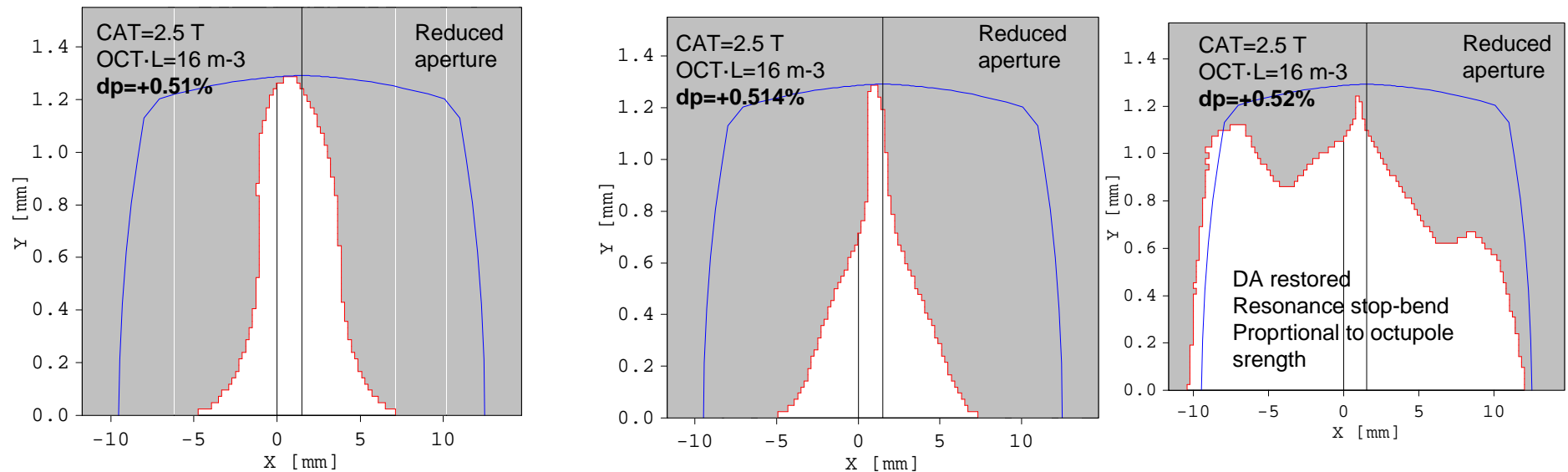
Resonance  
 $2Q_x+2Q_y=19$   
for OFF-Momentum  
particles  $\delta p/p \approx +0.5\%$   
driven by octupole  
SHRINKS DA to < 0.2 mm



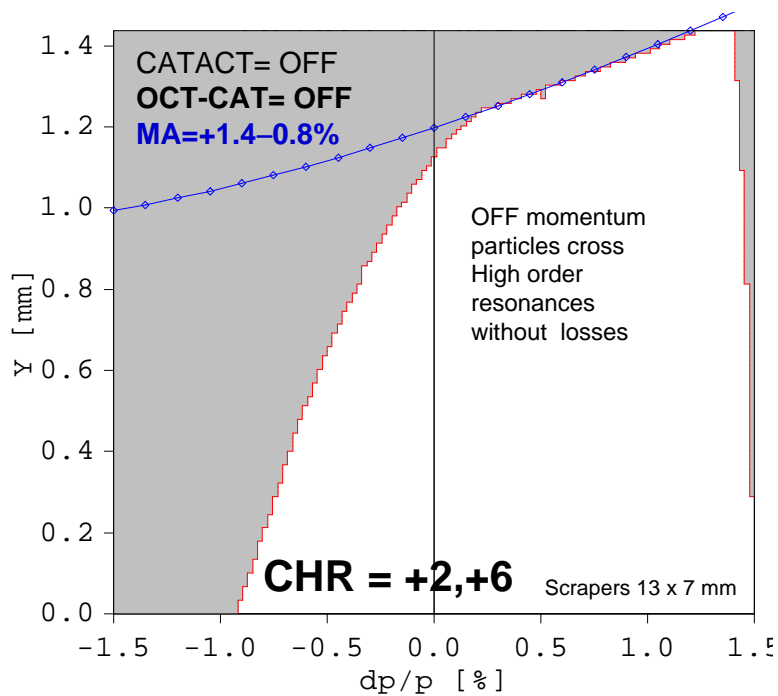
# Dynamic Aperture at different momentum offset. OLD tune $Q_y=2.69$ . Wiggler field $B=2.5$ T



Providing the strength of Octupole component exceeds tolerance in few times the OFF –momentum DA might shrink to Zero and beam might be LOST. Life time in ANKA is defined by Touschek inelastic scattering with large momentum deviation at high beam current and inelastic scattering on residual gas on large momentum offset  $\geq \pm 1\%$  (ANKA MA is measured as  $\pm 1\%$ ). Providing the OCTUPOLE resonance appears at dp=0.5% the off-momentum DA shrinks but not to ZERO, Thus MA and life time should be reduced



## Effect of Chromaticity reduction to improve momentum acceptance (old tune). Wiggler B=2.5 T.

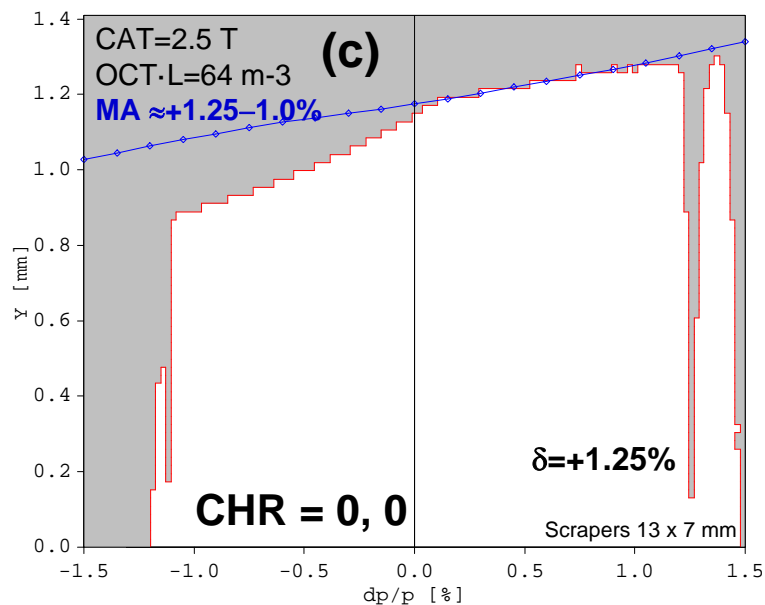
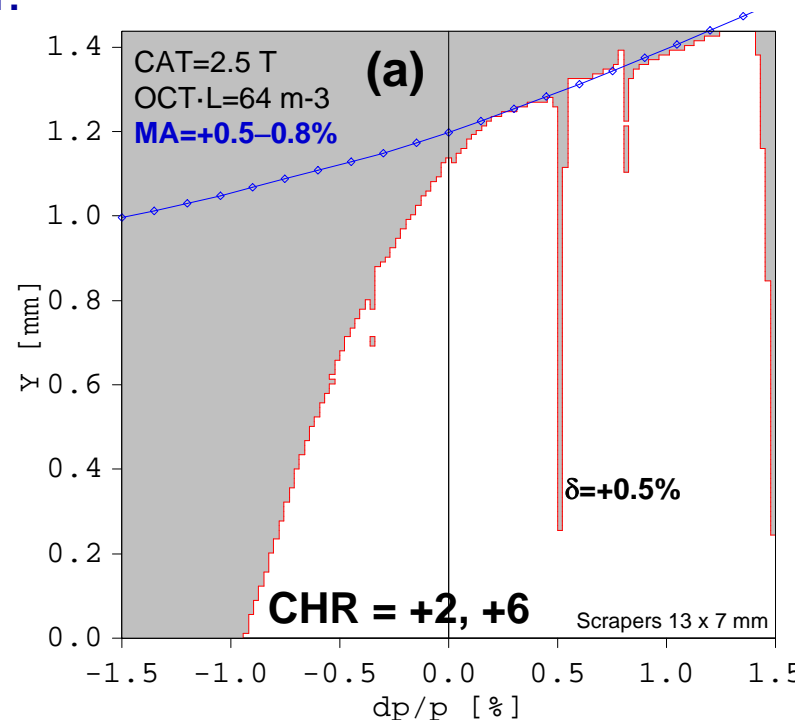


Resonance  
 $2Q_x + 2Q_y = 19$   
Driven by octupole  
Component of CATACT  
shrinks DA for particles  
with momentum offset

(a)  $\delta p/p = +0.5\%$   
CHR = +2, +6

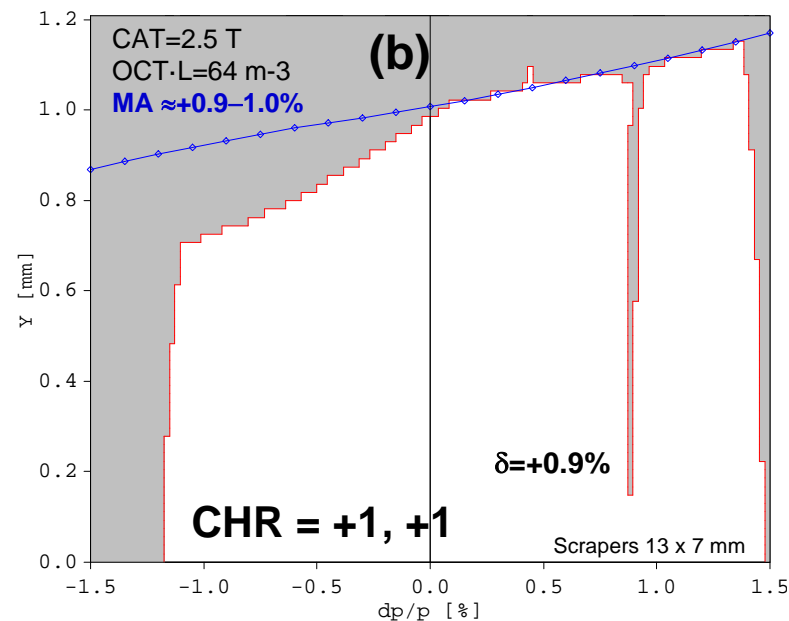
(b)  $\delta p/p = +0.9\%$   
CHR = +1, +1

(c)  $\delta p/p = +1.24\%$   
CHR = 0, 0

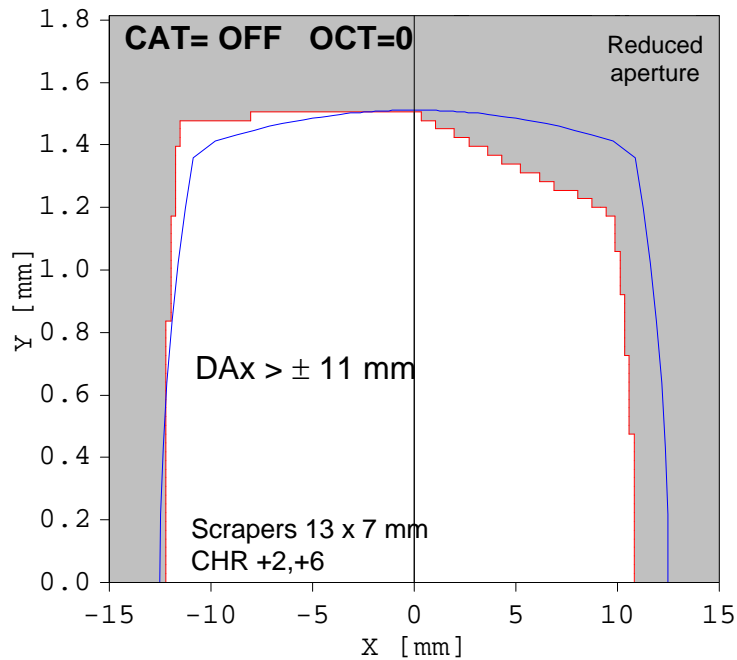


Momentum offset of  
resonance is shifted off  
reference energy while  
Chromaticity is reduced

The life time might be  
RESTORED by reducing  
of Chromaticity  
at 2.5 GeV and  
Feedback ON  
while CATACT  
at top field level  
B=2.5 T



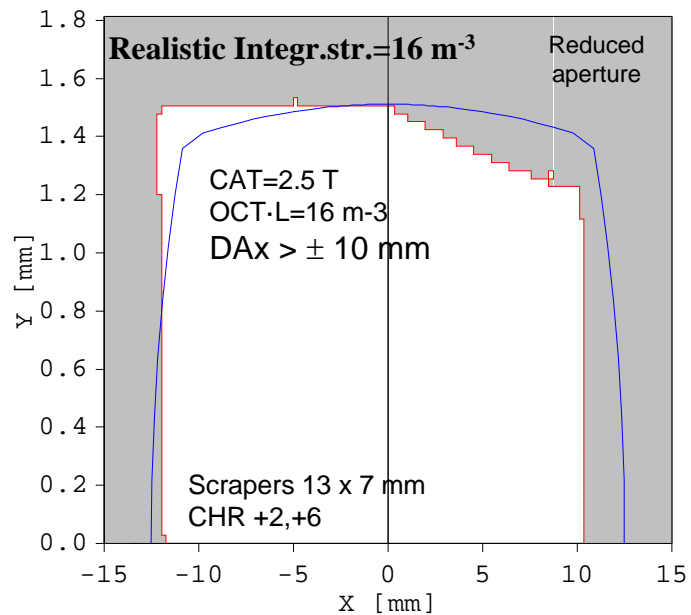
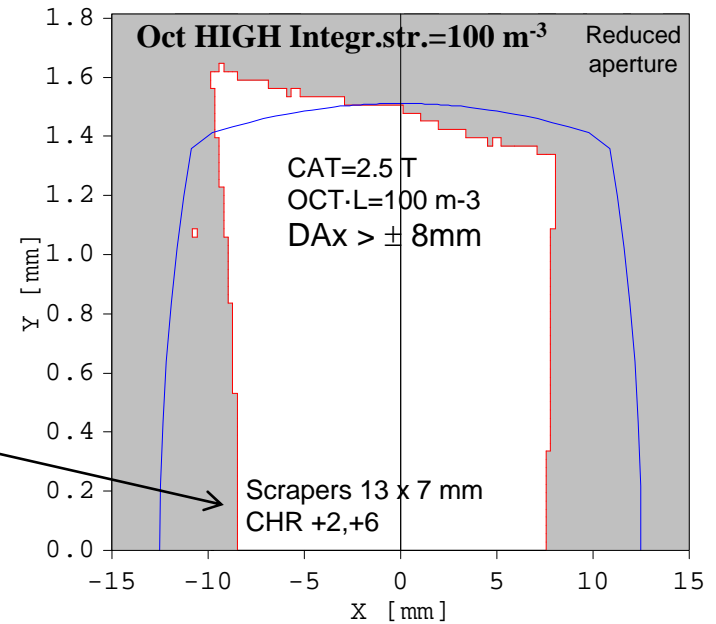
# Dynamic Aperture. HIGH tune $Q_y = 2.81$ CATACT Wiggler ON. $B = 2.5$ T



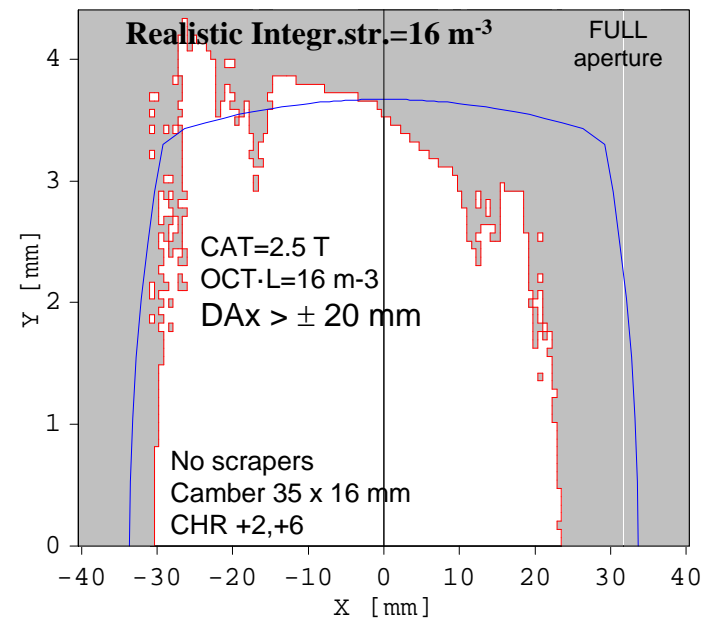
**High tune**  
 $Q_y = 2.81$

Life time might be  
Slightly reduced  
at high integr. octupole  
Strength  $> 100$  m-3

$$\sigma_x / \sigma_y = 1.04 / 0.03 \text{ mm}$$

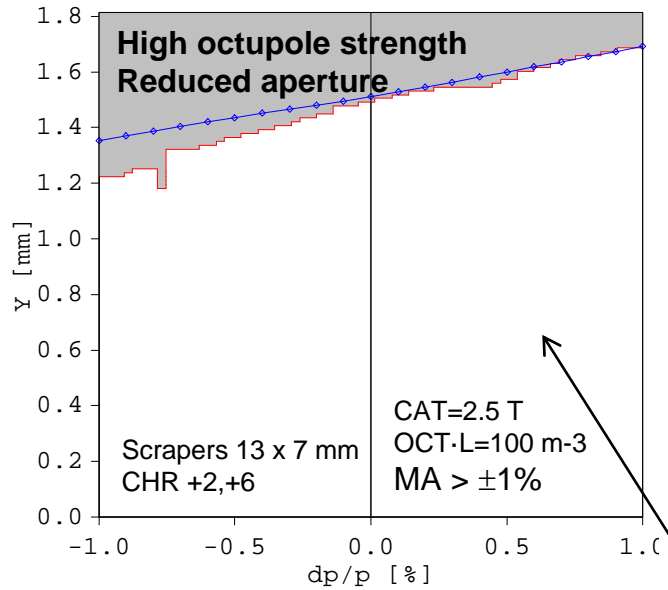


No CATACT neither CLIC  
Wigglers with small  
octupole components  
set by tolerances  
 $OCTGR \cdot L < 100T/m^3$   
Should NOT restrict  
ring operation at  
proposed workig point





# Momentum acceptance at HIGH TUNE $Q_y=2.81$ . CATACT Wiggler ON. $B= 2.5 T$



Betatron tune is chosen away of SXT and OCT resonances

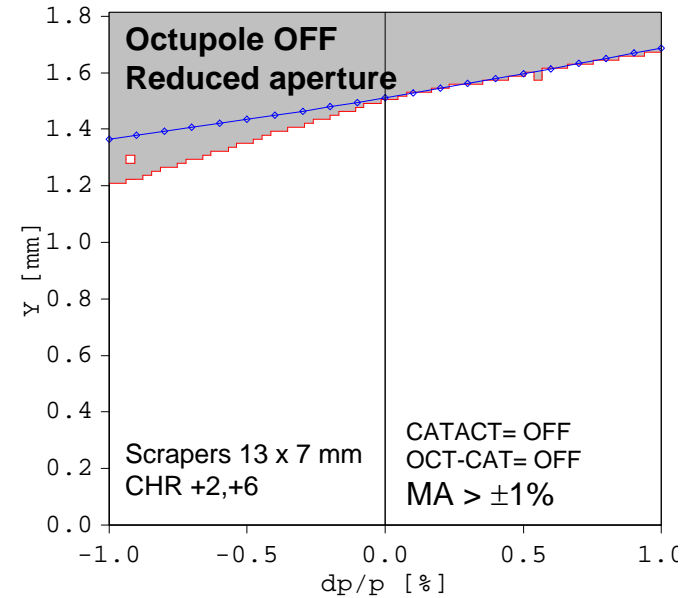
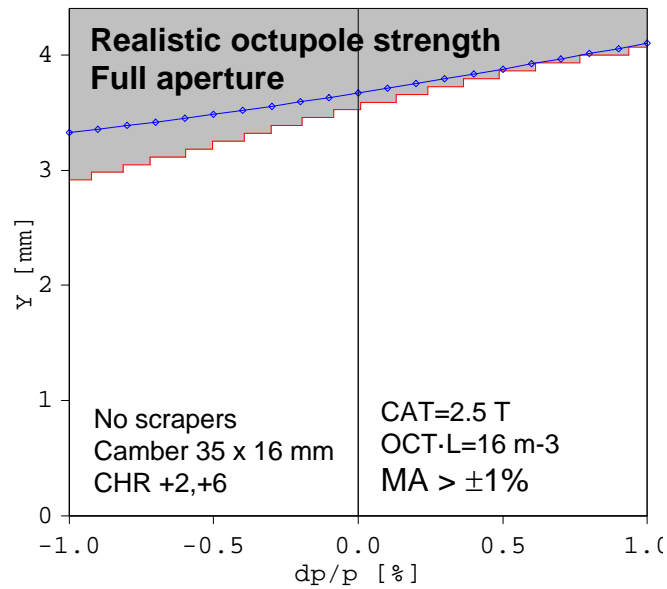
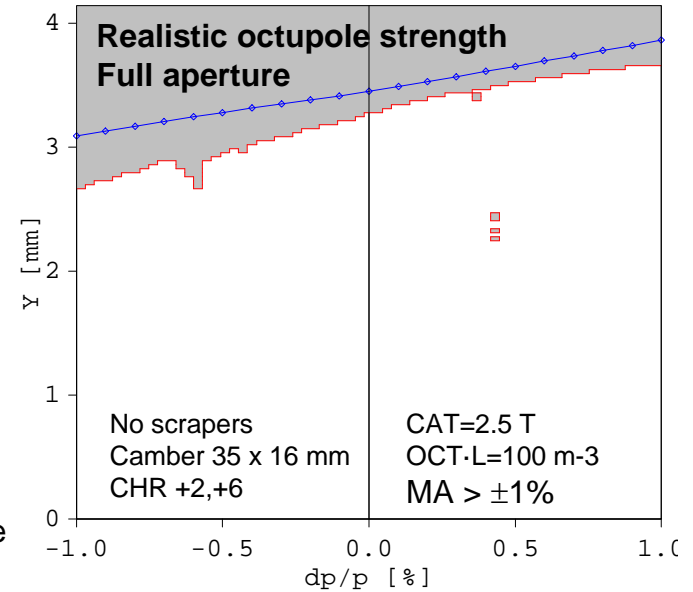
**High tune  
 $Q_y = 2.81$**

Stable motion for ON- momentum and OFF-momentum particles

No distortion of Phase space even at HIGH INTGR. OCTUPOLE Strength

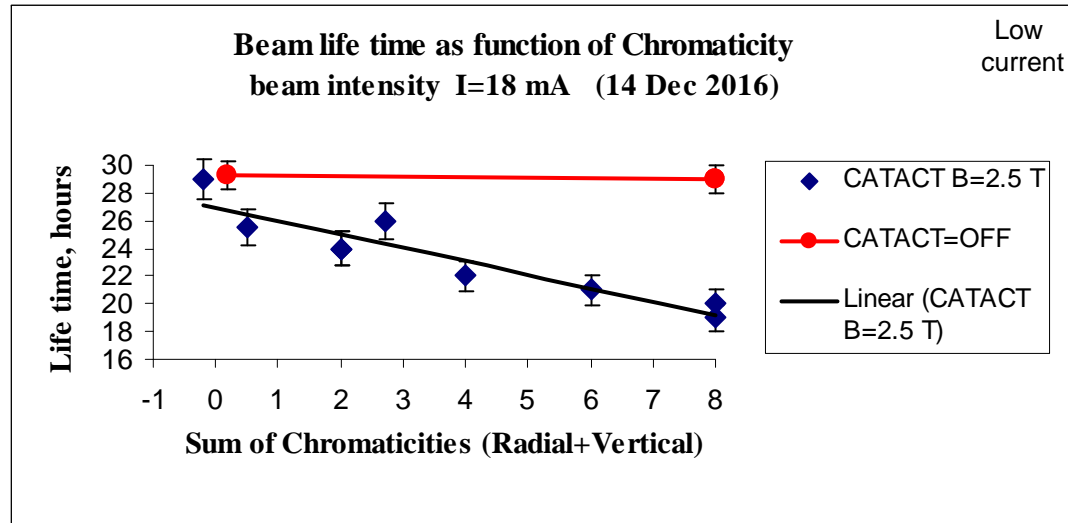
- 100 m-3 and large
- oscillation amplitude
- ANKA operates at safe
- margins of Scrapers

One might consider an option to introduce octupoles for manipulation with compaction factor and Landau damping of instabilities thus increasing stored beam current



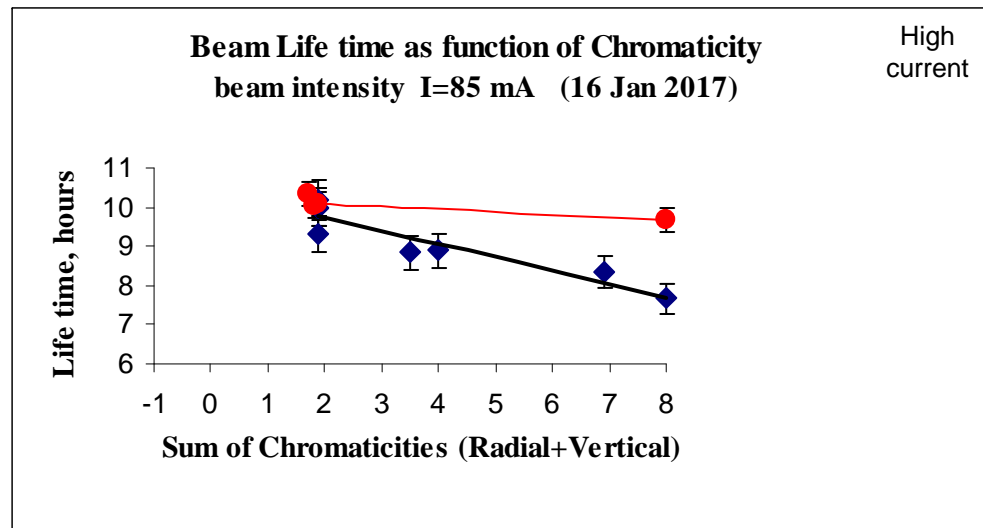
# Ring tests

## Life time measurements 2.5 GeV Qy=2.69



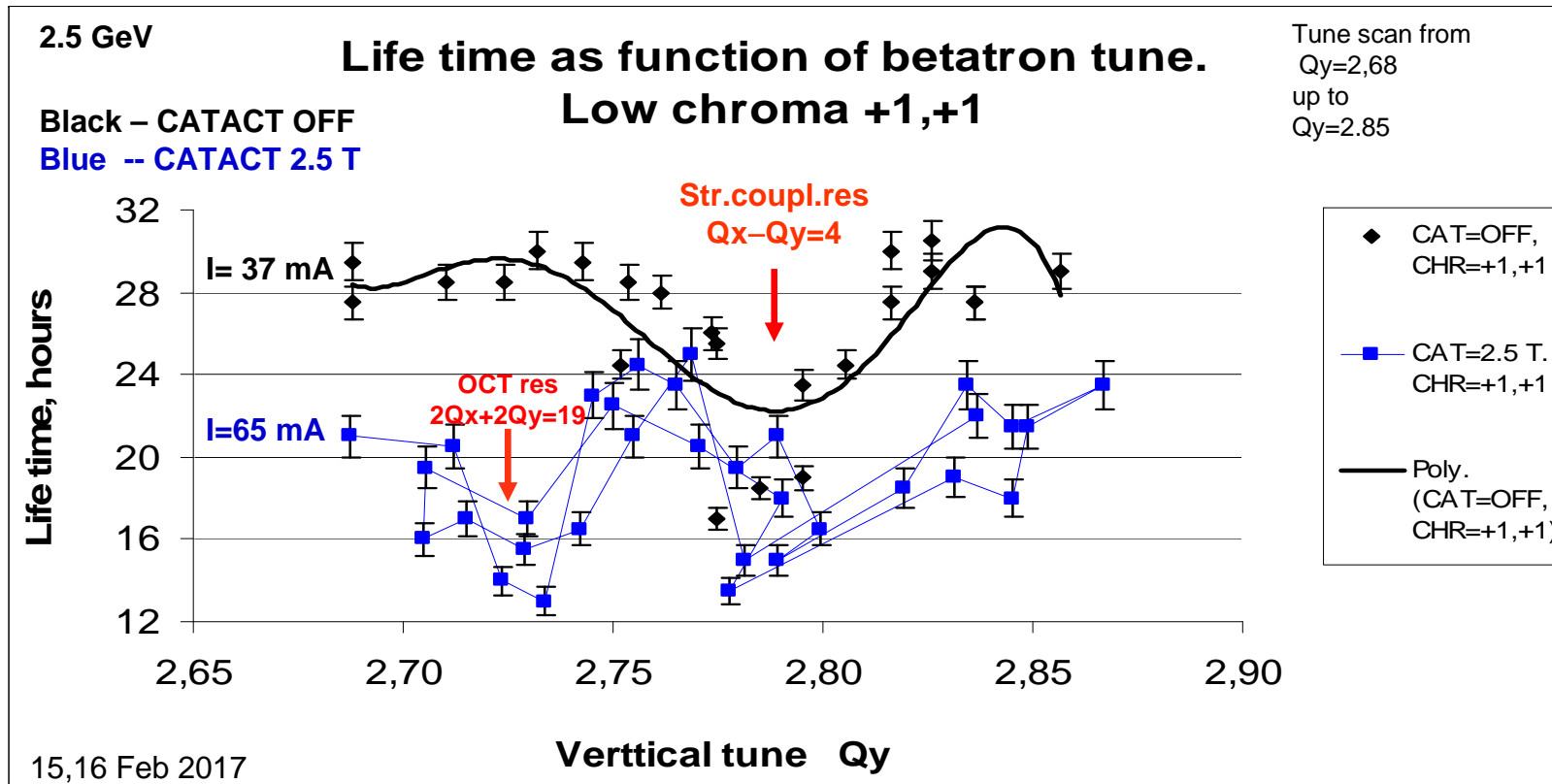
Red – CATACT OFF  
Blue – CATACT=2.5 T

Dependence of Life time on chromaticity (sum of  $\text{CHR}=\xi_x + \xi_y$ ). E=2.5 GeV.  
Beam current 18 mA ANKA tests 15 Dec 2016.

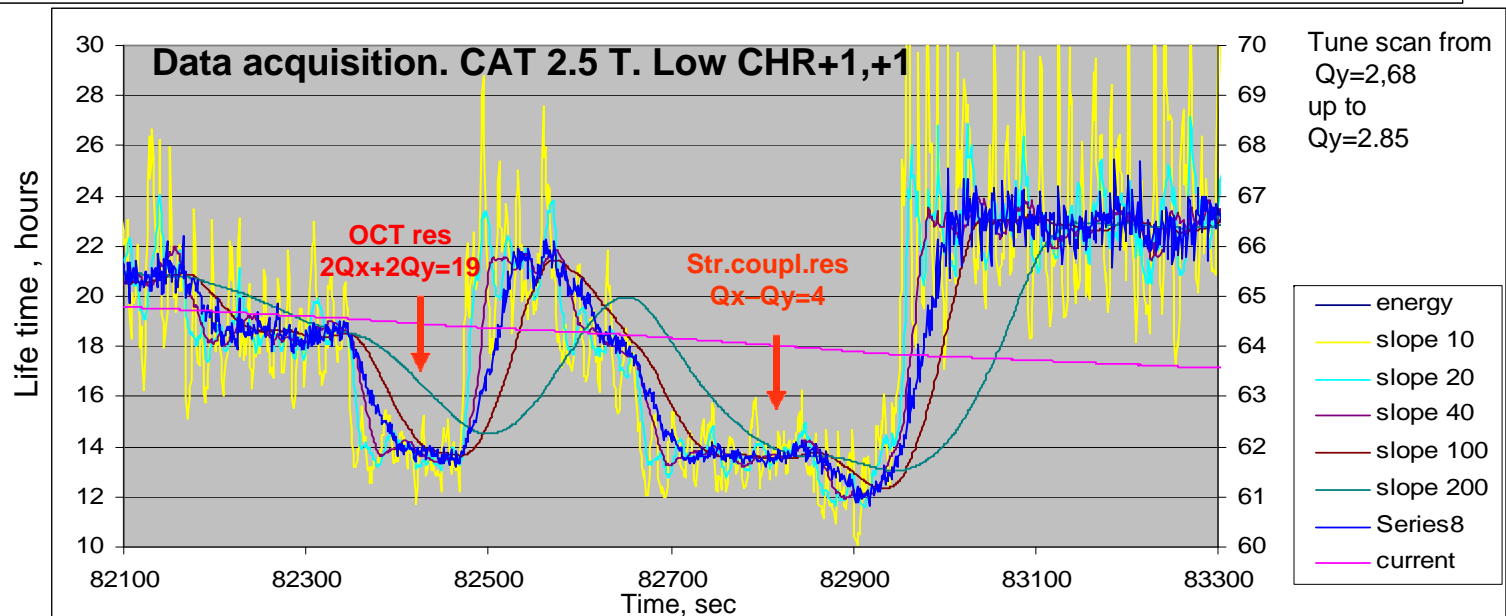


Red – CATACT OFF  
Blue – CATACT=2.5 T

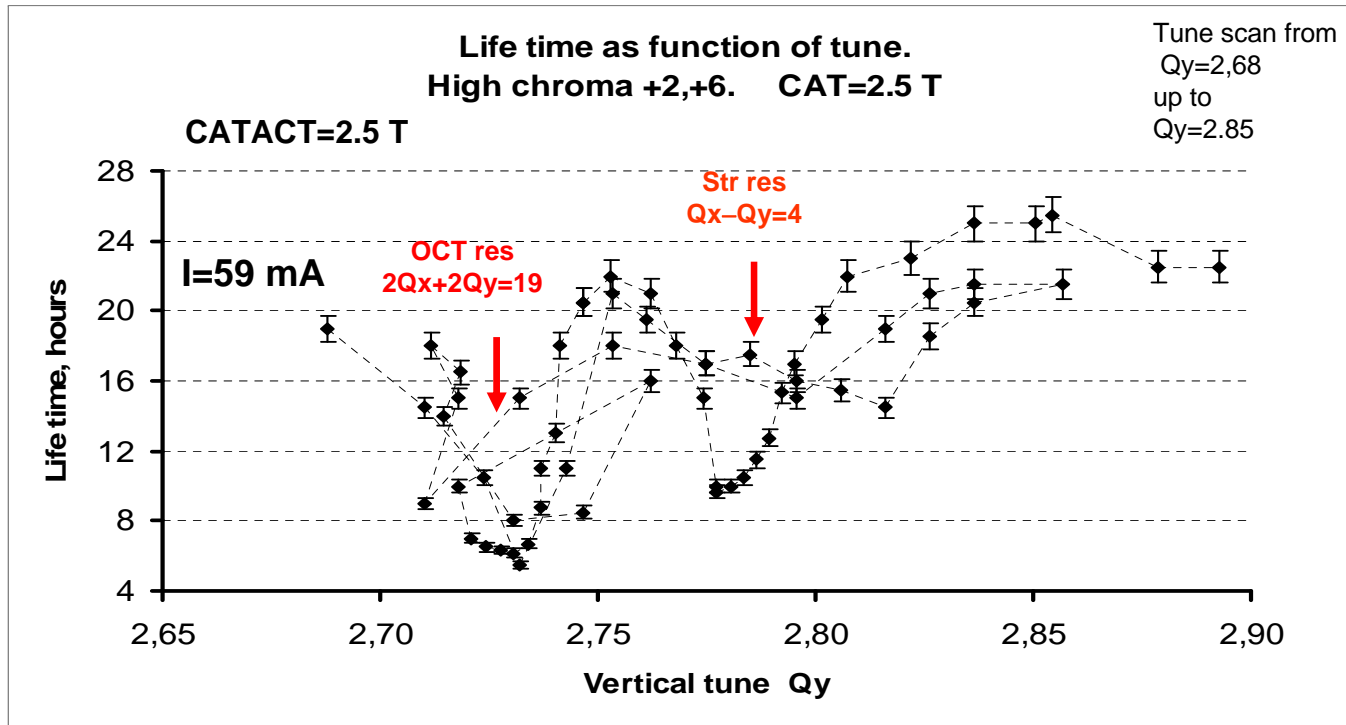
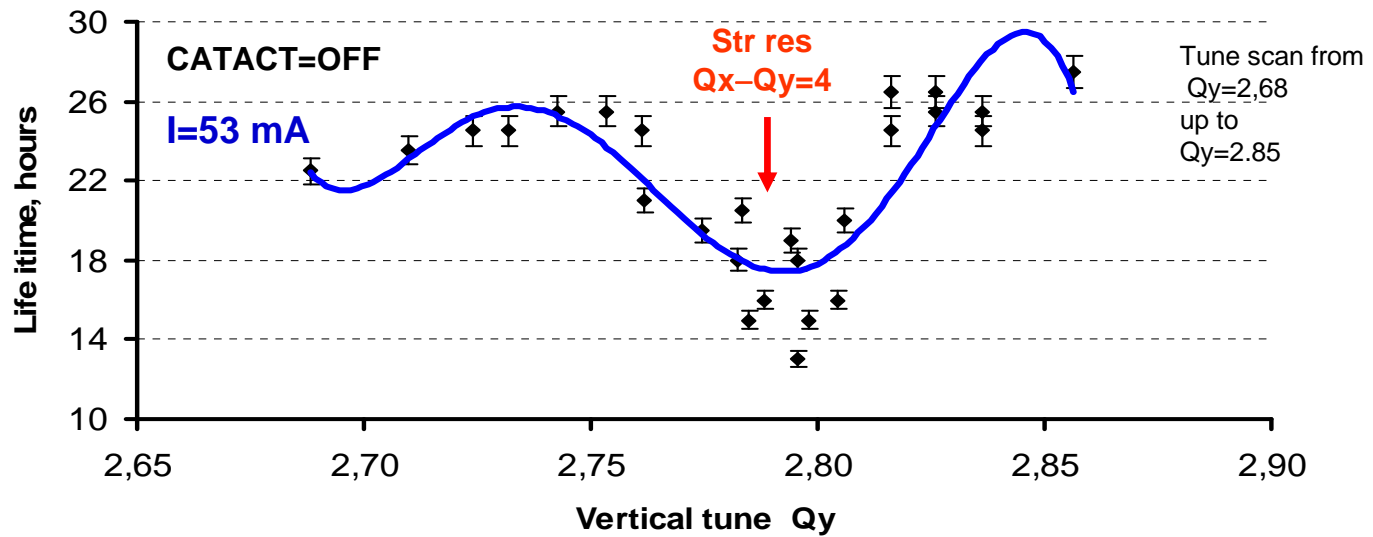
Life time as function of chromaticity (total= $\xi_x + \xi_y$ ). E=2.5 GeV.  
Beam current = 85 mA ANKA tests 16 Jan 2017.



10 data points slope  
 20 data points slope  
 40 data points slope  
 100 data point slope  
 200 data point slope

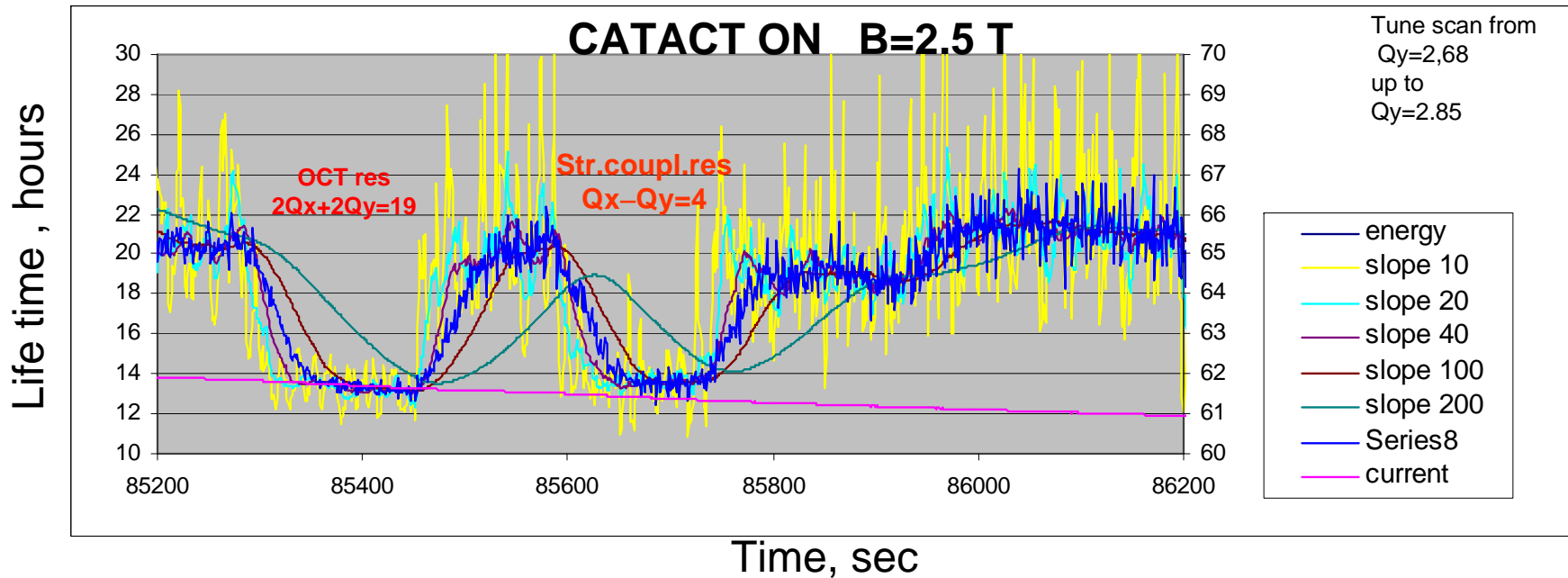
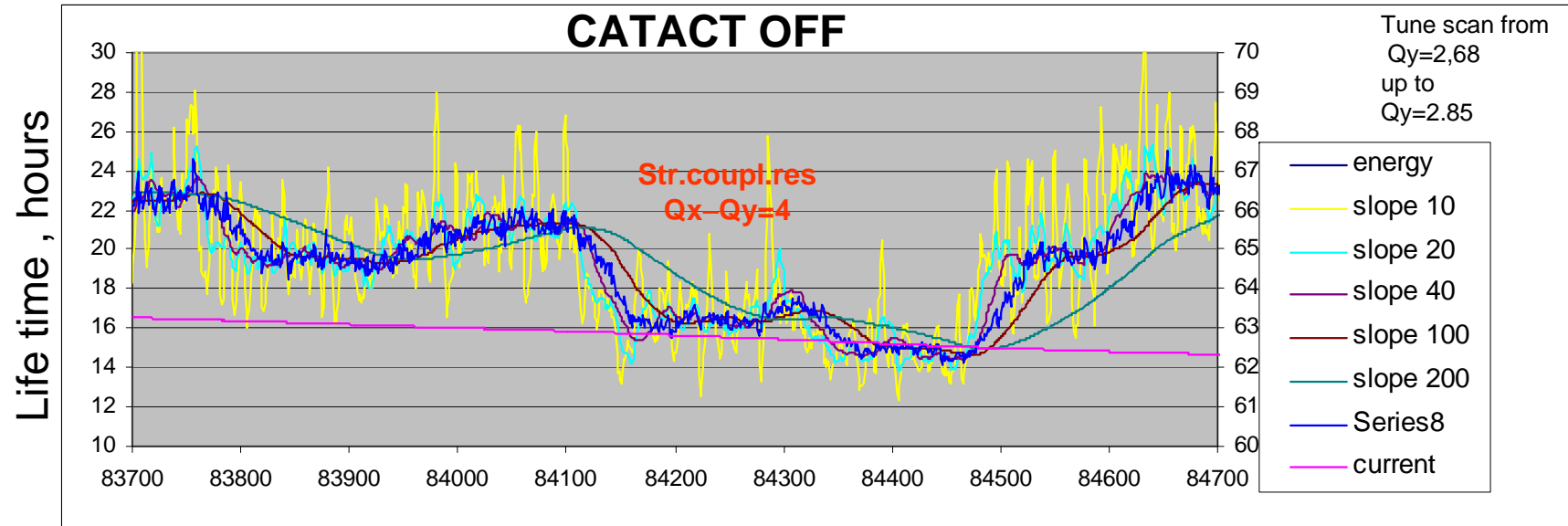


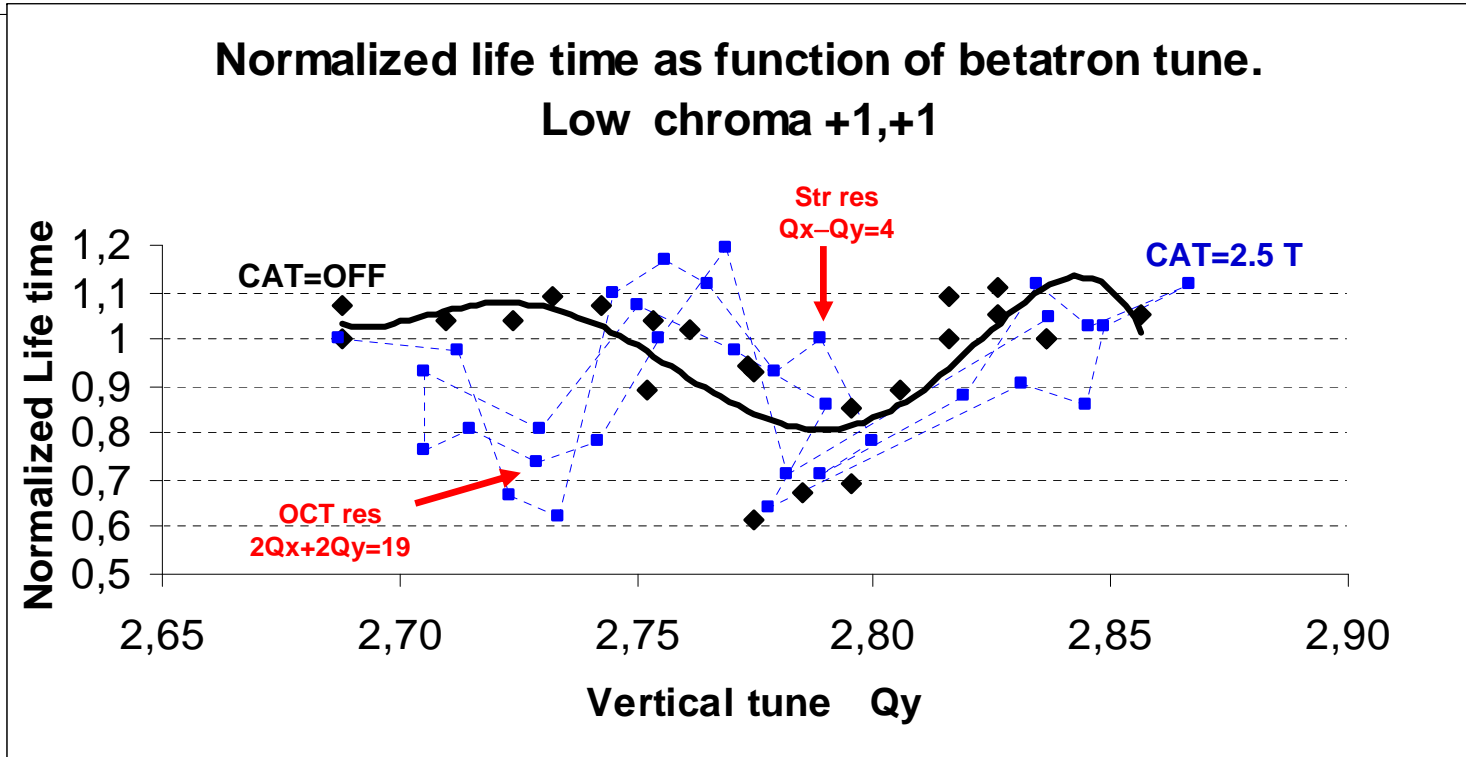
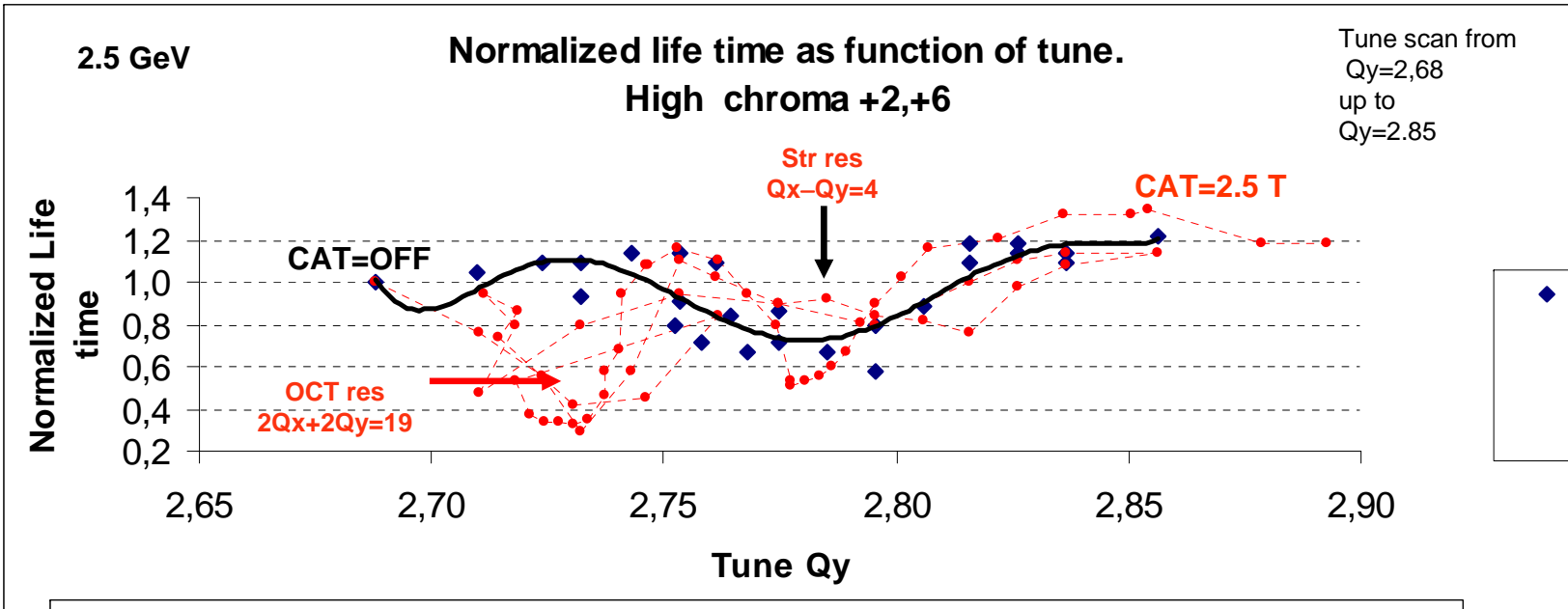
2.5 GeV  
**Life time as function of betatron tune.**  
**High chroma +2,+6. CATACT OFF**



# Life time data acquisition. High chromaticity +2,+6

2.5 GeV







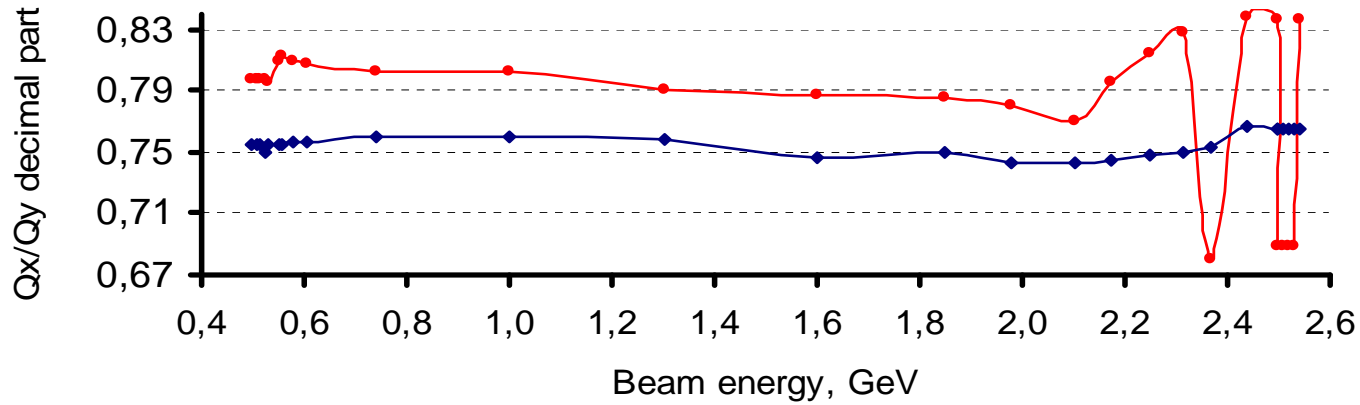
# **Injection and ramp tables**

**We found new settings  
of focusing elements  
to operate ring  
(injection + ramp + plateau)  
at one high tune working point**



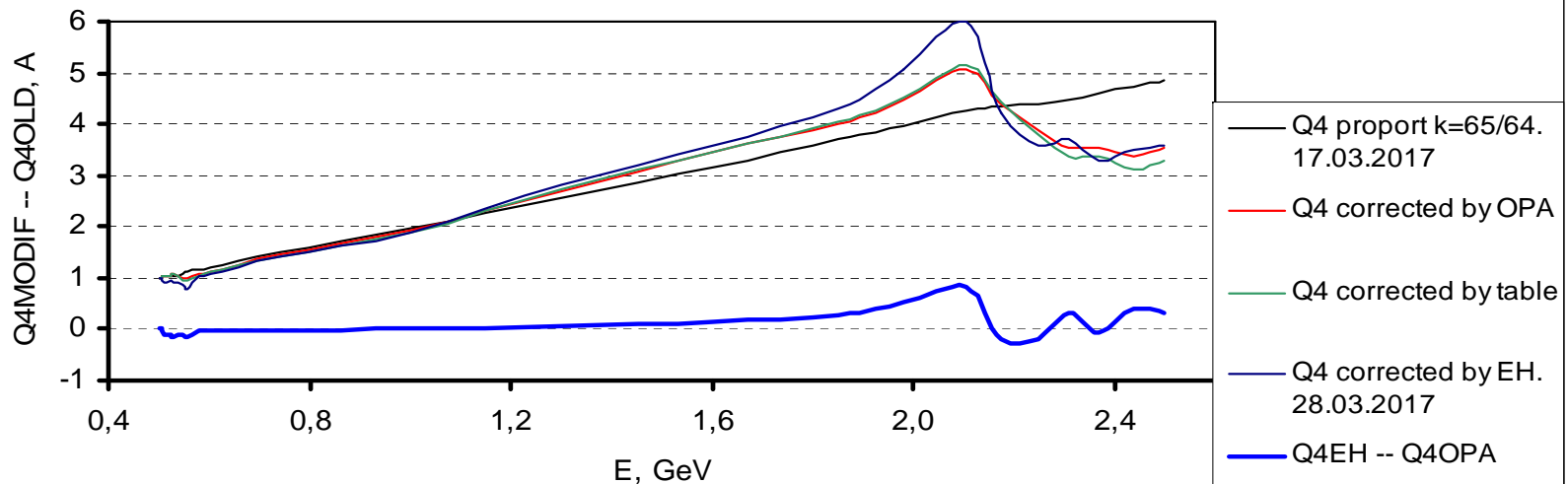
**Betatron tunes during ramp. High Qy mode**  
**Q4 quad strength is increased in proportion  $k=65/64$  to**  
**Q4 strength at USER mode ramp**  
 (170mA at 0.5GeV - 110 mA at 2.5 GeV) 17 March 2017

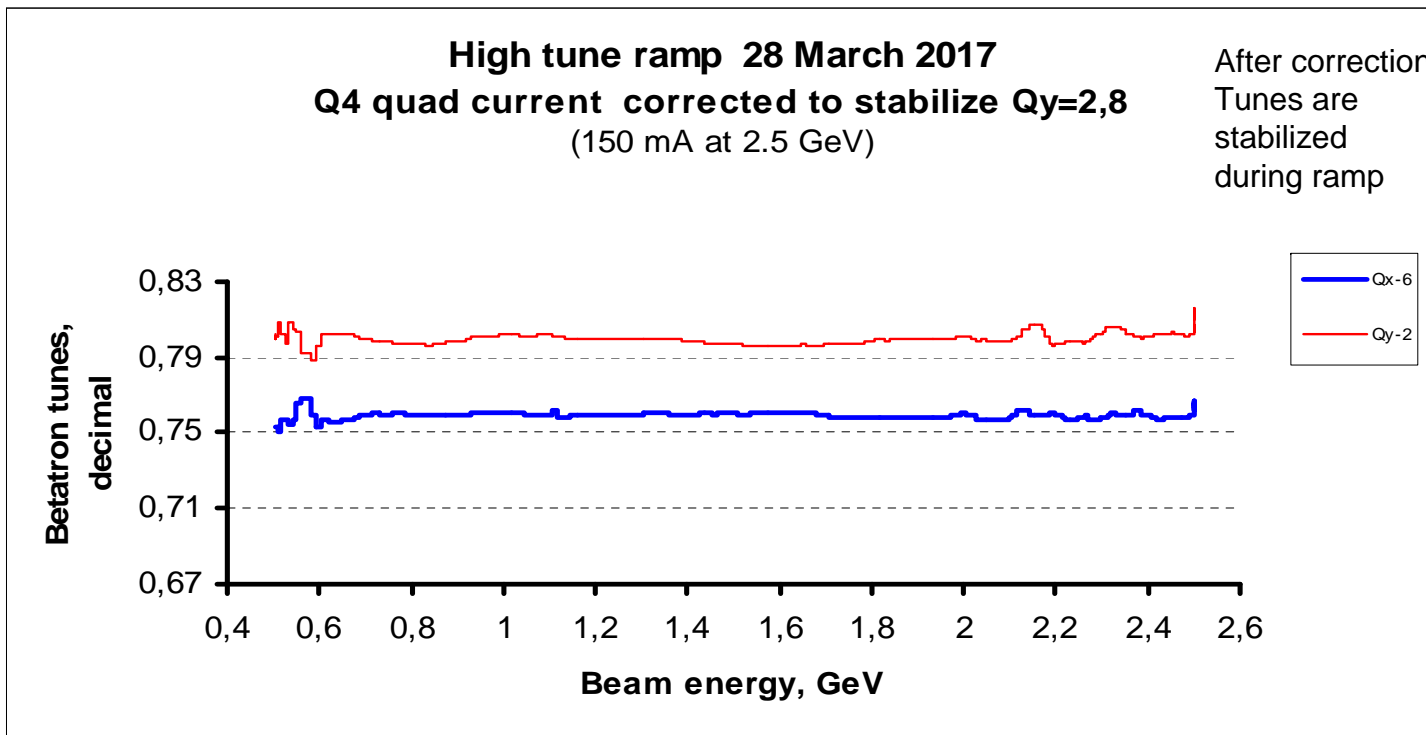
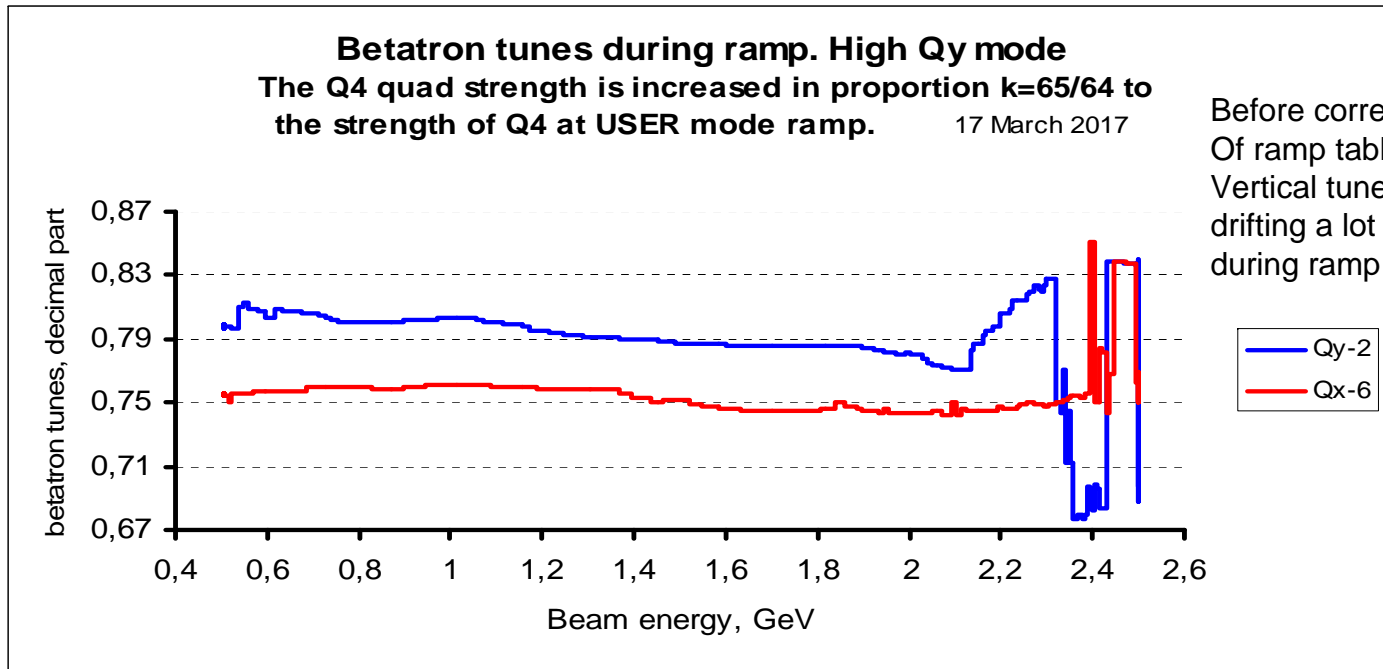
Before correction  
 Vertical tune  
 drifting a lot  
 during ramp



**Adjusting of Q4 quad at ramp**  
**to stabilize high vertical tune  $Q_y=2,8$**

Corrections to ramp table  
 to keep  $Q_y$  CONST during  
 increasing of beam energy





## Merit of new quads settings

New quads settings at high vertical betatron tune  $Q_y \approx 2.810$  are established at injection energy (0.5 GeV), during RAMP (0.5 – 2.5 GeV) and at TOP energy (2.5 GeV)

New quads setting stored in modified ramp tables allow:

(1) stay away from the sextupole resonance  $Q_y = 8/3$

(2) improve operation conditions (life time, stability)

(3) escape reduction of life time at ANKA caused by combination of (a) + (b) + (c) +(d)

(a) high order (octupole) field components

of wiggler  $B_w = 2.2 \div 2.5$  T

(b) proximity of old tune to coupling octupole resonance  $2Q_x + 2Q_y = 19$

(c) proximity of old tune to sextupole resonance  $Q_y = 2.666\dots$

(d) High chromaticity  $\xi_{x,y} = +2,+6$

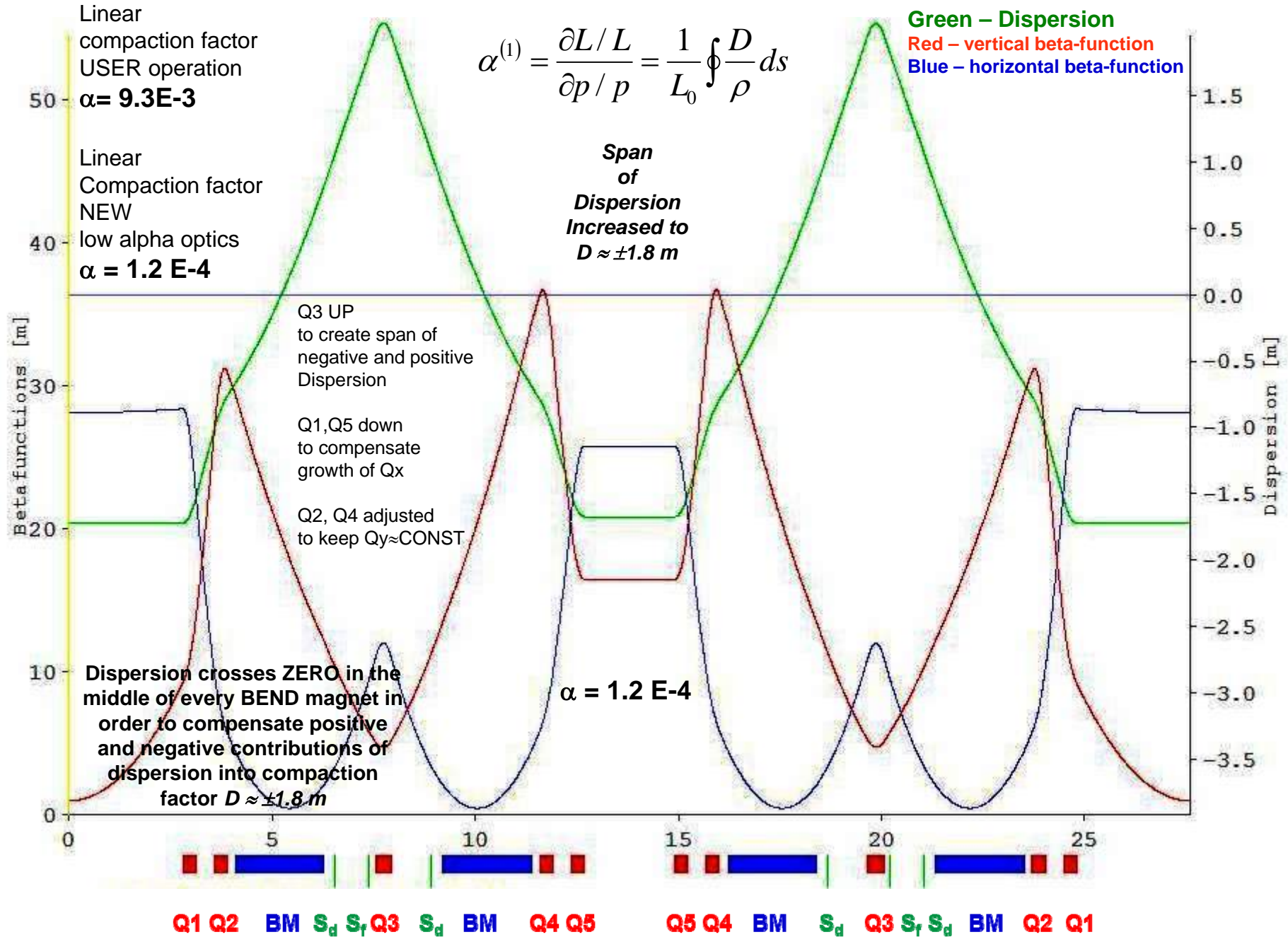
(4) new quads settings are adjusted to minimize SHAKING of betatron tunes during RAMP while quadrupole currents are changed a lot

(5) Small range of tune deviation allows to stabilize beam by applying of the fast feedback system during injection, ramp, at TOP

# **Low compaction factor Tests - 2017**

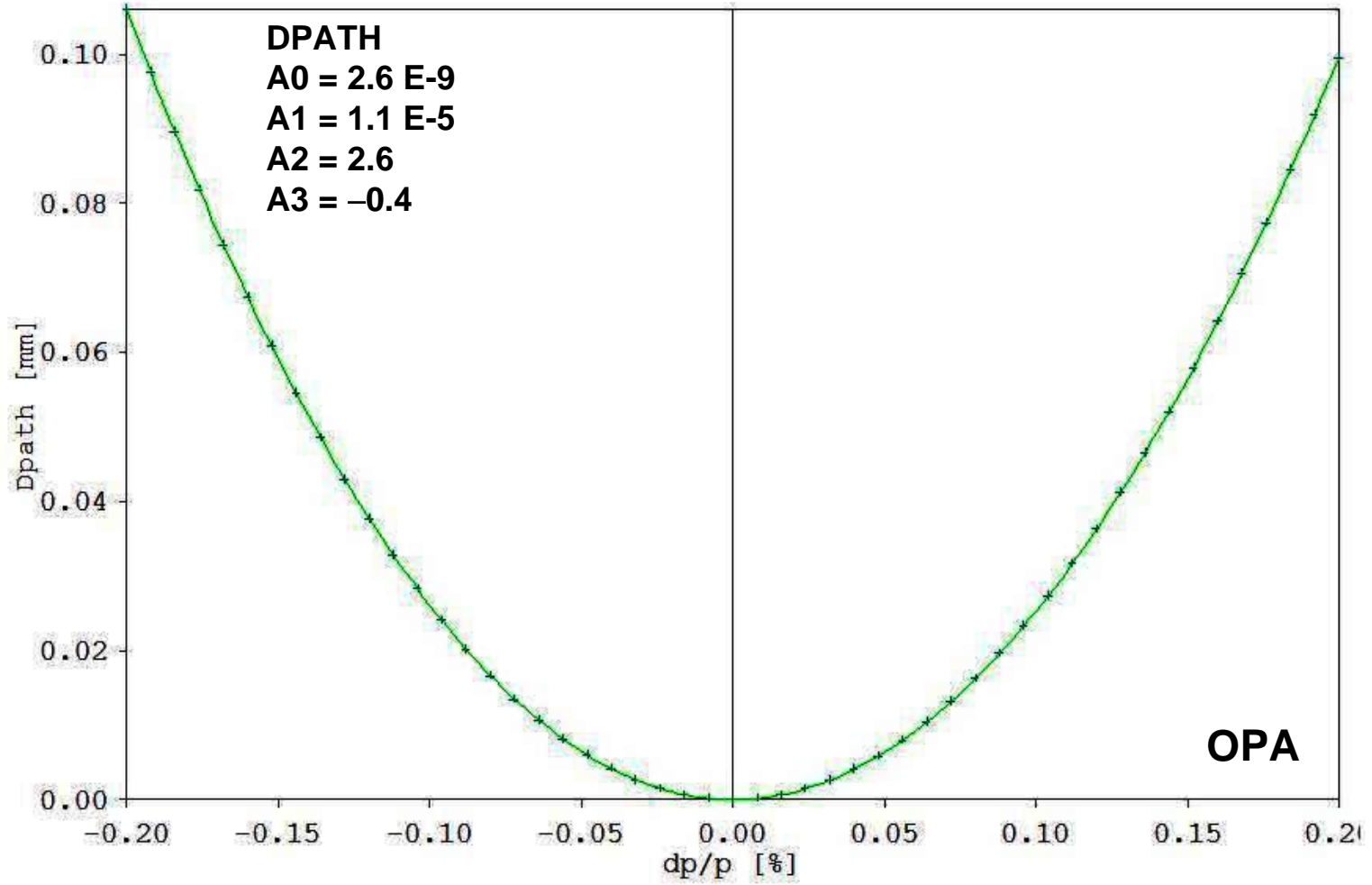
**We found new settings of quads  
for  
low alpha ramp-squeezing tables  
operating at high betatron tune  
and  
measured beam parameters  
at  
low alpha mode**

# Low APLHA Optics. One Cell

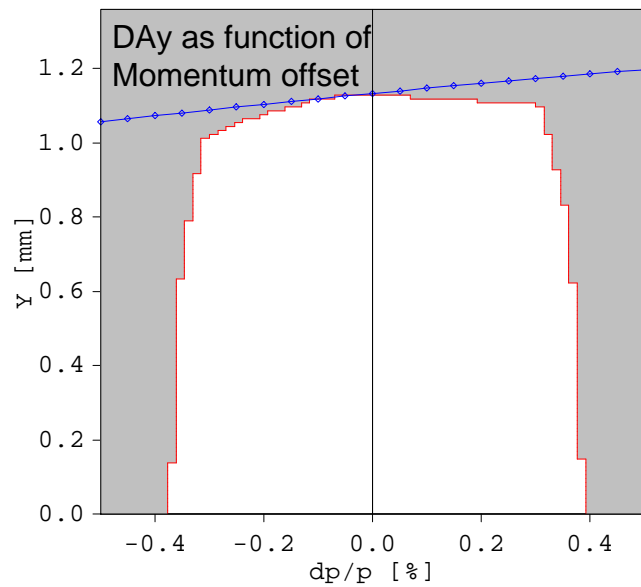
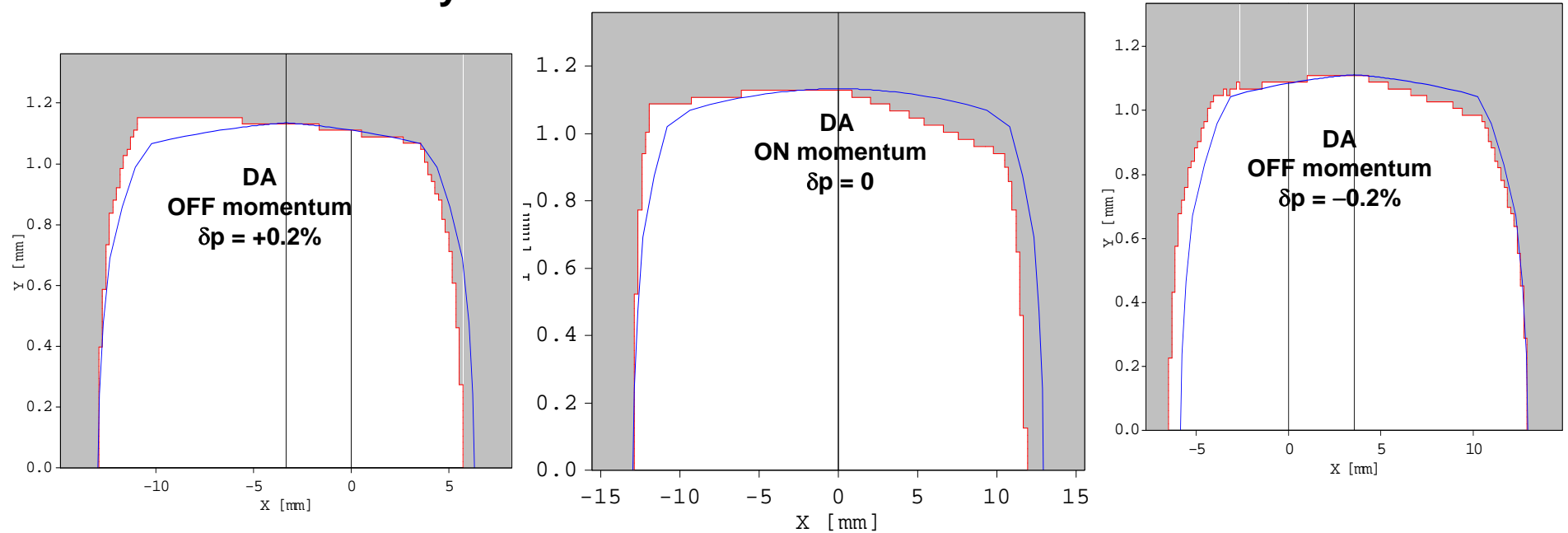




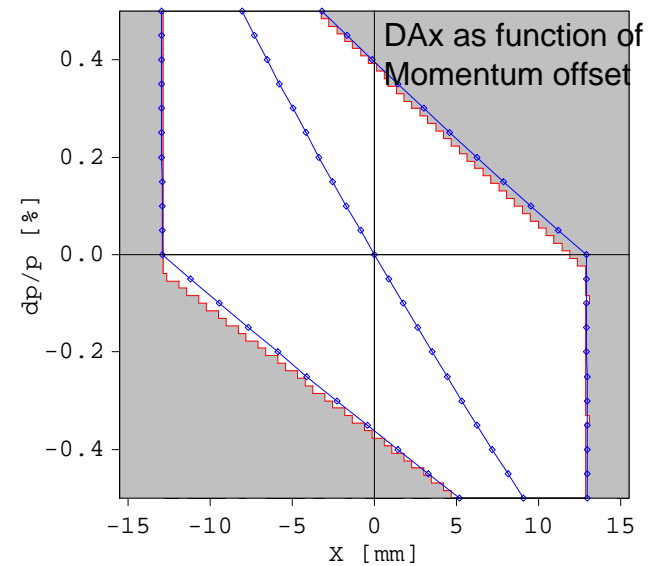
**Low ALPHA Mode.  
High order components of compaction factor**



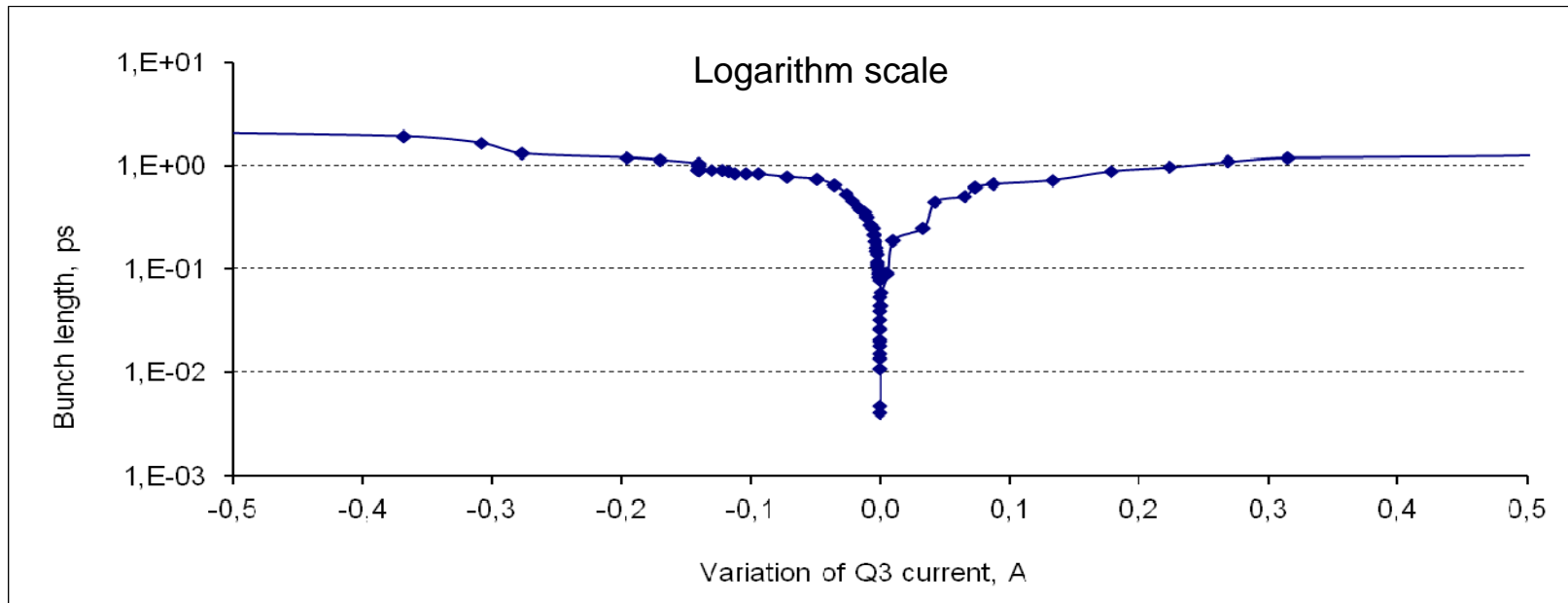
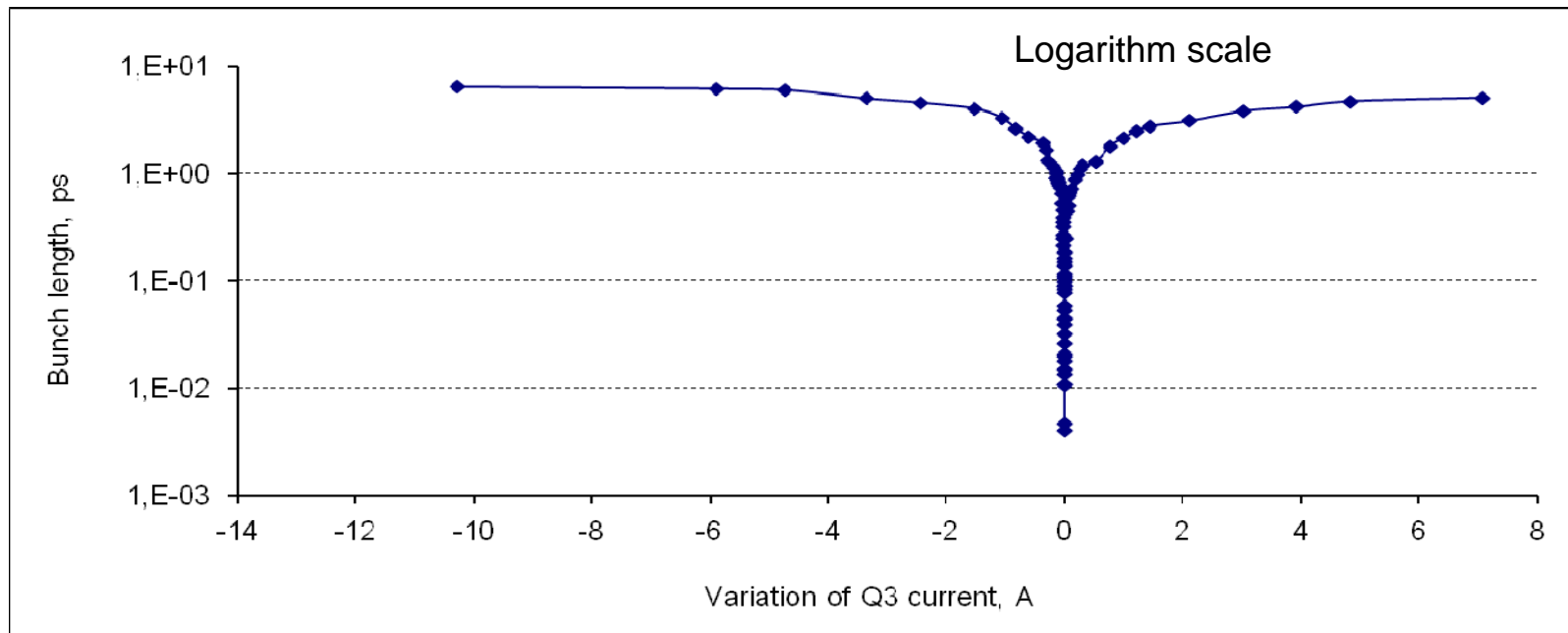
# Simulations of Dynamic aperture at Low ALPHA mode (high tune). Synchrtorton motion is NOT included



**Momentum Acceptance at low alpha is reduced from  $\Delta p/p \approx \pm 2\%$  down to  $\Delta p/p \approx \pm 0.2\%$ . Thus, Life time drops**



## Zero current Bunch length (simulations)



# Reduction of chromaticity during Low-ALPHA operation

## ADOL -- AMPLITUDE DEPENDENT ORBIT LENGTHENING

$$\delta C^{ADOL} = -2\pi \cdot (\xi_x \cdot J_x + \xi_y \cdot J_y) \qquad 2 \cdot J_{x,y} = \varepsilon_{x,y}$$

TO minimize smearing of bunch length as well as coupling between horizontal and longitudinal planes ( Path lengthening caused by transverse oscillations) one should reduce ADOL

$$\frac{\delta C^{ADOL}}{C_0} \ll \alpha_0 \cdot \delta_0$$

### Chromaticity tolerance limit during low- $\alpha$ operation (E=1.3 GeV)

| 2Jx     | $\alpha_0$ | $\xi_{x,y}$ |
|---------|------------|-------------|
| 80 nm·r | 1.E-4      | $\leq +2$   |
| 80 nm·r | 2.E-5      | $\leq +1$   |
| 80 nm·r | 2.E-6      | $\leq +0.2$ |

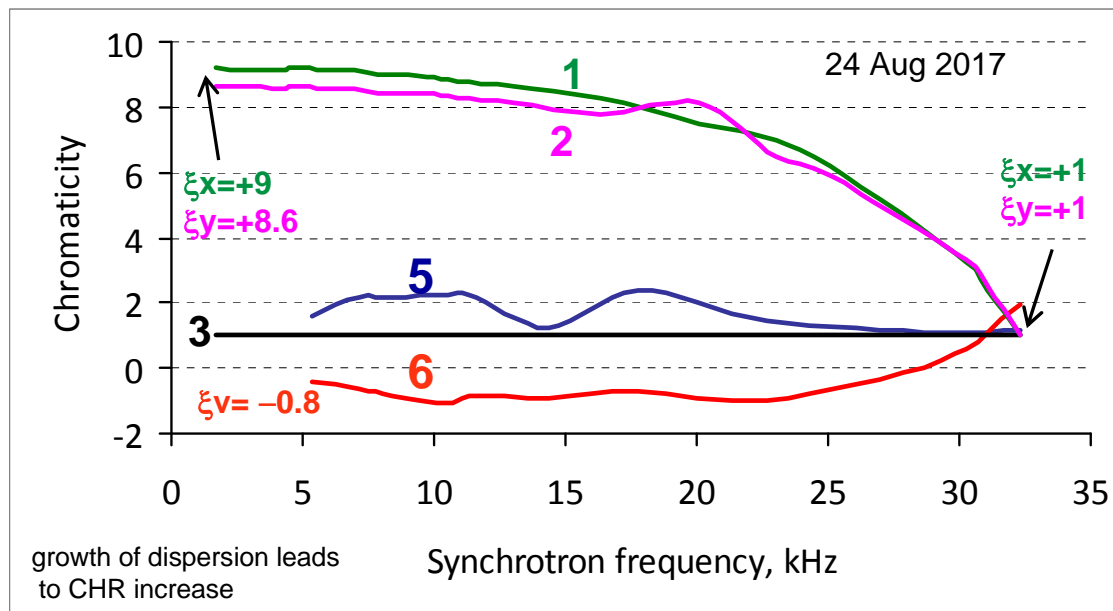
### Chromaticity limit during low- $\alpha$ operation at MLS (0.63 GeV)

|                 |                              |                               |
|-----------------|------------------------------|-------------------------------|
| <b>2Jx</b>      | <b><math>\alpha_0</math></b> | <b><math>\xi_{x,y}</math></b> |
| <b>200 nm·r</b> | <b>1.3E-4</b>                | <b>+0.2</b>                   |

# Merit of SXT strength reduction during low alpha squeeze (24Aug 2017)

High SPAN of Dispersions variation  
 Leads to essential increase of **chromaticity**  
 during low alpha Squeeze  
**IF SXT strength is FIXED**  
 (curve 1 and curve 2).  
 The effect is present at any beam energy  
 (0.5 GeV, 1.3 GeV etc.)

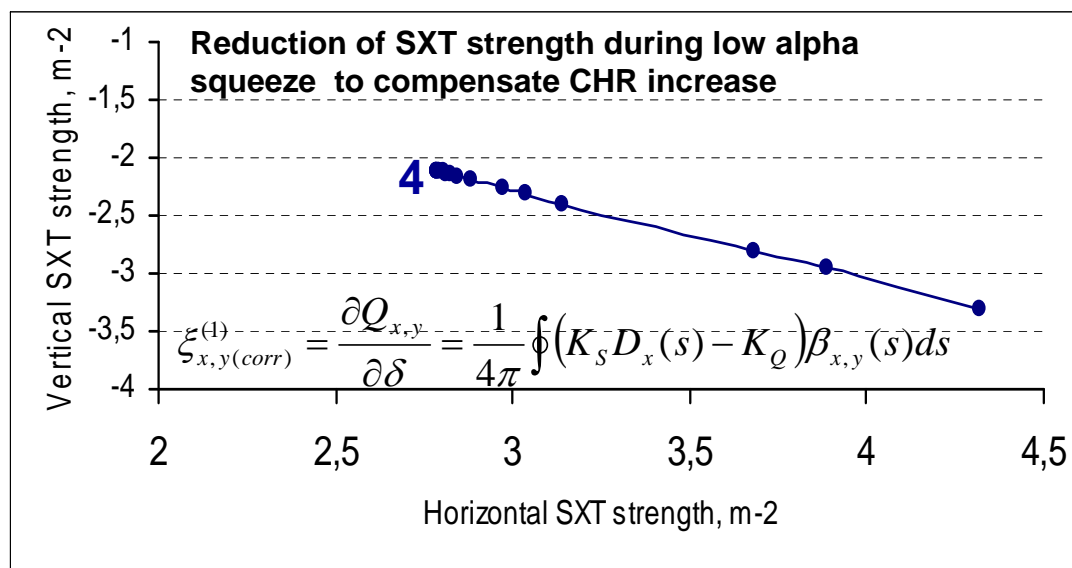
1 –  $kSF=+4,3 \text{ m}^{-2} = \text{const}$   
 2 –  $kSD = -3,3 \text{ m}^{-2} = \text{const}$



Reduction of SXT strength during low alpha  
 squeeze compensates growth of CHR  
 (curves 3, 4, 5, 6)

To keep CHR **unchanged** during low alpha  
 Squeeze ( $\xi_{h,v} = +1,+1$ ),  
 see **curve 3**,  
 SXT strength is reduced from  
 $kSF=+4,3$  down to  $+2,8 \text{ m}^{-2}$   
 $kSD = -3,3$  down to  $-2,1 \text{ m}^{-2}$ ,  
 see **curve 4**

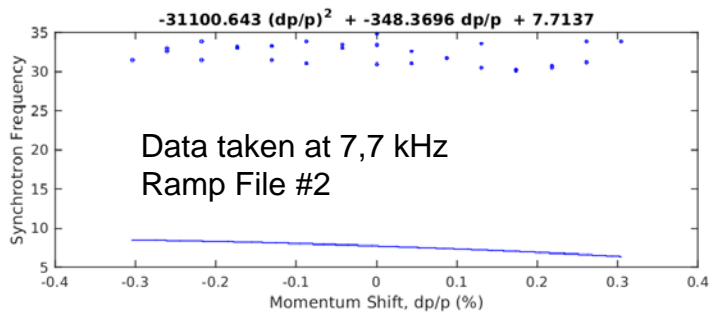
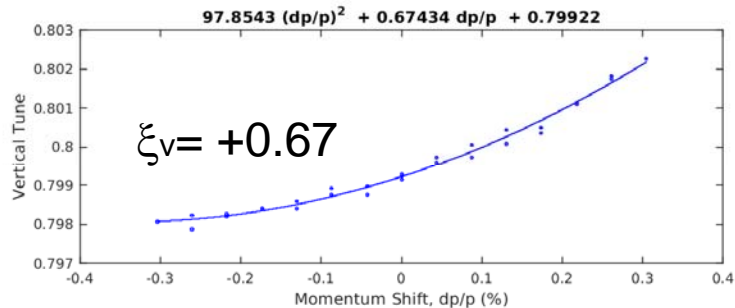
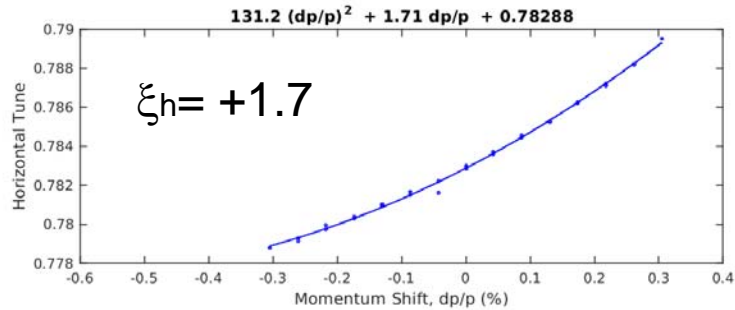
**Curve 5** and **curve 6** – CHRh and CHRv  
 MEASURED during low alpha squeeze at 1.3  
 GeV (tests 24 August 2017)  
**5** –  $\xi_h \approx +1$  to  $+2$  (ISF = 76 A down to 61 A)  
**6** –  $\xi_v \approx +2$  to  $-0,8$  (ISD = 70 A down to 54 A)



We should adjust CHR-h,v settings in the ramp/squeeze table in order to keep  $0 < \text{CHR}_{h,v} \leq 2$   
 We should measure Life Time and bunch stability during Squeeze at small  $(+1,+1)$ /high  $(+2,+6)$  CHR and choose OPTIMUM settings

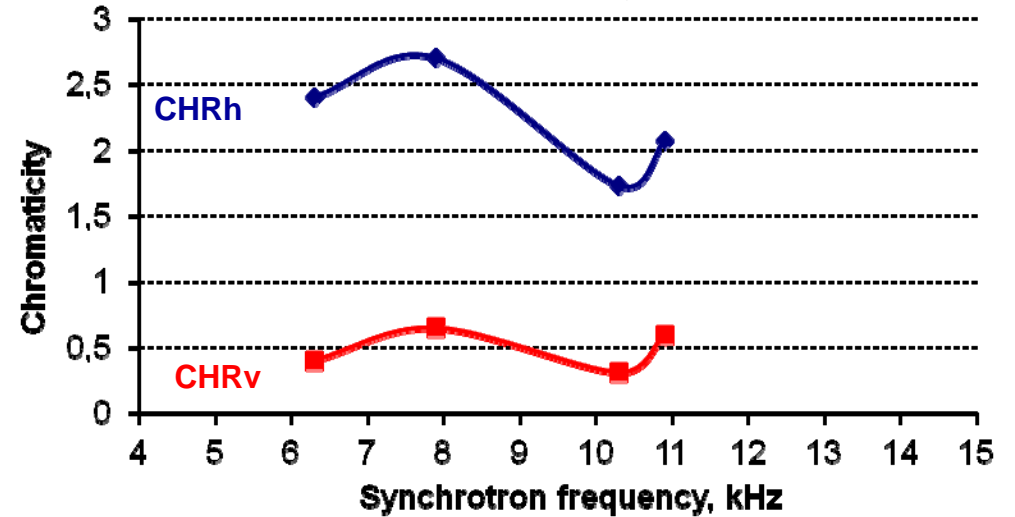
# Correction of SXT strength to keep CHR slightly positive during low-alpha squeeze ( BP tests 16-19 October 2017)

Chroma measurements of corrected ramp/squeeze file #2 (reduced SXT strength). Julian Gethmann 19 Oct 2017

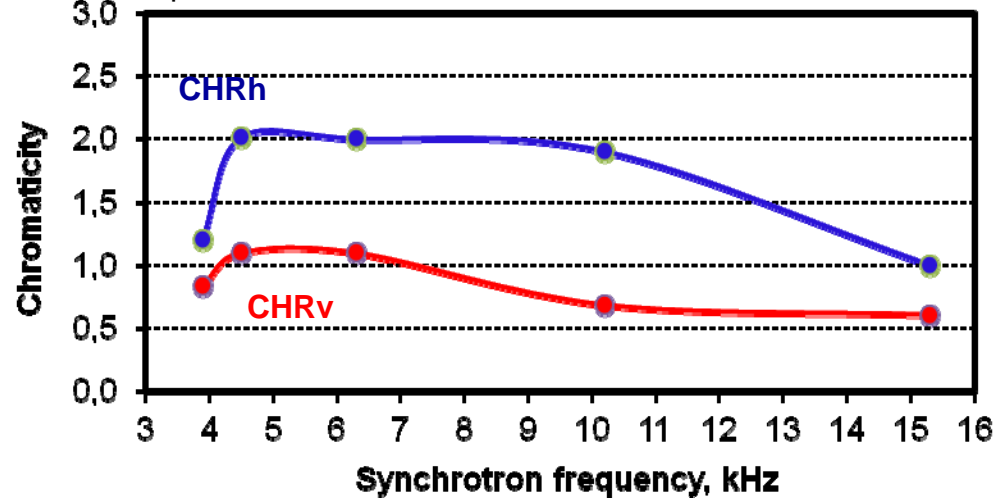


19-Oct-2017 19:34:22

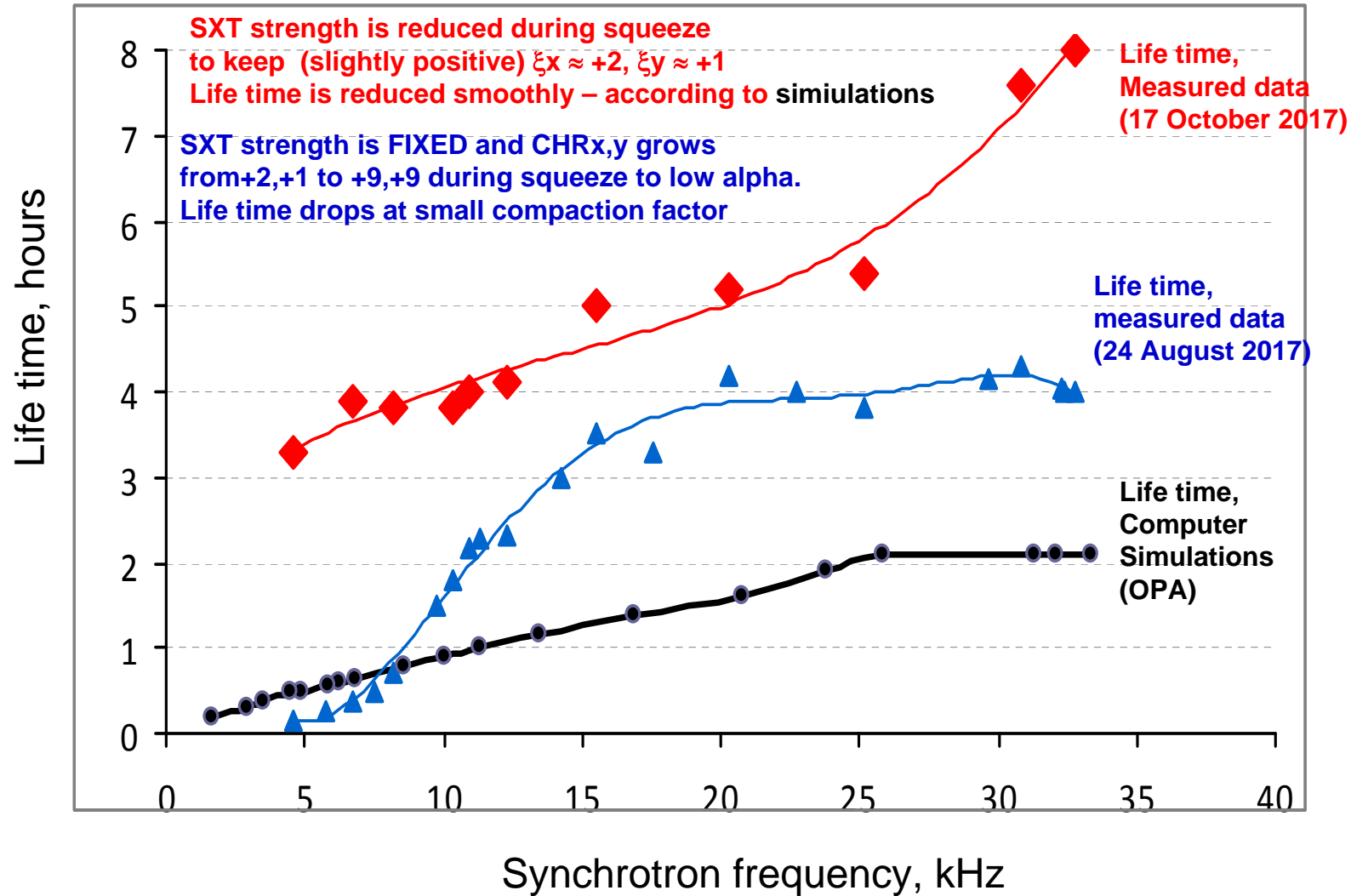
SXT strength corrected to keep positive chromaticity  
Ramp File #1 from 31 Aug 2017



SXT strength adjusted to optimize chromaticity during squeeze.  
Ramp file #2 from 16 October 2017



Life time at low compaction factor  
was improved (**red curve**)  
because of synchronized reduction of chromaticity  
has been applied during low alpha squeeze





- New Low Alpha tables (1.3 GeV) are modified to MINIMIZE tune deviation during SQUEEZE. Feedback is **ON** and stabilizes beam during squeeze
- Orbit correction is NOT required during low alpha squeeze except last point at very low alpha
- We adjusted CHR-x,y settings in the ramp/squeeze table in order to keep small CHROMA ( $1 \leq \xi_{x,y} \leq 2$ ) during reduction of compaction factor and low alpha operation
- We should measure Life Time and bunch stability during Squeeze at small (+1,+1) and high (+2,+6) CHR and choose OPTIMUM settings
- We should organize tests of influence of coupling between horizontal and vertical planes (from simulations – coupling up to 20%) on the beam life time at low alpha. Preliminary, RF noise on Y-Steerers might effectively increase hor/vert coupling, i.e. increase vertical emittance, thus improve life time at low alpha in a 2- 3 times

| Mode                               | rms bunch<br>Length (mm) | rms bunch<br>width (ps) | Fs<br>kHz  | E<br>GeV    | $\alpha_0$     | Frf<br>MHz |
|------------------------------------|--------------------------|-------------------------|------------|-------------|----------------|------------|
| User                               | 6.5                      | 21.6                    | 33.4       | 1.3         | 9.0E-3         | 500        |
| <b>Low-<math>\alpha</math></b>     | <b>0.8</b>               | <b>2.4</b>              | <b>5</b>   | <b>1.3</b>  | <b>1.2 e-4</b> | <b>500</b> |
| <b>MLS User</b>                    | <b>6</b>                 | <b>19</b>               | <b>106</b> | <b>0.63</b> | <b>3.0 e-2</b> | <b>500</b> |
| <b>MLS Low-<math>\alpha</math></b> | <b>0.8/1.1 (THz/IR)</b>  | <b>2.5/3 (THz/IR)</b>   | <b>6.9</b> | <b>0.63</b> | <b>1.3 e-4</b> | <b>500</b> |

**Thanks**

# **Backup Slides**

## Main parameters of CATACT and CLIC wigglers

| Name  | CATACT  | CLIC   |
|---|---|--|
| Field direction   | Vertical  | Vertical   |
| Wiggler period $\lambda_w$ , mm   | 48  | 51   |
| Peak field $B_w$ , T  | 2.5   | 3  |
| Magnetic rigidity $B \cdot R$ , T·m   | 8.33  | 8.33   |
| Magnetic length $L_w$ , mm  | 960   | 1836   |
| Number of pole pairs @ full field   | 36  | 68   |
| Number of pole pairs @ 1/4 field  | 2   | 2  |
| Number of pole pairs @ 3/4 field  | 2   | 2  |
| Number of full periods  | 18  | 34   |
| Wiggler aperture, $V \times H$ , mm   | 15×60   | 13×76  |
| Scrapers opening, $V \times H$ , mm   | 14×26   | 12×26  |
| Undulator parameter $k_w = 2\pi/\lambda_w$ , mm <sup>-1</sup>   | 11.2  | 14.29  |
| Orbit curvature $h_w = 1/\rho_w = B_w/B \cdot R$ m <sup>-1</sup>  | 0.3   | 0.36   |
| WGL bending angle $\theta_m = \lambda_w/2\pi\rho_w$ mr  | 2.3   | 2.9  |
| Hor/vert beta at WGL position $\beta_x/\beta_y$ , m   | 13.2 / 12.7   | 17 / 0.9   |
| Hor/vert coupling   | 0.5÷1%  | 0.5÷1%   |
| Equil. beam size $(\sqrt{\sigma_x^2 + (D \cdot \sigma_p)^2})/\sigma_y$  | 0.86 / 0.11 mm  | 1.04 / 0.03 mm   |
| <b>Vertical betatron tune shift</b> $\Delta\nu_y = \frac{1}{8\pi} h_w^2 L_w \bar{\beta}_y$  | +0.0436   | +0.0085  |
| Action variable $J_y = A_y^2/(2\beta_y)$ , m  | $\approx 1.5 \cdot 10^{-6} [m]$                                     | $\approx 5 \cdot 10^{-7} [m]$                                      |
| <b>ADTS Tune spread - pseudo-octupole field</b><br>$\delta\nu_y = \left( \frac{1}{8\pi} L_w k_w^4 \theta_m^2 \bar{\beta}_y^2 \right) J_y$ | $1.2 \cdot 10^4 \cdot J_y [m]$<br>$\delta\nu_y = 1.8 \cdot 10^{-2}$ | $1.17 \cdot 10^2 \cdot J_y [m]$<br>$\delta\nu_y = 6 \cdot 10^{-5}$ |

$$\Delta\nu_y = \frac{1}{8\pi} (B_w/B \cdot R)^2 \cdot L_w \cdot \bar{\beta}_y$$

$$\left( \sqrt{\sigma_x^2 + (D \cdot \sigma_p)^2} \right) / \sigma_y$$

$$\text{CLIC } \sigma_x / \sigma_y = 1.04 / 0.03 \text{ mm}$$

$$\text{CATACT } \sigma_x / \sigma_y = 0.86 / 0.11 \text{ mm}$$

$$DA \approx 12\sigma_x / 36\sigma_y = 12 / 1.1 \text{ mm}$$

$$\beta_x / \beta_y = 17 / 0.91 \text{ m}$$

$$\text{BM} = 22.5^\circ$$

**Negative  
Compaction  
Factor  
(simulations)**

Transition of compaction factor from positive to negative value.

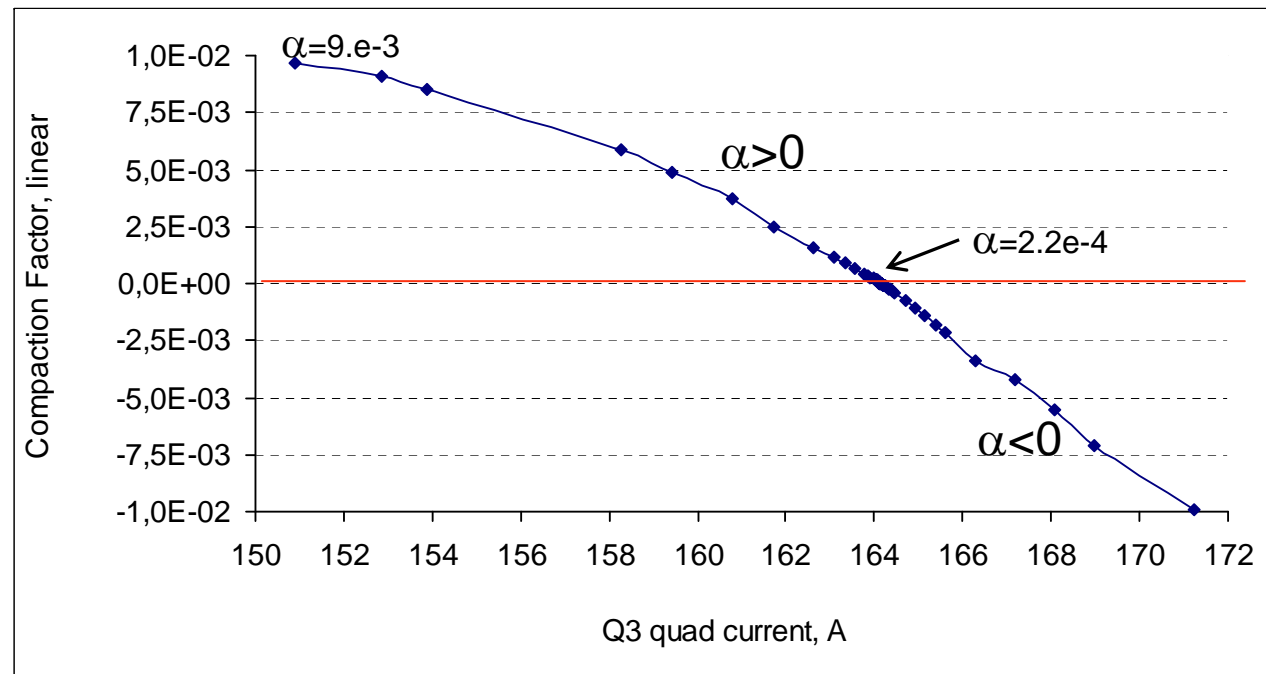
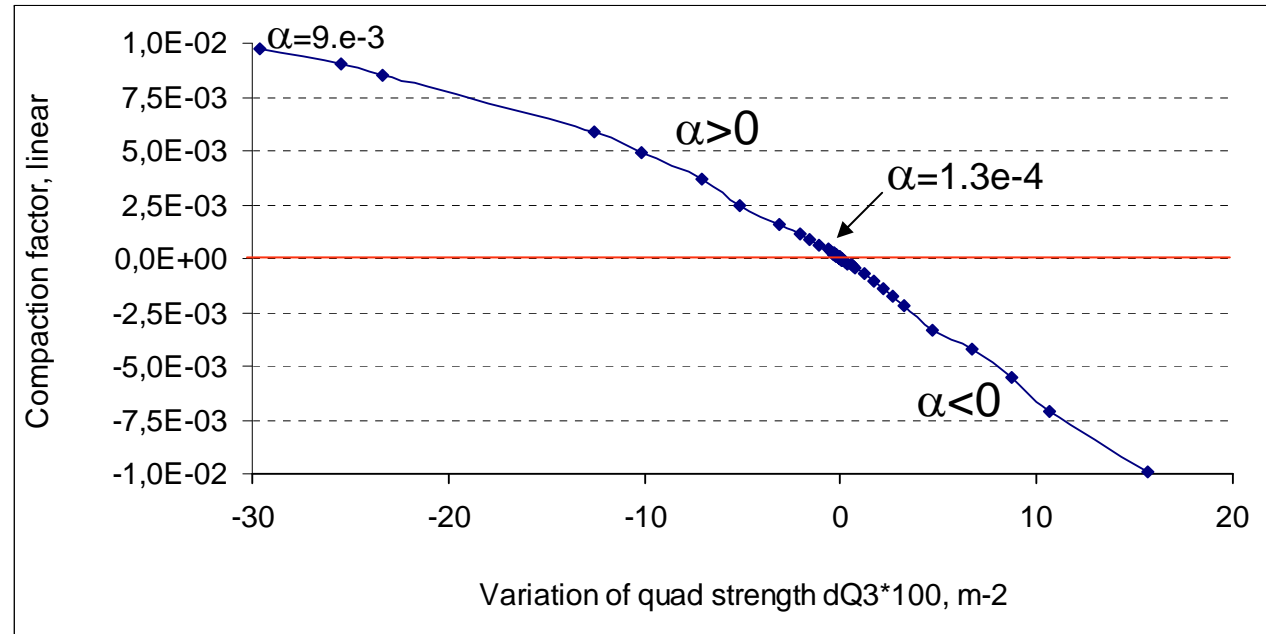
Linear scale

“zero“ is point where

alpha = 0

i.e. transition from

positive to negative value

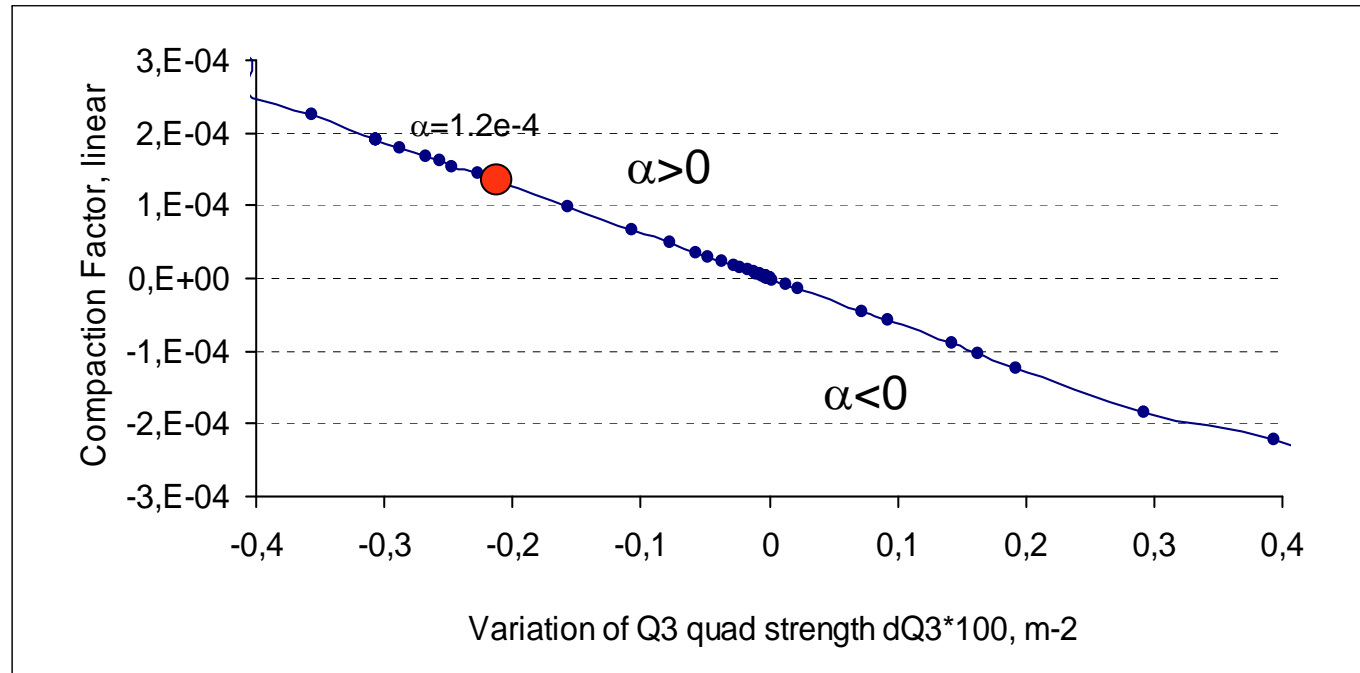


OPA simulations

**ZOOMED**

**Transition of compaction factor from positive to negative value.**

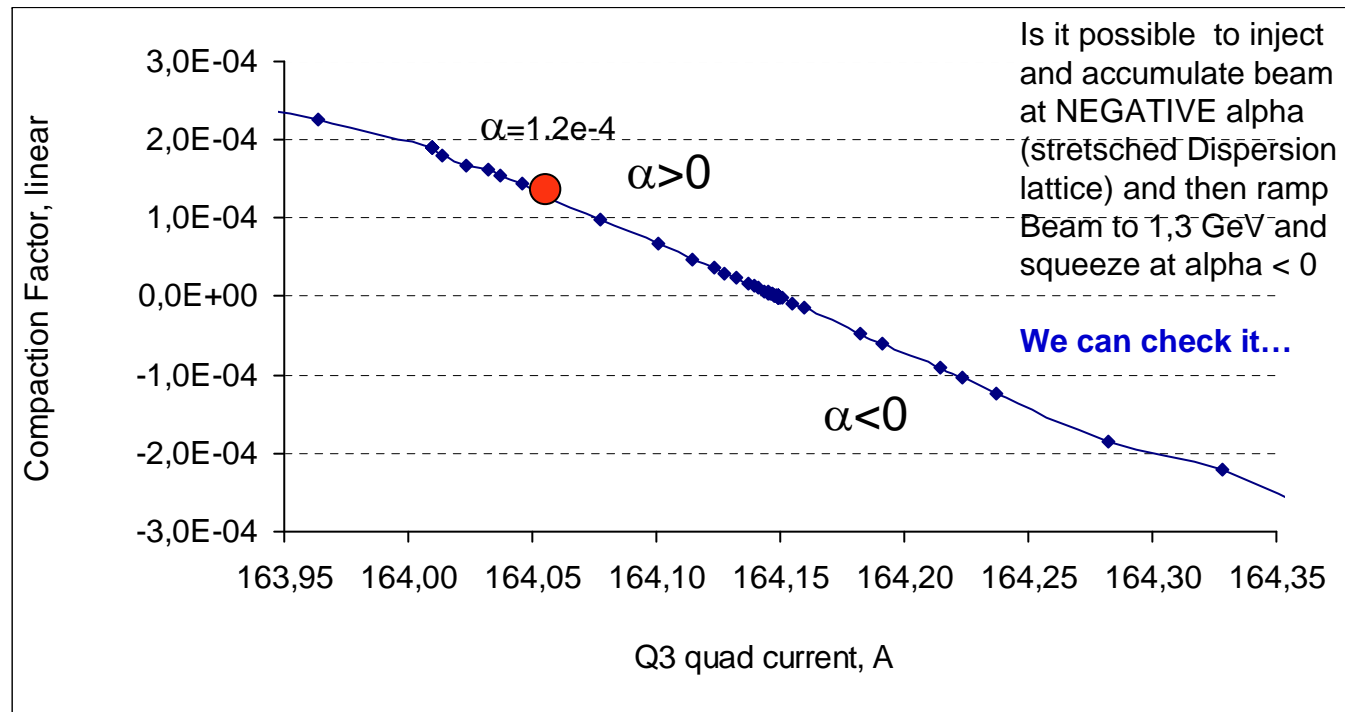
**Linear scale**



“zero“ is point where

$\alpha = 0$

i.e. transition from positive to negative value



# Transition of compaction factor from positive to negative value.

## Logarithmic scale

“zero“ is point where  
 $\alpha = 0$   
 i.e. transition from  
 positive to negative value

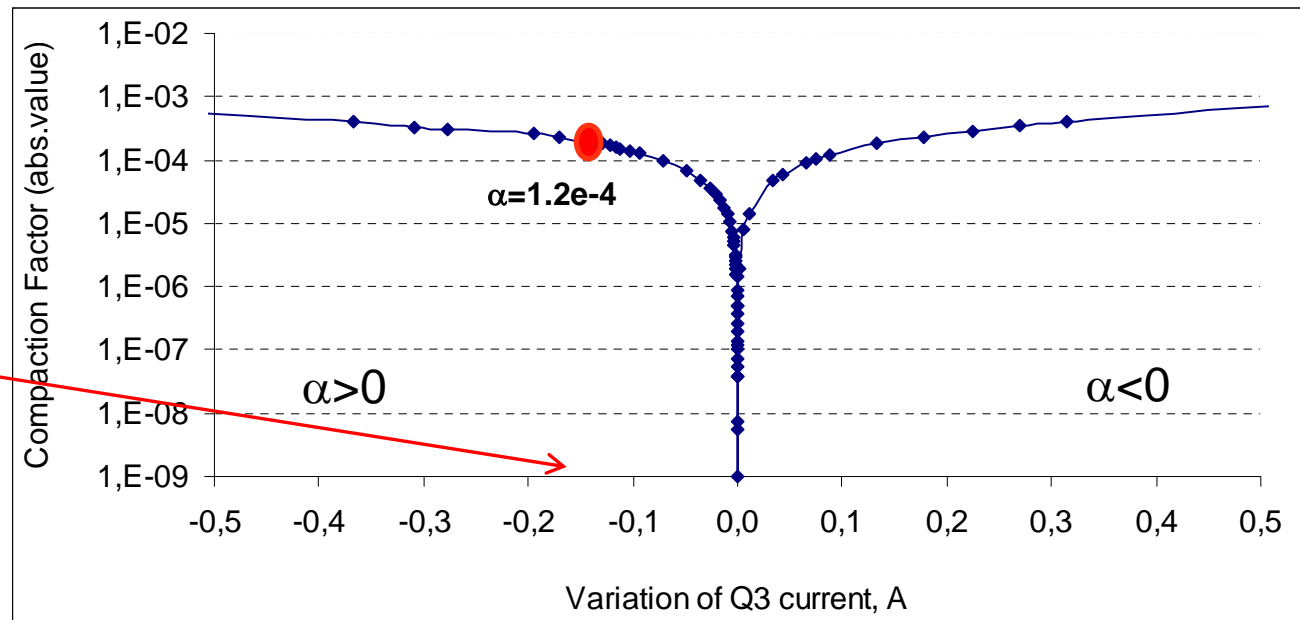
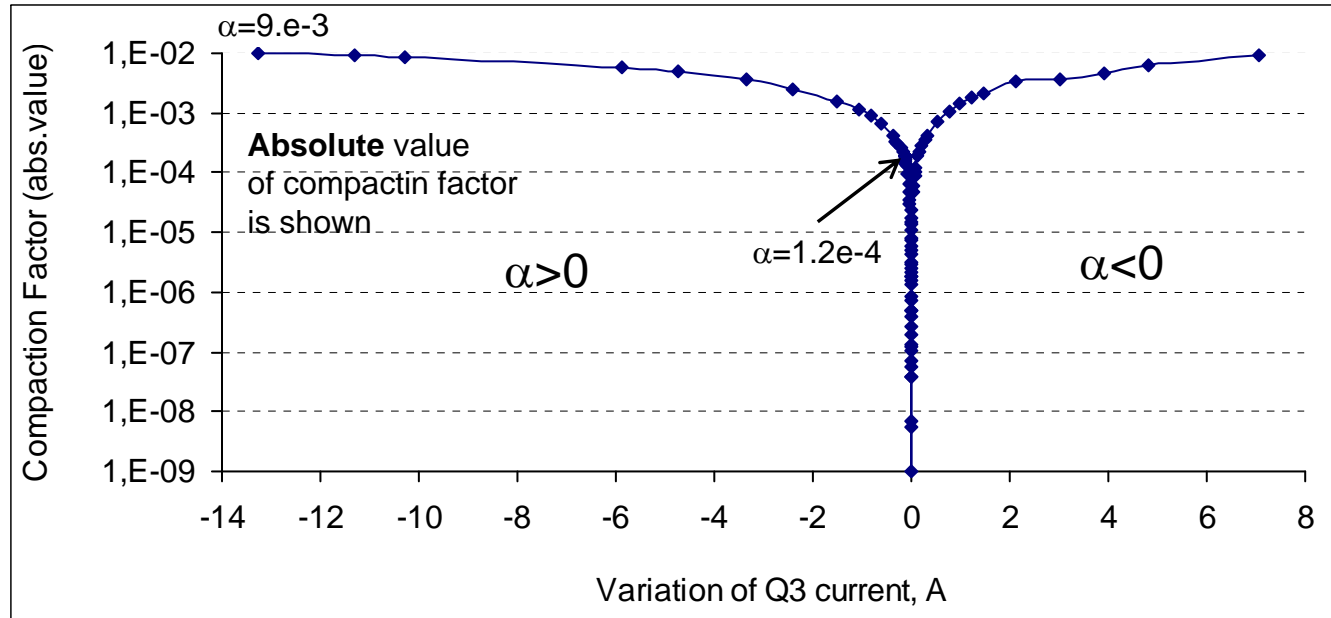
**For discussion:**

Assuming the beam is lost due to fluctuation of  
**COMPACTION FACTOR to ZERO**  
 value  
 because of the unstable gradient of quads field  
 and/or magnetic rigidity of bends  
 one could roughly estimate  
 stability of PSQ  
 to

$\delta/I = 1.e-3$  ???

Is it the case that the min allowable alpha at KARA is  $1.2e-4$  ???

One should check last measurements of alpha  $\approx 5.5 e-5$





# Zero current Bunch length

