

Diffractive quarkonium production in association with a photon at the LHC*

Maria Beatriz Gay Ducati
GFPAE – IF – UFRGS
www.if.ufrgs.br/gfpae
beatriz.gay@ufrgs.br

* Refer to work: [arXiv:hep/0908.0507](https://arxiv.org/abs/hep/0908.0507)



Outlook

- Motivation
- Diffractive Physics
- Hadroproduction quarkonium + photon
- Pomeron Structure Function
- Multiple Pomeron Scattering
- Results
- Conclusions



Motivation

- ✓ Higher statistics of small-x and hard diffractive processes



intensive experimental study

- ✓ Has been used to improve the knowledge about QCD

- ✓ Several mechanisms for quarkonium production in hadron colliders



Color singlet model

Color octet model¹

Color evaporation model

- ✓ Cross section for quarkonium production  gluon densities

- ✓ Pomeron with substructure  gluons

- ✓ Heavy quarkonium production  clean signature through leptonic decay modes



Introduction

- ❖ Diffractive processes → overall cross sections
- ❖ Regge Theory → exchange of a **Pomeron** with vacuum quantum numbers
- ❖ Nature of the Pomeron and its reaction mechanisms² → **not completely known**
- ❖ Use of hard scattering → quark and gluon content in the Pomeron
- ❖ Observations of diffractive deep inelastic scattering (DDIS) at HERA (1994)
- ❖ Increased the knowledge about the QCD Pomeron
- ❖ Diffractive Distributions of singlet quarks and gluons in the Pomeron

Diffractive structure function

Diffractive events

- ❖ Both colliding hadrons remain intact as they emit a Pomeron each

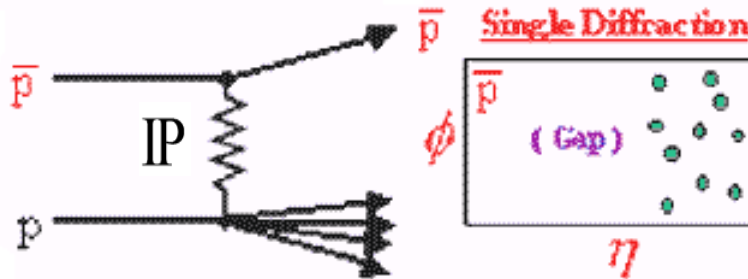


Central diffractive events

- ❖ Single diffraction in hadronic collisions



one of the colliding hadrons emits Pomeron that scatters off the other hadron



- ❖ Hard diffractive events with a large momentum transfer

Absence of hadronic energy in certain angular regions of the final state phase space



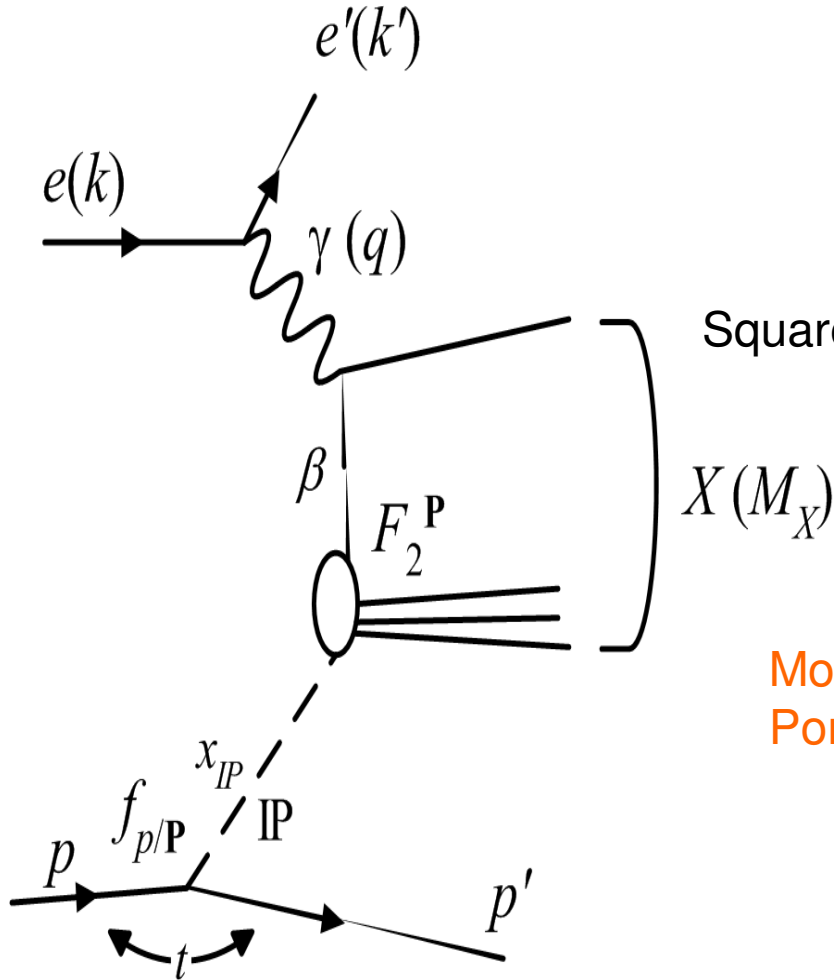
Rapidity gaps



Diffractive Physics

3

Ingelman-Schlein Model



$$t = (p - p')^2$$

Squared of the proton's four-momentum transfer

$X(M_X)$

$$x_{IP} = \frac{Q^2 + M_X^2 - t}{Q^2 + W^2}$$

Momentum fraction of the proton carried by the Pomeron

$$\beta = \frac{Q^2}{Q^2 + M_X^2 - t} = \frac{x}{x_{IP}}$$

Momentum fraction of partons inner the Pomeron

6



Diffractive hadroproduction

- o Focus on the following single diffractive processes

$$pp \rightarrow p + (J / \psi + \gamma) + X \qquad pp \rightarrow p + (Y + \gamma) + X$$

- o Diffractive ratios as a function of transverse momentum p_T of quarkonium state

- o Quarkonia produced with large p_T \longrightarrow easy to detect

- o **Singlet contribution**

$$g + g \rightarrow \gamma + (c\bar{c})(^3S_1^{(1)})(\rightarrow J/\psi)$$

- o **Octet contributions**



$$g + g \rightarrow \gamma + (c\bar{c})(^1S_0^{(8)})(\rightarrow J/\psi),$$

$$g + g \rightarrow \gamma + (c\bar{c})(^3P_J^{(8)})(\rightarrow J/\psi),$$

- o Higher contribution on high p_T ⁴



J/ ψ + γ production

- ✓ Considering the Non-relativistic Quantum Chromodynamics (NRQCD)
- ✓ Gluons fusion dominates over quarks annihilation ⁴
- ✓ Leading Order cross section  convolution of the partonic cross section with the PDF
- ✓ MRST 2001 LO  no relevant difference using MRST 2002 LO and MRST 2003 LO
- ✓ Non-perturbative aspects of quarkonium production
 - Expansion in powers of v
 - v is the relative velocity of the quarks in the quarkonia

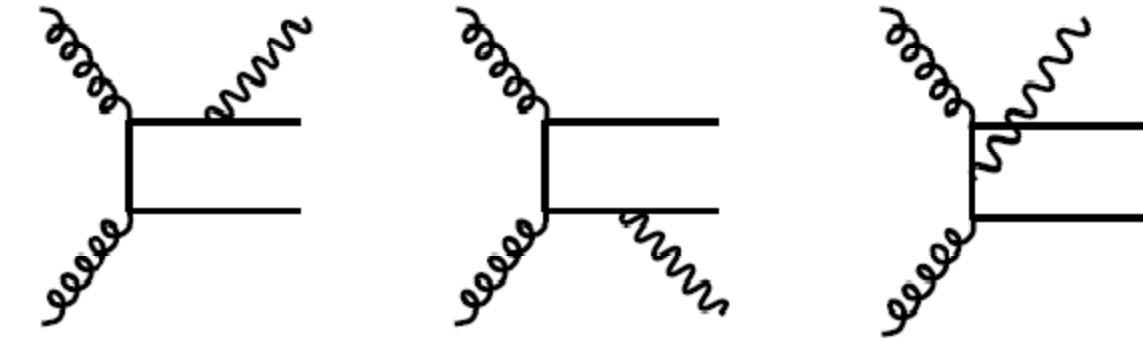
NLO expansions in α_s
 as one virtual correction
 and three real
 corrections



Quarkonium + photon production

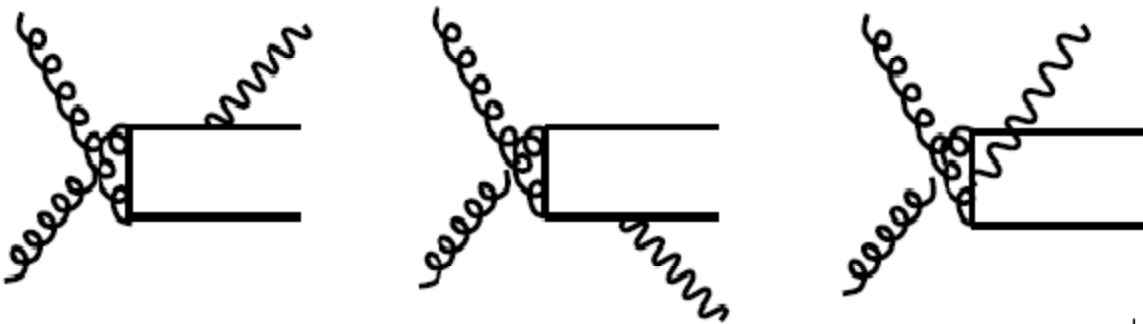
5

Singlet subprocess



No gluon interactions

$$g + g \rightarrow (c\bar{c})(^3S_1^{(1)}) + \gamma$$



Gluon interactions

$$g + g \rightarrow (c\bar{c})(^1S_0^{(8)}, ^3P_J^{(8)}) + \gamma$$

Octet subprocess



NRQCD Factorization

$$g + g \rightarrow \gamma + (c\bar{c}) [{}^3S_1^1, {}^3S_1^8]$$

$$g + g \rightarrow \gamma + (c\bar{c}) [{}^1S_0^8, {}^3P_J^8]$$

□ Negligible contribution of quarks annihilation at high energies⁶

$$\frac{d^2\sigma_{\text{inc}}}{dydp_T} = \int dx_1 g_p(x_1, \mu_F^2) g_p(x_2, \mu_F^2) \frac{4x_1x_2p_T}{2x_1 - \bar{x}_T e^y} \frac{d\hat{\sigma}}{d\hat{t}}$$

$$\bar{x}_T = 2m_T/\sqrt{s} \qquad m_T = \sqrt{p_T^2 + m_\psi^2}$$

J/ψ rapidity
9.2 GeV²

\sqrt{s} is the center mass energy (LHC = 14 TeV)



NRQCD factorization

✓ $x_1(x_2)$ is the momentum fraction of the proton carried by the gluon

$M^2/s \leq x_1 < 1$ $M \longrightarrow$ invariant mass of $J/\psi + \gamma$ system

$$x_2 = \frac{x_1 \bar{x}_T e^{-y} - 2\tau}{2x_1 - \bar{x}_T e^y} \qquad \tau = \frac{m_\psi^2}{s}$$

✓ Cross section written as

$$\sigma(H) = \sum_n c_n \langle 0 | O_n^H | 0 \rangle$$

Coefficients are computable in perturbation theory

Matrix elements of NRQCD operators



Matrix elements

$$\langle 0 | O_n^H | 0 \rangle = \sum_X \sum_\lambda \langle 0 | \kappa_n^\dagger | H(\lambda) + X \rangle \langle H(\lambda) + X | \kappa_n | 0 \rangle$$

Bilinear in heavy quarks fields which create as a pair $Q\bar{Q}$ Quarkonium state ⁷

$$\begin{aligned} \frac{d\sigma}{dt}(g + g \rightarrow J/\psi + \gamma) = & \frac{\pi^2 e_c^2 \alpha \alpha_s^2 m_c}{s^2} \left[\frac{10}{9} \left(\frac{s^2 s_1^2 + t^2 t_1^2 + u^2 u_1^2}{s_1^2 t_1^2 u_1^2} \right) \langle O_8^{J/\psi}(^3S_1) \rangle \right. \\ & + \frac{16}{27} \left(\frac{s^2 s_1^2 + t^2 t_1^2 + u^2 u_1^2}{s_1^2 t_1^2 u_1^2} \right) \langle O_1^{J/\psi}(^3S_1) \rangle + \frac{3}{2} \frac{tu}{s s_1^2 m_c^2} \langle O_8^{J/\psi}(^3S_1) \rangle \\ & \left. + \frac{3}{2} \frac{1}{s s_1^2 m_c^4} \left(2s(2m_c)^2 + 3tu - \frac{4tu(2m_c)^2}{s_1} \right) \langle O_8^{J/\psi}(^1P_0) \rangle \right], \end{aligned}$$

$$s_1 = s - 4m_c^2, \quad t_1 = t - 4m_c^2, \quad u_1 = u - 4m_c^2 \qquad e_c = \frac{2}{3}$$

α_s running



Matrix elements (GeV³)^{8,9}

$\langle O_1^{J/\psi} (^3S_1) \rangle$	1.16	$\langle O_1^{\Upsilon} (^3S_1) \rangle$	10.9
$\langle O_8^{J/\psi} (^3S_1) \rangle$	1.19×10^{-2}	$\langle O_8^{\Upsilon} (^3S_1) \rangle$	0.02
$\langle O_8^{J/\psi} (^1S_0) \rangle$	0.01	$\langle O_8^{\Upsilon} (^1S_0) \rangle$	0.136
$\langle O_8^{J/\psi} (^1P_0) \rangle$	$0.01 \times m_c^2$	$\langle O_8^{\Upsilon} (^1P_0) \rangle$	0

$$e_b = -\frac{1}{3}$$

$$m_b = 4.5 \text{ GeV}$$

$$m_Y = 9.46 \text{ GeV}/c^2$$

Diffractive cross section

$$\frac{d^2\sigma_{SD}}{dy dp_T} = \int_{x_{\mathbb{P}}^{min}}^{x_{\mathbb{P}}^{max}} dx_{\mathbb{P}} \int_{\frac{M^2}{sx_{\mathbb{P}}}}^1 dx_1 \int_{-1}^0 dt f_{\mathbb{P}/p}(x_{\mathbb{P}}, t) \times g_{\mathbb{P}}(x_{\mathbb{P}}, \mu_F^2) g_p(x_2, \mu_F^2) \frac{4x_1 x_{\mathbb{P}} x_2 p_T}{2x_1 x_{\mathbb{P}} - \bar{x}_T e^y} \frac{d\hat{\sigma}}{d\hat{t}}$$

Momentum fraction carried by the Pomeron

Squared of the proton's four-momentum transfer

Pomeron flux factor $f_{\mathbb{P}/p}(x_{\mathbb{P}}, t) \propto x_{\mathbb{P}}^{1-2\alpha(t)} F^2(t)$

$\alpha(t) = \alpha_{\mathbb{P}}(0) + \alpha'_{\mathbb{P}} t$ Pomeron trajectory



Variables to DDIS

Cuts for the integration over $x_{\mathbb{P}}$

$$x_{\mathbb{P}}^{\min} \leq x_{\mathbb{P}} \leq 0.05 \qquad x_{\mathbb{P}}^{\min} = \frac{\bar{x}_T e^y - 2\tau}{\bar{x}_T e^{-y} - 2}$$

Scales

$$Q_0^2 = 2.5 \text{ GeV}^2 \qquad \Lambda_{\text{QCD}} = 0.2 \qquad \mu_F^2 = \frac{(p_T^2 + m_\psi^2)}{4}$$

$$x_2 = \frac{x_1 x_{\mathbb{P}} \bar{x}_T e^{-y} - 2\tau}{2x_1 x_{\mathbb{P}} - \bar{x}_T e^y},$$

$$\hat{s} = x_1 x_2 x_{\mathbb{P}} s, \qquad \hat{t} = m_\psi^2 - x_2 \sqrt{s} m_T e^y$$

$$\hat{u} = m_\psi^2 - x_1 x_{\mathbb{P}} \sqrt{s} m_T e^{-y}.$$



Pomeron structure function

Parametrization of the pomeron flux factor and structure function ➔ **H1 Collaboration** ¹⁰

$$f_{\mathbb{P}/p}(x_{\mathbb{P}}, t) = A_{\mathbb{P}} \frac{e^{B_{\mathbb{P}}t}}{x_{\mathbb{P}}^{2\alpha_{\mathbb{P}}(t)-1}}$$

$$\alpha_{\mathbb{P}}(t) = \alpha(0) + \alpha'_{\mathbb{P}}t$$

$A_{\mathbb{P}}$ ➔ Normalization parameter

$$|t_{min}| \approx m_p^2 x_{\mathbb{P}}^2 / (1 - x_{\mathbb{P}})$$

m_p = proton mass

$$x_{\mathbb{P}} \int_{t_{cut}}^{t_{min}} f_{\mathbb{P}/p} dt = 1$$

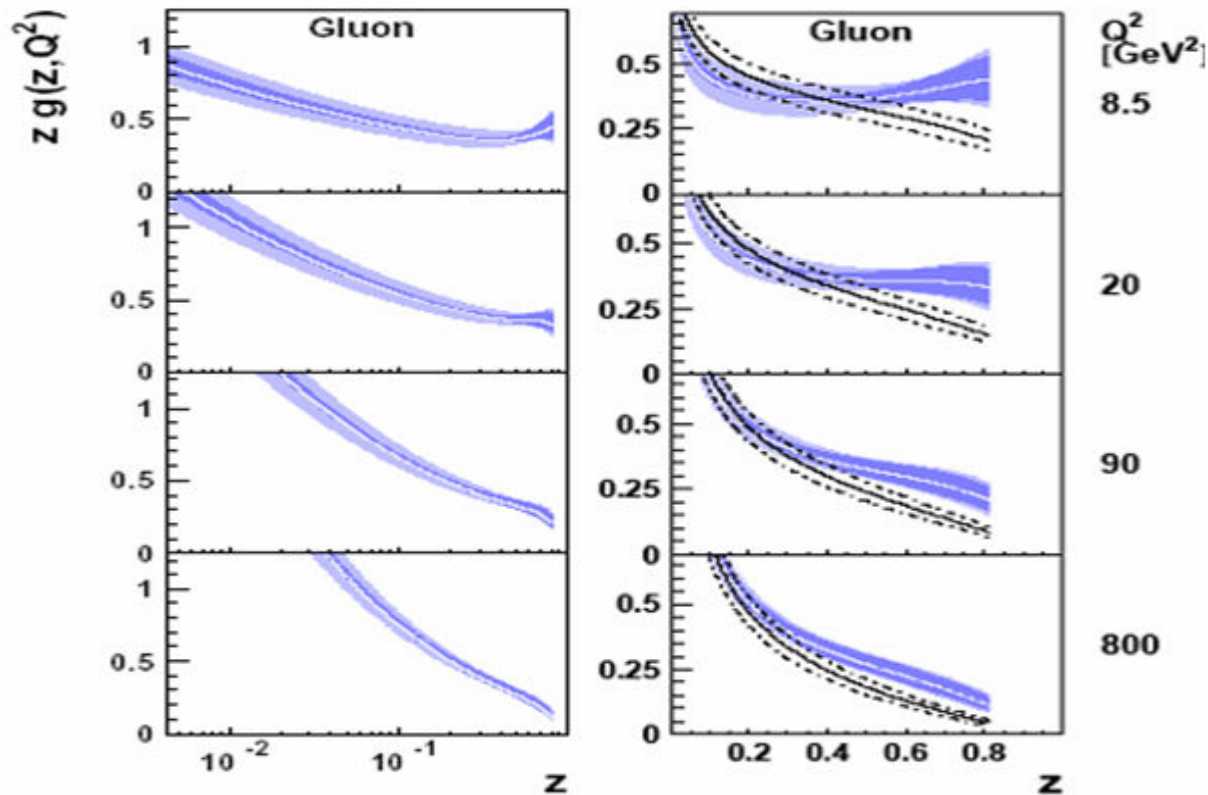
Normalized for $x_{\mathbb{P}} = 0.003$

$$|t_{cut}| = 1.0 \text{ GeV}^2$$

<i>Parameter</i>	<i>Value</i>
α'_{IP}	$0.06^{+0.19}_{-0.06} \text{ GeV}^2$
B_{IP}	$5.5^{+2.0}_{-0.7} \text{ GeV}^2$
$\alpha_{IR}(0)$	0.50 ± 0.10
α'_{IR}	$0.3^{+0.6}_{-0.3} \text{ GeV}^2$
B_{IR}	$1.6^{+1.6}_{-0.4} \text{ GeV}^2$
m_c	$1.4 \pm 0.2 \text{ GeV}$
m_b	$4.5 \pm 0.5 \text{ GeV}$
$\alpha_8^{(5)}(M_Z^2)$	0.118 ± 0.002



Gluon distribution



- Range $0.0043 < z < 0.8$
- Same of experiment
- In this work we use FIT A.
- Similar results with FIT B

H1 2006 DPDF Fit A
■ (exp. error)
■ (exp.+theor. error)

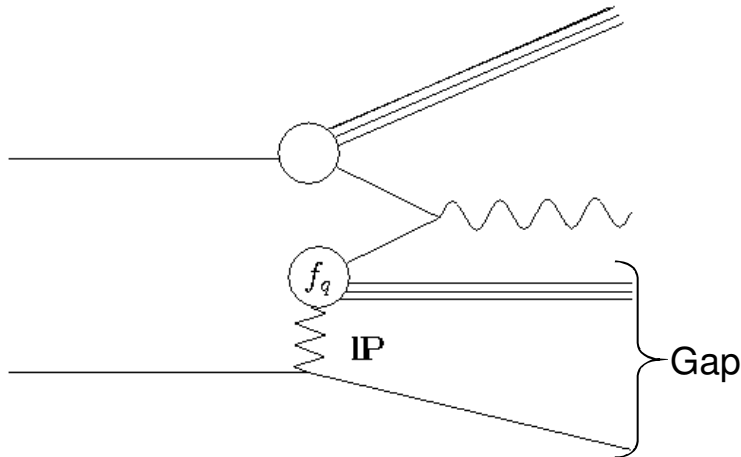
— H1 2006 DPDF Fit B
- - - (exp.+theor. error)

Fit A (and uncertainties) → color center line

Fit B (and uncertainties) → black line



Gap Survival Probability (GSP)



- Described in terms of screening or absorptive corrections
- Multiple Pomeron effects \longrightarrow absorptive corrections
- $\langle |S|^2 \rangle \longrightarrow$ gap survival probability (GSP)

$$\langle |S|^2 \rangle = \frac{\int d^2b |A(s, b)|^2 P^s(b, s)}{\int d^2b |A(s, b)|^2}$$

- $A(s, b) \longrightarrow$ amplitude of the particular diffractive process of interest
- $P^s(s, b) \longrightarrow$ probability that no inelastic interactions occur between scattering hadrons

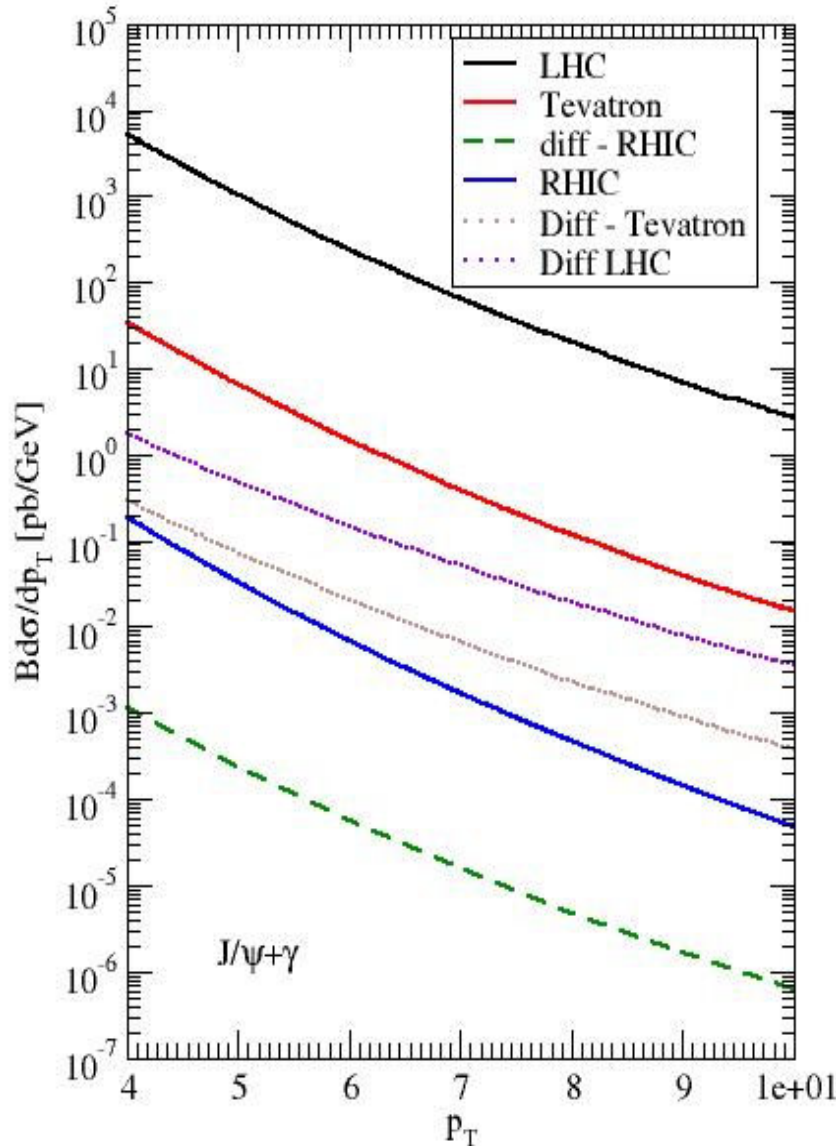


KKMR model

KKMR description to hadronic collisions embodies:¹¹

- **Pion-loop insertions** in the bare Pomeron pole \longrightarrow nearest singularity generated by t-channel unitarity
- **Two-channel eikonal** \longrightarrow incorporates Pomeron cuts generated by elastic and quasi-elastic s-channel unitarity
- **High-mass diffractive dissociation**
Multiple Pomeron effects \longrightarrow absorptive corrections
- Good description of the data of the total and differential elastic cross section
- Value of $\langle |S|^2 \rangle = 0.06$ at LHC single diffractive events

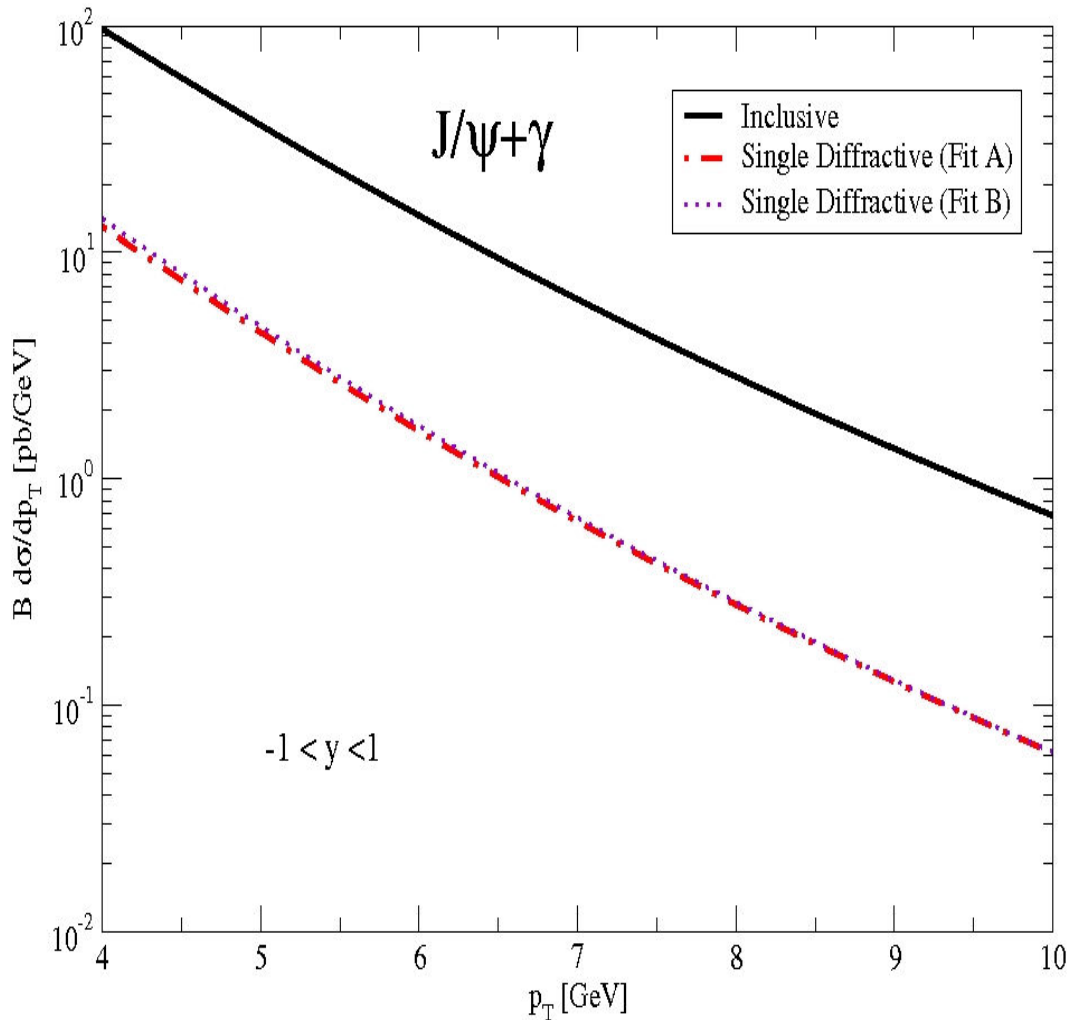
Results to $J/\psi + \gamma$




- Predictions for inclusive and diffractive cross sections
- RHIC, Tevatron and LHC
- Diffractive cross sections considering GSP ($\langle |S|^2 \rangle$)
- Reproduces descriptions of ⁵
 $-1 < |y| < 1$
- $B = 0.0594$ is the branching ratio into electrons

$1 \leq p_T \leq 20$ at LHC¹²

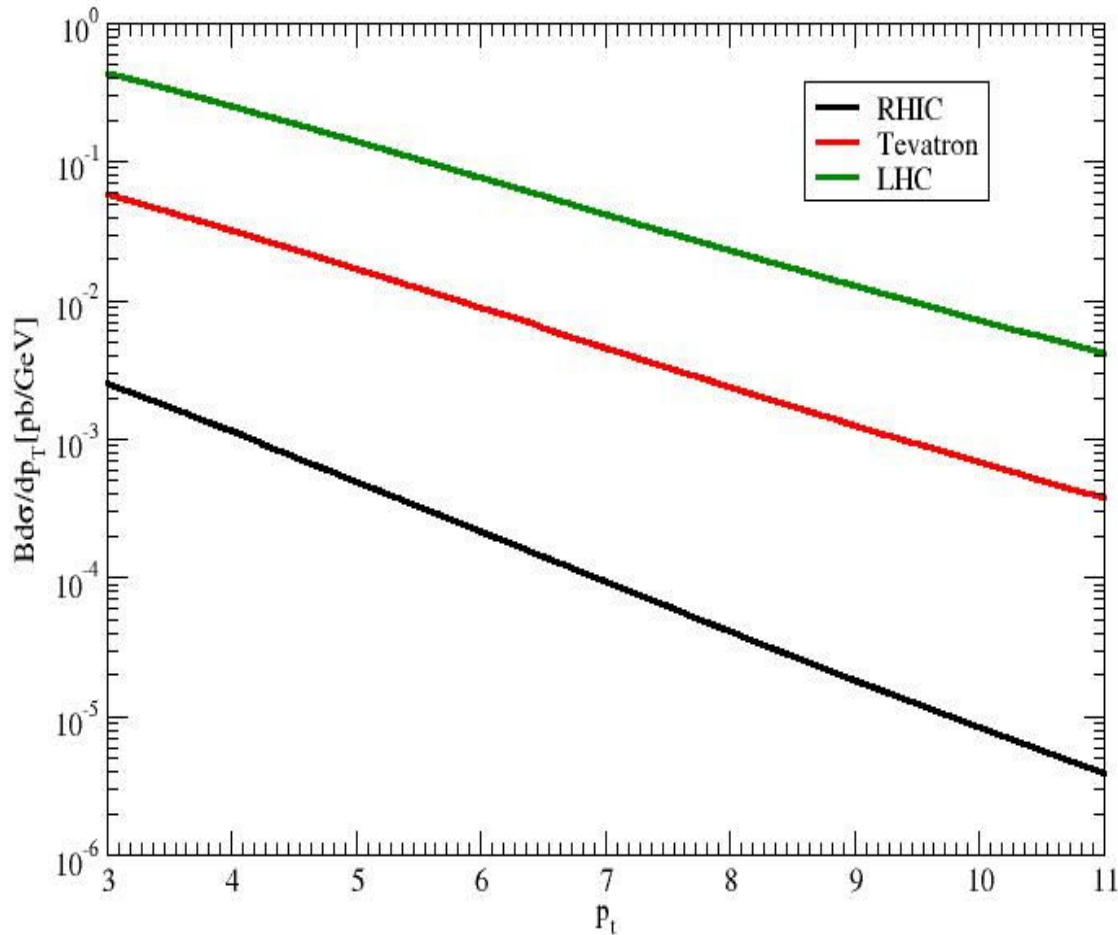
Results to $J/\psi + \gamma$ at LHC



- $B = 0.0594$
 - Absolute value of inclusive cross section strongly dependent
 - Quark mass
 - NRQCD matrix elements
 - Factorization scale
 - Diffractive cross sections (DCS) without GSP
 - Comparison between two different sets of diffractive gluon distribution (H1)
 - Absolute value of DCS
- weakly sensitive to the uncertainties of DPDF 



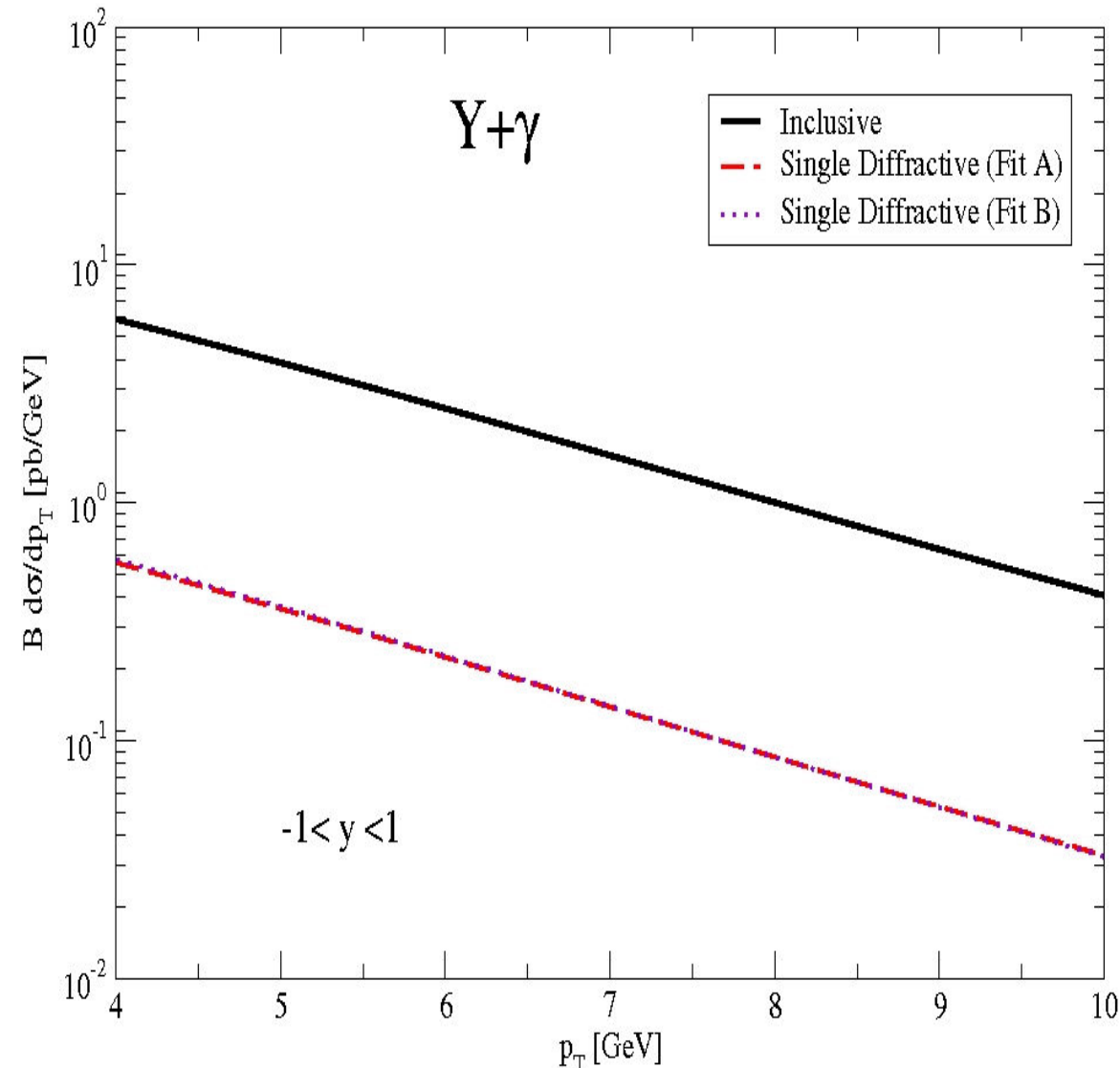
Results to $Y+\gamma$



- Predictions of inclusive cross section
- RHC, Tevatron and LHC
 $-1 < |y| < 1$
- $B = 0.0238$ is the branching ratio into electrons



Results to $Y+\gamma$ at LHC



- $B = 0.0238$
- Absolute value of inclusive cross section strongly dependent
 - Quark mass
 - NRQCD matrix elements
 - Factorization scale
- Diffractive cross sections (DCS) without GSP ($\langle |S|^2 \rangle$)
- Comparison between two different sets of diffractive gluon distribution (H1)
- Dependence of FITs are slight more pronounced in charmonium case



Diffractive ratio

[σ] = pb
considering FIT A

p_T [GeV]	4	5	6	7	8	9	10
$\frac{d\sigma_{inc}}{dp_T} (J/\Psi)$	97.04	36.46	14.54	6.21	2.82	1.36	0.68
$\frac{d\sigma_{SD}}{dp_T} (J/\Psi)$	0.78	0.26	0.10	0.04	0.017	0.008	0.0036
$R_{SD} [\%] (J/\Psi)$	0.8	0.71	0.69	0.64	0.6	0.59	0.53
$\frac{d\sigma_{inc}}{dp_T} (\Upsilon)$	5.91	3.88	2.49	1.58	1.00	0.64	0.41
$\frac{d\sigma_{SD}}{dp_T} (\Upsilon)$	0.036	0.022	0.013	0.008	0.0054	0.003	0.0018
$R_{SD} [\%] (\Upsilon)$	0.6	0.56	0.53	0.51	0.54	0.47	0.44

➤ Slight large diffractive ratio

in comparison to ⁵



❖ Could explain the p_T dependence

in our results

This work	Ref ⁵
$\mu_F = \sqrt{\frac{(p_T^2 + m_\psi^2)}{4}}$	$\mu_F = E_T$
$\langle S ^2 \rangle = 0.06$	Renormalized Pomeron flux
Evolution of Q^2 in gluon density	No evolution of Q^2



Conclusions

- Theoretical prediction for inclusive and single diffractive quarkonium + photon production at LHC energy in pp collisions
- Estimates for differential cross sections as a function of quarkonium transverse momentum
- Diffractive ratio is computed using hard diffractive factorization and absorptive corrections
- Ratios are less dependent on the heavy quarkonium production mechanism
- Quite sensitive to the absolute value of absorptive corrections
- Distribution on $4 \leq p_T \leq 10$  $R^{(J/\psi)}_{SD} = 0,8 - 0,5 \%$
 $R^{(\Upsilon)}_{SD} = 0,6 - 0,4 \%$
- Next step  Next-to-Leading Order