## DIFFRACTIVE ASPECTS OF HIGGS PRODUCTION

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- GLMM model for high energy soft interactions incorporating multi eikonal scattering plus multi-Pomeron vertices.
- Hard matrix element
- Comparison with competing models
- Estimates of Survival Probability for Central Higgs production at LHC.
- Summary


## Good-Walker Formalism-2

Unitarity constraints:

$$
\operatorname{Im} A_{i, k}(s, b)=\left|A_{i, k}(s, b)\right|^{2}+G_{i, k}^{i n}(s, b)
$$

$G_{i, k}^{i n}$ is the contribution of all non diffractive inelastic processes
i.e. it is the summed probability for these final states to be produced in the scattering of particle $i$ off particle $k$.

A simple solution to the above equation is:

$$
\begin{gathered}
A_{i, k}(s, b)=i\left(1-\exp \left(-\frac{\Omega_{i, k}(s, b)}{2}\right)\right) \\
G_{i, k}^{i n}(s, b)=1-\exp \left(-\Omega_{i, k}(s, b)\right)
\end{gathered}
$$

## Good-Walker Formalism-3

Note

$$
P_{i, k}^{S}=\exp \left(-\Omega_{i, k}(s, b)\right)
$$

is the probability that the initial projectiles $(i, k)$ reach the final state interaction unchanged, regardless of the initial state rescatterings, (i.e. no inelastic interactions).

Amplitudes in two channel formalism are:

$$
\begin{gathered}
a_{e l}(s, b)=i\left\{\alpha^{4} A_{1,1}+2 \alpha^{2} \beta^{2} A_{1,2}+\beta^{4} A_{2,2}\right\}, \\
a_{s d}(s, b)=i \alpha \beta\left\{-\alpha^{2} A_{1,1}+\left(\alpha^{2}-\beta^{2}\right) A_{1,2}+\beta^{2} A_{2,2}\right\}, \\
a_{d d}=i \alpha^{2} \beta^{2}\left\{A_{1,1}-2 A_{1,2}+A_{2,2}\right\} .
\end{gathered}
$$

With the G-W mechanism $\sigma_{e l}, \sigma_{s d}$ and $\sigma_{d d}$ occur due to elastic scattering of $\psi_{1}$ and $\psi_{2}$, the correct degrees of freedom.

## Opacities $\Omega_{i, k}$

$$
\Omega_{i, k}(s, b)=g_{i} g_{k}\left(\frac{s}{s_{0}}\right)^{\Delta_{\mathbb{P}}} S\left(b ; m_{i}, m_{k} ; \alpha_{\mathbb{P}}^{\prime} \ln \left(s / s_{0}\right)\right)
$$

The profile function
$S\left(b, \alpha_{P}^{\prime} ; m_{i}, m_{k} ; \ln \left(s / s_{0}\right)\right)$ at $s=s_{0}$,
corresponds to the power-like behaviour of the Pomeron-hadron vertices

$$
S\left(b ; m_{i}, m_{k} ; \alpha_{\mathbb{P}}^{\prime} \ln \left(s / s_{0}\right)=0\right)=\int \frac{d^{2} q}{(2 \pi)^{2}} g_{i}(q) g_{k}(q) e^{i \vec{q}_{\perp} \cdot \vec{b}}
$$

We choose

$$
g_{i}(q)=\frac{1}{\left(1+q^{2} / m_{i}^{2}\right)^{2}}
$$

## Opacities $\Omega_{i, k}$ contd.

We obtain for $S\left(b ; m_{i}, m_{k} ;, \alpha_{I P}^{\prime} \ln \left(s / s_{0}\right)=0\right)$

$$
\begin{aligned}
& \frac{1}{\left(1+q^{2} / m_{i}^{2}\right)^{2}} \times \frac{1}{\left(1+q^{2} / m_{k}^{2}\right)^{2}}, \Longrightarrow S\left(b ; m_{i}, m_{k} ;, \alpha_{\mathbb{P}}^{\prime} \ln \left(s / s_{0}\right)=0\right)= \\
& =\frac{m_{i}^{3} m_{k}^{3}}{4 \pi\left(m_{i}^{2}-m_{k}^{2}\right)^{3}} . \\
& \left\{4 m_{i} m_{k}\left(K_{0}\left(m_{i} b\right)-K_{0}\left(m_{k} b\right)\right)+\left(m_{i}^{2}-m_{k}^{2}\right) b\left(m_{k} K_{1}\left(m_{i} b\right)+m_{i} K_{1}\left(m_{k} b\right)\right)\right\} .
\end{aligned}
$$

TAU Parameters for the two channel model fit to elastic processes

$$
\sigma_{t o t}(s), \sigma_{e l}(s) \text { and } B_{e l}(s)
$$

| $\Delta_{\mathbb{P}}$ | $\beta$ | $\alpha_{I P}^{\prime}$ | $g_{1}$ | $g_{2}$ | $m_{1}$ | $m_{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.120 | 0.46 | $0.012 \mathrm{GeV}^{-2}$ | $1.27 \mathrm{GeV}^{-1}$ | $3.33 \mathrm{GeV}^{-1}$ | 0.913 GeV | 0.98 GeV |
| $\Delta_{\mathbb{R}}$ | $\beta$ | $\alpha_{\mathbb{}}^{\prime}$ | $g_{1}^{R R}$ | $g_{2}^{I R}$ | $R_{0,1}^{2}$ | $\chi^{2} /$ d.o.f. |
| -0.438 | 0.46 | $0.60 \mathrm{GeV}^{-2}$ | $4.0 \mathrm{GeV}^{-1}$ | $118.4 \mathrm{GeV}^{-1}$ | $4.0 \mathrm{GeV}^{-2}$ | 0.87 |

- With the above parameters the predicted values for $\sigma_{s d}(s)$ and $\sigma_{d d}(s)$ are much smaller than measured values.
- In G-W formalism something is missing in the diffractive channels.
- LARGE MASS DIFFRACTION


## Examples of Pomeron diagrams

## leading to diffraction NOT included in G-W mechanism



Examples of the Pomeron diagrams that lead to a different source of the diffractive dissociation that cannot be described in the framework of the G-W mechanism. (a) is the simplest diagram that describes the process of diffraction in the region of large mass $Y-Y_{1}=\ln \left(M^{2} / s_{0}\right)$. (b) and (c) are examples of more complicated diagrams in the region of large mass. The dashed line shows the cut Pomeron, which describes the production of hadrons.

## Example of enhanced and semi-enhanced diagram



Different contributions to the Pomeron Green's function a) examples of enhanced diagrams (which are included); b) examples of semi-enhanced diagrams (which have not yet been included in most of our calculations)
Multi-Pomeron interactions are crucial for the production of LARGE MASS DIFFRACTION

## Tel Aviv approach for summing interacting Pomeron diagrams

In the spirit of LO pQCD we write a generating function

$$
Z(y, u)=\sum_{n} P_{n}(y) u^{n}
$$

$P_{n}(y)$ is the probability to find $n$-Pomerons (dipoles) at rapidity $y$. The solution, with boundry conditions, gives us the sum of enhanced diagrams.

For the function $Z(u)$ the following evolution equation can be written

$$
-\frac{\partial Z(y, u)}{\partial y}=-\Gamma(1 \rightarrow 2) u(1-u) \frac{\partial Z(y, u)}{\partial u}+\Gamma(2 \rightarrow 1) u(1-u) \frac{\partial^{2} Z(y, u)}{\partial^{2} u}
$$

$\Gamma(1 \rightarrow 2)$ describes the decay of one Pomeron (dipole) into two Pomerons (dipoles), while $\Gamma(2 \rightarrow 1)$ relates to the merging of two Pomerons (dipoles) into one Pomeron (dipole).

Tel Aviv approach for summing interacting Pomeron diagrams contd.
Using the functional $Z$, we find the scattering amplitude, using the following formula:

$$
N(Y) \equiv \operatorname{Im} A_{e l}(Y)=\left.\sum_{n=1}^{\infty} \frac{(-1)^{n}}{n!} \frac{\partial^{n} Z(y, u)}{\partial^{n} u}\right|_{u=1} \gamma_{n}\left(Y=Y_{0}, b\right),
$$

$\gamma_{n}\left(Y=Y_{0}, b\right)$ is the scattering amplitude of $n$-partons (dipoles) at low energy.
Using the MPSI approximation (where only large $\mathbb{P}$ loops of rapidity size $\mathrm{O}(Y)$ contribute) we obtain the exact Pomeron Green's function

$$
G_{\mathbb{P}}(Y)=1-\exp \left(\frac{1}{T(Y)}\right) \frac{1}{T(Y)} \Gamma\left(0, \frac{1}{T(Y)}\right)
$$

$\Gamma(0, x)$ is the incomplete gamma function and

$$
T(Y)=\gamma e^{\Delta_{\mathbb{P}} Y}
$$

$\gamma$ is the amplitude of the two dipoles interaction at low energy. MPSI approximation is only valid for $Y \leq \frac{1}{\gamma}$.

## MPSI Approximation



L.H. figure: The exact Green's function of the Pomeron versus $Y=\ln \left(s / s_{0}\right)$ and $T(Y)=\gamma e^{\Delta Y}$ for $\Delta=0.339$ and $\gamma=0.0242$. The values of the parameters were taken from our fit.
R.H. figure:(from Kozlov and Levin) Comparison of the exact solution for the Pomeron Green's function $G(Y)$ with $G(Y)$ in the MPSI approximation.

Parameters for our model fit includes G-W PLUS enhanced Pomeron diagrams

| $\Delta_{\mathbb{P}}$ | $\beta$ | $\alpha_{\mathbb{P}}^{\prime}$ | $g_{1}$ | $g_{2}$ | $m_{2}$ | $m_{1}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.335 | 0.339 | $0.012 G e V^{-2}$ | $5.82 G e V^{-1}$ | $239.6 G e V^{-1}$ | $1.54 G e V$ | $3.06 G e V$ |
| $\Delta_{\mathbb{R}}$ | $\gamma$ | $\alpha_{\mathbb{R}}^{\prime}$ | $g_{1}^{\mathbb{R}}$ | $g_{2}^{\mathbb{R}}$ | $R_{0,1}^{2}$ | $\chi^{2} /$ d.o. $f$. |
| -0.60 | 0.0242 | $0.6 \mathrm{GeV}^{-2}$ | $13.22 \mathrm{GeV}^{-1}$ | $367.8 G e V^{-1}$ | 4.0 | 1.0 |

For comparison parameters for the two channel model fit (only G-W processes)

| $\Delta_{\mathbb{P}}$ | $\beta$ | $\alpha_{\mathbb{P}}^{\prime}$ | $g_{1}$ | $g_{2}$ | $m_{1}$ | $m_{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.120 | 0.46 | $0.012 G e V^{-2}$ | $1.27 G e V^{-1}$ | $3.33 G e V^{-1}$ | $0.913 G e V$ | $0.98 G e V$ |
| $\Delta_{\mathbb{R}}$ | $\beta$ | $\alpha_{\mathbb{R}}^{\prime}$ | $g_{1}^{\mathbb{R}}$ | $g_{2}^{\mathbb{R}}$ | $R_{0,1}^{2}$ | $\chi^{2} / d . o . f$. |
| -0.438 | 0.46 | $0.60 \mathrm{GeV}^{-2}$ | $4.0 \mathrm{GeV}^{-1}$ | $118.4 \mathrm{GeV}^{-1}$ | $4.0 G e V^{-2}$ | 0.87 |

## Energy dependence of cross sections



Note that $\sigma_{e l}$ and $\sigma_{s d}$ have different energy behaviour.
$\mathrm{KMR}(08)$ predict that $\sigma_{e l}$ and $\sigma_{s d}$ have similar energy dependence.

## Comparison of results obtained in GLMM and KMR models

|  | Tevatron |  |  | LHC (14 TeV) |  |  | W=10 ${ }^{5} \mathrm{GeV}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | GLMM | MR(07) | KMR(08) | GLMM | MR(07) | KMR(08) | GLMM | MR(07) | KMR(08) |
| $\sigma_{t o t}(\mathrm{mb})$ | 73.3 | 74.0 | 73.7 | 92.1 | 88.0 | 91.7 | 108.0 | 98.0 | 108.0 |
| $\sigma_{e l}(\mathrm{mb})$ | 16.3 | 16.3 | 16.4 | 20.9 | 20.1 | 21.5 | 24.0 | 22.9 | 26.2 |
| $\sigma_{s d}(\mathrm{mb})$ | 9.8 | 10.9 | 13.8 | 11.8 | 13.3 | 19.0 | 14.4 | 15.7 | 24.2 |
| $\sigma_{d d}(\mathrm{mb})$ | 5.4 | 7.2 |  | 6.1 | 13.4 |  | 6.3 | 17.3 |  |
| $\frac{\sigma_{e l}+\sigma_{\text {diff }}}{\sigma_{\text {tot }}}$ | 0.43 | 0.46 |  | 0.42 | 0.53 |  | 0.41 | 0.57 |  |

At an energy of 7 TeV the predictions of GLLM are:

$$
\begin{aligned}
& \sigma_{t o t}=86.0 \mathrm{mb}, \sigma_{e l}=19.5 \mathrm{mb}, \sigma_{s d}=10.7 \mathrm{mb} \\
& \sigma_{d d}=5.9 \mathrm{mb} \text { and } B_{e l}=19.4 \mathrm{GeV}^{-2}
\end{aligned}
$$

## Consequences of the GLM (and KMR) Model

- Have only ONE Pomeron

No requirement for "soft" and "hard" Pomeron.
In accord with the Hera data which is smooth throughout the transition region.

- GLM find from their fit that the slope of the Pomeron $\alpha_{\mathbb{P}}^{\prime} \approx 0.01$ (KMR assume $\left.\alpha_{I P}^{\prime}=0\right)$. Small values for $\alpha_{\mathbb{P}}^{\prime}$ obtained by Zeus and H 1 in their fits to DIS data.
- This is consistent with what one expects in pQCD since for a BFKL $\mathbb{P} \alpha_{\mathbb{P}}^{\prime} \propto 1 / Q_{s}^{2} \rightarrow 0$ as $s \rightarrow \infty$.
- GLM and KMR analyses (including enhanced absorptive effects) have for the bare $\mathbb{P}$ intercept $\Delta_{\mathbb{P}}=\alpha_{\mathbb{P}}(0)-1 \approx 0.3$ close to the value of the BFKL $\mathbb{P}$ (after NLL corrections are resummed).

Having $\alpha_{\mathbb{P}}^{\prime} \rightarrow 0$ provides a necessary condition that links
strong (soft) interactions with the hard interactions described by pQCD.

## H1 data in the Transition Region



Survival Probability for exclusive central diffractive production of the Higgs boson


Fig-a shows the contribution to the survival probability in the G-W mechanism Fig-b illustrates the origin of the additional factor $\langle | S_{e n h}^{2}| \rangle$

Eikonal s-channel corrections give rise to the LRG survival probability of hard diffraction.
Experimental evidence $\rightarrow$ hard dijets with LRG at Tevatron are scaled down by a factor $\langle | S^{2}| \rangle \approx 0.1$, compared to dijets at Desy (due to screening).

## Central Production of Two Hard Jets



## Survival Probability of diffractive Higgs production

$$
\begin{gathered}
\langle | S_{2 c h}^{2}| \rangle=\frac{N(s)}{D(s)}, \\
\text { where, } \\
N(s)=\int d^{2} b_{1} d^{2} b_{2}\left[\sum_{i, k}\langle p| i>^{2}<p \mid k>^{2} A_{H}^{i}\left(s, b_{1}\right) A_{H}^{k}\left(s, b_{2}\right)\left(1-A_{S}^{i, k}\left(\left(s,\left(\mathbf{b}_{1}+\mathbf{b}_{2}\right)\right)\right)\right]^{2},\right. \\
D(s)=\int d^{2} b_{1} d^{2} b_{2}\left[\sum_{i, k}\langle p| i>^{2}<p \mid k>^{2} A_{H}^{i}\left(s, b_{1}\right) A_{H}^{k}\left(s, b_{2}\right)\right]^{2} .
\end{gathered}
$$

$A_{s}$ denotes the "soft" strong interaction amplitude.

For the "hard" amplitude $A_{H}(b, s)$ we assume an input Gaussian b-dependence:

$$
\begin{gathered}
A_{i, k}^{H}=A_{H}(s) \Gamma_{i, k}^{H}(b) \\
\text { and } \\
\Gamma_{i, k}^{H}(b)=\frac{1}{\pi\left(R_{i, k}^{H}\right)^{2}} e^{-\frac{2 b^{2}}{\left(R_{i, k}^{H}\right)^{2}} .}
\end{gathered}
$$

The "hard" radii are constants determined from HERA data on elastic and inelastic $J / \Psi$ production. We introduce TWO hard b-profiles

$$
A_{H}^{p p}(b)=\frac{V_{p \rightarrow p}}{2 \pi B_{e l}^{H}} \exp \left(-\frac{b^{2}}{2 B_{e l}^{H}}\right), \quad \text { and } \quad A_{H}^{p d i f}(b)=\frac{V_{p \rightarrow d i f}}{2 \pi B_{i n}^{H}} \exp \left(-\frac{b^{2}}{2 B_{i n}^{H}}\right) .
$$

The values $B_{e l}^{H}=5.0$ (3.6) $\mathrm{GeV}^{-2}$ and $B_{i n}^{H}=1 \mathrm{GeV}^{-2}$ have been taken from ZEUS data.

- Contrast to KMR treatment they assume: $A_{H}^{p p}(b)=A_{H}^{p d i f}(b) \propto \exp \left(-\frac{b^{2}}{2 B^{H}}\right)$
- with $B_{e l}^{H}=B_{\text {inel }}^{H}=4$ or $5.5 \mathrm{GeV}^{-2}$


The dependence of $S^{2}$ at the LHC on $B_{e l}^{H}$ and $B_{i n}^{H}$


Energy dependence of centrally produced Higgs survival probability


## Comparison of results obtained in GLMM and KMR models

|  | Tevatron <br> GLMM KMR(07) KMR(08) |  | LHC (14 TeV) <br> GLMM KMR(07) KMR(08) |  |  | W $=10^{5} \mathrm{GeV}$ <br> GLMM KMR(07) KMR(08) |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $S_{2 c h}^{2}(\%)$ | 5.3 | $2.7-4.8$ | 3.9 | $1.2-3.2$ | 3.2 | $0.9-2.5$ |  |
| $S_{e n h}^{2}(\%)$ | 28.5 | 100 | 6.3 | 100 | 33.3 | 3.3 | 100 |
| $S^{2}(\%)$ | 1.51 | $2.7-4.8$ | 0.24 | $1.2-3.2$ | 1.5 | 0.11 | $0.9-2.5$ |

At an energy of 7 TeV we obtain a value of: $S^{2} \approx 0.6 \%$

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Other results for }\mp@subsup{S}{2ch}{2}\mathrm{ ,
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Calculations based on L.O. QCD by Bartels, Bondarenko, Kuta and Motyka [P.R.,D73,093004 (2006)] find

$$
S_{2 c h}^{2}=0.024
$$

They have also calculated corrections for hard rescattering which depend on the value taken for $\alpha_{s}$.

Frankfurt, Strikman and Weiss have used a mean field approximation (independent hard and soft scattering).

They find that at LHC energies absorptive interactions of hard spectator partons associated with the process $g+g \rightarrow H$, reach the black disc region and cause substantial additional suppression, pushing

$$
S_{2 c h}^{2}<0.01
$$

## Other results for $S_{e n h}^{2}$ contd.

New paper of Jeremy Miller, arXiv:09083450
in which he derives an analytic expression for diagrams with an arbitary number of BFKL Pomeron loops, and finds a solution to the summation over these loop diagrams.

The leading contribution comes from the largest size loops (in rapidity space) in agreement with the MPSI approach.

His results indicate that $S_{e n h}^{2}$ decreases rapidly as the rapidity between the two protons increases.

$$
\text { For } \mathrm{W}=14 \mathrm{TeV}(\mathrm{Y}=19), S_{e n h}^{2}<1 \%
$$

## Other results for $S^{2}$, contd.

New version of the Durham model (EPJC60,265(2009)) includes 3 components of the POMERON, with different transverse momenta of the partons in each component, to mimic BFKL diffusion in $k_{t}$.

The Survival Probability is now multiplied by a "renormalizing" factor $\left(\left\langle p_{t}^{2}\right\rangle B\right)^{2}$ and referred to as $\left\langle S_{e f f}^{2}\right\rangle$

Their result for LHC energy is $\left\langle S_{e f f}^{2}\right\rangle=0.015_{-0.005}^{+0.01}$
For enhanced screening limited to outside the rapidity threshold:-

$$
\begin{array}{rlrl}
\text { For } \Delta \mathrm{y} & =0 & 1.5 & 2.3 \\
S_{e f f}^{2}(\%) & = & 0.4 & 0.9
\end{array}
$$

The new Durham result $\left\langle S_{\text {eff }}^{2}(\%)\right\rangle=1.0-2.5$ is compatable with their "old" Soft Model result of $S^{2}(\%)=1.2-3.2 \quad$ If $\left\langle S_{e n h}^{2}\right\rangle=\approx 1 / 3$

Then the difference with the amended Tel Aviv value of $S^{2}(\%) \approx 0.2-0.4$ is small.

## G-W, Enhanced and Semi-Enhanced Diagrams contributing to $\langle | S^{2}| \rangle$



The set of diagrams that is selected and summed for the calculation of the survival probability for diffractive Higgs production.fig(a) shows the diagrams in G-W + enhanced diagrams approach, in fig(b) the same approach is shown but we add the first semi-enhanced diagram to calculate the value of the survival probability. The approach for $\tilde{g}_{i} T(Y) \approx 1$ but $\Delta T(Y) \ll 1$ (net diagrams) is shown in fig(c).

# Survival Probalitity including G-W, Enhanced, and Semi-Enhanced diagrams 

(Preliminary)

| Survival probability $\left(S^{2} \%\right)$ | Tevatron | LHC |
| :--- | :--- | :--- |
| G-W + enhanced diagrams | 1.51 | 0.24 |
| G-W + enhanced diagrams <br> + semi-enhanced (perturbative) | 1.48 | 0.23 |

## Summary

- We present a model for soft interactions having two components:
(i) G-W mechanism for elastic and low mass diffractive scattering
(ii) Pomeron enhanced contributions for high mass diffractive production.
- Key Hypothesis:

Soft processes are not "soft", but orginate from short distances:

- Due to enhanced $\mathbb{P}$ diagrams, find $\sigma_{t o t}$ and $\sigma_{e l}$ at LHC energy will be SMALLER than D.L. predictions.
- Result with practical application is value obtained for $S_{H}^{2}$, for central diffractive Higgs production at the LHC, of about 0.24 \% as $S_{2 c h}^{2}$, is multiplied by a small $S_{e n h}^{2}$, while $S_{\text {semi-enh }}^{2} \approx 1$.


## Total Cross Section at Low Energies



The total cross section $\left(\sigma_{t o t}=\right.$ $\left.1 / 2\left[\sigma_{t o t}(p p)+\sigma_{t o t}(p \bar{p})\right]\right)$. The curve illustrates our parametrization.

