

Top Pair-Production theory overview



17-22 September, Braga, Portugal

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Science & Technology
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- ▶ Precision in production
 - ▶ news from NNLO-QCD
 - ▶ an application and a problem
- ▶ Towards the physical final states of $t\bar{t}$
 - ▶ toward NNLO production & decay in NWA
 - ▶ offshell and offshell + parton showers

Apologies in advance for omissions in this talk.

I will talk about work done on $t\bar{t}$ mainly in the past year or so.

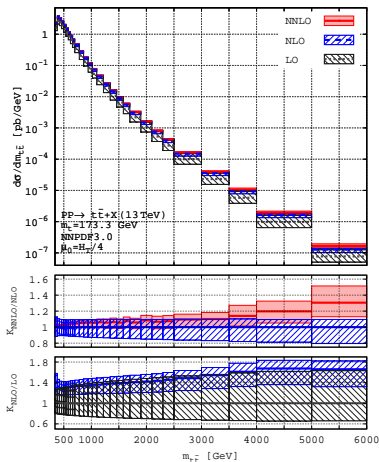
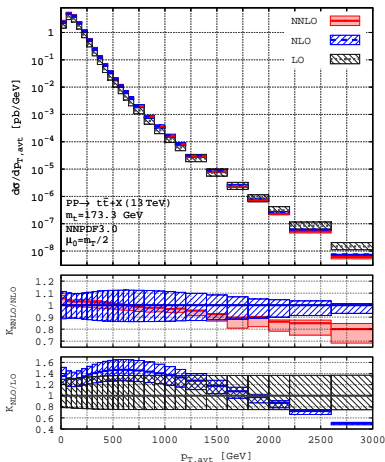
I will also not have time to cover $t\bar{t}$ with resummations: talk by A. Ferroglia
today 16:00

Precision in Production

The state-of-the-art

- fully-differential NNLO-QCD predictions for $t\bar{t}$ production

[Czakon, Heymes, Mitov '16]



Precision in Production

The state-of-the-art

Important outcomes of [1606.03350] :

[Czakon,Heymes,Mitov '16]

- ▶ detailed study of scale dependence **through NNLO** at fixed order
- ▶ dynamical scales crucial in multi-TeV regimes, however, how to pick dynamical scale? (typically large differences between choices)
- ▶ based on criterion of best (fastest) perturbative convergence, across full ranges of distributions, the following scales were found to be optimal

$$\mu = \begin{cases} M_T/2, & \text{for } p_T(t), p_T(\bar{t}), p_T(t)_{\text{ave}} \\ H_T/4, & \text{for all others studied } (y(t), m_{t\bar{t}}, p_T(t\bar{t}), y_{t\bar{t}}) \end{cases}$$

- ▶ Note: $\sigma^{\text{NNLO}}(\mu = H_T/4) \simeq \sigma^{\text{NNLO+NNLL}}(\mu = m_t)$
- ▶ forms basis for scale choices in all NNLO studies that follow
- ▶ given scale uncertainty under control, in TeV-region leading uncertainty now comes from PDFs (different sets giving v. different results!)

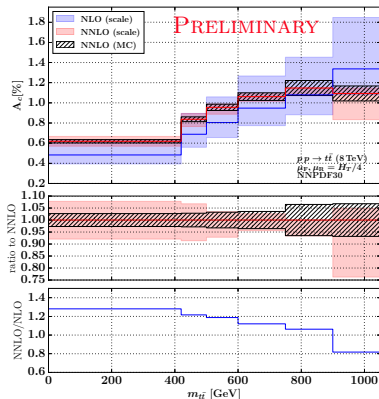
Precision in Production

New observables: LHC charge asymmetry, A_c

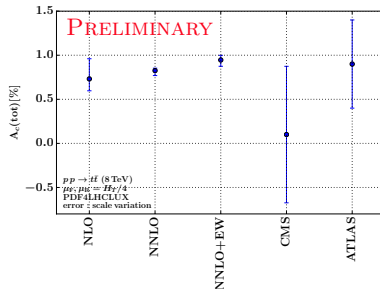
Thanks to
D. Heymes for plots!

$$A_c = \frac{N(\Delta|y| > 0) - N(\Delta|y| < 0)}{N(\Delta|y| > 0) + N(\Delta|y| < 0)}$$

$$\Delta|y| = |y(t)| - |y(\bar{t})|$$



[Czakon, Heymes, Mitov, Pagani, Tsinikos, Zaro - in preparation]



- ▶ unexpanded denominator
- ▶ NNLO-QCD corrections (& NLO-EW) increase total asymmetry (but not asymmetry in all bins of $m_{t\bar{t}}$)
- ▶ very challenging numerically due to large cancellations in numerator

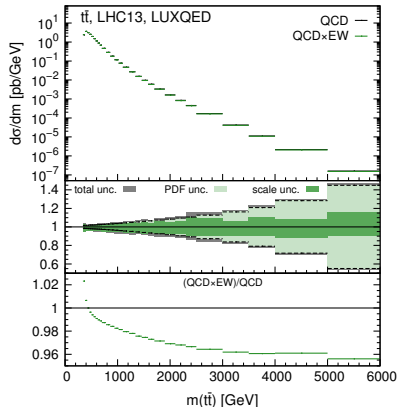
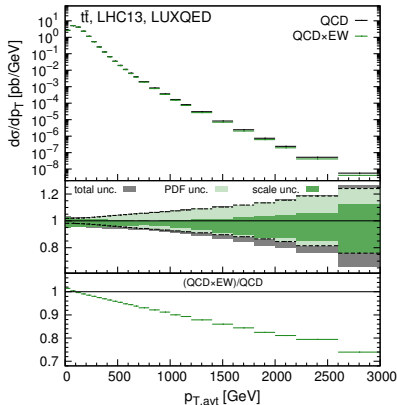
Dedicated talk by D. Pagani, tomorrow 16:30

- ▶ NLO-EW corrections tend to be small for total cross section, but
- ▶ large EW-Sudakov logarithms could have a large impact in tails of distributions, and in TeV-regime kinematics
- ▶ in [1705.04105] (see also [1606.01915]) [Czakon, Heymes, Mitov, Pagani, Tsinikos, Zaro '17; Pagani, Tsinikos, Zaro '16]
 - ▶ assessment of overall size of EW corrections to $p_T(t)$, $m_{t\bar{t}}$, $y(t)$, $y_{t\bar{t}}$ for LHC 13 TeV
 - ▶ study effects of different photon PDFs

Precision in Production

NNLO QCD + NLO EW

[Czakon,Heymes,Mitov,Pagani,Tsinikos,Zaro '17]



- ▶ $p_T(t)$: EW corrections grow from +2% \rightarrow -25% in range $[0, 3]$ TeV
- ▶ $p_T(t)$: EW corrections as significant as NNLO-QCD scale uncertainty
- ▶ smaller effects for $m_{t\bar{t}}$

Precision in Production

Ease of use: fastNLO tables

[Czakon,Heymes,Mitov '17]

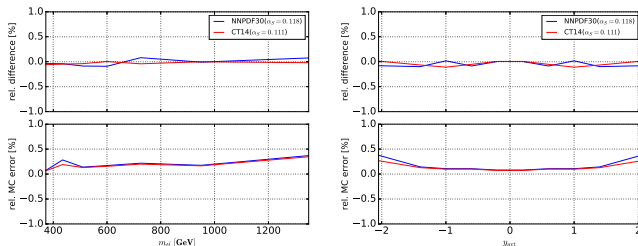
- ▶ typically $\mathcal{O}(10^5)$ CPU hours for a single NNLO calculation (for fixed observables, scales, m_t , PDFs)
- ▶ option to compute distributions quickly with updated/improved PDF sets preferable to re-running each time a new set is released
- ▶ applications such as PDF fitting, α_s or m_t extractions require results computed with $\mathcal{O}(10 - 1000)$ PDFs ...
 - ⇒ require flexible storage format for fast evaluations
- ▶ fastNLO [Britzger et al.] has been interfaced to STRIPPER
- ✓ PDF and α_s independent storage ⇒ fast, $\mathcal{O}(\text{seconds})$, recalculation of distributions
- ▶ fastNLO first tables produced for the central (dynamical) scale choice, as prescribed in [1606.03350]

Precision in Production

Ease of use: fastNLO tables

[Czakon, Heymes, Mitov '17]

- ▶ same MC sample used for direct calculation and filling of tables
- ✓ interpolation error $\lesssim 0.1\%$, much smaller than MC error of NNLO calculation $< 0.5\%$
- ✓ all results checked against statistically independent calculations



- ▶ tables for $p_T(t)$, $y(t)$, $y(t\bar{t})$, $M(t\bar{t})$ at 8 TeV (ATLAS & CMS binnings) available at: www.precision.hep.phy.cam.ac.uk
- ▶ tables for 13 TeV, 2D observables, different masses *on the way!*

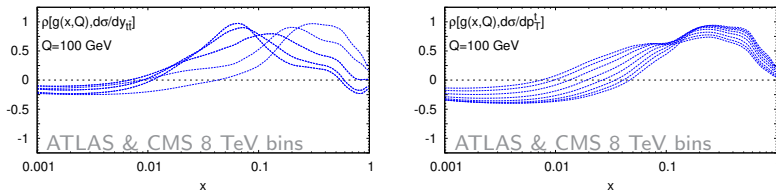
Precision in Production

An application: probing high- x gluon

see also E. Nocera's talk
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[Czakon,Hartland,Mitov,Nocera,Rojo '16]

- ▶ top-pair production data sensitive to large- x gluon PDF



- ▶ [1611.08609] performed a global fit (in NNPDF framework) using NNLO $t\bar{t}$ predictions to study impact of diff. top data on PDF fit
- ▶ baseline fit data: \sim NNPDF3.0, without $\sigma_{t\bar{t}}$ & inclusive-jet data
- ▶ fit with top data: included (all 8TeV, l +jets channel)
 - ▶ ATLAS normalized y_t distribution
 - ▶ CMS normalized $y_{t\bar{t}}$ distribution
 - ▶ ATLAS & CMS measurement of $\sigma_{t\bar{t}}$

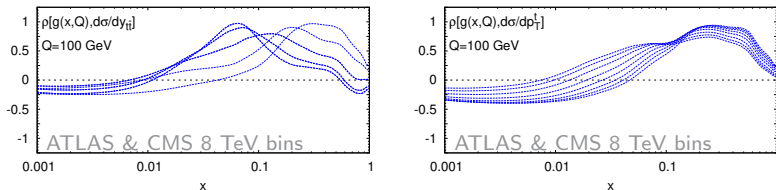
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}

✓

small dependence on m_t uncertainty

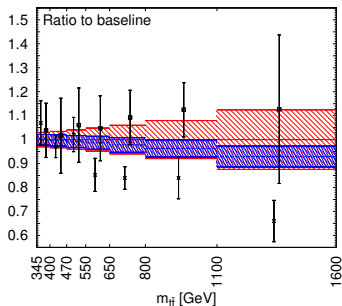
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low BSM sensitivity

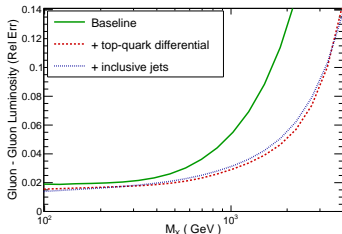
Precision in Production

Application: probing high- x gluon – outcomes

[Czakon,Hartland,Mitov,Nocera,Rojo '16]



- ▶ red: baseline-fit PDFs (NNPDF)
- ▶ blue: PDFs after select top data included
- ✓ bands: PDF uncertainties \rightarrow reduction by factor 2!
- ▶ description of obs. included in fit improves, but little/no improvement of distributions not included in fit



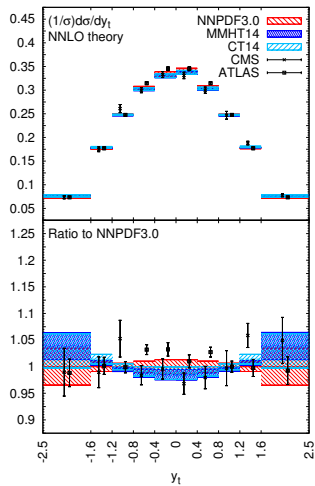
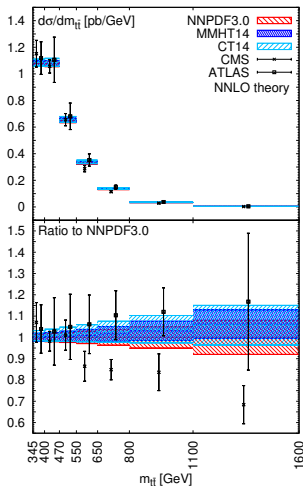
- ▶ Relative uncertainty on gluon-gluon lumi at high M_X shows remarkable reduction, with inclusion of just 17 data points!
- ▶ differential top data is very constraining and perhaps can compete with jets
- ▶ surely one of the big motivations for $t\bar{t}$?

Precision in Production

Some unsettling observations

[Czakon,Hartland,Mitov,Nocera,Rojo '16]

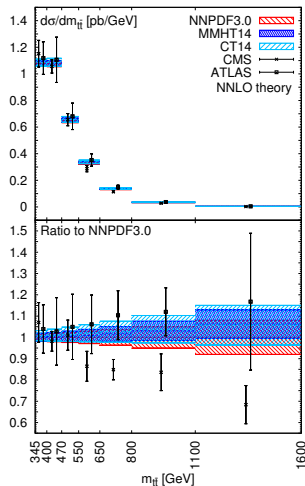
Two examples of 'tension' between measurements:



Precision in Production

Some unsettling observations

[Czakov, Hartland, Mitov, Nocera, Rojo '16]



- ▶ very difficult to get a good description of both ATLAS and CMS (l +jets 8TeV) data, particularly for normalized y_t , $p_T(t)$ and $m_{t\bar{t}}$
- ▶ for best fit quality authors had use a different observable from each experiment (multiple distributions from each exp. not possible due to lack of correlations b/w distributions)
- ▶ to maximize benefit of NNLO predictions, such discrepancies must be resolved
- ▶ has there been any understanding to the reasons behind discrepancies?
 - ▶ are we missing/underestimating some systematic uncertainty?
 - ▶ are ATLAS and CMS presenting exactly the same 'stable-top' quantities?

Moving towards physical final states

The top quark is not stable

- ▶ due to its large width, Γ_t , top quark decays before hadronizing ...
- ▶ top quarks not directly measured – presence always inferred through their decay products: **leptons, (b)jets, missing energy**
- ▶ To compare to stable top predictions, experiments have to
 - ▶ extrapolate their measurements from fiducial to inclusive
 - ▶ extrapolate/model from particle-level to top-quark partons
- ▶ this back-modelling depends on Monte Carlo
 - ▶ each MC generator has a different shower & (potentially) way of attaching the decay
 - ⇒ is the top ‘parton’ one arrives at is a **MC-dependent** object?
 - ▶ these steps currently use MCs that **treat top decay at LO**
 - ⇒ no reliable estimate of uncertainty on shape & normalization due to higher order corrections to decay

Moving towards physical final states

Predictions (fixed order)

Two mainstream ways of calculating, when top decay is included:

- ▶ Narrow-width approximation (NWA), $p(t)^2 = m_t^2$, $\Gamma_t \rightarrow 0$ limit
 - ▶ NLO: [Bernreuther, Si; Melnikov, Schulze; Campbell, Ellis (MCFM)]
 - ▶ production / decay of onshell tops completely factorize
 - ▶ compute higher-order corrections to prod. & decay separately
 - ▶ for large class of observables NWA is an excellent approx (error $\sim \mathcal{O}(\Gamma_t/m_t)$)
- ▶ Offshell, $p(t)^2 \neq m_t^2$
 - ▶ NLO: [Bevilacqua et al, Denner et al, Falgari et al, Heinrich et al, Frederix, Cascioli et al]
 - ▶ diagrams involving top quarks only form a subset of all required contributions
 - ▶ since there are both resonant and non-resonant contributions, notion of a physical, onshell top-quark parton loses meaning
 - ▶ finite-width effects vital in certain regions of phase space, e.g. edge of M_{bl} distribution!

Moving towards physical final states

Predictions (fixed order)

Key features:

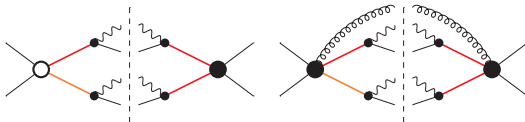
- ▶ predictions built from matrix-elements with **bs & leptons** in final state
- ▶ consistently include higher order corrections in production & decay

Measurements can be directly compared to predictions from these codes!

Moving towards physical final states

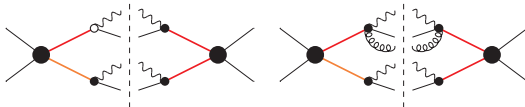
Narrow-width approximation (NWA)

NLO
production



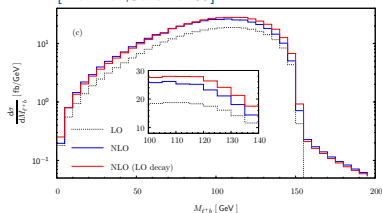
[Bernreuther, Si;
Melnikov, Schulze;
Badger et al;
Campbell, Ellis]

NLO
decay



[Bernreuther et al;
Campbell et al;
Melnikov, Schulze ...]

[Melnikov, Schulze '09]

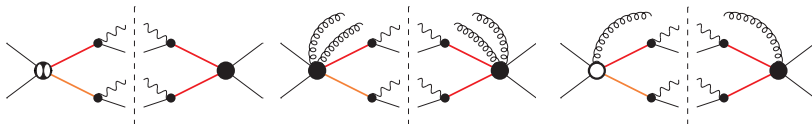


- ▶ NLO corrections to decay, in general, change **normalization** and **shape**
- ▶ decay corrections **enhanced** when cuts imposed on top-quark decay products

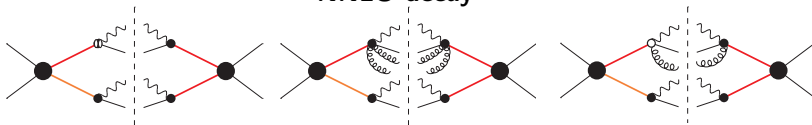
Moving towards physical final states

Narrow-width approximation (NWA)

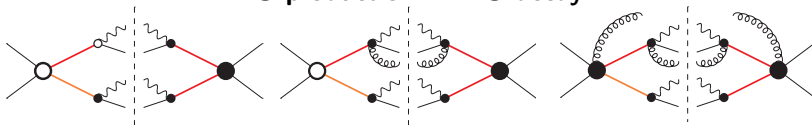
NNLO production



NNLO decay



NLO-production x NLO-decay

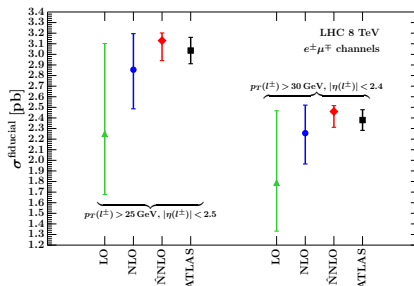
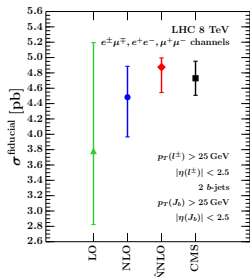


(also: NLO- t decay x NLO- \bar{t} decay)

Moving towards physical final states

Towards NNLO production & decay

- ▶ exact NNLO not yet available: ongoing work within Stripper
- ▶ recent work: approx-NNLO prod. [Broggio,AP,Signer '14] with exact NNLO in decay [Gao,Li,Zhu '12] (& exact interferences): **$\hat{\text{NNLO}}$** [Gao,AP '17]



- ▶ significant improvement in agreement of theory with measurements
- ▶ to see good agreement for both ATLAS and CMS fiducial volumes, must include corrections in **prod. & decay** – including no corrections in decay \Rightarrow cross section $\sim 8\%$ larger than full result, for CMS volume

Moving towards physical final states

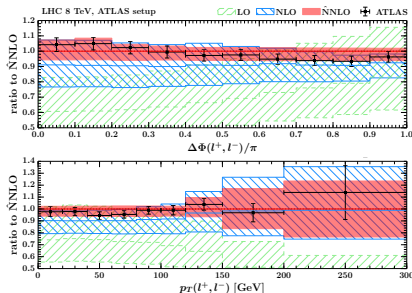
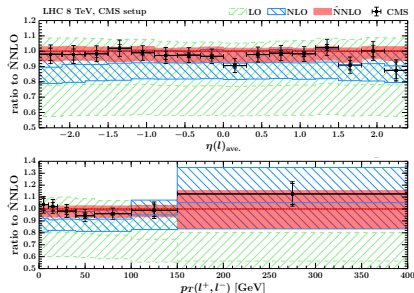
Towards NNLO production & decay

[Gao, AP '17]

Comparisons also made differentially:

- ▶ CMS 8 TeV: [1505.04480, 1510.03072]
- ▶ ATLAS 8 TeV: [ATLAS-CONF-2017-044]

$m_t = 173.3$ GeV
 $\mu \in [m_t/2, 2m_t]$
 MMHT2014 PDFs

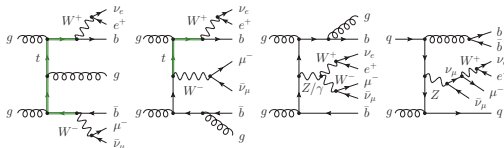


- ▶ good agreement in norm. & shape with $\hat{\text{N}}\text{NLO}$ predictions
- ▶ start exploiting these for applications, e.g. m_t^{pole} -extraction from σ^{fid} .

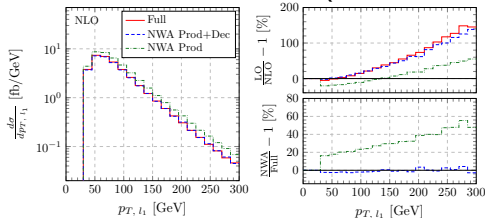
Moving towards physical final states

Offshell state-of-the-art

- ▶ NLO corrections to $e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} + X$ known [5FS: Bevilacqua et al, Denner et al, Heinrich et al; 4FS: Frederix, Cascioli et al]
- ▶ recently: NLO corrections to $e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$ [Bevilacqua, Hartando, Krauss, Worek '15,16']



From B. Hartando's talk @ QCD@LHC2017



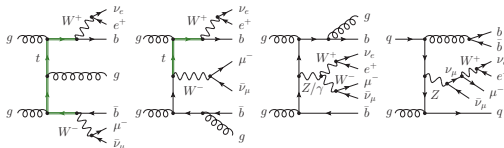
[Bevilacqua, Hartando, Krauss, Schulze, Worek – in preparation]

- ▶ offshell & nonresonant effects very small for large class of obs.
- ▶ excellent performance of NWA, when NLO corrections to prod & decay included
- ▶ Notice: NLO-production with LO-decay not a good approx. of full result (shape & norm.)

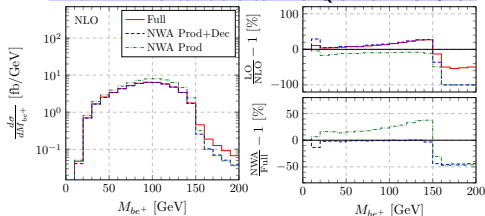
Moving towards physical final states

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From B. Hartando's talk @ QCD@LHC2017



[Bevilacqua, Hartando, Krauss, Schulze, Worek – in preparation]

- ▶ near kinematic thresholds / edges of distributions, offshell effects become crucial
- ▶ good description of these phase space regions relies on top kept offshell
 \Rightarrow NWA fails (not designed to capture these effects)

Moving towards physical final states

NWA & Offshell $t\bar{t}$ matched to parton showers

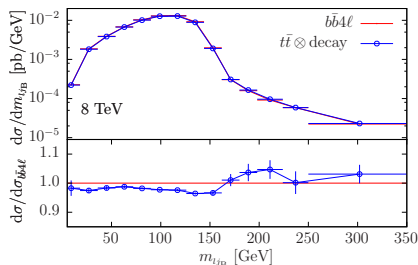
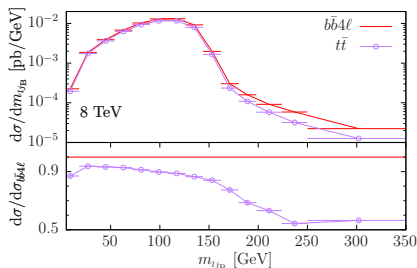
See also talk by T. Ježo → tomorrow 11:50

- ▶ Aim: to match $e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b} + X$ to parton showers
- ▶ despite top quarks not being a final state in the matrix elements, an ‘intermediate top’ must be written in event file if one wants the PS to preserve the resonance mass
- ▶ resonance-aware matching to parton showers for $t\bar{t}$ (NWA & offshell) have been developed in the POWHEG framework over last couple of years
- ▶ two state-of-the-art generators:
 - ▶ “ $t\bar{t} \otimes \text{decay}$ ”: NWA, NLO corrections in prod. & decay, and LO approximation of finite-width effects [Campbell,Ellis,Nason,Re '14]
 - ▶ “ $b\bar{b}4l$ ”: fully offshell, NLO corrections to resonant & nonresonant contributions [Ježo, Nason '15; Ježo, Lindert, Nason, Oleari, Pozzorini '16]
- ▶ study differences between these and the older (but routinely used today):
 - ▶ “ $t\bar{t}$ ”: NWA, NLO corrections in production **only**

Moving towards physical final states

NWA & Offshell $t\bar{t}$ matched to parton showers

[POWHEG;NWA: Campbell, Ellis, Nason, Re '14; offshell: Ježo, Nason '15; Ježo, Lindert, Nason, Oleari, Pozzorini '16]

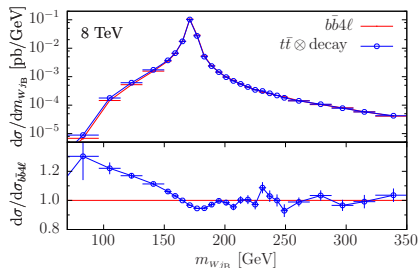
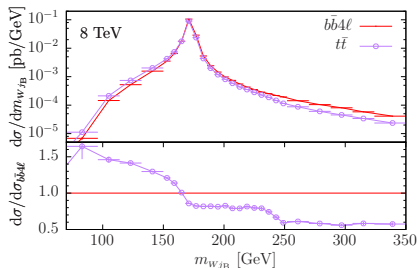


- ▶ sizeable differences in shape (10-50%) and normalization ($\sim 10\%$) between $bb4l$ and $t\bar{t}$ generators
- ▶ much milder differences between $bb4l$ and $t\bar{t} \otimes \text{decay}$ generators
- ▶ these features are repeated for a number of observables
- ▶ even though offshell effects are modelled ($\sim \text{LO}$) in $t\bar{t}$ and $t\bar{t} \otimes \text{decay}$ generators, it is clear that to get close to full result when using an onshell approx., it is **imperative** to include corrections in decay

Moving towards physical final states

NWA & Offshell $t\bar{t}$ matched to parton showers

[POWHEG;NWA: Campbell, Ellis, Nason, Re '14; offshell: Ježo, Nason '15; Ježo, Lindert, Nason, Oleari, Pozzorini '16]



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Summary & Outlook

- ▶ It is clear that at the stable-top level, theory for $t\bar{t}$ is at a high level of precision: NNLO-QCD, +NLO-EW, +resummation, and its potential for **impactful** applications using LHC data is **huge!**
- ▶ Fast re-evaluations of differential observables now possible via fastNLO interface, and there is an ongoing 'production line' of new runs, observables, K -factors, tables... all of which will be available at www.precision.hep.phy.cam.ac.uk
- ▶ Also clear, that certain unsettling aspects such as p_T -discrepancy (not fully gone away) & consistency b/w measurements still remain.
- ▶ To benefit maximally from precision stable-top theory (e.g. for PDF fits) such issues/features must be understood.
- ▶ Given **non-trivial nature** of higher-order corrections in decay, their effect on extrapolations to 'parton level' ought to be accounted for (this is a systematic error we currently **don't have an estimate for**).
- ▶ The tools to do this at high precision are already available.

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Obrigado!