



# Neutral Current Events

## and the Long-baseline neutrino experiments

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[arXiv:1508.06275](#) [[pdf](#), [other](#)]

## **The impact of sterile neutrinos on CP measurements at long baselines**

[Raj Gandhi](#), [Boris Kayser](#), [Mehedi Masud](#), [Suprabh Prakash](#)

Comments: Published in Journal of High Energy Physics, Volume 2015, Issue 11

Journal-ref: JHEP 1511 (2015) 039

[arXiv:1607.02152](#) [[pdf](#), [other](#)]

## **Capabilities of long-baseline experiments in the presence of a sterile neutrino**

[Debajyoti Dutta](#), [Raj Gandhi](#), [Boris Kayser](#), [Mehedi Masud](#), [Suprabh Prakash](#)

Comments: Published in JHEP, 24 pages, 12 figures, IH results added

Journal-ref: JHEP 11(2016)122

[arXiv:1708.01816](#) [[pdf](#), [other](#)]

## **What measurements of neutrino neutral current events can reveal**

[Raj Gandhi](#), [Boris Kayser](#), [Suprabh Prakash](#), [Samiran Roy](#)

Comments: 22 pages, 10 figures

Journal-ref: JHEP 1711 (2017) 202

# Implications from previous works

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From a probability and event rate analysis, we show that the effects of the sterile oscillation parameters can be large at the chosen baseline of 1300 km.

Depending on the values of sterile mixing angles and phases, the sensitivities can be both significantly enhanced or suppressed compared to the 3+0 case.

We have noted above that in the presence of even a single sterile neutrino, conclusions such as a) CP is conserved or violated, or, b) if the latter, whether the violation is ascribable to the active neutrinos or the additional sterile neutrino, or a combination of the two, are all rendered significantly ambiguous.

A precise knowledge of the source fluxes, relevant cross-sections and the reduction of systematic errors by a near detector assumes an even more crucial role than it did before.

Synergistic linkage between global LBL and SBL efforts.

# Sterile neutrinos and NC measurements

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Most studies of new physics at long and short-baselines have focused on the charged current measurements. We investigate the potential of the neutral current (NC) events at these experiments.

NC events can comprise:

neutrino-nucleon  $\nu + A \rightarrow \nu + A$

neutrino-electron elastic scattering  $\nu + e \rightarrow \nu + e$ ,

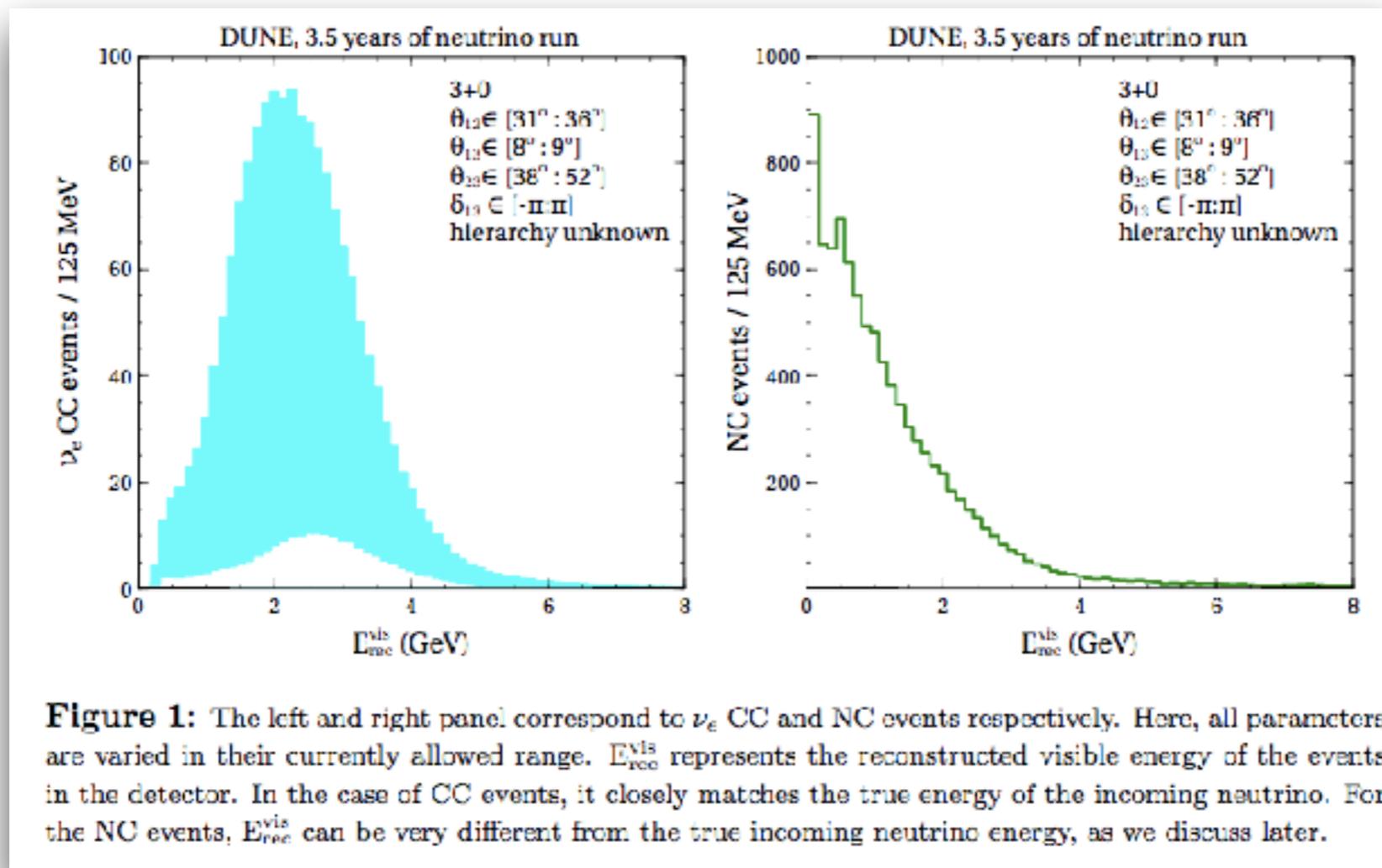
neutrino deep-inelastic scattering  $\nu + n \rightarrow \nu + X$ ,

neutrino-nucleon resonant scattering  $\nu + p \rightarrow \nu + p + \pi^0$  (or  $n + \pi^+$ ),  
 $\nu + n \rightarrow \nu + n + \pi^0$  (or  $p + \pi^-$ )

neutrino coherent pion scattering  $\nu + A \rightarrow \nu + A + \pi^0$ .

# Sterile neutrinos and NC measurements

The measurement and study of NC events can in some cases provide a qualitatively different, complementary and statistically superior handle on neutrino properties in new physics scenarios compared to CC measurements.



NC event measurements are typically statistically rich. For instance, in the Deep Underground Neutrino Experiment (DUNE), a 7-ton fine-grained tracking near detector at 500 m is planned, and it is expected to detect in excess of 400000 NC current events in a year. Even at long baselines, NC events are typically higher in number compared to any one measured CC channel.

# Short baselines and CPV - 3+2

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The oscillation probability between the flavours  $\alpha$  and  $\beta$  can be given by:

$$P(\alpha \rightarrow \beta) = \delta_{\alpha\beta} - 4\text{Re} \sum_{k>j} (U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^*) \sin^2 \Delta_{kj} \\ + 2\text{Im} \sum_{k>j} (U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^*) \sin 2\Delta_{kj}.$$

- Express  $P_{\mu e}$ , and  $P_{NC} = 1 - P_{\mu s1} - P_{\mu s2}$  in the above form.
- Calculate  $D_{NC} = P_{NC} - \text{bar}(P_{NC})$  and  $D_{CC} = P_{\mu e} - \text{bar}(P_{\mu e})$

# Short baselines and CPV - 3+2

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In a scenario geared towards explaining the short baseline anomalies [49–53], further simplifications are possible, *e.g.*  $\delta m_{lm}^2 \gg \delta m_{mn}^2$ ,  $l = 4$  or  $l = 5$ ,  $m, n = 1, 2, 3$ <sup>5</sup>. After a little algebra, one then finds that the CP violating difference between NC events measured using an initially muon-flavoured neutrino beam, and those measured using its anti-neutrino counterpart, will be proportional to the quantity  $D_{NC}$ , given by

$$\underline{D_{NC} \propto \text{Im}[U_{\mu 5}^* U_{\mu 4} (U_{s_1 5} U_{s_1 4}^* + U_{s_2 5} U_{s_2 4}^*)] \sin \Delta_{54} \sin \Delta_{43} \sin \Delta_{53}.} \quad (2.5)$$

On the other hand, the analogous difference for CC events from  $\nu_\mu \rightarrow \nu_e$  transitions is proportional to

$$\underline{D_{CC} \propto \text{Im}[U_{\mu 5}^* U_{\mu 4} U_{e 5} U_{e 4}^*] \sin \Delta_{54} \sin \Delta_{43} \sin \Delta_{53}.} \quad (2.6)$$

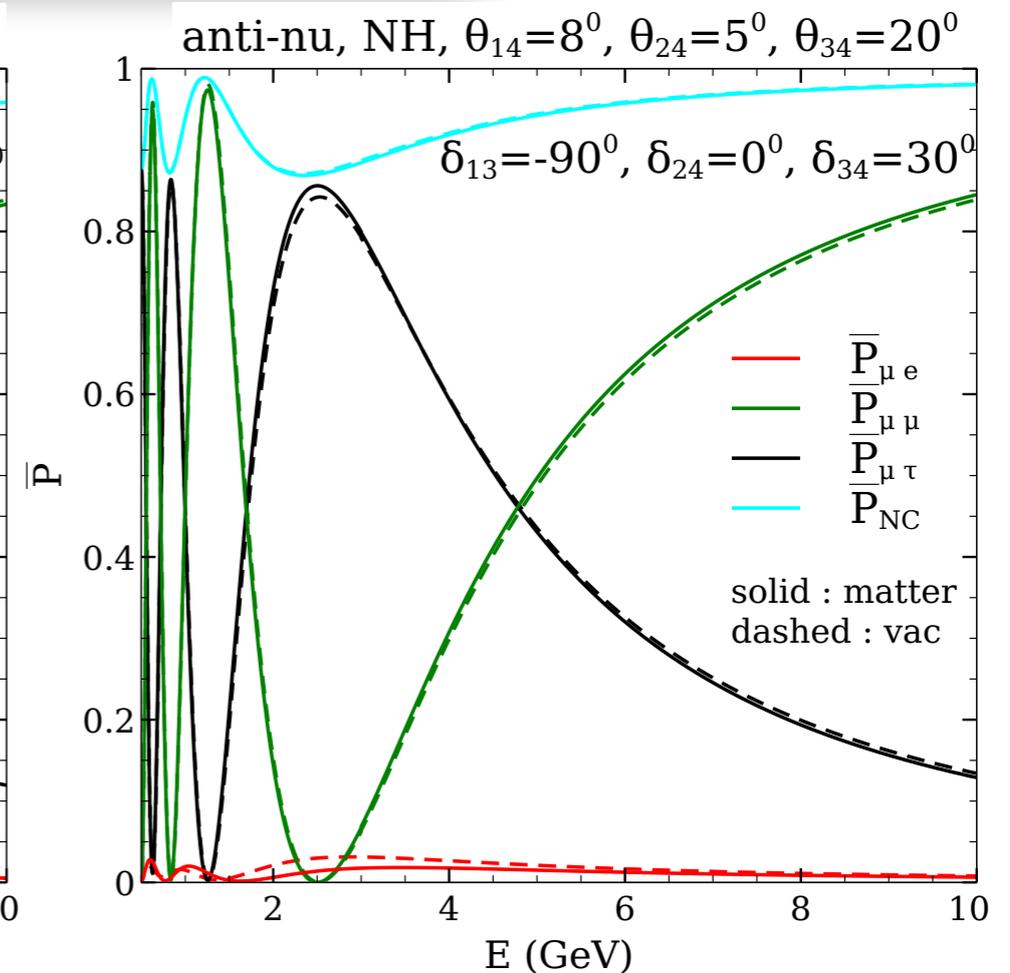
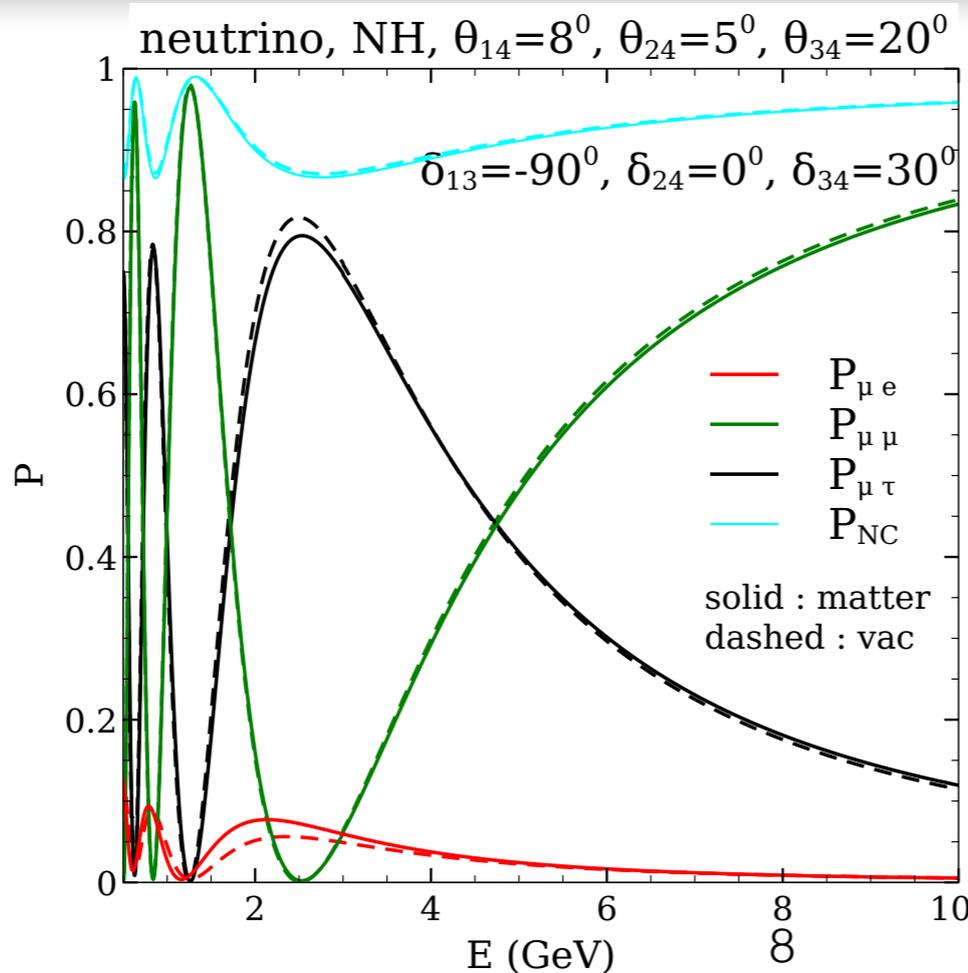
Thus, it can be said that CC and NC channels in general would tap into different CPV phases. Consequently, the NC measurements will provide a qualitatively and quantitatively different window into the CP violating and mixing sectors of a new physics scenario compared to the CC measurements.

# $P_{\mu s}$ : sterile neutrino appearance probability

$$U_{\text{PMNS}}^{3+1} = O(\theta_{34}, \delta_{34})O(\theta_{24}, \delta_{24})O(\theta_{14})O(\theta_{23})O(\theta_{13}, \delta_{13})O(\theta_{12})$$

$$P_{\mu s}^{\text{vac}} \simeq \cos^4 \theta_{13} \cos^2 \theta_{24} \sin^2 \theta_{34} - \cos^2 \theta_{13} \cos^2 \theta_{24} \cos^2 \theta_{34} \sin^2 \theta_{24} + \frac{1}{\sqrt{2}} \sin 2\theta_{13} \sin 2\theta_{34} \sin \theta_{14} \cos^3 \theta_{24} \cos(\delta_{13} + \delta_{34}) \left[ \sin^2 \frac{\Delta m_{41}^2 L}{4E} + \frac{1}{2} \cos^2 \theta_{13} \cos^2 \theta_{24} \sin 2\theta_{34} \sin \theta_{24} \sin(\delta_{34} - \delta_{24}) \sin \frac{\Delta m_{31}^2 L}{2E} \right]$$

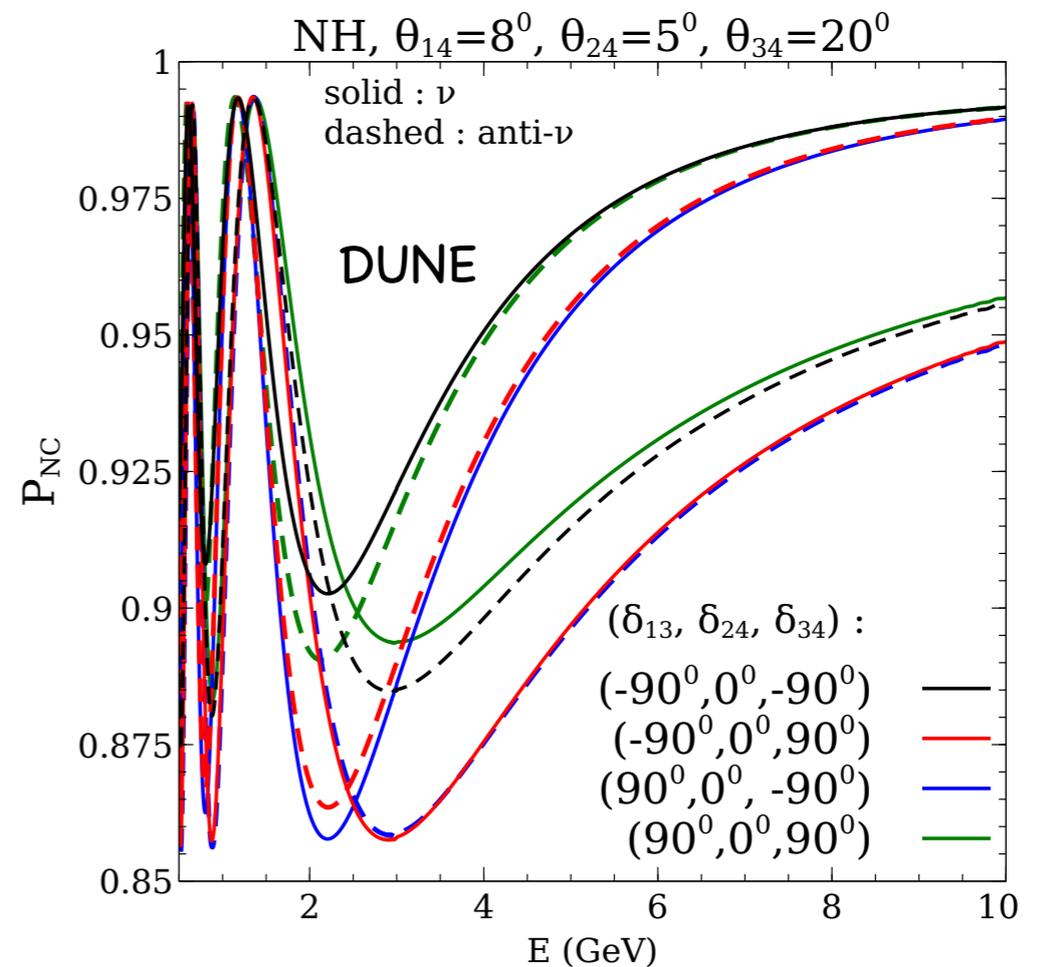
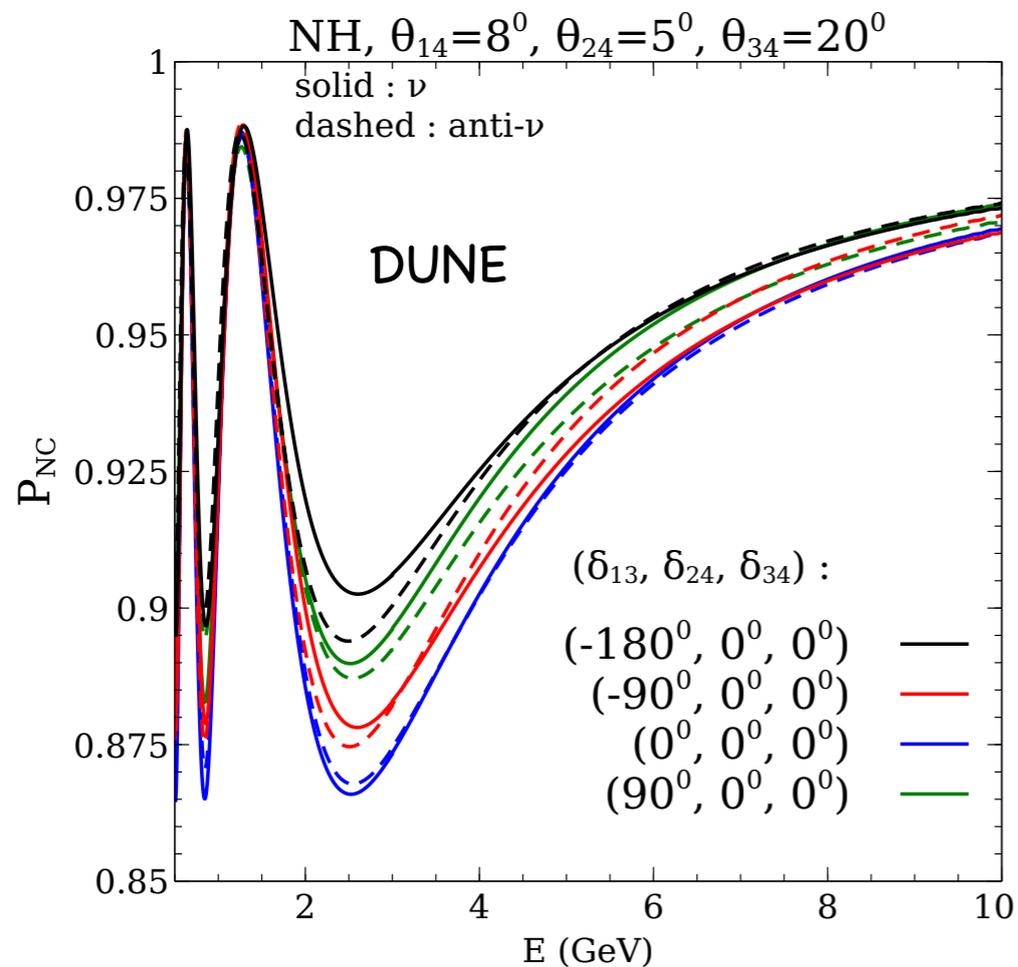
for DUNE  
 $P_{\text{NC}} = 1 - P_{\mu s}$



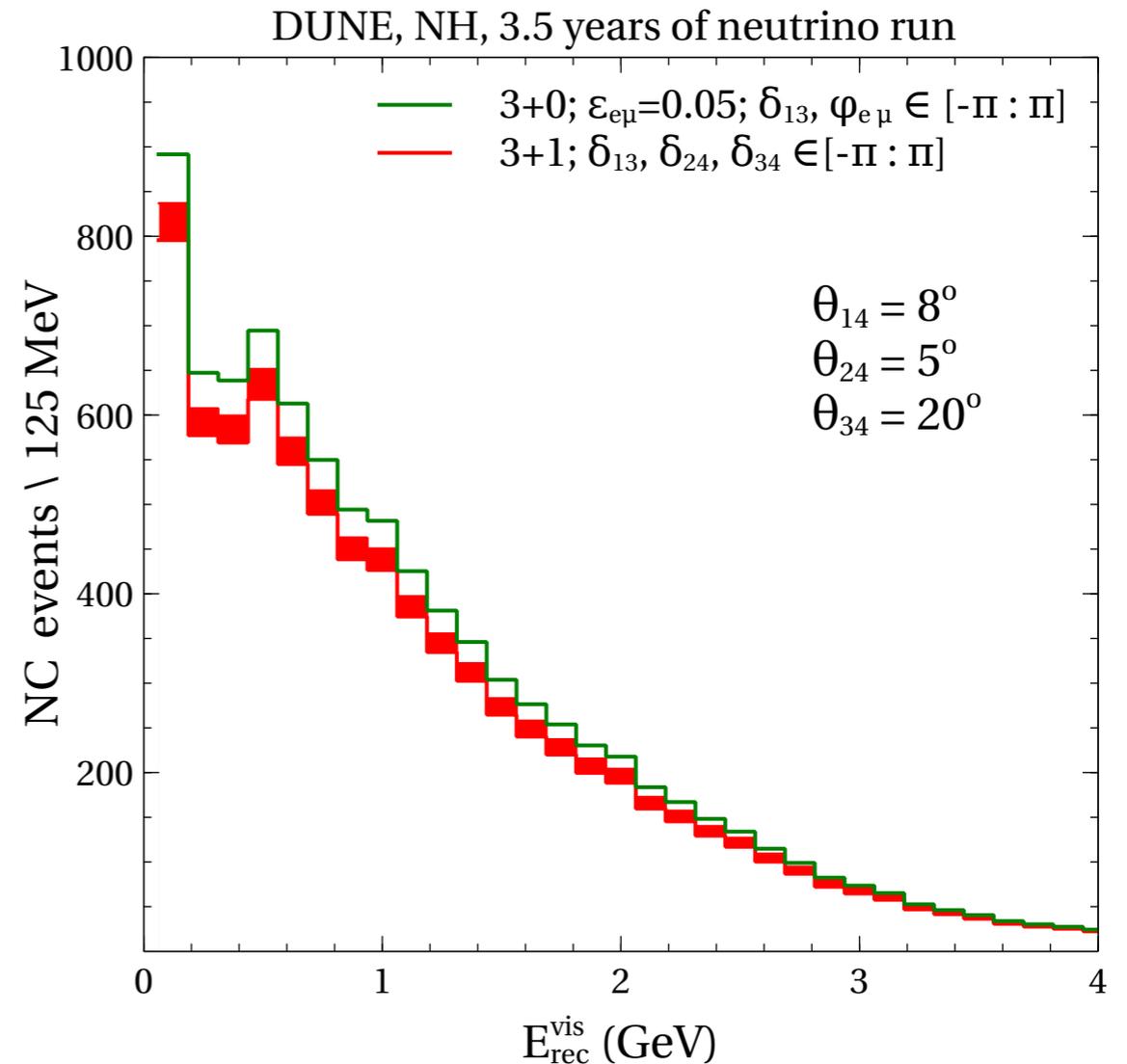
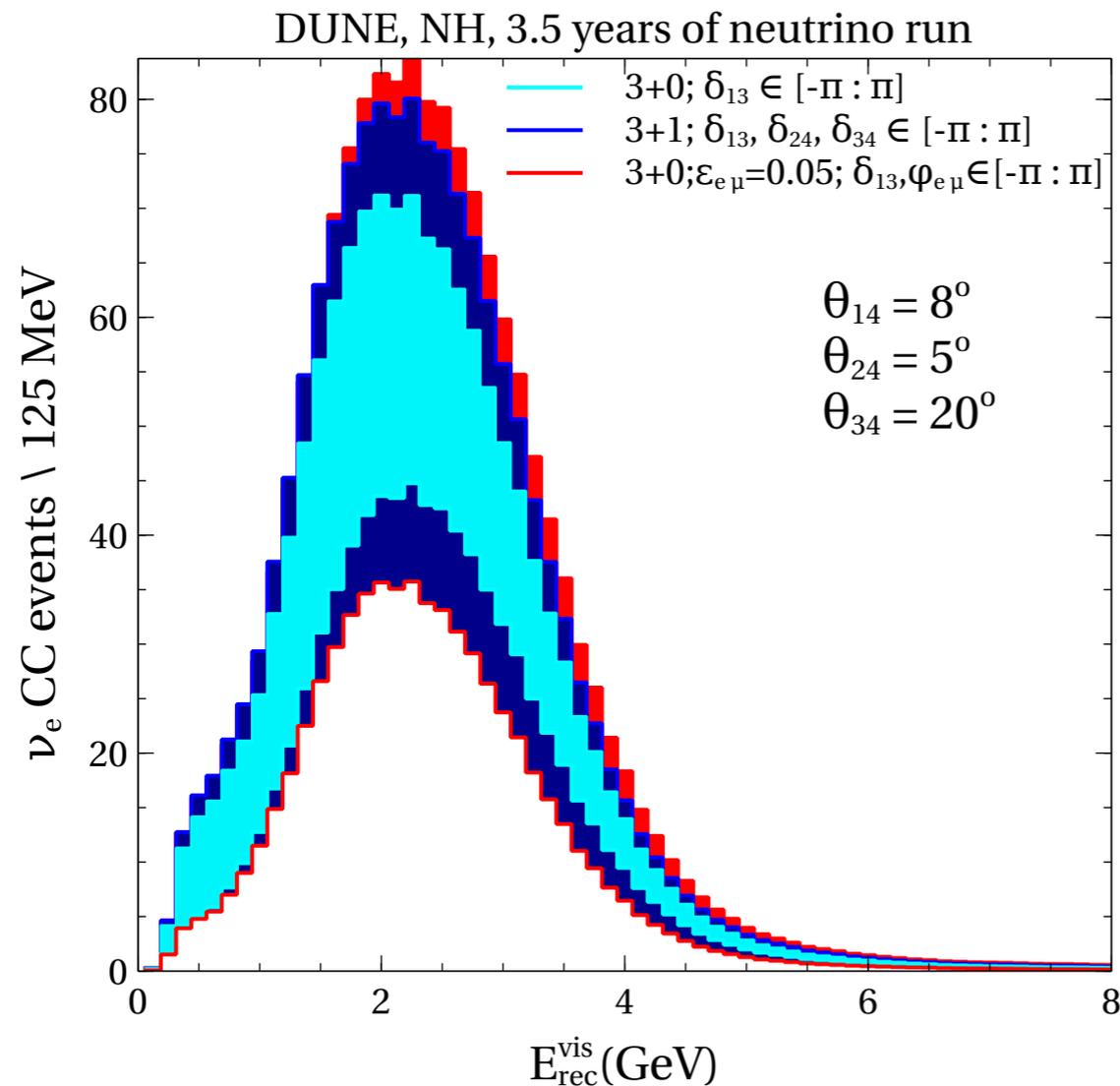
# $P_{\mu s}$ : sterile neutrino appearance probability

$$\begin{aligned}
 P_{\mu s}^{\text{vac}} \simeq & \cos^4 \theta_{14} \cos^2 \theta_{34} \sin^2 2\theta_{24} \sin^2 \frac{\Delta m_{41}^2 L}{4E} \\
 & + \left[ \cos^4 \theta_{13} \cos^2 \theta_{24} \sin^2 \theta_{34} - \cos^2 \theta_{13} \cos^2 \theta_{24} \cos^2 \theta_{34} \sin^2 \theta_{24} \right. \\
 & + \left. \frac{1}{\sqrt{2}} \sin 2\theta_{13} \sin 2\theta_{34} \sin \theta_{14} \cos^3 \theta_{24} \cos(\delta_{13} + \delta_{34}) \right] \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\
 & + \frac{1}{2} \cos^2 \theta_{13} \cos^2 \theta_{24} \sin 2\theta_{34} \sin \theta_{24} \sin(\delta_{34} - \delta_{24}) \sin \frac{\Delta m_{31}^2 L}{2E}.
 \end{aligned}$$

Note the y axis scale!!



# NC events as a tool to distinguish new physics scenarios



While we choose propagation based non-standard interactions (NSI) and a 3+1 sterile scenario to demonstrate our point, our conclusion will hold for any two new physics settings, one of which does not break 3+0 unitarity (in this example, the propagation NSI) and another one which does (3+1 sterile). A similar conclusion would hold, for example, for NSI in propagation and neutrino decay, or NSI in propagation and NSI in production or detection (which inherently violate unitarity by adding to or depleting the source neutrino beam).

# Constraints on the mixings

<sup>8</sup>It should be noted that there are global analyses of the existing oscillation data that provide constraints on the 3+1 paradigm [65–67]. However, there exist differences in their results corresponding to the fits in the parameter space  $\Delta m_{41}^2 - \sin^2 \theta_{34}$ . There is also the difficulty in reconciling the appearance data with the disappearance data. Keeping these points in mind, we adhere to the constraints on 3+1 from the disappearance data from the above-mentioned standalone experiments.

[65] J. Kopp, P. A. N. Machado, M. Maltoni, and T. Schwetz, JHEP **05**, 050 (2013), [1303.3011](#).

[66] G. H. Collin, C. A. Argüelles, J. M. Conrad, and M. H. Shaevitz, Phys. Rev. Lett. **117**, 221801 (2016), [1607.00011](#).

[67] S. Gariazzo, C. Giunti, M. Laveder, and Y. F. Li, JHEP **06**, 135 (2017), [1703.00860](#).

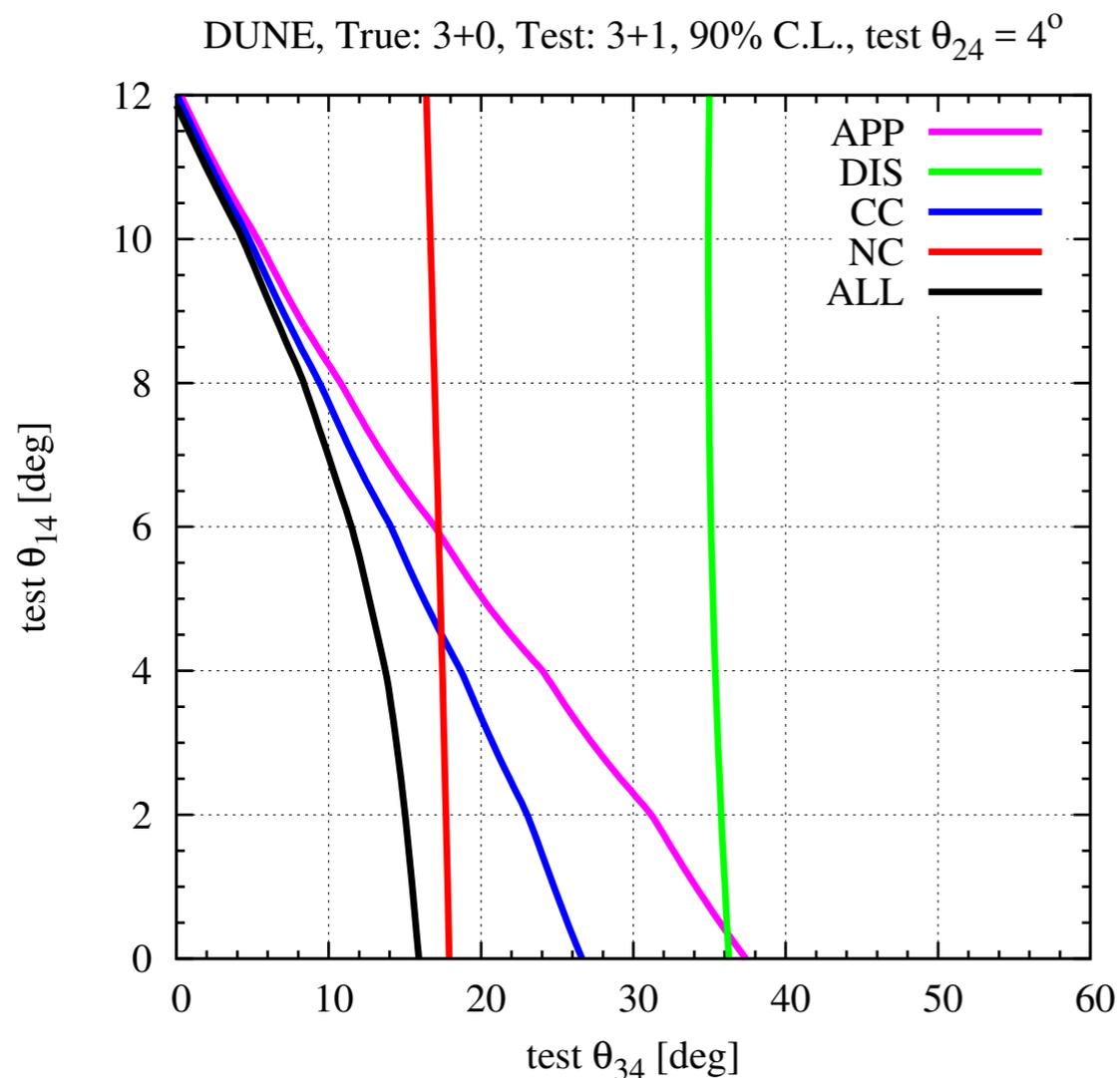
P. Adamson et al. (NOvA) (2017),  
1706.04592



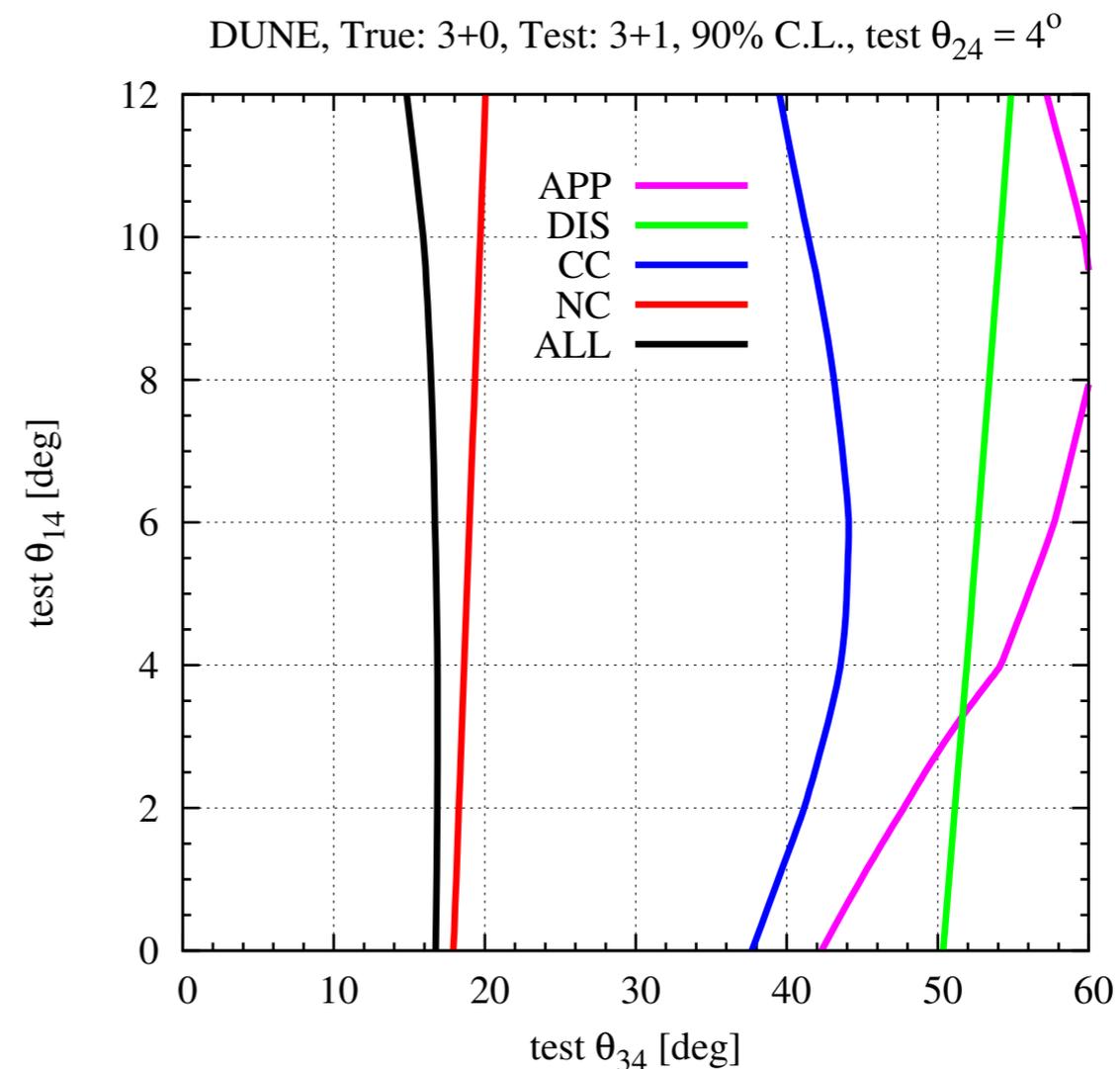
TABLE III: The 90% C.L. upper limits on sterile mixing angles and matrix elements for NOvA compared to MINOS [24], Super-Kamiokande [26], IceCube [27], and IceCube-DeepCore [68]. The limits are shown for  $\Delta m_{41}^2 = 0.5 \text{ eV}^2$  for all experiments, except for IceCube-DeepCore, where the results are reported for  $\Delta m_{41}^2 = 1.0 \text{ eV}^2$ .

	$\theta_{24}$	$\theta_{34}$	$ U_{\mu 4} ^2$	$ U_{\tau 4} ^2$
NOvA	20.8°	31.2°	0.126	0.268
MINOS	7.3°	26.6°	0.016	0.20
SuperK	11.7°	25.1°	0.041	0.18
IceCube	4.1°	-	0.005	-
IceCube-DeepCore	19.4°	22.8°	0.11	0.15

# Constraining 3+1 with NC events



Left: CP phases fixed at true values  
Right: CP phases varied in the fit

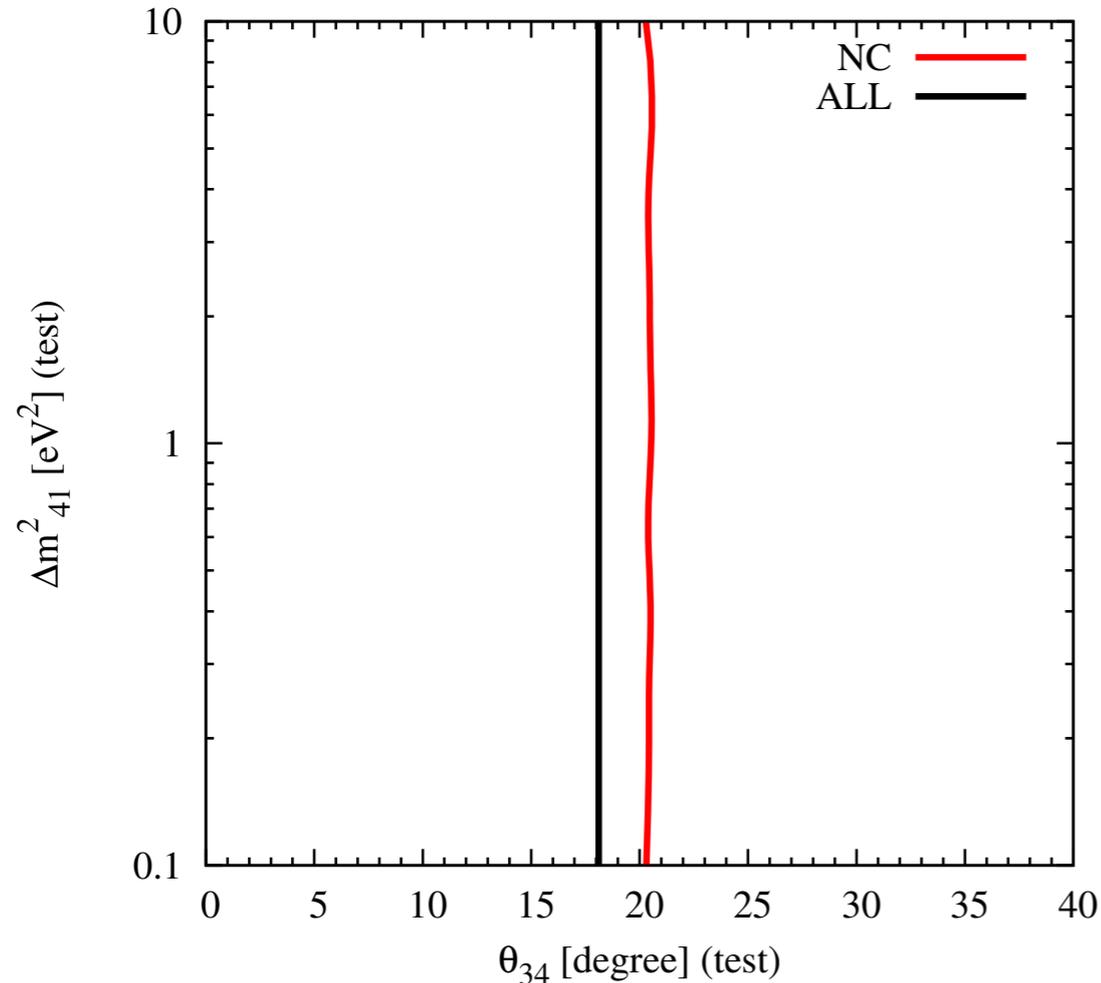


test  $\Delta m_{41}^2 = 1 \text{ eV}^2$   
true  $\delta_{13} = -90^\circ$

Even with CP violating phases present, it would be easier to rule out a moderately large value of  $\Theta_{34}$  with the NC data compared to ruling out moderately large values of  $\Theta_{14}$  and  $\Theta_{24}$  with the CC data

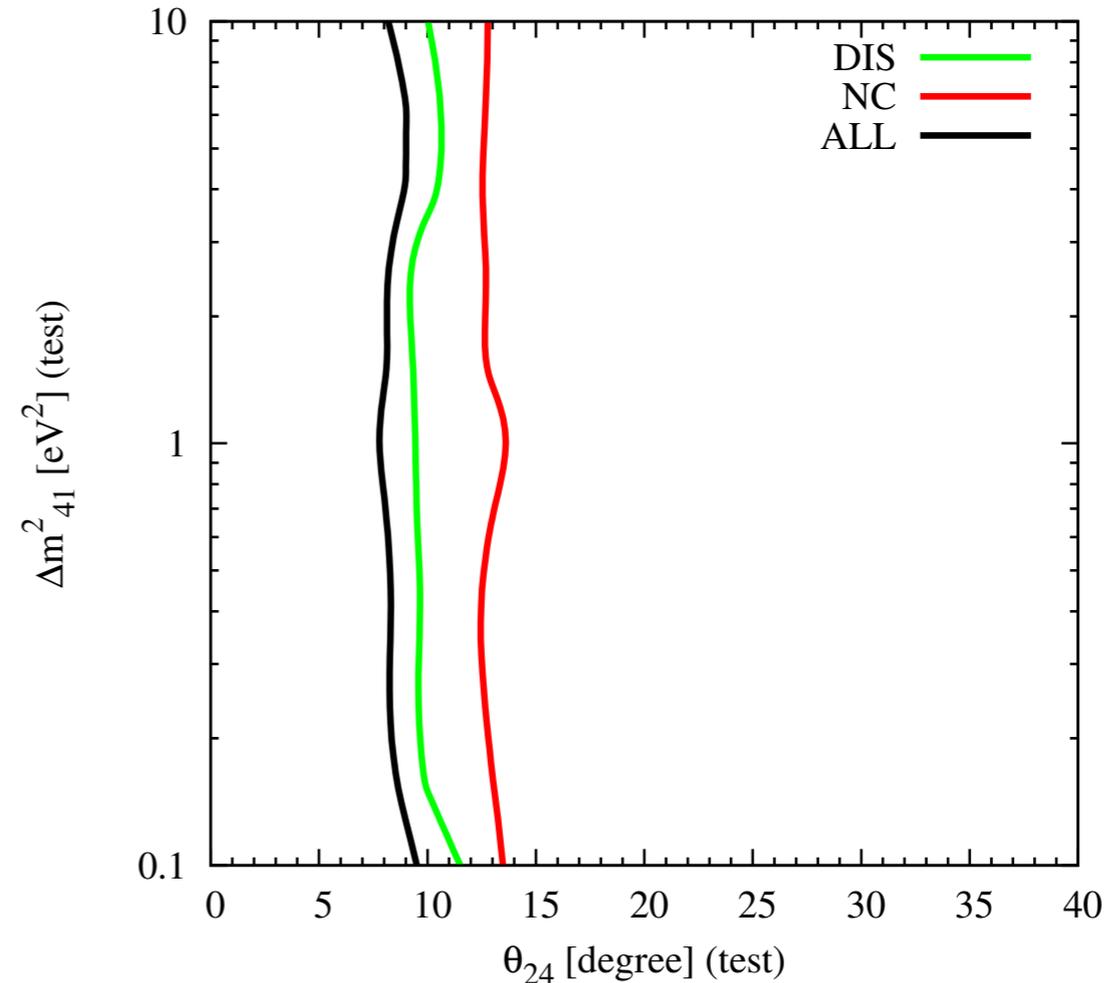
# Constraining 3+1

NH, DUNE, True: 3+0, Test: 3+1, 90% C.L.



sensitivity to the exclusion  
of  $\Theta_{34}$  comes from the NC  
data

NH, DUNE, True: 3+0, Test: 3+1, 90% C.L.



sensitivity to the exclusion  
of  $\Theta_{24}$  comes from the  
disappearance data

DUNE can provide a strong constraint on  $\Theta_{24}$  and  $\Theta_{34}$  that is relatively  
independent of test  $\Delta m^2_{41}$

## **DUNE sensitivities to the mixing between sterile and tau neutrinos**

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(Dated: July 17, 2017)

# Implications & Conclusions

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We examine how NC events can synergistically aid the search for new physics and CP violation when combined with other measurements.

We show that typically the NC events offer a window to CP phases and mixing angles that is complementary to that accessed by CC event measurements.

They can break degeneracies existing in CC measurements, allowing one to distinguish between new physics that violates  $3+0$  unitarity and new physics that does not.

NC events seem not to be affected greatly by matter effects which arise at energies and baselines relevant to DUNE, rendering analytical understanding of new physics somewhat easier.

Thank you :)

# Sterile Neutrinos

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The standard three flavour framework provides a satisfactory fit to most of the existing data.

However, there are several observed anomalies (excesses or deficits) in the data which cannot be fit with a three flavour framework.

These anomalies can be accommodated (in varying capacities) in an extended framework where we have one or more additional neutrino flavours.

From LEP measurements, the number of active neutrinos which participate in the weak interactions can only be three. Therefore, these additional flavours must be  $SU(2) \times U(1)$  singlets.

These “Sterile” neutrinos will not undergo any of the known standard interactions except gravitational.

They can however mix with the active flavours and can possibly be detected via neutrino oscillations.

# Latest Oscillation Measurements

## Status of neutrino oscillations 2017

P. F. de Salas, D. V. Forero, C. A. Ternes, M. Tortola, J. W. F. Valle

parameter	best fit $\pm 1\sigma$		
$\Delta m_{21}^2$ [ $10^{-5}\text{eV}^2$ ]	$7.56 \pm 0.19$		
$ \Delta m_{31}^2 $ [ $10^{-3}\text{eV}^2$ ] (NO)	$2.55 \pm 0.04$	$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.155^{+0.090}_{-0.075}$
$ \Delta m_{31}^2 $ [ $10^{-3}\text{eV}^2$ ] (IO)	$2.49 \pm 0.04$	$\theta_{13}/^\circ$	$8.44^{+0.18}_{-0.15}$
$\sin^2 \theta_{12}/10^{-1}$	$3.21^{+0.18}_{-0.16}$	$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.140^{+0.082}_{-0.085}$
$\theta_{12}/^\circ$	$34.5^{+1.1}_{-1.0}$	$\theta_{13}/^\circ$	$8.41^{+0.16}_{-0.17}$
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$4.30^{+0.20}_{-0.18} \text{ }^a$	$\delta/\pi$ (NO)	$1.40^{+0.31}_{-0.20}$
$\theta_{23}/^\circ$	$41.0 \pm 1.1$	$\delta/^\circ$	$252^{+56}_{-36}$
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.96^{+0.17}_{-0.18} \text{ }^b$	$\delta/\pi$ (IO)	$1.44^{+0.26}_{-0.23}$
$\theta_{23}/^\circ$	$50.5 \pm 1.0$	$\delta/^\circ$	$259^{+47}_{-41}$

Liquid Scintillator Neutrino Detector (1993–1998)  
Los Alamos National Laboratory

Source: Decay-at-rest Pions



Signal events:

App:  $\text{anti-}\nu_e + p \rightarrow e^+ + n$  - IBD events

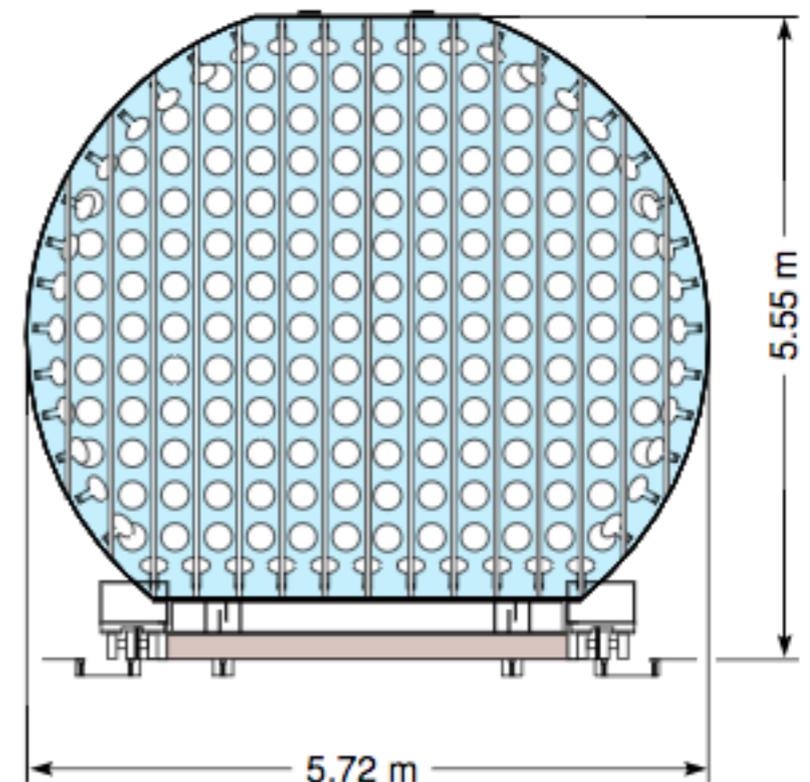
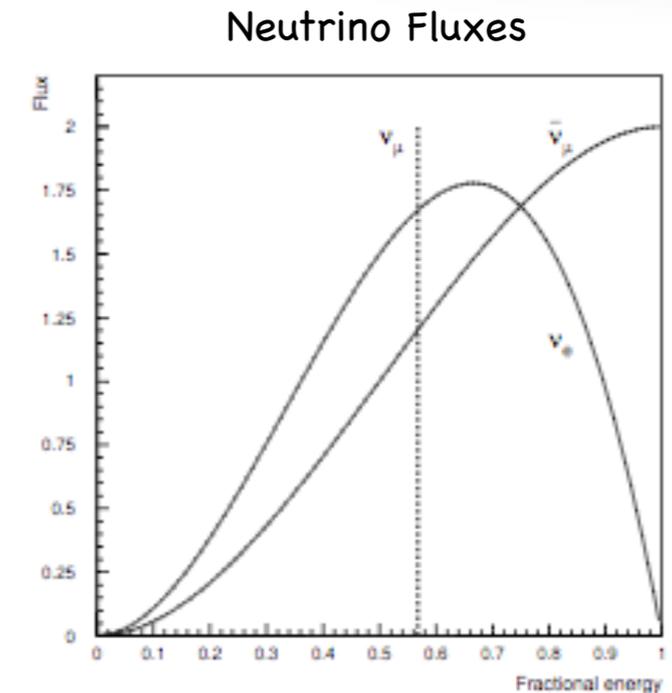
Correlated neutron capture - 2.2 MeV  $\gamma$

Signal events:

Disapp:  $\nu_e + {}^{12}\text{C} \rightarrow {}^{12}\text{N}_{\text{gs}} + e^-$

No correlated neutron capture

$L = 30 \text{ m}$ ,  $E_\nu \in [20 \text{ MeV}, 52 \text{ MeV}]$   $L/E \sim 1\text{m/MeV}$



8.3 m long by 5.7 m in diameter

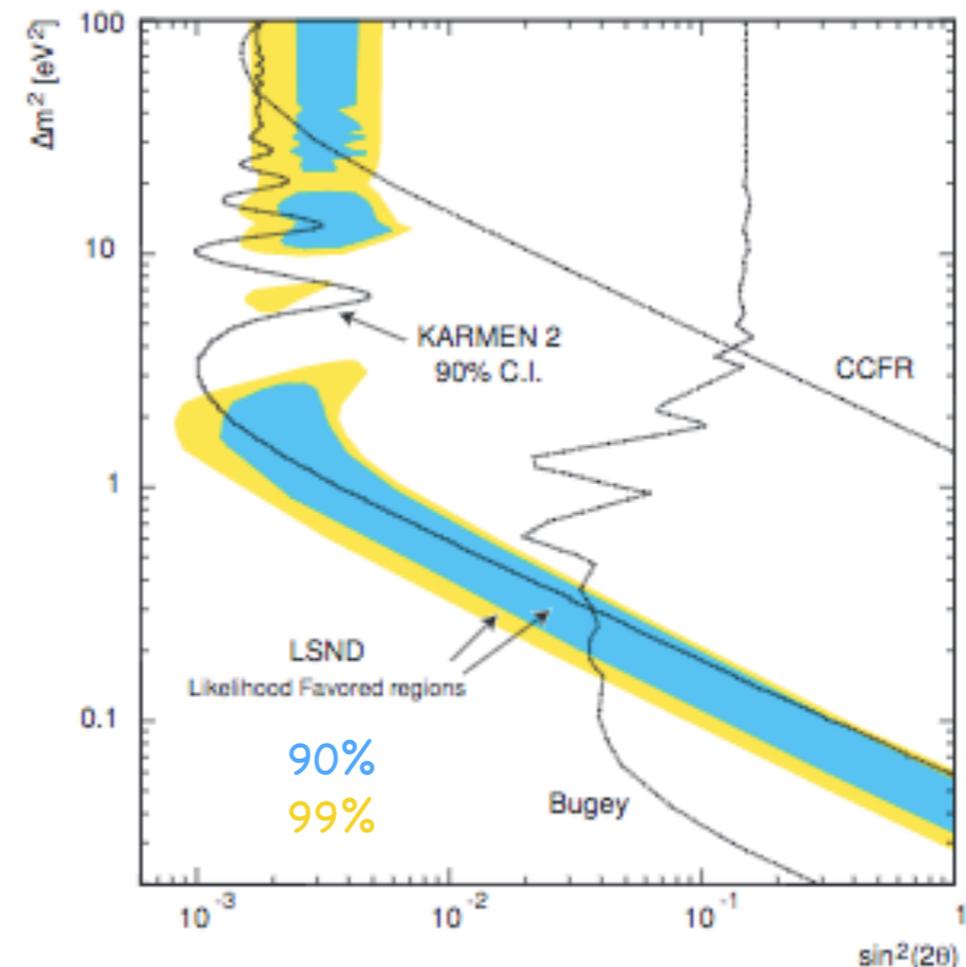
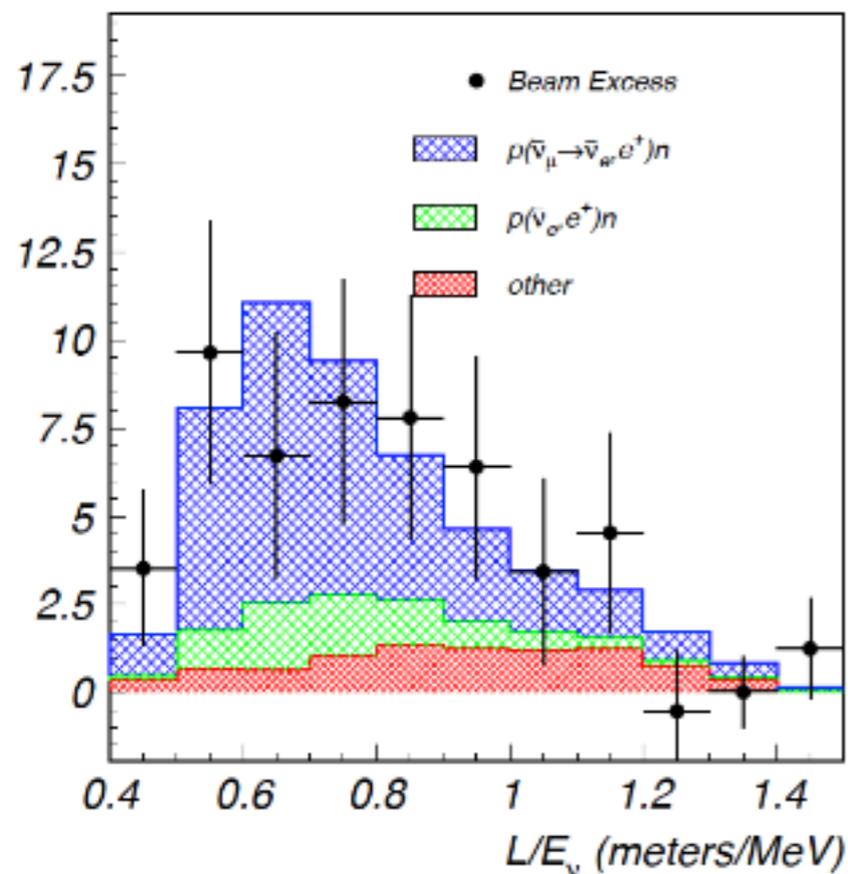
LSND observed an excess of  $87.9 \pm 22.4 \pm 6.0$  events over the expected backgrounds

For 100% conversion of  $\bar{\nu}_\mu$  to  $\bar{\nu}_e$ ,  
33,300  $\pm$  3,300 events expected.  
Prob =  $(0.00264 \pm 0.00067 \pm 0.00045)$

The Karlsruhe-Rutherford Medium  
Energy Neutrino

D-A-R beam, L = 17.7 m

$N^{\text{obs}} = 15$  anti- $\nu_e$  events,  
consistent with  
 $N^{\text{exp}}_{\text{BG}} = 15.8 \pm 0.5$



Mini Booster Neutrino Experiment  
made use of the conventional  
decay-in-flight neutrino beam at Fermilab.

$L = 541 \text{ m}$ , peak  $E_\nu \sim 800 \text{ MeV}$

Although LSND and MiniBooNE  
probe similar  $L/E$  region, they have  
very different event signatures,  
backgrounds and systematics.

2002 - 2012

$\nu$  :  $6.46e20 \text{ POT}$

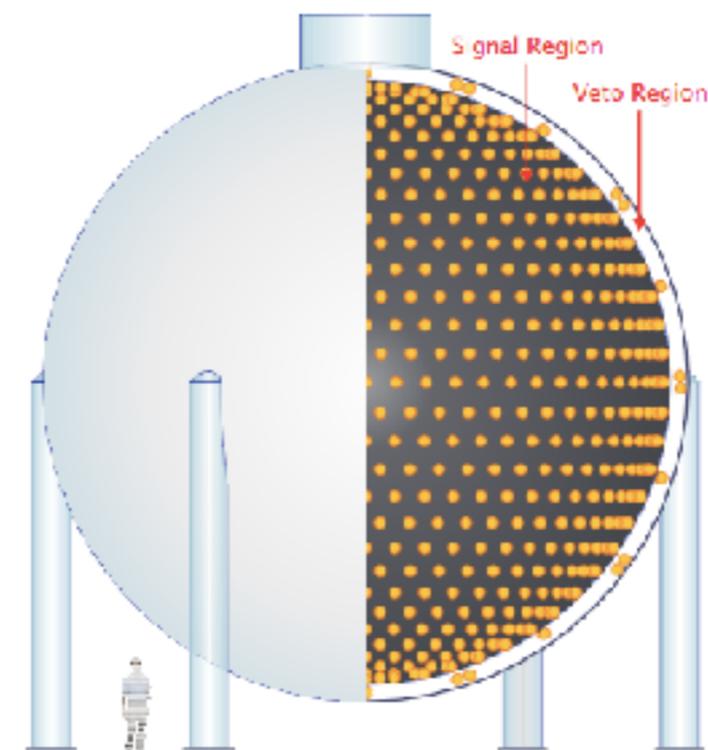
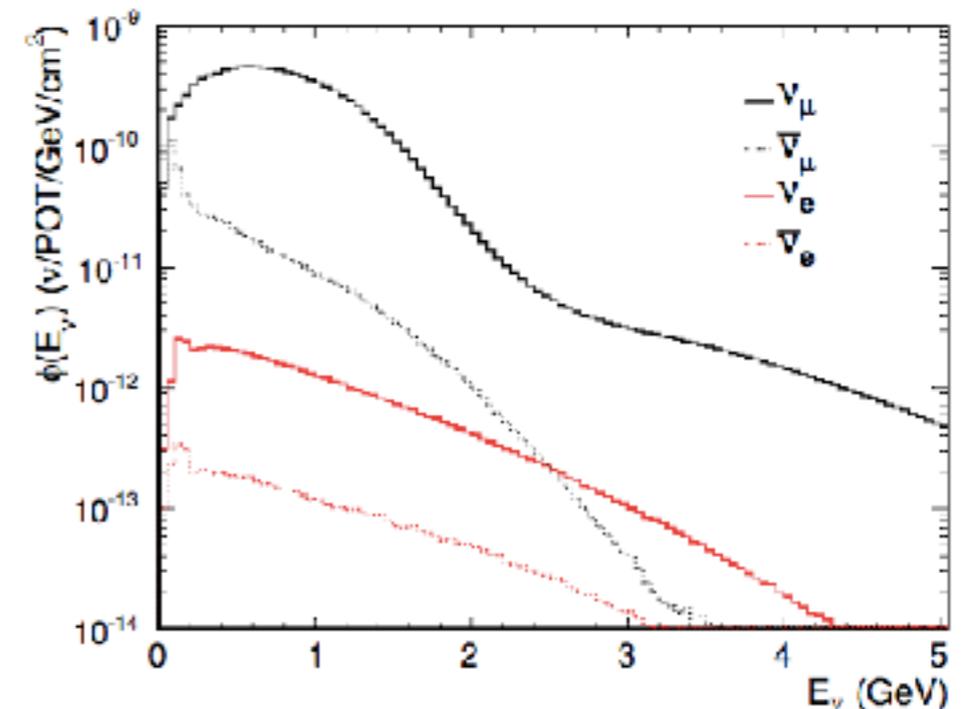
anti- $\nu$ :  $11.27e20 \text{ POT}$

$\nu_\mu \rightarrow \nu_e$  :  $\nu_e + n \rightarrow e^- + p$

anti- $\nu_\mu \rightarrow \text{anti-}\nu_e$  :  $\text{anti-}\nu_e + p \rightarrow e^+ + n$

CCQE events

Booster Neutrino Beam



12.2 m diameter spherical  
tank filled with Mineral Oil

$E_{\nu}^{\text{QE}} \in [200 \text{ MeV}, 1250 \text{ MeV}]$

$\nu$  mode:

expected BG:  $790.0 \pm 28.1 \pm 38.7$

observed: 952

excess:  $162 \pm 47.8$

anti- $\nu$  mode:

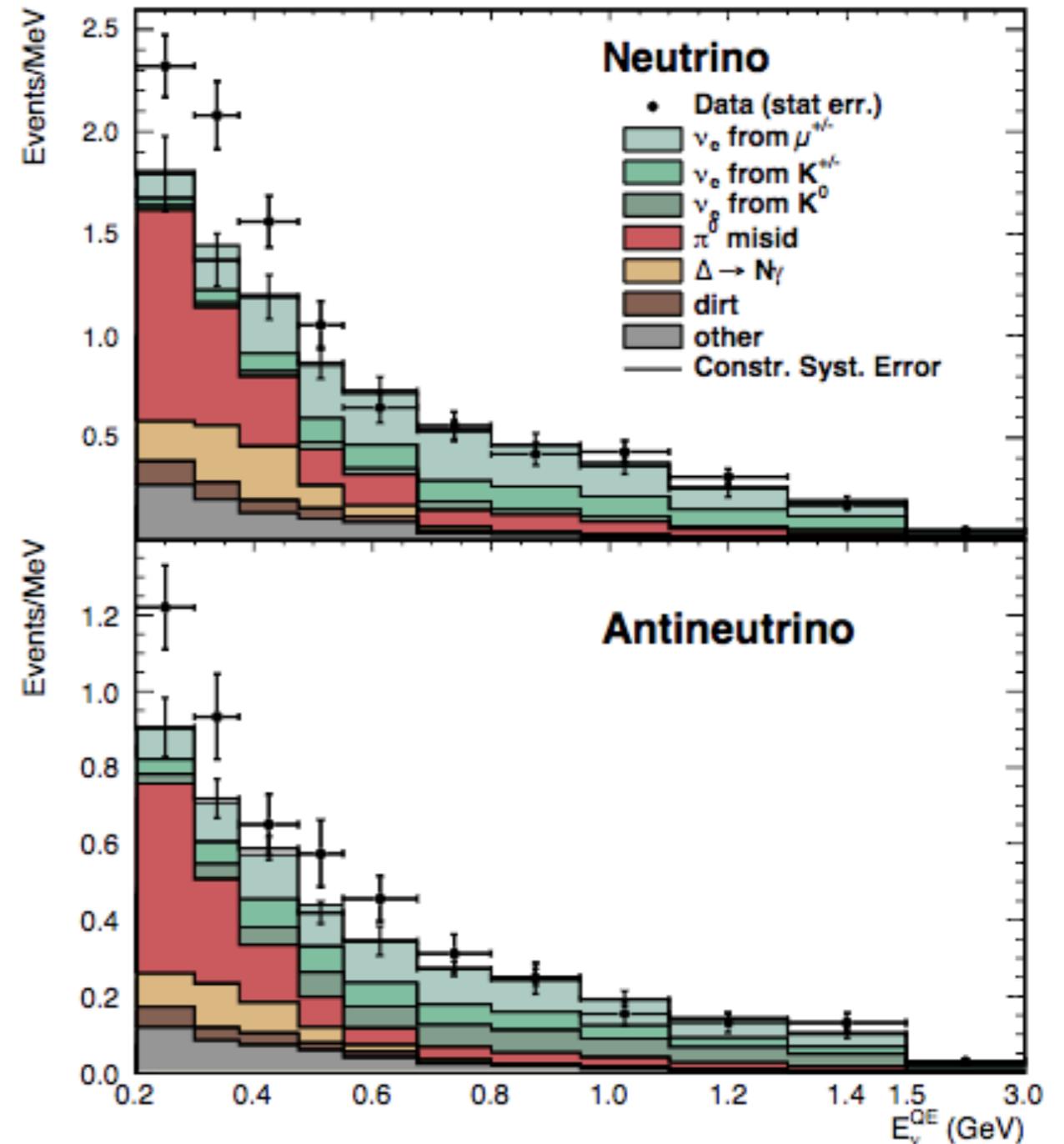
expected BG:  $399.6 \pm 20.0 \pm 20.3$

observed: 478

excess:  $78.4 \pm 28.5$

The backgrounds in MiniBooNE are very well understood and are constrained directly from in-situ measurements.

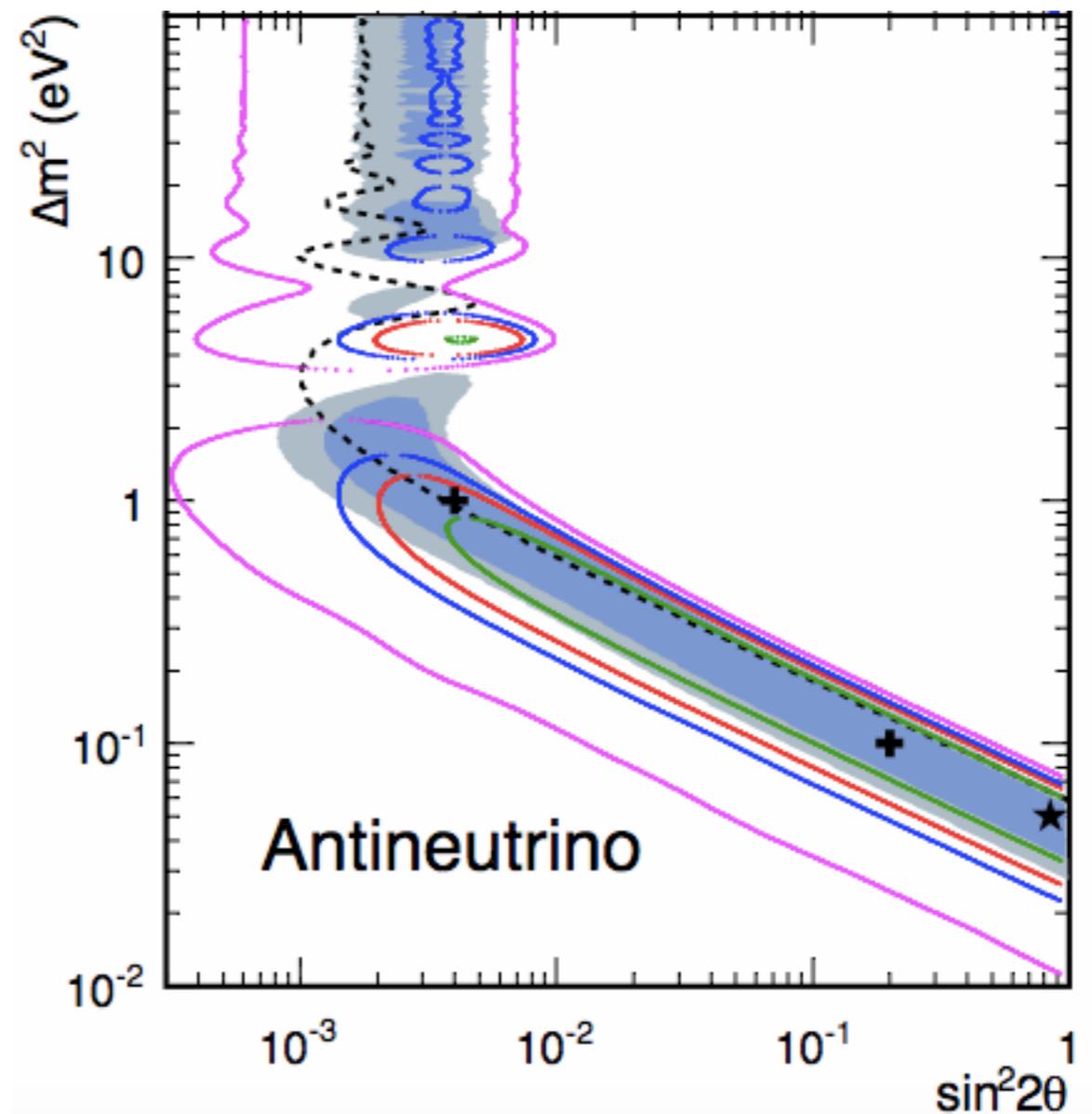
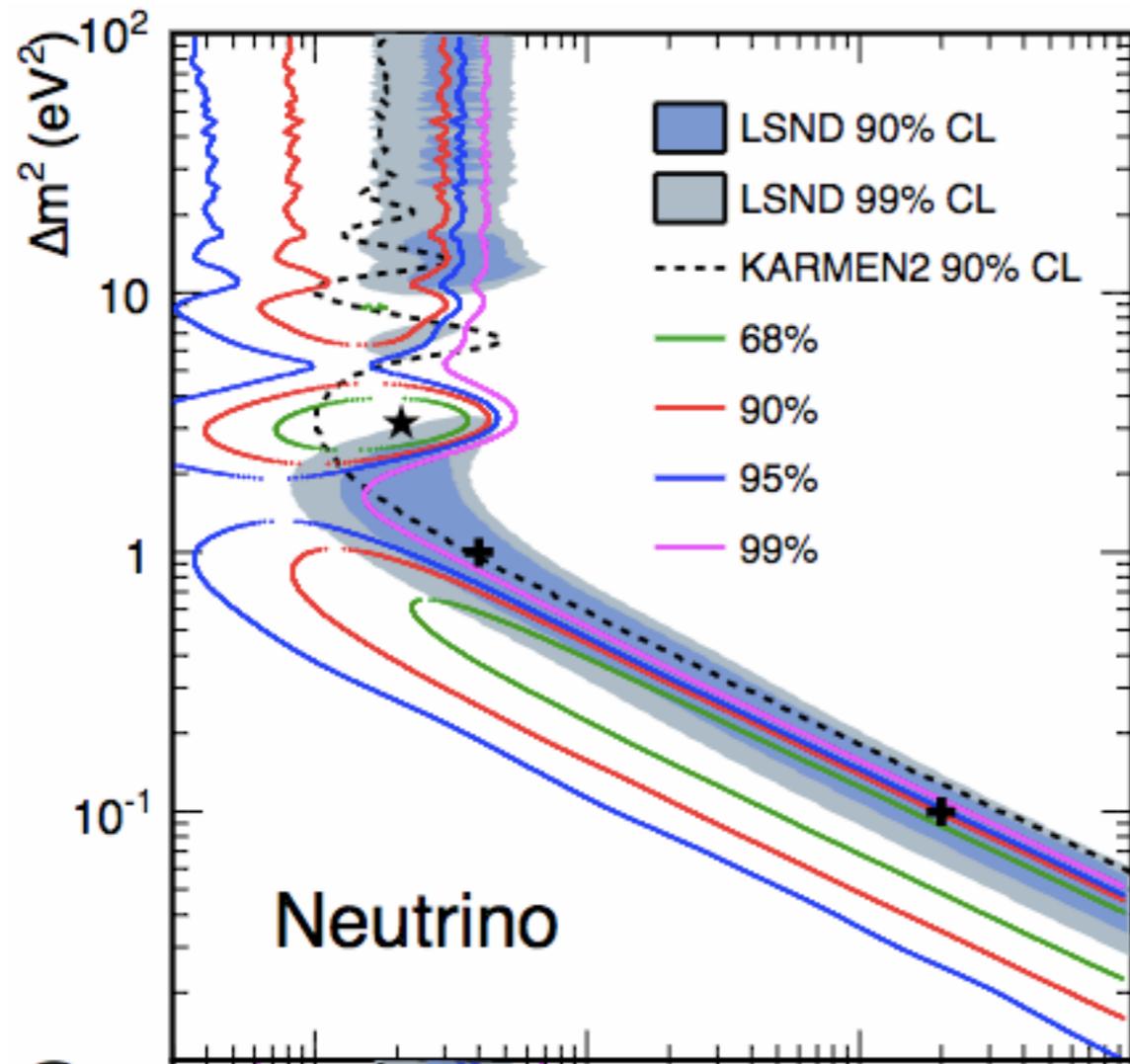
Low energy excess



# MiniBooNE results in 3+1

MiniBooNE anti-neutrino results are consistent with LSND

The neutrino results are less so!



# LSND & MiniBooNE: Stressed-out 3+1

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$$\sin^2 2\theta_{\mu\mu} = 4U_{\mu 4}^2(1 - U_{\mu 4}^2) \quad (\mu \text{ flavor}),$$

$$\sin^2 2\theta_{ee} = 4U_{e 4}^2(1 - U_{e 4}^2) \quad (e \text{ flavor}).$$

$$\sin^2 2\theta_{e\mu} = 4U_{e 4}^2 U_{\mu 4}^2.$$

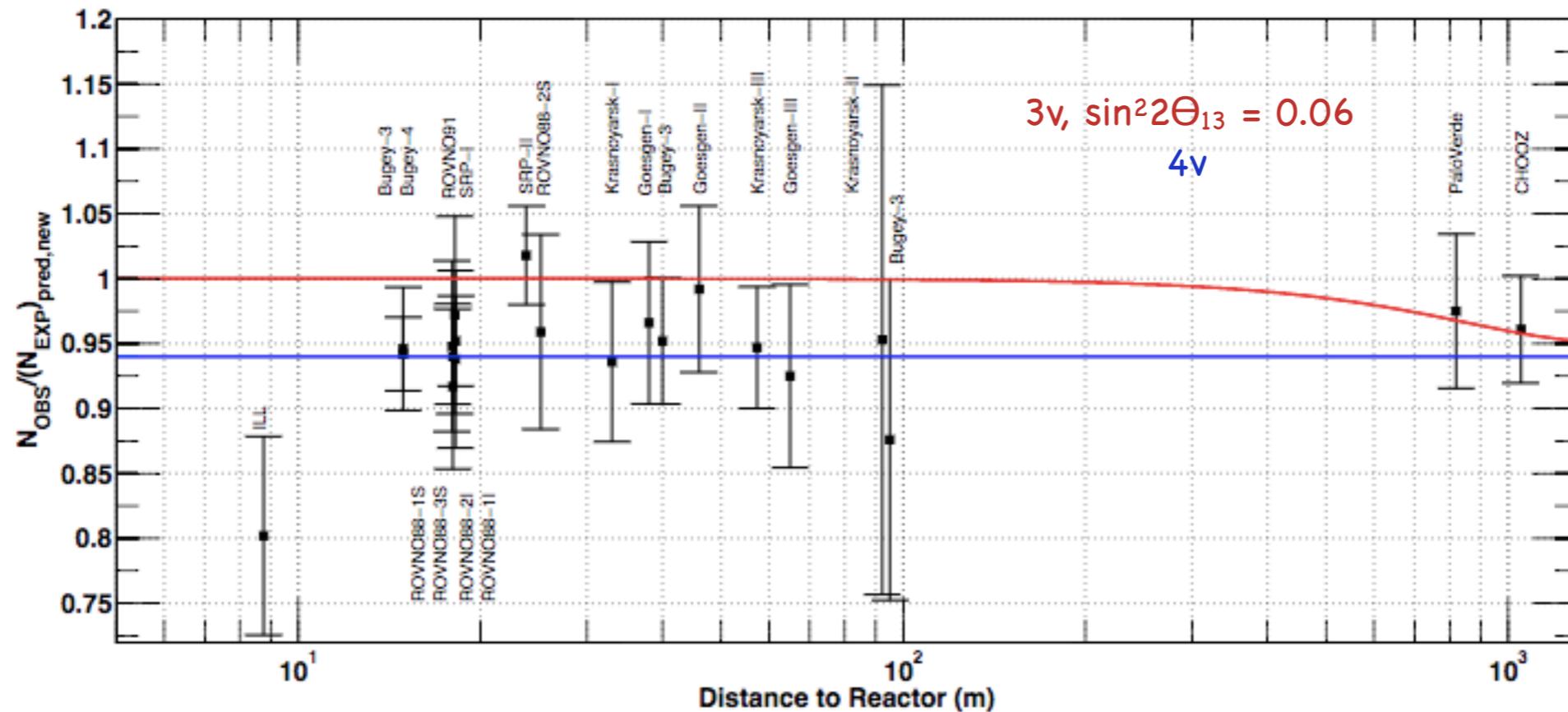
LSND - KARMEN cross section analyses :  $|U_{e 4}|^2 \lesssim 0.05$

MiniBooNE - SciBooNE joint analysis :  $|U_{\mu 4}|^2 \lesssim 0.025$

The disappearance results favour a very small appearance mixing angle  
 $\sin^2 2\theta_{\mu e} \sim 0.005$  - inconsistent with LSND and MiniBooNE

3+2 fits improve the disagreement between  $\nu$  and anti- $\nu$  but worsen the discrepancy between appearance and disappearance

# The Reactor Antineutrino anomaly



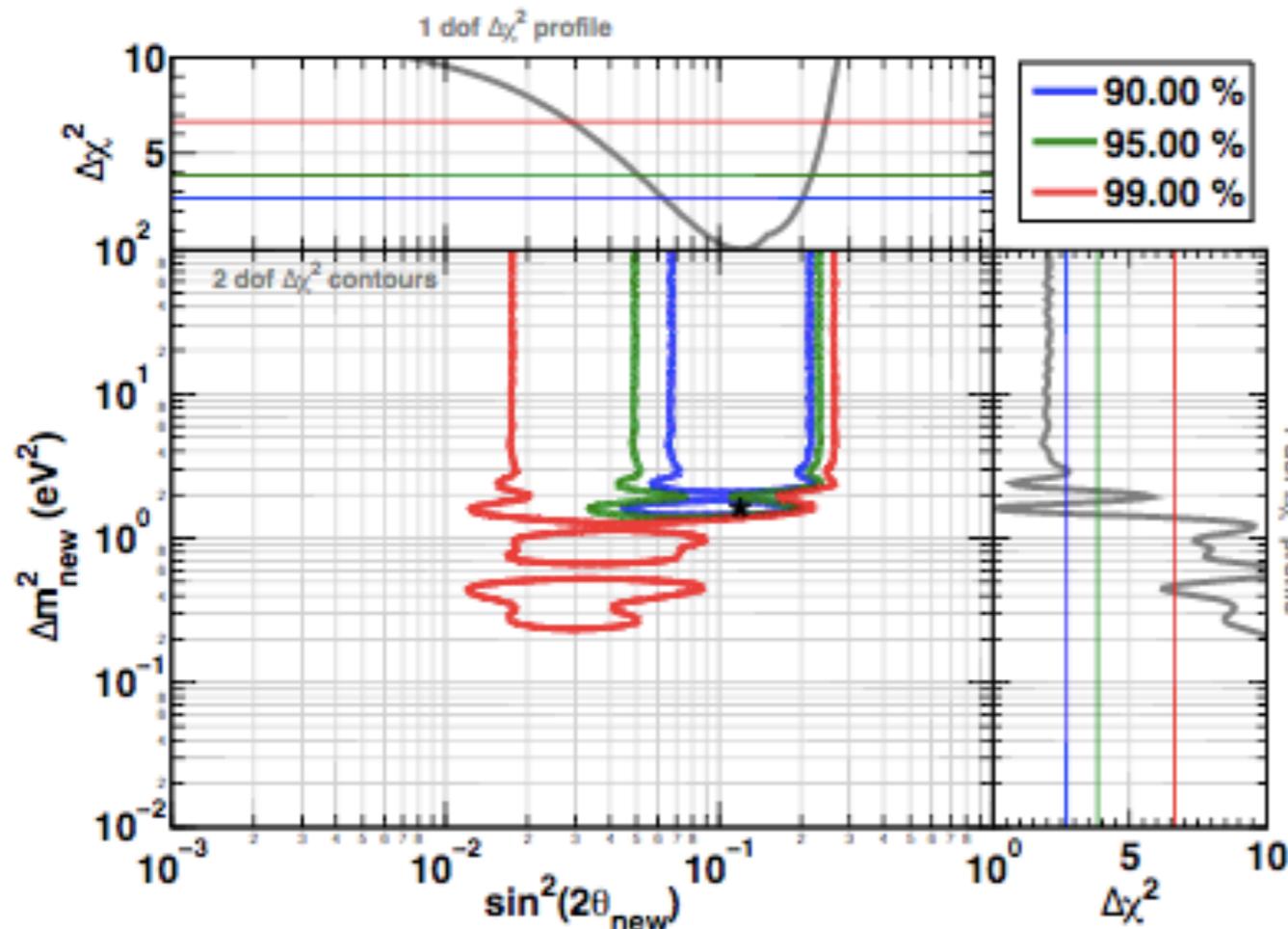
A recalculation of the reactor antineutrino spectrum leads to an increment of the mean flux by about 3%

$N_{\text{obs}}/N_{\text{exp}}$  for experiments with  $L > 15$  m changes from  $0.976 \pm 0.02$  to  $0.943 \pm 0.023$ , leading to 98.6% C.L. deviation from Unity.

# The Reactor Antineutrino anomaly

For baselines below 2 km, assuming 3+1,

$$P_{ee} = 1 - \cos^4 \theta_{\text{new}} \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m_{31}^2 L}{4E_{\bar{\nu}_e}}\right) - \sin^2(2\theta_{\text{new}}) \sin^2\left(\frac{\Delta m_{\text{new}}^2 L}{4E_{\bar{\nu}_e}}\right).$$



The no-oscillation hypothesis is disfavoured at 99.8% C. L.

$|\Delta m_{\text{new}}^2| > 1.5 \text{ eV}^2$  95% C.L.  
 $\sin^2 2\theta_{\text{new}} = 0.14 \pm 0.08$  95% C.L.

1107.2755 PRD

# 3+1 Searches : Daya Bay/Bugey-3 & MINOS

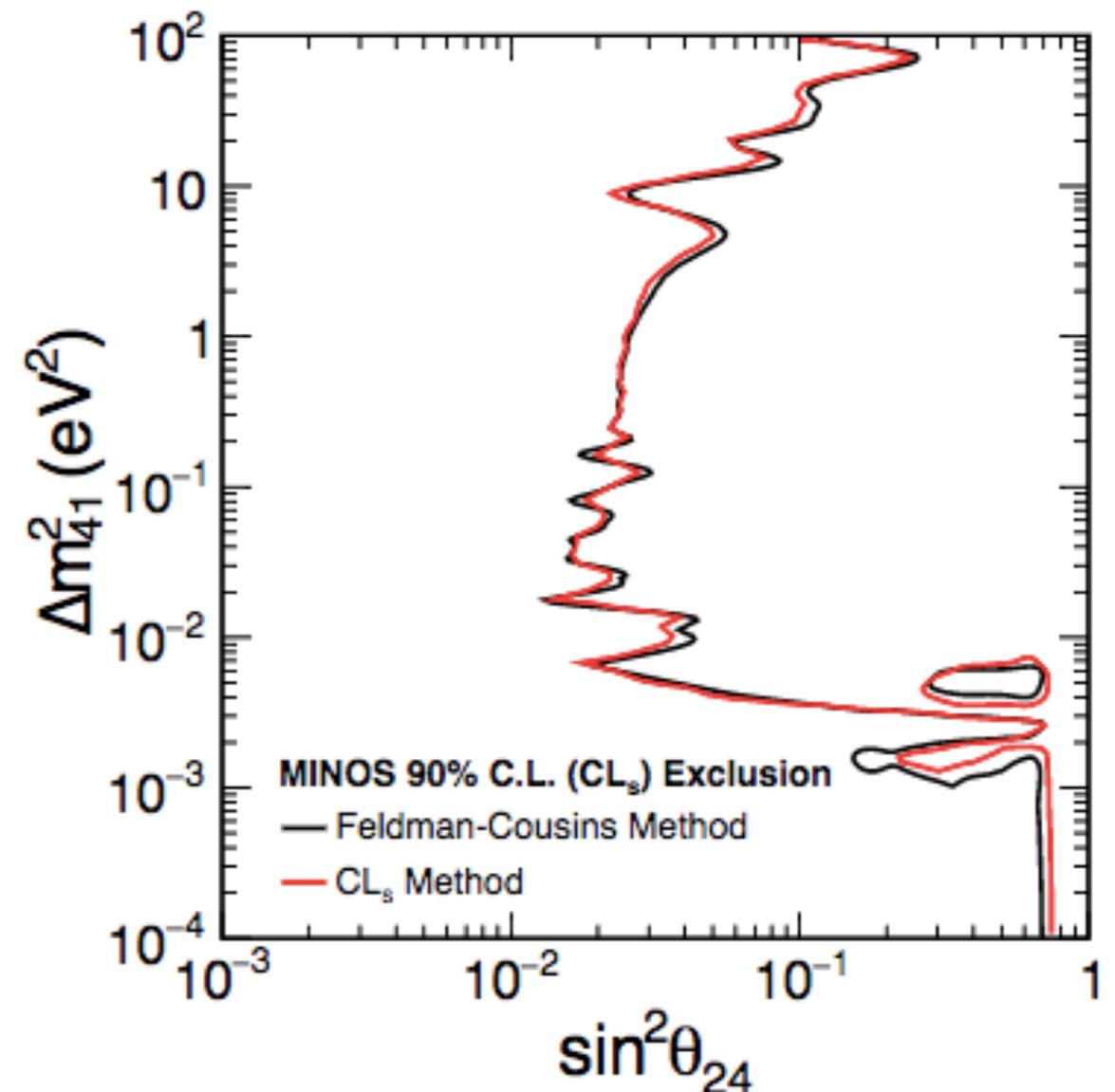
MINOS: Long-baseline super beam experiment  
L = 734 km, peak  $E_\nu = 3$  GeV  
1 kton Near and 5.4 ton Far magnetised steel and  
scintillation calorimeters

1607.01177 PRL

Constrains  $|U_{\mu 4}|^2$  via  $(\text{anti-})\nu_\mu \rightarrow (\text{anti-})\nu_\mu$

Additional sensitivity is obtained by  
analysing the reconstructed energy  
spectrum of NC events

Depending on the  $\Delta m^2$ , there can be  
an oscillatory signature or a depletion  
and therefore a sensitivity to 3+1

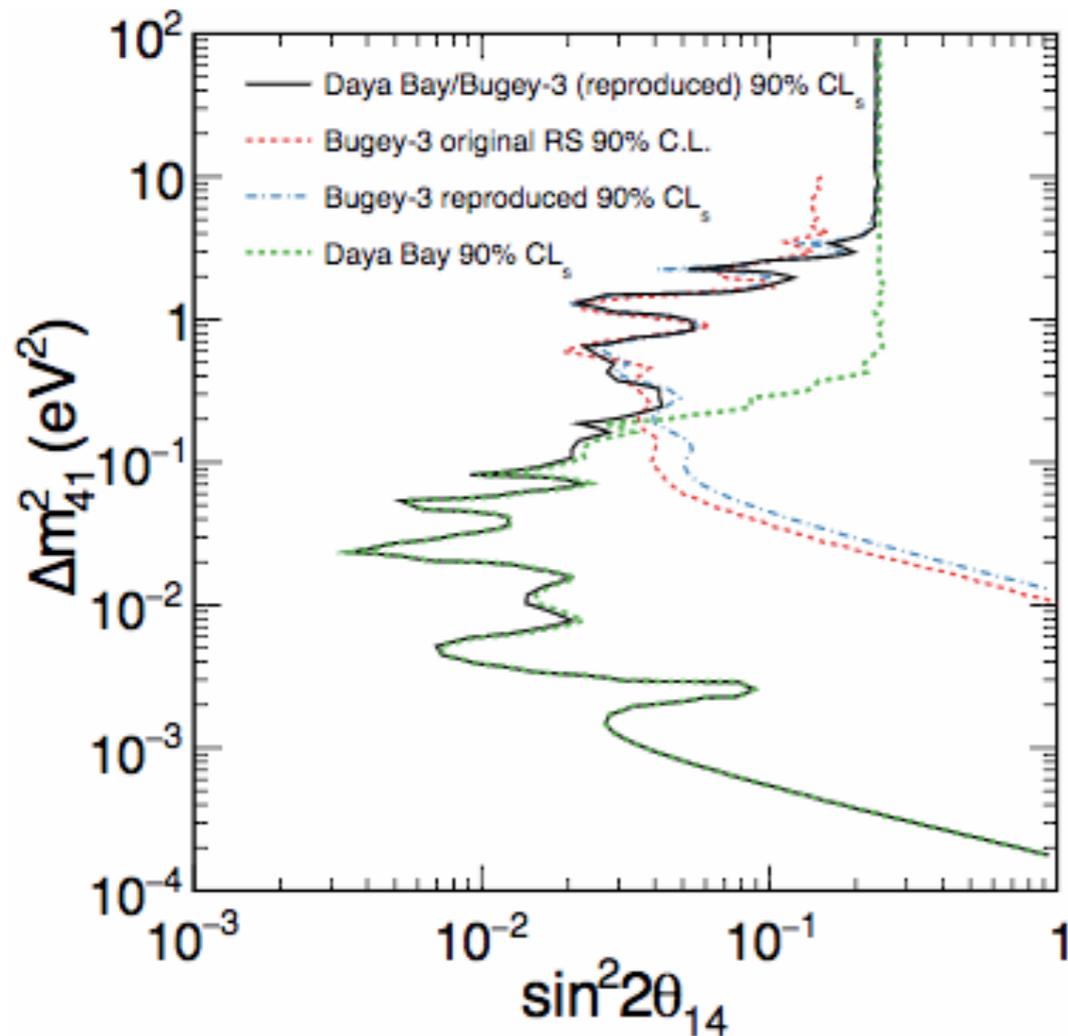


# 3+1 Searches : Daya Bay/Bugey-3 & MINOS

Daya Bay: Reactor anti- $\nu$   
 $L = 520, 570, \text{ and } 1590 \text{ m}$

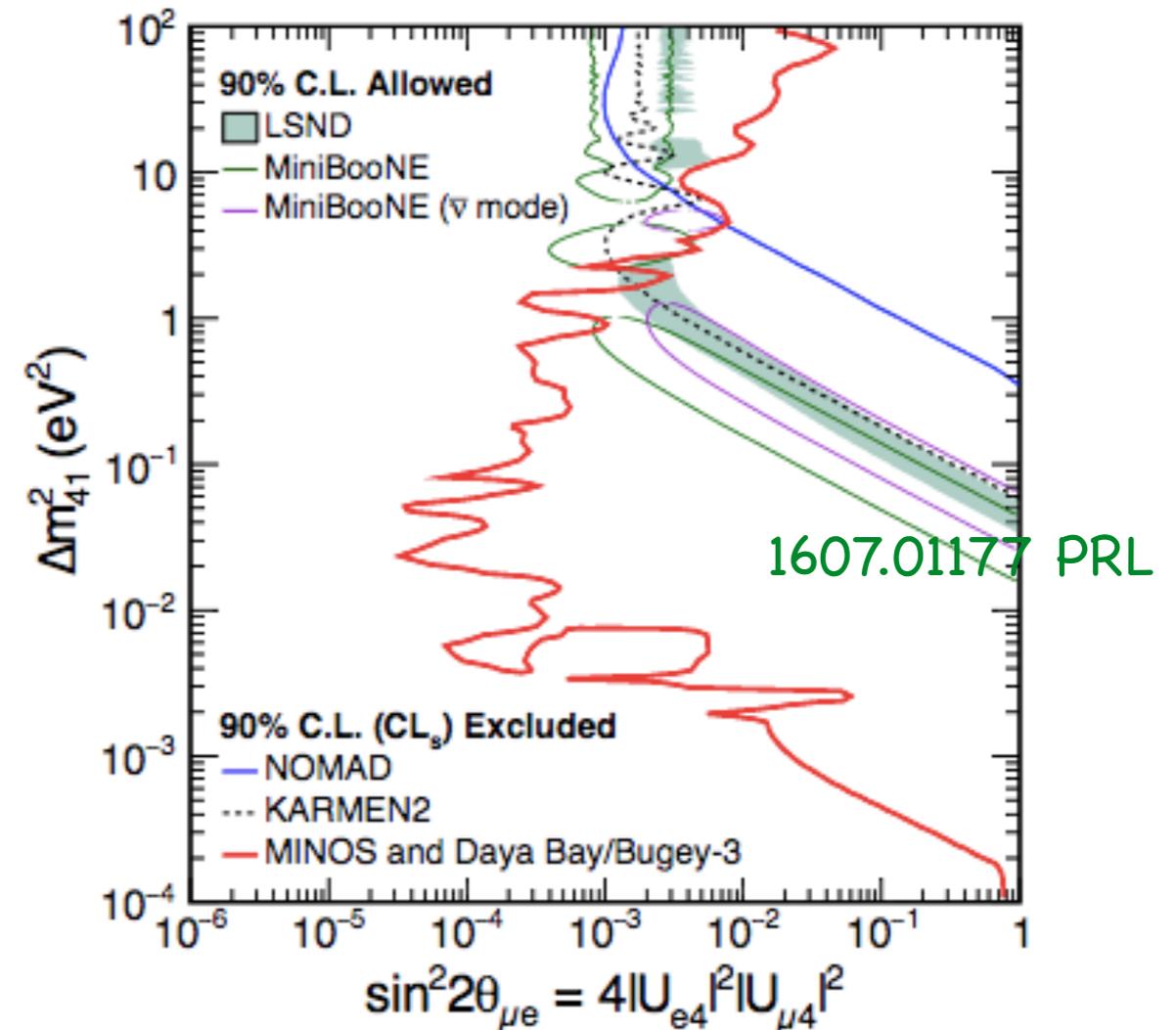
Bugey-3: Reactor anti- $\nu$   
 $L = 15, 40 \text{ and } 95 \text{ m}$

Constrains  $|U_{e4}|^2$  via anti- $\nu_e \rightarrow \text{anti-}\nu_e$



The combined data from MINOS, Daya Bay and Bugey-3 can constrain the LSND and MiniBooNE allowed regions

$\Delta m^2_{41} > 0.8 \text{ eV}^2$  regions are excluded at 95% C.L.



# 3+1 searches : IceCube

Detects atmospheric neutrinos produced in  
Cosmic showers  
throughout the Earth's atmosphere

Only up-going neutrinos are selected

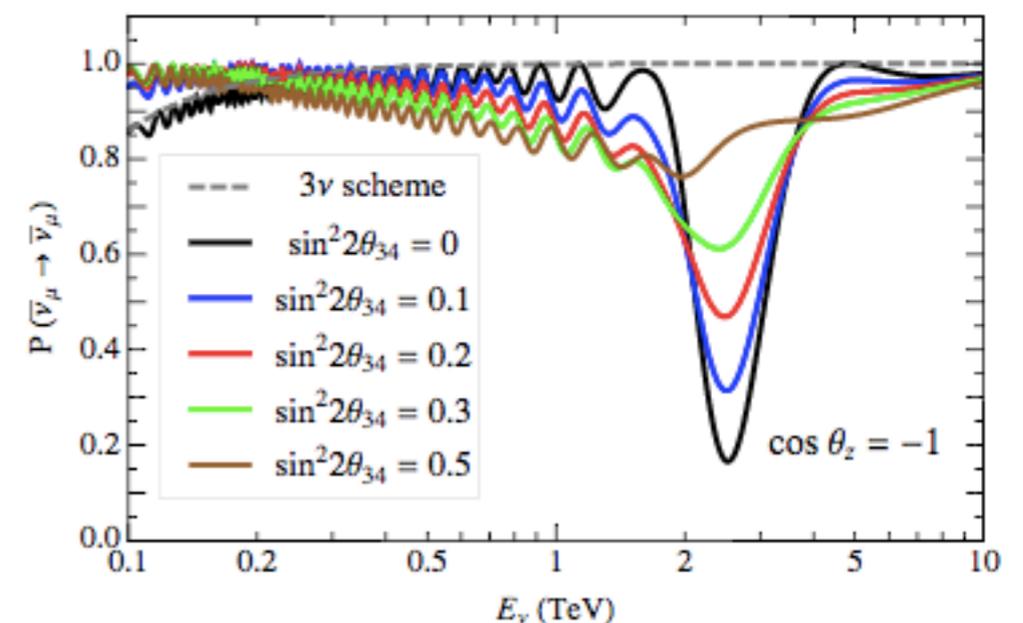
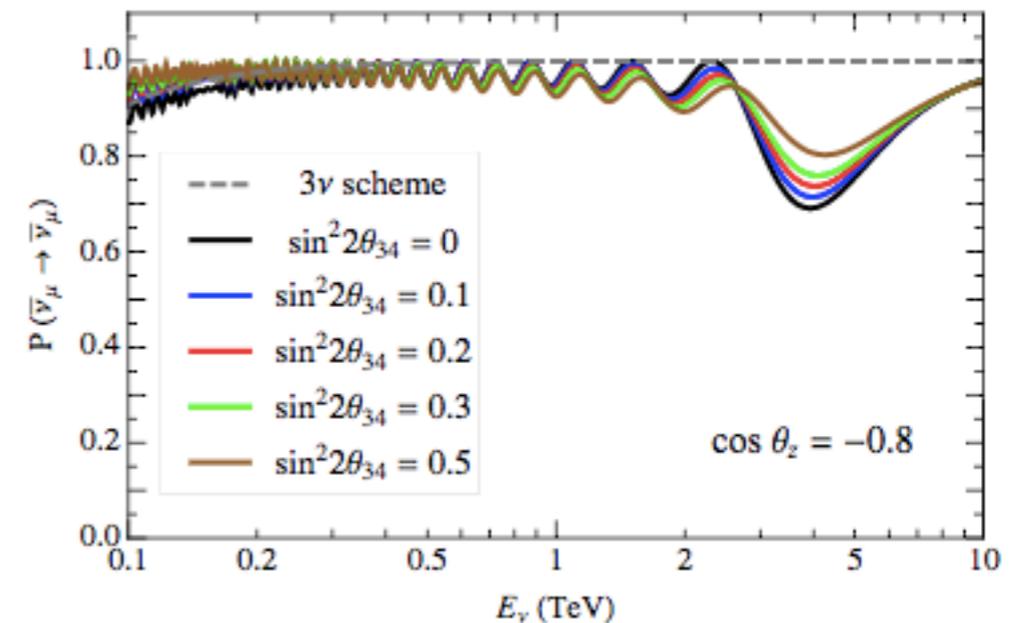
For  $E_\nu > 100$  GeV, oscillations due to  
 $\Delta m^2_{31}$  and  $\Delta m^2_{21}$  can be ignored

Search for  $(\nu_\mu + \text{anti-}\nu_\mu)$  disappearance  
in 320 GeV to 20 TeV range

The MSW effect depletes anti- $\nu$  in  
the 3+1 model or  $\nu$  in 1+3 for  
 $\Delta m^2_{41} \in [0.01 \text{eV}^2, 10 \text{eV}^2]$

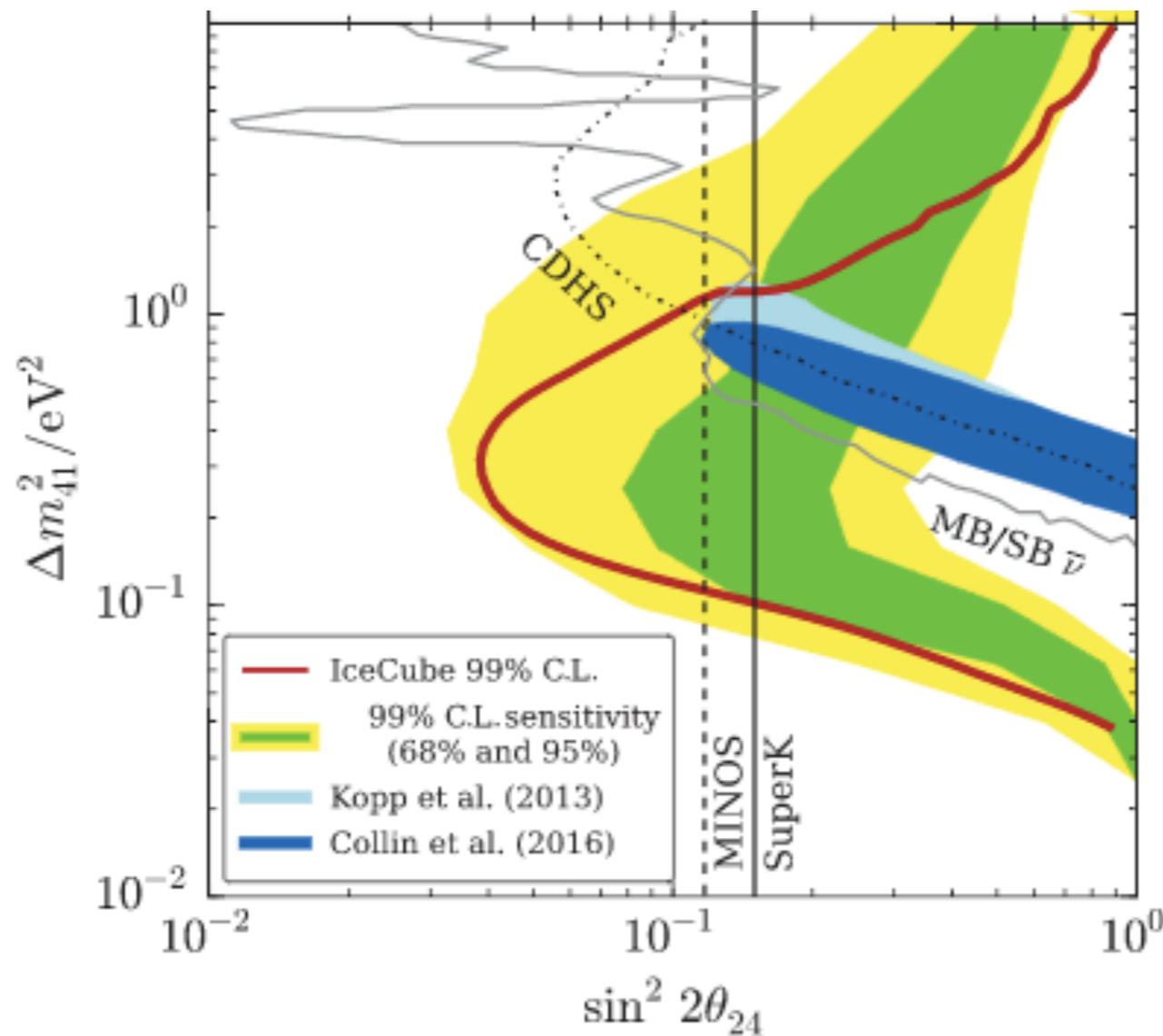
The choice  $\Theta_{34} = 0$  leads  
to the most conservative  
exclusion in  $\Theta_{24}$

1307.6824 JHEP



# 3+1 searches : IceCube

IceCube results along with 99% C. L. allowed regions from Global fits appearance experiments including MiniBooNE and LSND assuming  $|U_{e4}|^2 = 0.023$  and  $|U_{e4}|^2 = 0.027$



1605.01990 PRL

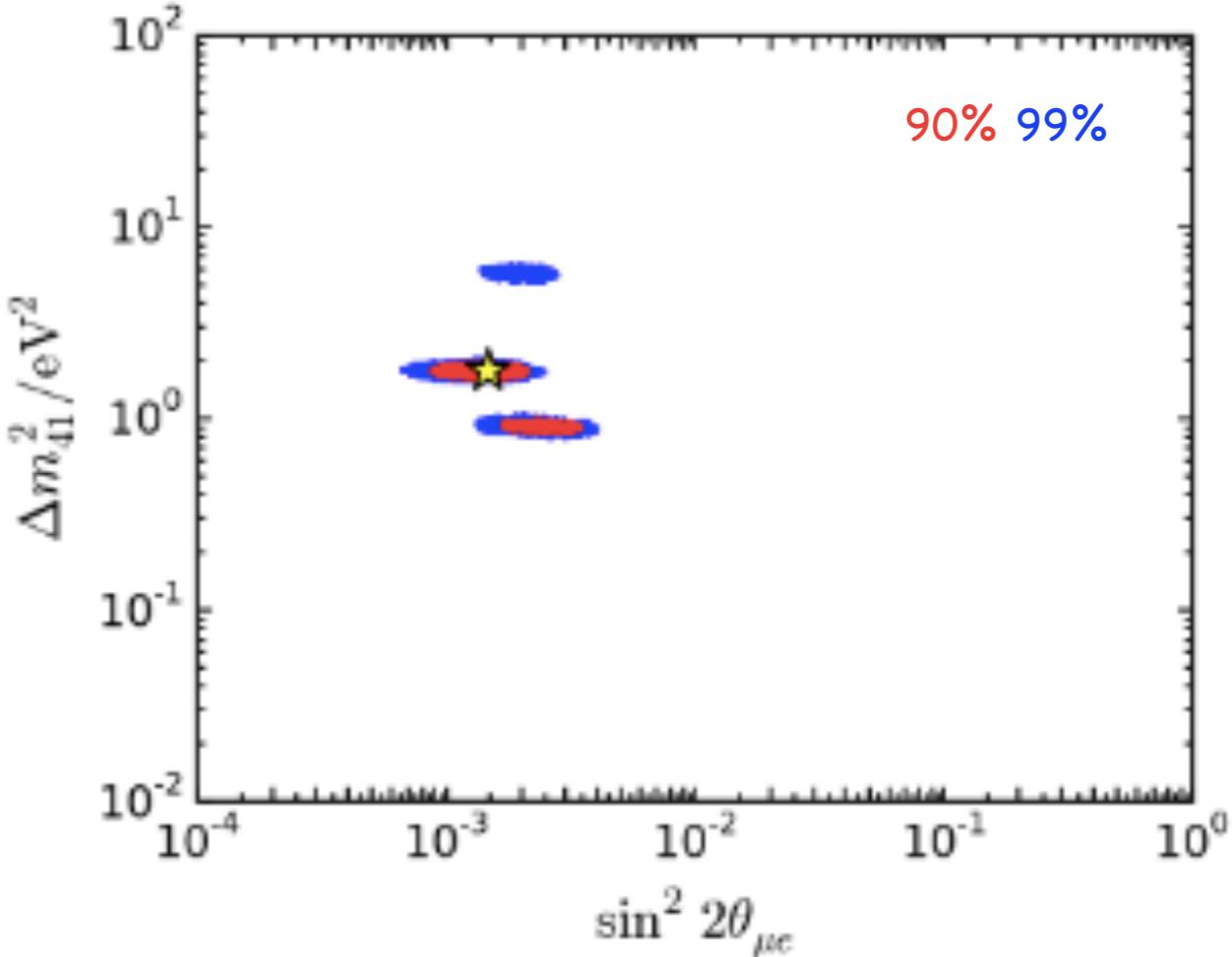
### Data considered

Tag	Process	$\nu$ vs. $\bar{\nu}$	Type	$N_{bins}$
LSND [2]	$\nu_\mu \rightarrow \nu_e$	$\bar{\nu}$	App	5
KARMEN [9]	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$	$\bar{\nu}$	App	9
KARMEN/LSND(xsec) [11]	$\nu_e \rightarrow \nu_e$	$\nu$	Dis	11
BNB-MiniBooNE- $\nu$ [3, 28]	$\nu_\mu \rightarrow \nu_e$	$\nu$	App	19
BNB-MiniBooNE- $\bar{\nu}$ [4, 29]	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$	$\bar{\nu}$	App	19
NuMI-MB( $\nu_{app}$ ) [10]	$\nu_\mu \rightarrow \nu_e$	$\nu$	App	10
Bugey [5, 6]	$\bar{\nu}_e \rightarrow \bar{\nu}_e$	$\bar{\nu}$	Dis	60
Gallium [7, 8]	$\nu_e \rightarrow \nu_e$	$\nu$	Dis	4
BNB-MiniBooNE/SciBooNE- $\nu$ [15]	$\nu_\mu \rightarrow \nu_\mu$	$\nu$	Dis	48
BNB-MiniBooNE/SciBooNE- $\bar{\nu}$ [16]	$\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$	$\bar{\nu}$	Dis	42
NOMAD [12]	$\nu_\mu \rightarrow \nu_e$	$\nu$	App	30
CCFR84 [13]	$\nu_\mu \rightarrow \nu_\mu$	$\nu$	Dis	18
CDHS [14]	$\nu_\mu \rightarrow \nu_\mu$	$\nu$	Dis	15
MINOS-CC [17, 18]	$\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$	$\bar{\nu}$	Dis	25

### Best fit

3+1	$\Delta m_{41}^2$	$ U_{e4} $	$ U_{\mu 4} $
All	1.75	0.163	0.117

$\Delta\chi^2$  (dof) = 52.34 (3) w.r.t. null hypothesis



Data considered

+ IceCube IC86

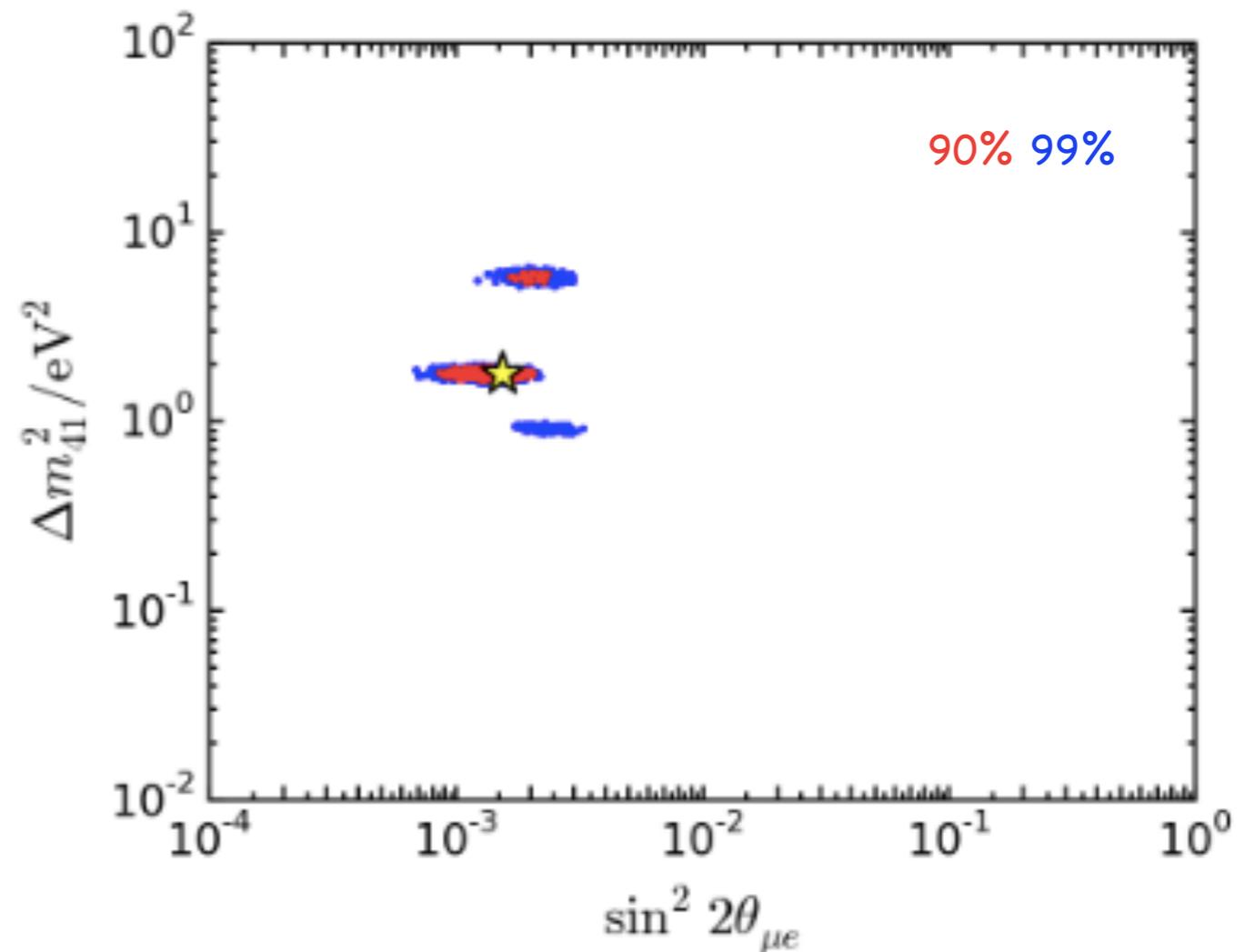
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LSND [2]	$\nu_\mu \rightarrow \nu_e$	$\bar{\nu}$	App	5
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KARMEN/LSND(xsec) [11]	$\nu_e \rightarrow \nu_e$	$\nu$	Dis	11
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BNB-MiniBooNE- $\bar{\nu}$ [4, 29]	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$	$\bar{\nu}$	App	19
NuMI-MB( $\nu_{app}$ ) [10]	$\nu_\mu \rightarrow \nu_e$	$\nu$	App	10
Bugey [5, 6]	$\bar{\nu}_e \rightarrow \bar{\nu}_e$	$\bar{\nu}$	Dis	60
Gallium [7, 8]	$\nu_e \rightarrow \nu_e$	$\nu$	Dis	4
BNB-MiniBooNE/SciBooNE- $\nu$ [15]	$\nu_\mu \rightarrow \nu_\mu$	$\nu$	Dis	48
BNB-MiniBooNE/SciBooNE- $\bar{\nu}$ [16]	$\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$	$\bar{\nu}$	Dis	42
NOMAD [12]	$\nu_\mu \rightarrow \nu_e$	$\nu$	App	30
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MINOS-CC [17, 18]	$\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$	$\bar{\nu}$	Dis	25

The significance of the IceCube data is that it excludes the LSND solution at  $\sim 1\text{eV}^2$  at 90% although it does exist at 99%

Best fit

3+1	$\Delta m_{41}^2$	$ U_{e4} $	$ U_{\mu 4} $	$ U_{\tau 4} $
SBL	1.75	0.163	0.117	-
SBL+IC	1.75	0.164	0.119	0.00

$\Delta\chi^2$  (dof) = 50.61 (4) w.r.t. null hypothesis



# The Fermilab SBL neutrino program

The primary aim of the Fermilab SBL neutrino program is to search for the evidence of Sterile neutrinos as hinted by MiniBooNE and LSND

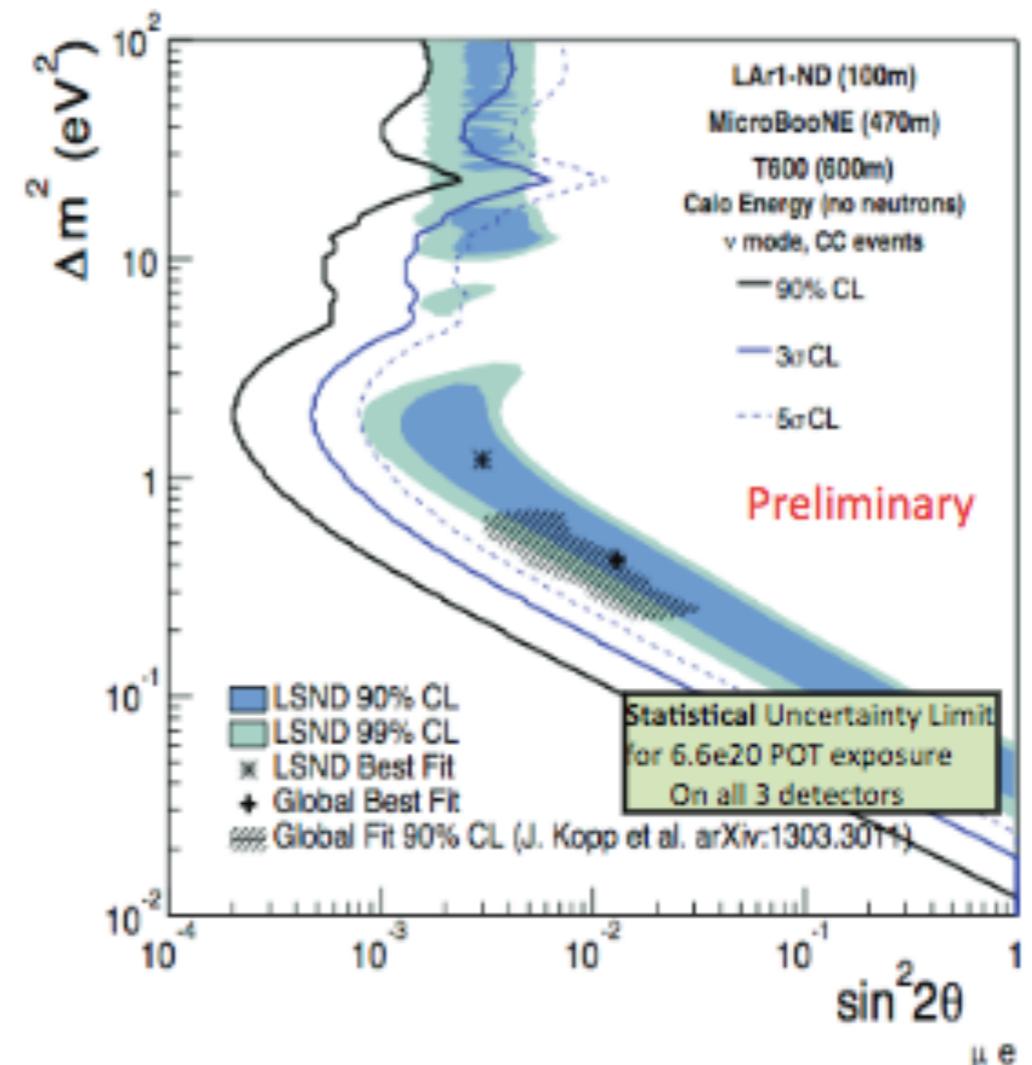
The program consists of three experiments:

MicroBooNE at 470 m

LAr1-ND at 110 m

ICARUS at 600 m

- 1) Precise measurements of fluxes
- 2) Determine the nature of MiniBooNE excess
- 3) Observe  $(\text{anti-})\nu_\mu \rightarrow (\text{anti-})\nu_e$



L. Camilleri AIP Conference Proceedings 1680, 020004 (2015)

# Future Sterile neutrino searches: Accelerators

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Pion Decay-in-flight experiment: Fermilab SBL

Muon Decay-in-flight experiment: NuSTORM

Pion Muon and Kaon Decay-at-rest experiment: OscSNS, JPARK MLF

Isotope Decay-at-rest experiment: ISODAR

J. Spitz AIP Conference Proceedings 1666, 180004 (2015)

# Future Sterile neutrino searches: Reactors

To investigate the Reactor Antineutrino anomaly

Experiment	$P_{th}$ (MW)	$M_{target}$ (tons)	L (m)	Depth (m.w.e)
Nucifer (France)	70	0.8	7	13
Poseidon (Russia)	100	3	5-8	15
Stereo (France)	57	1.75	8.8-12	18
Neutrino4 (Russia)	100	1.5	6-11	10
Hanaro (Korea)	30-2800	1	6	few
DANSS (Russia)	3000	0.9	9.7-12.2	50
Prospect (USA)	85	1& 10	7-18	few
Solid (UK)	45-80	2.9	6-8	10

D. Lhuillier AIP Conference Proceedings 1666, 180003 (2015)

# A short summary...

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There are several inconclusive hints which point towards the existence of a fourth neutrino.

A simple 3+1 model seems unlikely especially in the wake of contradictory evidences. 3+1 may just be a marginal description.

Recent measurements by MINOS, Daya Bay and IceCube tightly constrain the MiniBooNE-LSND allowed regions.

A host of SBL neutrino experiments to follow to conclusively prove or disprove the four-neutrino hypothesis.

A major goal of the present and future long-baseline neutrino oscillation experiments is to establish that leptons violate CP, or else to place a stringent upper limit on any such violation.

The studies related to these experiments have been done assuming the standard three-neutrino-only paradigm.

Several short-baseline anomalies hint at the possible existence of short-wavelength oscillations driven by one or more  $O(1 \text{ eV}^2)$  mass-squared splittings.

These oscillations are significant when  $L/E \sim 1 \text{ km/GeV}$  but they are also present at the far detector where  $L/E \sim 500 \text{ km/GeV}$ .

At  $L/E \sim 500 \text{ km/GeV}$ , the rapid oscillations driven by  $O(1 \text{ eV}^2)$  neutrinos get averaged to a  $L/E$ -independent value due to the finite energy resolution of any realistic detector.

# Sterile neutrinos at LBL

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However, these oscillations can have a major impact on the probability amplitudes over and above that of the standard oscillations.

We restrict ourselves to the scenario where there is only one additional mass eigenstate (3+1).

For 3+N scenarios where  $N > 1$ , the consequences on measurements made at the far-detector site can be expected to be manifold.

We perform some calculations relevant to the CP searches in the 3+1 scenario as manifested in the proposed **Deep Underground Neutrino Experiment** (DUNE).

See [arXiv:1303.3011](https://arxiv.org/abs/1303.3011), Kopp et. al. for a global fit of data for 3+N.

See [arXiv:1605.03829](https://arxiv.org/abs/1605.03829), Hannestad et. al. for a compatibility study with Cosmology.

# The 3+1 model

We consider a  $O(1 \text{ eV}^2)$  mass sterile neutrino, heavier than the other 3 mass eigenstates  $\Rightarrow \Delta m^2_{41} = +1 \text{ eV}^2$ .  $\Delta m^2_{31}$  can be + or -

The oscillations are now characterised by 6 mixing angles, 3 CP-violating phases and 3 mass-squared differences.

$$U^{3+1}_{\text{PMNS}} = O(\Theta_{34}, \delta_{34}) O(\Theta_{24}, \delta_{24}) O(\Theta_{14}) O(\Theta_{23}) O(\Theta_{13}, \delta_{13}) O(\Theta_{12})$$

$\sin^2 \Delta_{4i}$  averages to 0.5

$\sin 2\Delta_{4i}$  averages to 0

$$P_{\mu e}^{3+1} = 4|U_{\mu 4} U_{e 4}|^2 \times 0.5 - 4\text{Re}(U_{\mu 1} U_{e 1}^* U_{\mu 2}^* U_{e 2}) \sin^2 \Delta_{21} + 2\text{Im}(U_{\mu 1} U_{e 1}^* U_{\mu 2}^* U_{e 2}) \sin 2\Delta_{21} - 4\text{Re}(U_{\mu 1} U_{e 1}^* U_{\mu 3}^* U_{e 3}) \sin^2 \Delta_{31} + 2\text{Im}(U_{\mu 1} U_{e 1}^* U_{\mu 3}^* U_{e 3}) \sin 2\Delta_{31} - 4\text{Re}(U_{\mu 2} U_{e 2}^* U_{\mu 3}^* U_{e 3}) \sin^2 \Delta_{32} + 2\text{Im}(U_{\mu 2} U_{e 2}^* U_{\mu 3}^* U_{e 3}) \sin 2\Delta_{32}$$

# Why are the 3+1 effects large?

$$\begin{aligned}
 P_{\mu e}^{3+1} &= \frac{1}{2} \sin^2 2\theta_{\mu e}^{4\nu} \\
 &+ \frac{(a^2 \sin^2 2\theta_{\mu e}^{3\nu} - \frac{1}{4} \sin^2 2\theta_{13} \sin^2 2\theta_{\mu e}^{4\nu}) [\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32}]}{4} \\
 &+ \cos(\delta_{13}) b a^2 \sin 2\theta_{\mu e}^{3\nu} [\cos 2\theta_{12} \sin^2 \Delta_{21} + \sin^2 \Delta_{31} - \sin^2 \Delta_{32}] \\
 &+ \cos(\delta_{24}) b a \sin 2\theta_{\mu e}^{4\nu} [\cos 2\theta_{12} \cos^2 \theta_{13} \sin^2 \Delta_{21} - \sin^2 \theta_{13} (\sin^2 \Delta_{31} - \sin^2 \Delta_{32})] \\
 &+ \cos(\delta_{13} + \delta_{24}) a \sin 2\theta_{\mu e}^{3\nu} \sin 2\theta_{\mu e}^{4\nu} \left[ -\frac{1}{2} \sin^2 2\theta_{12} \cos^2 \theta_{13} \sin^2 \Delta_{21} \right. \\
 &\left. + \cos 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32}) \right] \\
 &- \frac{1}{2} \sin(\delta_{13}) b a^2 \sin 2\theta_{\mu e}^{3\nu} [\sin 2\Delta_{21} - \sin 2\Delta_{31} + \sin 2\Delta_{32}] \\
 &+ \frac{1}{2} \sin(\delta_{24}) b a \sin 2\theta_{\mu e}^{4\nu} [\cos^2 \theta_{13} \sin 2\Delta_{21} + \sin^2 \theta_{13} (\sin 2\Delta_{31} - \sin 2\Delta_{32})] \\
 &+ \frac{1}{2} \sin(\delta_{13} + \delta_{24}) a \sin 2\theta_{\mu e}^{3\nu} \sin 2\theta_{\mu e}^{4\nu} [\cos^2 \theta_{12} \sin 2\Delta_{31} + \sin^2 \theta_{12} \sin 2\Delta_{32}] \\
 &+ (b^2 a^2 - \frac{1}{4} a^2 \sin^2 2\theta_{12} \sin^2 2\theta_{\mu e}^{3\nu} - \frac{1}{4} \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 2\theta_{\mu e}^{4\nu}) \sin^2 \Delta_{21}
 \end{aligned}$$

$$\begin{aligned}
 \text{where } \sin 2\theta_{\mu e}^{3\nu} &= \sin 2\theta_{13} \sin \theta_{23}, & b &= \cos \theta_{13} \cos \theta_{23} \sin 2\theta_{12}, \\
 \sin 2\theta_{\mu e}^{4\nu} &= \sin 2\theta_{14} \sin \theta_{24} & \text{and } a &= \cos \theta_{14} \cos \theta_{24}
 \end{aligned}$$

# Appearance probability in 3+1 in vacuum

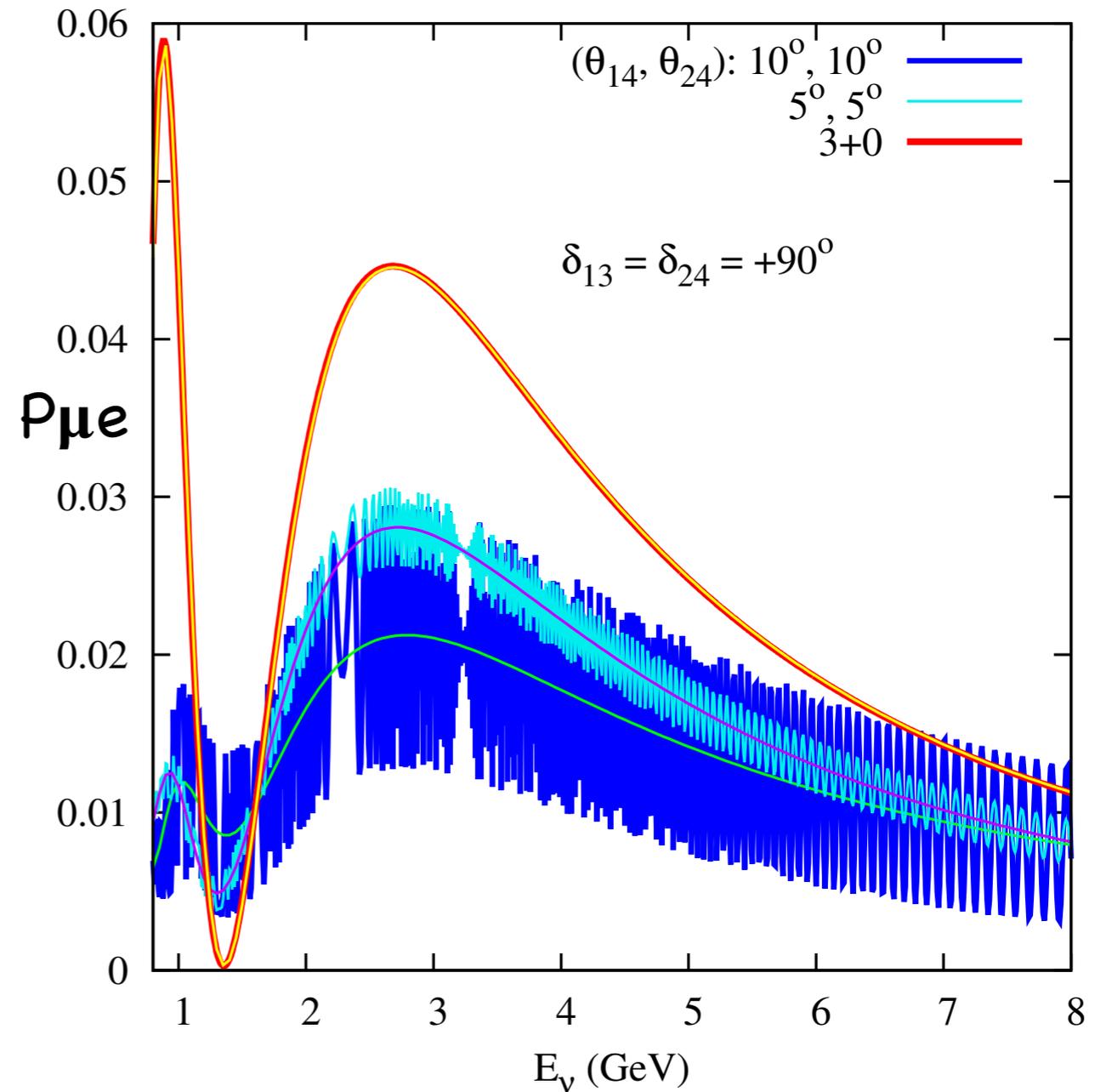
Comparison of analytical expression with GLoBES =>

In the limit that  $\Theta_{i4} = 0$ , the 3+0 probabilities are reproduced.

When 3+1 effects are switched on, the probabilities match quite well.

The rapid oscillations due to  $\Delta m^2_{4i}$  for a 1 eV<sup>2</sup> sterile neutrino will not be visible in the DUNE far detector.

DUNE, L = 1300 km, vacuum



$$\Theta_{12} = 33.48^\circ, \Theta_{13} = 8.5^\circ, \Theta_{23} = 45^\circ$$

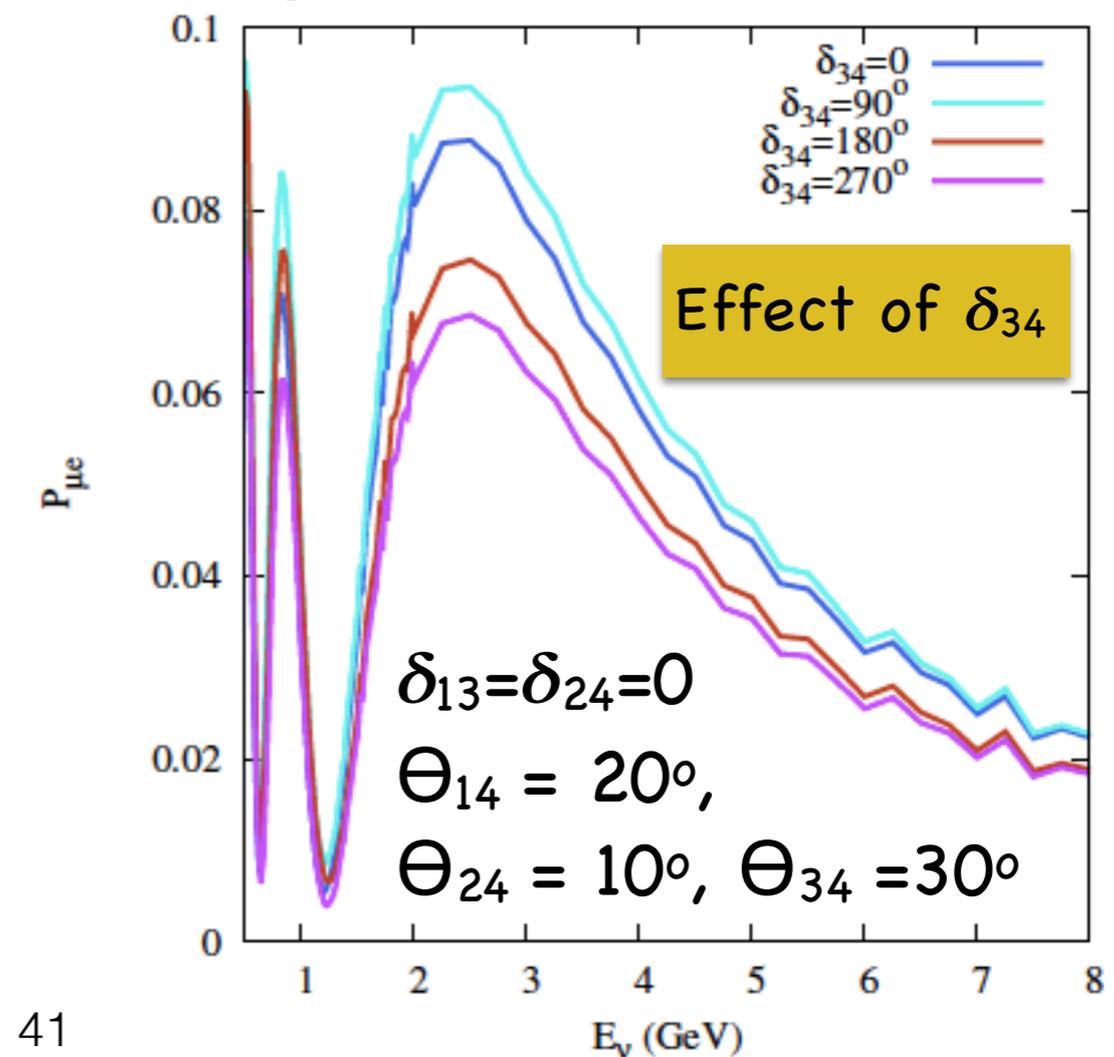
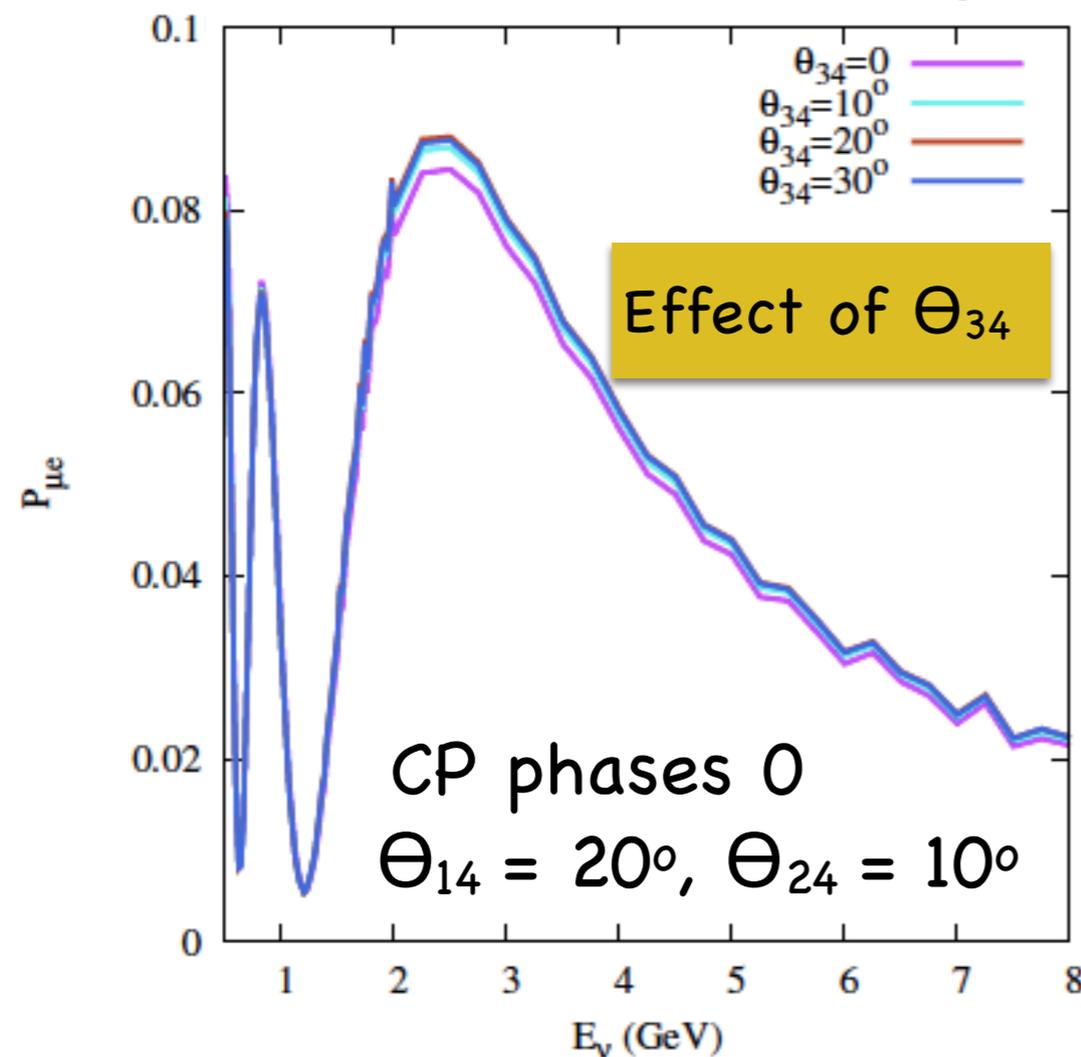
$$\Delta m^2_{31} = +2.4e-3 \text{ eV}^2, \Delta m^2_{21} = 7.5e-5 \text{ eV}^2$$

# Appearance probability in 3+1 in matter

$\Theta_{34}$  and  $\delta_{34}$  which were irrelevant for 3+1 electron appearance in vacuum, play significant roles in the presence of matter.

In producing these plots, we have averaged over the  $\Delta m^2_{4i}$  induced oscillations.

DUNE, L = 1300 km, matter

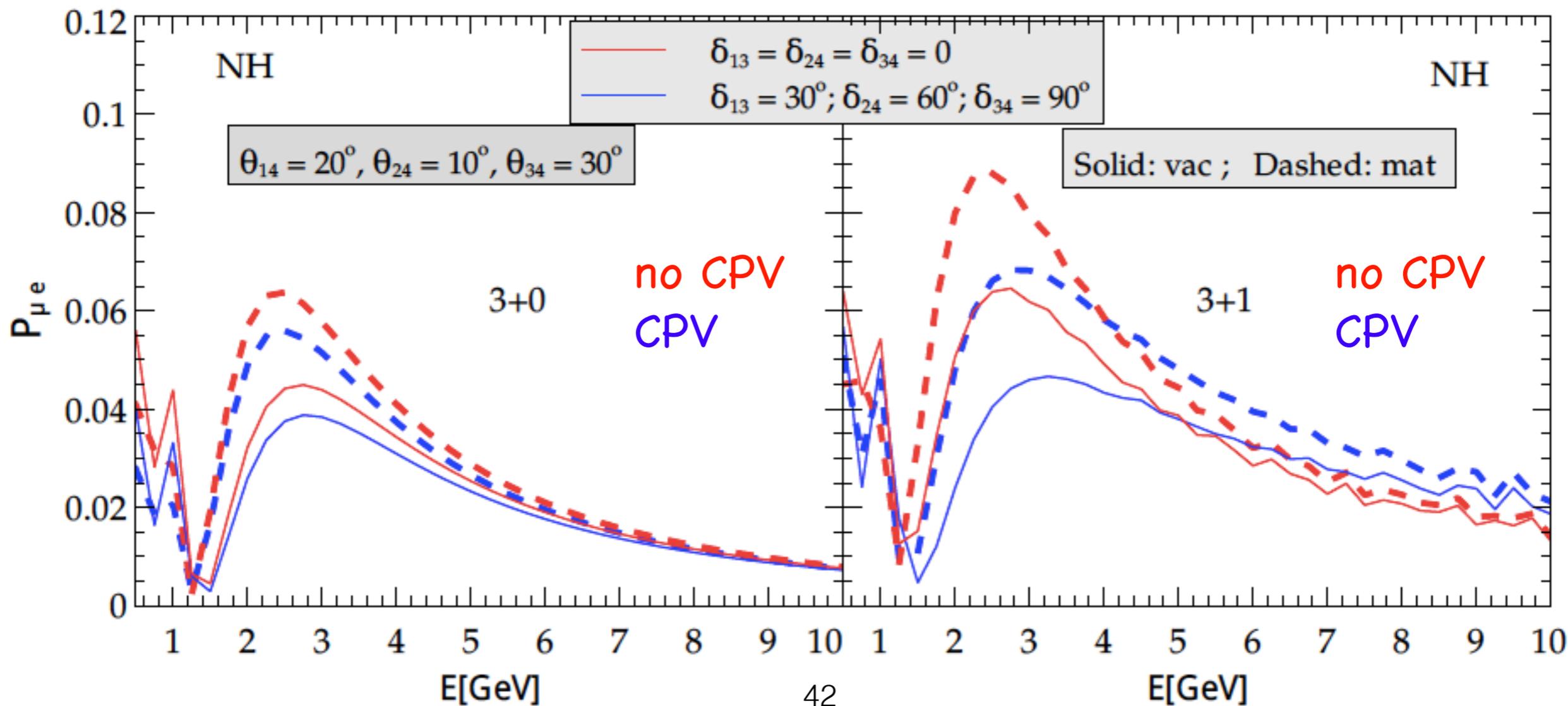


# Appearance probability in 3+1 in matter

**Left vs. Right** - Even at far detector, sterile neutrinos have large effects.

**Red vs. Blue** - Phases play an important role, more so in 3+1.

**Solid vs. Dashed** - Matter effects are important, more in 3+1.



# Constraints on the active-sterile mixings

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Constraints derived are calculated in the region of  $\Delta m^2_{41}$  of 1 eV<sup>2</sup> .

Consistent parameterisation.

We assume the lower limits on the active-sterile mixings to be 0.

$\nu_e$  and anti- $\nu_e$  disappearance searches probe  $|U_{e4}| = \sin\Theta_{14}$  .

$\nu_\mu$ , anti- $\nu_\mu$  and NC disappearance searches probe  $|U_{\mu 4}| = \cos\Theta_{14}\sin\Theta_{24}$  and  $|U_{\tau 4}| = \cos\Theta_{14}\cos\Theta_{24}\sin\Theta_{34}$ .

Daya Bay:  $\Theta_{14} \in [0, 13^\circ]$  95% C.L. PRL 113, 141802 (2014), 1407.7259.

IceCube:  $\Theta_{24} \in [0, 7^\circ]$  99% C.L. PRL 117, 071801 (2016)

MINOS(+):  $\Theta_{34} \in [0, 26^\circ]$  90% C.L. PRL 107, 011802 (2011), 1104.3922.

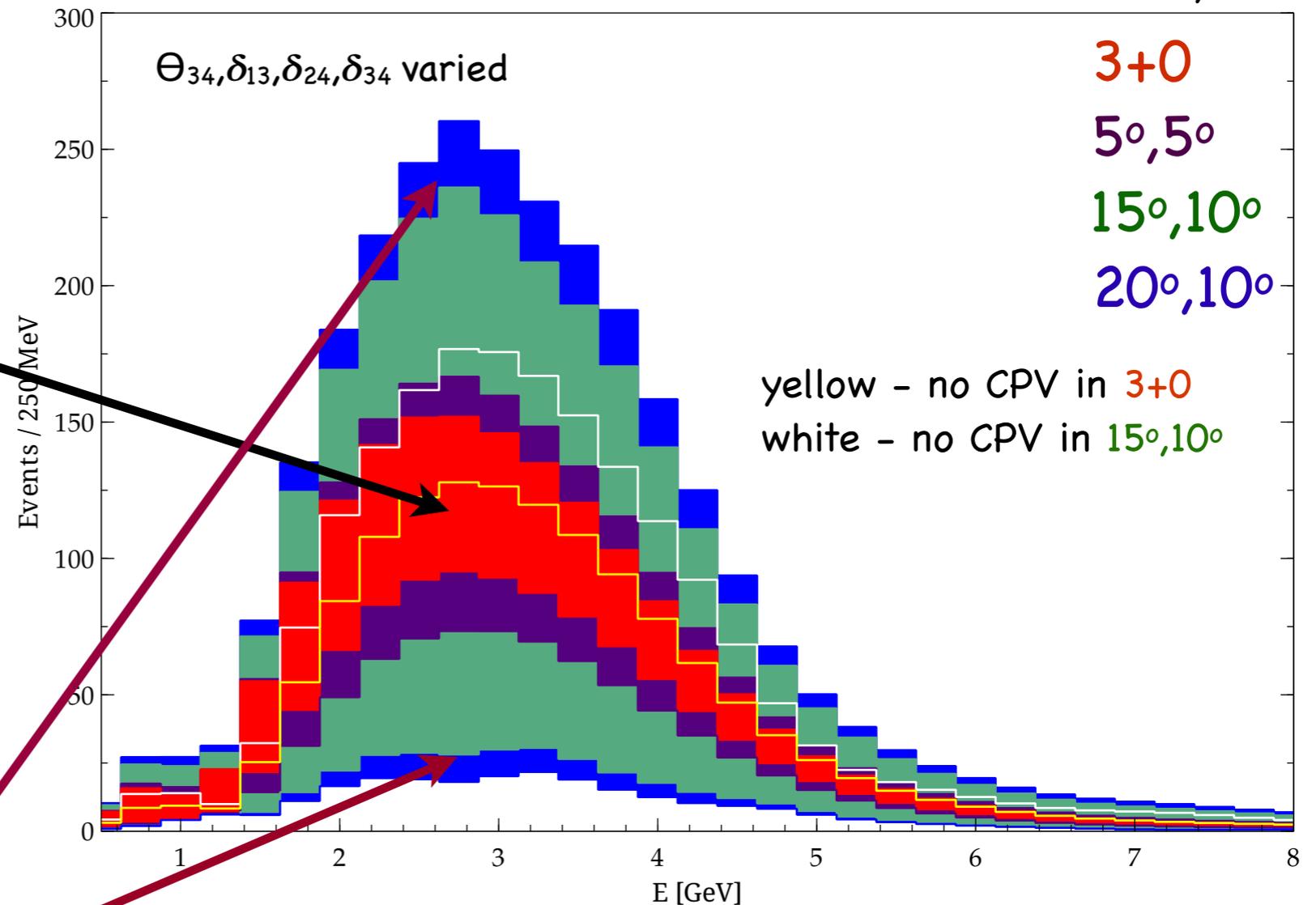
The CP phases remain unconstrained.

LSND:  $\sin^2 2\Theta_{\mu e} < 0.008$  for  $\Delta m^2_{41}$  of around 1 eV<sup>2</sup>

# Events rates plots for DUNE

We assume the standard DUNE setup ([arXiv:1311.0212](https://arxiv.org/abs/1311.0212), Bass et. al.) and use GLOBES for carrying out simulations. 1.2 MW - 120 GeV beam.  $10^{21}$  POT/yr

DUNE, 1300 km, 35 kt, 5 yrs  $\nu$



The 3+1 band can potentially encompass the 3+0 band, leading to substantial degeneracy.

For large active-sterile mixings, an excess or shortage of events, esp. at osc. max. will be pointers to the existence of new physics.

$$\Theta_{12} = 33.48^\circ, \Theta_{13} = 8.5^\circ, \Theta_{23} = 45^\circ$$

$$\Delta m_{31}^2 = +2.457e-3 \text{ eV}^2, \Delta m_{21}^2 = 7.5e-5 \text{ eV}^2$$

# Robustness of 3+0 parameters

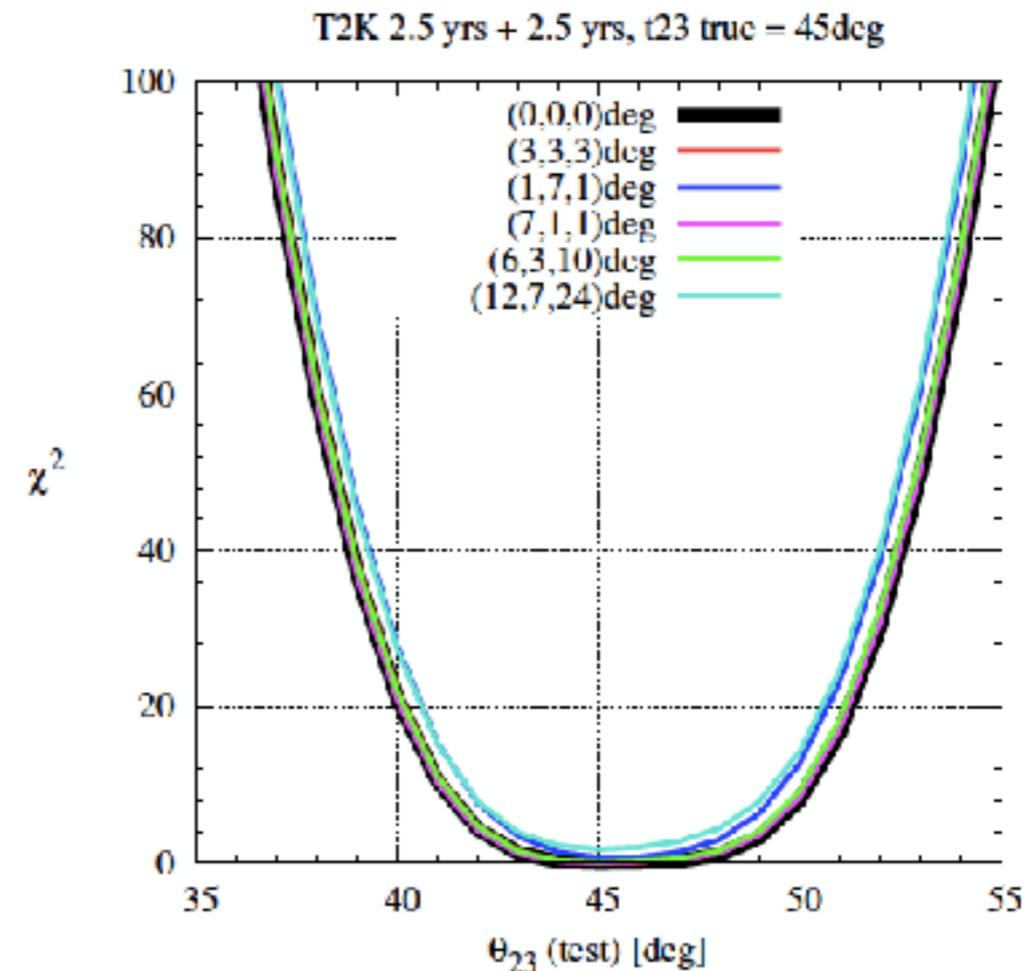
Some of our early calculations showed that the disappearance data at the far detector are less affected by the active-sterile mixing angles compared to the appearance data.

See [arXiv:1308.6218](https://arxiv.org/abs/1308.6218), Esmaili et. al. for robustness of  $\Theta_{13}$  in 3+1.

Berryman et. al. [arXiv:1507.03986](https://arxiv.org/abs/1507.03986)

3-nu-fit to 4-nu-data:

- 1) similar best-fits and precisions
- 2) bad goodness-of-fit



For the first time, this new result on  $|U_{\tau 4}|$  allows us to have a complete picture of the extended lepton mixing matrix:

$|U| =$  [Collin et. al. \(arXiv:1607.00011\)](https://arxiv.org/abs/1607.00011)

$$\begin{bmatrix} 0.79 \rightarrow 0.83 & 0.53 \rightarrow 0.57 & 0.14 \rightarrow 0.15 & 0.13 & (0.17) \rightarrow 0.20 & (0.21) \\ 0.25 \rightarrow 0.50 & 0.46 \rightarrow 0.66 & 0.64 \rightarrow 0.77 & 0.09 & (0.10) \rightarrow 0.15 & (0.13) \\ 0.26 \rightarrow 0.54 & 0.48 \rightarrow 0.69 & 0.56 \rightarrow 0.75 & 0.0 & (0.0) \rightarrow 0.7 & (0.05) \\ \dots & \dots & \dots & \dots & \dots & \dots \end{bmatrix} \quad (6)$$

Above, "... " represents parameters constrained by the overall unitarity of the  $4 \times 4$  matrix. The ranges in the matrix correspond to 90% confidence intervals. The entries in the last column correspond to this work and are given for  $\Delta m^2 \sim 2 \text{ eV}^2$  ( $\Delta m^2 \sim 6 \text{ eV}^2$ ). The intervals

# CP violation

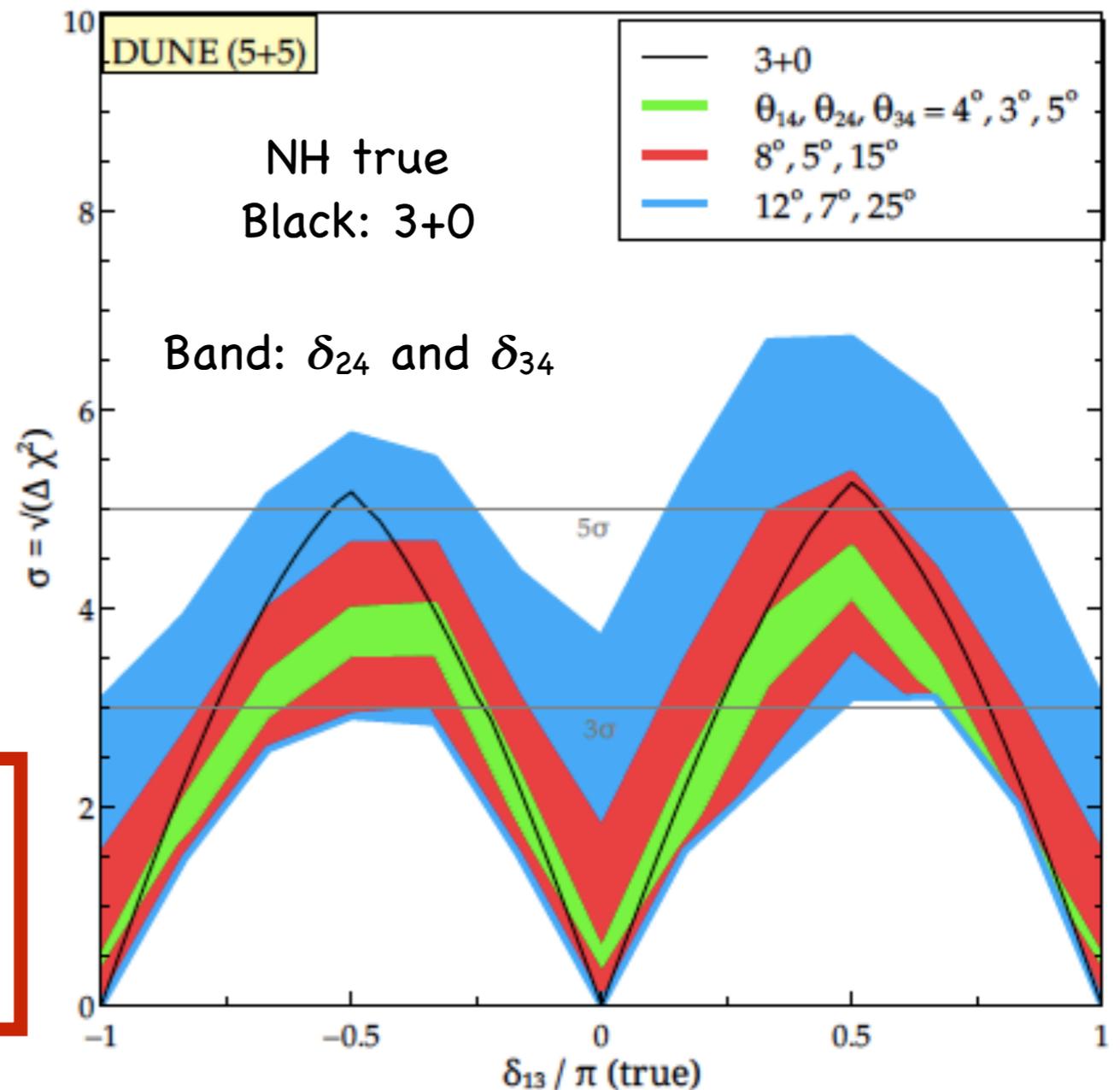
Excluding CP conserving values as a function of true 3+1 oscillation parameters

Fit: CP conserving  
 $\delta_{13}$ ,  $\delta_{24}$  and  $\delta_{34}$

No marginalisation  
over 3+0 osc. params

Marginalisation over CP  
conserving phases and  
active-sterile mix. angles

Small mixings: Sensitivity decreases  
Large mixings: Sensitivity spans  
on both sides of the 3+0 sensitivity



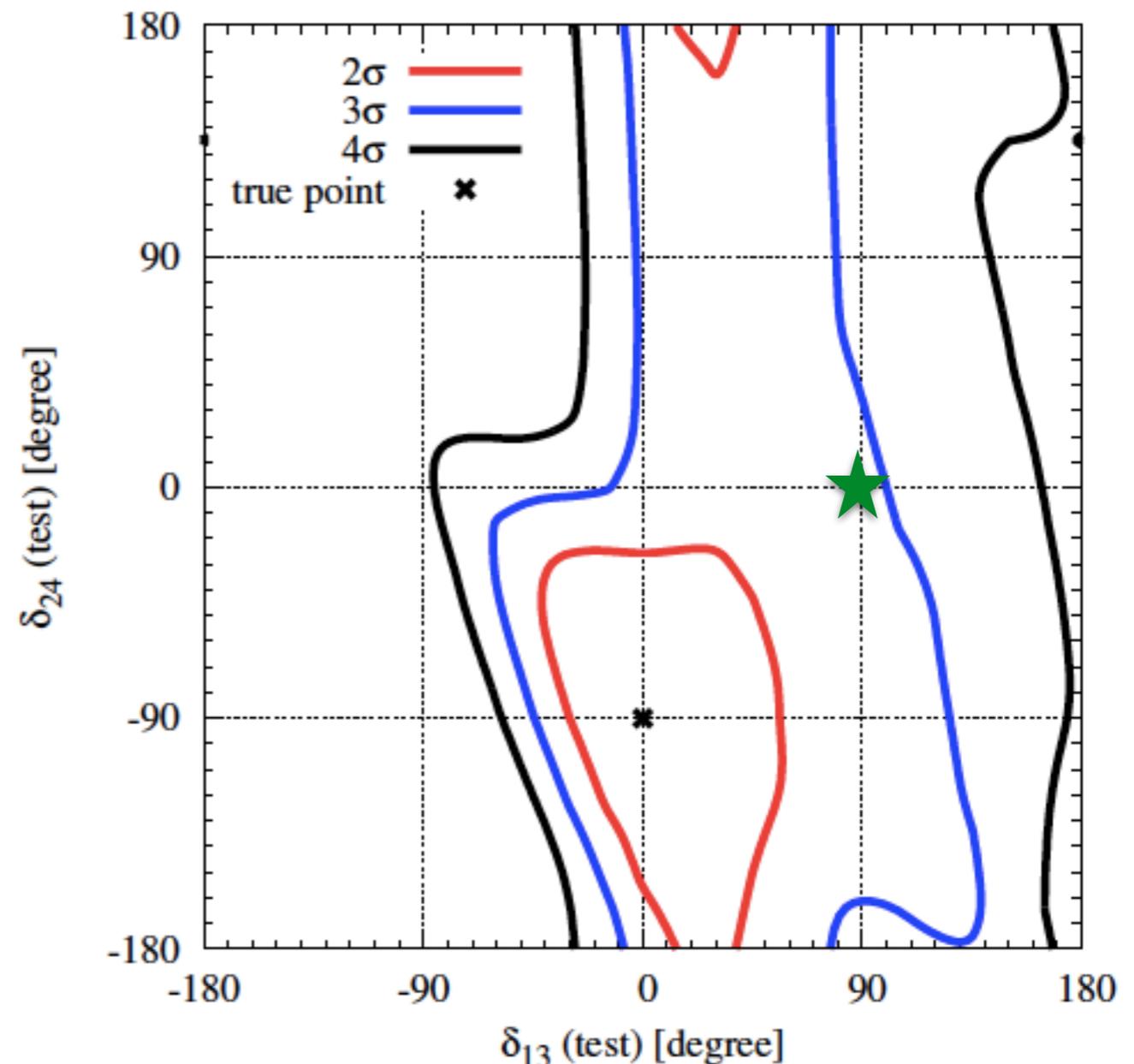
# Determining the phase responsible for CPV

Suppose that the results of short-baseline experiments indicate the presence of a  $1 \text{ eV}^2$  neutrino, and, in addition, DUNE finds evidence of CP violation. Can then DUNE identify the source of this violation?

Test values of  $(\delta_{13}, \delta_{24})$  close to  $(90^\circ, 0)$  and  $(90^\circ, 180^\circ)$  are allowed within  $3\sigma$

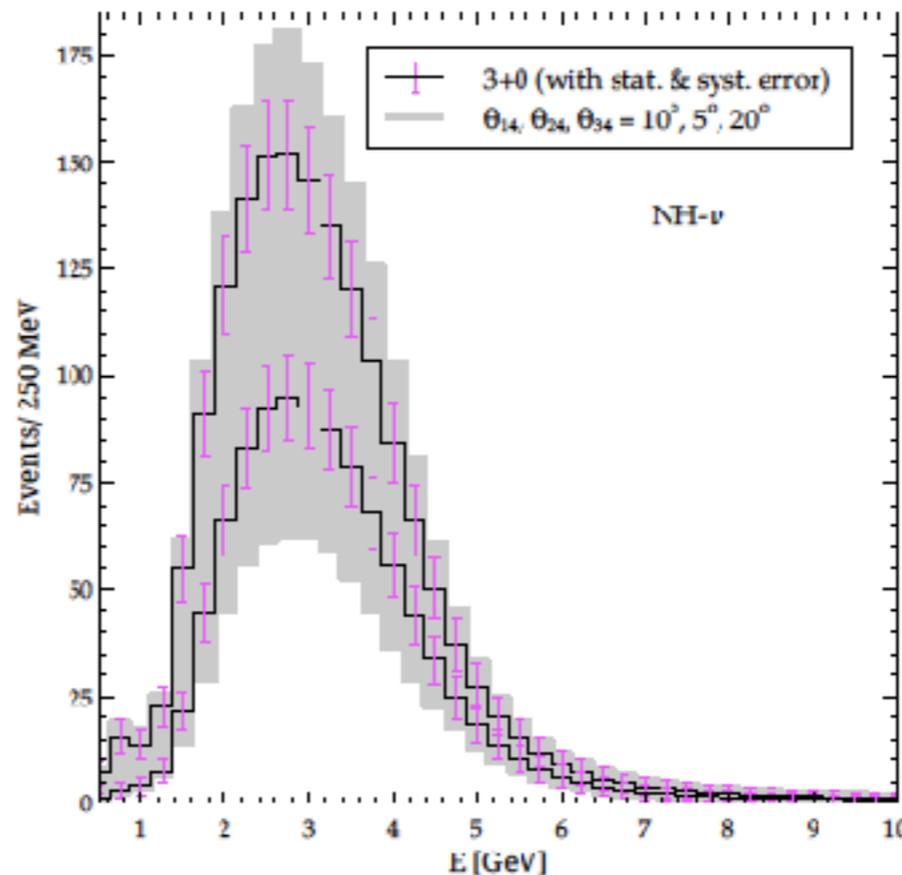
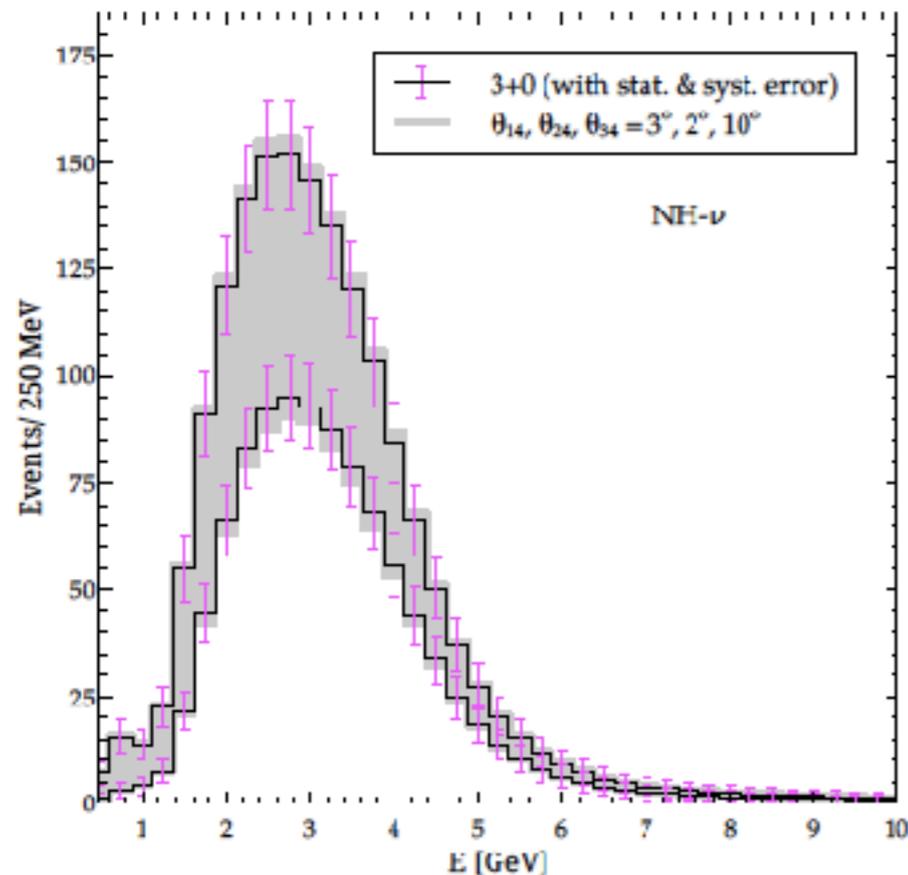
Attributing CP violation unambiguously to any one phase may not be possible at  $3\sigma$

True:  $\Theta_{14} = 12^\circ, \Theta_{24} = 7^\circ, \Theta_{34} = 25^\circ, \delta_{34} = 0$



# Far-detector's sensitivity to 3+1

How large do active-sterile mixings need to be before DUNE becomes sensitive to their presence?



Bands: CP variation

**Left:** the 3+1 band is degenerate with the 3+0, incl. errors

**Right:** grey band now extends significantly beyond the expected event rates for 3+0, even after accounting for errors.

# Mass hierarchy

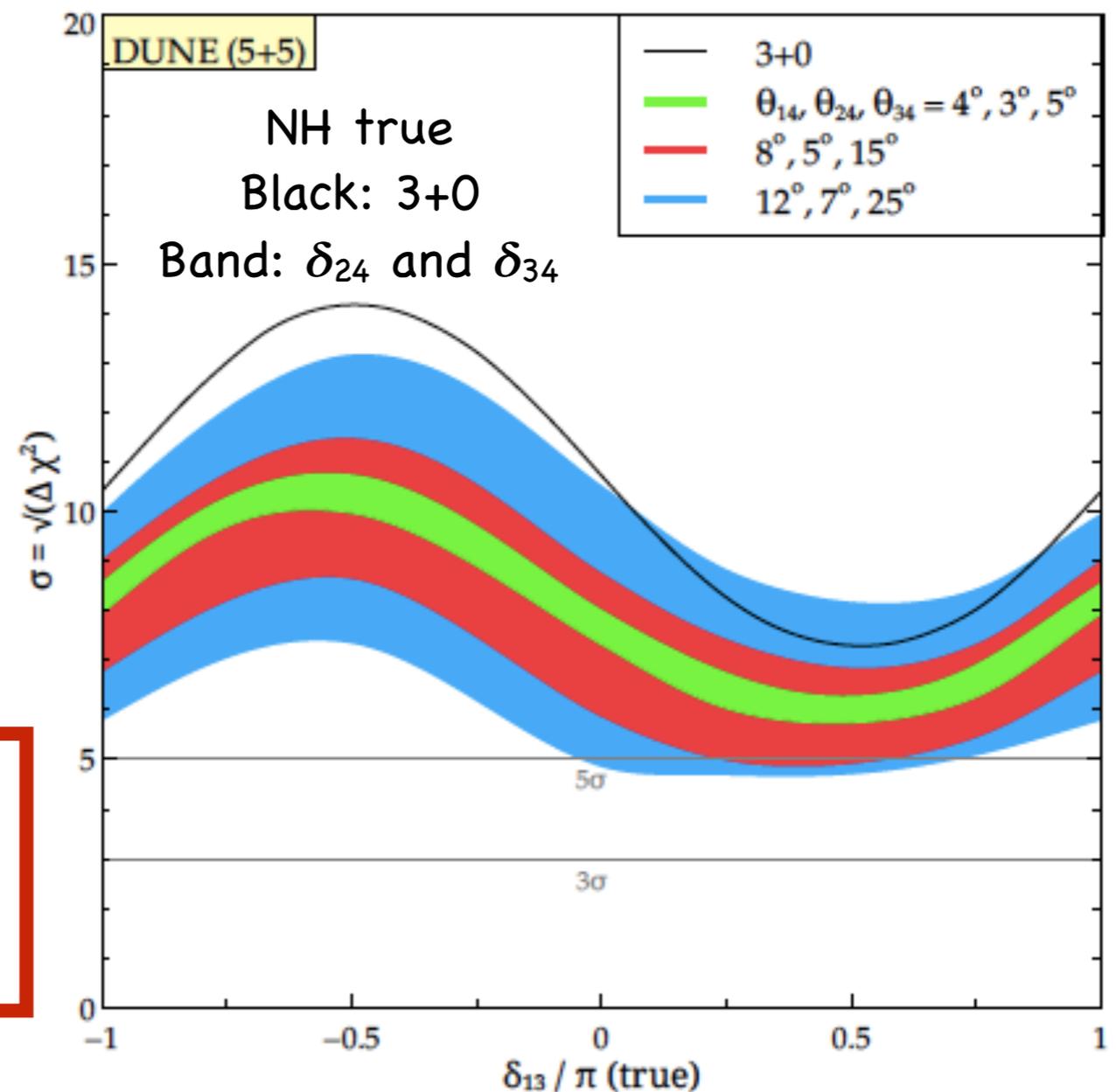
Establishing MH as a function of true  
3+1 oscillation parameters

Fit: IH

No marginalisation  
over 3+0 osc. params

Marginalisation over all  
CP values and  
active-sterile mix. angles

Sensitivity usually below 3+0  
but  $5\sigma$  discovery with DUNE

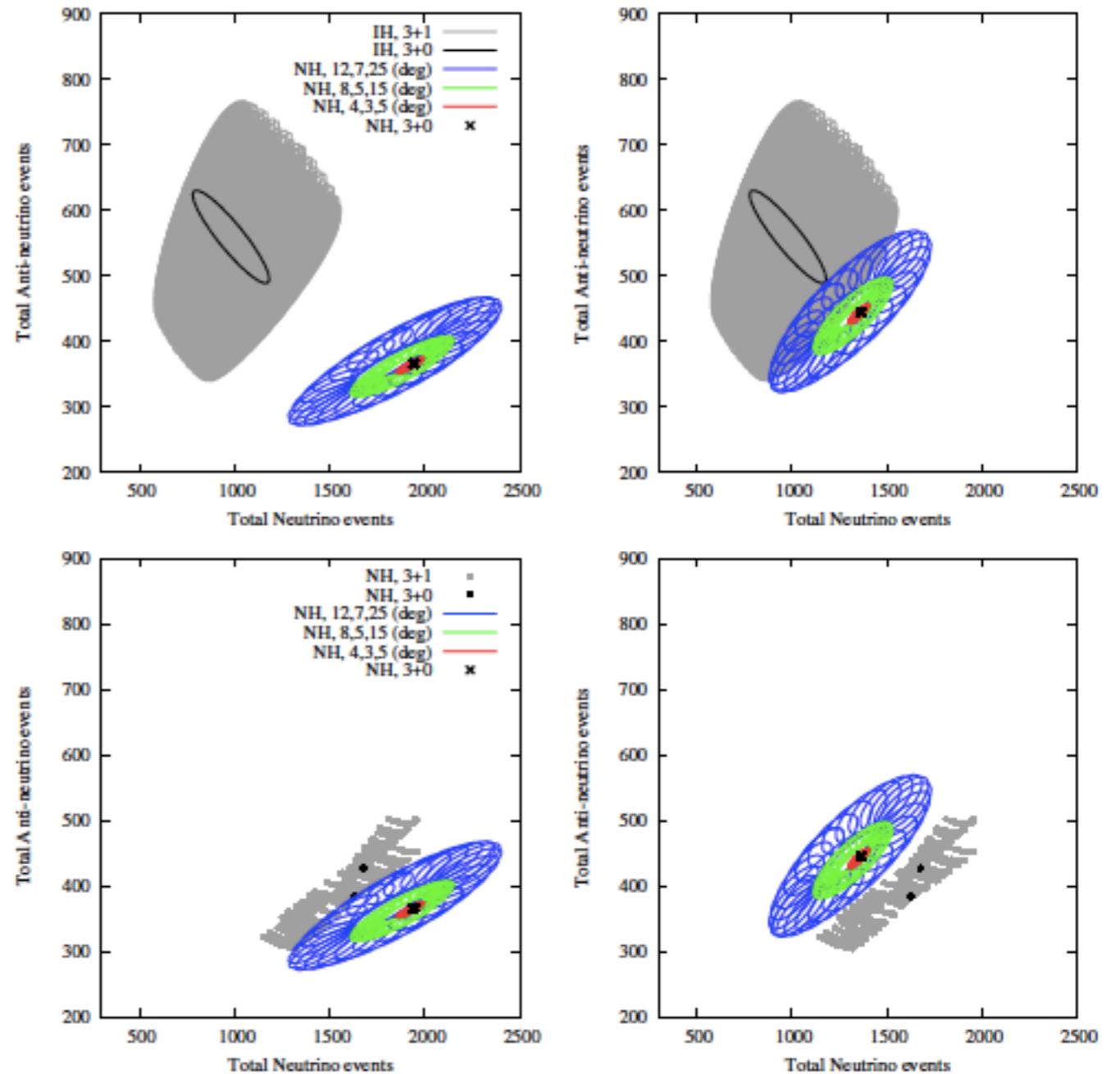


# MH and CPV behaviour in 3+1

DUNE, 1300 km, 35 kt, 5 yrs  $\nu$  + 5 yrs anti- $\nu$

The fit event rates region increases drastically as we go from 3+0 to 3+1 (black ellipses and dots compared to grey regions).

For small mixing angles the event rate regions are small compared to their size for large mixing angles (red compared to green and blue).



Left:  $\delta_{13} = -90^\circ$

Right:  $\delta_{13} = 90^\circ$

Top: MH  
Bottom: CPV

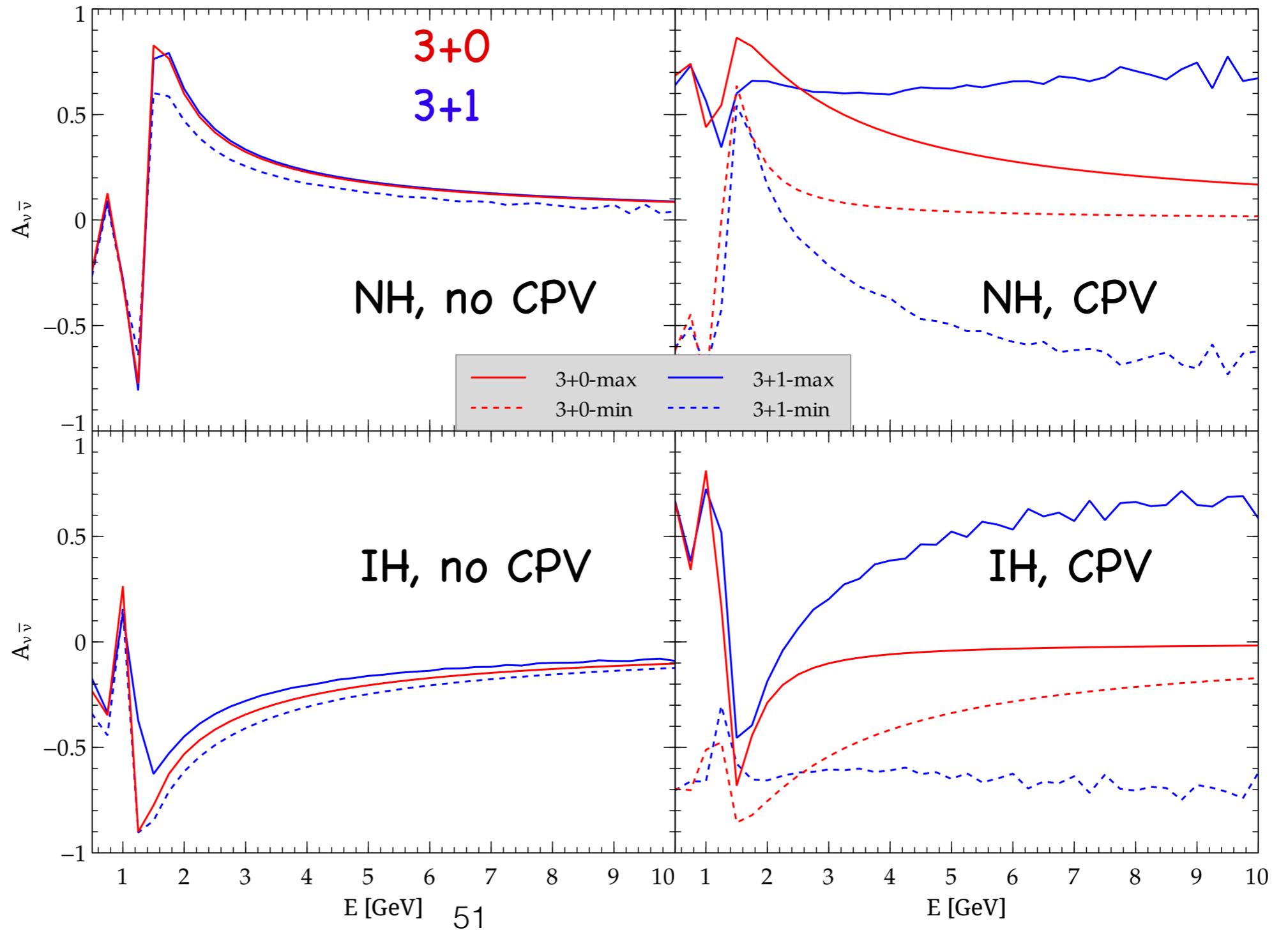
# CP asymmetries in 3+0 and 3+1

If an experiment were to measure asymmetries which consistently lie outside these two bands it would provide evidence of CP violation in either the 3+0 or the 3+1 case.

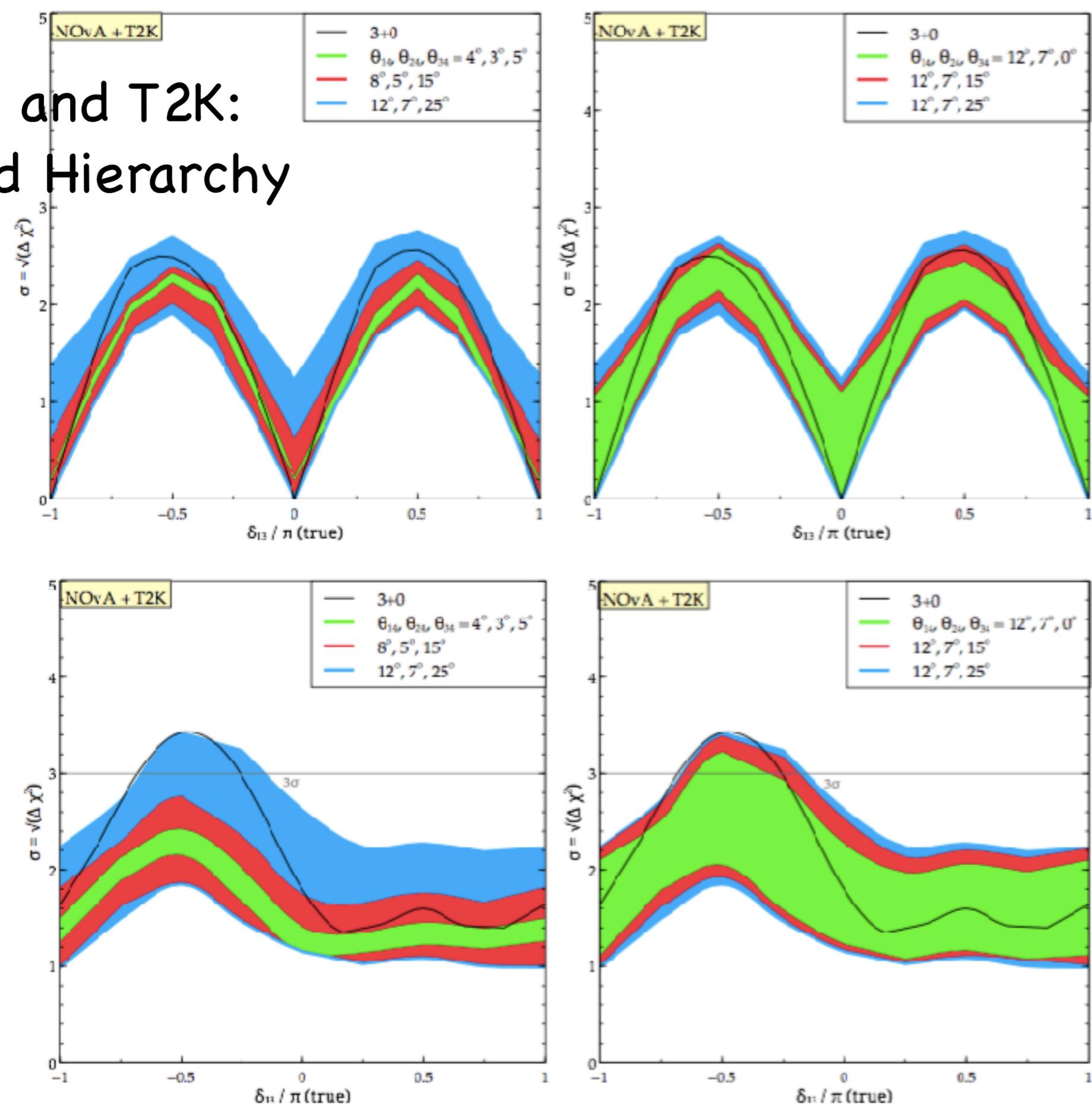
Asymmetry values measured within these two bands in the left panels do not unambiguously signal a CP conserving situation.

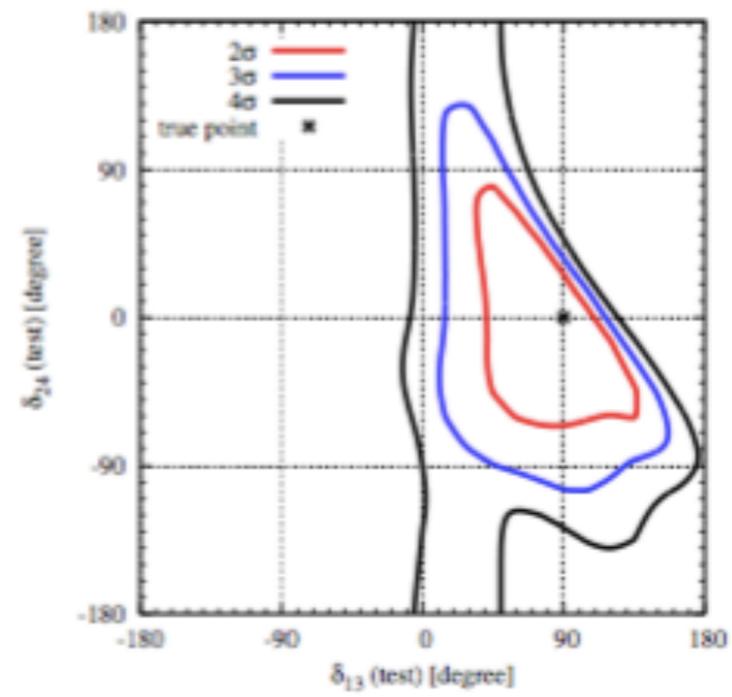
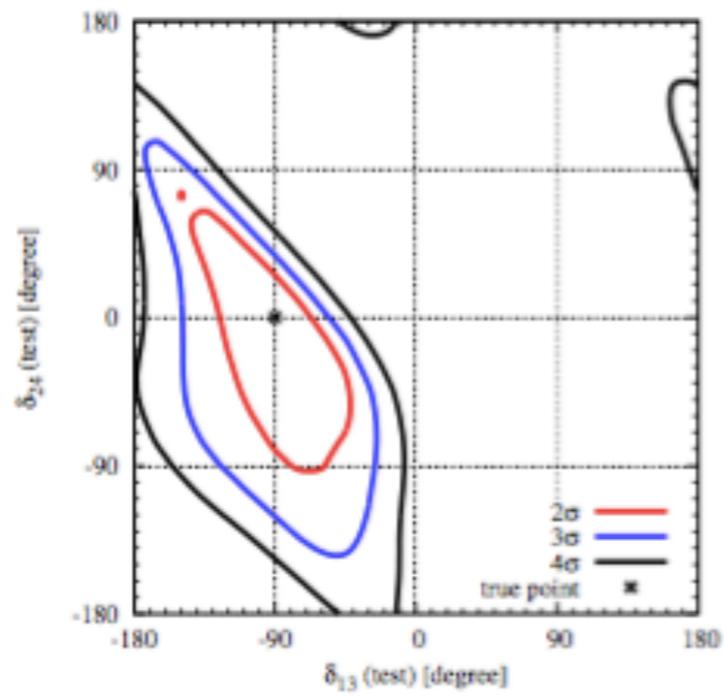
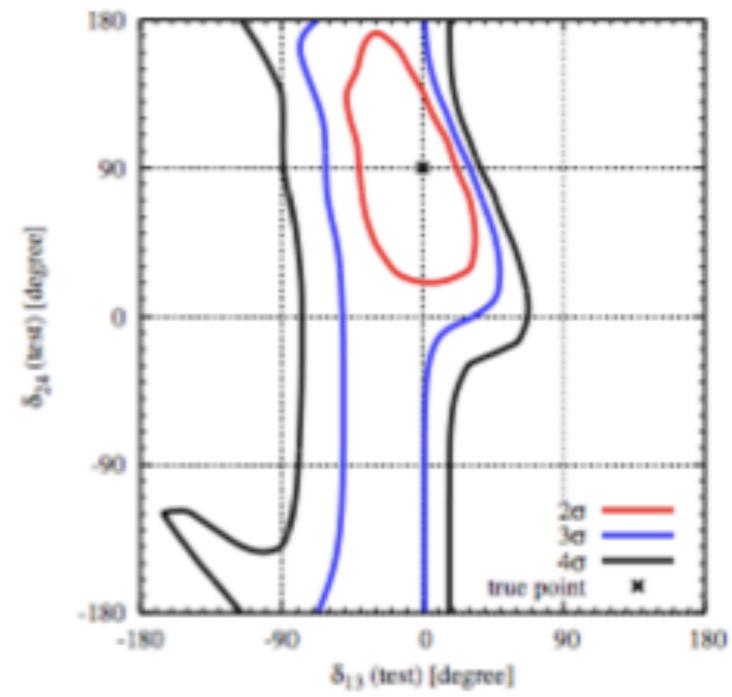
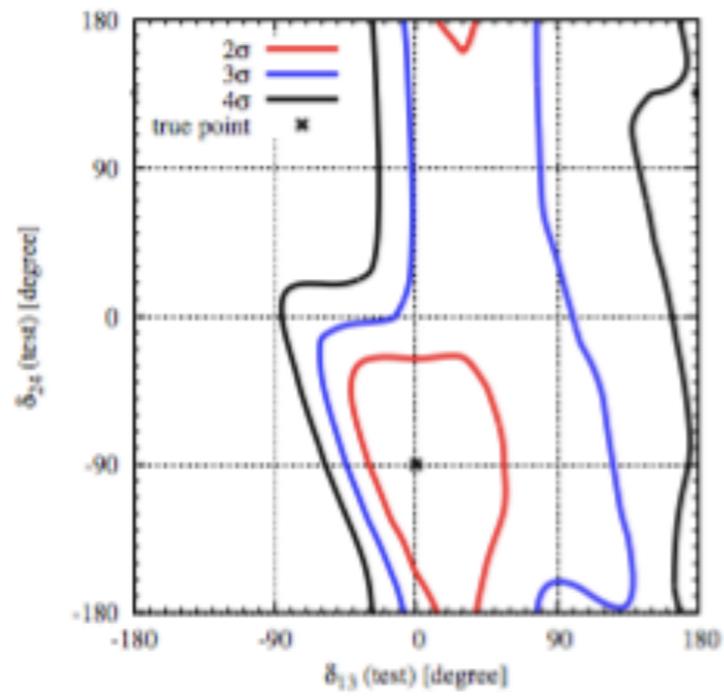
$$A_{\nu\bar{\nu}}^{\alpha\beta} = \frac{P(\alpha \rightarrow \beta) - P(\bar{\alpha} \rightarrow \bar{\beta})}{P(\alpha \rightarrow \beta) + P(\bar{\alpha} \rightarrow \bar{\beta})} = \frac{\Delta P_{\alpha\beta}}{P(\alpha \rightarrow \beta) + P(\bar{\alpha} \rightarrow \bar{\beta})}$$

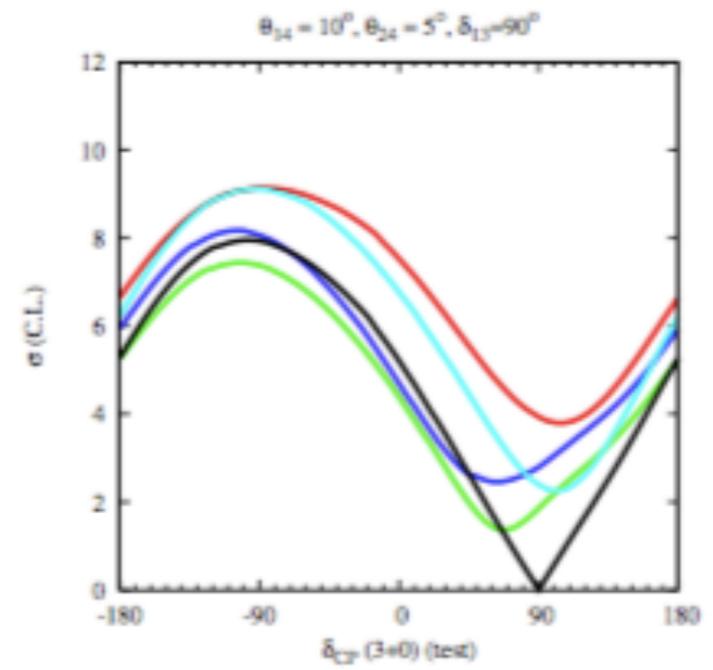
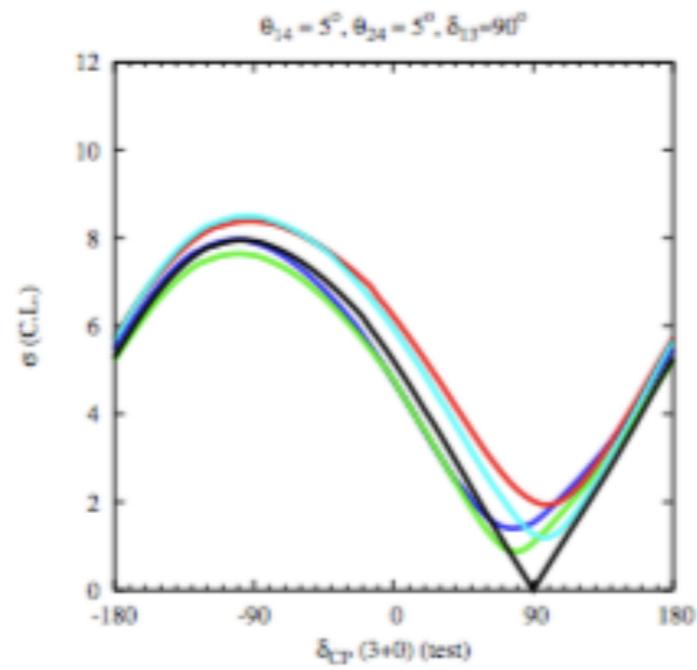
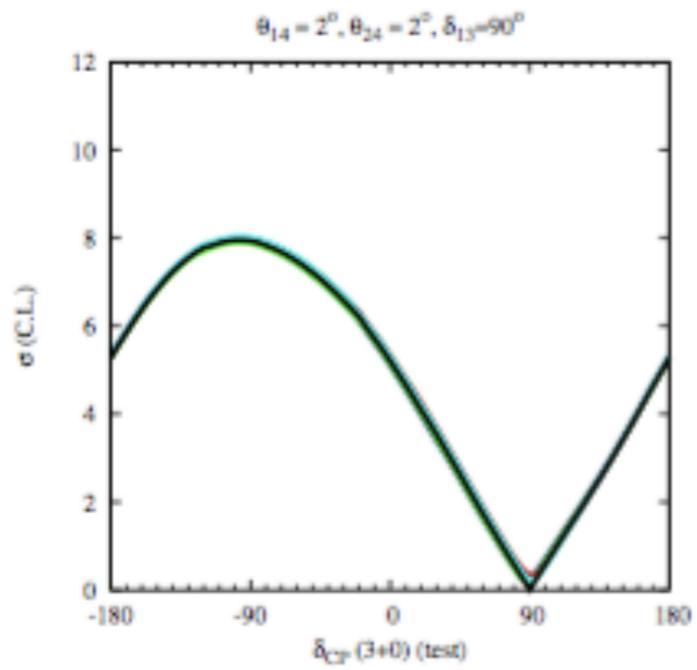
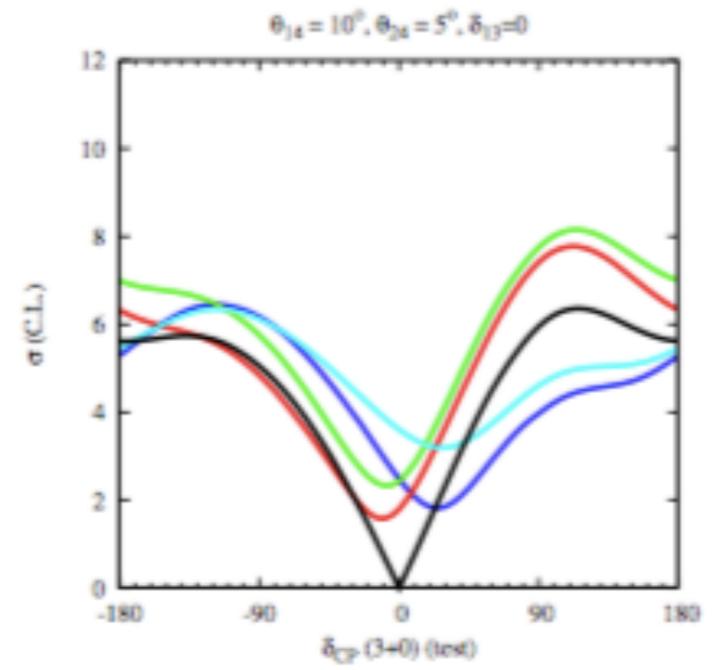
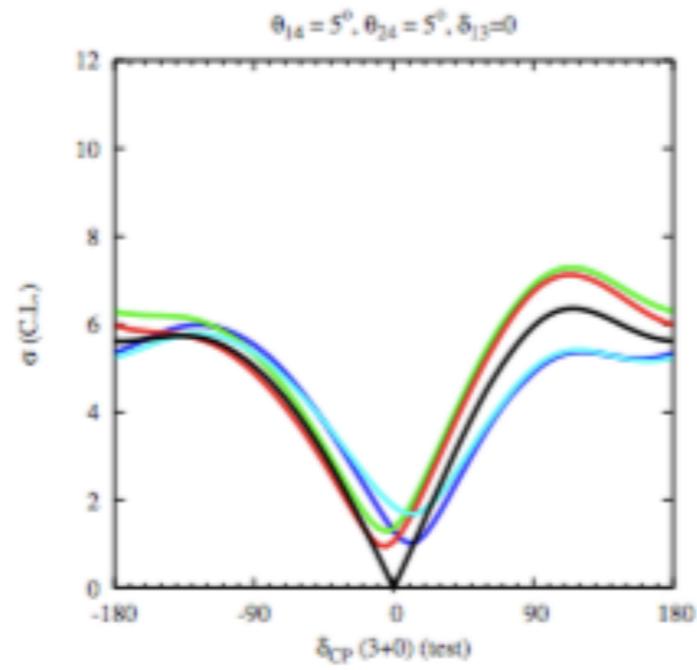
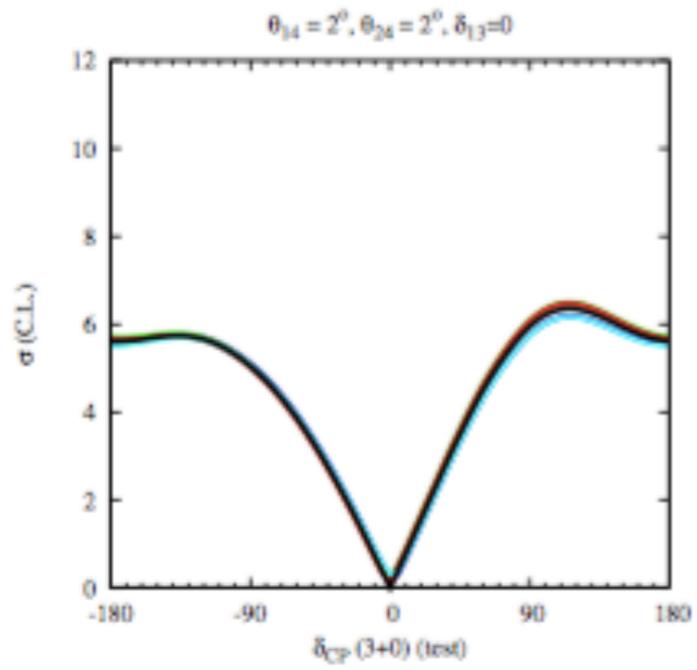
DUNE, L = 1300 km, matter



# NOvA and T2K: CPV and Hierarchy







# Appearance probability in 3+1 in vacuum

$$\begin{aligned}
 P_{\mu e}^{3+1} = & \frac{1}{2} \sin^2 2\theta_{\mu e}^{4\nu} \\
 & + \left( a^2 \sin^2 2\theta_{\mu e}^{3\nu} - \frac{1}{4} \sin^2 2\theta_{13} \sin^2 2\theta_{\mu e}^{4\nu} \right) \left[ \cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32} \right] \\
 & + \cos(\delta_{13}) b a^2 \sin 2\theta_{\mu e}^{3\nu} \left[ \cos 2\theta_{12} \sin^2 \Delta_{21} + \sin^2 \Delta_{31} - \sin^2 \Delta_{32} \right] \\
 & + \cos(\delta_{24}) b a \sin 2\theta_{\mu e}^{4\nu} \left[ \cos 2\theta_{12} \cos^2 \theta_{13} \sin^2 \Delta_{21} + \sin^2 \theta_{12} \cos^2 \theta_{13} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32} \right] \\
 & + \cos(\delta_{13} + \delta_{24}) a \sin 2\theta_{\mu e}^{3\nu} \sin 2\theta_{\mu e}^{4\nu} \left[ \cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32} \right] \\
 & + \cos 2\theta_{13} \left( \cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32} \right) \\
 & - \frac{1}{2} \sin(\delta_{13}) b a^2 \sin 2\theta_{\mu e}^{3\nu} \left[ \sin 2\Delta_{21} - \sin 2\Delta_{31} + \sin 2\Delta_{32} \right] \\
 & + \frac{1}{2} \sin(\delta_{24}) b a \sin 2\theta_{\mu e}^{4\nu} \left[ \cos^2 \theta_{13} \sin 2\Delta_{21} + \sin^2 \theta_{13} \sin 2\Delta_{31} + \sin^2 \theta_{13} \sin 2\Delta_{32} \right] \\
 & + \frac{1}{2} \sin(\delta_{13} + \delta_{24}) a \sin 2\theta_{\mu e}^{3\nu} \sin 2\theta_{\mu e}^{4\nu} \left[ \cos^2 \theta_{12} \sin 2\Delta_{31} + \sin^2 \theta_{12} \sin 2\Delta_{32} \right] \\
 & + \left( b^2 a^2 - \frac{1}{4} a^2 \sin^2 2\theta_{12} \sin^2 2\theta_{\mu e}^{3\nu} - \frac{1}{4} \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 2\theta_{\mu e}^{4\nu} \right) \sin^2 \Delta_{21}
 \end{aligned}$$

$\Theta_{14}$  and  $\Theta_{24}$  come in certain combinations only..

In vacuum, the expression does not depend on  $\Theta_{34}$  and  $\delta_{34}$

$$\begin{aligned}
 \text{where } \sin 2\theta_{\mu e}^{3\nu} &= \sin 2\theta_{13} \sin \theta_{23}, & b &= \cos \theta_{13} \cos \theta_{23} \sin 2\theta_{12}, \\
 \sin 2\theta_{\mu e}^{4\nu} &= \sin 2\theta_{14} \sin \theta_{24} & \text{and } a &= \cos \theta_{14} \cos \theta_{24}
 \end{aligned}$$

# Appearance probability in 3+1 in vacuum

$$\begin{aligned}
 P_{\mu e}^{3+1} &= \frac{1}{2} \sin^2 2\theta_{\mu e}^{4\nu} \\
 &+ \left( a^2 \sin^2 2\theta_{\mu e}^{3\nu} - \frac{1}{4} \sin^2 2\theta_{13} \sin^2 2\theta_{\mu e}^{4\nu} \right) \left[ \cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32} \right] \\
 &+ \cos(\delta_{13}) b a^2 \sin 2\theta_{\mu e}^{3\nu} \left[ \cos 2\theta_{12} \sin^2 \Delta_{21} + \sin^2 \Delta_{31} - \sin^2 \Delta_{32} \right] \\
 &+ \cos(\delta_{24}) b a \sin 2\theta_{\mu e}^{4\nu} \left[ \cos 2\theta_{12} \cos^2 \theta_{13} \sin^2 \Delta_{21} - \sin^2 \theta_{13} (\sin^2 \Delta_{31} - \sin^2 \Delta_{32}) \right] \\
 &+ \cos(\delta_{13} + \delta_{24}) a \sin 2\theta_{\mu e}^{3\nu} \sin 2\theta_{\mu e}^{4\nu} \left[ -\frac{1}{2} \sin^2 2\theta_{12} \cos^2 \theta_{13} \sin^2 \Delta_{21} \right. \\
 &+ \left. \cos 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32}) \right] \\
 &- \frac{1}{2} \sin(\delta_{13}) b a^2 \sin 2\theta_{\mu e}^{3\nu} \left[ \sin 2\Delta_{21} - \sin 2\Delta_{31} + \sin 2\Delta_{32} \right] \\
 &+ \frac{1}{2} \sin(\delta_{24}) b a \sin 2\theta_{\mu e}^{4\nu} \left[ \cos^2 \theta_{13} \sin 2\Delta_{21} + \sin^2 \theta_{13} (\sin 2\Delta_{31} - \sin 2\Delta_{32}) \right] \\
 &+ \frac{1}{2} \sin(\delta_{13} + \delta_{24}) a \sin 2\theta_{\mu e}^{3\nu} \sin 2\theta_{\mu e}^{4\nu} \left[ \cos^2 \theta_{12} \sin 2\Delta_{31} + \sin^2 \theta_{12} \sin 2\Delta_{32} \right] \\
 &+ \left( b^2 a^2 - \frac{1}{4} a^2 \sin^2 2\theta_{12} \sin^2 2\theta_{\mu e}^{3\nu} - \frac{1}{4} \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 2\theta_{\mu e}^{4\nu} \right) \sin^2 \Delta_{21}
 \end{aligned}$$

$$\begin{aligned}
 \text{where } \sin 2\theta_{\mu e}^{3\nu} &= \sin 2\theta_{13} \sin \theta_{23}, & b &= \cos \theta_{13} \cos \theta_{23} \sin 2\theta_{12}, \\
 \sin 2\theta_{\mu e}^{4\nu} &= \sin 2\theta_{14} \sin \theta_{24} & \text{and } a &= \cos \theta_{14} \cos \theta_{24}
 \end{aligned}$$

# How small a 3+1 can LBL ignore?

Can CP measurements at DUNE get affected by assuming the absence of sterile neutrinos when they exist in reality, but are obscure because of very small mixings?

Left: the results obtained are essentially the same

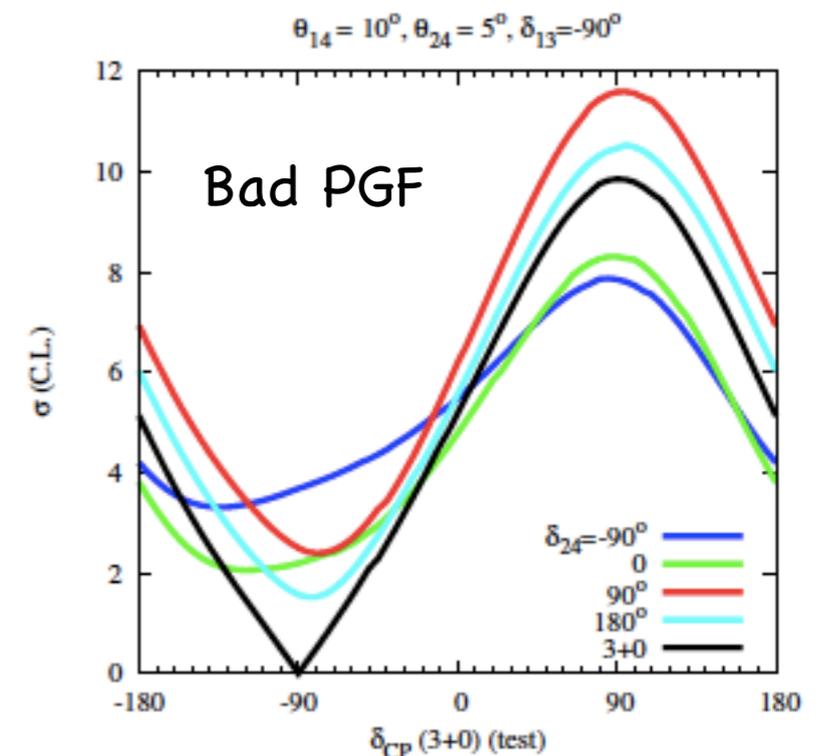
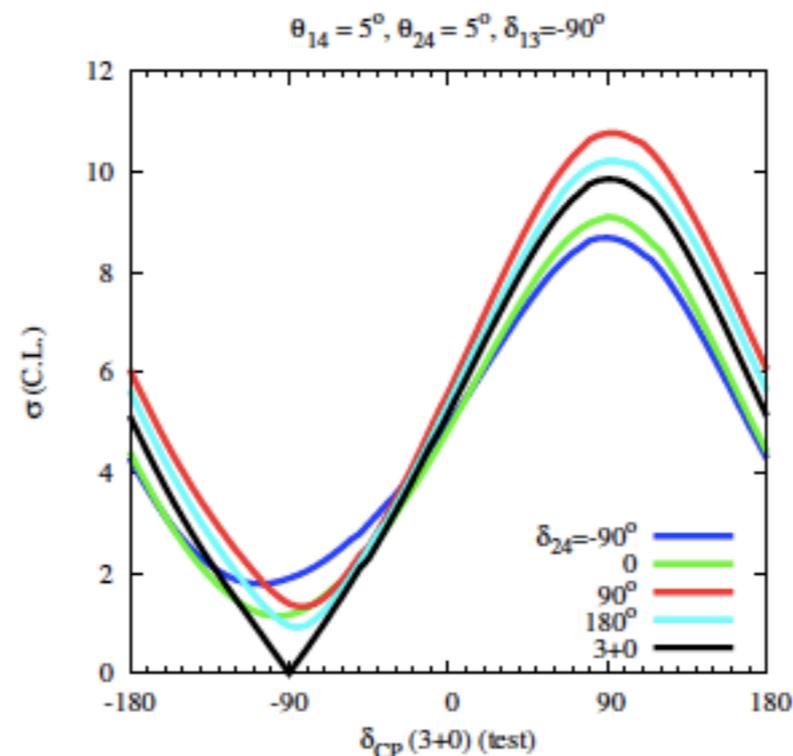
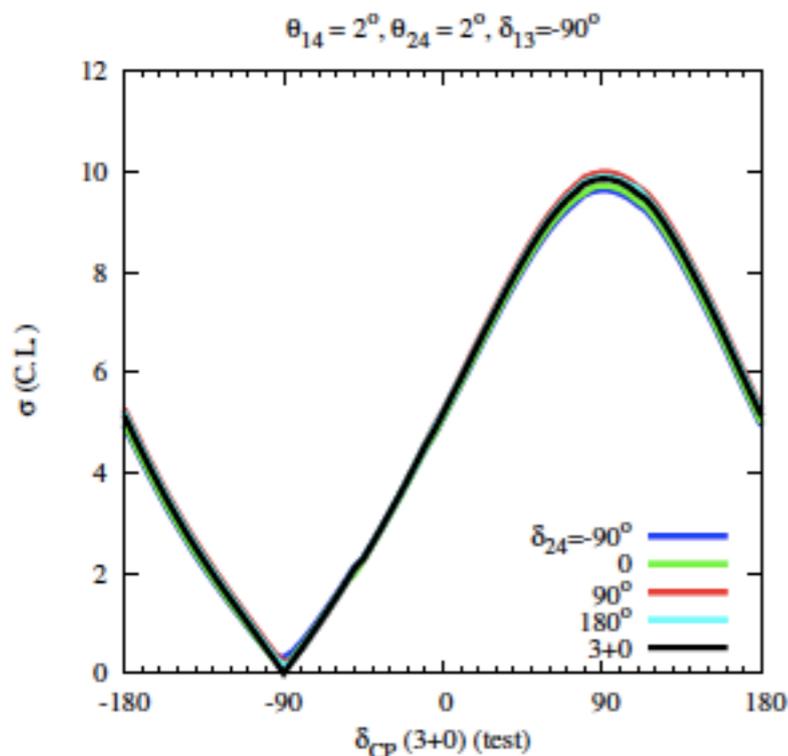
Middle: small deviations from the 3+0 results

Right: the precision can vary by around 10%

Sim. Data: 3+1

Fit: 3+0,  $\delta_{CP}$

$\sin^2 2\theta_{\mu e} < 0.001$   
(SBL Limit)



# Sterile Neutrinos or Flux Uncertainties? – Status of the Reactor Anti-Neutrino Anomaly

Mona Dentler, Álvaro Hernández-Cabezudo, Joachim Kopp, Michele Maltoni, Thomas Schwetz

*(Submitted on 13 Sep 2017)*

The  $\sim 3\sigma$  discrepancy between the predicted and observed reactor anti-neutrino flux, known as the reactor anti-neutrino anomaly, continues to intrigue. The recent discovery of an unexpected bump in the reactor anti-neutrino spectrum, as well as indications that the flux deficit is different for different fission isotopes seems to disfavour the explanation of the anomaly in terms of sterile neutrino oscillations. We critically review this conclusion in view of all available data on electron (anti)neutrino disappearance. We find that the sterile neutrino hypothesis cannot be rejected based on global data and is only mildly disfavored compared to an individual rescaling of neutrino fluxes from different fission isotopes. The main reason for this is the presence of spectral features in recent data from the NEOS and DANSS experiments. If state-of-the-art predictions for reactor fluxes are taken at face value, sterile neutrino oscillations allow a consistent description of global data with a significance close to  $3\sigma$  relative to the no-oscillation case. Even if reactor fluxes and spectra are left free in the fit, a  $2\sigma$  hint in favour of sterile neutrinos remains, with allowed parameter regions consistent with an explanation of the anomaly in terms of oscillations.

Comments: 24 pages, 5 figures

Subjects: **High Energy Physics – Phenomenology (hep-ph)**; High Energy Physics – Experiment (hep-ex)

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