

Constraints on the Scalar Sector of the Minimal Left-Right Symmetric Model

Tanmoy Mondal

HRI, Allahabad

Based On

1308.1291, 1311.5666
1508.04960, 1604.06987

Outline

- The Model : Left Right Symmetry
- Scalar Potential : MLRSM
- Tree Unitarity
- Plots

Left Right Symmetry

$$L \leftrightarrow R$$

Discrete symmetry that connects left and right sector.

$$G_{LR} = SU(3)_c \otimes SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$$

Quarks and leptons are in doublets

$$L_{iL} = \begin{pmatrix} \nu_i \\ \ell_i \end{pmatrix}_L : (2, 1, -1) \quad ; \quad L_{iR} = \begin{pmatrix} \nu_i \\ \ell_i \end{pmatrix}_R : (1, 2, -1)$$
$$Q_{iL} = \begin{pmatrix} u_i \\ d_i \end{pmatrix}_L : (2, 1, \frac{1}{3}) \quad ; \quad Q_{iR} = \begin{pmatrix} u_i \\ d_i \end{pmatrix}_R : (1, 2, \frac{1}{3})$$

LR Model Symmetry Breaking Pattern

$$SU(2)_L \otimes \underbrace{SU(2)_R \otimes U(1)_{B-L}}$$



$$\underbrace{SU(2)_L \otimes U(1)_Y}$$



$$U(1)_Q$$

LR Model Symmetry Breaking Pattern

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$$SU(2)_L \otimes U(1)_Y$$



$$U(1)_Q$$

- Triplet Scalars

$$\Delta_{L,R} = \begin{pmatrix} \delta_{L,R}^+/\sqrt{2} & \delta_{L,R}^{++} \\ \delta_{L,R}^+ & -\delta_{L,R}^0/\sqrt{2} \end{pmatrix}$$

- Doublet Scalars $(3, 1, 2)$ & $(1, 3, 2)$

$$H_{L,R} = \begin{pmatrix} h_{L,R}^0 \\ h_{L,R}^+ \end{pmatrix} : (2, 1, 1) \& (1, 2, 1)$$

- Higgs bi-doublet

$$\Phi = \begin{pmatrix} \phi_1^0 & \phi_1^+ \\ \phi_2^- & \phi_2^0 \end{pmatrix} : (2, 2, 0)$$

LR Model with Triplet Scalars

Most general Scalar Potential

$$\begin{aligned}
 V(\Phi, \Delta_L, \Delta_R) = & - \mu_1^2 \left\{ \text{Tr}[\Phi^\dagger \Phi] \right\} - \mu_2^2 \left\{ \text{Tr}[\tilde{\Phi} \Phi^\dagger] + \text{Tr}[\tilde{\Phi}^\dagger \Phi] \right\} - \mu_3^2 \left\{ \text{Tr}[\Delta_L^\dagger \Delta_L] + \text{Tr}[\Delta_R^\dagger \Delta_R] \right\} \\
 & + \lambda_1 \left\{ \left(\text{Tr}[\Phi^\dagger \Phi] \right)^2 \right\} + \lambda_2 \left\{ \left(\text{Tr}[\tilde{\Phi} \Phi^\dagger] \right)^2 + \left(\text{Tr}[\tilde{\Phi}^\dagger \Phi] \right)^2 \right\} + \lambda_3 \left\{ \text{Tr}[\tilde{\Phi} \Phi^\dagger] \text{Tr}[\tilde{\Phi}^\dagger \Phi] \right\} \\
 & + \lambda_4 \left\{ \text{Tr}[\Phi^\dagger \Phi] \left(\text{Tr}[\tilde{\Phi} \Phi^\dagger] + \text{Tr}[\tilde{\Phi}^\dagger \Phi] \right) \right\} \\
 & + \lambda_5 \left\{ \left(\text{Tr}[\Delta_L \Delta_L^\dagger] \right)^2 + \left(\text{Tr}[\Delta_R \Delta_R^\dagger] \right)^2 \right\} \\
 & + \lambda_6 \left\{ \text{Tr}[\Delta_L \Delta_L] \text{Tr}[\Delta_L^\dagger \Delta_L^\dagger] + \text{Tr}[\Delta_R \Delta_R] \text{Tr}[\Delta_R^\dagger \Delta_R^\dagger] \right\} + \lambda_7 \left\{ \text{Tr}[\Delta_L \Delta_L^\dagger] \text{Tr}[\Delta_R \Delta_R^\dagger] \right\} \\
 & + \lambda_8 [\Delta_L \Delta_L^\dagger] \left\{ \text{Tr}[\Delta_L \Delta_L^\dagger] \text{Tr}[\Delta_R \Delta_R^\dagger] \right\} \\
 & + \lambda_9 \left\{ \text{Tr}[\Phi^\dagger \Phi] \left(\text{Tr}[\Delta_L \Delta_L^\dagger] + \text{Tr}[\Delta_R \Delta_R^\dagger] \right) \right\} \\
 & + (\lambda_{10} + i \lambda_{11}) \left\{ \text{Tr}[\Phi \tilde{\Phi}^\dagger] \text{Tr}[\Delta_R \Delta_R^\dagger] + \text{Tr}[\Phi^\dagger \tilde{\Phi}] \text{Tr}[\Delta_L \Delta_L^\dagger] \right\} \\
 & + (\lambda_{10} - i \lambda_{11}) \left\{ \text{Tr}[\Phi^\dagger \tilde{\Phi}] \text{Tr}[\Delta_R \Delta_R^\dagger] + \text{Tr}[\tilde{\Phi}^\dagger \Phi] \text{Tr}[\Delta_L \Delta_L^\dagger] \right\} \\
 & + \lambda_{12} \left\{ \text{Tr}[\Phi \Phi^\dagger \Delta_L \Delta_L^\dagger] + \text{Tr}[\Phi^\dagger \Phi \Delta_R \Delta_R^\dagger] \right\} + \lambda_{13} \left\{ \text{Tr}[\Phi \Delta_R \Phi^\dagger \Delta_L^\dagger] + \text{Tr}[\Phi^\dagger \Delta_L \Phi \Delta_R^\dagger] \right\} \\
 & + \lambda_{14} \left\{ \text{Tr}[\tilde{\Phi} \Delta_R \Phi^\dagger \Delta_L^\dagger] + \text{Tr}[\tilde{\Phi}^\dagger \Delta_L \Phi \Delta_R^\dagger] \right\} + \lambda_{15} \left\{ \text{Tr}[\Phi \Delta_R \tilde{\Phi}^\dagger \Delta_L^\dagger] + \text{Tr}[\Phi^\dagger \Delta_L \tilde{\Phi} \Delta_R^\dagger] \right\},
 \end{aligned}$$

LR Model with Triplet Scalars

Neutral component of scalar field will get vev

$$\langle \Phi \rangle = \begin{pmatrix} v_1 & 0 \\ 0 & v_2 \end{pmatrix}_{(2,2,0)}, \quad \langle \Delta_L \rangle = \begin{pmatrix} 0 & 0 \\ v_L & 0 \end{pmatrix}_{(3,1,2)}, \quad \langle \Delta_R \rangle = \begin{pmatrix} 0 & 0 \\ v_R & 0 \end{pmatrix}_{(1,3,2)}$$

Step 1 : v_R breaks the $SU(2)_R \otimes U(1)_{B-L}$ symmetry to $U(1)_Y$,

$$\frac{Y}{2} = T_{3R} + \frac{B-L}{2}$$

Step 2 : $\langle \Phi \rangle, \langle \Delta_L \rangle$ breaks the $SU(2)_L \otimes U(1)_Y$ symmetry to $U(1)_{em}$

Higgs Sector after Symmetry Breaking

20 real fields (8 from bi-doublet and 6 from each triplet)

- 6 Goldstone Bosons ($Z_1, Z_2, W_L^\pm, W_R^\pm$)
- 4 CP-even neutral Higgs ($H_0^0, H_1^0, H_2^0, H_3^0$)
- 2 CP-odd neutral pseudo scalars (A_1^0, A_2^0)
- 2 Singly charged scalars ($H_{1/2}^\pm$) and
- 2 Doubly charged scalars ($H_{L/R}^{\pm\pm}$) .

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Constraint from ρ parameter

EW symmetry is broken by v_1, v_2, v_L .

$$\rho = \frac{\sum_{T,Y} [4T(T+1) - Y^2] |V_{T,Y}|^2}{\sum_{T,Y} 2Y^2 |V_{T,Y}|^2}$$

ρ parameter tells v_L should be < 2 GeV.

Higgs Sector after Symmetry Breaking

If $v_R \gg v_1$ then masses can be written as

$$\begin{aligned}M_{H_0}^2 &\simeq 2 \lambda_1 v_1^2 \\M_{H_1}^2 &\simeq \frac{1}{2} \lambda_5 v_R^2 \\M_{H_2}^2 &\simeq M_{A_1}^2 \simeq M_{H_2^\pm}^2 \simeq 2 \lambda_{12} v_R^2 \\M_{H_3}^2 &\simeq M_{A_2}^2 \simeq M_{H_1^\pm}^2 \simeq M_{H_L^{\pm\pm}}^2 \simeq \frac{1}{2} (\lambda_7 - 2 \lambda_5) v_R^2 \\M_{H_R^{\pm\pm}}^2 &\simeq 2 \lambda_6 v_R^2\end{aligned}$$

Unitarity

Using partial wave decomposition we have

$$\mathcal{M} = 16\pi \sum_{J=0}^{\infty} (2J+1) P_J(\cos\theta) a_J(\theta)$$

And the the cross-section

$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2 s} |\mathcal{M}|^2 \quad \Longrightarrow \quad \sigma = \frac{16\pi}{s} \sum_{J=0}^{\infty} (2J+1) |a_J|^2.$$

According to optical theorem:

$$\Im |\mathcal{M}(\theta=0)| = 2E_{cm} p_{cm} \sigma \quad \Longrightarrow \quad \sigma = \frac{1}{s} \Im |\mathcal{M}(\theta=0)|$$

We get

$$|a_J|^2 = \Im(a_J) \Longrightarrow \Re(a_J)^2 + \Im(a_J)^2 = \Im(a_J) \Longrightarrow |\Re(a_J)| \leq \frac{1}{2}$$

$$|\mathcal{M}| \leq 8\pi$$

Computation of Unitarity constraints : Method I

Rewrite scalar potential in terms of field components



Find all possible $0, 1, \dots, q$ charged 2-particle states



Taking 2-particle states as rows and columns construct the matrix



This matrix contains scattering amplitude of $2 \rightarrow 2$ processes



Find the eigenvalues. **Eigenvalues $\leq 8\pi$**



Satisfy above constraint along with VS and perturbativity.

Computation of Unitarity constraints : Method I

Number of all possible q -charged 2-particle states constructed from n neutral, s singly charged and d doubly charged fields.

Charge(q)	0	1	2	3	4
Number of states (general)	$\frac{n(n+1)}{2} + s^2 + d^2$	$s(n + d)$	$nd + \frac{s(s+1)}{2}$	sd	$\frac{d(d+1)}{2}$
Number of states (LRT Model)	56	40	26	8	3
Independent constraints	29	14	16	3	2

Computation of Unitarity constraints : Method I

$$\Phi = \begin{pmatrix} \frac{\phi_1^{0r} + i \phi_1^{0i}}{\sqrt{2}} & \phi_1^+ \\ \phi_2^- & \frac{\phi_1^{0r} + i \phi_1^{0i}}{\sqrt{2}} \end{pmatrix}$$

$$\Delta_R = \begin{pmatrix} \frac{\delta_R^+}{\sqrt{2}} & \delta_R^{++} \\ \frac{i\delta_R^{0i} + \delta_R^{0r}}{\sqrt{2}} & -\frac{\delta_R^+}{\sqrt{2}} \end{pmatrix}, \Delta_L = \begin{pmatrix} \frac{\delta_L^+}{\sqrt{2}} & \delta_L^{++} \\ \frac{i\delta_L^{0i} + \delta_L^{0r}}{\sqrt{2}} & -\frac{\delta_L^+}{\sqrt{2}} \end{pmatrix}$$

Computation of Unitarity constraints : Method I

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Doubly charged basis(26-d)

$$\begin{pmatrix} \phi_1^{+2} \\ \phi_1^+ \phi_2^+ \\ \delta_R^+ \phi_1^+ \\ \delta_L^+ \phi_1^+ \\ \phi_2^{+2} \\ \delta_R^+ \phi_2^+ \\ \delta_L^+ \phi_2^+ \\ \delta_R^{+2} \\ \delta_L^+ \delta_R^+ \\ \delta_L^{+2} \\ \delta_R^{++} \phi_1^{0r} \\ \vdots \end{pmatrix}$$

Computation of Unitarity constraints : Method I

$$\Phi = \begin{pmatrix} \frac{\phi_1^{0r} + i \phi_1^{0i}}{\sqrt{2}} & \phi_1^+ \\ \phi_2^- & \frac{\phi_1^{0r} + i \phi_1^{0i}}{\sqrt{2}} \end{pmatrix}$$

$$\Delta_R = \begin{pmatrix} \frac{\delta_R^+}{\sqrt{2}} & \delta_R^{++} \\ \frac{i\delta_R^{0i} + \delta_R^{0r}}{\sqrt{2}} & -\frac{\delta_R^+}{\sqrt{2}} \end{pmatrix}, \Delta_L = \begin{pmatrix} \frac{\delta_L^+}{\sqrt{2}} & \delta_L^{++} \\ \frac{i\delta_L^{0i} + \delta_L^{0r}}{\sqrt{2}} & -\frac{\delta_L^+}{\sqrt{2}} \end{pmatrix}$$

We have constructed all 0, 1, 2, 3 and 4-charged two-particle scattering matrix and find their eigenvalues.

Doubly charged basis(26-d)

$$\begin{pmatrix} \phi_1^{+2} \\ \phi_1^+ \phi_2^+ \\ \delta_R^+ \phi_1^+ \\ \delta_L^+ \phi_1^+ \\ \phi_2^{+2} \\ \delta_R^+ \phi_2^+ \\ \delta_L^+ \phi_2^+ \\ \delta_R^{+2} \\ \delta_L^+ \delta_R^+ \\ \delta_L^{+2} \\ \delta_R^{++} \phi_1^{0r} \\ \vdots \end{pmatrix}$$

Constraints on physical scalar masses

$$\begin{aligned}M_{H_0}^2 &\simeq 2 \lambda_1 v_1^2 = (125 \text{ GeV})^2 \\M_{H_1}^2 &\simeq \frac{1}{2} \lambda_5 v_R^2 \\M_{H_2}^2 \simeq M_{A_1}^2 \simeq M_{H_2^\pm}^2 &\simeq 2 \lambda_{12} v_R^2 \\M_{H_3}^2 \simeq M_{A_2}^2 \simeq M_{H_1^\pm}^2 \simeq M_{H_L^{\pm\pm}}^2 &\simeq \frac{1}{2} (\lambda_7 - 2\lambda_5) v_R^2 \\M_{H_R^{\pm\pm}}^2 &\simeq 2 \lambda_6 v_R^2\end{aligned}$$

- Randomly vary the quartic couplings $\lambda_5, \lambda_6, (\lambda_7 - 2\lambda_5)$ and λ_{12} in their allowed range $[0, 4\pi]$.
- These quartic couplings run according to their respective RGEs.
- Ensure that the quartic couplings obey all the conditions coming from vacuum stability, unitarity & perturbativity.
- The input quartic couplings which obey these conditions, till M_{Pl} , are interpreted as the accepted mass scale of physical scalars

Computation of Unitarity constraints : Method II

Rewrite the scalar potential in terms of physical fields

$$V \left(H_{0,1,2,3}^0, A_{1,2}^0, H_{1,2}^\pm, H_{1,2}^{\pm\pm} \right) = \sum_m \Lambda_m H_i H_j H_k H_\ell$$

Find all possible $H_i H_j \rightarrow H_k H_\ell$ processes

Gauge boson mediated terms diverges logarithmically. Neglect.

Conditions: $\Lambda_m \leq 8\pi$

Satisfy above constraint along with VS and perturbativity.

Computation of Unitarity constraints : Method II

$$\lambda_1 < 4\pi/3, (\lambda_1 + 4\lambda_2 + 2\lambda_3) < 4\pi,$$

$$(\lambda_1 - 4\lambda_2 + 2\lambda_3) < 4\pi,$$

$$\lambda_4 < 4\pi/3,$$

$$\alpha_1 < 8\pi, \alpha_2 < 4\pi, (\alpha_1 + \alpha_3) < 8\pi,$$

$$\rho_1 < 4\pi/3, (\rho_1 + \rho_2) < 2\pi, \rho_2 < 2\sqrt{2}\pi,$$

$$\rho_3 < 8\pi, \rho_4 < 2\sqrt{2}\pi.$$

Constraints coming from FCNC

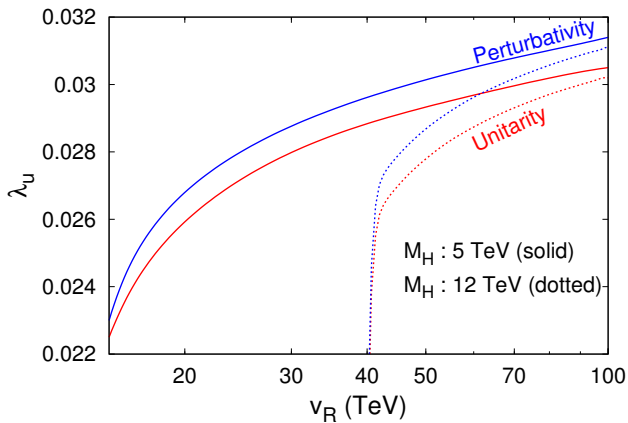
$$\frac{\sqrt{2}}{\kappa_-^2} \bar{\mathbf{U}}^L \left[\phi_-^0 \frac{\kappa_-^2}{\kappa_+} \mathbf{M}^U + \phi_+^0 \left(\frac{-2\kappa_1^* \kappa_2}{\kappa_+} \mathbf{M}^U + \kappa_+ \mathbf{V}_L^{\text{CKM}} \mathbf{M}^D \mathbf{V}_R^{\text{CKM}^\dagger} \right) \right] \mathbf{U}^R$$

$$\frac{\sqrt{2}}{\kappa_-^2} \bar{\mathbf{D}}^L \left[\phi_-^{0*} \frac{\kappa_-^2}{\kappa_+} \mathbf{M}^D + \phi_+^{0*} \left(\frac{-2\kappa_1 \kappa_2^*}{\kappa_+} \mathbf{M}^D + \kappa_+ \mathbf{V}_L^{\text{CKM}^\dagger} \mathbf{M}^U \mathbf{V}_R^{\text{CKM}} \right) \right] \mathbf{D}^R$$

- ϕ_+^0 gives tree level FCNC.
- Mass of this scalar is constrained severely (≥ 10 TeV).
- $\sqrt{\alpha_3(\lambda_{12})} v_R > 10$ TeV

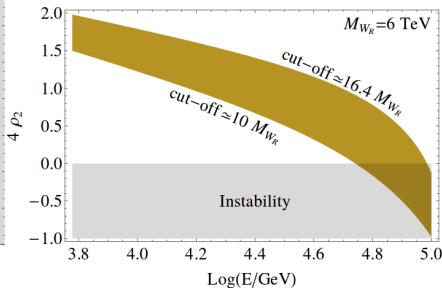
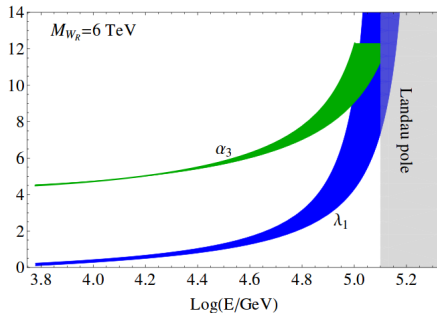
Constraints on LRSM parameter space from unitarity

Constraints on “universal” quartic couplings

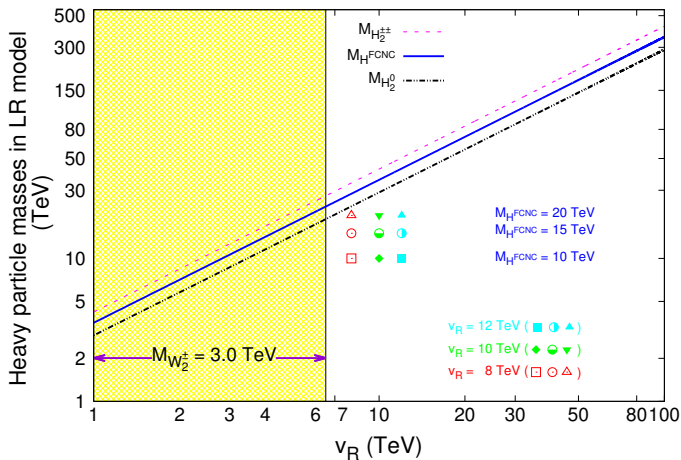


LHC scale W_R

$$W_R = 6 \text{ TeV} \implies v_R \simeq 13 \text{ TeV}$$

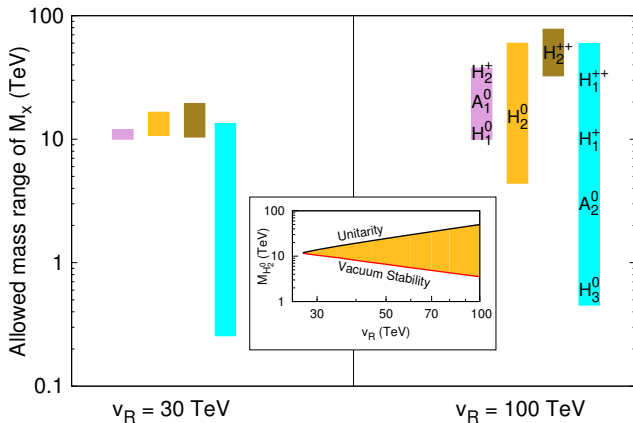


Constraints on physical scalars



Constraints on physical scalar masses

$$M_{H_1^0} \geq 10 \text{ TeV and } \lambda_u = 0.01.$$



Color codes

Purple : $M_{H_1^0}, M_{A_1^0} \geq 10 \text{ TeV} \Rightarrow$ Bound on λ_{12} from below. Maximum allowed value is restricted by perturbativity. Large v_R relaxes maximum bound on λ_{12} .

Yellow : Explained in Inset. λ_5 and λ_{12} are coupled through vacuum stability. Maximum allowed value of λ_5 is restricted from unitarity. Minimum depends on λ_{12} . Higher $v_R \Rightarrow$ lower $\lambda_{12} \Rightarrow$ low λ_5 .

Brown : With low initial value, λ_6 decreases with energy and eventually becomes negative leading to tachyonic states. To get rid of this λ_6 should be high enough \Rightarrow higher mass states.

Cyan : $(\lambda_7 - 2\lambda_5)$ is not constrained from vacuum stability and can be very low. $\mathcal{O}(100)$ GeV physical scalar masses are possible.

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v_R (TeV)	$M_{H_1^0}, M_{A_1^0}, M_{H_2^\pm}$ (TeV)	$M_{H_2^0}$ (TeV)	$M_{H_2^{\pm\pm}}$ (TeV)	$M_{H_3^0}, M_{A_2^0}, M_{H_1^\pm}, M_{H_1^{\pm\pm}}$ (TeV)
30	10 – 12	10.5 – 16.5	10.5 – 20	$\mathcal{O}(0.1) - 13.5$
100	10 – 37.5	4.4 – 60	33 – 78	$\mathcal{O}(0.1) - 59$

Conclusion

- BSM scalar sector is constrained by VS, unitarity and perturbativity.
- LRSM symmetry breaking vev is related to Unitarity via scalar masses.
- LHC scale W_R is valid upto ~ 100 TeV.
- Scalars which take part in FCNC are very heavy.
- In turn most of the scalars become heavy for low v_R .
- For heavy W_R some of the scalars can be light.

Conclusion

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- For heavy W_R some of the scalars can be light.

Thank You

Back up

Constraints on physical scalars

$$\lambda_1 = 0.13, \lambda_2 = 0, \lambda_3 = 0, \lambda_4 = 0,$$

$$\alpha_1 = 0, \alpha_2 = 0, \alpha_3 = 1.39,$$

$$\rho_1 = 1.0, \rho_2 = 7.5 \times 10^{-4}, \rho_3 = 2.003.$$

All masses are given in GeV:

$$M_{H_0^0} = 125,$$

$$M_{H_1^0} = 10000, M_{H_2^0} = 16971, M_{H_3^0} = 465,$$

$$M_{A_1^0} = 10000, M_{A_2^0} = 465,$$

$$M_{H_1^\pm} = 487, M_{H_2^\pm} = 10001,$$

$$M_{H_1^{\pm\pm}} = 508, M_{H_2^{\pm\pm}} = 508.$$

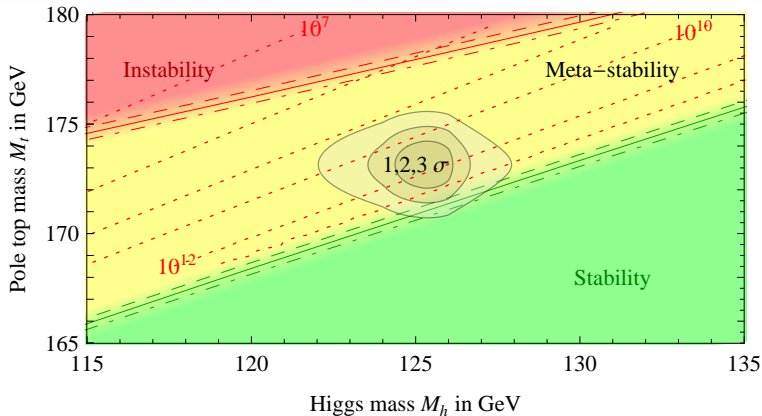


Figure: Dead or Alive ??

- SM in metastable region with 98% C.L.