

Inclusive jet and dijet production at the LHC

João Pires

CFTP, Instituto Superior Técnico, Lisbon

QCD@LHC2018

Dresden, 29 August 2018

FCT

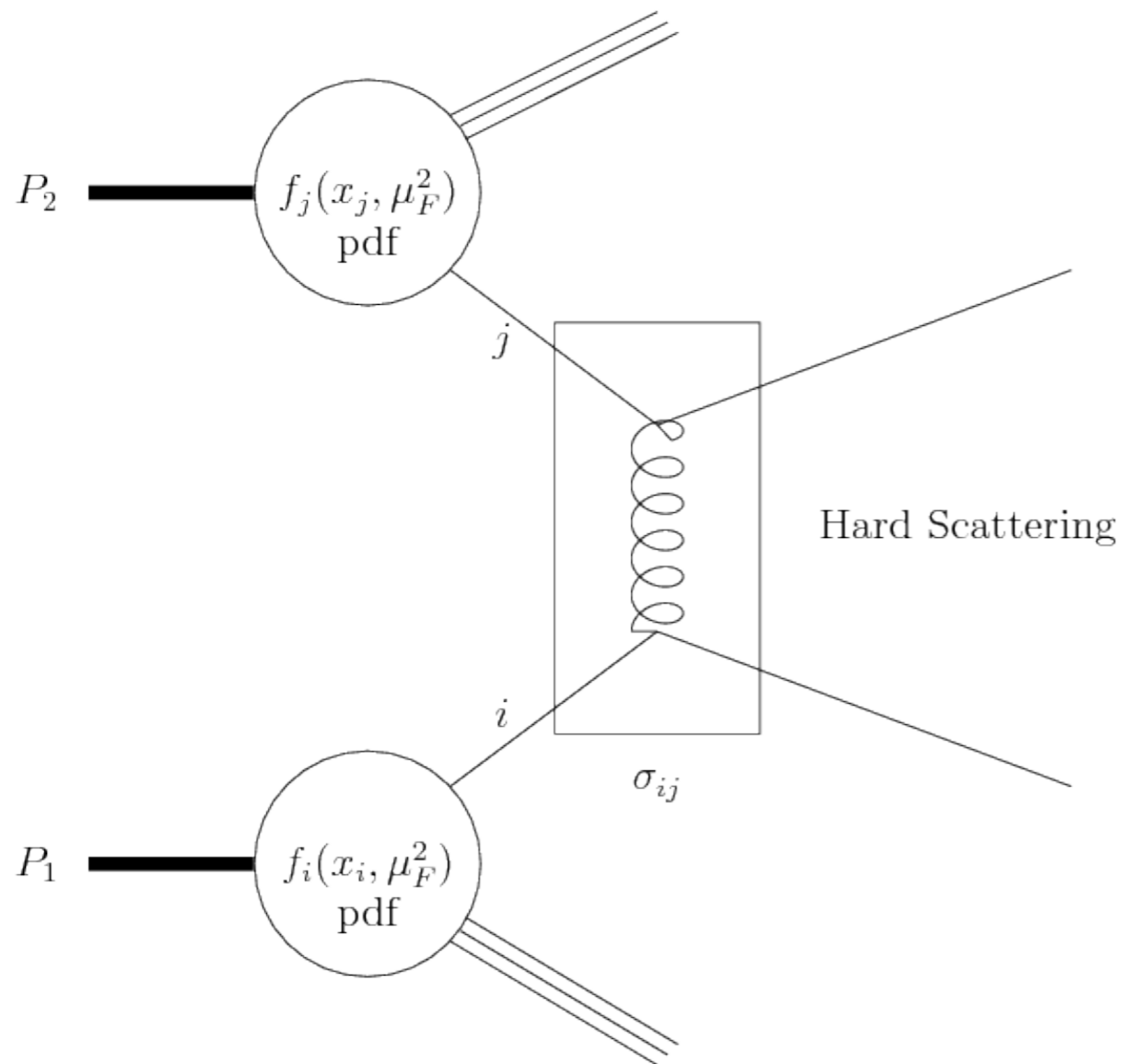
Fundação para a Ciência e a Tecnologia
MINISTÉRIO DA CIÊNCIA, TECNOLOGIA E ENSINO SUPERIOR

FCT-project
UID/FIS/00777/2013



- Theoretical framework: improved **parton model formula**

$$\sigma(P_1, P_2) = \sum_{i,j} \int dx_1 dx_2 f_i(x_1, \mu_F^2) f_j(x_2, \mu_F^2) \hat{\sigma}_{ij}(p_1, p_2, \alpha_s(\mu^2), s/\mu^2, s/\mu_F^2)$$

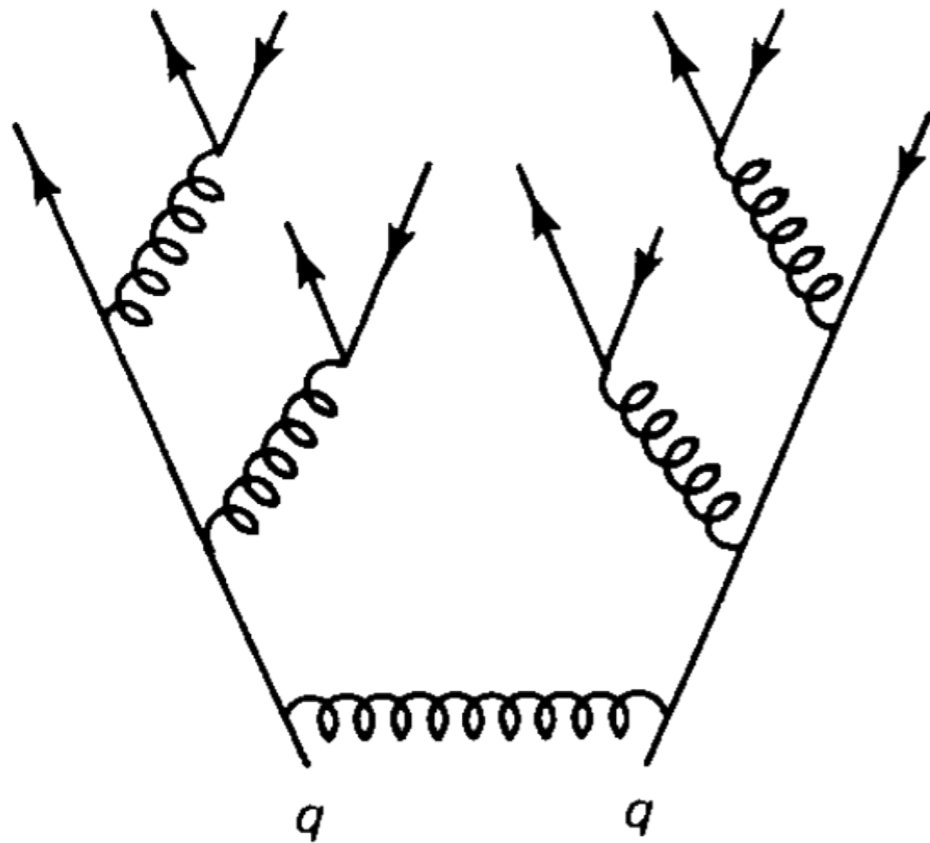


To apply:

- require large **momentum transfer**
- scale** of the reaction $Q^2 \gg \Lambda_{\text{hadronic}}$
- quarks** and **gluons** behave as **free particles** in the collision
- running **coupling** $\alpha_s(Q^2)$ decreases at **high-scales**
- compute partonic cross section σ_{ij} in **perturbation theory** \rightarrow QCD Lagrangian

After hard scattering respect *quark confinement*:

- individual **quarks** cannot be observed directly



- force between **quarks** increases as they are **separated**
 - I - soft and collinear radiation produces new **$q\bar{q}$** pairs
 - **higher order corrections** and **parton shower** **matched** to ME calculation simulate QCD radiation from the scattering scale Q^2 to the hadronization scale $\Lambda_{\text{hadronic}}$
 - II - **hadronization** of **quarks** and **gluons** to form collimated bound states of baryons and mesons \rightarrow **final state jet**
- properties of the **final state jet** follow closely the properties of the parton that initiated it local *parton-hadron duality*

Jet algorithms

Jet algorithms standardise the definition of jets and reduce the complexity of the final state to simpler calculable objects

- find the smallest distance measure d_{ij} between two particles and combine them if d_{ij} smaller than the jet resolution size R

$$d_{ij} = \min(p_{ti}^{2p}, p_{tj}^{2p}) \frac{\Delta R_{ij}^2}{R^2}, \quad \Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$
$$d_{iB} = p_{ti}^{2p},$$

- CMS and ATLAS have settled on anti- k_T jets ($p=-1$)

$$\mathcal{J}_{n+1}(p_1, \dots, p_i, p_j) \stackrel{p_i // p_j}{=} \mathcal{J}_n(p_1, \dots, p_{ij})$$
$$\mathcal{J}_{n+1}(p_1, \dots, p_n, p_i) \stackrel{p_i \rightarrow 0}{=} \mathcal{J}_n(p_1, \dots, p_n)$$

- infrared-safe jet definition \rightarrow allows inclusion of higher order perturbative corrections to the inclusive jet cross section

Inclusive jet cross section: theory status

Much progress in fixed-order calculations/resummed and parton-shower predictions

- NLO QCD *[Ellis, Kunszt, Soper '92] [Giele, Glover, Kosower '94] [Nagy 02]*
- NLO EW *[Dittmaier, Huss, Speckner '13]*
[Frederix, Frixione, Hirschi, Pagani, Shao, Zaro '17]
- NLO QCD + PS (POWHEG) *[Alioli, Hamilton, Nason, Oleari, Re '11]*
- NLO QCD + PS (MC@NLO) *[Hoeche, Schonherr '12]*
- NLO QCD + Resummation (threshold+jet radius)
[Dasgupta, Dreyer, Salam, Soyez '14] [Liu, Moch, Ringer '17]
- NNLO QCD *[Gehrmann-De Ridder, Gehrmann, Glover, JP '13] [Currie, Glover, JP '16]*
[Currie, Gehrmann-De Ridder, Gehrmann, Glover, Huss, JP '17]

NLO QCD + PS (POWHEG)

Nason [[arXiv:hep-ph/0409146](#)] *JHEP* 0411 (2004) 040

Alioli, Hamilton, Nason, Oleari, Re [[arXiv: 1012.3380](#)] *JHEP* 1104 (2011) 081

- **hardest emission** generated first according to:

$$d\sigma = \bar{B}(\Phi_B) d\Phi_B \left[\Delta_R(p_T^{\min}) + \frac{R(\Phi_R)}{B(\Phi_B)} \Delta_R(k_T(\Phi_R)) d\Phi_{\text{rad}} \right]$$

- with the **born cross section** replaced with the **NLO differential cross section** at fixed Born kinematics **integrated** over **single emission** → preserves **NLO accuracy** for **inclusive quantities**

$$\bar{B}(\Phi_B) = B(\Phi_B) + \left[V(\Phi_B) + \int d\Phi_{\text{rad}} R(\Phi_R) \right]$$

- **probability** of not having an emission **harder** than p_T → POWHEG Sudakov

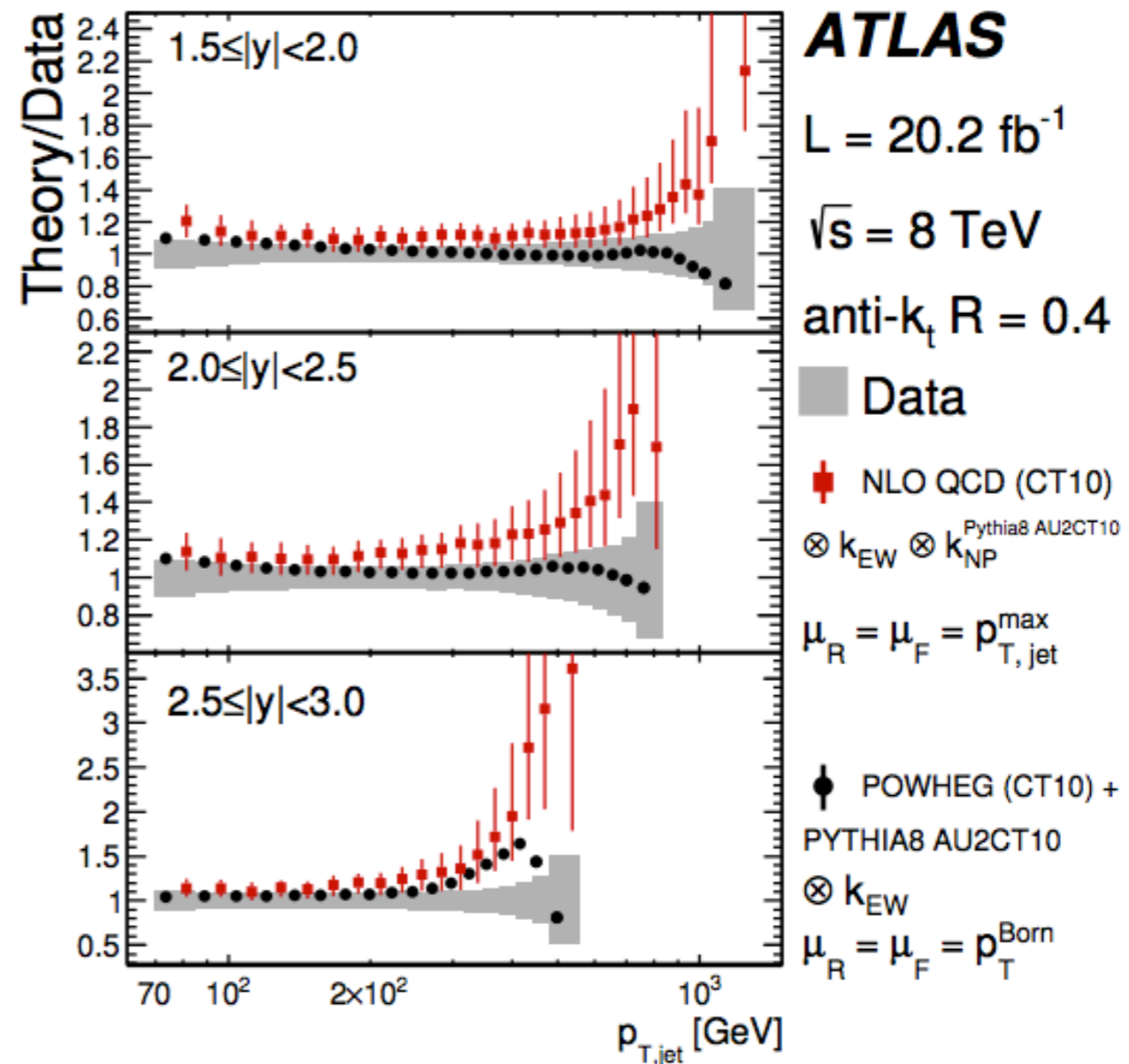
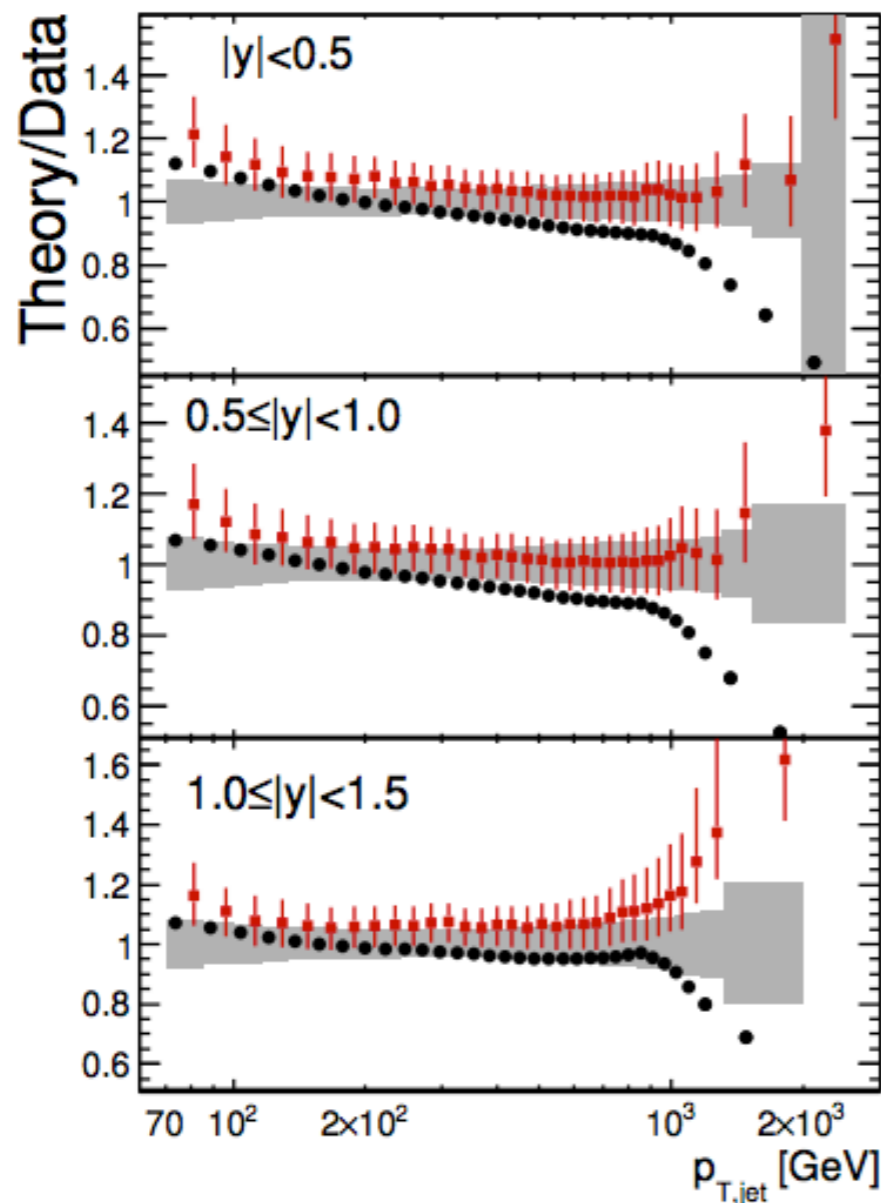
$$\Delta_R(p_T) = \exp \left[- \int d\Phi_{\text{rad}} \frac{R(\Phi_R)}{B(\Phi_B)} \theta(k_T(\Phi_R) - p_T) \right]$$

- **interface** with **shower generator** to develop the rest of the **shower vetoing emissions** **harder** than the first one

NLO QCD + PS (POWHEG)

ATLAS [arXiv: 1706.03192] JHEP 1709 (2017) 020

- Comparison to cross section data $R = 0.4; 0.6$ @ 8 TeV
- POWHEG prediction lower than fixed-order NLO QCDxNP → more in Bogdan's talk
- Ratio to data less sensitive to the jet radius in POWHEG



NLO QCD + Resummation (threshold+jet radius)

Liu, Moch, Ringer [arXiv: 1708.04641] Phys. Rev. Lett. 119, 212001 (2017)

Liu, Moch, Ringer [arXiv: 1801.07284] Phys.Rev. D97 (2018) no.5, 056026

Dasgupta, Dreyer, Salam, Soyez [arXiv: 1602.01110] JHEP 1606 (2016) 057

Double differential single jet inclusive cross section:

$$\frac{p_T^2 d^2 \sigma}{dp_T^2 dy} = \sum_{i_1 i_2} \int_0^{V(1-W)} dz \int_{\frac{vW}{1-z}}^{1-\frac{1-v}{1-z}} dv x_1^2 f_{i_1}(x_1) x_2^2 f_{i_2}(x_2) \frac{d^2 \hat{\sigma}_{i_1 i_2}}{dv dz}(v, z, p_T, R)$$

- $z = s_4/s$ invariant mass recoiling against the jet

- in the small R -limit and threshold limit $z \rightarrow 0$ cross section factorizes within SCET

$$\begin{aligned} \frac{d^2 \hat{\sigma}_{i_1 i_2}}{dv dz} = & s \int ds_X ds_c ds_G \delta(zs - s_X - s_G - s_c) \text{Tr} [\mathbf{H}_{i_1 i_2}(v, p_T, \mu_h, \mu) \mathbf{S}_G(s_G, \mu_{sG}, \mu)] \\ & \times J_X(s_X, \mu_X, \mu) \sum_m \text{Tr} [J_m(p_T R, \mu_J, \mu) \otimes_{\Omega} S_{c,m}(s_c R, \mu_{sc}, \mu)] , \end{aligned}$$

- perturbative contributions know at least to NLO

- joint resummation at NLL accuracy $\alpha_s^n \left(\ln^k(z)/z \right)_+$; $\alpha_s^n \ln^k(R)$

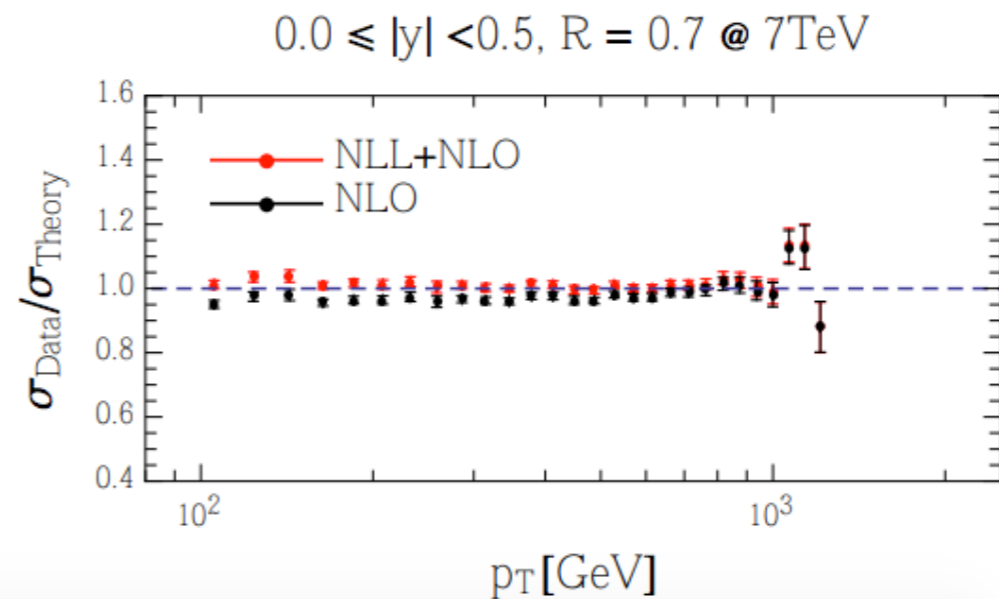
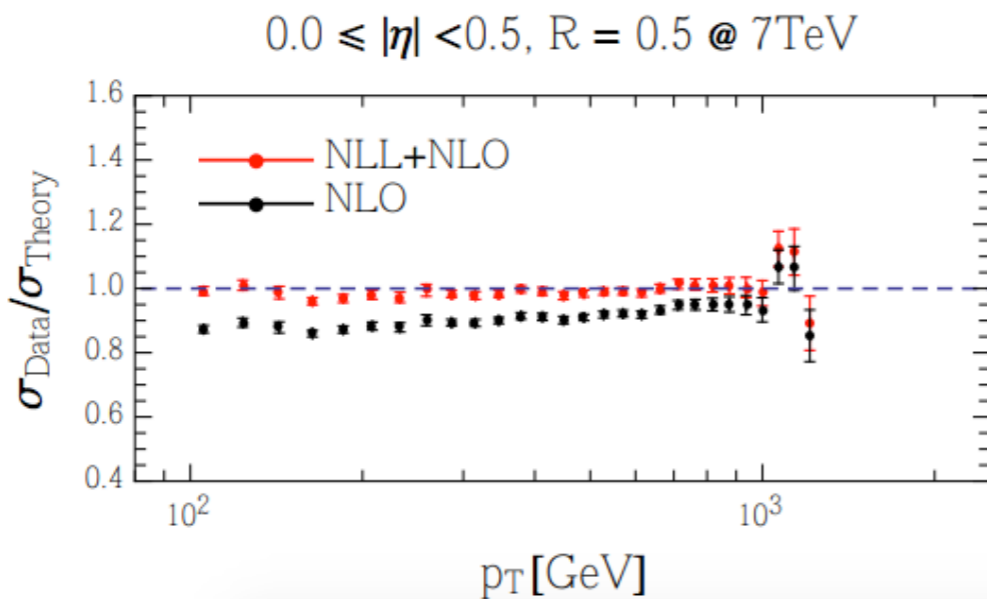
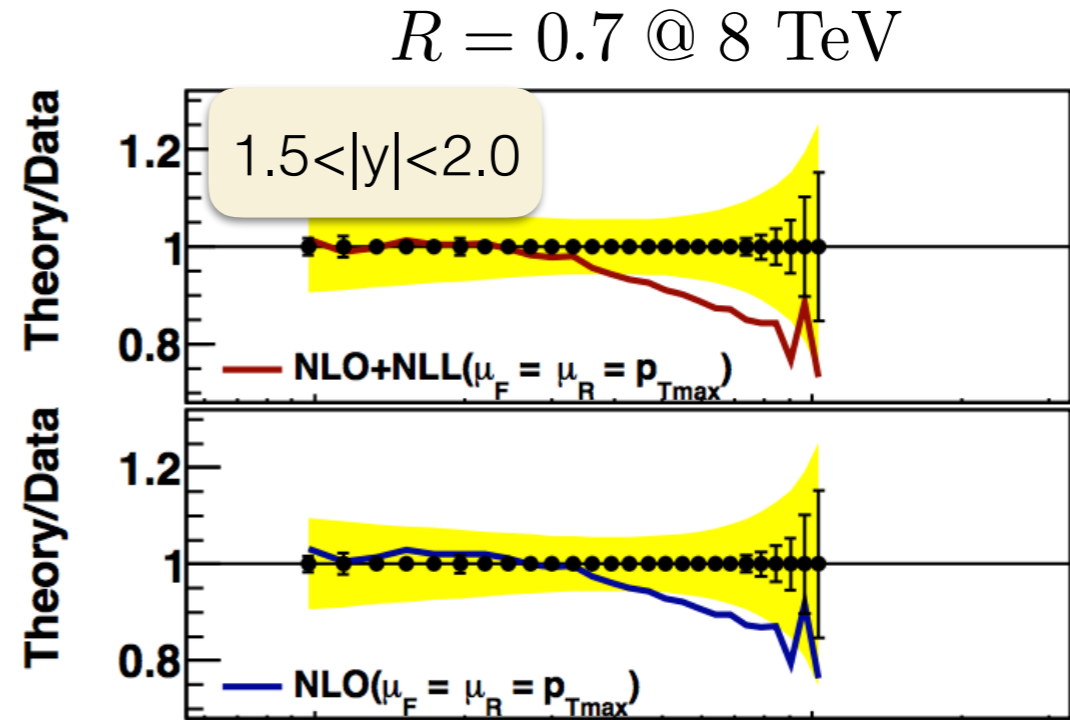
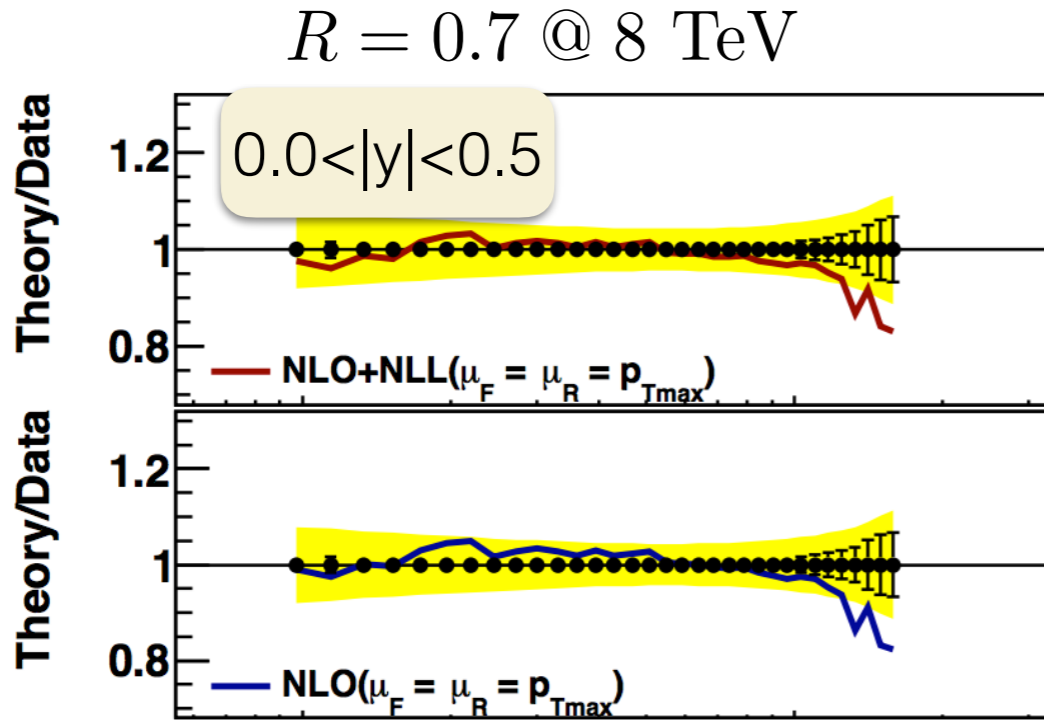
- additive matching to fixed-order NLO QCD result

$$\sigma_{\text{NLO+NLL}} = \sigma_{\text{NLO}} - \sigma_{\text{NLO}_{\text{sing}}} + \sigma_{\text{NLL}}$$

- resummation scales μ_i evolved through RGE equations to common hard scale $\mu = \mu_h = p_T^{\text{max}}$

NLO QCD + Resummation (threshold+jet radius)

Liu, Moch, Ringer [arXiv: 1801.07284] Phys.Rev. D97 (2018) no.5, 056026
 Liu, Moch, Ringer [arXiv: 1808.04574]



- **threshold logs** lead to an **enhancement** of the cross section for large p_T $\mu = \mu_h = p_T^{max}$
- **resummation** of **small R-logs** lead to a **decrease** in the **cross section** in the entire range p_T

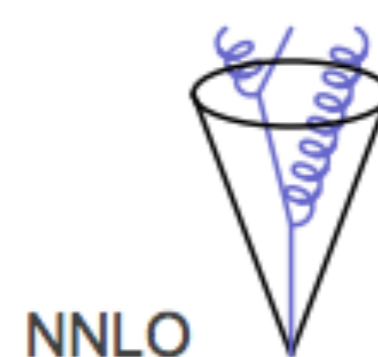
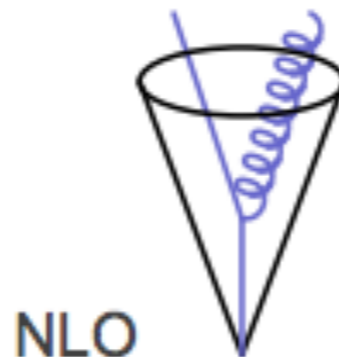
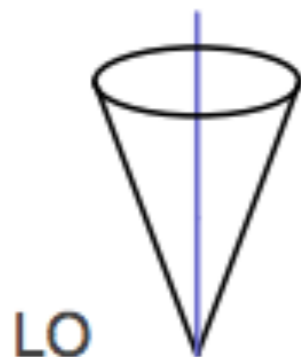
NNLO QCD

Motivations:

- **Reduced scale dependence** of the prediction, i.e. μ_R with $L_R = \log(\mu_R/\mu_0)$

$$\begin{aligned}\sigma(\mu_R, \alpha_s(\mu_R), L_R) &= \left(\frac{\alpha_s(\mu_R)}{2\pi}\right)^2 \sigma_{ij}^0 + \left(\frac{\alpha_s(\mu_R)}{2\pi}\right)^3 \left\{ \sigma_{ij}^1 + 2\beta_0 L_R \sigma_{ij}^0 \right\} \\ &+ \left(\frac{\alpha_s(\mu_R)}{2\pi}\right)^4 \left\{ \sigma_{ij}^2 + L_R (3\beta_0 \sigma_{ij}^1 + 2\beta_1 \sigma_{ij}^0) + L_R^2 3\beta_0^2 \sigma_{ij}^0 \right\} \\ &+ \mathcal{O}(\alpha_s(\mu_R)^5)\end{aligned}$$

- Jets **modelled** by **extra partons** → perturbation theory can start **reconstructing** the **shower**
- Better **matching** of **jet algorithm** between **theory** and **experiment** and **improved** understanding of the **jet shape**

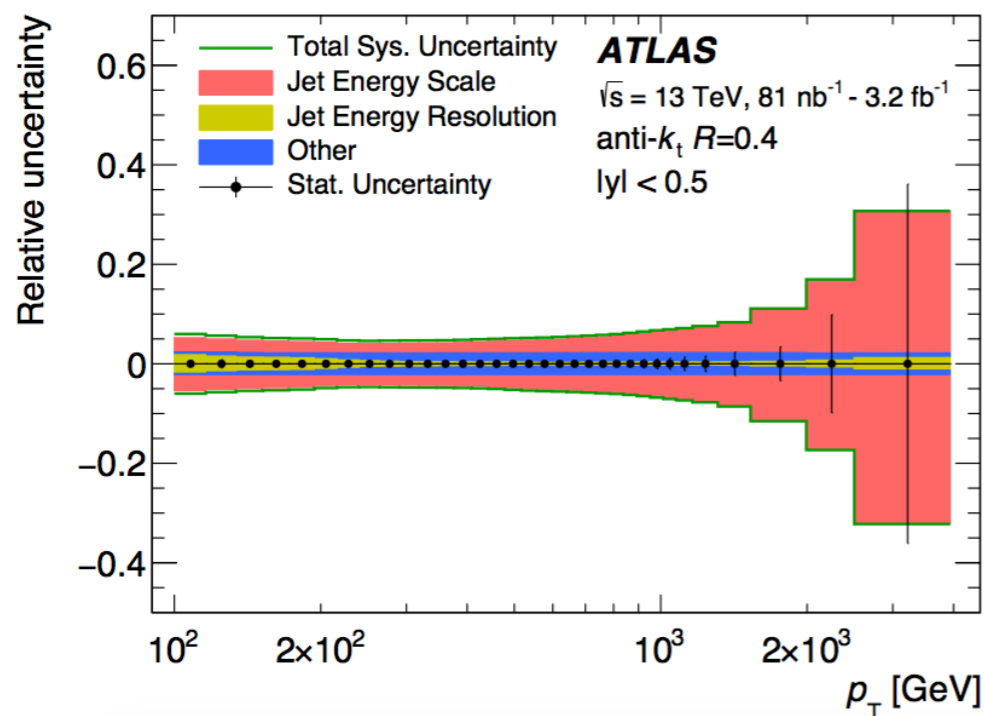


NNLO QCD

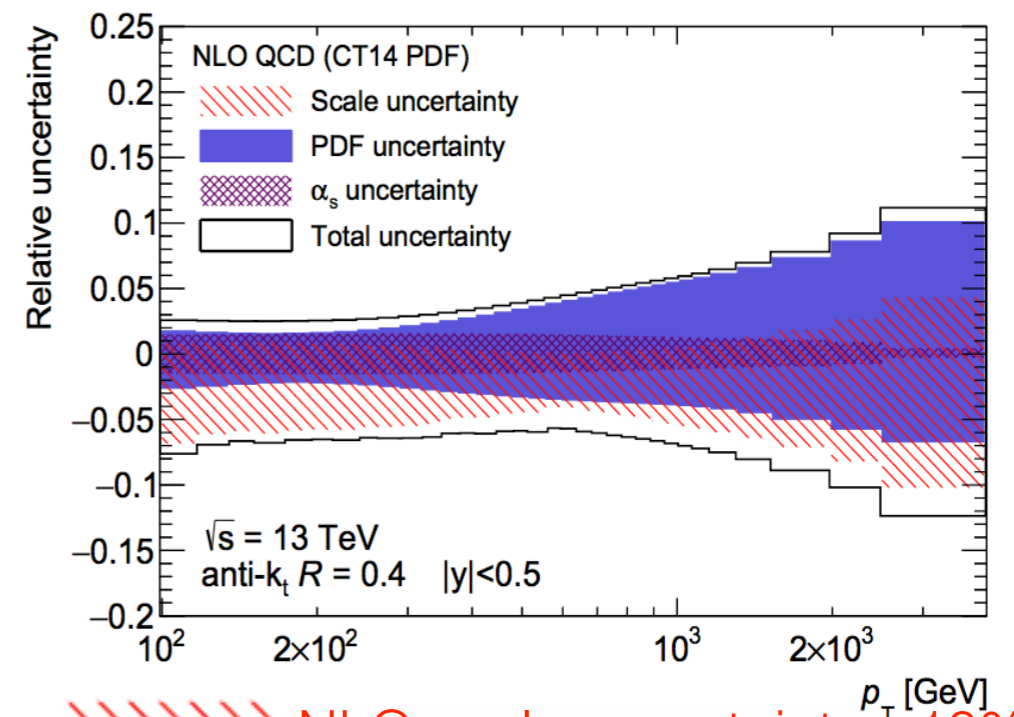
- At LO **final state** has no **transverse momentum**
- Better description of the **transverse momentum** of the **final state** due to double radiation off **initial state**



- NNLO provides the **first serious estimate** of the **theory error** → allows **comparison** with wealth of **experimental jet data** which have **similar precision**



dominant exp. systematic uncertainty
 jet energy scale: $\pm 5-10\%$



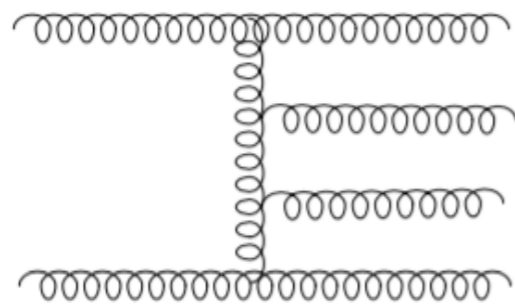
////// NLO scale uncertainty $\sim 10\%$
 NNLO needed

NNLO contributions

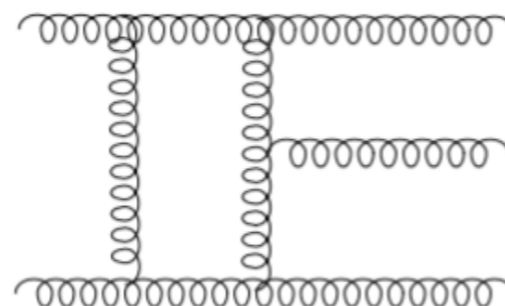
- Perturbative QCD **expansion** of the inclusive jet cross section at **hadron colliders**

$$d\sigma = \sum_{i,j} \int \left[d\hat{\sigma}_{ij}^{LO} + \left(\frac{\alpha_s}{2\pi}\right) d\hat{\sigma}_{ij}^{NLO} + \left(\frac{\alpha_s}{2\pi}\right)^2 d\hat{\sigma}_{ij}^{NNLO} + \mathcal{O}(\alpha_s^3) \right] f_i(x_1) f_j(x_2) dx_1 dx_2$$

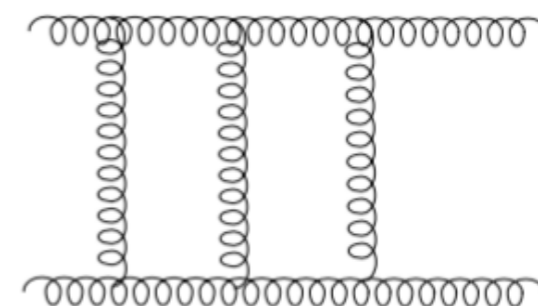
- NNLO gluonic contributions



$A_6^{(0)}(gg \rightarrow gggg)$



$A_5^{(1)}(gg \rightarrow ggg)$



$A_4^{(2)}(gg \rightarrow gg)$

- tree-level 2→4 matrix elements
- one-loop 2→3 matrix elements
- two-loop 2→2 matrix elements
- NNLO DGLAP evolution
- NNLO PDF's

[Berends, Giele '87] [Mangano, Parke, Xu '87]
[Britto, Cachazo, Feng '06]

[Bern, Dixon, Kosower '93] [Kunszt, Signer, Trocsanyi '94]

[Anastasiou, Glover, Oleari, Tejeda-Yeomans '01] [Bern, De Freitas, Dixon '02]

[Moch, Vermaseren, Vogt '04]

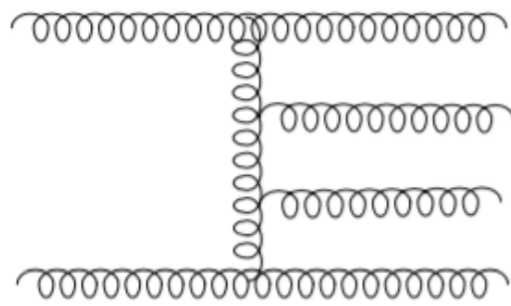
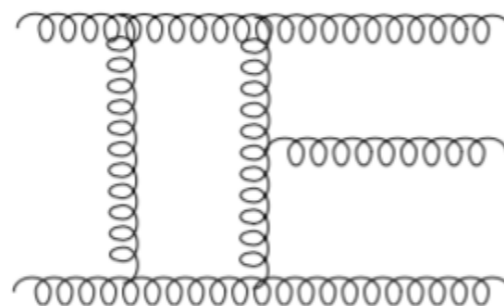
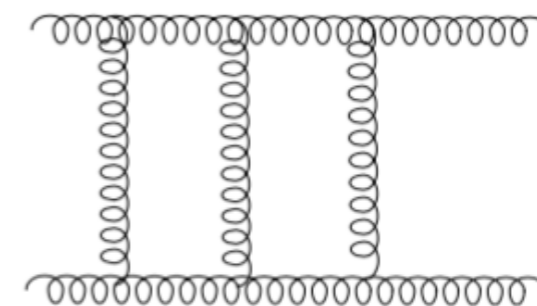
[ABMP, CT, NNPDF, MMHT]

$$d\hat{\sigma}_{NNLO} = \int_{d\Phi_4} d\hat{\sigma}_{NNLO}^{RR} + \int_{d\Phi_3} d\hat{\sigma}_{NNLO}^{RV} + \int_{d\Phi_2} d\hat{\sigma}_{NNLO}^{VV}$$

$$d\hat{\sigma}_{NNLO}^{RR} = \mathcal{N} d\Phi_4(p_3, p_4, p_5, p_6; p_1, p_2) |\mathcal{M}_{gg \rightarrow gggg}^{(0)}|^2 J_2^{(4)}(p_3, p_4, p_5, p_6)$$

$$d\hat{\sigma}_{NNLO}^{RV} = \mathcal{N} d\Phi_3(p_3, p_4, p_5; p_1, p_2) \left(\mathcal{M}_{gg \rightarrow ggg}^{(0)*} \mathcal{M}_{gg \rightarrow ggg}^{(1)} + \mathcal{M}_{gg \rightarrow ggg}^{(0)} \mathcal{M}_{gg \rightarrow ggg}^{(1)*} \right) J_2^{(3)}(p_3, p_4, p_5)$$

$$d\hat{\sigma}_{NNLO}^{VV} = \mathcal{N} d\Phi_2(p_3, p_4; p_1, p_2) \left(\mathcal{M}_{gg \rightarrow gg}^{(2)*} \mathcal{M}_{gg \rightarrow gg}^{(0)} + \mathcal{M}_{gg \rightarrow gg}^{(0)} \mathcal{M}_{gg \rightarrow gg}^{(2)*} + |\mathcal{M}_{gg \rightarrow gg}^{(1)}|^2 \right) J_2^{(2)}(p_3, p_4)$$


 $A_6^{(0)}(gg \rightarrow gggg)$

 $A_5^{(1)}(gg \rightarrow ggg)$

 $A_4^{(2)}(gg \rightarrow gg)$

- explicit infrared poles from loop integrations
- implicit poles in phase space regions corresponding to single and double unresolved gluon emission
- procedure to extract the infrared singularities and assemble all the parts

NNLO antenna subtraction

$$\begin{aligned}
 d\hat{\sigma}_{NNLO} &= \int_{d\Phi_4} \left(d\hat{\sigma}_{NNLO}^{RR} - d\hat{\sigma}_{NNLO}^S \right) \\
 &+ \int_{d\Phi_3} \left(d\hat{\sigma}_{NNLO}^{RV} - d\hat{\sigma}_{NNLO}^T \right) \\
 &+ \int_{d\Phi_2} \left(d\hat{\sigma}_{NNLO}^{VV} - d\hat{\sigma}_{NNLO}^U \right)
 \end{aligned}$$

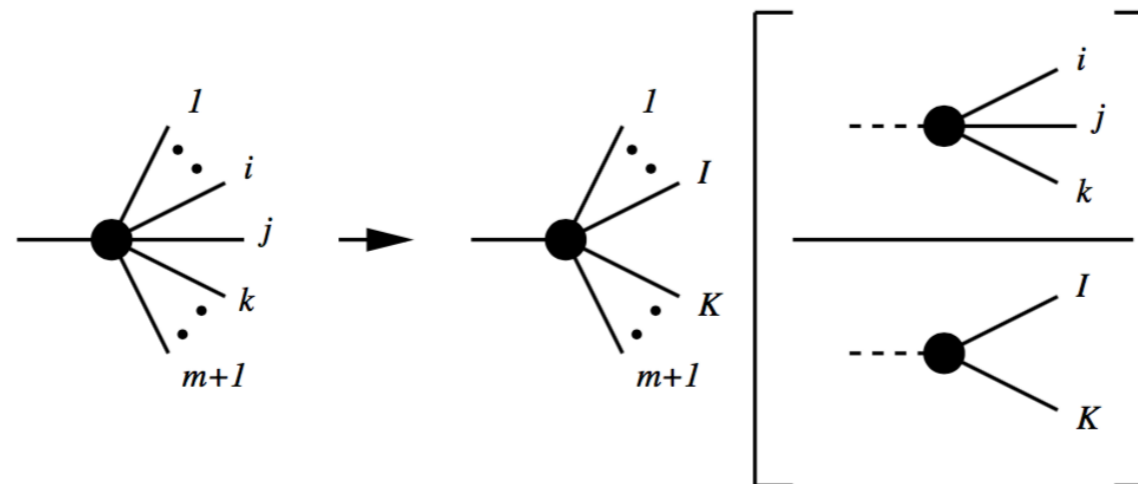
$$d\hat{\sigma}_{NNLO}^S \quad d\hat{\sigma}_{NNLO}^T$$

- mimic RR,RV in unresolved limits

$$d\hat{\sigma}_{NNLO}^T \quad d\hat{\sigma}_{NNLO}^U$$

- analytically cancel the poles in RV and VV matrix elements

- matrix elements: universal factorization properties in IR limits



- phase space factorization

$$d\Phi_{m+1}(p_1, \dots, p_{m+1}; q) = d\Phi_m(p_1, \dots, \tilde{p}_I, \tilde{p}_K, \dots, p_{m+1}; q) \cdot d\Phi_{X_{ijk}}(p_i, p_j, p_k; \tilde{p}_I + \tilde{p}_K)$$

NNLO antenna subtraction

$$\begin{aligned}
 d\hat{\sigma}_{NNLO} &= \int_{d\Phi_4} \left(d\hat{\sigma}_{NNLO}^{RR} - d\hat{\sigma}_{NNLO}^S \right) && d\hat{\sigma}_{NNLO}^S & d\hat{\sigma}_{NNLO}^T \\
 &+ \int_{d\Phi_3} \left(d\hat{\sigma}_{NNLO}^{RV} - d\hat{\sigma}_{NNLO}^T \right) && && d\hat{\sigma}_{NNLO}^T & d\hat{\sigma}_{NNLO}^U \\
 &+ \int_{d\Phi_2} \left(d\hat{\sigma}_{NNLO}^{VV} - d\hat{\sigma}_{NNLO}^U \right) && && &
 \end{aligned}$$

- mimic RR,RV in unresolved limits

- analytically cancel the poles in RV and VV matrix elements

For inclusive jet and dijet production: $pp \rightarrow \text{jet} + X$; $pp \rightarrow 2\text{jet} + X$

- NNLO corrections known [Currie, Gehrmann-De Ridder, Gehrmann, Glover, Huss, JP '17]
- all channels $\{gg, qg, q\bar{q}, qq, qq', q\bar{q}'\}$ at leading colour $\alpha_s^2 N^2, \alpha_s^2 NN_F, \alpha_s^2 N_F^2$
- gg-channel with full colour
- sub-leading colour contributions: (suppressed by $1/N^2$)
 - below two percent at NLO (all channels)

NNLOJET

NNLO **fully differential** parton-level **generator**

- Based on **antenna subtraction** for the **analytic** cancellation of IR **singularities** at NNLO

Infrastructure

- Process management
- Phase space, histogram routines
- Validation and testing
- ApplFast interface in progress

Processes implemented at NNLO

- $Z+(0,1)$ jet, $W+(0,1)$ jet
- $H+(0,1)$ jet
- DIS-2jet
- VBF $H+2$ jet
- Inclusive jet production

**X.Chen, J.Cruz-Martinez, J.Currie, R.Gauld, T.Gehrmann, A.Gehrmann-De Ridder, E.W.N.Glover, M.Höfer, A.Huss, T.Morgan, I.Majer, J.Niehues, D.Walker, JP [arXiv: 1801.06415] and references therein*

Dijet inclusive production $\sqrt{s}=7$ TeV

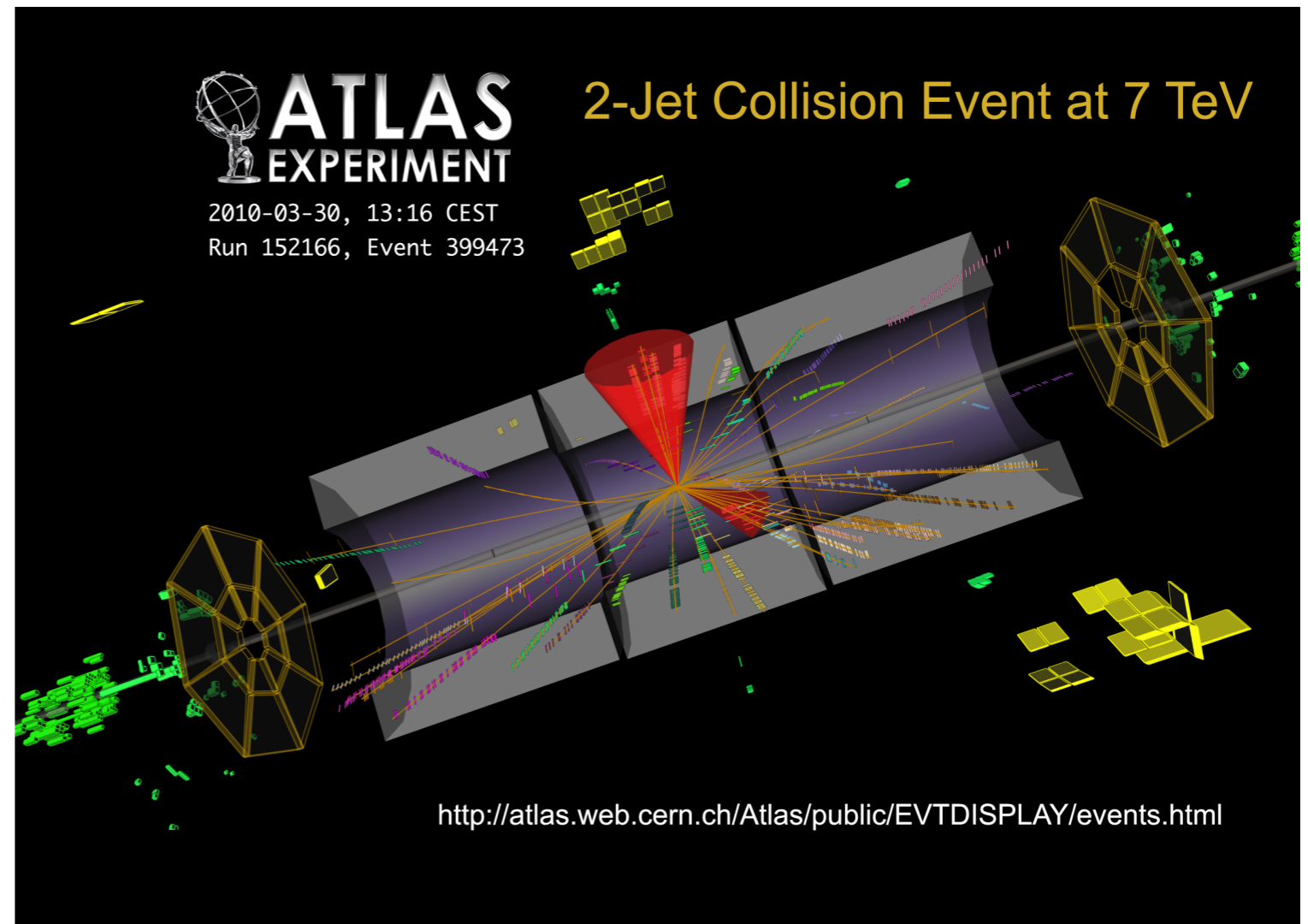
J. Currie, T. Gehrmann, A. Gehrmann-De Ridder, E.W.N. Glover, A. Huss, JP [arXiv: 1705.10271] Phys. Rev. Lett. 119, 152001 (2017)

Theory setup

- MMHT2014 nnlo
- anti- k_T jet algorithm
- $p_{T1} > 100$ GeV; $p_{T2} > 50$ GeV;*
- $|y_{j1}|, |y_{j2}| < 3.0$
- $\mu_R = \mu_F = \{m_{jj}, \langle p_T \rangle\}$
- vary scales by factors of 2 and 1/2

Comparison to data

- ATLAS 7 TeV ; $L=4.5$ fb $^{-1}$
- $R=0.4$



**[ATLAS, arXiv:1312.3524]
JHEP 1405 (2014) 059**

**measurement requires observation of a dijet system in the final state; asymmetric p_T cuts increase phase space available for real-gluon emission suppressing large logs in the QCD perturbative expansion of the observable*

Dijet inclusive production: scale choice

$pp \rightarrow 2\text{jets} + X$:

- cross section measured differentially in:

$$m_{jj}^2 = (p_{j1} + p_{j2})^2$$

$$y^* = \frac{1}{2}(y_{j1} - y_{j2})$$

- compare behaviour of the scales (normalised to data)

$$\mu = m_{jj} \quad ; \quad \mu = \langle p_T \rangle = \frac{1}{2}(p_{T1} + p_{T2})$$

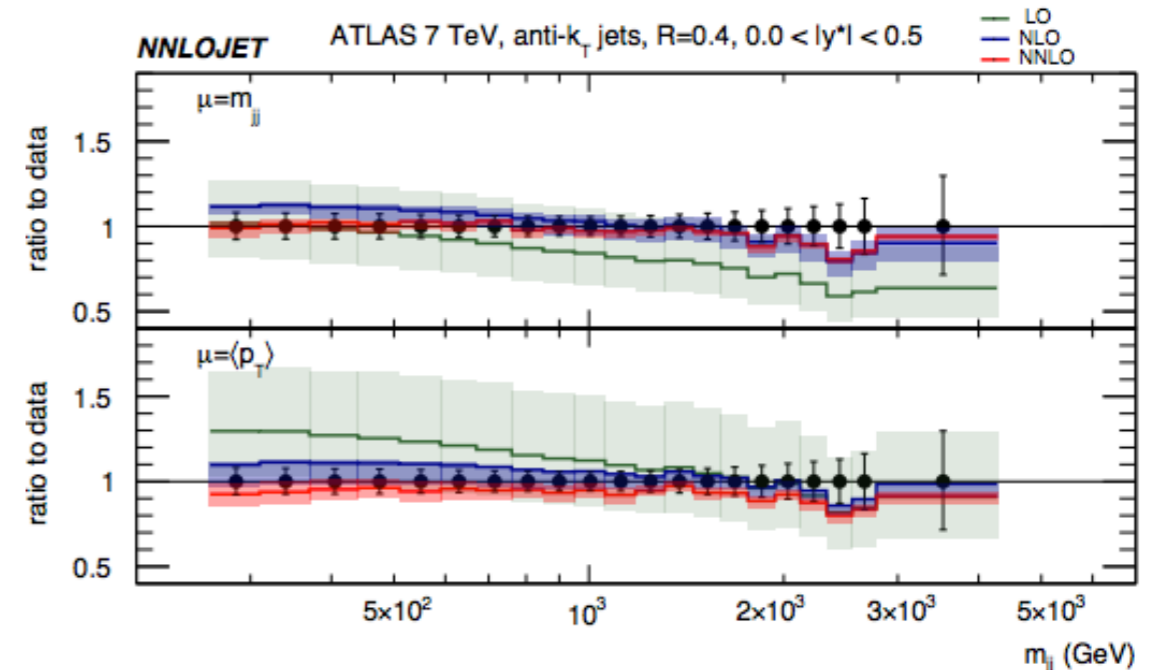
small $|y^*|$:

- both scales give reasonable predictions

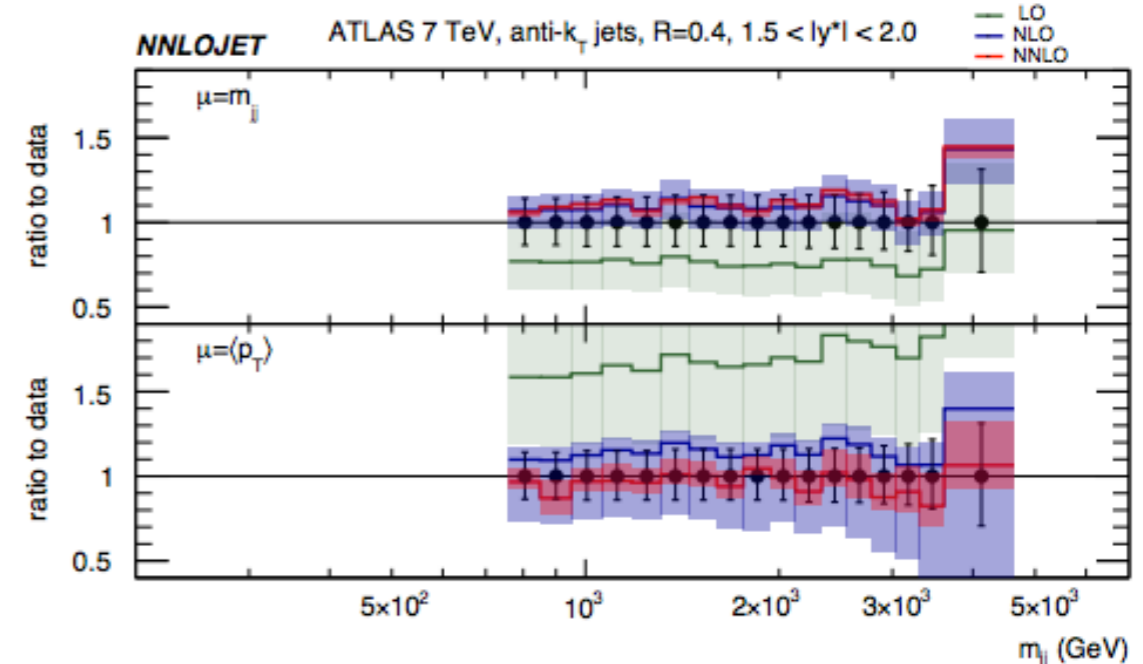
large $|y^*|$:

- large negative NLO corrections, non-overlapping scale bands and residual NLO, NNLO scale uncertainties of $\sim 100\%$, $\sim 20\%$ with $\mu = \langle p_T \rangle$

- stable prediction with $\mu = m_{jj}$**

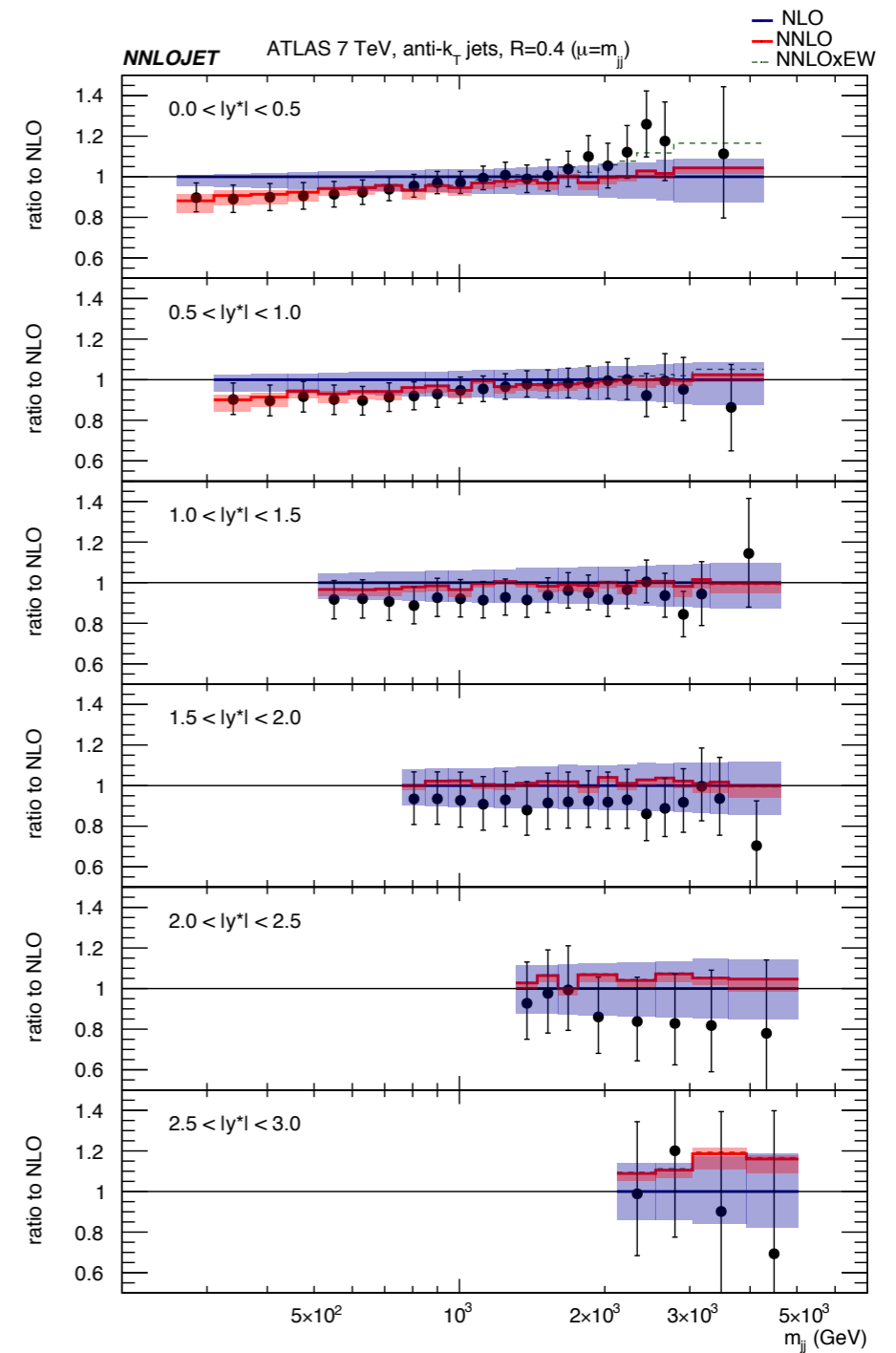
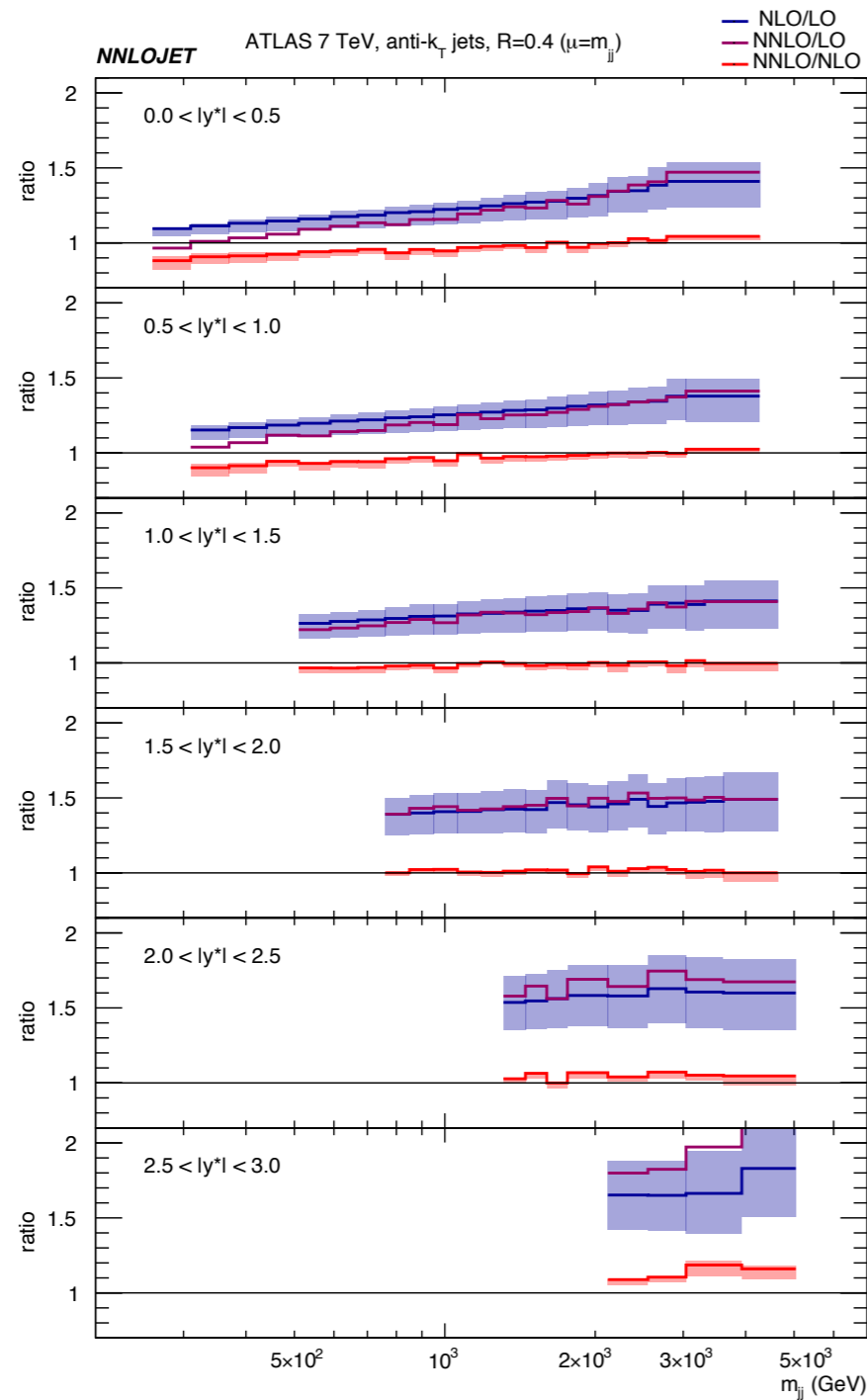


$$0.0 < |y^*| < 0.5$$



$$1.5 < |y^*| < 2.0$$

Dijet inclusive production: $\mu = m_{jj}$



- Excellent convergence of the perturbative expansion; NNLO/NLO < 10% and flat
- **Improved description** of the dijet data at NNLO
- **NNLO: scale choice issue resolved**

Single jet inclusive production

J. Currie, E.W.N. Glover, JP

[arXiv: 1611.01460] Phys. Rev. Lett. 118, 072002 (2017)

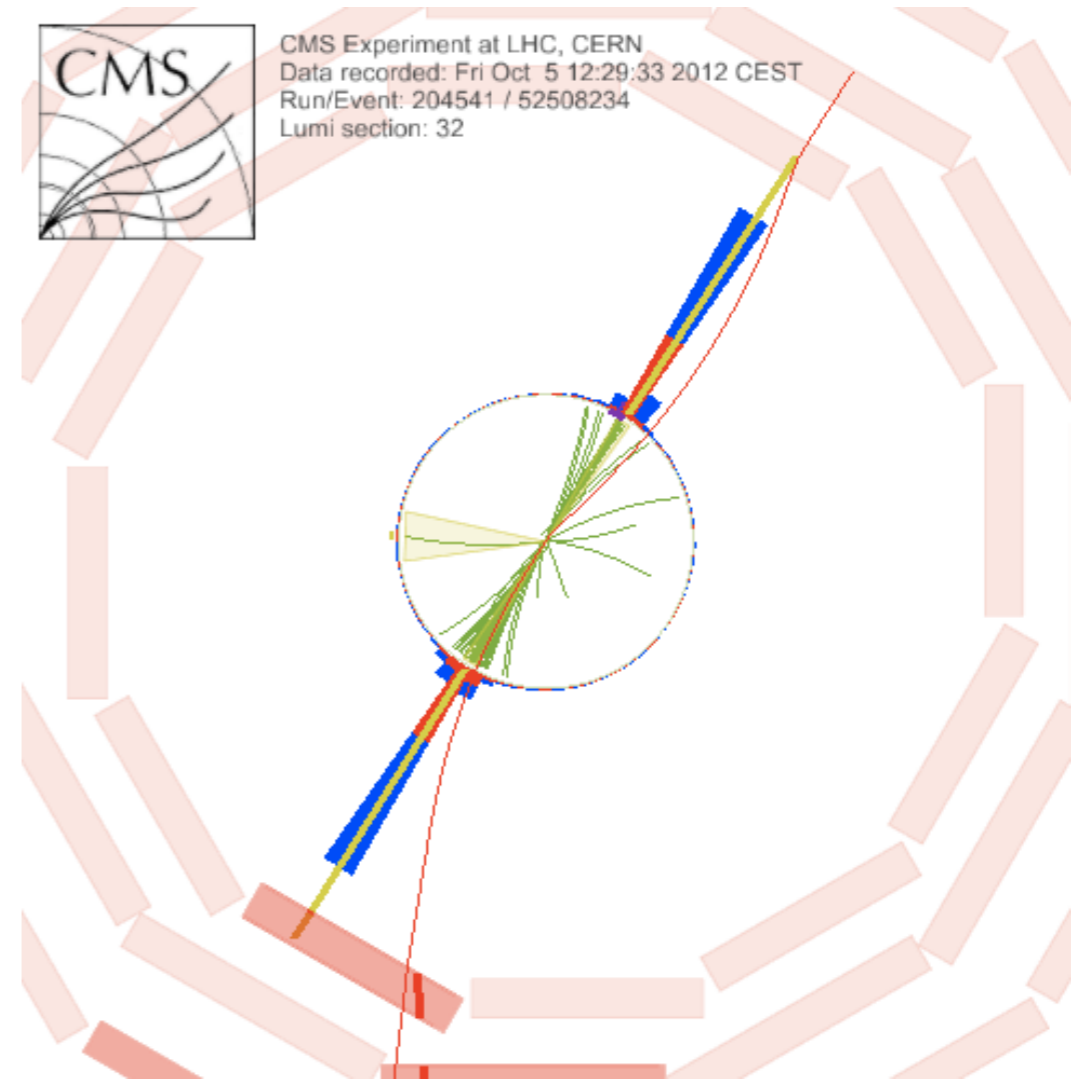
*J. Currie, T. Gehrmann, A. Gehrmann-De Ridder, E.W.N. Glover,
A. Huss, JP [arXiv: 1807.03692]*

Theory setup

- PDF4LHC15nnlo
- anti- k_T jet algorithm
- $R=0.4$; $R=0.7$;
- $p_T > 114$ GeV*
- $|y_j| < 4.7^*$
- theory uncertainty: vary renormalization μ_R
and factorization μ_F scales by factors
[1/2,2] around pre-defined central scale

Comparison to data

- CMS $\sqrt{s} = 13$ TeV ; $L=71$ pb⁻¹
- $R=0.4$ and $R=0.7$



*[CMS, arXiv:1605.04436]
Eur.Phys.J. C76 (2016) no.8, 451*

**single jet inclusive observable obtained by summing over all jets that are observed in the event*

Single jet inclusive production: scale choices μ_R, μ_F

- $p_T \rightarrow$ transverse momentum of the individual jets
- $p_{T1} \rightarrow$ transverse momentum of the leading jet
- $H_T \rightarrow$ scalar sum of the transverse momenta of the reconstructed jets
- $\check{H}_T \rightarrow$ scalar sum of the transverse momenta of all partons
- μ_R, μ_F are arbitrary and unphysical parameters and are absent from the true result \rightarrow *a priori* each scale above is an equally valid scale choice

$$\mu \sim p_T$$
$$\mu \sim p_{T1}$$
$$\mu \sim H_T$$
$$\mu \sim \hat{H}_T$$

However, a suitable scale choice would

- minimize ratios of Q^2/μ^2 , i.e, faster perturbative convergence and smaller scale uncertainties
- avoid scales that introduce pathological behaviours in the prediction, i.e, $\sigma < 0$
- avoid scales that are discontinuous on the phase space of the observable, i.e, no kinks in k-factors

\rightarrow recently derived NNLO predictions for inclusive jet production allow for the first time a robust study on scale setting, making use of the knowledge of three orders in the perturbative expansion of the observable

Individual jet contributions and jet fractions

- Single jet inclusive observable receives contributions from all jets in the event, at $O(\alpha_s^4)$

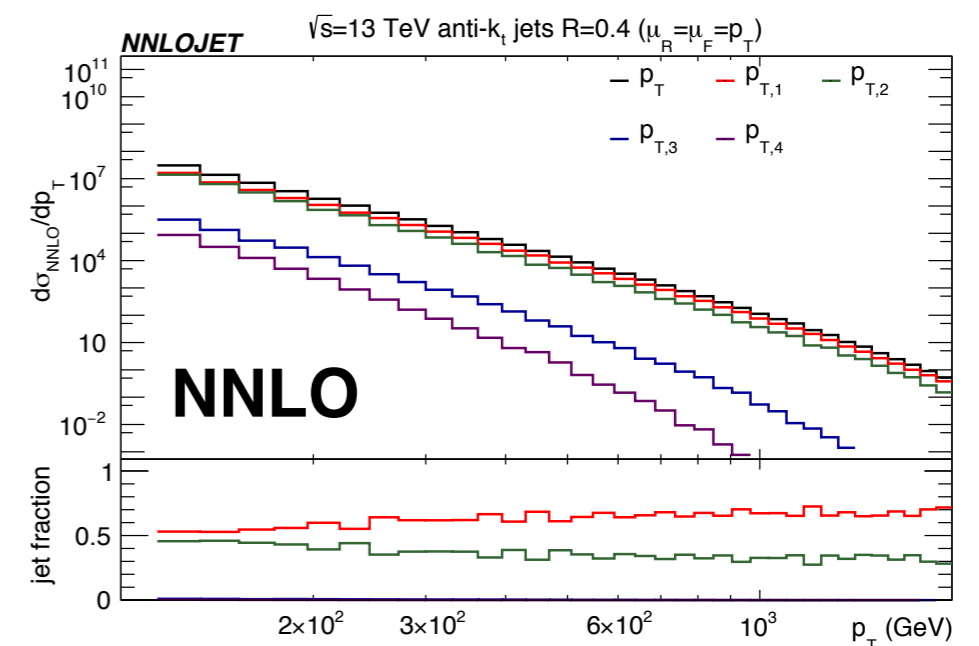
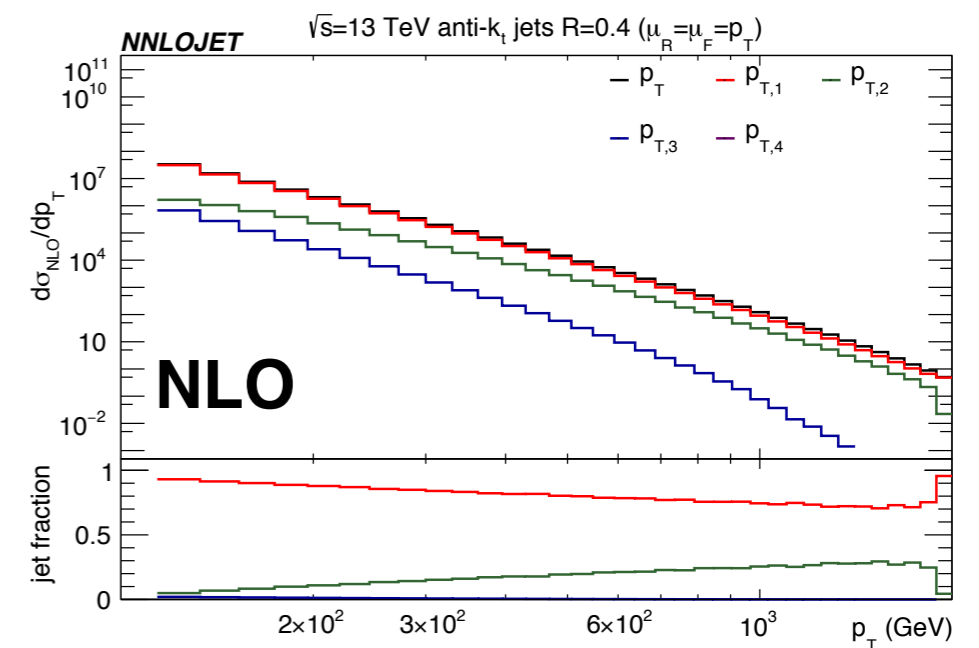
$$\frac{d\sigma}{dp_T}(\mu = p_T) = \frac{d\sigma}{dp_{T1}}(\mu = p_{T1}) + \frac{d\sigma}{dp_{T2}}(\mu = p_{T2}) + \frac{d\sigma}{dp_{T3}}(\mu = p_{T3}) + \frac{d\sigma}{dp_{T4}}(\mu = p_{T4})$$

NLO:

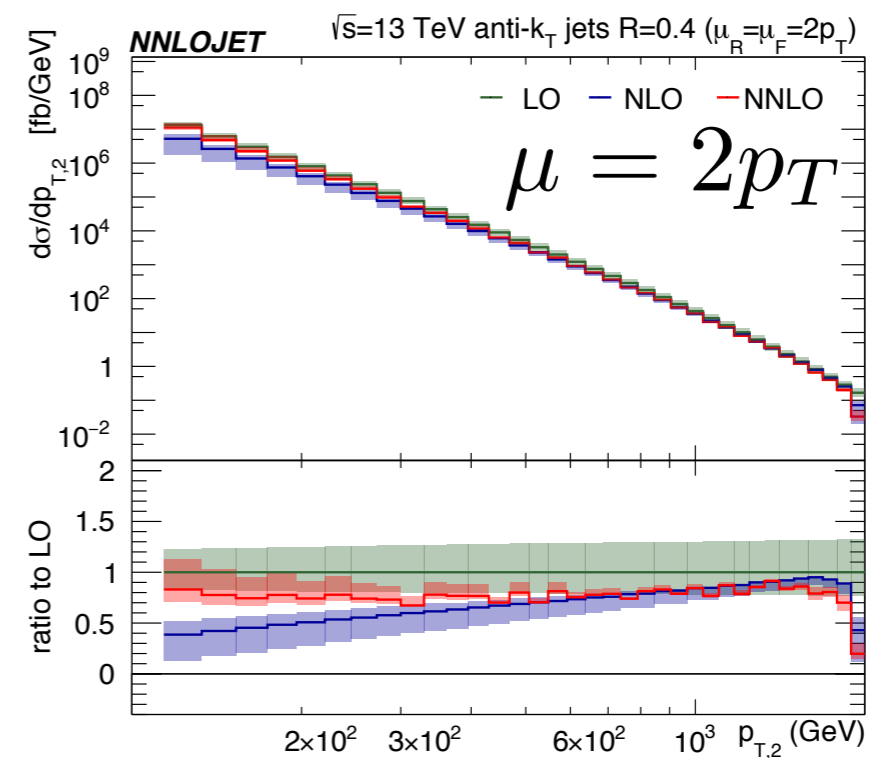
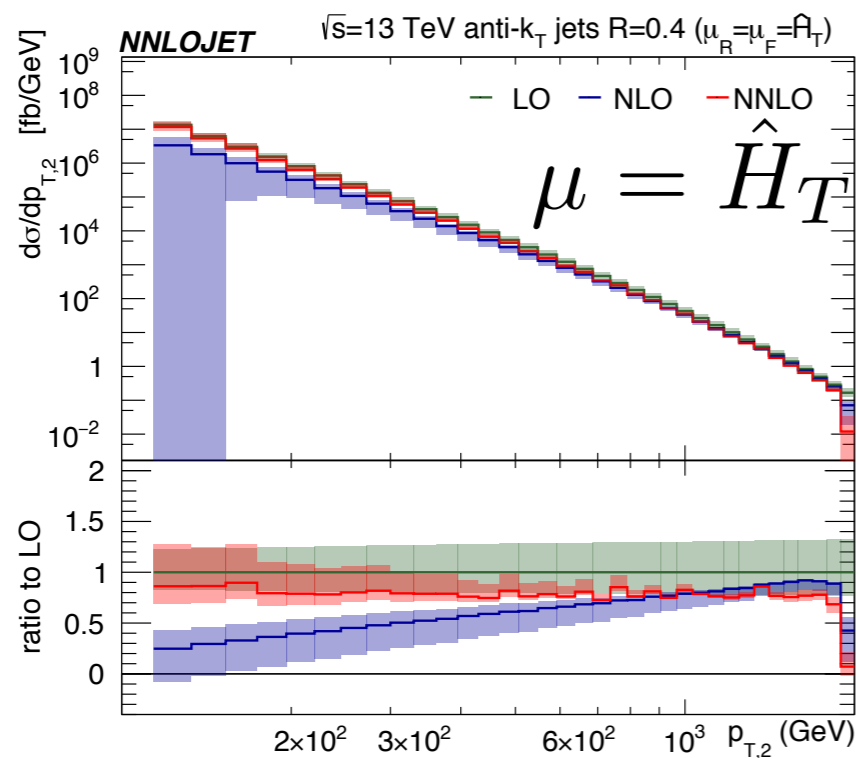
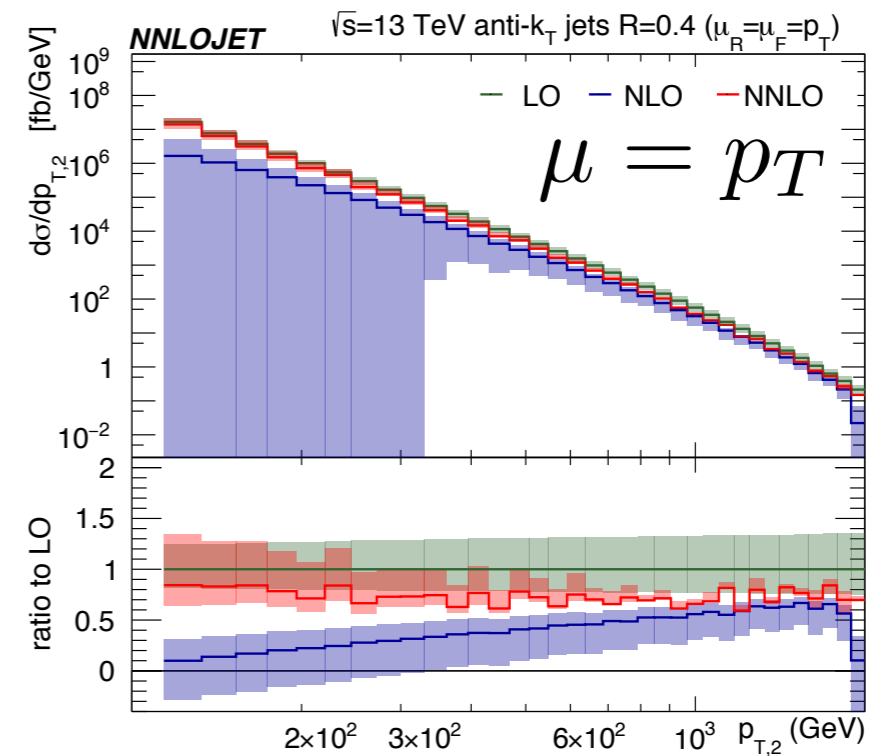
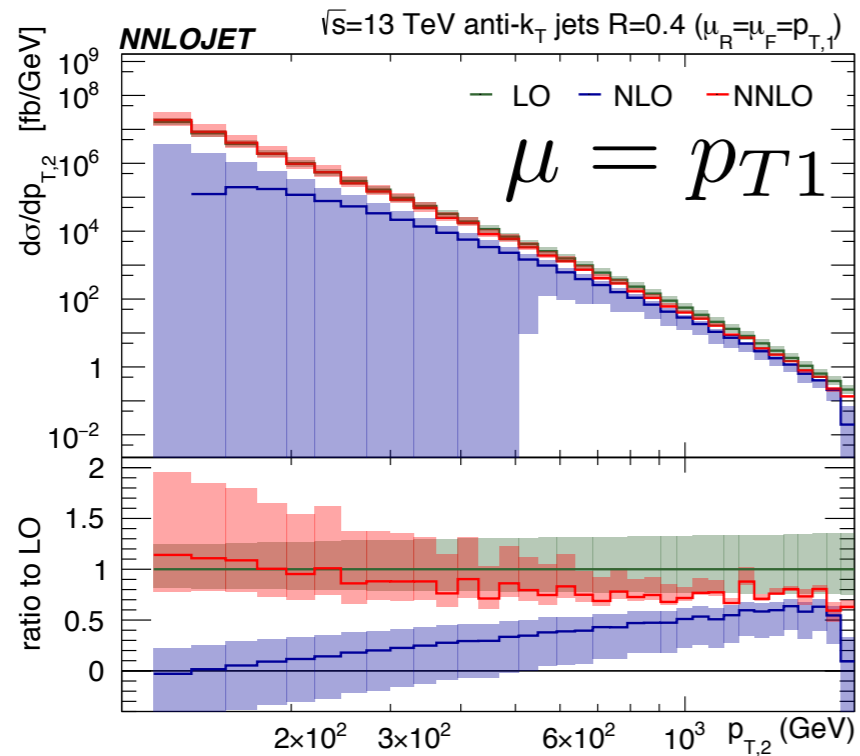
- leading jet dominates
- third jet negligible
- second jet sizeable at high p_T negligible at low p_T

NNLO:

- leading and second jet fractions similar over the whole p_T range
- significant increase in second jet p_T contribution to the inclusive jet sample at NNLO with respect to NLO



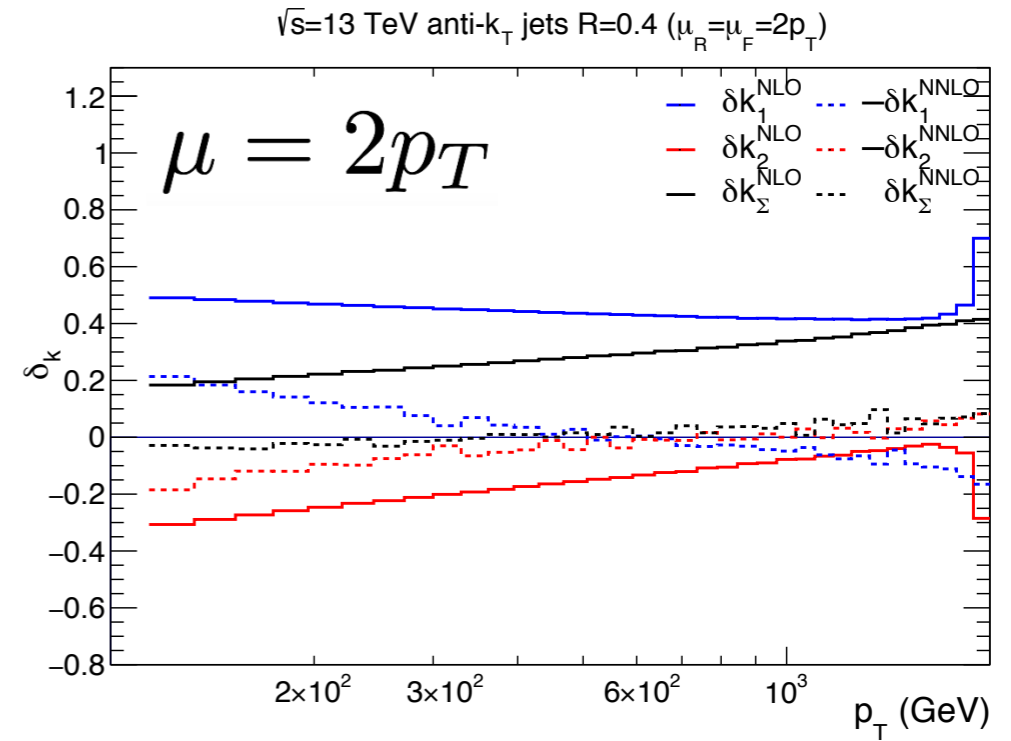
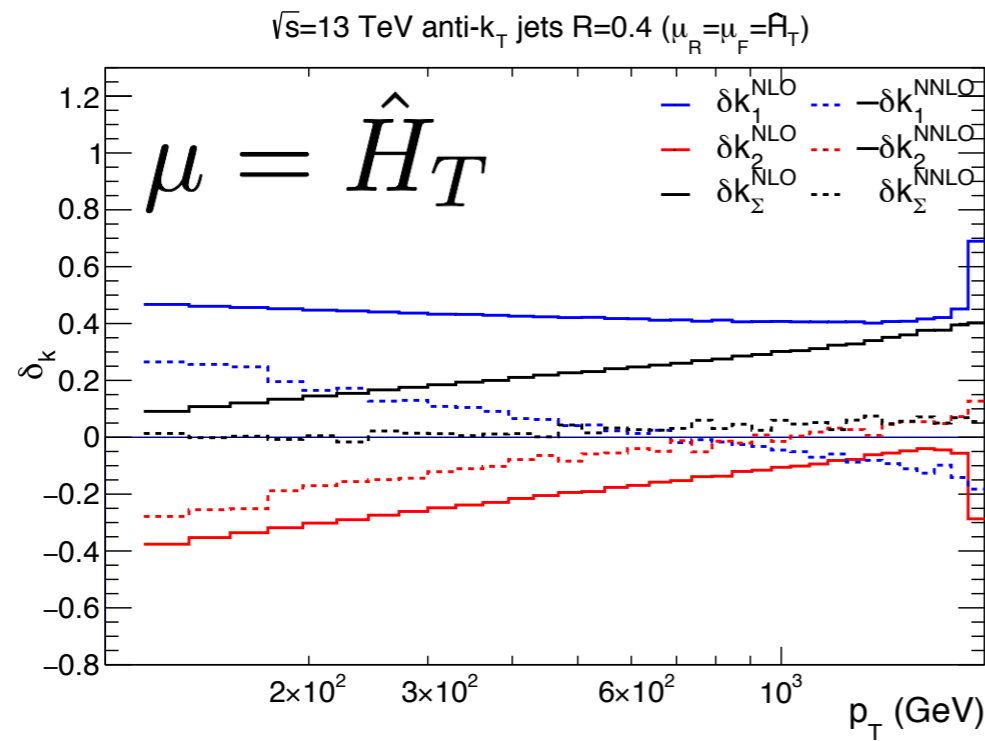
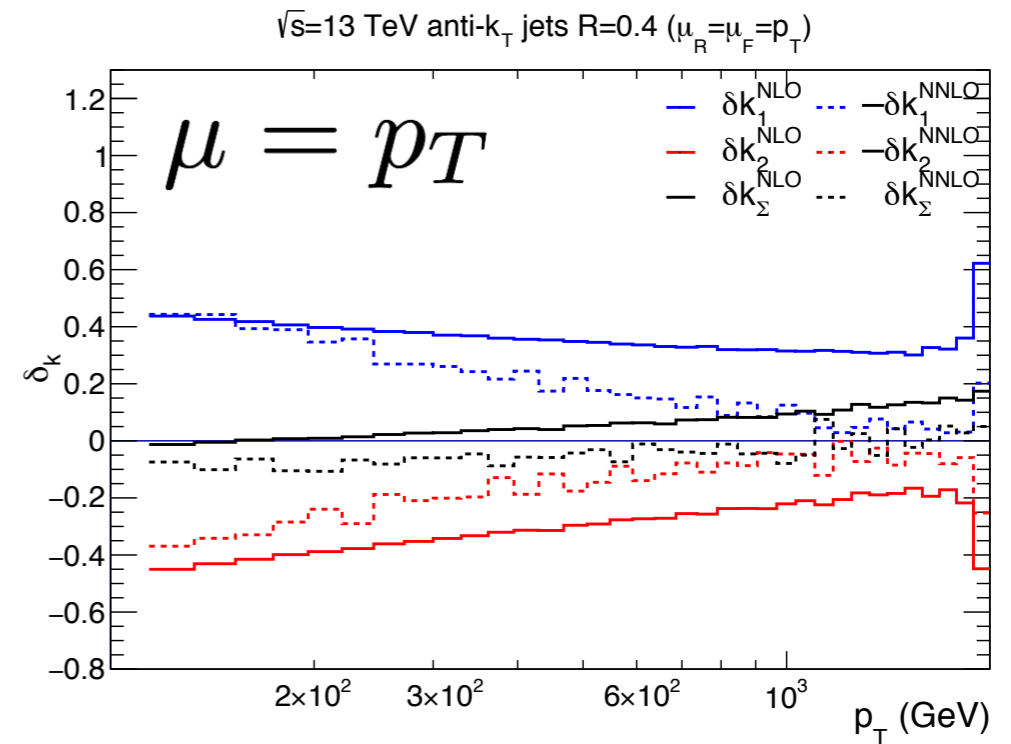
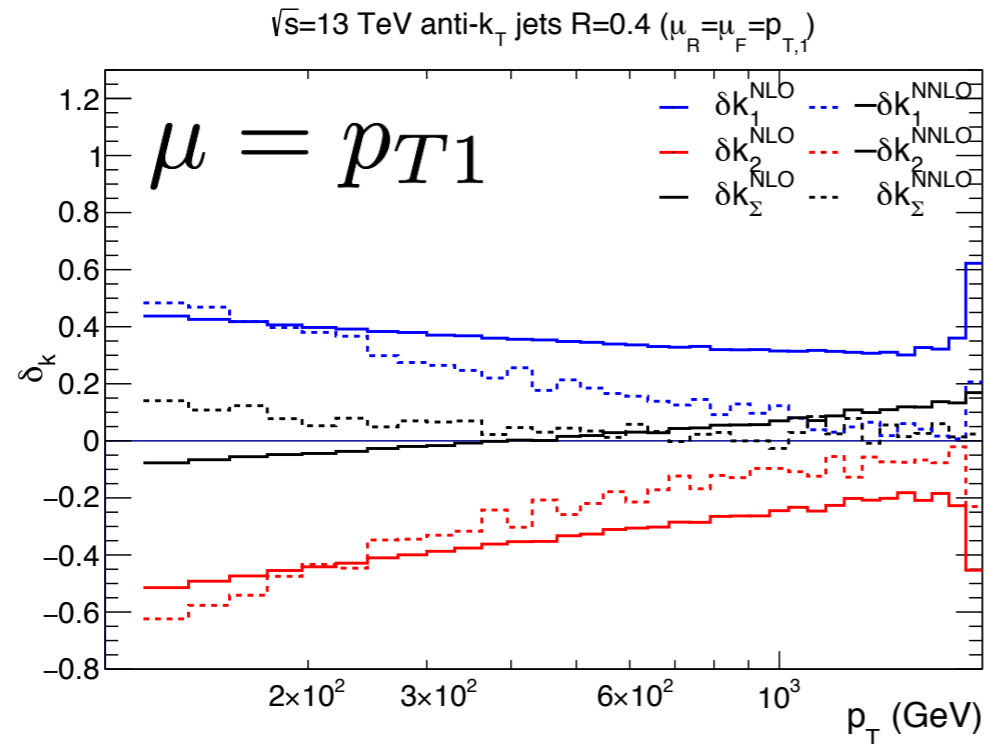
Second jet transverse momentum distribution



Corrections to second jet distribution integrated over rapidity $R=0.4$

- **NLO**: large and negative with huge uncertainty → potentially large logs sensitive on IR effects; NNLO: large and positive
- **Stabilization of the predictions at NNLO** (in line with the LO) → functional form of the scale matters

Differential corrections for leading and subleading jet



- large cancellations between corrections to first (blue) and second jet (red) at NLO (solid), NNLO (dashed)
- smaller perturbative coefficients for $\mu = 2p_T$; $\mu = \hat{H}_T$ for leading and subleading jet

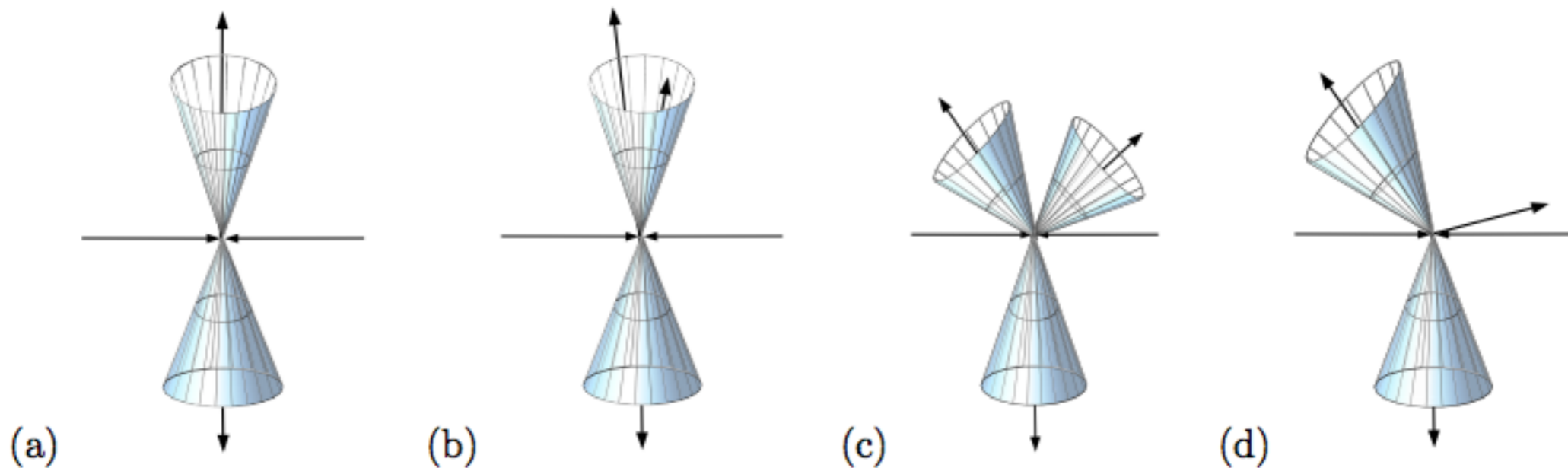
$\mu=p_T$ versus $\mu=p_{T1}$: Similarities and Differences

$p_T=p_{T1}$

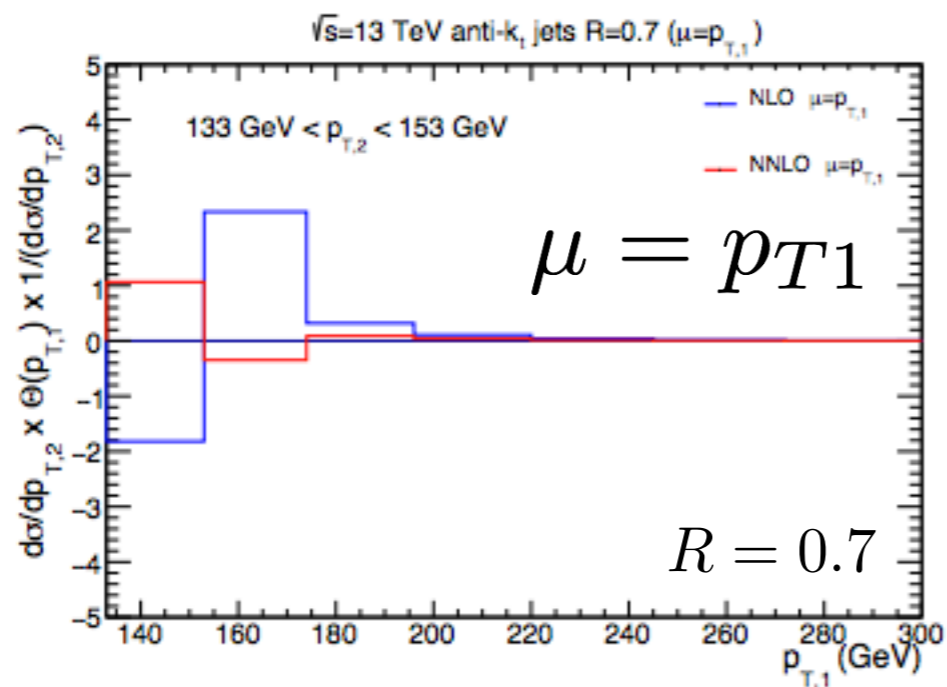
- for leading-order kinematics ($2 \rightarrow 2$ kinematics)
- for high p_T -jets (back to back and balanced in p_T)

$p_T \neq p_{T1}$

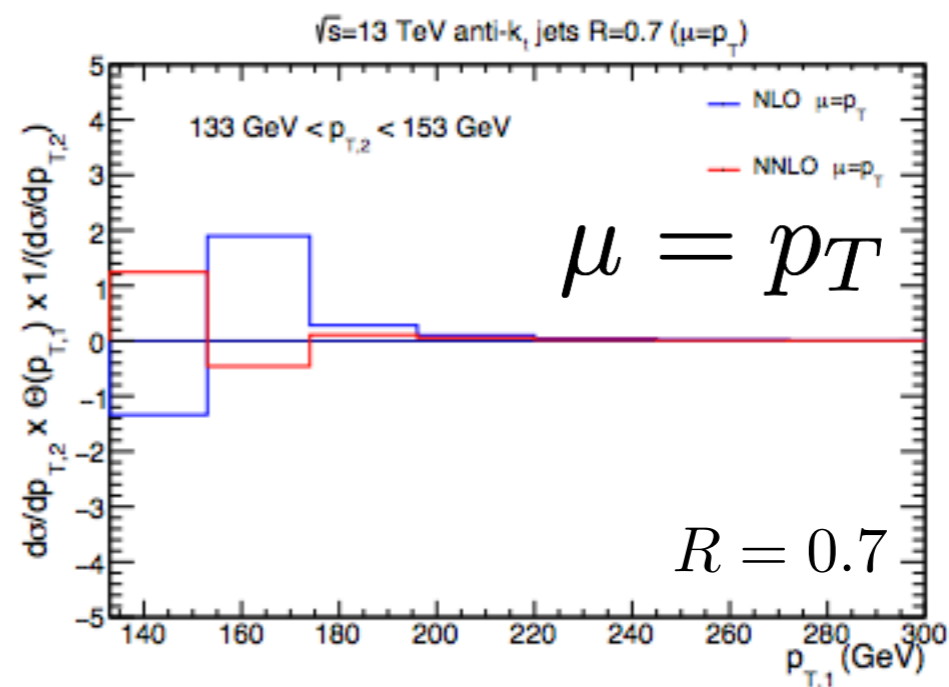
- events with three or more hard jets (small rate as seen before)
- events with jets outside the fiducial cuts (worse for small R)



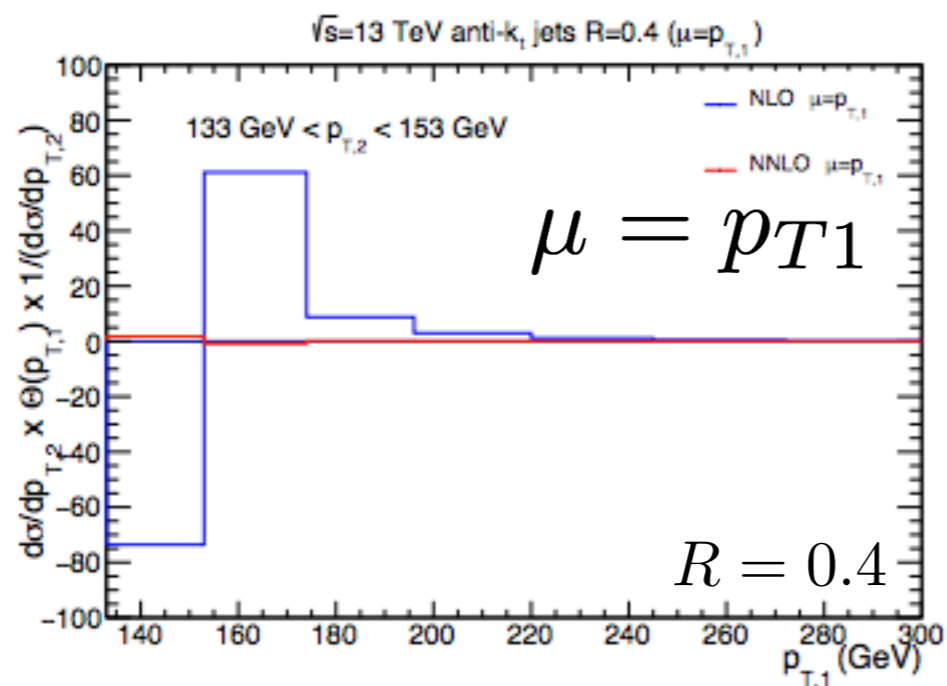
Decomposition of events contributing to a single bin in $p_{T,2}$



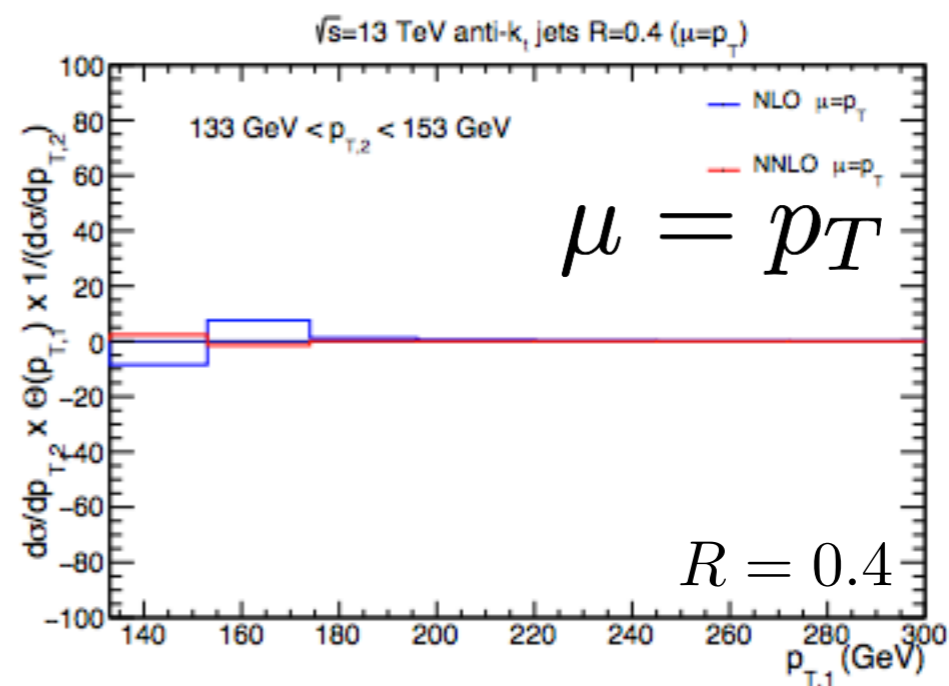
(a)



(b)



(c)



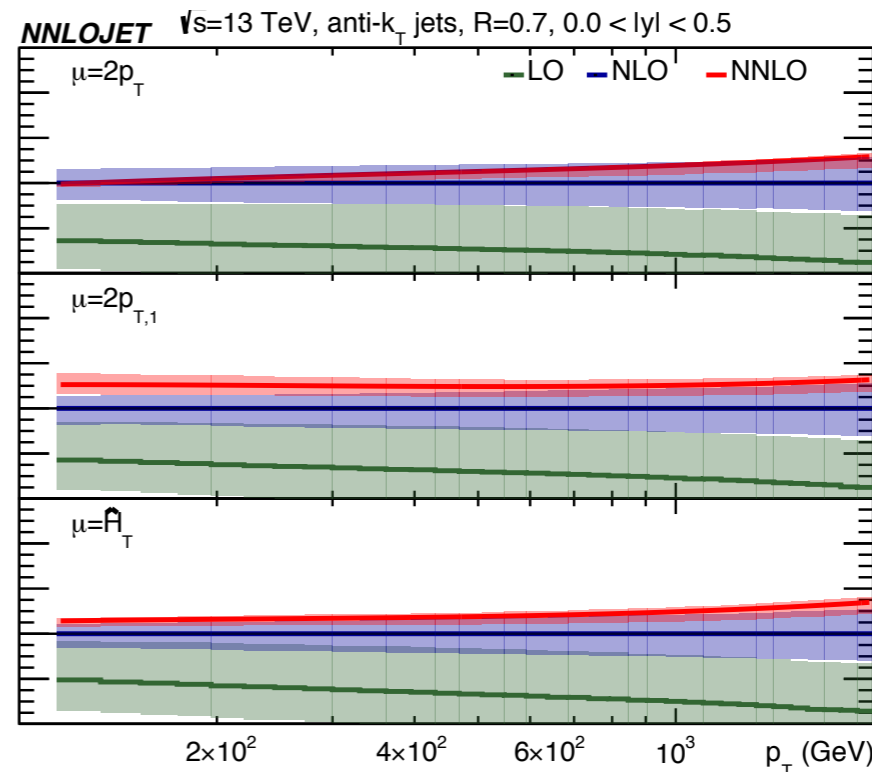
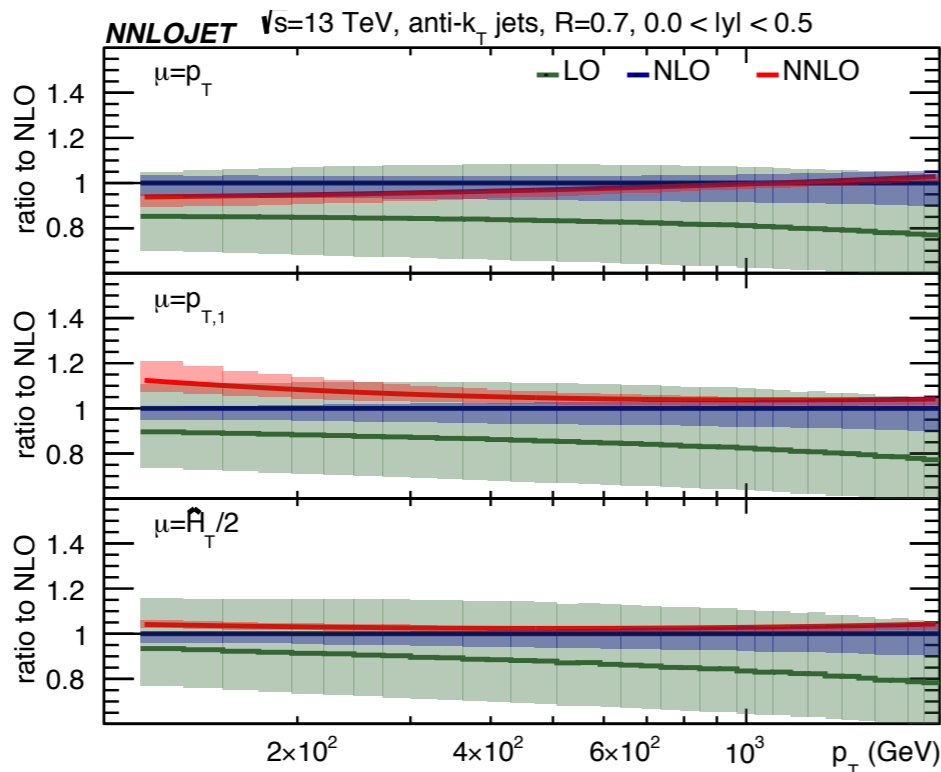
(d)

Large cancellations/imbalance between positive real emission and large negative virtual correction

- worse for $\mu = p_{T,1}$ that changes event-by-event in the distribution; $\mu = p_T$ remains constant

Differential single jet inclusive k-factors CMS cuts

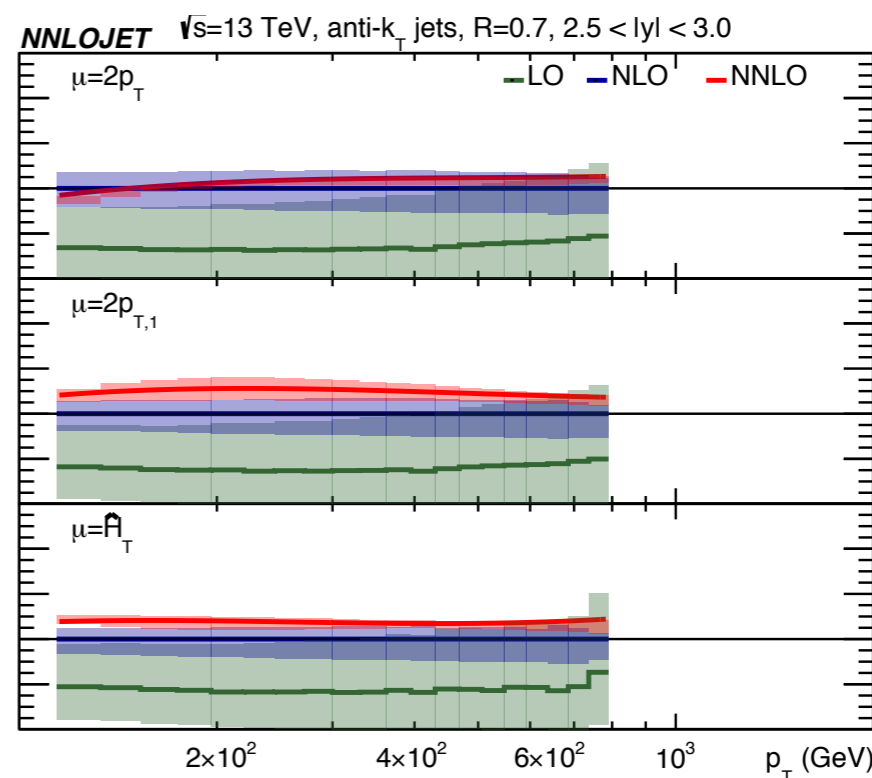
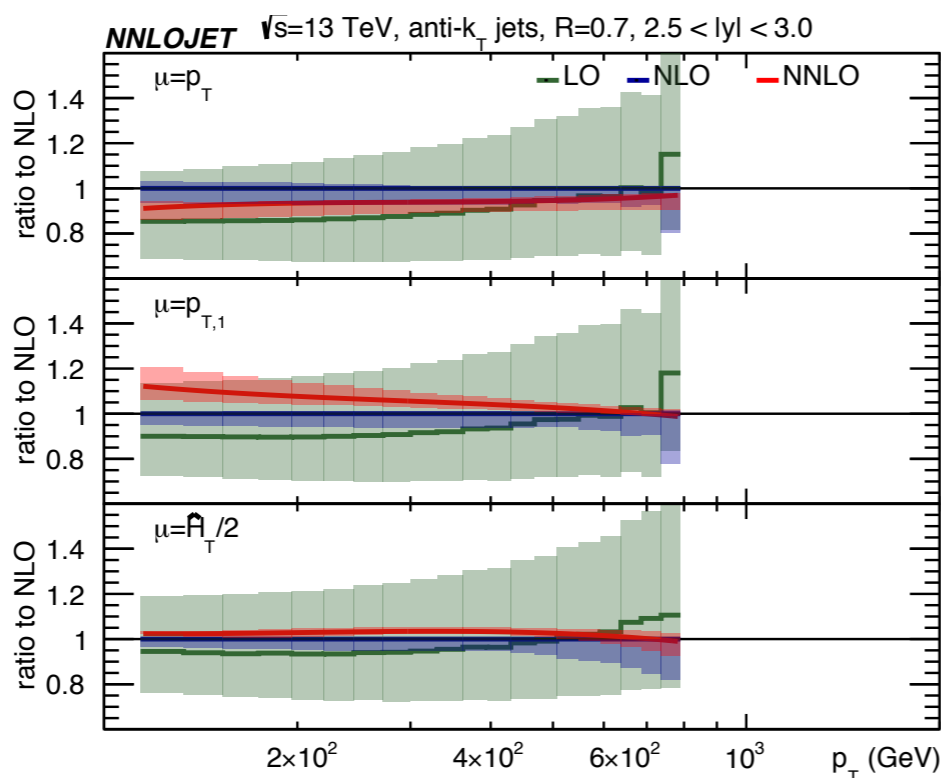
$0.0 < |y| < 0.5$



$\mu = 2p_T$

$\mu = \hat{H}_T$

$2.5 < |y| < 3.0$



$\mu = 2p_T$

$\mu = \hat{H}_T$

- Excellent convergence of the perturbative expansion and overlapping scale uncertainty bands observed for $\mu = 2p_T$ and $\mu = \hat{H}_T$

Define scale choice criteria for single jet inclusive cross section

Studied the IR sensitivity of the different ingredients and introduced an extended set of criteria to help identify the most appropriate scale choice for the perturbative description of single jet inclusive production

- **(a) perturbative convergence:** size of the corrections to the inclusive cross section reduces at each successive order
- **(b) scale uncertainty as theory estimate:** overlapping scale uncertainty bands between the last two orders, i.e., between NLO and NNLO
- **(c) perturbative convergence of the individual jet spectra:** perturbative convergence of the corrections to the individual p_{T1} and p_{T2} distributions
- **(d) stability of the second jet distribution:** require the predictions and associated scale uncertainty to provide physical, positive cross sections

Singled out $\mu = 2p_T$ and $\mu = \hat{H}_T$ as scales that satisfy all the criteria above for both cone sizes $R=0.4$ and $R=0.7 \Rightarrow \mu = p_{T,1}$ **strongly disfavoured**

scale	criterion			
	(a)	(b)	(c)	(d)
$p_{T,1}$	–	–	✓	✓
$2p_{T,1}$	✓	–	✓	✓
p_T	–	✓	✓	✓
$2p_T$	✓	✓	✓	✓
$\hat{H}_T/2$	✓	✓	✓	–
\hat{H}_T	✓	✓	✓	✓

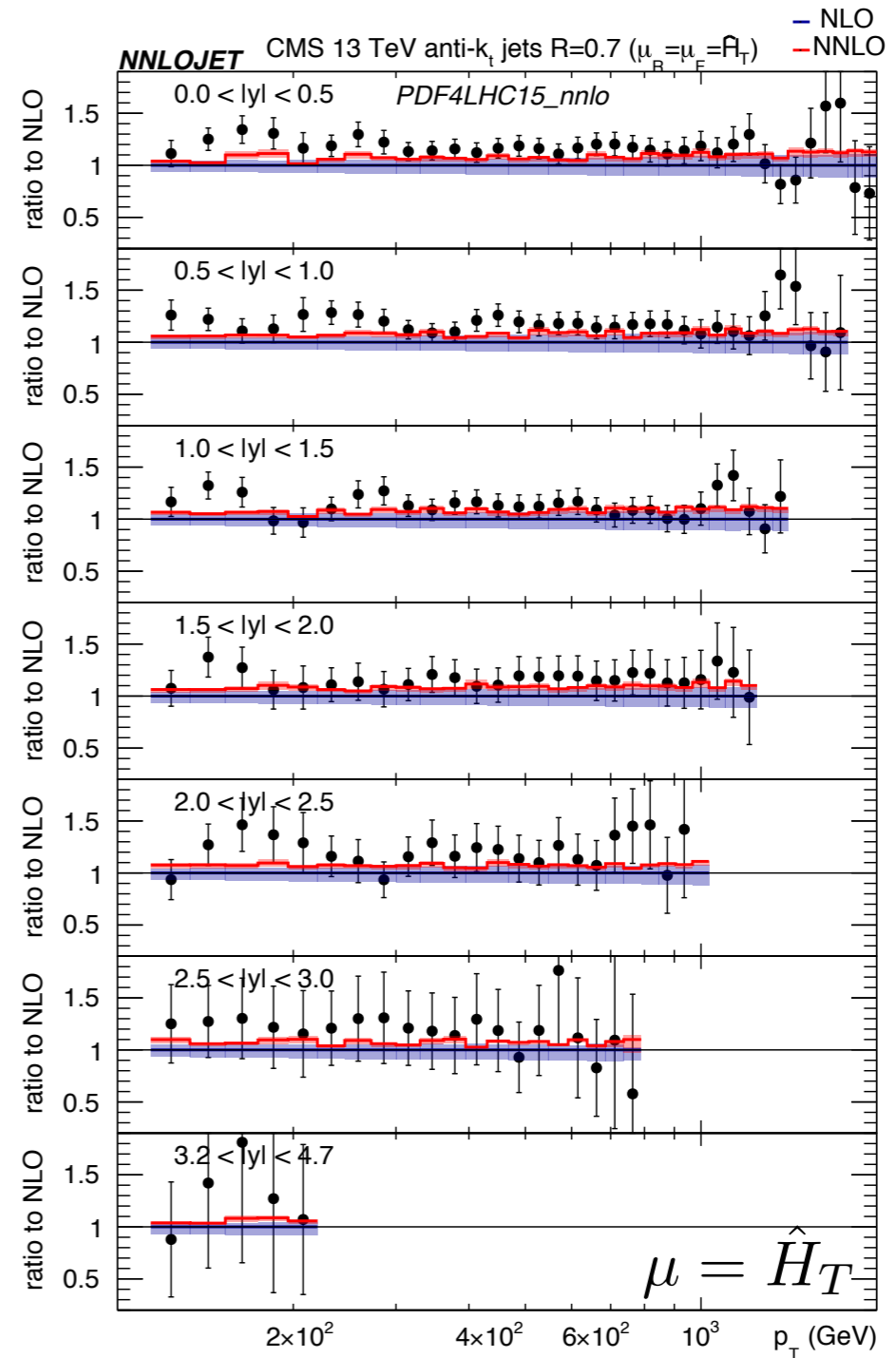
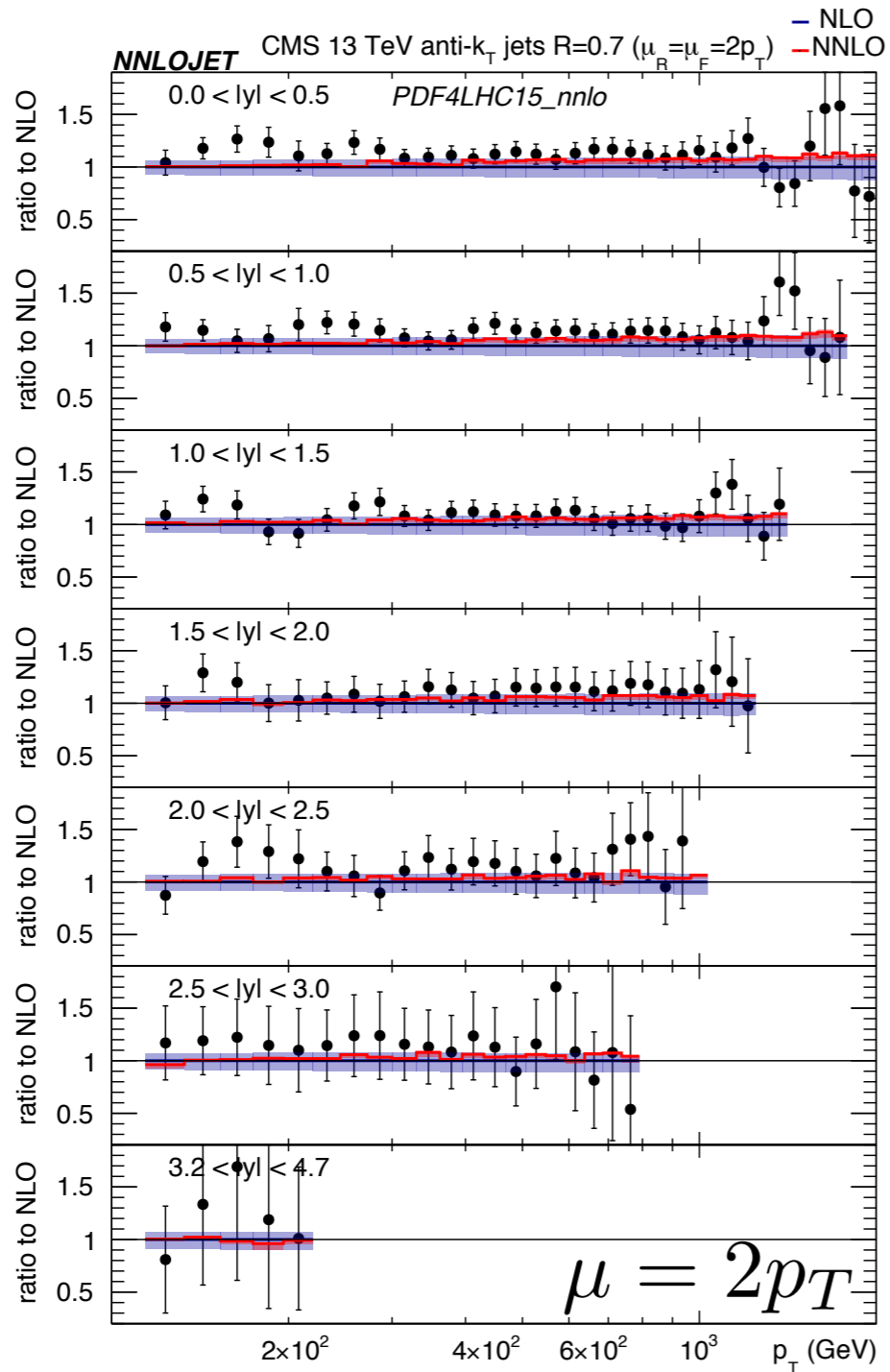
(a) $R = 0.7$

scale	criterion			
	(a)	(b)	(c)	(d)
$p_{T,1}$	–	–	–	–
$2p_{T,1}$	✓	–	✓	(✓)
p_T	–	–	–	–
$2p_T$	✓	✓	✓	✓
$\hat{H}_T/2$	✓	✓	–	–
\hat{H}_T	✓	✓	✓	(✓)

(b) $R = 0.4$

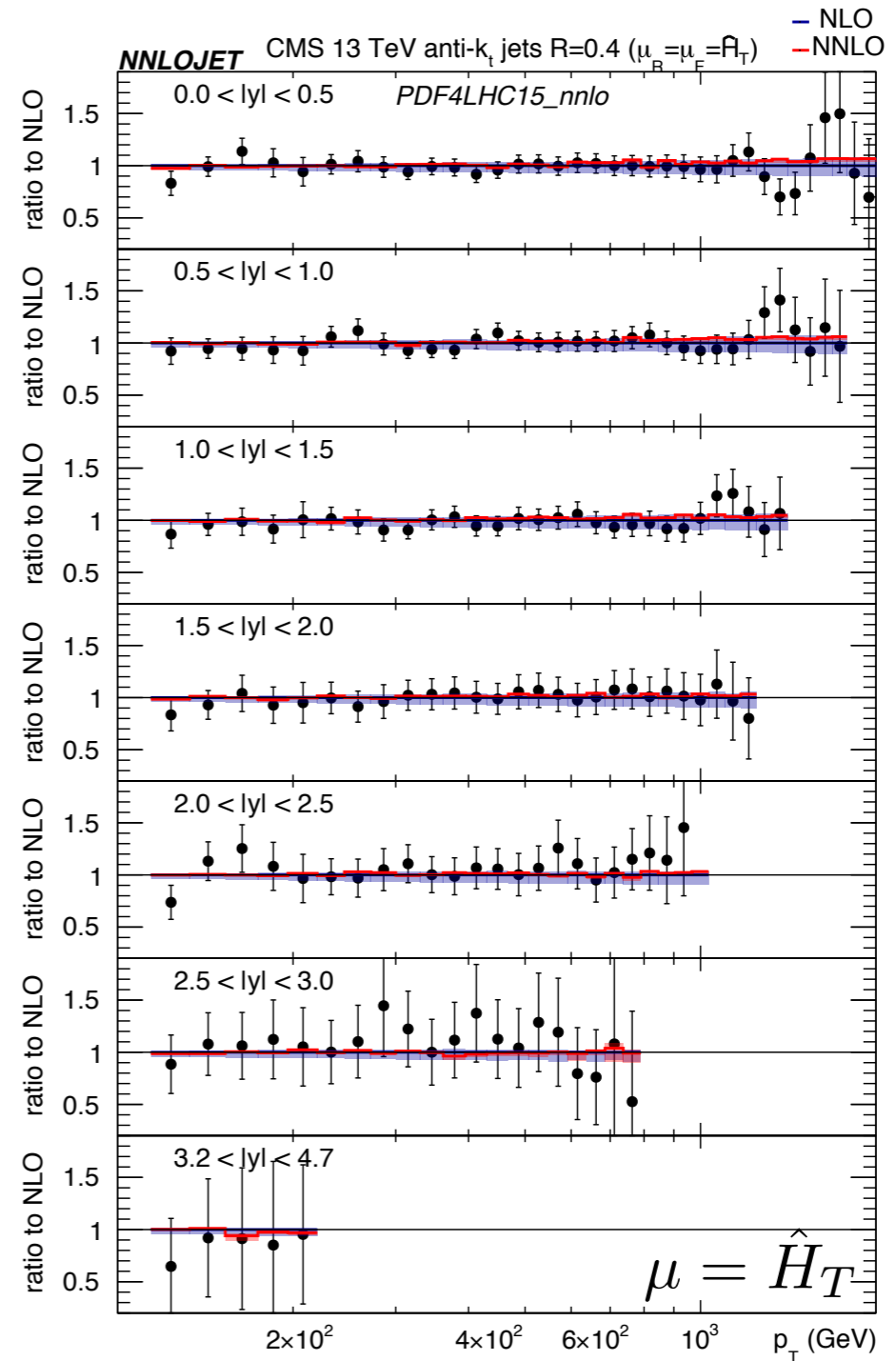
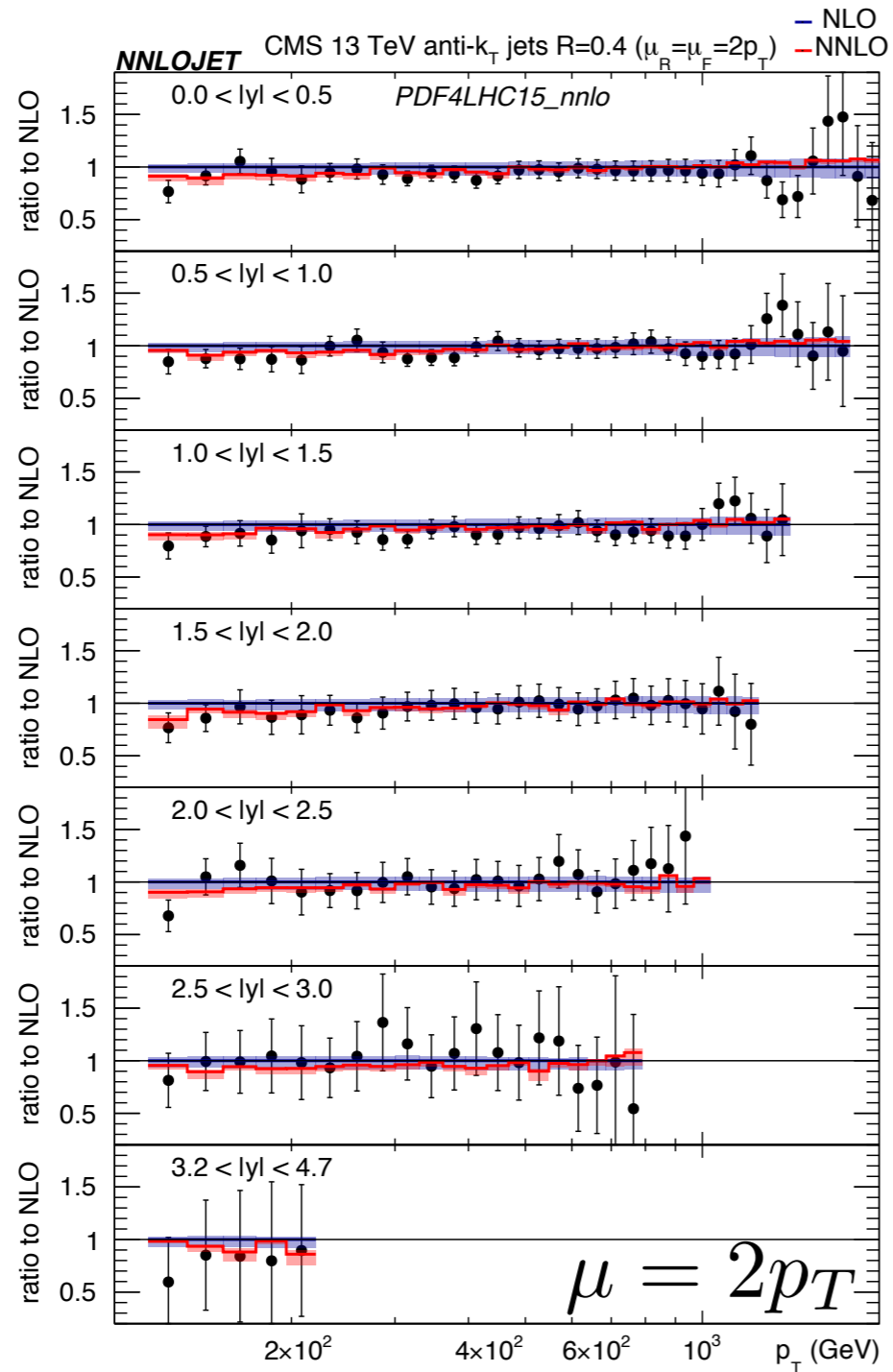
Table 2: Summary of scales vs. criteria for (a) $R=0.7$ and (b) $R=0.4$ cone sizes.

Comparison with LHC CMS data R=0.7



- **small positive NNLO corrections improve** the **agreement** with CMS data with respect to NLO
- **significant reduction in scale uncertainty** from **NLO** to **NNLO** → roughly more than a factor of 2 in a wide range of p_T and rapidity

Comparison with LHC CMS data R=0.4



- improved agreement with data at NNLO with respect to NLO
- both scale choices are stable and provide reasonable predictions for R=0.7 and R=0.4

Summary/Outlook

Summary:

- Significant theoretical progress in the description of inclusive jet and dijet production at the LHC
- Theoretical developments driven by the increase in precision of the experimental measurements
- New theoretical calculations available that can be used to understand the impact of the effects of higher order corrections in the description of jet data at hadron colliders

Outlook

- Perform further quantitative comparisons between data and theory (different energies, covering wide jet p_T and rapidity and jet cone sizes)
- Use new data to understand effects in tuning of hadronization and underlying event parameters and respective uncertainties
- Extend existing phenomenological predictions to triple-differential measurements and angular observables and jet shapes
- Study sensitivity of jet-based observables to α_s and PDF extractions and assess ultimate reach in precision in a combined fit