

The SMEFTsim package

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The SMEFTsim package: purpose

have a UFO & FeynRules tool with:

1. the complete Warsaw basis for 3 generations , including all complex phases and ~~CP~~ terms
2. automatic implementation of field redefinitions to have canonical kinetic terms
3. automatic implementation of parameters shifts due to the choice of an input parameters set

→ a Lagrangian that can be directly used for phenomenology:

- ▶ analytic computations in FeynRules/FeynArts/FormCalc
- ▶ montecarlo generation in MadGraph5

Main scope:

estimate **tree-level interference** terms between SM and $d = 6$ corrections

→ accuracy \sim %

More in detail: field redefinitions

Gauge bosons

$$\begin{aligned}\mathcal{L}_{\text{SMEFT}} \supset & -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}W_{\mu\nu}^I W^{I\mu\nu} - \frac{1}{4}G_{\mu\nu}^a G^{a\mu\nu} + \\ & + C_{HB}(H^\dagger H)B_{\mu\nu}B^{\mu\nu} + C_{HW}(H^\dagger H)W_{\mu\nu}^I W^{I\mu\nu} + C_{HWB}(H^\dagger \sigma^I H)W_{\mu\nu}^I B^{\mu\nu} \\ & + C_{HG}(H^\dagger H)G_{\mu\nu}^a G^{a\mu\nu}\end{aligned}$$

to have **canonically normalized kinetic terms** we need to

1. redefine fields and couplings keeping (gV_μ) unchanged:

$$\begin{aligned}B_\mu &\rightarrow B_\mu(1 + C_{HB}v^2) & g_1 &\rightarrow g_1(1 - C_{HB}v^2) \\ \mathcal{W}_\mu^I &\rightarrow \mathcal{W}_\mu^I(1 + C_{HW}v^2) & g_2 &\rightarrow g_2(1 - C_{HW}v^2) \\ \mathcal{G}_\mu^a &\rightarrow \mathcal{G}_\mu^a(1 + C_{HG}v^2) & g_s &\rightarrow g_s(1 - C_{HG}v^2)\end{aligned}$$

2. correct the rotation to mass eigenstates:

$$\begin{pmatrix} \mathcal{W}_\mu^3 \\ \mathcal{B}_\mu \end{pmatrix} = \begin{pmatrix} 1 & -v^2 C_{HWB}/2 \\ -v^2 C_{HWB}/2 & 1 \end{pmatrix} \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} Z_\mu \\ A_\mu \end{pmatrix}$$

(equivalent to a shift of the Weinberg angle)

More in detail: field redefinitions

Higgs

$$\mathcal{L}_{\text{SMEFT}} \supset \frac{1}{2} D_\mu H^\dagger D^\mu H + C_{H\Box} (H^\dagger H) (\Box H) + C_{HD} (H^\dagger D_\mu H)^* (\Box H)$$

to have a canonically normalized kinetic term, in unitary gauge, we need to replace

$$h \rightarrow h \left(1 + v^2 C_{H\Box} - \frac{v^2}{4} C_{HD} \right)$$

More in detail: field redefinitions

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These redefinitions are embedded by default in the SMEFTsim models

More in detail: parameter shifts from input choice

SM case.

Parameters in the canonically normalized Lagrangian : $\bar{v}, \bar{g}_1, \bar{g}_2, s_{\bar{\theta}}$

The values can be inferred from the measurements e.g. of $\{\alpha_{\text{em}}, m_Z, G_f\}$:

$$\alpha_{\text{em}} = \frac{\bar{g}_1 \bar{g}_2}{\bar{g}_1^2 + \bar{g}_2^2}$$
$$m_Z = \frac{\bar{g}_2 \bar{v}}{2c_{\bar{\theta}}}$$
$$G_f = \frac{1}{\sqrt{2}\bar{v}^2}$$

→

$$\hat{v}^2 = \frac{1}{\sqrt{2}G_f}$$
$$\sin \hat{\theta}^2 = \frac{1}{2} \left(1 - \sqrt{1 - \frac{4\pi\alpha_{\text{em}}}{\sqrt{2}G_f m_Z^2}} \right)$$
$$\hat{g}_1 = \frac{\sqrt{4\pi\alpha_{\text{em}}}}{\cos \hat{\theta}}$$
$$\hat{g}_2 = \frac{\sqrt{4\pi\alpha_{\text{em}}}}{\sin \hat{\theta}}$$

in the SM at tree-level $\bar{k} = \hat{k}$

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$$\alpha_{\text{em}} = \frac{\bar{g}_1 \bar{g}_2}{\bar{g}_1^2 + \bar{g}_2^2} \left[1 + \bar{v}^2 C_{HWB} \frac{\bar{g}_2^3 / \bar{g}_1}{\bar{g}_1^2 + \bar{g}_2^2} \right]$$

$$m_Z = \frac{\bar{g}_2 \bar{v}}{2c_{\bar{\theta}}} + \delta m_Z(C_i) \quad \rightarrow$$

$$G_f = \frac{1}{\sqrt{2}\bar{v}^2} + \delta G_f(C_i)$$

$$\hat{v}^2 = \frac{1}{\sqrt{2}G_f}$$

$$\sin \hat{\theta}^2 = \frac{1}{2} \left(1 - \sqrt{1 - \frac{4\pi\alpha_{\text{em}}}{\sqrt{2}G_f m_Z^2}} \right)$$

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$$\hat{g}_2 = \frac{\sqrt{4\pi\alpha_{\text{em}}}}{\sin \hat{\theta}}$$

in the SM at tree-level $\bar{\kappa} = \hat{\kappa}$

in the SMEFT $\bar{\kappa} = \hat{\kappa} + \delta\kappa(C_i)$

More in detail: parameter shifts from input choice

To have numerical predictions it is necessary to replace $\bar{\kappa} \rightarrow \hat{\kappa} + \delta\kappa(C_i)$ for all the parameters in the Lagrangian.

$\{\alpha_{\text{em}}, m_Z, G_f\}$ scheme

$$\delta m_Z^2 = m_Z^2 \hat{v}^2 \left(\frac{c_{HD}}{2} + 2c_{\hat{\theta}} s_{\hat{\theta}} c_{HWB} \right)$$

$$\delta G_f = \frac{\hat{v}^2}{\sqrt{2}} \left((c_{HI}^{(3)})_{11} + (c_{HI}^{(3)})_{22} - (c_{II})_{1221} \right)$$

$$\delta g_1 = \frac{s_{\hat{\theta}}^2}{2(1-2s_{\hat{\theta}}^2)} \left(\sqrt{2}\delta G_f + \delta m_Z^2/m_Z^2 + 2\frac{c_{\hat{\theta}}^3}{s_{\hat{\theta}}} c_{HWB} \hat{v}^2 \right)$$

$$\delta g_2 = -\frac{c_{\hat{\theta}}^2}{2(1-2s_{\hat{\theta}}^2)} \left(\sqrt{2}\delta G_f + \delta m_Z^2/m_Z^2 + 2\frac{s_{\hat{\theta}}^3}{c_{\hat{\theta}}} c_{HWB} \hat{v}^2 \right)$$

$$\delta s_{\hat{\theta}}^2 = 2c_{\hat{\theta}}^2 s_{\hat{\theta}}^2 (\delta g_1 - \delta g_2) + c_{\hat{\theta}} s_{\hat{\theta}} (1 - 2s_{\hat{\theta}}^2) c_{HWB} \hat{v}^2$$

$$\delta m_h^2 = m_h^2 \hat{v}^2 \left(2c_{H\Box} - \frac{c_{HD}}{2} - \frac{3c_H}{2\lambda m} \right)$$

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$$\delta m_h^2 = m_h^2 \hat{v}^2 \left(2c_{H\Box} - \frac{c_{HD}}{2} - \frac{3c_H}{2\lambda m} \right)$$

the redefinitions $\bar{\kappa} \rightarrow \hat{\kappa} + \delta\kappa$
are performed automatically
in the Lagrangian
(both schemes)

Numerical inputs chosen

Input parameters	Value	Ref.
$\hat{\alpha}_{ew}(m_Z)$		1/127.950 PDG 2016, 1203.5425
\hat{m}_W	GeV	80.365 ± 0.016 TeVatron: 1307.7627
\hat{m}_Z	GeV	91.1876 ± 0.0021 PDG 2016, hep-ex/0509008,1203.5425
\hat{G}_F	GeV^{-2}	$1.1663787(6) \times 10^{-5}$ PDG 2016, 1203.5425
\hat{m}_h	GeV	$125.09 \pm 0.21 \pm 0.11$ 1503.07589
$\hat{\alpha}_s(m_Z)$	GeV	0.1185 ± 0.0011 PDG 2016
\hat{m}_e	GeV	$0.5109989461(31) \times 10^{-3}$ PDG 2016
\hat{m}_μ	GeV	$105.6583745(24) \times 10^{-3}$ PDG 2016
\hat{m}_τ	GeV	1.77686 ± 0.00012 PDG 2016
\hat{m}_u	GeV	$2.2^{+0.6}_{-0.4} \times 10^{-3}$ PDG 2016
\hat{m}_c	GeV	1.28 ± 0.03 PDG 2016
\hat{m}_t	GeV	$173.21 \pm 0.51 \pm 0.71$ PDG 2016
\hat{m}_d	GeV	$4.7^{+0.5}_{-0.4} \times 10^{-3}$ PDG 2016
\hat{m}_s	GeV	$0.096^{+0.008}_{-0.004}$ PDG 2016
\hat{m}_b	GeV	$4.18^{+0.04}_{-0.03}$ PDG 2016
CKM: λ		0.22506 PDG 2016
A		0.811 PDG 2016
ρ		0.124 PDG 2016
η		0.356 PDG 2016

Implemented frameworks

We implemented **6** different frameworks:

$$3 \text{ flavor structures} \left\{ \begin{array}{l} \text{general} \\ U(3)^5 \text{ symmetric} \\ \text{linear MFV} \end{array} \right. \times 2 \text{ input schemes} \left\{ \begin{array}{l} \hat{\alpha}_{\text{em}}, \hat{m}_Z, \hat{G}_f \\ \hat{m}_W, \hat{m}_Z, \hat{G}_f \end{array} \right.$$

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completely general flavor indices:

2499 parameters including all complex phases

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assume an **exact flavor symmetry**

$$U(3)^5 = U(3)_q \times U(3)_u \times U(3)_d \times U(3)_l \times U(3)_e$$

under which: $\psi \mapsto U_\psi \psi$ for $\psi = \{u, d, q, l, e\}$

► The Yukawas are the only **spurions** breaking the symmetry:

$$Y_u \mapsto U_u Y_u U_q^\dagger \quad Y_d \mapsto U_d Y_d U_q^\dagger \quad Y_l \mapsto U_e Y_l U_l^\dagger.$$

► flavor indices contractions are fixed by the symmetry \rightarrow less parameters

Examples:

$$Q_{Hu} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{u}_r \gamma^\mu u_s) \delta_{rs}$$

$$Q_{eB} = B_{\mu\nu} (\bar{l}_r H \sigma^{\mu\nu} e_s) (\mathbf{Y}_l)_{rs}$$

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assume $U(3)^5$ symmetry + CKM only source of ~~CP~~

- ▶ all Wilson coefficients $\in \mathbb{R}$
- ▶ CP odd bosonic operators are absent ($\propto J_{CP} \simeq 10^{-5}$)
- ▶ includes the first order in flavor violation expansion. E.g.:

$$\mathcal{Q}_{Hu} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}_r \gamma^\mu u_s) [\mathbb{1} + (\mathbf{Y}_u \mathbf{Y}_u^\dagger)]_{rs}$$

$$\mathcal{Q}_{Hq}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{q}_r \gamma^\mu q_s) [\mathbb{1} + (\mathbf{Y}_u^\dagger \mathbf{Y}_u) + (\mathbf{Y}_d^\dagger \mathbf{Y}_d)]_{rs}$$

$$\begin{aligned} \hookrightarrow & \bar{u}_L \gamma^\mu [\mathbb{1} + Y_u^\dagger Y_u + V_{\text{CKM}} Y_d^\dagger Y_d V_{\text{CKM}}^\dagger] u_L \\ & + \bar{d}_L \gamma^\mu [\mathbb{1} + V_{\text{CKM}}^\dagger Y_u^\dagger Y_u V_{\text{CKM}} + Y_d^\dagger Y_d] d_L \end{aligned}$$

SMEFTsim: basic structure and main features

- 2 independent, equivalent models sets: best for debugging and validation
each contains: 6 pre-exported UFO models + FeynRules sources

Main characteristics:

- ▶ contain SM + SM radiative Higgs couplings ($hgg, h\gamma\gamma, hZ\gamma$) + complete Warsaw basis for 3 generations
- ▶ canonical kinetic terms + input shifts automatically implemented
- ▶ restrictions available for massless fermions ($\neq t, b$) + CP conserving
- ▶ only unitary gauge : ghost Lagrangian not adjusted for $d = 6$ effects
- ▶ only tree level calculations in MadGraph5
- ▶ by construction: theoretical uncertainty of order % (neglected $d = 8$, radiative corrections etc)

Possible application: a pole observables program

The most general SMEFT setup has too many parameters!

How to reduce them?

- ▶ IR assumptions (symmetries: CP, flavor)
- ▶ smart choice of observables + phase space

Basic idea: the dominant effects are **interference terms** between the SM and $d = 6$ contributions



close to the narrow SM bosons resonances (Z, W, h)
the pole structure can enhance/suppress
the impact of certain operators

... + less trouble with **EFT validity** in this phase space

Possible application: a pole observables program

– Close to a narrow resonance peak –

Relevant terms

- ▶ non-SM corrections to SM interactions $\sim \langle H^\dagger | \mathcal{L}_{\text{SM}} | H \rangle$
- ▶ non-SM corrections to SM interactions $\sim \partial$
- ▶ corrections to propagators: δm_W

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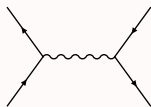
Suppressed terms

- ▶ most ψ^4 operators: give diagrams with less resonances

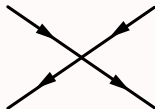
In general: expected to be suppressed wrt. “pole operators” by

$$\left(\frac{\Gamma_B m_B}{v^2} \right)^n \text{ or } \left(\frac{\Gamma_B m_B}{\mathcal{I}} \right)^n, \quad B = \{Z, W, h\}, \quad \mathcal{I} \sim s, \quad n = \# \text{ missing resonances}$$

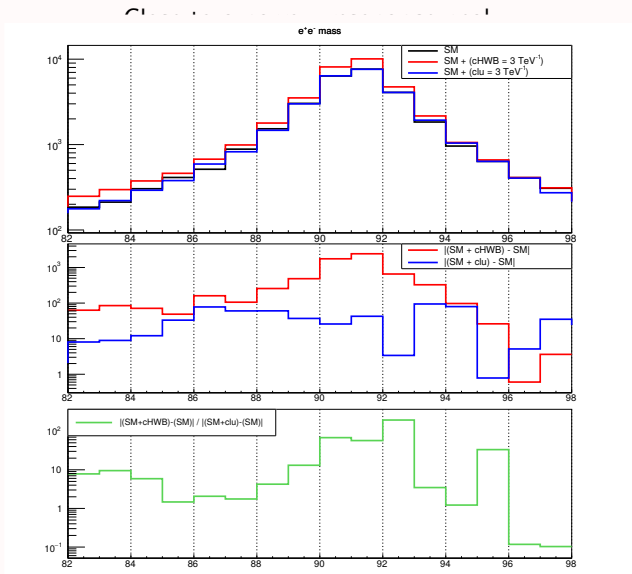
Example: Drell-Yan via Z resonance



vs.



Possible application: a pole observables program



Possible application: a pole observables program

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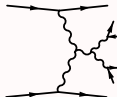
In general: expected to be suppressed wrt. “pole operators” by

$$\left(\frac{\Gamma_{Bm_B}}{v^2} \right)^n \text{ or } \left(\frac{\Gamma_{Bm_B}}{\mathcal{I}} \right)^n, \quad B = \{Z, W, h\}, \quad \mathcal{I} \sim s, \quad n = \# \text{ missing resonances}$$

! Not *always* the case. E.g. VBS



vs



the 4-fermion diagram is not removed by poles selection.

Other kinematic variables may help? ▶ can be checked with MG

Other possible selection criteria

The SM – ($d = 6$) interference can also be suppressed by:

- ▶ proportionality to **light fermion masses** .

Example: dipole operators can be neglected for $f \neq t, b$



- ▶ **flavor violation** in neutral currents can also be neglected

The SM amplitude is very suppressed:

The diagram shows a wavy line (representing a W boson) interacting with a fermion line (represented by two straight lines with arrows) at a vertex. The vertex is labeled 'W'. The amplitude is given by the equation:

$$\sim \frac{m_j^2 V_{jk}^* V_{ji}}{32\pi^2 m_W^2}$$

(similar suppression for Higgs vertex)

- ▶ ...

Summary

A sensible reduction of the # of parameters:

Case	total # par.	par. for $W/Z/h$ pole obs.
general	2499	~ 84
$U(3)^5$ symmetric	~ 80	~ 37
MFV	~ 90	~ 30

Takeaway message on poles program

- ▶ poles are an interesting (and safe!) place to look into. They can give relevant information, complementary to that in the tails.
- ▶ the pole structure selects a small number of parameters compared to the complete set (even in the flavor general case).
- ▶ the SMEFTsim package can help to develop a consistent poles program!

Backup slides

X^3		φ^6 and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	Q_φ	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
Q_W	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	Q_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s^k q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^j)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqqu}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk\ell mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^m)^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^m)^T C l_t^n]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		