Directed flow and freeze-out in relativistic heavy-ion collisions at NICA and FAIR energies





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in collaboration with

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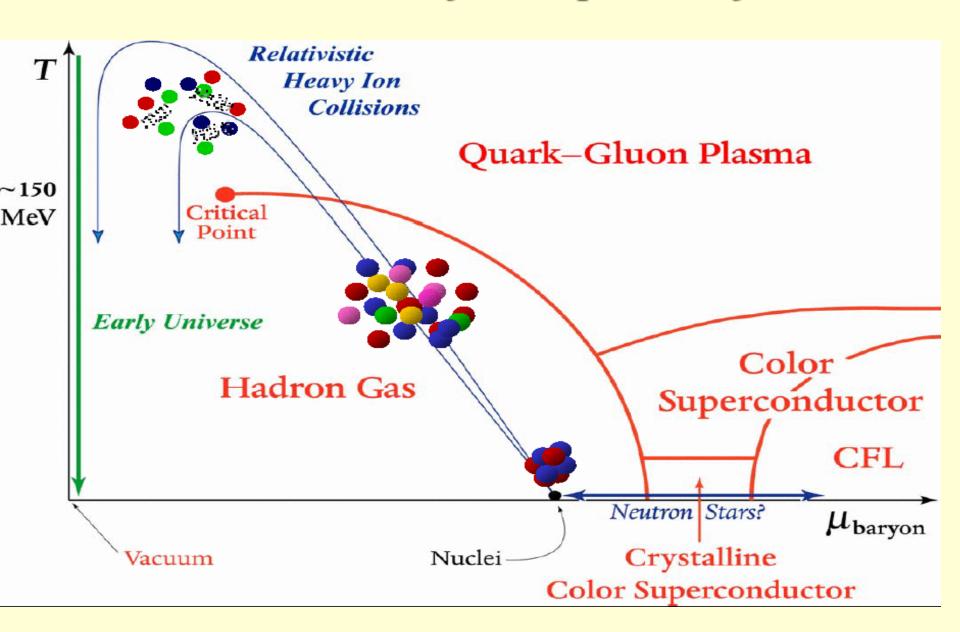




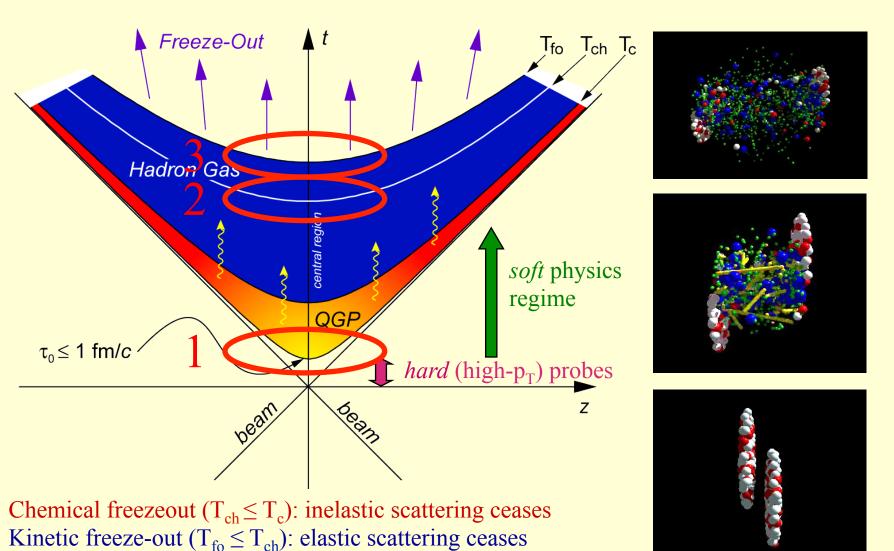
7-th International Conference on New Frontiers in Physics ICNFP-2018
Kolymbari, Crete, Greece, 4-12.07.2018



Present status of the Equation of State



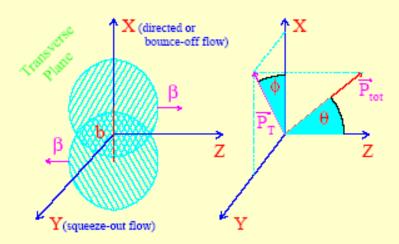
Motivation



Flow: We have to quatify this phenomenon

Definitions. Non-central Collisions (b>0)

Reaction Plane

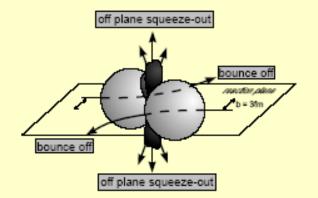


Flow Decomposition:

Transverse flow = Radial + Bounce-off + Squeeze-out

S. Voloshin and Y. Zhang, ZPC 70 (1996) 665

Modern analysis:



$$\mathbf{E}\frac{\mathbf{d^3N}}{\mathbf{d^3p}} = \frac{1}{2\pi} \frac{\mathbf{d^2N}}{\mathbf{p_T} \mathbf{dp_T} \mathbf{dy}} \left(\mathbf{1} + \sum_{\mathbf{n=1}}^{\infty} \mathbf{2v_n} \cos{(\mathbf{n}\phi')} \right)$$

Directed flow:

$$\mathbf{v_1} = \left\langle \frac{\mathbf{p_x}}{\mathbf{p_T}} \right\rangle \equiv \left\langle \cos\left(\phi'\right) \right\rangle$$

Elliptic flow:

$$\begin{array}{ll} \mathbf{v_2} &= \left\langle \left(\frac{\mathbf{p_x}}{\mathbf{p_T}}\right)^2 - \left(\frac{\mathbf{p_y}}{\mathbf{p_T}}\right)^2 \right\rangle &\equiv \\ \left\langle \cos\left(2\phi'\right)\right\rangle \end{array}$$

Distributions

Rapidity dependence

$$\mathbf{v_n}(\mathbf{y}, \Delta \mathbf{p_t}, \Delta \mathbf{b}) = \frac{\int_{\Delta \mathbf{p_t}} \int_{\Delta \mathbf{b}} \cos(\mathbf{n}\phi) \frac{\mathbf{d^3N}}{\mathbf{dydbdp_t}} \mathbf{dp_t db}}{\int_{\Delta \mathbf{p_t}} \int_{\Delta \mathbf{b}} \frac{\mathbf{d^3N}}{\mathbf{dydbdp_t}} \mathbf{dp_t db}}$$

Transverse momentum dependence

$$\mathbf{v_n}(\mathbf{p_t}, \Delta \mathbf{y}, \Delta \mathbf{b}) = \frac{\int_{\Delta \mathbf{y}} \int_{\Delta \mathbf{b}} \cos(\mathbf{n}\phi) \frac{\mathbf{d^3N}}{\mathbf{dydbdp_t}} \mathbf{dydb}}{\int_{\Delta \mathbf{y}} \int_{\Delta \mathbf{b}} \frac{\mathbf{d^3N}}{\mathbf{dydbdp_t}} \mathbf{dydb}}$$

n=1,2,...

Centrality dependence

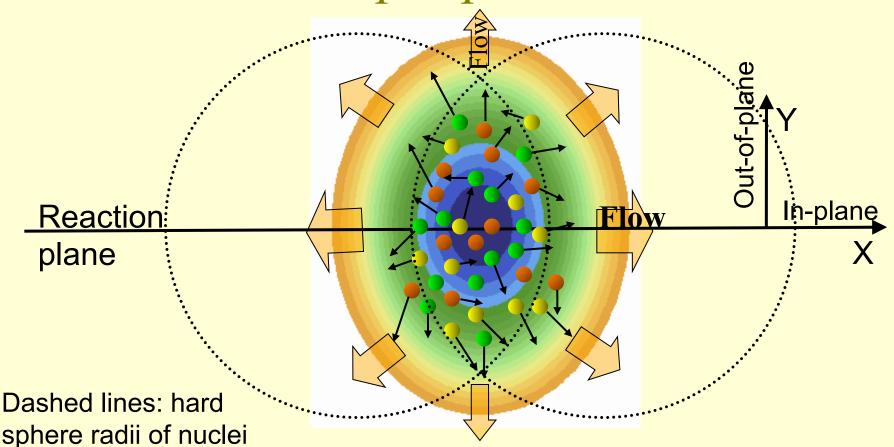
$$\mathbf{v_n}(\mathbf{b}, \Delta \mathbf{p_t}, \Delta \mathbf{y}) = \frac{\int_{\Delta \mathbf{p_t}} \int_{\Delta \mathbf{y}} \cos(\mathbf{n}\phi) \frac{\mathbf{d^3N}}{\mathbf{dydbdp_t}} \mathbf{dp_t dy}}{\int_{\Delta \mathbf{p_t}} \int_{\Delta \mathbf{y}} \frac{\mathbf{d^3N}}{\mathbf{dydbdp_t}} \mathbf{dp_t dy}}$$

Motivation: connection to Equation of State

F. Retiere, QM2004 talk

Flow (in the transverse plane)

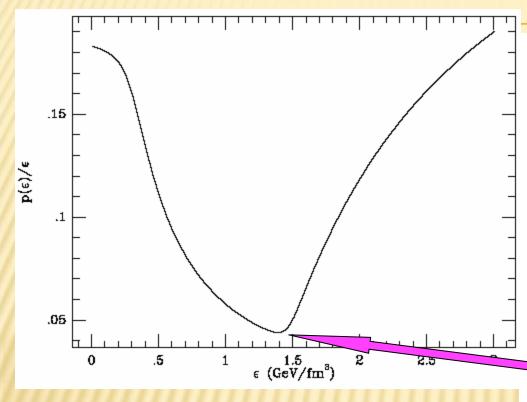
A mid-peripheral collision



Re-interactions → FLOW

Re-interactions among what? **Hadrons, partons or both?** *In other words, what equation of state?*

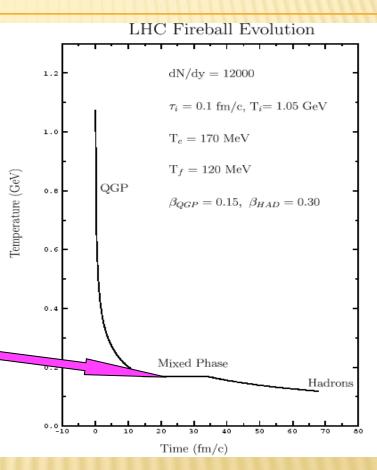
DISAPPEARANCE OF DIRECTED FLOW



Hung and Shuryak, PRL 75 (1995) 4003

In case of first order phase transition

$$\frac{dP}{d\varepsilon} = c_s^2 = 0$$



Braun-Munzinger, NPA 661 (1999) 261c

V1 OF NUCLEONS AND FRAGMENTS AT LOWER ENERGIES

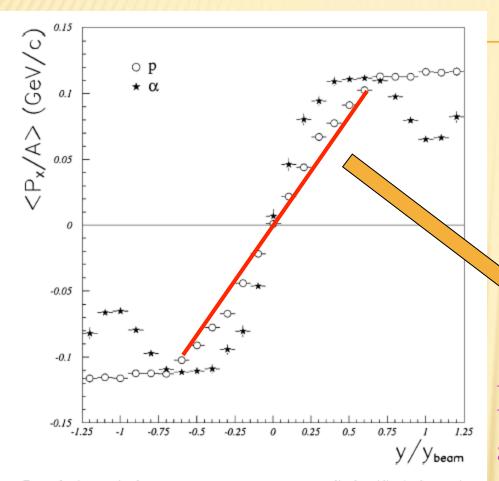


Figure 1 Average in-plane transverse momentum versus normalized rapidity in the reaction Au+Au at 800A MeV. The points at $y/y_{beam} < 0$ are reflected.

W. Reisdorf, H.G. Ritter Annu.Rev.Nucl.Part.Sci. 47 (1997) 663 Plastic Ball Collaboration introduced a slope parameter

$$\mathbf{F} = \frac{\mathbf{d} \langle \mathbf{p_x} \rangle / \mathbf{A}}{\mathbf{dy_n}}, \quad \mathbf{y_n} = \mathbf{y} / \mathbf{y_{max}}$$

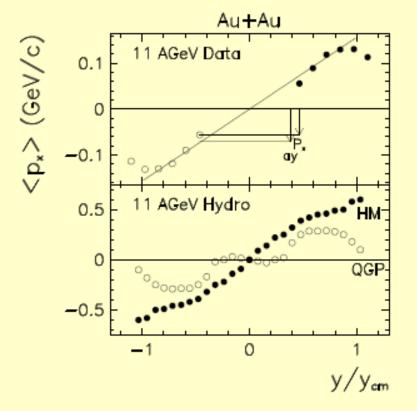
$$\mathbf{F_y} = \frac{\mathbf{d} \langle \mathbf{p_x} \rangle / \mathbf{A}}{\mathbf{dy}}$$

Directed flow of nucleons and fragments has linear slope in normal direction

=> normal flow

SOFTENING OF DIRECTED FLOW

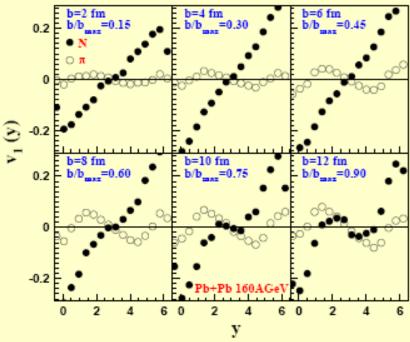
L.P. Csernai, D. Röhrich, PLB 458 (1999) 454



Transition to the Quark-Gluon Plasma

→ decrease in pressure → softening
of the directed flow

L. Bravina, PLB 334, 49 (1995)
H. Liu, S. Panitkin, N. Xu, PRC 59, 348 (1999)
R.J.M. Snellings et al., PRL 84, 2803 (2000)
L. Bravina et al., PRC 61, 064902 (2000)



Wiggle structure: The effect is more pronounced in peripheral and light-ion collisions, therefore, it cannot be explained by the softening of the EOS because of the formation of strings

Directed flow at FAIR and NICA

Beam energy scan results for v_1 (STAR)

S. Singha et al. (STAR Collab.), PoS CPOD2017 (2018) 004

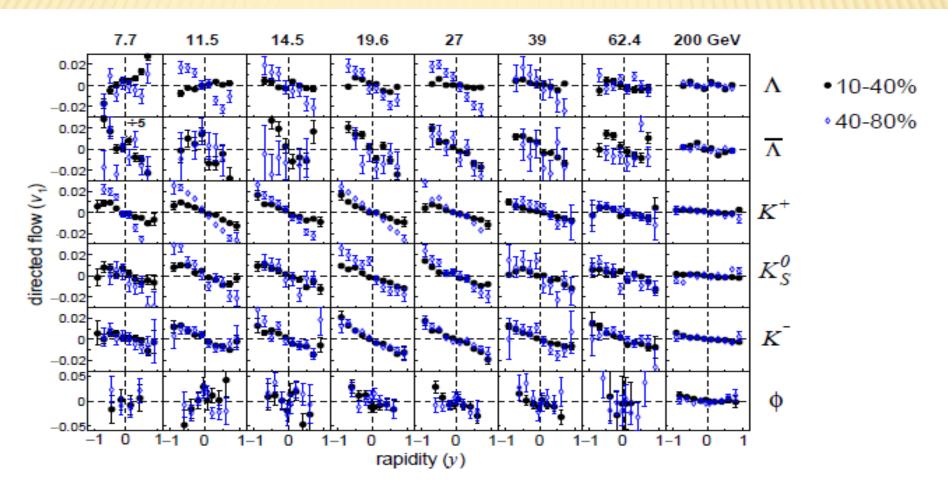
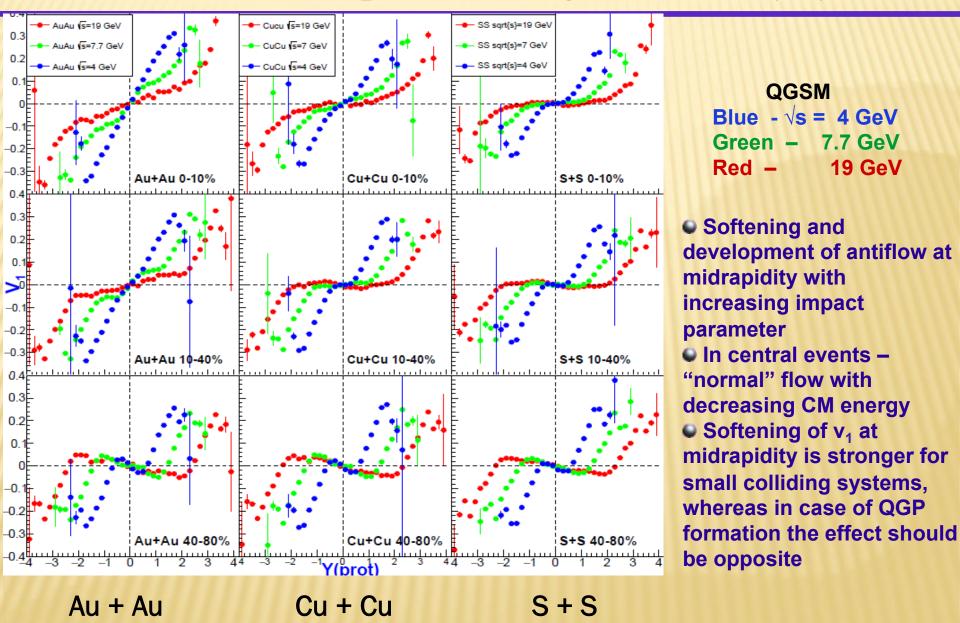
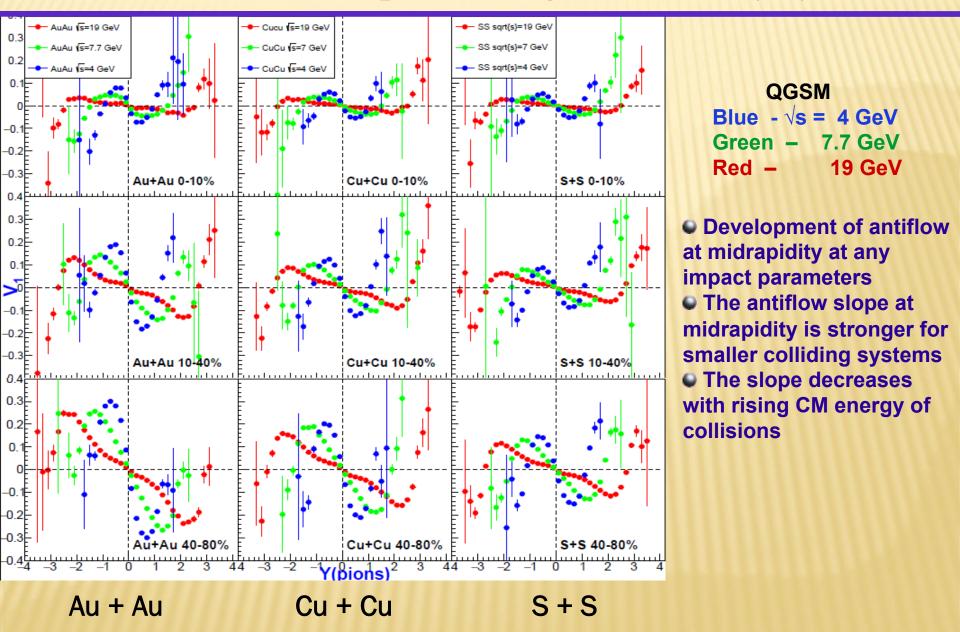


Figure 1: (Color online) Rapidity dependence of directed flow (v_1) for Λ , $\overline{\Lambda}$, K^+ , K_s^0 , K^- and ϕ in 10-40% and 40-80% Au+Au collisions at $\sqrt{s_{NN}}=7.7$, 11.5, 14.5, 19.6, 27, 39, 62.4 and 200 GeV.

Directed flow of protons in light and heavy systems



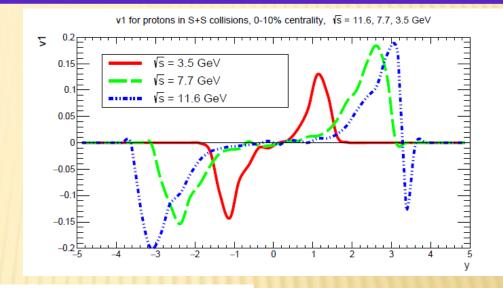
Directed flow of pions in light and heavy systems

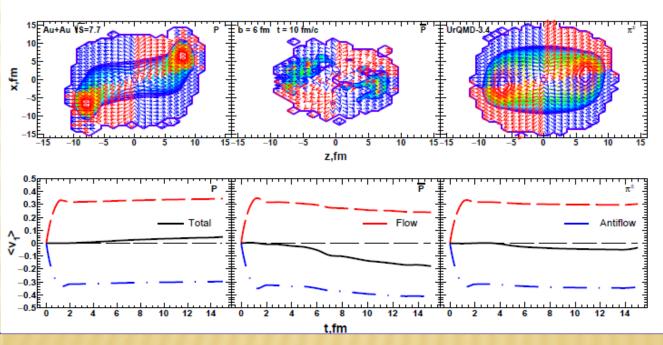


Directed flow in HI collisions at FAIR/NICA energies

Origin of changing of proton directed flow from antiflow to normal flow with decrease of CM energy in microscopic transport models

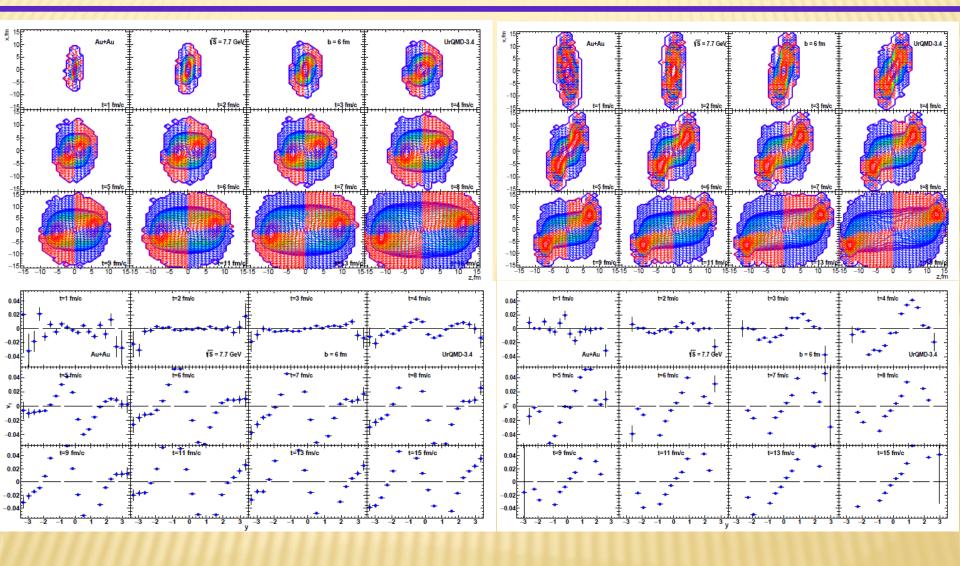
See poster by O.Vityuk





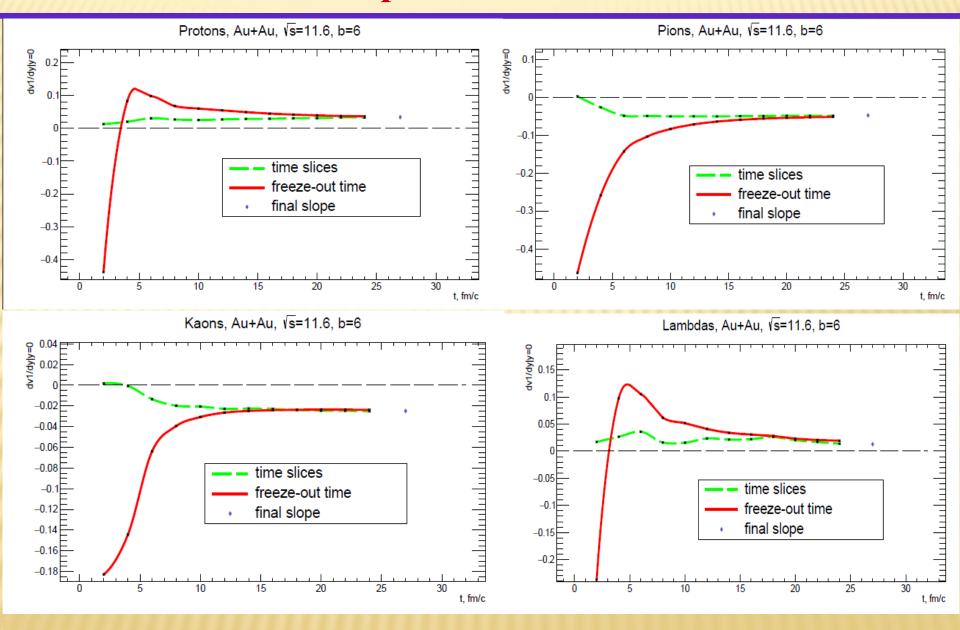
Directed flow = Normal flow – Antiflow

Time development of directed flow



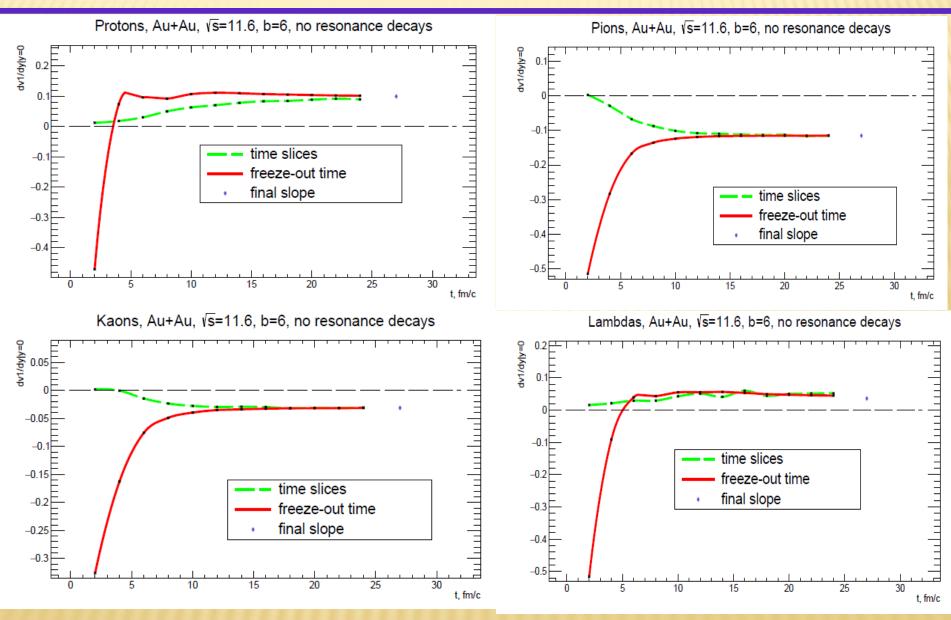
• It appears that V_1 of both pions and protons at midrapidity is formed not earlier than 5-6 fm/c

Time development of directed flow



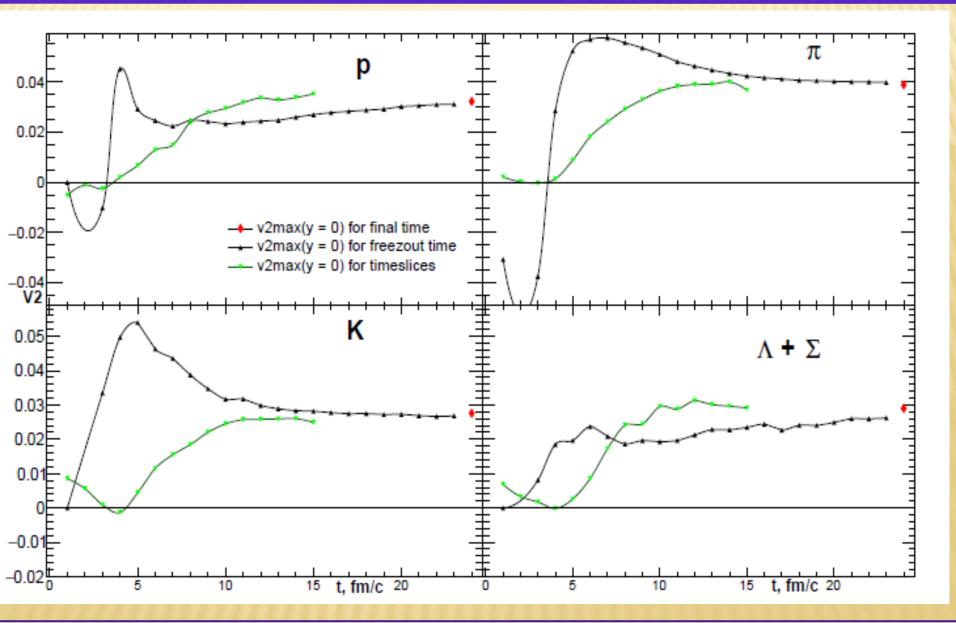
■ V₁ of both mesons and baryons at midrapidity is formed at approximately 6 – 10 fm/c

Influence of resonances on the development of $\mathbf{V_1}$



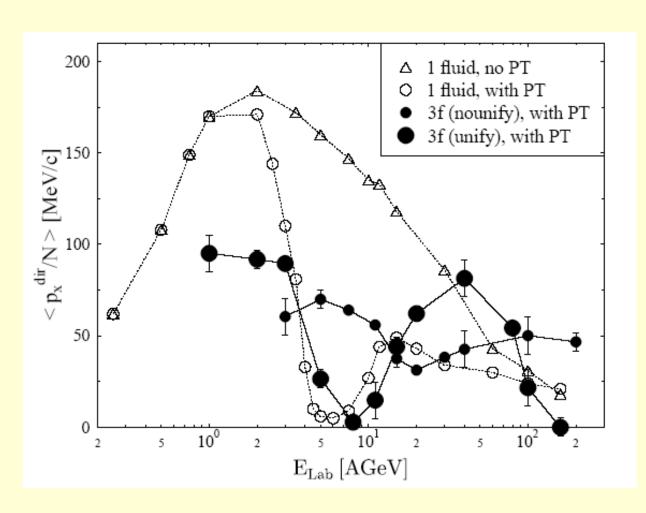
○ Difference is seen only for Lambdas and for protons (not so distinct) at t ≈ 5 fm/c

(for comparison): Time development of elliptic flow



V₂ of both mesons and baryons at midrapidity is formed after 10 fm/c

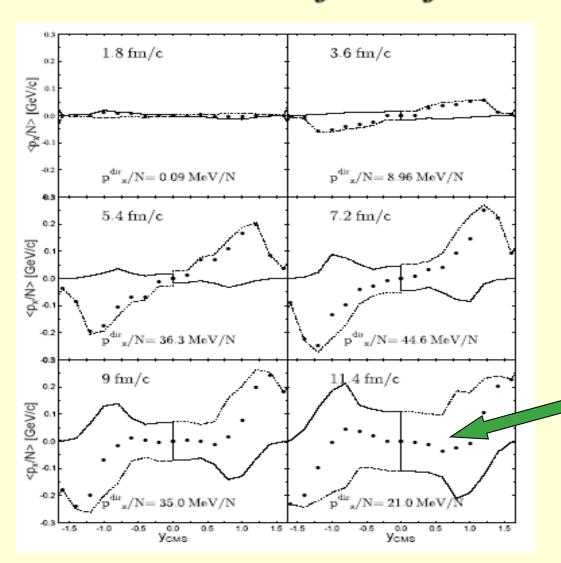
Directed flow of nucleons. 3-fluid hydro



The model predicts a local minimum in the excitation function of directed flow at energies between 10 and 20 AGeV (so far not been observed)

J. Brachmann et al., PRC 61 (2000) 024909

Directed flow of nucleons. 3-fluid hydro



The antiflow component is a source of the reduction of directed flow at midrapidity

NB! This is a very rare case when the antiflow behavior is reproduced in hydrodynamic model

J. Brachmann et al., PRC 61 (2000) 024909

Directed flow of hadrons in 3-fluid hydro THESEUS

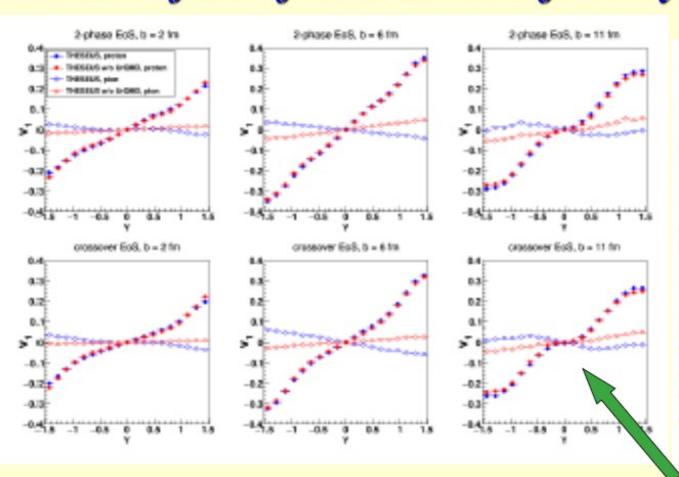


Figure 5. Two upper rows: Directed flow (v_1) of protons (full symbols) and pions (open symbols) for central (b = 2 fm), semicentral (b = 6 fm) and peripheral (b = 11 fm) Au+Aucollisions at $E_{lab} = 8 \text{ A GeV}$. The upper row is for the 2-phase EoS while the lower row shows results for the crossover EoS. In each panel we show the direct comparison of THESEUS with (blue symbols) and without (red symbols) UrQMD afterburner. Remarkable is the effect of turning pion flow to antiflow due to hadronic rescattering in the dense baryonic medium.

P. Batyuk, ... Yu. Ivanov et al., 1711. 07959

Directed flow of hadrons in 3-fluid hydro THESEUS

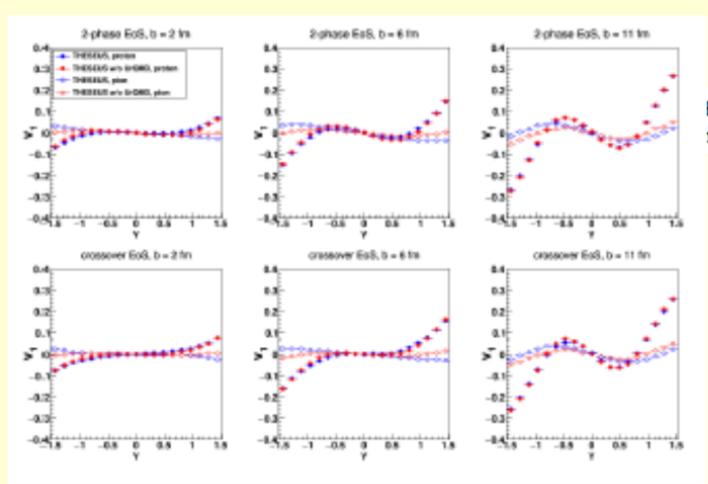
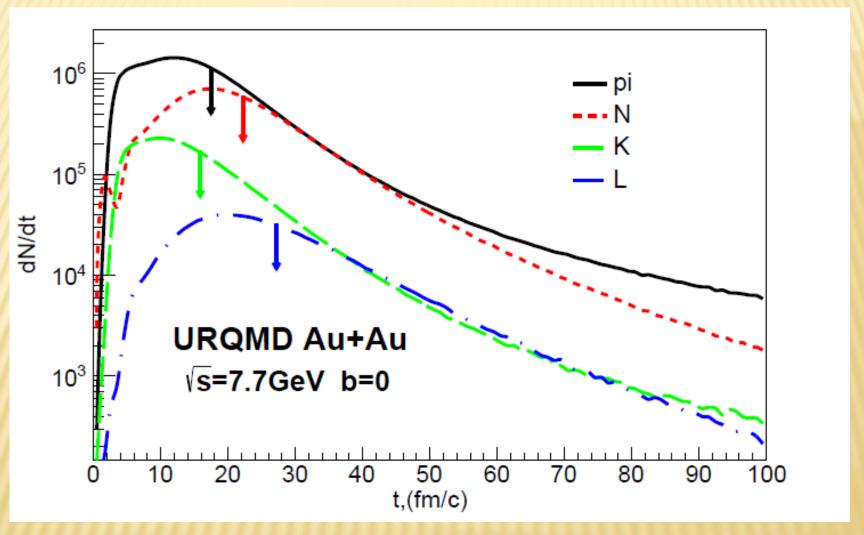


Figure 6. Same as in Fig. 5 out for $E_{lab} = 30 \text{ A GeV}$.

P. Batyuk, ... Yu. Ivanov et al., 1711. 07959

Directed flow and freeze-out

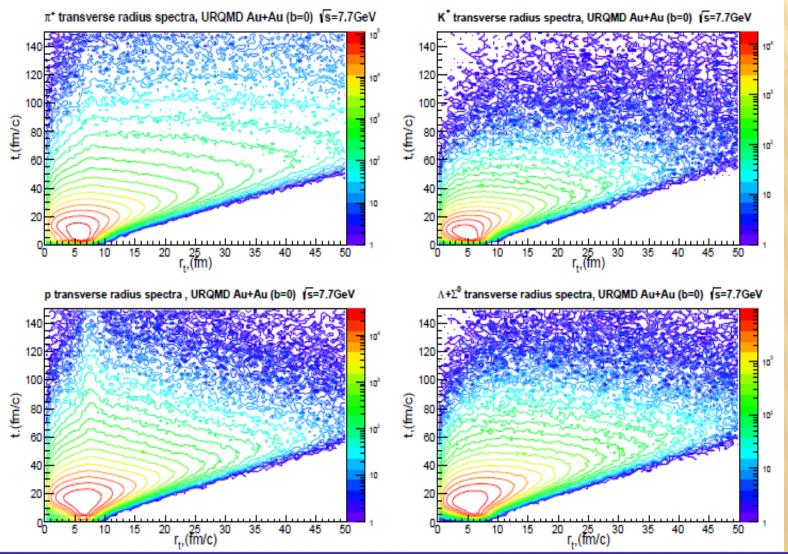
Sequential freeze-out of hadrons at NICA energies



- There is no sharp freeze-out for different hadrons
- The order of freeze-out is as follows: mesons (kaons and pions), nucleons and lambdas

Freeze-out of hadrons at NICA energies

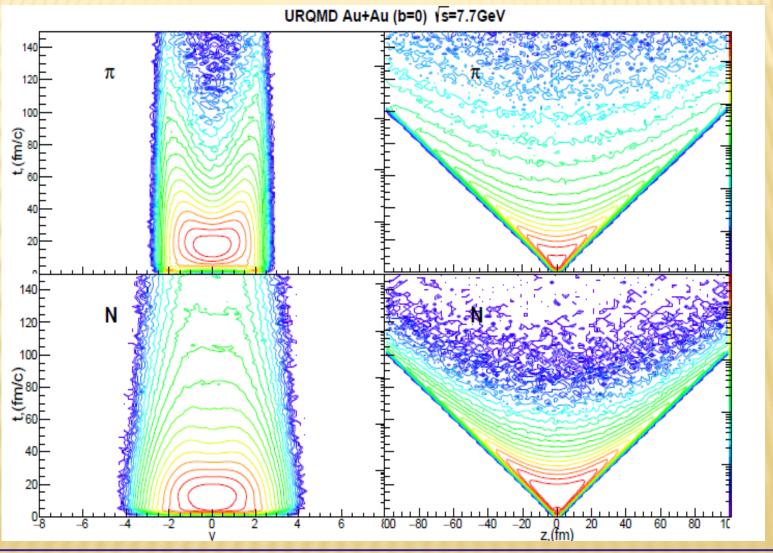
Au + Au @ 7.7 GeV ; b = 0 fm



Baryons are emitted longer and from larger areas than mesons

Freeze-out of hadrons at NICA energies

Au + Au @ 7.7 GeV ; b = 0 fm



Baryons are emitted longer and from larger areas than mesons

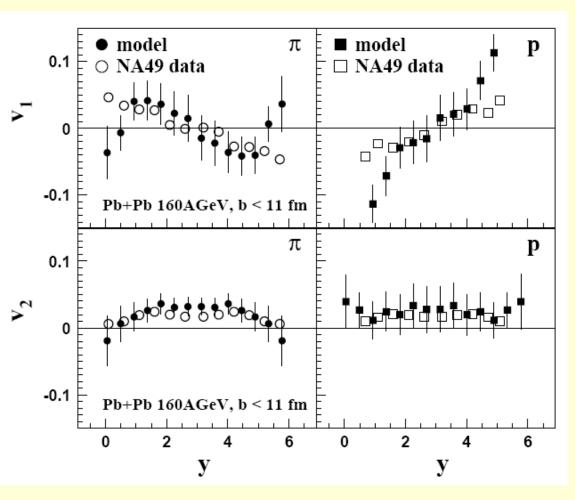
CONCLUSIONS

- **◆** Directed flow = Normal Flow Antiflow
- Normal Flow \geq Antiflow (except of the midrapidity range)
- **◆** The softening of the flow can be misinterpreted as the softening of EOS due to formation of the QGP, but:
- QGP → the effect is stronger for semi-central collisions

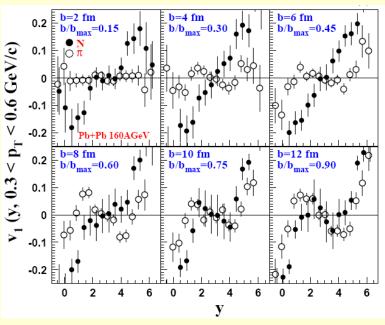
 Cascade → the effect is stronger for semi-peripheral and peripheral ones
- **♦** At energies about few GeV: normal directed flow of protons at midrapidity in central collisions and antiflow in peripheral ones. Mesons antiflow for all centralities.
- **◆** The directed flow of high-P_T is elongated in normal direction
- **◆** Development of both directed and elliptic flow of hadrons at midrapidity in transport models takes about 6-8 fm/c (or longer)
- **♦** Collective phenomena, such as anisotropic flow, should be studied together with the freeze-out conditions

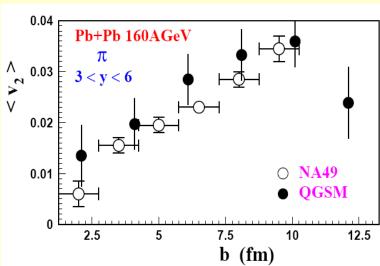
Back-up Slides

Comparison with QGSM calculations

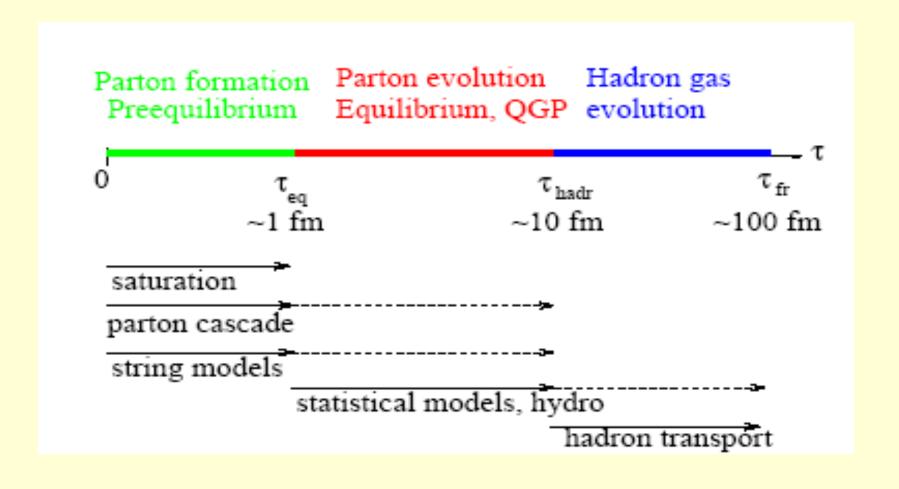








Applicability of different models



Predictions for A+A at 200 and 5500 GEV

