On Formalisms and Interpretations arXiv:1710.07212 [BW17]

Veronika Baumann

USI Lugano & University of Vienna

12.07.2018





National Centre of Competence in Research

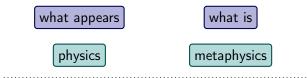


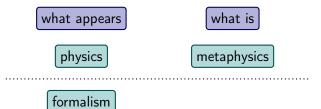
what appears

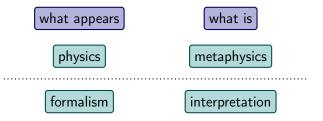


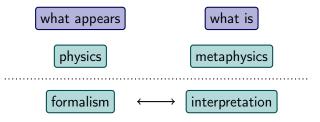


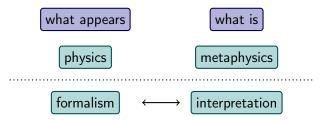




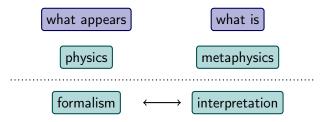




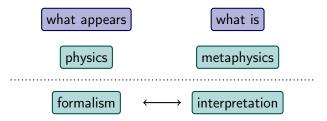




• prediction of measurement results (empirical equivalence)



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- formalism \neq interpretation



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- classical: empirically equivalent formalisms \rightarrow interpretation quantum: formalism \rightarrow ?

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- Observer measuring the system (observable A) getting result $a\in\sigma(A)$ with probability

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$$p_{\phi}(a) = \operatorname{Tr}(|a\rangle\langle a||\phi\rangle\langle\phi|) = |\langle a|\phi\rangle|^2 \tag{1}$$

Born rule

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Born rule

• Measurement update rule: (collapse)

$$|\phi\rangle \xrightarrow[result: a]{A} |a\rangle$$
 (2)

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Born rule

• Measurement update rule: (collapse)

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... giving probabilities for subsequent measurements!

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 angle$
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 $|A(a)\rangle$ state of the observer seeing a

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 $|A(a)\rangle$ state of the observer seeing a

• Probabilities of outcomes are probabilities of states of the observer:

$$q_{\phi}(a) = \operatorname{Tr}(\mathbb{1} \otimes |A\rangle \langle A||\phi_{tot}\rangle \langle \phi_{tot}|)$$
"Born" rule
$$(4)$$

• empirically equivalent:

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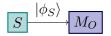
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 - QBism

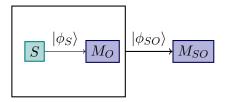
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• Observers observing the same quantum system.

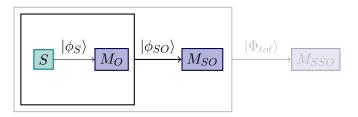
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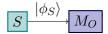
- Observers observing the same quantum system.
- *Superobservers* observing *systems and observers* as a joint system.

Observing the Observer

Wigner's-friend experiments combine different levels of observation.



- Observers observing the same quantum system.
- Superobservers observing systems and observers as a joint system.
- *Super-superobservers* etc.



$$\begin{split} M_{O_1} &: \{|\uparrow\rangle_S, |\downarrow\rangle_S\}; \ M_{O_2} &: \{|a\rangle_S, |b\rangle_S\}\\ &\dots \text{ where } |\uparrow\rangle = \alpha |a\rangle + \beta |b\rangle, \ |\downarrow\rangle = \beta |a\rangle - \alpha |b\rangle \end{split}$$

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Probabilities in the Collapse Formalism

 O_2 observing c=a,b, given O_1 observed $z=\uparrow,\downarrow$ $p(c|z)=\mathrm{Tr}(|c\rangle\langle c||z\rangle\langle z|)=|\langle c|z\rangle|^2.$

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$$M_{O_1} : \{|\uparrow\rangle_S, |\downarrow\rangle_S\}; M_{O_2} : \{|a\rangle_S, |b\rangle_S\}$$

... where $|\uparrow\rangle = \alpha |a\rangle + \beta |b\rangle, |\downarrow\rangle = \beta |a\rangle - \alpha |b\rangle$
 $|\phi_S\rangle = \sqrt{\frac{1}{2}}(|\uparrow\rangle + |\downarrow\rangle)$

• Collapse:

$$\begin{array}{c|c} z & p(a \mid z) & p(b \mid z) \\ \hline \uparrow & \alpha^2 & \beta^2 \\ \downarrow & \beta^2 & \alpha^2 \end{array}$$

Probabilities in the Relative State Formalism

$$O_2$$
 observing $c = a, b$, given O_1 observed $z = \uparrow, \downarrow$
$$q(c|z) = \frac{1}{q_z} \operatorname{Tr}(\mathbb{1} \otimes |Z\rangle \langle Z| \otimes |C\rangle \langle C||\phi_{tot}\rangle \langle \phi_{tot}|).$$

$$\begin{split} M_{O_1} &: \{|\uparrow\rangle_S, |\downarrow\rangle_S\}; \ M_{O_2} : \{|a\rangle_S, |b\rangle_S\}\\ \dots \text{ where } |\uparrow\rangle &= \alpha |a\rangle + \beta |b\rangle, \ |\downarrow\rangle &= \beta |a\rangle - \alpha |b\rangle\\ |\phi_S\rangle &= \sqrt{\frac{1}{2}}(|\uparrow\rangle + |\downarrow\rangle) \end{split}$$

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• Relative state:

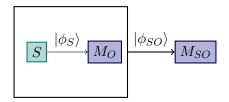
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empirically equivalent

• Relative state:



 $M_O: \{|\uparrow\rangle_S, |\downarrow\rangle_S\}; M_{SO}: \{|A\rangle_{S,O}, |B\rangle_{S,O}\}$

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$$\begin{array}{c|c} Z & p(A \mid Z) & p(B \mid Z) \\ \hline U & \alpha^2 & \beta^2 \\ D & \beta^2 & \alpha^2 \end{array}$$

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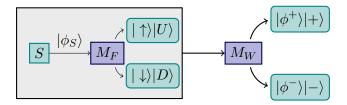
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• Collapse:

• Relative state:

empirically inequivalent

$$\begin{split} |\phi_S\rangle &= \sqrt{\frac{1}{2}}(|\uparrow\rangle + |\downarrow\rangle)\\ |\phi^{\pm}\rangle &= \sqrt{\frac{1}{2}}\,(|\uparrow,U\rangle \pm |\downarrow,D\rangle), \ \alpha = \beta = \sqrt{\frac{1}{2}} \end{split}$$



Collapse

Collapse

Z
$$p(+ \mid Z)$$
 $p(- \mid Z)$ Is "-" possible?U $\frac{1}{2}$ $\frac{1}{2}$ yesD $\frac{1}{2}$ $\frac{1}{2}$ yes

Relative State $Z \mid q(+ \mid Z) \mid q(- \mid Z) \mid$ Is "-" possible? $U \mid 1 \mid 0 \mid$ no $D \mid 1 \mid 0 \mid$ no

Friend

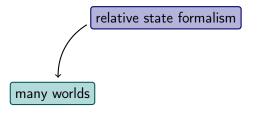
| Z | $p(+ \mid Z)$ | $p(- \mid Z)$ | Is "—" possible? | |
|--------|---------------|---------------|------------------|--|
| U | $\frac{1}{2}$ | $\frac{1}{2}$ | yes | |
| D | $\frac{1}{2}$ | $\frac{1}{2}$ | yes | |
| Wigner | | | | |
| Z | q(+ Z) | $q(- \mid Z)$ | Is "—" possible? | |
| U | 1 | 0 | no | |
| D | 1 | 0 | no | |

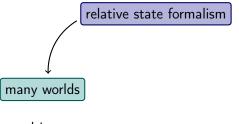
Friend

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|---------------|-----------------------------------|------------------|--|--|
| $\frac{1}{2}$ | $\frac{1}{2}$ | yes | | |
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| Wigner | | | | |
| $q(+ \mid Z)$ | $q(- \mid Z)$ | Is "—" possible? | | |
| 1 | 0 | no | | |
| 1 | 0 | no | | |
| | $\frac{\frac{1}{2}}{\frac{1}{2}}$ | | | |

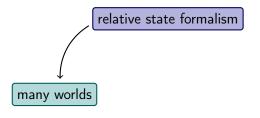
Wigner's - friend paradox: Different agents use different formalisms for friend's measurement. *(subjective collapse)*

relative state formalism

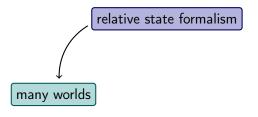




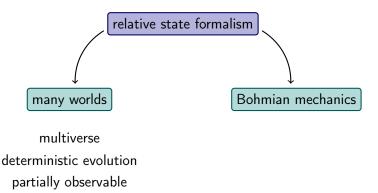
multiverse

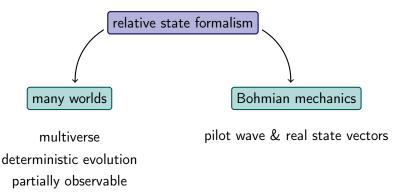


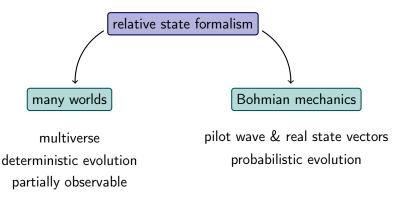
multiverse deterministic evolution

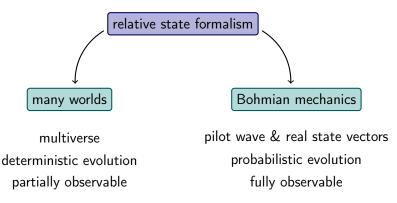


multiverse deterministic evolution partially observable

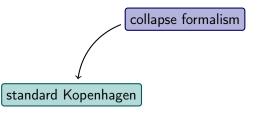


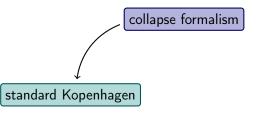




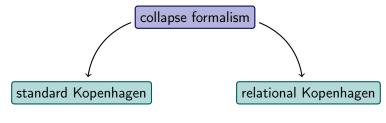


collapse formalism

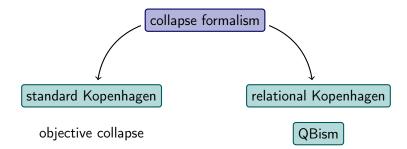


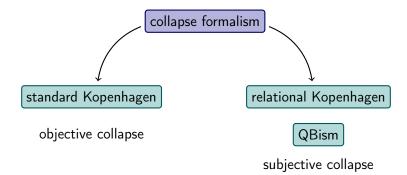


objective collapse



objective collapse



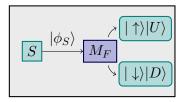


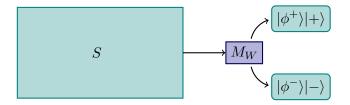
Relative-state formalism is *empirically inequivalent* to collapse formalism.

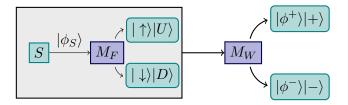
Friend

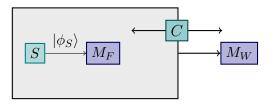
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| Wigner | | | |
| Z | $q(+ \mid Z)$ | $q(- \mid Z)$ | ls "—" possible? |
| U | 1 | 0 | no |
| D | 1 | 0 | no |

Wigner's - friend paradox: Different agents use different formalisms for friend's measurement. *(subjective collapse)*

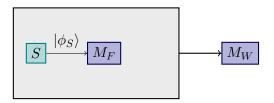




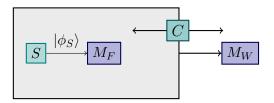




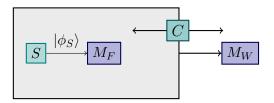
A contradiction requires classical information.



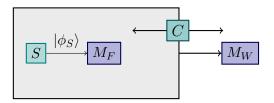
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- Classical communication in the Wigner's friend setup

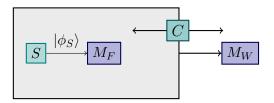


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 - possible conflict with full quantum control

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Thank you!

[BHW16] Veronika Baumann, Arne Hansen, and Stefan Wolf.

The measurement problem is the measurement problem is the measurement problem.

arXiv:1611.01111 [quant-ph], 2016.

[BW17] Veronika Baumann and Stefan Wolf. On formalisms and interpretations. *arXiv preprint arXiv:1710.07212*, 2017.

[FR16] Daniela Frauchiger and Renato Renner. Single-world interpretations of quantum theory cannot be self-consistent. arXiv:1604.07422, 2016.

[Sud17] Anthony Sudbery.

Single-world theory of the extended wigner's friend experiment.

Foundations of Physics, 47(5):658-669, 2017.