

# Radiation damage models: comparison between Silvaco and Synopsys

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# Introduction & Outline

TCAD simulation became an essential tool when designing silicon pixel sensors and predicting their properties.

Two main tools are available: Silvaco and Synopsys TCAD tools.

Are they compatible with one another in default settings and simple questions?

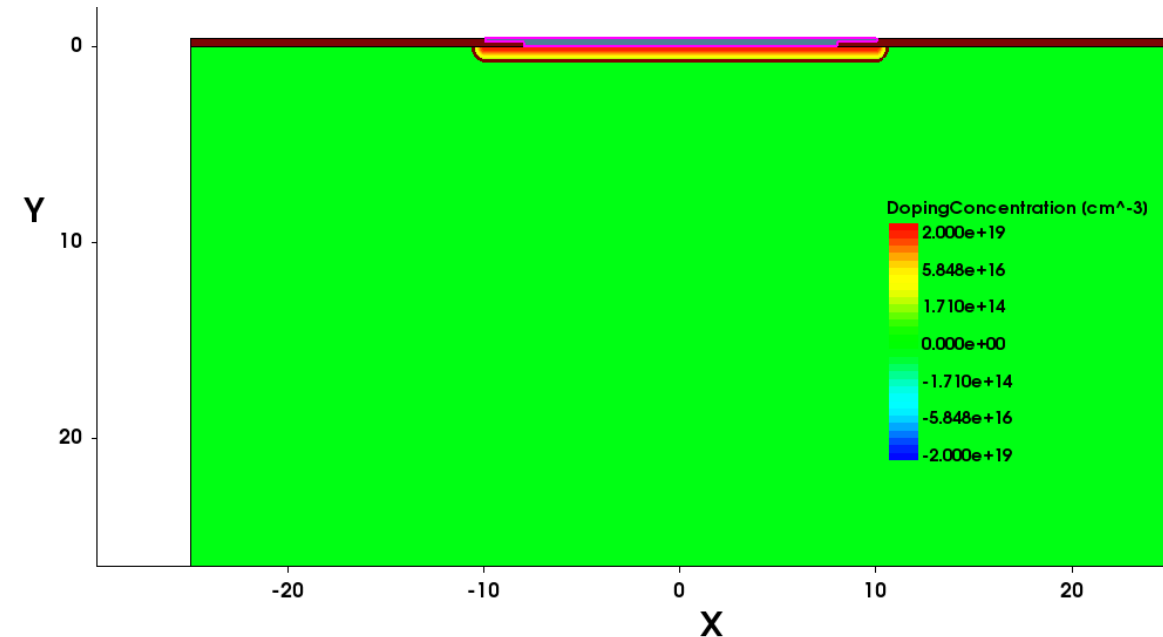
Do common radiation damage models developed with one of them, also work for the other?



# Setup for the comparison

## Structure and perspectives

- use a simple 2D TCAD model to reduce any possible difference arising from different implementations of the structure
- aims:
  - compare CV and IV curves for not-irradiated case at various temperatures
  - compare CV, IV and CCE (MIP based) after irradiation
    - compare the models with one simulator
    - compare the simulators with one model



# Setup for the comparison

## Radiation damage models

- radiation damage in TCAD:
  - bulk damage:
    - traps characterised by energy level, e/h cross-section and introduction rate
    - use New Delhi<sup>1</sup> and Perugia 2017<sup>2</sup> irradiation model here
  - surface damage:
    - fixed oxide charge of  $1 \times 10^{11} \text{cm}^{-2}$  for not-irradiated and  $1 \times 10^{12} \text{cm}^{-2}$  for irradiated sensors
    - no interface traps
- radiation level:  $1 \times 10^{15} n_{\text{eq}} \text{cm}^{-2}$
- temperature:  $-20^\circ\text{C}$ ,  $0^\circ\text{C}$ ,  $20^\circ\text{C}$

<sup>1</sup> R. Dalal et al., Simulation of Irradiated Si Detectors ,PoS Vertex2014 (2015).

<sup>2</sup> F. Moscatelli et al., Effects of Interface Donor Trap States on Isolation Properties of Detectors Operating at High-Luminosity LHC, IEEE Trans. on Nucl. Science 2017

TABLE II  
RADIATION DAMAGE MODEL FOR P-TYPE SUBSTRATES  
(UP TO  $7 \times 10^{15} \text{N}/\text{CM}^2$ )

Perugia 2017

| Type     | Energy (eV)  | $\sigma_e (\text{cm}^{-2})$ | $\sigma_h (\text{cm}^{-2})$ | $\eta (\text{cm}^{-1})$ |
|----------|--------------|-----------------------------|-----------------------------|-------------------------|
| Acceptor | $E_C - 0.42$ | $1 \times 10^{-15}$         | $1 \times 10^{-14}$         | 1.613                   |
| Acceptor | $E_C - 0.46$ | $7 \times 10^{-15}$         | $7 \times 10^{-14}$         | 0.9                     |
| Donor    | $E_V + 0.36$ | $3.23 \times 10^{-13}$      | $3.23 \times 10^{-14}$      | 0.9                     |

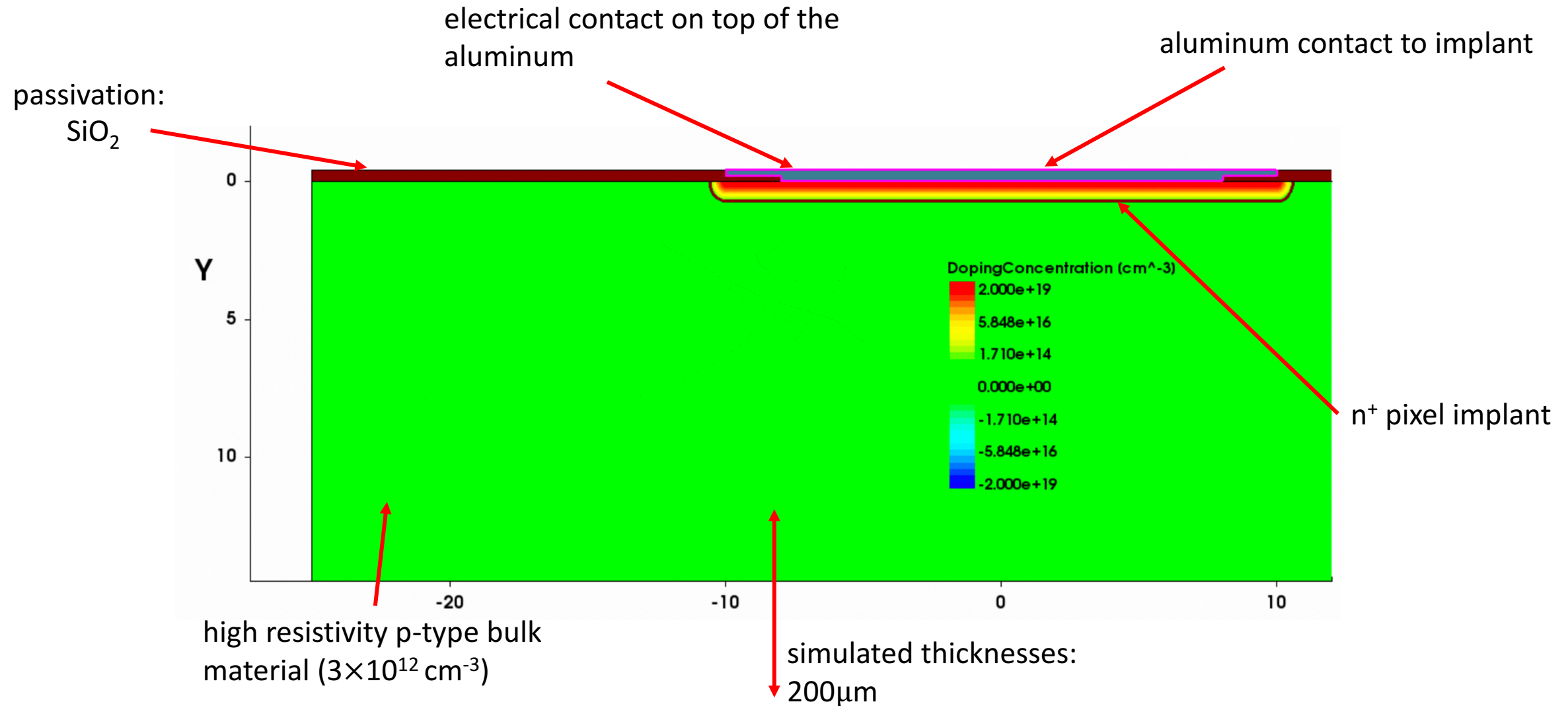
New Delhi

| Trap Type | Energy Level (eV)       | Introduction Rate ( $\text{cm}^{-1}$ ) | $\sigma_e (\text{cm}^2)$ | $\sigma_h (\text{cm}^2)$ |
|-----------|-------------------------|--|--------------------------|--------------------------|
| Acceptor  | $E_C - 0.51 \text{ eV}$ | 4                                      | $2 \cdot 10^{-14}$       | $3.8 \cdot 10^{-14}$     |
| Donor     | $E_V + 0.48 \text{ eV}$ | 3                                      | $2 \cdot 10^{-15}$       | $2 \cdot 10^{-15}$       |

Energy levels based on work of Eremin / Verbitskaya / Li

# Setup for the comparison

Structure of interest



# Setup for the comparison

## Physics models - Synopsys

### Mobility:

- doping dependent mobility according to Masetti model:

$$\mu_{\text{dop}} = \mu_{\text{min1}} \exp\left(-\frac{P_c}{N_{A,0} + N_{D,0}}\right) + \frac{\mu_{\text{const}} - \mu_{\text{min2}}}{1 + ((N_{A,0} + N_{D,0})/C_r)^\alpha} - \frac{\mu_1}{1 + (C_s/(N_{A,0} + N_{D,0}))^\beta} \quad (245)$$

- high field saturation according to extended Canali model (Electrical field as driving force):

$$\mu(F) = \frac{(\alpha + 1)\mu_{\text{low}}}{\alpha + \left[1 + \left(\frac{(\alpha + 1)\mu_{\text{low}} F_{\text{hfs}}}{v_{\text{sat}}}\right)^\beta\right]^{1/\beta}} \quad (338) \quad \beta = \beta_0 \left(\frac{T}{300 \text{ K}}\right)^{\beta_{\text{exp}}} \quad (339)$$

### Recombination:

- Shokley-Read-Hall (with doping, temperature and electric field (Hurx lifetime) dependence)
- no avalanche

$$R_{\text{net}}^{\text{SRH}} = \frac{np - n_{i,\text{eff}}^2}{\tau_p(n + n_1) + \tau_n(p + p_1)}$$

$$\tau_{\text{dop}}(N_{A,0} + N_{D,0}) = \tau_{\text{min}} + \frac{\tau_{\text{max}} - \tau_{\text{min}}}{1 + \left(\frac{N_{A,0} + N_{D,0}}{N_{\text{ref}}}\right)^y} \quad (367)$$

### Band-gap narrowing

- Old Slotboom

$$\chi(T) = \chi_0 + \frac{(\alpha + \alpha_2)T^2}{2(T + \beta + \beta_2)} + \text{Bgn2Chi} \cdot E_{\text{bgn}} \quad (160)$$

Formulas from  
Synopsys sDevice  
manual

# Setup for the comparison

Physics models - Silvaco

## Mobility:

- Lookup table depending on concentration and simple power law temperature dependence.
- Field dependent mobility model: Caughey and Thomas for low field regime; Schwarz and Russe for high field

## Recombination:

- Concentration dependent SRH recombination term (Roulston, Arora and Chamberlain - Law – Fossum, Lee and Lee)

## Band-gap narrowing

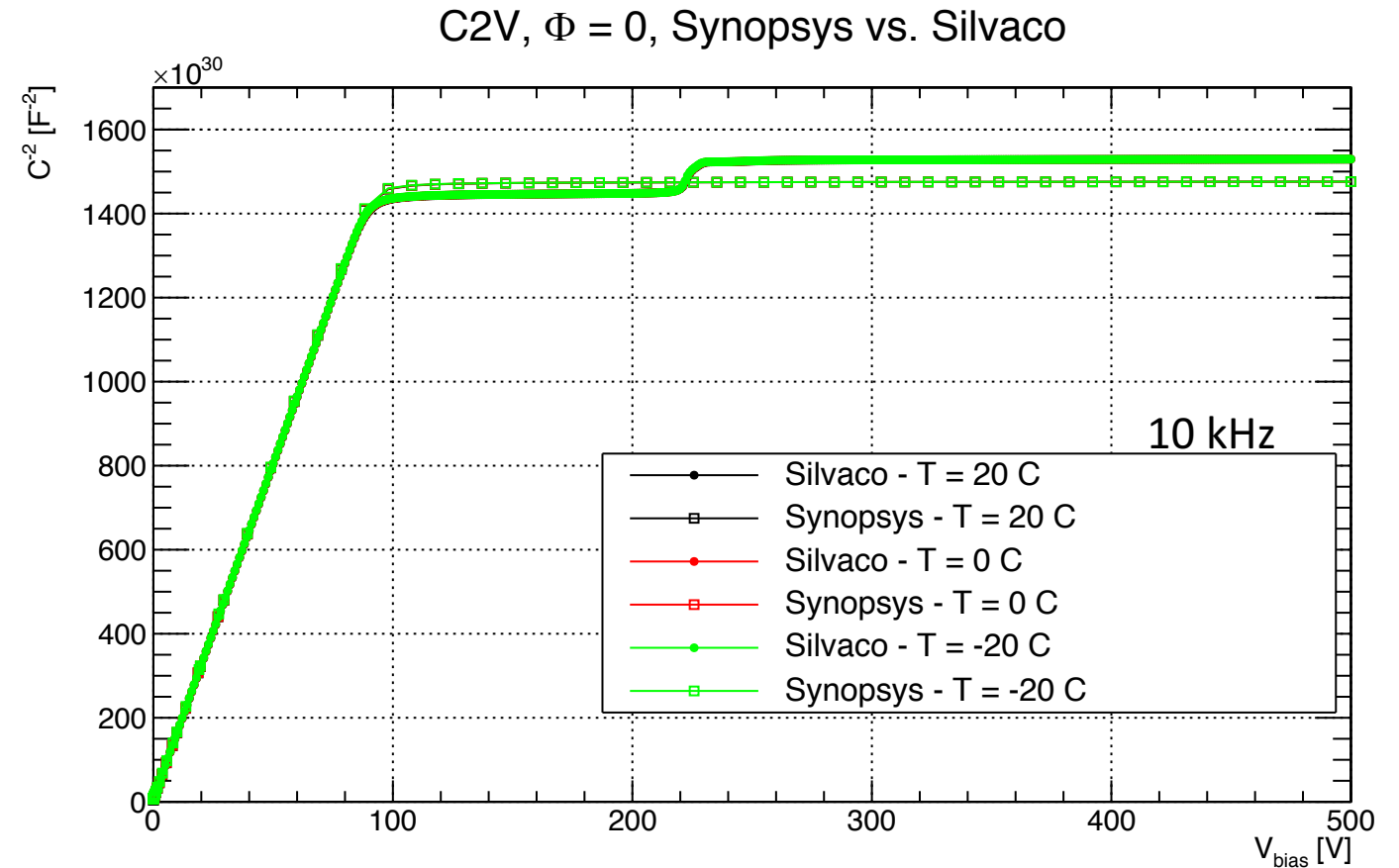
- Klaassen model

Want to cross-check physics models one by one across the two simulators in the future!

# First tests

## Not-irradiated structure – CV curves

- comparing CV curves at various temperatures
  - no temperature dependence between -20°C and 20°C
- Synopsys vs. Silvaco
  - rising edge matches perfectly
  - step in plateau observed with Silvaco but not with Synopsys
    - but agreement in the important (pre)-depletion region is at % level



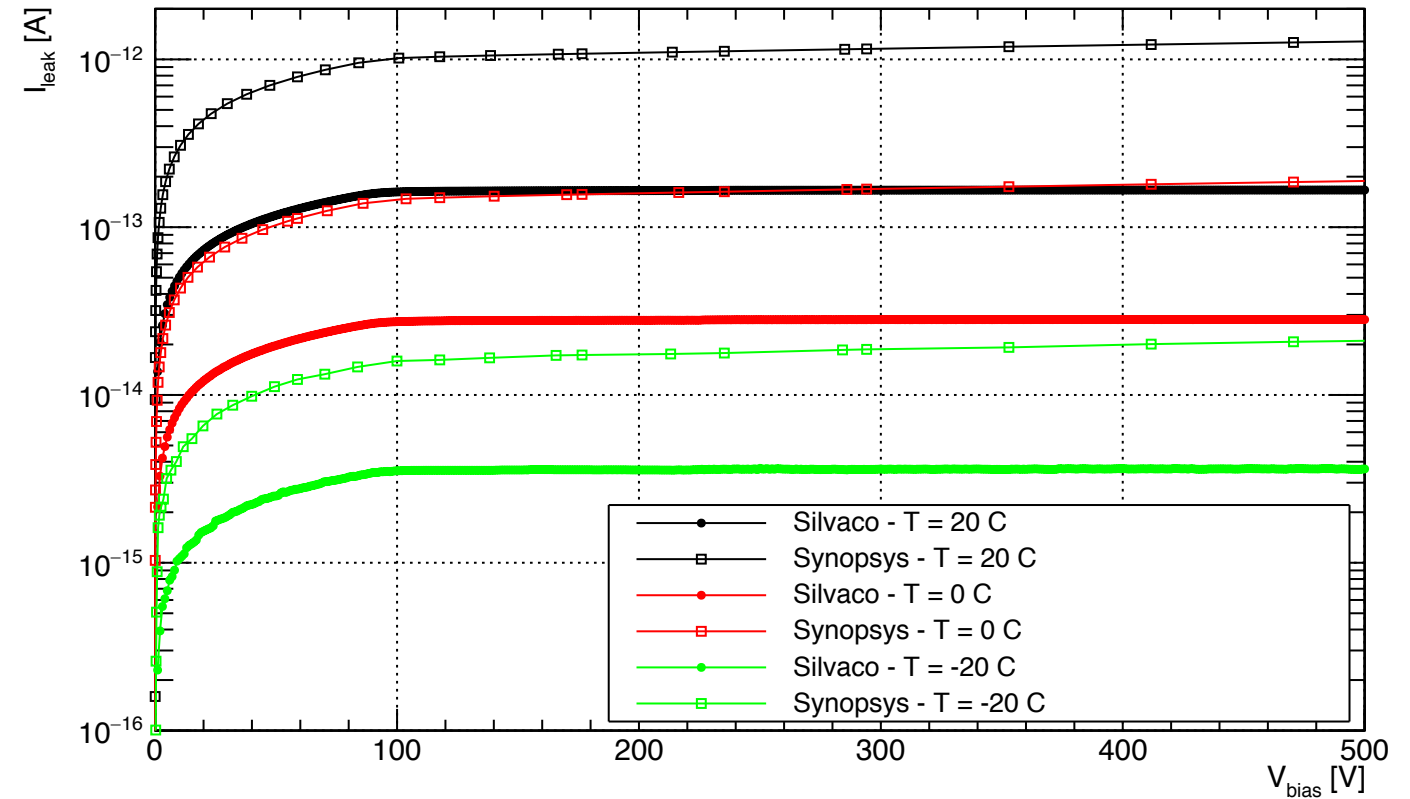


# First tests

## Not-irradiated structure – IV curves

- comparing IV curves at different temperatures
- Synopsys vs. Silvaco
  - Synopsys predicts slightly increasing plateau current
  - differences between Silvaco and Synopsys increase with increasing temperature
  - big difference in predicted plateau
    - what is the cause?

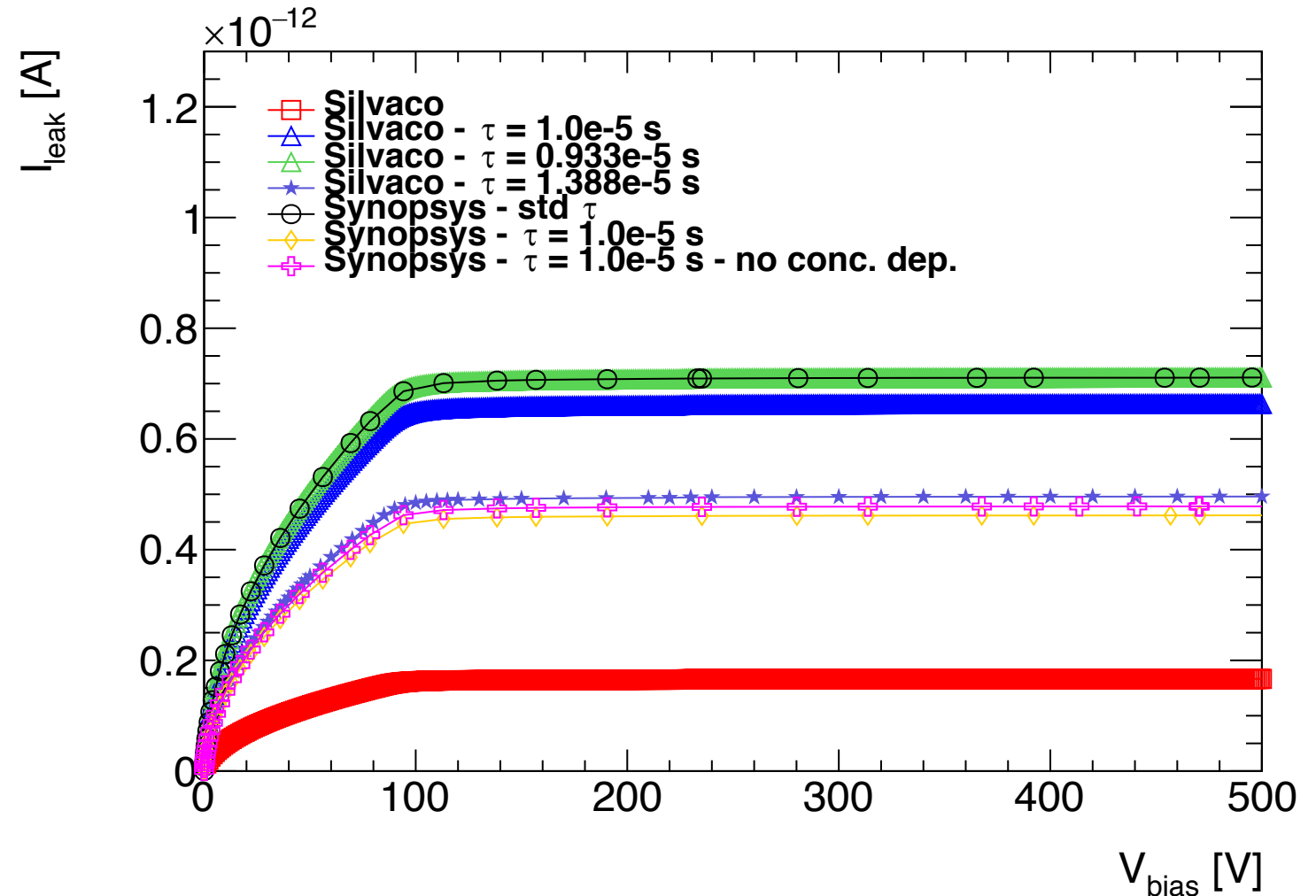
IV,  $\Phi = 0$ , Synopsys vs. Silvaco



# First tests

Not-irradiated structure – IV curves, closer look

- comparing IV curves at 20°C, vary the carrier lifetime  $\tau$
- can join the two simulators by artificially changing the carrier lifetime
- the differences in default  $\tau$  between Silvaco and Synopsys shouldn't matter after irradiation



# Irradiated Structure – $1 \times 10^{15} n_{eq} \text{cm}^{-2}$

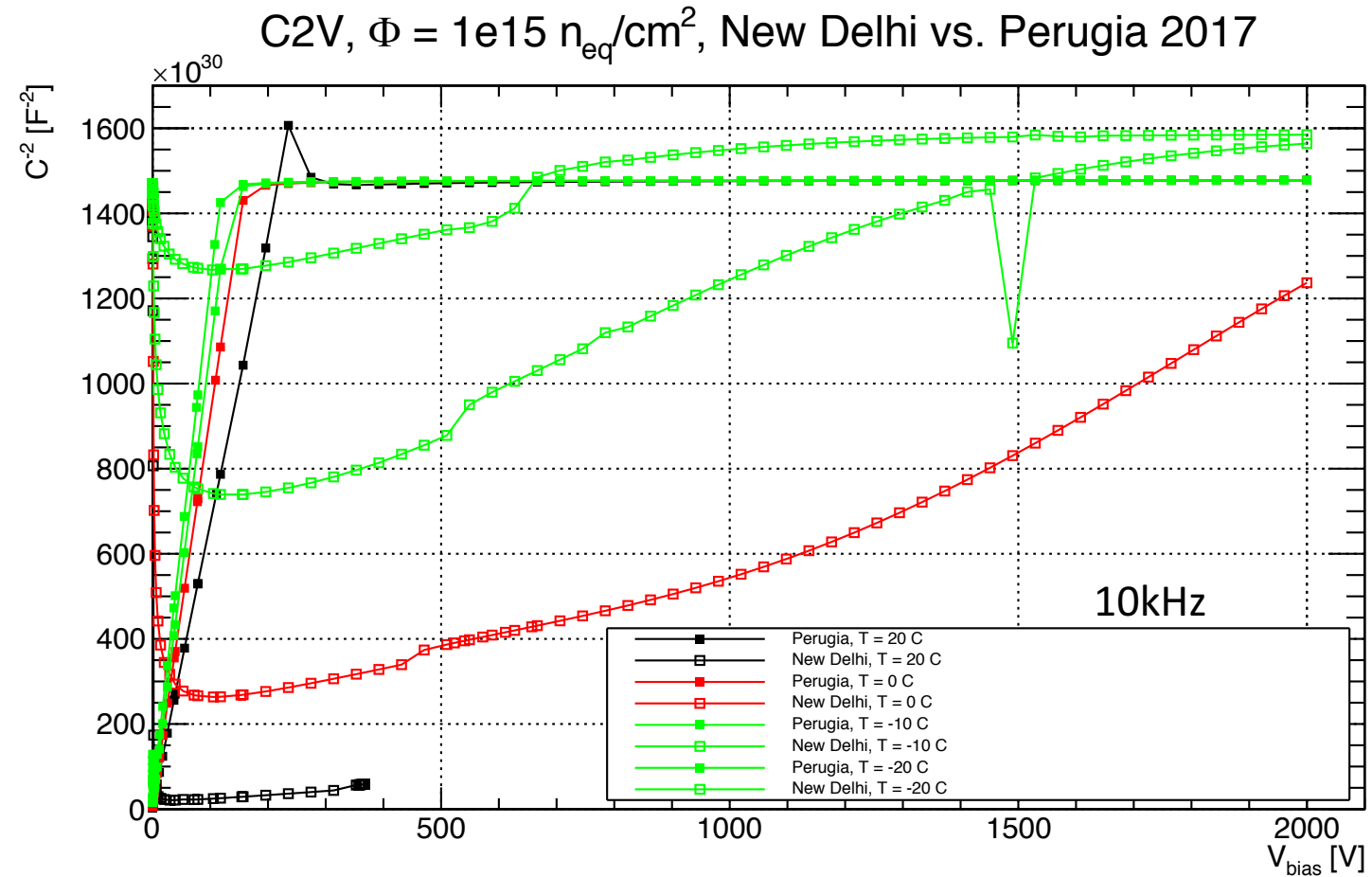
1.comparing Perugia and New Delhi models (Synopsys)

2.comparing Synopsys and Silvaco (Perugia model)

# Comparison of models - Synopsys

Irradiated structure – CV curves

- comparing CV curves at various temperatures
  - depletion with Perugia 2017 in a reasonable range of 100-200V
  - small temperature dependence
- depletion with New Delhi at 650 - >>2000V bias voltage
- huge temperature dependence
  - expected given the energy levels are much closer to the intrinsic level than in Perugia model

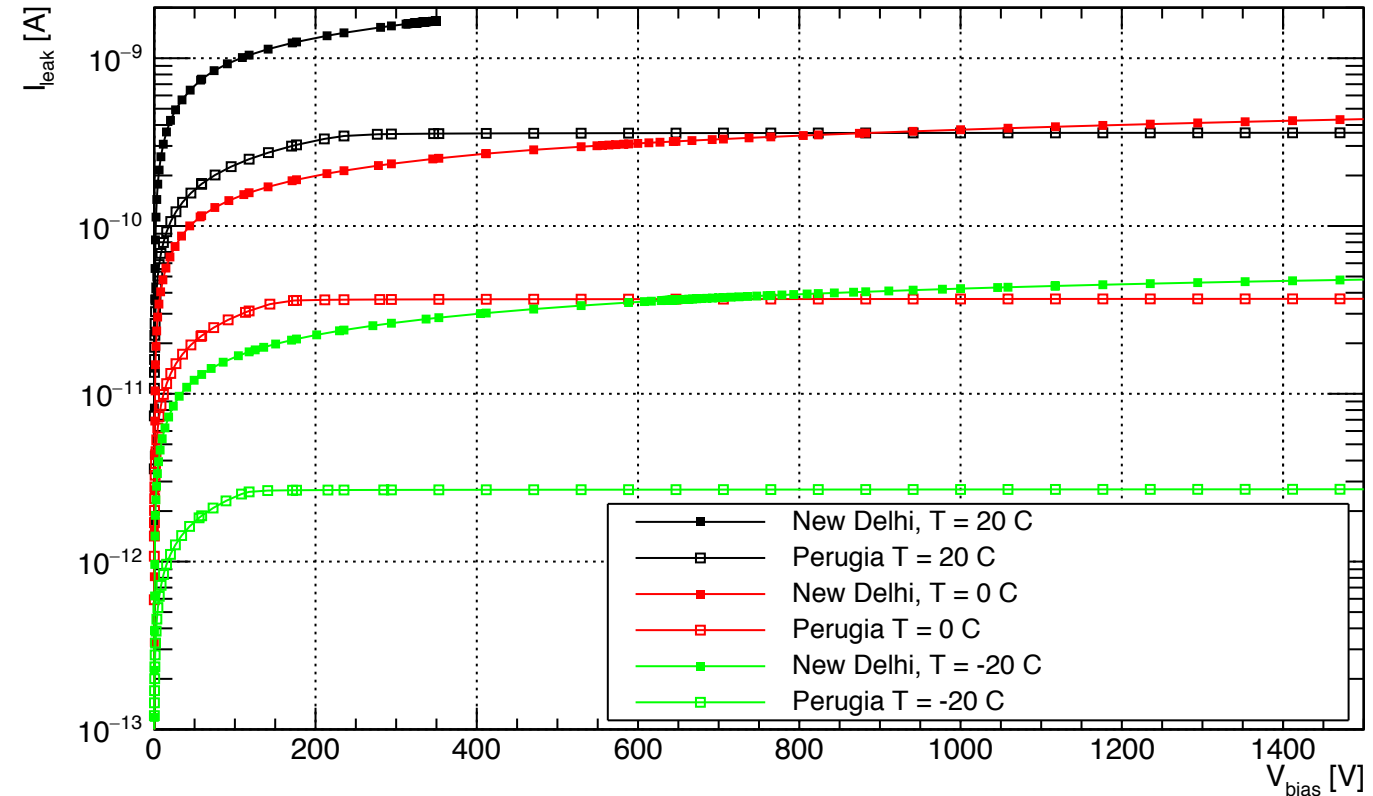


# Comparison of models - Synopsys

Irradiated structure – IV curves

- comparing IV curves at various temperatures
  - significantly higher current with New Delhi model
  - New Delhi predicts increasing plateau current, should be due to no depletion yet
  - differences between the models get smaller for increasing temperature

IV,  $\Phi = 1e15 n_{eq}/cm^2$ , New Delhi vs. Perugia 2017

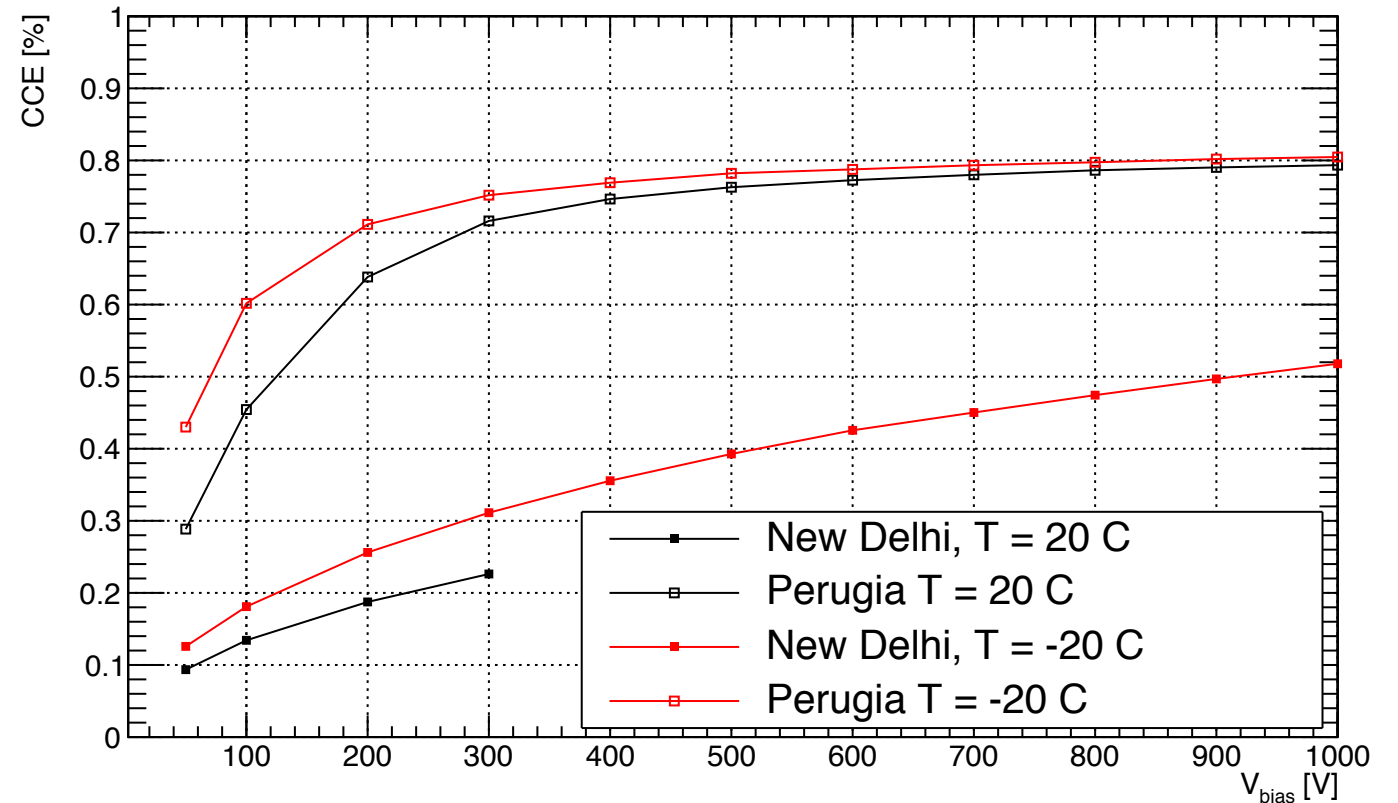


# Comparison of models - Synopsys

Irradiated structure – charge collection efficiency

- comparing CCE at different temperatures
  - temperature dependence for Perugia model mainly in the rising edge in agreement with depletion voltage variation
  - New Delhi model seems to exhibit more difference for higher bias voltages
- comparing New Delhi and Perugia 2017 model
  - significantly less charge collected using New Delhi model
    - plateau is not yet reached at 1000V
    - reason: bulk not yet depleted ( $C^{-2}V$ )

CCE,  $\Phi = 1e15 n_{eq}/cm^2$ , New Delhi vs. Perugia 2017



# Irradiated Structure – $1 \times 10^{15} n_{eq} \text{cm}^{-2}$

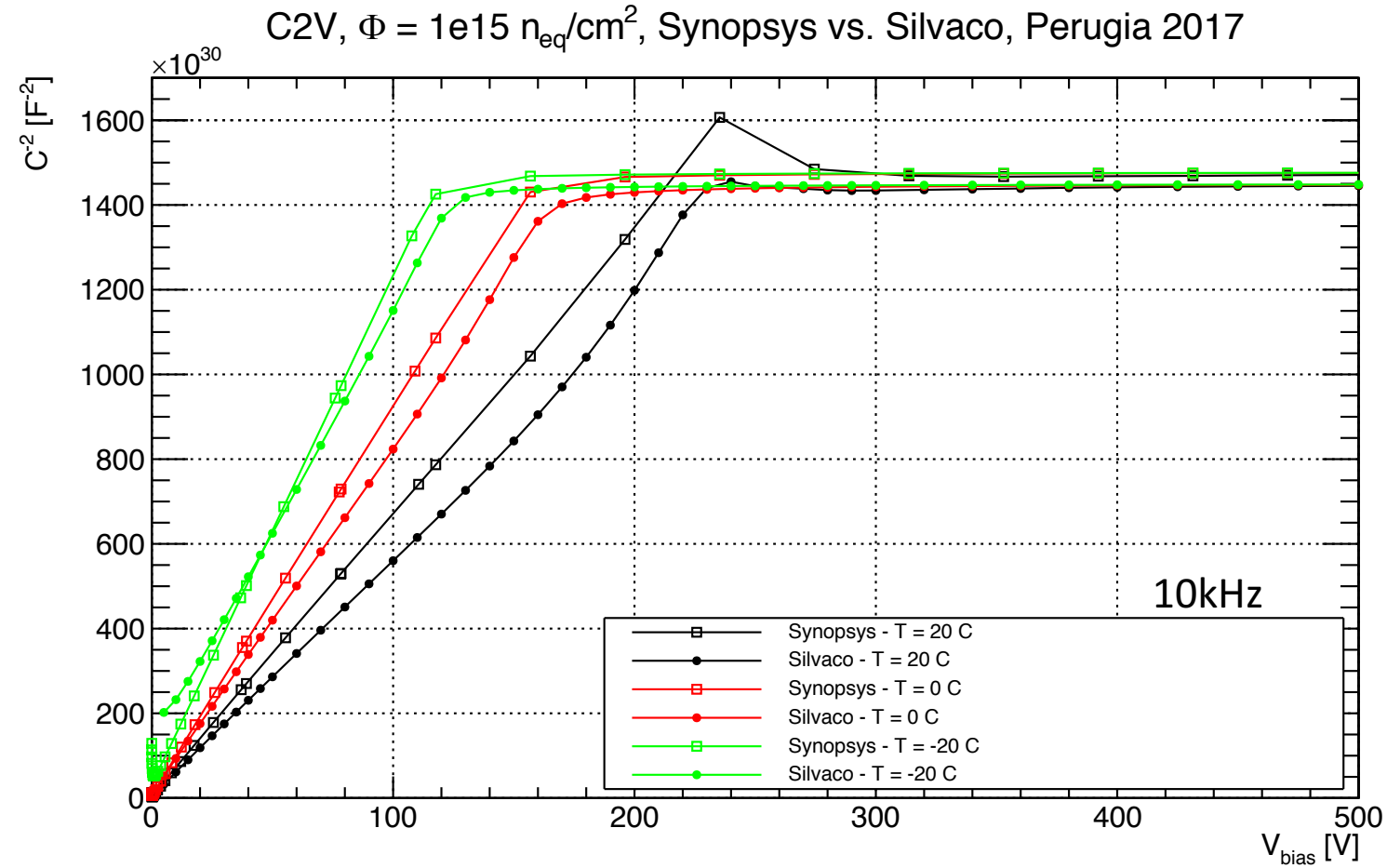
1.comparing Perugia and New Delhi models (Synopsys)

2.comparing Synopsys and Silvaco (Perugia model)

# Comparison of Simulators - Perugia

Irradiated structure – CV curves

- compare CV curves from both simulators at different temperatures
  - overall good agreement between Synopsys and Silvaco
  - differences increasing with increasing temperature
  - difference is between 10V – 30V



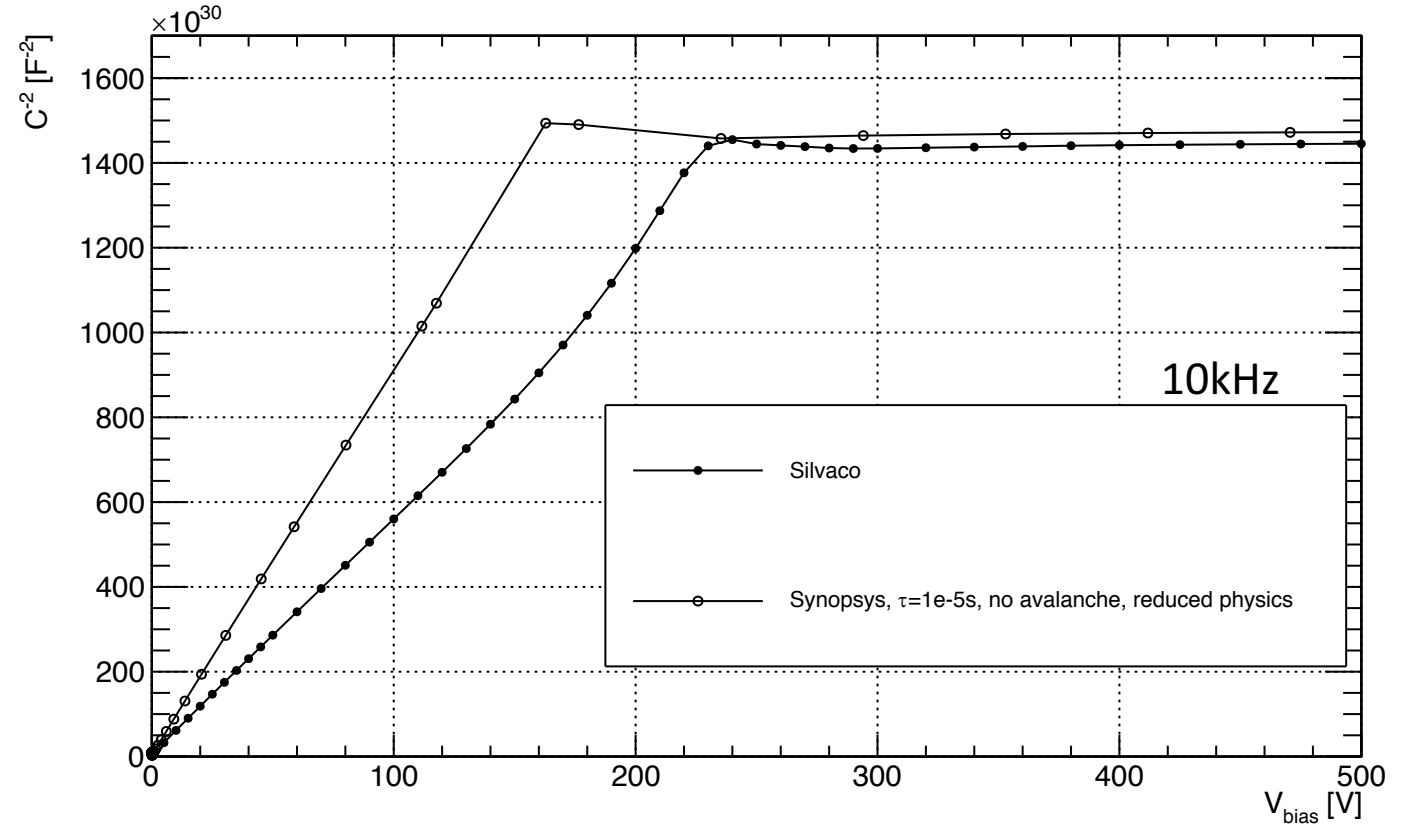


# Comparison of Simulators - Perugia

Irradiated structure – closer look: CV curves

- investigating the impact of physics models
  - start with Synopsys reduced physics and adapted carrier lifetime to match IV not-irr

C2V,  $\Phi = 1e15$ ,  $T = 20C$ , Perugia 2017



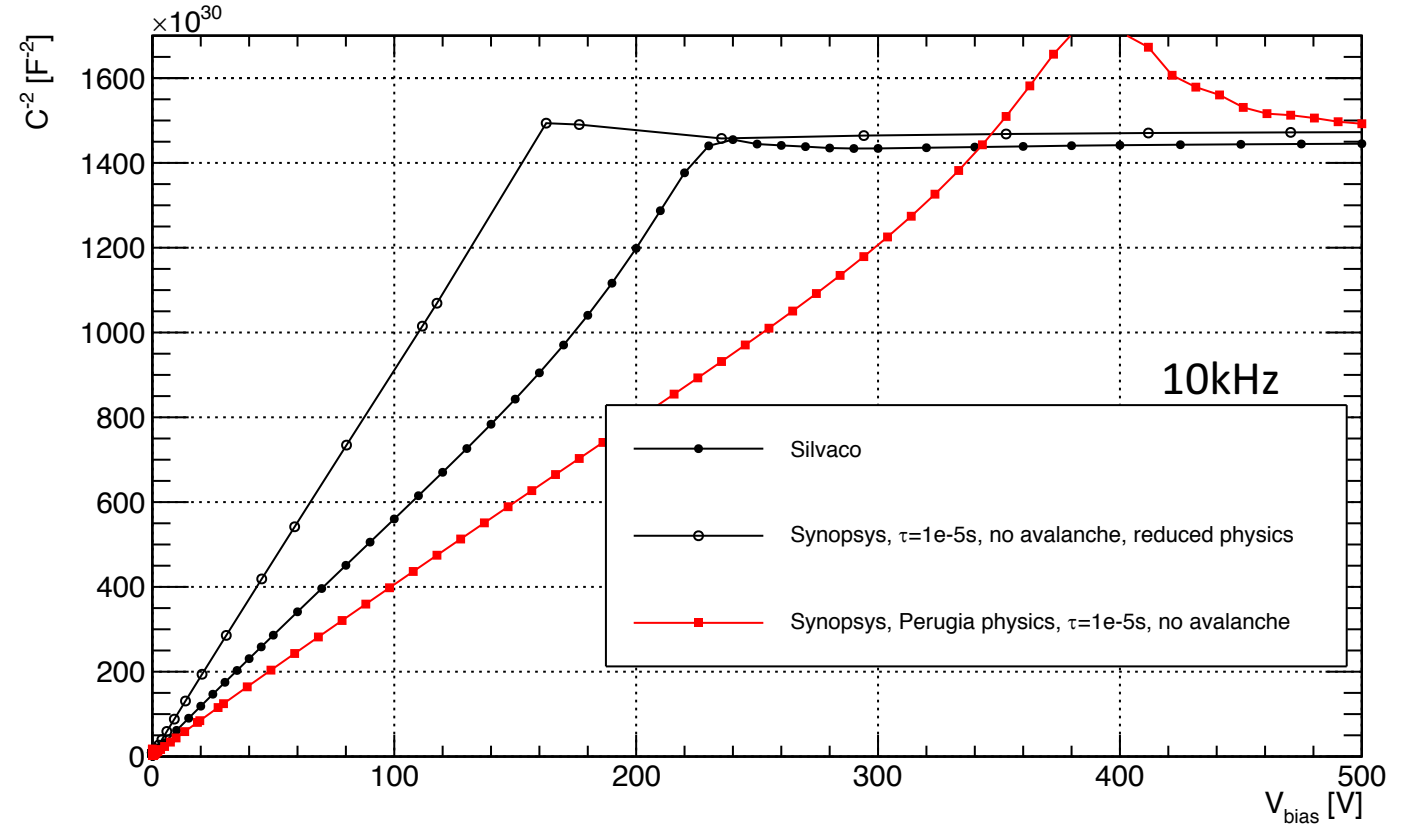
| Tool           | Silvaco | Synopsys |
|----------------|---------|----------|
| $V_{depl}$ [V] | ~ 240   | ~ 160    |

# Comparison of Simulators - Perugia

Irradiated structure – closer look: CV curves

- investigating the impact of physics models
  - start with Synopsys reduced physics and adapted carrier lifetime to match IV not-irr
  - use advanced physics models as used by the Perugia group

C2V,  $\Phi = 1e15$ ,  $T = 20C$ , Perugia 2017



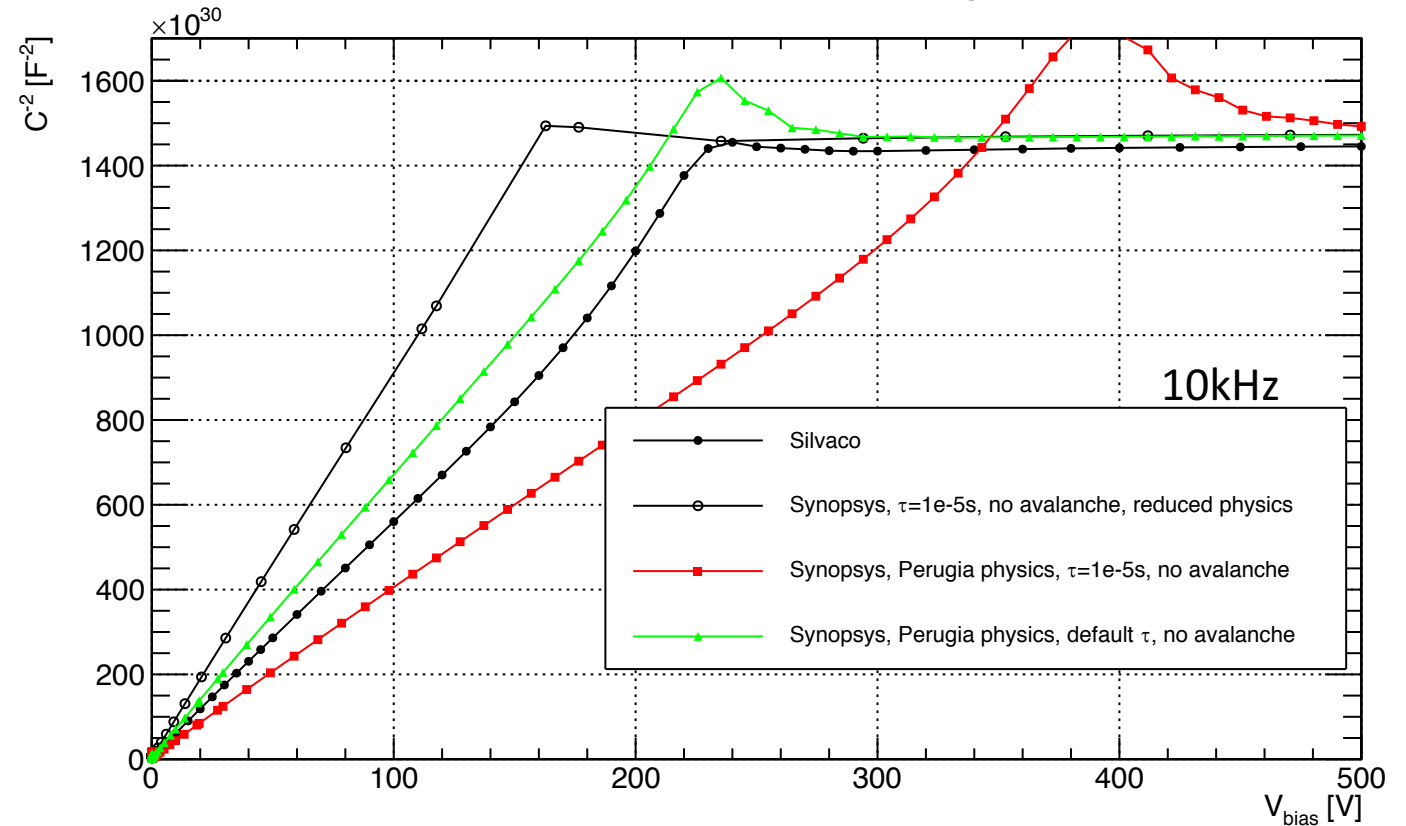
| Tool           | Silvaco | Synopsys | +physics |
|----------------|---------|----------|----------|
| $V_{depl}$ [V] | ~ 240   | ~ 160    | ~400V    |

# Comparison of Simulators - Perugia

Irradiated structure – closer look: CV curves

- investigating the impact of physics models
  - start with Synopsys reduced physics and adapted carrier lifetime to match IV not-irr
  - use advanced physics models as used by the Perugia group
  - use the default carrier lifetime again

C2V,  $\Phi = 1e15$ ,  $T = 20C$ , Perugia 2017



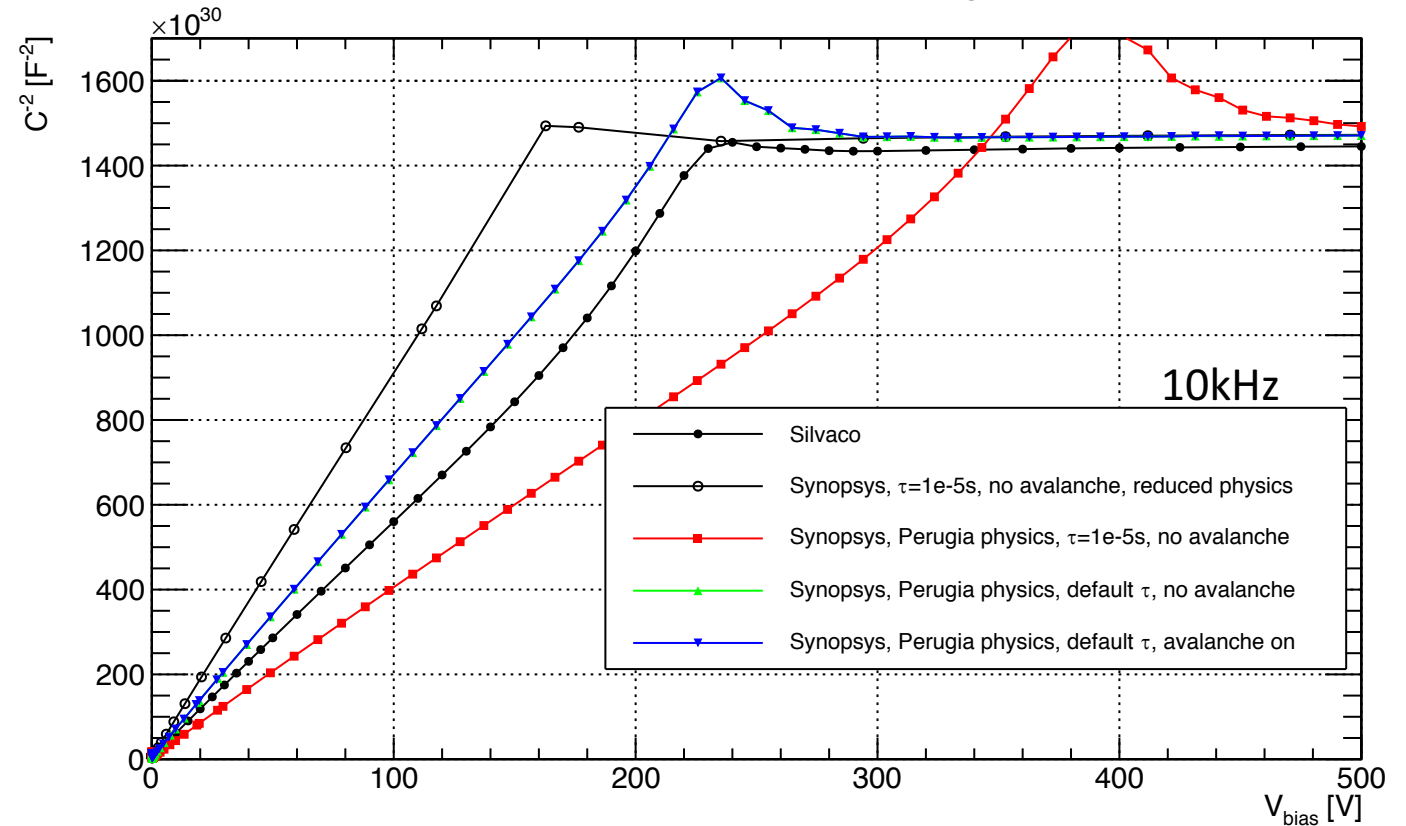
| Tool           | Silvaco | Synopsys | +physics | +default $\tau$ |
|----------------|---------|----------|----------|-----------------|
| $V_{depl}$ [V] | ~ 240   | ~ 160    | ~400V    | ~220            |

# Comparison of Simulators - Perugia

Irradiated structure – closer look: CV curves

- investigating the impact of physics models
  - start with Synopsys reduced physics and adapted carrier lifetime to match IV not-irr
  - use advanced physics models as used by the Perugia group
  - use the default carrier lifetime again
  - add avalanche

C2V,  $\Phi = 1e15$ ,  $T = 20C$ , Perugia 2017



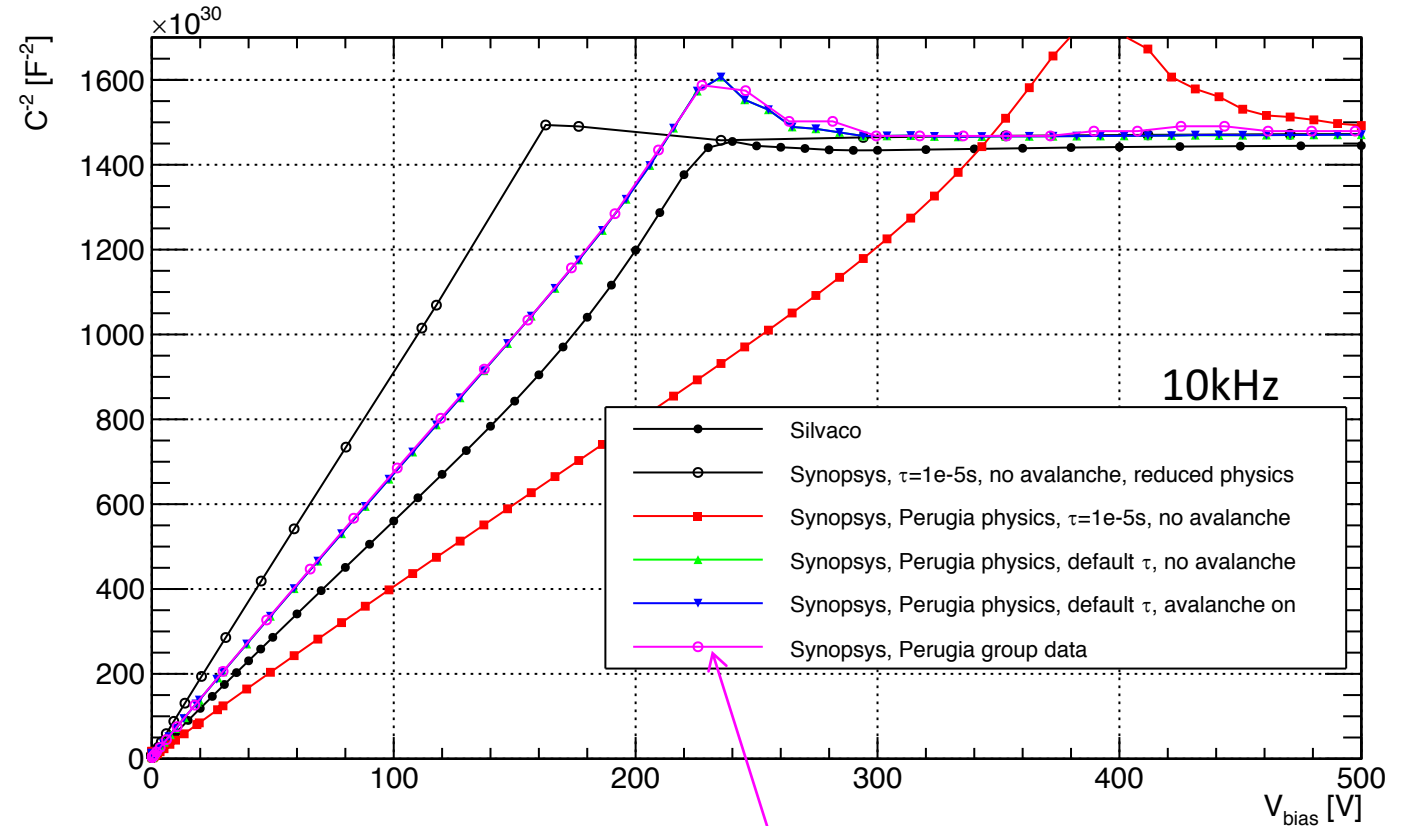
| Tool           | Silvaco | Synopsys | +physics | +default $\tau$ |
|----------------|---------|----------|----------|-----------------|
| $V_{depl}$ [V] | ~ 240   | ~ 160    | ~400V    | ~220            |

# Comparison of Simulators - Perugia

Irradiated structure – closer look: CV curves

- investigating the impact of physics models
  - start with Synopsys reduced physics and adapted carrier lifetime to match IV not-irr
  - use advanced physics models as used by the Perugia group
  - use the default carrier lifetime again
  - add avalanche
  - compare to data simulated by the Perugia group

C2V,  $\Phi = 1e15$ ,  $T = 20C$ , Perugia 2017



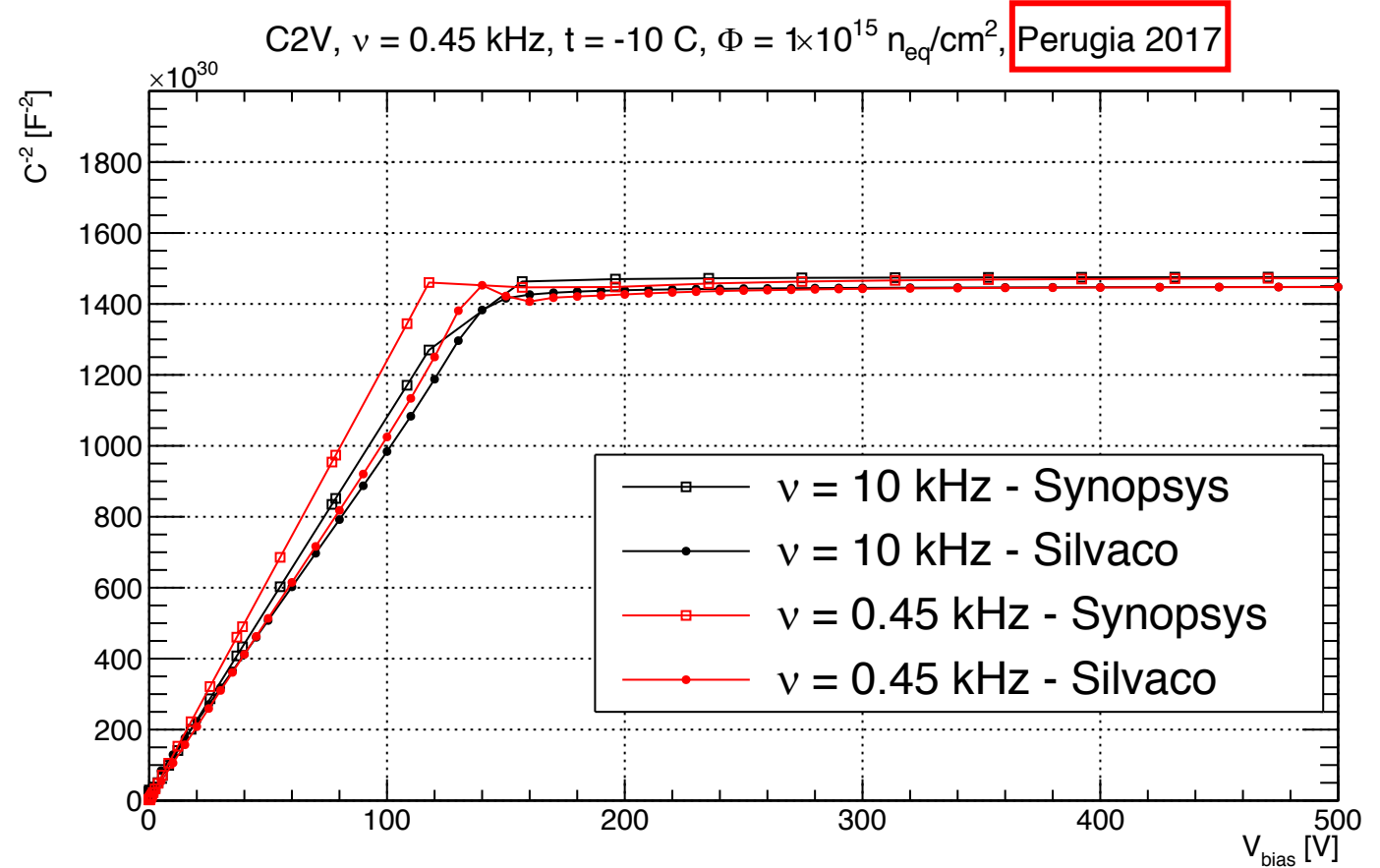
Cfr. Bomben, 28<sup>th</sup> RD50 WS, Torino, June 2016

| Tool           | Silvaco | Synopsys | +physics | +default $\tau$ |
|----------------|---------|----------|----------|-----------------|
| $V_{depl}$ [V] | ~ 240   | ~ 160    | ~400V    | ~220            |

# Comparison of Simulators - Perugia

Irradiated structure – influence of frequency on CV

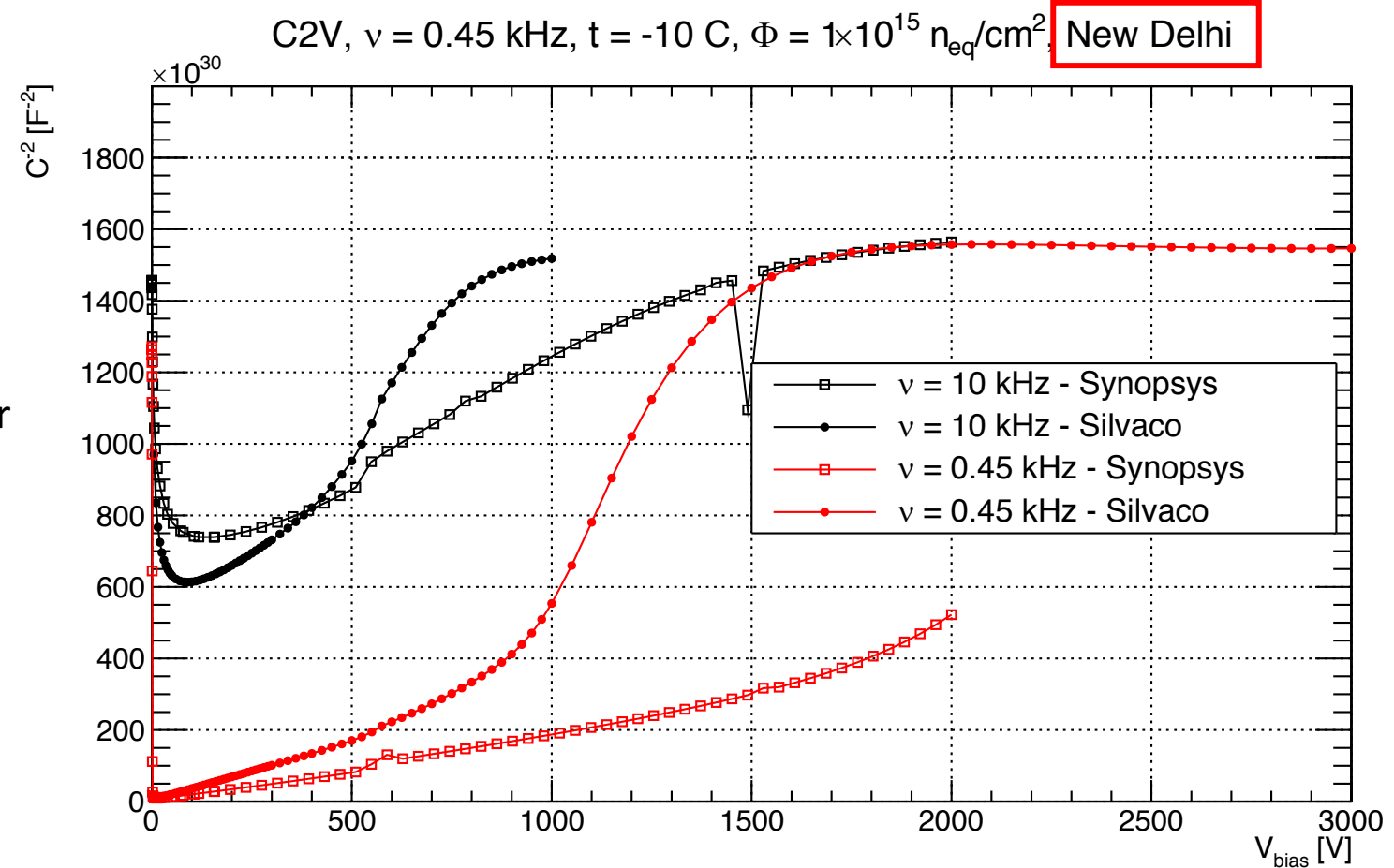
- compare  $C^2V$  with the default 10kHz and 0.45kHz at  $-10^\circ\text{C}$  for both simulators
  - same trend of higher depletion voltage for higher frequency
  - smaller influence on Silvaco simulation
  - overall small influence only



# Comparison of Simulators – Delhi

Irradiated structure – influence of frequency on CV

- compare  $C^2V$  with the default 10kHz and 0.45kHz at  $-10^\circ\text{C}$  for both simulators
  - same trend of higher depletion voltage for lower frequency (opposite of Perugia)
  - smaller influence on Silvaco simulation
  - huge influence by frequency



# Comparison of Simulators - Perugia

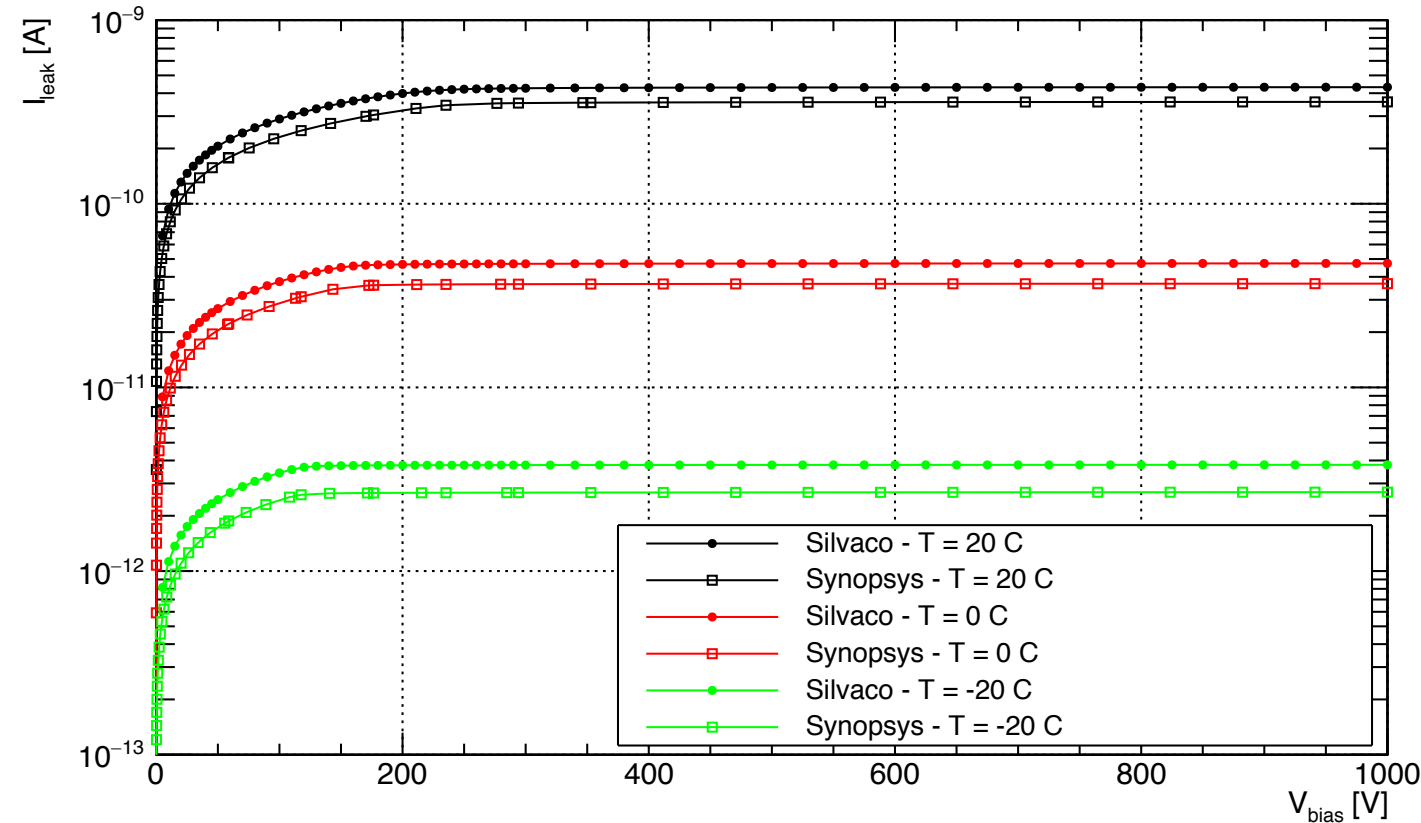
Irradiated structure – IV curves

- compare IV curves from both simulators at different temperatures
  - small difference between the two
  - current lower in Synopsys
  - constant ratio – difference could be due to temperature scaling

Evaluation of the current related damage rate  $\alpha$  at 20 C (no rescale for temperature needed) gives:

| Tool                        | Silvaco       | Synopsys      |
|-----------------------------|---------------|---------------|
| $\alpha$ [ $10^{-17}$ A/cm] | $4.2 \pm 0.1$ | $3.5 \pm 0.1$ |

IV,  $\Phi = 1e15 \text{ n}_{eq}/\text{cm}^2$ , Synopsys vs Silvaco, Perugia 2017

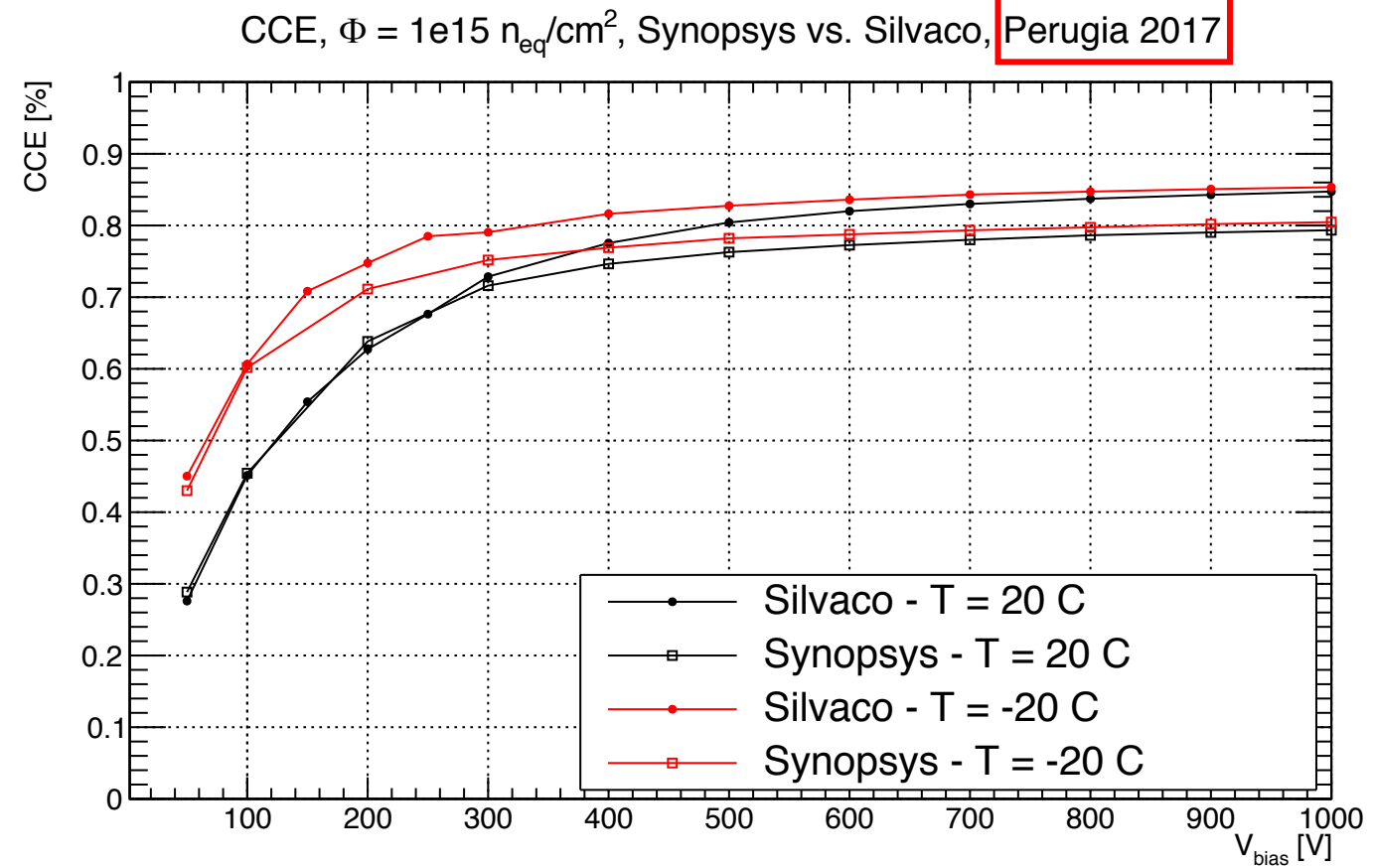




# Comparison of Simulators - Perugia

Irradiated structure – charge collection efficiency

- compare charge collection efficiency for Perugia model at -20°C and 20°C
- normalised to collected charge at 200V-500V, before irradiation
  - exact same rising edge
  - same temperature dependence
  - plateau efficiency different by ~5%

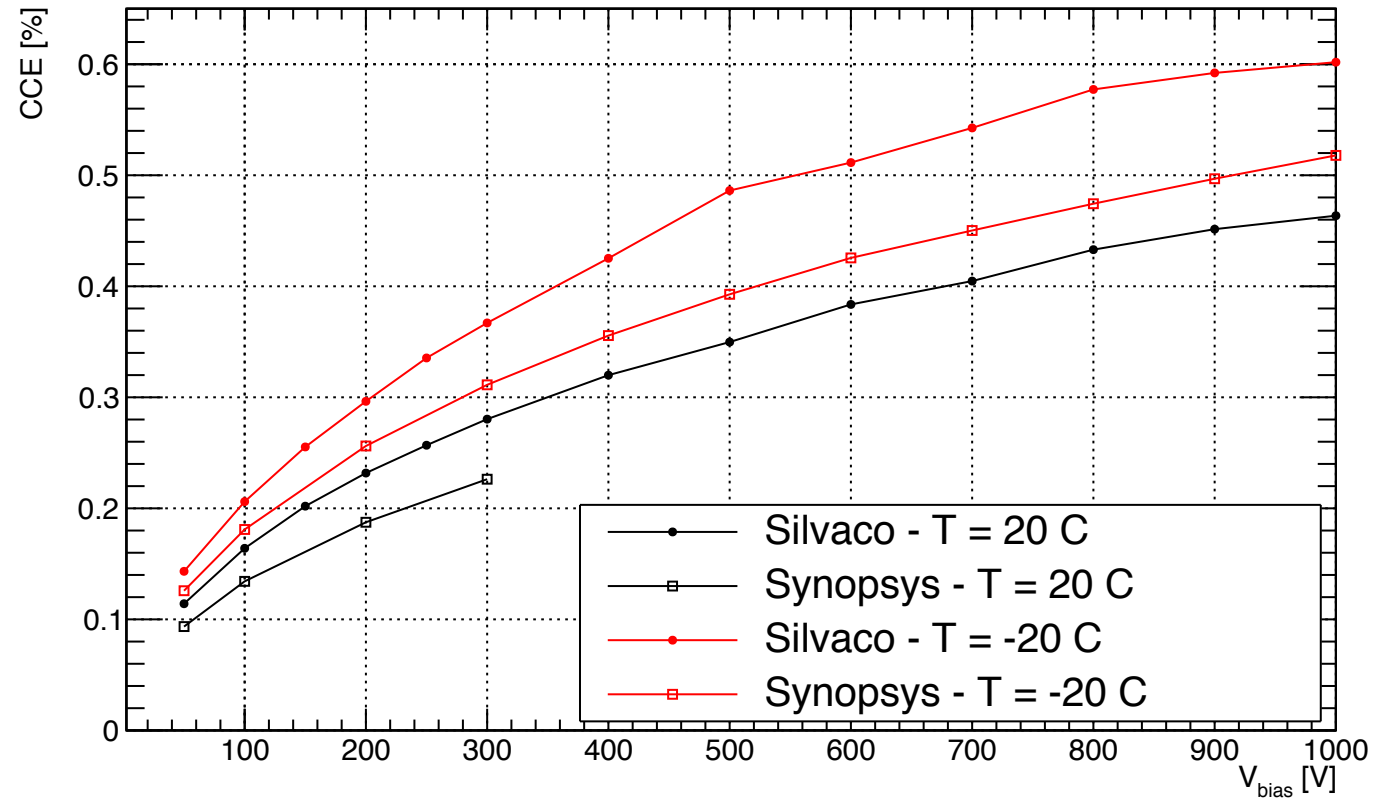


# Comparison of Simulators - Delhi

Irradiated structure – charge collection efficiency

- compare charge collection efficiency for New Delhi model at -20°C and 20°C
  - both do not reach a plateau
  - efficiency different by ~14% at 1000V

CCE,  $\Phi = 1e15 n_{eq}/cm^2$ , Synopsys vs. Silvaco, **New Delhi**



# Summary

1. Comparing New Delhi and Perugia 2017 radiation damage models
  - depletion voltage much higher and much larger temperature dependence using New Delhi model
  - higher currents and no saturation of current up to 1500V given the high depletion voltage
  - CCE is  $\sim 80\%$  for Perugia and  $\sim 50\%$  for New Delhi @ 1000V and  $1 \times 15 n_{eq}/cm^2$
2. Comparing Synopsys and Silvaco TCAD tools
  - CV agrees down to the % level before irradiation, after irradiation small differences with Perugia model
  - IV different before irradiation due to different  $\tau$  value, after irradiation close together, compatible with 2016 data
  - CCE in good agreement in the rising edge, plateau slightly different, difference is 5%-14%
3. Outlook:
  - project has just started, more cooperation planned
    - *DEFPIXELS* project, Embassy of France in Germany and DAAD Procope grant call
  - compare the physics models in more detail between the two simulators
  - more complex structures to spot higher order differences
  - compare avalanche models

Thank you for your attention!

# Backup