Next-to-Leading Order QCD Corrections to Inclusive Heavy-Flavor Production in Polarized Deep-Inelastic Scattering

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Introduction - Heavy Quarks (HQ)

- Heavy Quarks (HQ): $c(m_c = 1.5 \text{ GeV})$, $b(m_b = 4.75 \text{ GeV})$, $t(m_{t} = 175 \, \text{GeV})$
- EIC will reach region with HQ relevant to structure functions
- compare unpolarized case HERA@DESY: at small $x \sim 30\%$ charm contributions [Laenen, Riemersma, Smith, van Neerven]





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- measure ∆g as dominated by photon-gluon fusion (PGF)
- first full NLO computation of polarized process [Blümlein, Bojak, Stratmann]
- need improved charm tagging
- fully inclusive cross section is complicated to reconstruct
- no hadronization here

■ scale of hard process is in a pertubative regime m > Λ_{QCD}

■ finite mass *m* provides total cross sections





- scale of hard process is in a pertubative regime m > Λ_{QCD}
- finite mass m provides total cross sections
- full m² dependence makes computations complicated: phase space + matrix elements
- 2-scale problem: $\ln\left(\frac{s-4m^2}{4m^2}\right)$ and/or $\ln(Q^2/m^2)$
- keep analytic expressions





Introduction - DIS Setup

(q)

 $g(k_1)$

00

 $e^{-}(l_{1})$

h(p)

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- use factorisation theorem: PDF and $s = \xi S_h$
- PGF: $g(k_1) + \gamma^*(q) \rightarrow \overline{Q}(p_2) + Q(p_1)$
- three massive particles: $m^2 > 0, q^2 = -Q^2 < 0$



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- **compute 2-to-3-phase space: e.g.** $dPS_3 \sim dt_1 du_1 d\Omega_n d\hat{I}$ [Laenen, Bojak]



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- **u** compute 2-to-3-phase space: e.g. $dPS_3 \sim dt_1 du_1 d\Omega_n d\hat{\mathcal{I}}$ [Laenen, Bojak]
- γ_5 and $\varepsilon_{\mu\nu\rho\sigma}$ in *n*-dimension? \rightarrow HVBM scheme ['t Hooft, Veltman, Breitenlohner, Maison]

Computation Review - Collinear Poles

collinear poles appear in, e.g.,

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remove by mass factorization $\rightarrow \overline{\text{MS}}$ $\Rightarrow g_1 \sim e_H^2 \cdot \Delta g \otimes \ln(\mu_F^2/m^2) \bar{c}_{P,g}^{F,(1)}$ $\bar{c}_{P,g}^{F,(1)}(\chi, \chi_q) = c_1(\chi, \chi_q) \ln(\chi) + c_2(\chi, \chi_q) \operatorname{Li}_2\left(\frac{1-\chi_q}{1+\chi}\right) + \dots (\checkmark \text{ for } Q^2 \gg m^2 \text{ [Buza,Matiounine,Smith,van Neerven]})$

Computation Review - UV and IR Poles

virtual diagrams are, e.g.,

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soft poles appear in the limit of a soft gluon, e.g.,



soft + virtual + renormalization (\overline{MS}_m) + factorization is finite! [Laenen, Bojak]

Computation Review - Analytic Expressions

$$D_{0}(m^{2}, 0, q^{2}, m^{2}, t, s, 0, m^{2}, m^{2}, m^{2}) = \frac{iC_{\epsilon}}{\beta s t_{1}} \times \left[-\frac{2}{\epsilon} \ln(\chi) - 2\ln(\chi) \ln\left(\frac{-t_{1}}{m^{2}}\right) + \text{Li}_{2}(1-\chi^{2}) - 4\zeta(2) + \ln^{2}(\chi_{q}) + 2\text{Li}_{2}(-\chi\chi_{q}) + 2\text{Li}_{2}\left(\frac{-\chi}{\chi_{q}}\right) + 2\ln(\chi\chi_{q}) \ln(1+\chi\chi_{q}) + 2\ln\left(\frac{\chi}{\chi_{q}}\right) \ln\left(1+\frac{\chi}{\chi_{q}}\right) \right]$$

$$\int \frac{d\Omega_n}{t' u_7^2} = -\frac{2\pi (m^2 + s_4)(s' + t_1)}{s_4 t_1^2 u_1^2} \left[-2 + \frac{t_1 u_1 (-q^2 s_4 + (2m^2 + s_4)(s' + u_1))}{(s' + t_1) (q^2 s_4 t_1 + m^2 (s' + u_1)^2)} + \frac{2}{\epsilon} + \ln \left(\frac{t_1^2 u_1^2 (m^2 + s_4)}{(s' + t_1)^2 (m^2 (s' + u_1)^2 + q^2 t_1 s_4)} \right) \right]$$

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Computation Review - Analytic Expressions

$$D_{0}(m^{2}, 0, q^{2}, m^{2}, t, s, 0, m^{2}, m^{2}, m^{2}) = \frac{iC}{\beta s}$$

$$+ \text{Li}_{2}(1 - \chi^{2}) - 4\zeta(2) + \ln^{2}(\chi_{q}) + 2 \text{Li}_{2}(-)$$

$$+ 2 \ln(\chi\chi_{q}) \ln(1 + \chi\chi_{q}) + 2 \ln\left(\frac{\chi}{\chi_{q}}\right) \ln\left(\frac{1}{2}\right)$$

$$\int \frac{d\Omega_{n}}{t'u_{7}^{2}} = -\frac{2\pi(m^{2} + s_{4})(s' + t_{1})}{s_{4}t_{1}^{2}u_{1}^{2}} \left[-2 + \frac{2}{\epsilon} + \ln\left(\frac{t_{1}^{2}u_{1}^{2}(m^{2} + s_{4})}{(s' + t_{1})^{2}(m^{2}(s' + u_{1})}\right)\right]$$

$$OOO, I'VE THOUGHT OF A NEW ONE! TWO SQUIEGELES AND A BACKWARDS 6!$$

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Partonic Results - Gluon Channel





f I polarized \sim unpolarized near threshold, but not at high energy

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Partonic Results - Light Quark Channel

$$g_{1} \sim \alpha_{s}^{2} \sum_{q} \left(\Delta q + \Delta \bar{q} \right) \otimes \left(e_{H}^{2} \left[c_{P,q}^{(1)} + \ln \left(\frac{\mu_{F}^{2}}{m^{2}} \right) \bar{c}_{P,q}^{(1)} \right] + e_{q}^{2} d_{P,q}^{(1)} \right)$$

• no interference term $\sim e_H e_q$

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- Compton subprocess contains $\ln(Q^2/m^2)$
 - Felix Hekhorn NLO HQ structure function in DIS

Hadronic Results - Unpolarized vs. Polarized



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Hadronic Results - PDF Uncertainties DSSV (I)



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Hadronic Results - PDF Uncertainties DSSV (II)



•
$$A_1^c(x, Q^2) = \frac{g_1^c(x, Q^2)}{F_1^c(x, Q^2)}$$

 error band are only due to DSSV uncertainties (no correlations!)



Hadronic Results - PDF Uncertainties DSSV (II)



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•
$$A_1^c(x, Q^2) = \frac{g_1^c(x, Q^2)}{F_1^c(x, Q^2)}$$

- error band are only due to DSSV uncertainties (no correlations!)
- sign unconstrained
- need measurement of $\mathcal{O}(10^{-3})$

 $\blacksquare \text{ NLO} \lessapprox \texttt{LO}$



$$\mu_F^2 = \mu_R^2 = 10^a \mu_0^2$$
 with $\mu_0^2 = 4m^2 + Q^2$

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Hadronic Results - Scale Uncertainties (II)



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Outlook

inclusive distributions:
 ^{dg1}/_{dp7,\bar{a}},
 ^{dg1}/_{dy\bar{a}}, ... [Laenen, Riemersma, Smith, van Neerven]

 correlated distributions:
 ^{dg1}/_{dM²\bar{a\bar{a}}},
 ^{dg1}/_{d\bar{a\bar{a}}}, TMD, ... [Harris, Smith]





Outlook

- **inclusive distributions:** $\frac{dg_1}{dp_{T,\bar{Q}}}, \frac{dg_1}{dy_{\bar{Q}}}, \dots$ [Laenen,Riemersma,Smith,van Neerven]
- correlated distributions: $\frac{dg_1}{dM_{Q\bar{Q}}^2}, \frac{dg_1}{d\phi_{Q\bar{Q}}}, \text{TMD}, \dots$ [Harris, Smith]
- full neutral current (NC) contributions: $F_3^{Z\gamma}, g_4^{Z\gamma}, g_5^{Z\gamma}$ and F_2^Z, F_L^Z, g_1^Z

■ distributions of full NC structure functions: $\frac{dg_1^{NC}}{dp_{T,\bar{Q}}}, \frac{dg_1^{NC}}{dM_{Q\bar{Q}}^2}, \dots$

Outlook

- inclusive distributions: $\frac{dg_1}{dp_{\tau \bar{O}}}, \frac{dg_1}{dy_{\bar{O}}}, \dots$ [Laenen, Riemersma, Smith, van Neerven]
- **correlated distributions:** $\frac{dg_1}{dM_{O\bar{O}}^2}, \frac{dg_1}{d\phi_{Q\bar{O}}}, \text{TMD}, \dots$ [Harris, Smith]
- full neutral current (NC) contributions: $F_3^{Z\gamma}, g_4^{Z\gamma}, g_5^{Z\gamma}$ and F_2^Z, F_L^Z, g_1^Z
- distributions of full NC structure functions: $\frac{dg_1^{NC}}{dp_{\tau \bar{Q}}}, \frac{dg_1^{NC}}{dM_{Q\bar{Q}}^2}, \dots$

Thank you for your attention!





Backup: Partonic Results - Gluon Channel



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Backup: Partonic Results - Light Quark Channel



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Backup: Hadronic Results - PDF Uncertainties DSSV



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Backup: Hadronic Results - Mass Variation



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