Polarization from hadronic to heavy-ion collisions

Dilepton Production with Meson and Antiptoton Beams November 9, 2017

ECT*, Trento

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- Phys.Rev. C88 (2013) 061901, C93 (2016) 031902, C95 (2017) 011902, ArXiv 1701.00923, 1705.0165

Main Topics

- Polarization: from nucleons to ions
- Anomalous mechanism: 4-velocity as gauge field
- Chemical potential and Energy dependence
- Rotation in heavy-ion collisions: Vortical structures
- Polarization of hyperons
- Tensor polarization of dileptons
- Conslusions

Tensor polarization (alignment)

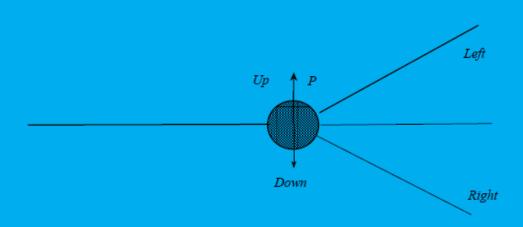
T and P even

 Virtual photon (or vector mesons): directly revealed in angular distributions of dileptons

 5 elements of spin-1 density matrix (traceless symmetric tensor)

Single Spin Asymmetries (vector polarization)

Simplest example - (non-relativistic) elastic pion-nucleon scattering $\pi \vec{N} \to \pi N$



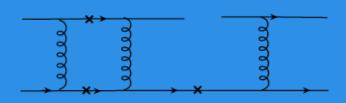
 $M = a + ib(\vec{\sigma}\vec{n}) \vec{n}$ is the normal to the scattering plane.

Density matrix: $\rho = \frac{1}{2}(1 + \vec{\sigma}\vec{P}),$

Differential cross-section: $d\sigma \sim 1 + A(\vec{P}\vec{n}), A = \frac{2Im(ab^*)}{|a|^2 + |b|^2}$

Perturbative PHASES IN QCD

QCD factorization: where to borrow imaginary parts? Simplest way: from short distances - loops in partonic subprocess. Quarks elastic scattering (like q - e scattering in DIS):

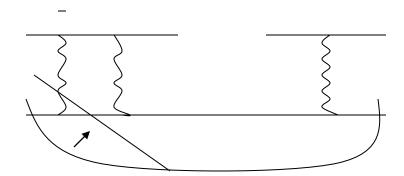


$$A \sim \frac{\alpha_S m p_T}{p_T^2 + m^2}$$

Large SSA "...contradict QCD or its applicability"

Short+ large overlap twist 3

- Quarks only from hadrons
- Various options for factorization shift of SH separation



- New option for SSA: Instead of 1-loop twist 2 Born twist 3 (quark-gluon correlator): Efremov, OT (85, Fermionic poles); Qiu, Sterman (91, GLUONIC poles -> T-odd Sivers function-talk of M. Anselmino)
- Further shift to large distances T-odd fragmentation functions

SSA

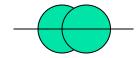
- Parity conservation normal to scattering plane (HIC – angular momentum)
- Interference LS coupling (HIChydrodynamical axial anomaly)
- T conservation absorptive phases (HIC : dissipation)
- QCD for hadrons quark-gluon correlations (twist 3)~ T-odd TMD

Λ-polarisation

- Self-analyzing in weak decay
- Directly related to s-quarks polarization: complementary probe of strangeness
- Widely explored in hadronic processes
- Disappearance-probe of QCD matter formation (Hoyer; Jacob, Rafelsky: '87): Randomization – smearing – no direction normal to the scattering plane

Global polarization

Global polarization normal to REACTION plane



- Predictions (Z.-T.Liang et al.): large orbital angular momentum -> large polarization
- Search by STAR (Selyuzhenkov et al.'07): polarization NOT found at % level!
- Maybe due to locality of LS coupling while large orbital angular momentum is distributed
- How to transform rotation to spin?

Magnetic field?

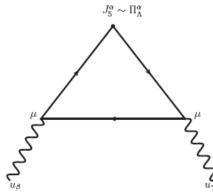
- Heavy-ion collisions fast charged particles - largest ever magnetic field (~m_π²)
- Magnetic moment -> polarization
- Field is typically increasing for large energies but polarization is observed by STAR (Nature 548 (2017) 62-65)at lower energies!

Anomalous mechanism – polarization similar to CM(V)E

• 4-Velocity is also a GAUGE FIELD (V.I. Zakharov et al): $\mu Q = \mu J_0 V^0 -> \mu J_y V^y$

$$e_j A_\alpha J^\alpha \Rightarrow \mu_j V_\alpha J^\alpha$$

- Triangle anomaly leads to polarization of quarks and hyperons (Rogachevsky, Sorin, OT '10)
- Analogous to anomalous gluon contribution to nucleon spin (Efremov,OT'88)
- 4-velocity instead of gluon field!



Anomaly for polarization

Induced axial charge

$$c_V = \frac{\mu_s^2 + \mu_A^2}{2\pi^2} + \frac{T^2}{6}, \quad Q_5^s = N_c \int d^3x \, c_V \gamma^2 \epsilon^{ijk} v_i \partial_j v_k$$

- Neglect axial chemical potential
- T-dependent term- related to gravitational anomaly
- Lattice simulation: suppressed due to collective effects

Energy dependence

Coupling -> chemical potential

$$Q_5^s = \frac{N_c}{2\pi^2} \int d^3x \, \mu_s^2(x) \gamma^2 \epsilon^{ijk} v_i \partial_j v_k$$

- Field -> velocity; (Color) magnetic field strength -> vorticity;
- Topological current -> hydrodynamical helicity
- Large chemical potential: appropriate for NICA/FAIR energies

One might compare the prediction below with the right panel figures

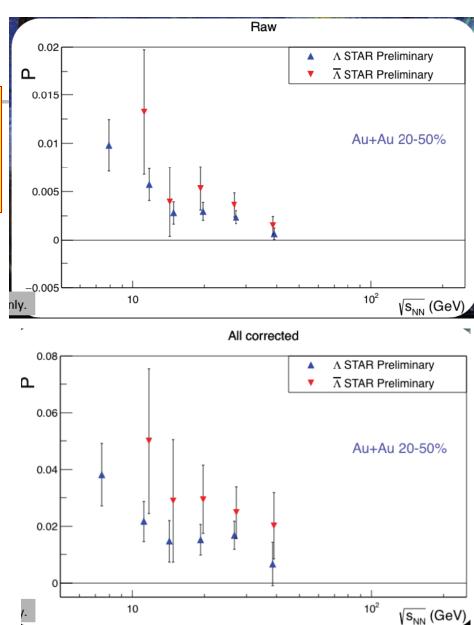
O. Rogachevsky, A. Sorin, O. Teryaev Chiral vortaic effect and neutron asymmetries in heavy-ion collisions PHYSICAL REVIEW C 82, 054910 (2010)

One would expect that polarization is proportional to the anomalously induced axial current [7]

$$j_A^{\mu} \sim \mu^2 \left(1 - \frac{2\mu n}{3(\epsilon + P)} \right) \epsilon^{\mu\nu\lambda\rho} V_{\nu} \partial_{\lambda} V_{\rho},$$
 (6)

where n and ϵ are the corresponding charge and energy densities and P is the pressure. Therefore, the μ dependence of polarization must be stronger than that of the CVE, leading to the effect's increasing rapidly with decreasing energy.

This option may be explored in the framework of the program of polarization studies at the NICA [17] performed at collision points as well as within the low-energy scan program at the RHIC.





Joint Institute for Nuclear Research, Dubna





Main targets of "NICA Complex":

- study of hot and dense baryonic matter
- investigation of nucleon spin structure,

polarization phenomena

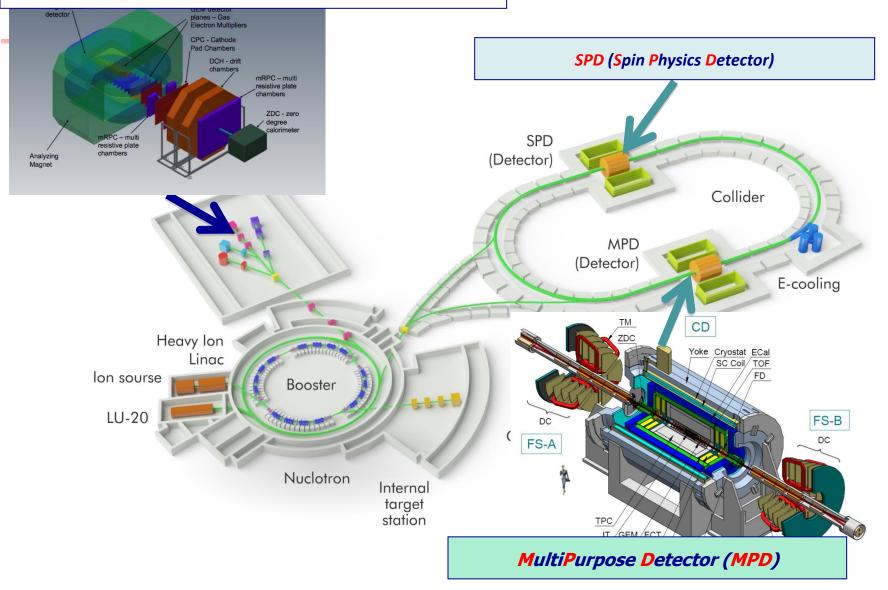
- development of accelerator facility for HEP @ JINR providing

intensive beams of relativistic ions from p to Au

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polarized protons and deuterons 79+ with energy up to 32 VSNN=11 GeV (Au , L ~ 10 cm c ) VS=27 GeV (p, L ~ 10 cm c )
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NICA Complex

Baryonic Matter at Nuclotron (BM@N)



Microworld: where is the fastest possible rotation?

- Non-central heavy ion collisions (Angular velocity ~ c/Compton wavelength)
- ~25 orders of magnitude faster than Earth's rotation
- Differential rotation vorticity
- P-odd :May lead to various P-odd effects
- Calculation in kinetic quark gluon string model (DCM/QGSM) - Boltzmann type eqns + phenomenological string amplitudes): Baznat,Gudima,Sorin,OT, PRC'13,16

Rotation in HIC and related quantities

- Non-central collisions orbital angular momentum
- L=Σrxp
- Differential pseudovector characteristics vorticity
- ໙ = curl v
- Pseudoscalar helicity
- H ~ <(v curl v)>
- Maximal helicity Beltrami chaotic flows
 v || curl v

Simulation in QGSM (Kinetics -> HD)

$$50 \times 50 \times 100 \text{ cells}$$
 $dx = dy = 0.6 \text{ fm}, dz = 0.6/\gamma \text{ fm}$

Velocity

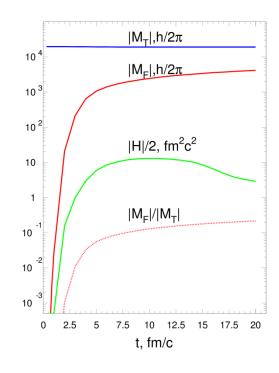
$$\vec{v}(x, y, z, t) = \frac{\sum_{i} \sum_{j} \vec{P}_{ij}}{\sum_{i} \sum_{j} E_{ij}}$$

 Vorticity – from discrete partial derivatives

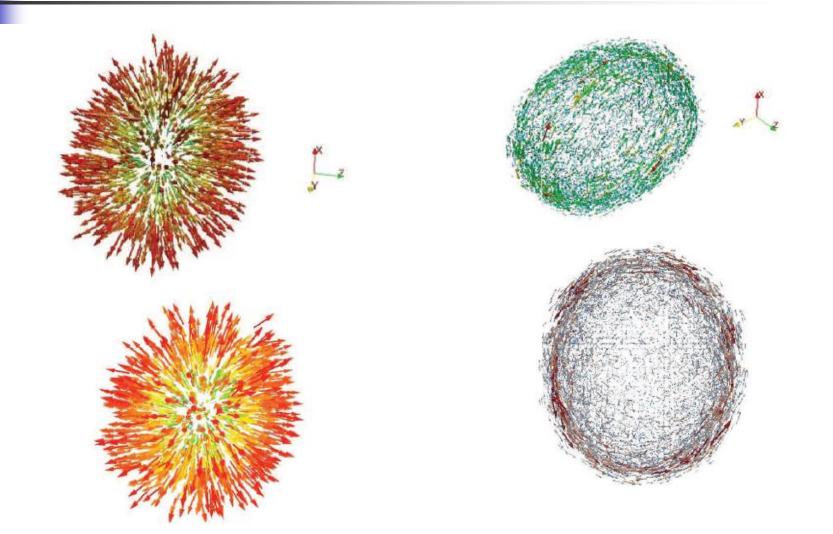


- Helicity vs orbital angular momentum (OAM) of fireball
- (~10% of total)

Conservation of OAM with a good accuracy!



Structure of velocity and vorticity fields (NICA@JINR-5 GeV/c)

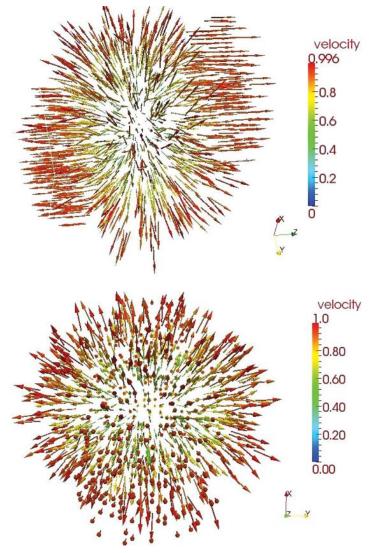


Distribution of velocity ("Small Bang")

3D/2D projection

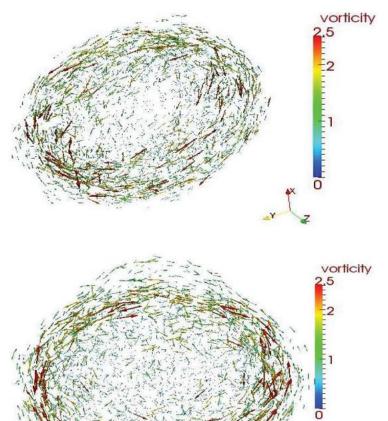
z-beams direction

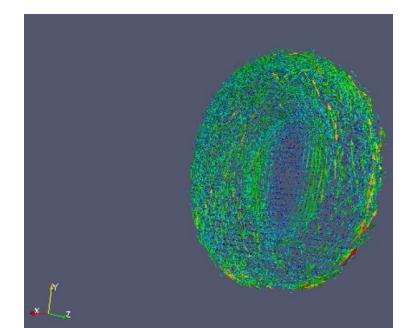
x-impact paramater



Distribution of vorticity ("small galaxies")

Layer (on core corona borderline) patterns

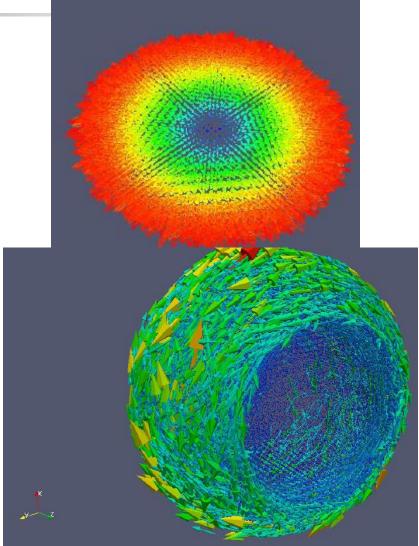




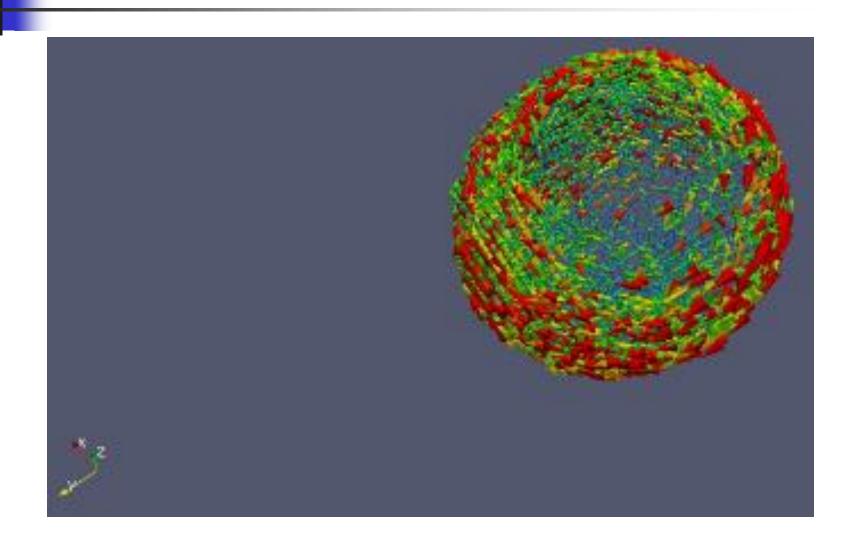
Velocity and vorticity patterns

Velocity

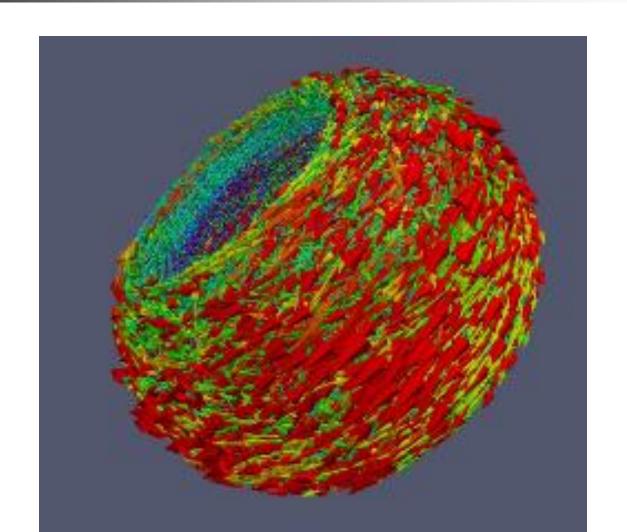
Vorticity pattern –
 vortex sheets due to L BUT
 cylinder symmetry!



Vortex sheet (fixed direction of L)

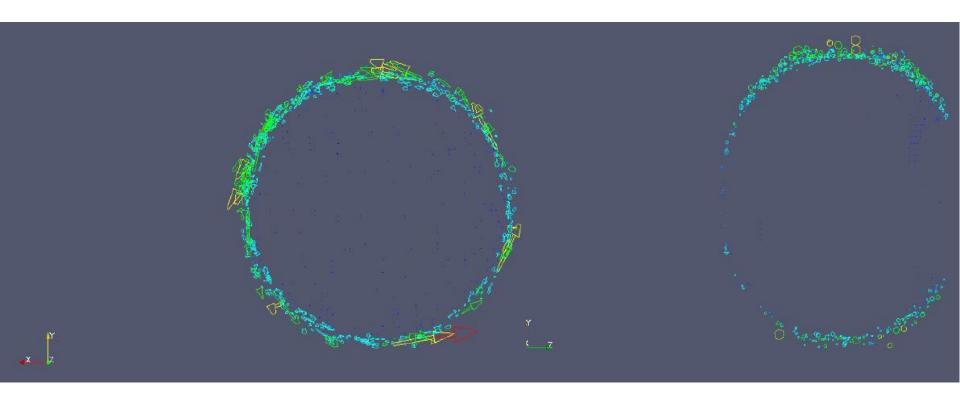


Vortex sheet (Average over L directions)



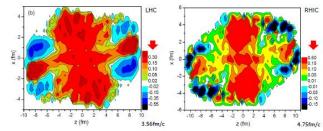
Sections of vorticity patterns

Front and side views

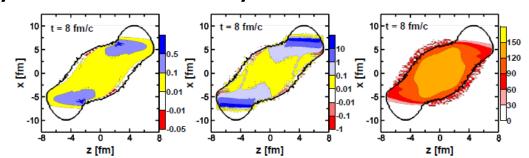


Vortex sheets

- Naturally appears in kinetic models
- Absent in viscous HD (L. Csernai et al)



Appears in 3 fluid dynamics model (Yu. Ivanov, A. Soldatov, <u>arXiv:1701.01319</u>)

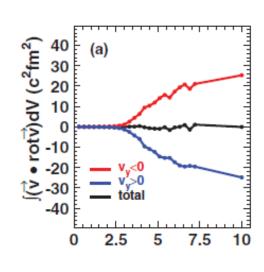


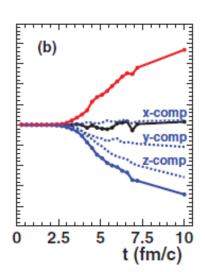


- Total helicity integrates to zero BUT
- Mirror helicities below and above the reaction plane

Confirmed in HSD (OT, Usubov, PRC92

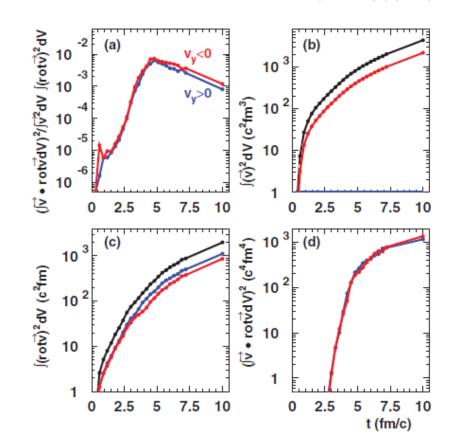
(2015) 014906





What is the relative orientation of velocity and vorticity?

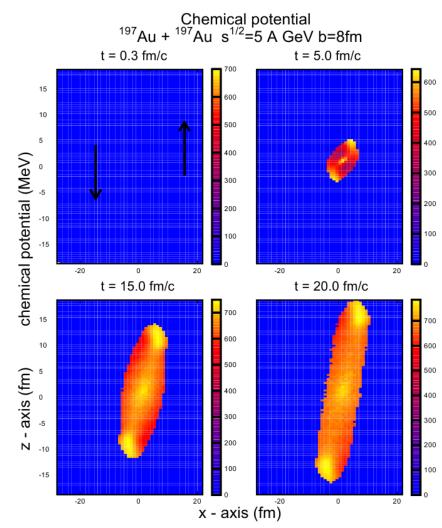
- Measure Cauchy-Schwarz inequality
- Small but non-negligible correlation
- Maximal correlation -Beltrami flows



Chemical potential: Kinetics

-> TD

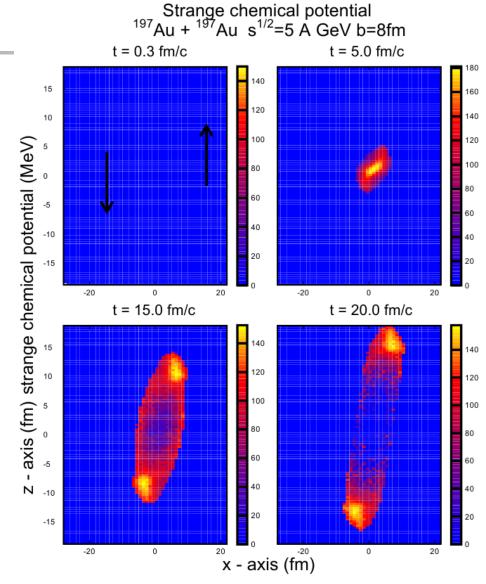
- TD and chemical equilibrium
- Conservation laws
- Chemical potential from equilibrium distribution functions
- 2d section: y=0



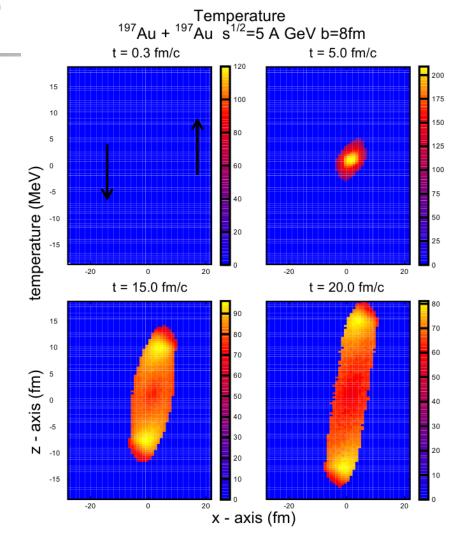
Strange chemical potential (polarization of Lambda is carried by strange quark!)

Strange chemical potential Strange chemical potential 197Au + 197Au

Non-uniform in space and time



Temperature



From axial charge to polarization (and from quarks to confined hadrons)

 Analogy of matrix elements and classical averages

$$< p_n | j^0(0) | p_n > = 2p_n^0 Q_n$$
 $< Q > \equiv \frac{\sum_{n=1}^N Q_n}{N} = \frac{\int d^3x \, j_{class}^0(x)}{N}$

Lorentz boost: compensate the sign of helicity $\Pi^{\Lambda,lab} = (\Pi_0^{\Lambda,lab}, \Pi_x^{\Lambda,lab}, \Pi_y^{\Lambda,lab}, \Pi_z^{\Lambda,lab}) = \frac{\Pi_0^{\Lambda}}{m} (p_y, 0, p_0, 0)$

$$<\Pi_{0}^{\Lambda}> \ = \ \frac{m_{\Lambda} \, \Pi_{0}^{\Lambda,lab}}{p_{y}} \ = \ < \frac{m_{\Lambda}}{N_{\Lambda} \, p_{y}} > Q_{5}^{s} \ \equiv \ < \frac{m_{\Lambda}}{N_{\Lambda} \, p_{y}} > \frac{N_{c}}{2\pi^{2}} \int d^{3}x \, \mu_{s}^{2}(x) \gamma^{2} \epsilon^{ijk} v_{i} \partial_{j} v_{k}$$

 Antihyperons (smaller N): same sign and larger value (confirmed by STAR)

Other approach to confinement: vortices in pionic superfluid (V.I. Zakharov, OT:1705.01650)

 Pions may carry the axial current due to quantized vortices in pionic superfluid (Kirilin, Sadofyev, Zakharov'12)

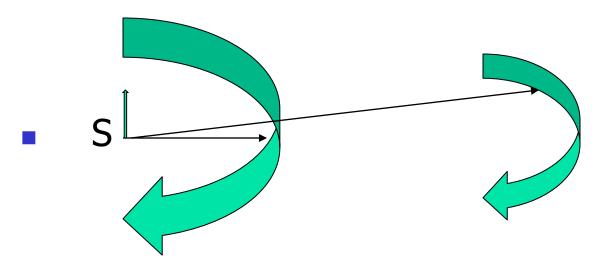
$$j_5^{\mu} = \frac{1}{4\pi^2 f_{\pi}^2} \epsilon^{\mu\nu\rho\sigma} (\partial_{\nu}\pi^0) (\partial_{\rho}\partial_{\sigma}\pi^0) \qquad \frac{\pi_0}{f_{\pi}} = \mu \cdot t + \varphi(x_i) \qquad \oint \partial_i \varphi dx_i = 2\pi n$$

$$\partial_i \varphi = \mu v_i$$

- Suggestion: core of the vortex- baryonic degrees of freedom- polarization
- (Quantum) Macro to micro at short distances

Core of quantized vortex

 Constant circulation – velocity increases when core is approached

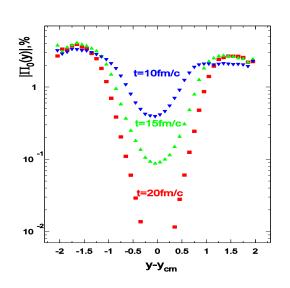


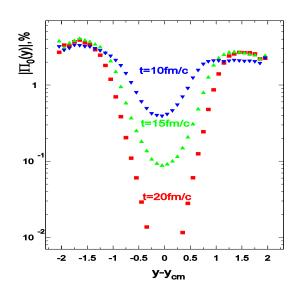
- Helium (v < v_{sound}) bounded by intermolecular distances
- Pions (v<c) -> (baryon) spin in the center

Helicity -> rest frame polarization

 Helicity ~ 0th component of polarization in lab. frame – effect of boost to Lambda rest frame – various options

 $\Pi_0(y) = 1/(4\pi^2) \int \gamma^2(x) \mu_s^2(x) | v \cdot rot(v) | n_{\Lambda}(y,x) w_1 d^3x / \int n_{\Lambda}(y,x) w_2 d^3x$ $w_1 = 1, \quad w_2 = p_{\nu}/m$



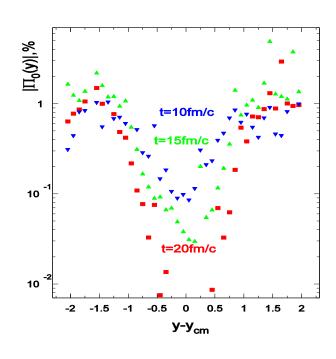


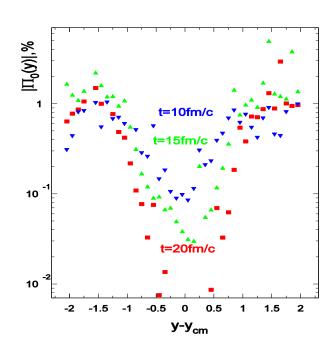
Various methods of boost implementation

 $w_1=m/p_y$

$$w_2 = 1$$

 $w_1=m/p_v$, $w_2=p_v/m$





Comparison of methods

• Wigner function – induced axial current (triangle diagram – V.I. Zakharov) – Prokhorov, OT $\alpha_{\mu} = \frac{1}{T} u^{\nu} \partial_{\nu} u_{\mu} = \frac{a_{\mu}}{T}, \quad w_{\mu} = \frac{1}{2T} \epsilon_{\mu\nu\alpha\beta} u^{\nu} \partial^{\alpha} u^{\beta} = \frac{\omega_{\mu}}{T}$

$$\langle : j_{\mu}^{5} : \rangle = \left(\frac{1}{6} \left[T^{2} + \frac{a^{2} - \omega^{2}}{4\pi^{2}} \right] + \frac{\mu^{2}}{2\pi^{2}} \right) \omega_{\mu} + \frac{1}{12\pi^{2}} (\omega \cdot a) a_{\mu}$$

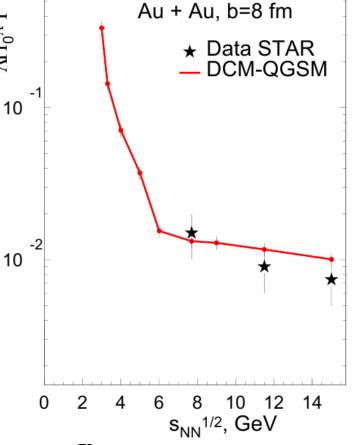
$$\langle : j_{\mu}^5 : \rangle = 2\pi \operatorname{Im} \left[\left(\frac{1}{6} (T^2 + \varphi^2) + \frac{\mu^2}{2\pi^2} \right) \varphi_{\mu} \right] \qquad \varphi_{\mu} = \frac{a_{\mu}}{2\pi} + \frac{i\omega_{\mu}}{2\pi}$$

- New terms of higher order in vorticity
- T-independent: Hawking/Unruh?

Energy dependence (preliminary)

Growth at low energy

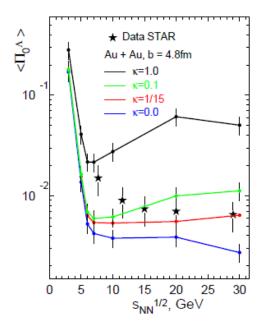
Surprisingly close to STAR data!



 Structure – may be due to fluctuation for low particles number

The role of (gravitational anomaly related) T² term

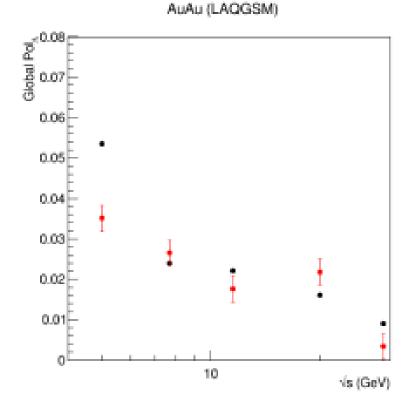
Different values of coefficient probed



 LQCD suppression by collective effects supported

Polarization at NICA/MPD (A. Kechechyan)

 QGSM Simulations and recovery accounting for MPD acceptance effects

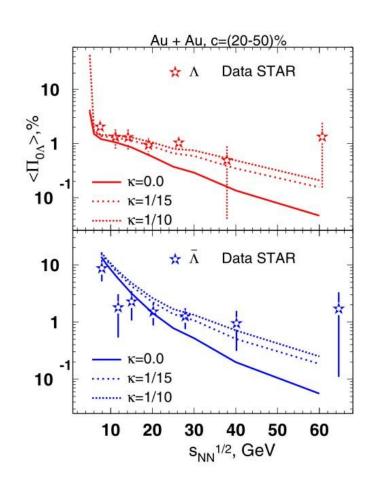


Role of vector mesons

- Strange axial charge may be also carried by K* mesons
- Λ accompanied by (+,anti 0) K* mesons
 with two sea quarks small corrections
- Anti Λ more numerous (-,0) K* mesons with single (sea) strange antiquark

 Vector polarization implies also tensor polarization – anisotropy measurable in dilepton angular distributions

Λ vs Anti Λ (Baznat, Gudima, Sorin, OT, 1701.00923)

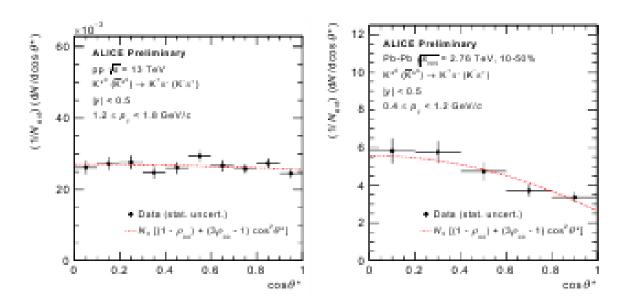


Tensor polarization

- P-even: quadratic effect of vorticity and/or magnetic field (tensor polarizability)
- Lattice: low invariant mass- longitudinal polarization (Buividovich, Polikarpov, OT'12)
- Lattice for vector mesons non-trivial dependence on magnetic field (Lushevskaya, Slovjeva, OT'16)

Tensor polarization@ALICE

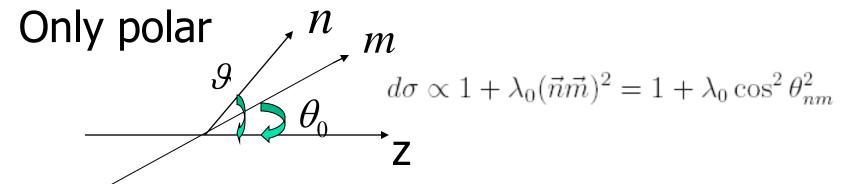
Protons vs heavy ions



Large energy - magnetic field effect?



Polar and azimuthal asymmetries: kinematically related



asymmetry with respect to m!

 $\cos \theta_{nm} = \cos \theta \cos \theta_0 + \sin \theta \sin \theta_0 \cos \phi$

angle dependence appears with new

- azimuthal

$$\lambda = \lambda_0 \frac{2 - 3\sin^2 \theta_0}{2 + \lambda_0 \sin^2 \theta_0}$$
$$\nu = \lambda_0 \frac{2\sin^2 \theta_0}{2 + \lambda_0 \sin^2 \theta_0}$$

Generalized Lam-Tung relation (OT'05)

Relation between coefficients (high school math sufficient!)

$$\lambda_0 = \frac{\lambda + \frac{3}{2}\nu}{1 - \frac{1}{2}\nu}$$

- Reduced to standard LT relation for transverse polarization ($\lambda_0 = 1$)
- LT contains two very different inputs: kinematical asymmetry+transverse polarization

Properties of GLT

- Provides rotation-invariant observable (Faccioli,Lourenco,Seixas'10)
- Unknown collision axis non-coplanarity (Peng, Chang, McClellan, OT'15, talk of W.-C. Chang) violation of LT even for λ_0 =1
- Quarkonia production, HIC... different λ_0
- HIC two natural axes: momentum direction in medium rest frame and normal to reaction plane – extra non-coplanarity appears if reaction plane is known only approximately

Conclusions/Outlook

- Polarization new probe of anomaly (analogous to gluon polarization in nucleon) in quark-gluon matter: to be studied at NICA
- Generated by femto-vortex sheets
- Energy dependence predicted and confirmed
- Same sign and larger magnitude of antihyperon polarization
- Polarization from core of vortices in pionic superfluid
- Dileptons first results to be compared with hadronic collisions



 Decrease of polarization with energy – natural in Regge theory

Vorticity in p(π p)A collisions? Angular momentum is smaller, but vorticity is local?

Gauge links with velocity fields?!

•?!

BACKUP

Properties of SSA

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The same for the case of initial or final state polarization. Various possibilities to measure the effects: change sign of \vec{n} or \vec{P}: left-right or up-down asymmetry. Qualitative features of the asymmetry
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Transverse momentum required (to have \vec{n})

Transverse polarization (to maximize $(\vec{P}\vec{n})$)

Interference of amplitudes

IMAGINARY phase between amplitudes - absent in Born approximation

Phases and T-oddness

Clearly seen in relativistic approach:

$$\rho = \frac{1}{2}(\hat{p} + m)(1 + \hat{s}\gamma_5)$$

Than: $d\sigma \sim Tr[\gamma_5....] \sim im\varepsilon_{sp_1p_2p_3}...$

Imaginary parts (loop amplitudes) are required to produce real observable.

 $\varepsilon_{abcd} \equiv \varepsilon^{\alpha\beta\gamma\delta} a_{\alpha} b_{\beta} c_{\gamma} d_{\delta}$ each index appears once: P- (compensate S) and T- odd.

However: no real T-violation: interchange $|i> \leftrightarrow |f>$ is the nontrivial operation in the case of nonzero phases of $< f|S|i>^*=< i|S|f>$.

SSA - either T-violation or the phases.

DIS - no phases ($Q^2 < 0$)- real T-violation.

Correlations of jets handedness

- LEP quarks are polarized due to weak interaction
- BUT how to ditinguish quark/antiquark jets?
- 2 jets correlation of helicities correlation of handedness
- Hadronic collisions for jets from the same quark-antiquark pair



Spin-gravity/rotation (~ 25 orders of magnitude slower!) interactions

- How to describe hadron spin/gravity(inertia) couplings?
- Matrix elements of Energy-Momentum Tensor
- May be studied in non-gravitational experiments/theory
- Simple interpretation in comparison to EM field case

Gravitational Formfactors

$$\langle p'|T_{q,g}^{\mu\nu}|p\rangle = \bar{u}(p')\Big[A_{q,g}(\Delta^2)\gamma^{(\mu}p^{\nu)} + B_{q,g}(\Delta^2)P^{(\mu}i\sigma^{\nu)\alpha}\Delta_{\alpha}/2M]u(p)$$

• Conservation laws - zero Anomalous Gravitomagnetic Moment : $\mu_G = J$ (g=2)

$$\begin{split} P_{q,g} &= A_{q,g}(0) & A_{q}(0) + A_{g}(0) = 1 \\ J_{q,g} &= \frac{1}{2} \left[A_{q,g}(0) + B_{q,g}(0) \right] & A_{q}(0) + B_{q}(0) + A_{g}(0) + B_{g}(0) = 1 \end{split}$$

- May be extracted from high-energy experiments/NPQCD calculations
- Describe the partition of angular momentum between quarks and gluons
- Describe interaction with both classical and TeV gravity

Generalized Parton Diistributions (related to matrix elements of non local operators) — models for both EM and Gravitational Formfactors (Selyugin,OT '09)

Smaller mass square radius (attraction vs repulsion!?)

$$\begin{split} \rho(b) &= \sum_{q} e_{q} \int dx q(x,b) &= \int d^{2}q F_{1}(Q^{2} = q^{2}) e^{i\vec{q}\,\vec{b}} \\ &= \int_{0}^{\infty} \frac{q \, dq}{2\pi} J_{0}(qb) \frac{G_{E}(q^{2}) + \tau G_{M}(q^{2})}{1 + \tau} \end{split}$$

$$\rho_0^{\text{Gr}}(b) = \frac{1}{2\pi} \int_{-\infty}^{0} dq \, q J_0(qb) A(q^2)$$

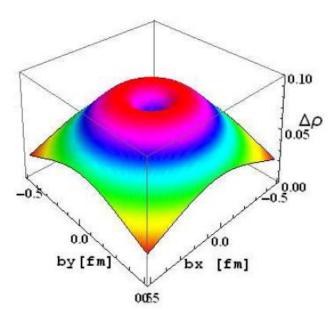


FIG. 17: Difference in the forms of charge density F_1^P and "matter" density (A)

Electromagnetism vs Gravity

Interaction – field vs metric deviation

$$M = \langle P' | J_q^{\mu} | P \rangle A_{\mu}(q) \qquad M = \frac{1}{2} \sum_{r,G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$$

Static limit

$$\langle P|J_q^{\mu}|P\rangle = 2e_q P^{\mu}$$

$$M_0 = \langle P|J_q^{\mu}|P\rangle A_{\mu} = 2e_q M \phi(q)$$

$$\sum_{q,G} \langle P|T_i^{\mu\nu}|P\rangle = 2P^{\mu}P^{\nu}$$

$$h_{00} = 2\phi(x)$$

$$M_0 = \frac{1}{2} \sum_{q,G} \langle P | T_i^{\mu\nu} | P \rangle h_{\mu\nu} = 2M \cdot M\phi(q)$$

 Mass as charge – equivalence principle (Einstein '10-11, Praha)

Equivalence principle

- Newtonian "Falling elevator" well known and checked with high accuracy (also for elementary particles)
- Post-Newtonian gravity action on SPIN known since 1962 (Kobzarev and Okun' ZhETF paper contains acknowledgment to Landau: probably his last contribution to theoretical physics before car accident); rederived from conservation laws -Kobzarev and Zakharov
- Anomalous gravitomagnetic (and electric-CP-odd) moment iz ZERO or
- Classical and QUANTUM rotators behave in the SAME way
- For GEDM —checked with sometimes controversial results
- For AGM not checked on purpose but in fact checked in the same atomic spins experiments at % level (Silenko,OT'07)

Gravitomagnetism

• Gravitomagnetic field (weak, except in gravity waves) – action on spin from $M = \frac{1}{2} \sum_{G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$

$$ec{H}_J = rac{1}{2} rot ec{g}; \; ec{g}_i \equiv g_{0i}$$
 spin dragging twice smaller than EM

• Lorentz force — similar to EM case: factor $\frac{1}{2}$ cancelled with 2 from $h_{00} = 2\phi(x)$ Larmor frequency same as EM $\mu_{G,H}$ H_L

$$\omega_J = \frac{\mu_G}{J} H_J = \frac{H_L}{2} = \omega_L \ \vec{H}_L = rot \vec{g}$$

 Orbital and Spin momenta dragging – the same -Equivalence principle

Experimental test of PNEP

Reinterpretation of the data on G(EDM) search
PHYSICAL REVIEW LETTERS

VOLUME 68	13 JANUARY 1992	Number 2

Search for a Coupling of the Earth's Gravitational Field to Nuclear Spins in Atomic Mercury

B. J. Venema, P. K. Majumder, S. K. Lamoreaux, B. R. Heckel, and E. N. Fortson Physics Department, FM-15, University of Washington, Seattle, Washington 98195 (Received 25 September 1991)

 If (CP-odd!) GEDM=0 -> constraint for AGM (Silenko, OT'07) from Earth rotation – was considered as obvious (but it is just EP!) background

$$\mathcal{H} = -g\mu_N \mathbf{B} \cdot \mathbf{S} - \zeta \hbar \boldsymbol{\omega} \cdot \mathbf{S}, \quad \zeta = 1 + \chi$$

 $|\chi(^{201}\text{Hg}) + 0.369\chi(^{199}\text{Hg})| < 0.042 \quad (95\%\text{C.L.})$

Equivalence principle for moving particles

- Compare gravity and acceleration: gravity provides EXTRA space components of metrics $h_{zz} = h_{xx} = h_{yy} = h_{00}$
- Matrix elements DIFFER

$$\mathcal{M}_{g}=(\pmb{\epsilon}^{2}+\pmb{p}^{2})h_{00}(q), \qquad \mathcal{M}_{a}=\pmb{\epsilon}^{2}h_{00}(q)$$

- Ratio of accelerations: $R = \frac{\epsilon^2 + p^2}{\epsilon^2}$ confirmed by explicit solution of Dirac equation (Silenko, OT, '05)
- Arbitrary fields Obukhov, Silenko, OT '09,'11,'13

Gravity vs accelerated frame for spin and helicity

- Spin precession well known factor 3 (Probe B; spin at satellite probe of PNEP!) smallness of relativistic correction (~P²) is compensated by 1/ P² in the momentum direction precession frequency
- Helicity flip the same!
- No helicity flip in gravitomagnetic field another formulation of PNEP (OT'99)

Gyromagnetic and Gravigyromagnetic ratios

- Free particles coincide
- $<P+q|T^{mn}|P-q> = P^{m}<P+q|J^{n}|P-q>/e$ up to the terms linear in q
- Special role of g=2 for any spin (asymptotic freedom for vector bosons)
- Should Einstein know about PNEP, the outcome of his and de Haas experiment would not be so surprising
- Recall also g=2 for Black Holes. Indication of "quantum" nature?!

Cosmological implications of PNEP

- Necessary condition for Mach's Principle (in the spirit of Weinberg's textbook) -
- Lense-Thirring inside massive rotating empty shell (=model of Universe)
- For flat "Universe" precession frequency equal to that of shell rotation
- Simple observation-Must be the same for classical and quantum rotators – PNEP!
- More elaborate models Tests for cosmology ?!

Torsion – acts only on spin (violates EP)

Dirac eq+FW transformation-Obukhov, Silenko, OT, arXiv:1410.6197

Hermitian Dirac Hamiltonian

$$\begin{split} e_i^{\widehat{0}} &= V \, \delta_i^0, \qquad e_i^{\widehat{a}} = W^{\widehat{a}}{}_b \left(\delta_i^b - c K^b \, \delta_i^0 \right) \\ &ds^2 = V^2 c^2 dt^2 - \delta_{\widehat{a}\widehat{b}} W^{\widehat{a}}{}_c W^{\widehat{b}}{}_d (dx^c - K^c c dt) (dx^d - K^d c dt) \\ &\qquad \qquad + \frac{c}{2} \left(K \cdot \pi + \pi \cdot K \right) + \frac{\hbar c}{4} \left(\Xi \cdot \Sigma - \Upsilon \gamma_5 \right), \\ &\mathcal{F}^b{}_a = V W^b{}_{\widehat{a}}, \qquad \Upsilon = V \epsilon^{\widehat{a}\widehat{b}\widehat{c}} \Gamma_{\widehat{a}\widehat{b}\widehat{c}}, \qquad \Xi^a = \frac{V}{c} \, \epsilon^{\widehat{a}\widehat{b}\widehat{c}} \left(\Gamma_{\widehat{0}\widehat{b}\widehat{c}} + \Gamma_{\widehat{b}\widehat{c}\widehat{0}} + \Gamma_{\widehat{b}\widehat{c}\widehat{0}} \right) \end{split}$$

Spin-torsion coupling

$$-\frac{\hbar cV}{4} \left(\boldsymbol{\Sigma} \cdot \boldsymbol{\check{T}} + c \gamma_5 \boldsymbol{\check{T}}^{\hat{0}} \right)$$

$$\check{T}^{\alpha} = -\frac{1}{2} \eta^{\alpha\mu\nu\lambda} T_{\mu\nu\lambda}$$

FW – semiclassical limit - precession

$$\Omega^{(T)} = -\frac{c}{2}\check{\boldsymbol{T}} + \beta \frac{c^3}{8} \left\{ \frac{1}{\epsilon'}, \left\{ \boldsymbol{p}, \check{\boldsymbol{T}}^{\hat{0}} \right\} \right\} + \frac{c}{8} \left\{ \frac{c^2}{\epsilon'(\epsilon' + mc^2)}, \left(\left\{ \boldsymbol{p}^2, \check{\boldsymbol{T}} \right\} - \left\{ \boldsymbol{p}, (\boldsymbol{p} \cdot \check{\boldsymbol{T}}) \right\} \right) \right\}$$

Experimental bounds for torsion

Magnetic field+rotation+torsion

$$H = -g_N \frac{\mu_N}{\hbar} \mathbf{B} \cdot \mathbf{s} - \boldsymbol{\omega} \cdot \mathbf{s} - \frac{c}{2} \check{\mathbf{T}} \cdot \mathbf{s}$$

Same '92 EDM experiment

$$\frac{\hbar c}{4} |\check{T}| \cdot |\cos\Theta| < 2.2 \times 10^{-21} \,\text{eV}, \qquad |\check{T}| \cdot |\cos\Theta| < 4.3 \times 10^{-14} \,\text{m}^{-1}$$

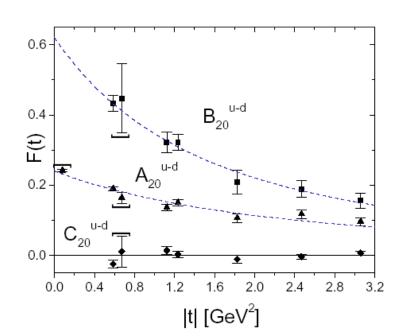
New(based on Gemmel et al '10)

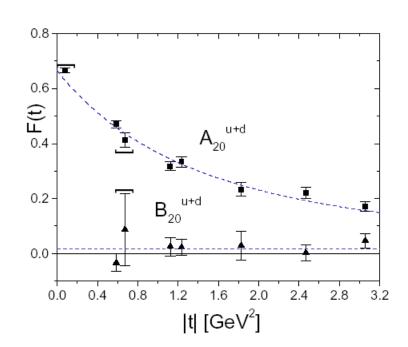
$$\frac{\hbar c}{2} |\check{T}| \cdot |(1 - \mathcal{G}) \cos \Theta| < 4.1 \times 10^{-22} \,\text{eV}, \qquad |\check{T}| \cdot |\cos \Theta| < 2.4 \times 10^{-15} \,\text{m}^{-1}.$$

$$\mathcal{G} = g_{He}/g_{Xe}$$

Generalization of Equivalence principle

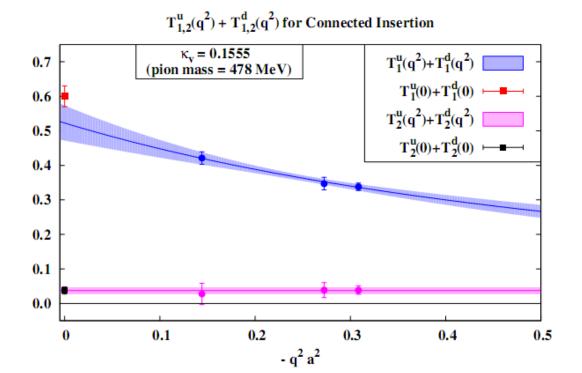
 Various arguments: AGM ≈ 0 separately for quarks and gluons – most clear from the lattice (LHPC/SESAM)





Recent lattice study (M. Deka et al. <u>arXiv:1312.4816</u>)

 Sum of u and d for Dirac (T1) and Pauli (T2) FFs



Extended Equivalence Principle=Exact EquiPartition

- In pQCD violated
- Reason in the case of ExEP- no smooth transition for zero fermion mass limit (Milton, 73)
- Conjecture (O.T., 2001 prior to lattice data)
 valid in NP QCD zero quark mass limit is safe due to chiral symmetry breaking
- Gravity-proof confinement (should the hadrons survive enetering Black Hole?)?!



Another manifestation of post-Newtonian (E)EP for spin 1 hadrons

- Tensor polarization coupling of gravity to spin in forward matrix elements inclusive processes
- Second moments of tensor distributions should sum to zero

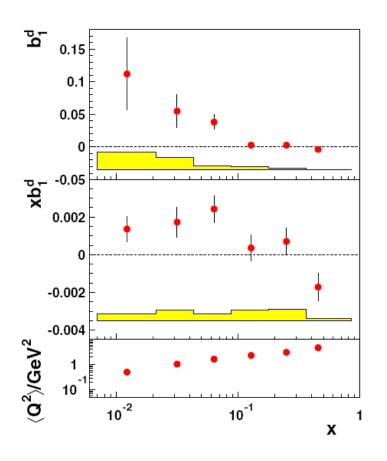
$$\begin{split} \langle P, S | \bar{\psi}(0) \gamma^{\nu} D^{\nu_{1}} ... D^{\nu_{n}} \psi(0) | P, S \rangle_{\mu^{2}} &= i^{-n} M^{2} S^{\nu\nu_{1}} P^{\nu_{2}} ... P \nu_{n} \int_{0}^{1} C_{q}^{T}(x) x^{n} dx \\ \sum_{q} \langle P, S | T_{i}^{\mu\nu} | P, S \rangle_{\mu^{2}} &= 2 P^{\mu} P^{\nu} (1 - \delta(\mu^{2})) + 2 M^{2} S^{\mu\nu} \delta_{1}(\mu^{2}) \\ \langle P, S | T_{g}^{\mu\nu} | P, S \rangle_{\mu^{2}} &= 2 P^{\mu} P^{\nu} \delta(\mu^{2}) - 2 M^{2} S^{\mu\nu} \delta_{1}(\mu^{2}) \end{split}$$

$$\sum_{q} \int_{0}^{1} C_{i}^{T}(x)xdx = \delta_{1}(\mu^{2}) = 0 \text{ for ExEP}$$

HERMES – data on tensor spin structure function PRL 95, 242001 (2005)

- Isoscalar target –
 proportional to the
 sum of u and d
 quarks –
 combination
 required by EEP
- Second moments –
 compatible to zero
 better than the first one
 (collective glue << sea)
 - for valence:

$$\int_0^1 C_i^T(x) dx = 0.$$





- Probe of equivalence principle for spin
- May be tested in EDM search experiments
- Extension of EP –validity separately for quarks and gluons

Sum rules for EMT (and OAM)

 First (seminal) example: X. Ji's sum rule ('96). Gravity counterpart – OT'99

Burkardt sum rule – looks similar: can it be derived from EMT?

 Yes, if provide correct prescription to gluonic pole (OT'14)

Pole prescription and Burkardt SR

- Pole prescription (dynamics!) provides ("T-odd") symmetric part!
- SR: $\sum \int dx T(x,x) = 0$ SR: $\sum \int dx T(x,x) = 0$ (but relation of gluon Sivers to twist 3 still not founs prediction!)
- Can it be valid separately for each quark flavour: nodes (related to "sign problem")?
- Valid if structures forbidden for TOTAL EMT do not appear for each flavour
- Structure contains besides S gauge vector n: If GI separation of EMT – forbidden: SR valid separately!

Are more accurate data possible?

HERMES – unlikely

 JLab may provide information about collective sea and glue in deuteron and indirect new test of Equivalence Principle



CONCLUSIONS

- Spin-gravity interactions may be probed directly in gravitational (inertial) experiments and indirectly – studing EMT matrix element
- Torsion and EP are tested in EDM experiments
- SR's for deuteron tensor polarizationindirectly probe EP and its extension separately for quarks and gluons

EEP and AdS/QCD

- Recent development calculation of Rho formfactors in Holographic QCD (Grigoryan, Radyushkin)
- Provides g=2 identically!
- Experimental test at time –like region possible